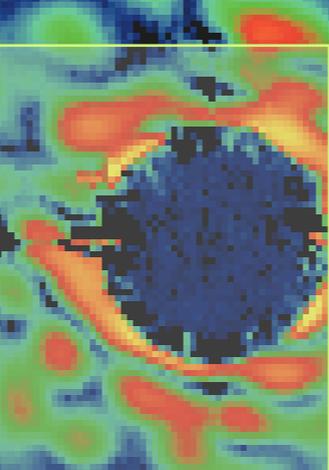


# Imaging Molecular Structures using Short Intense X-ray Pulses

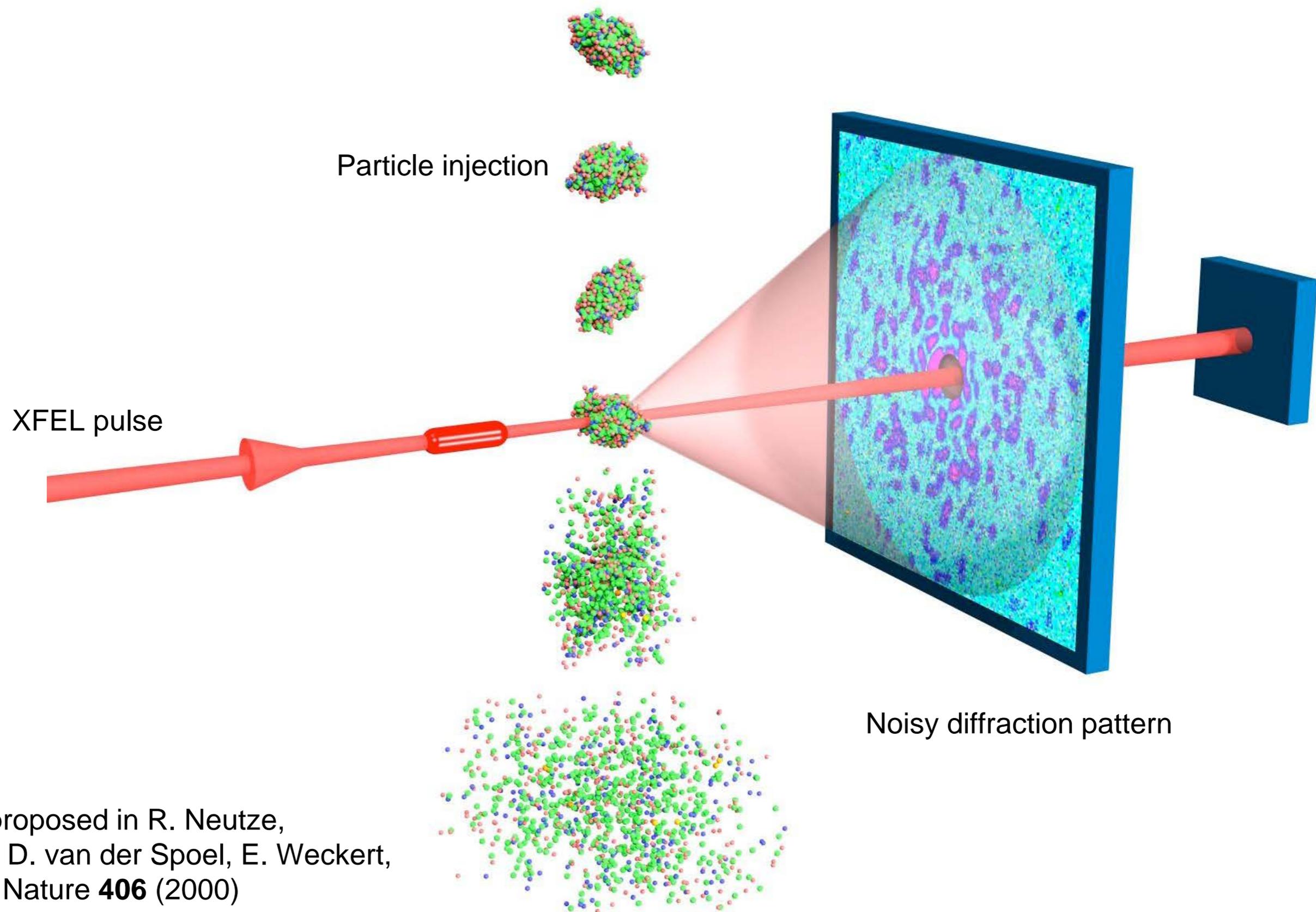
**Henry Chapman**

*Center for Free-Electron Laser Science  
DESY and University of Hamburg*

*Nobel Symposium, June 2015*

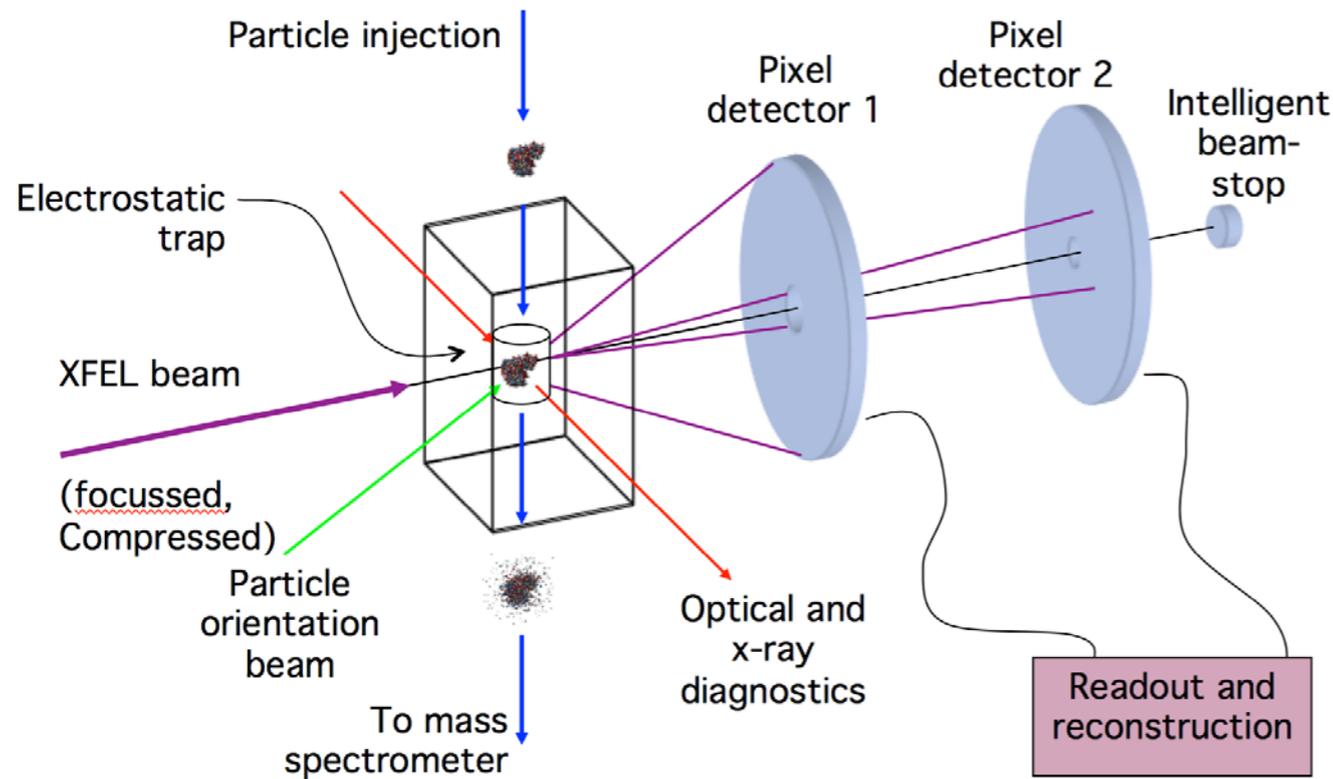


# X-ray free-electron lasers may enable atomic-resolution imaging of biological macromolecules



Scheme proposed in R. Neutze,  
R. Wouts, D. van der Spoel, E. Weckert,  
J. Hajdu, *Nature* **406** (2000)

# Our first experiments set out to answer a number of open questions

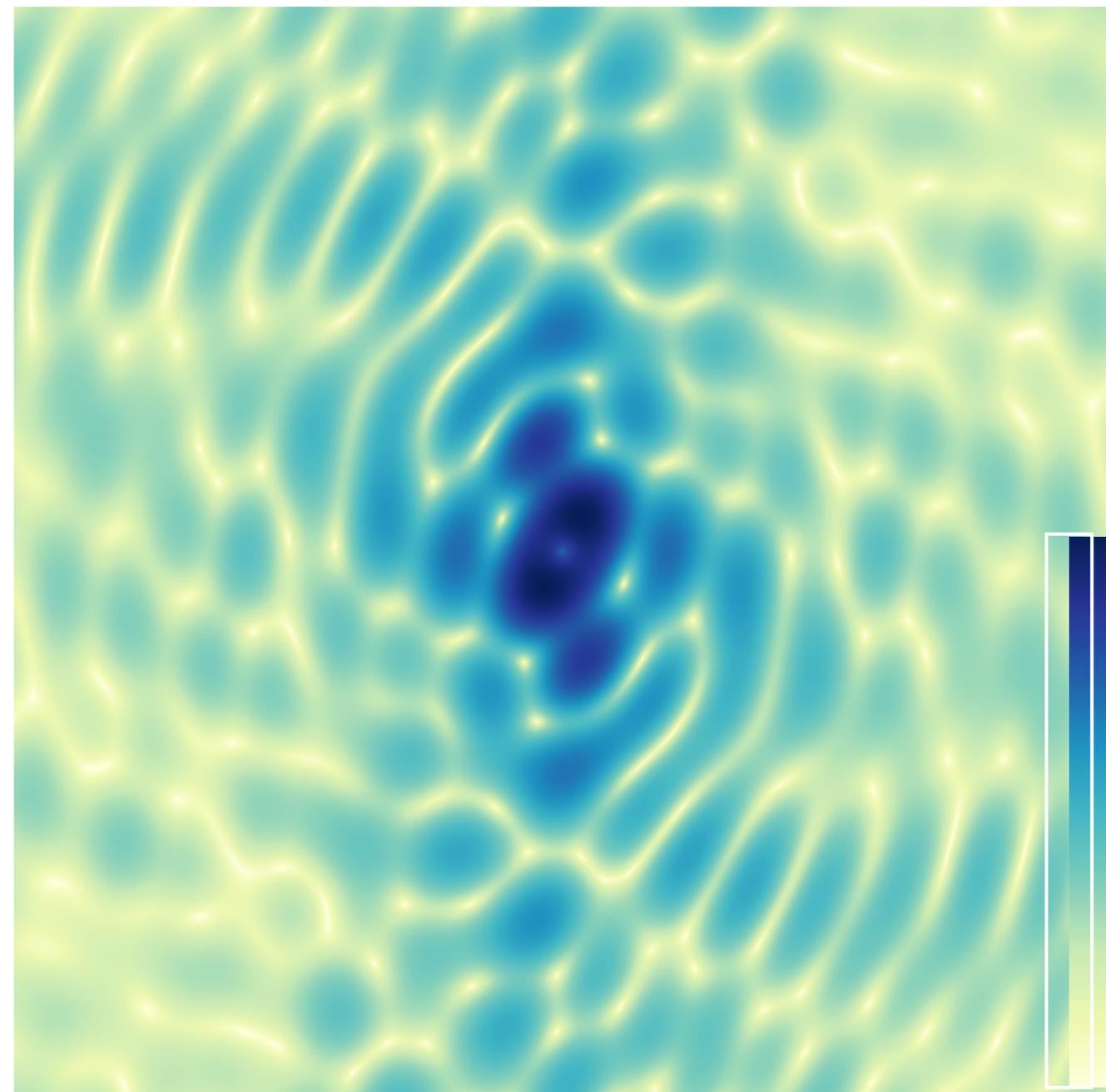


CBST - DOE Workshop  
March 2004 at SLAC

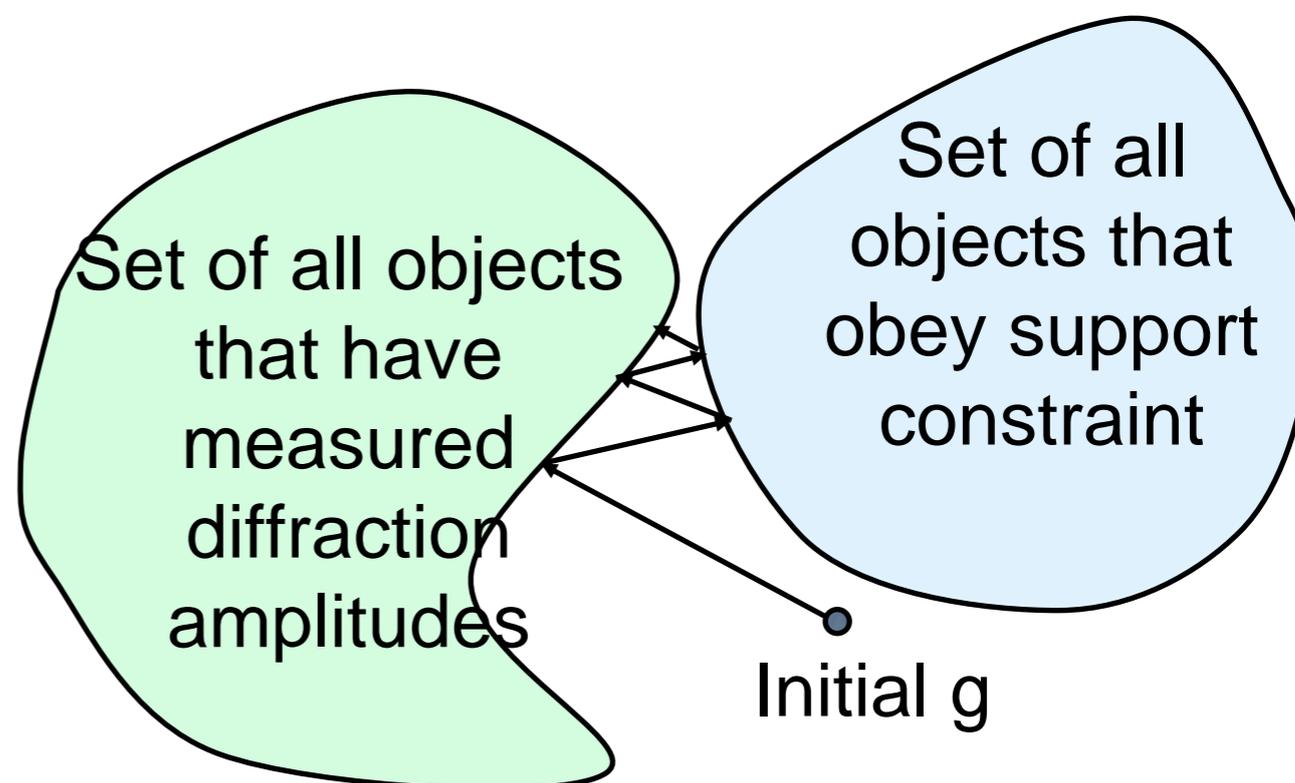
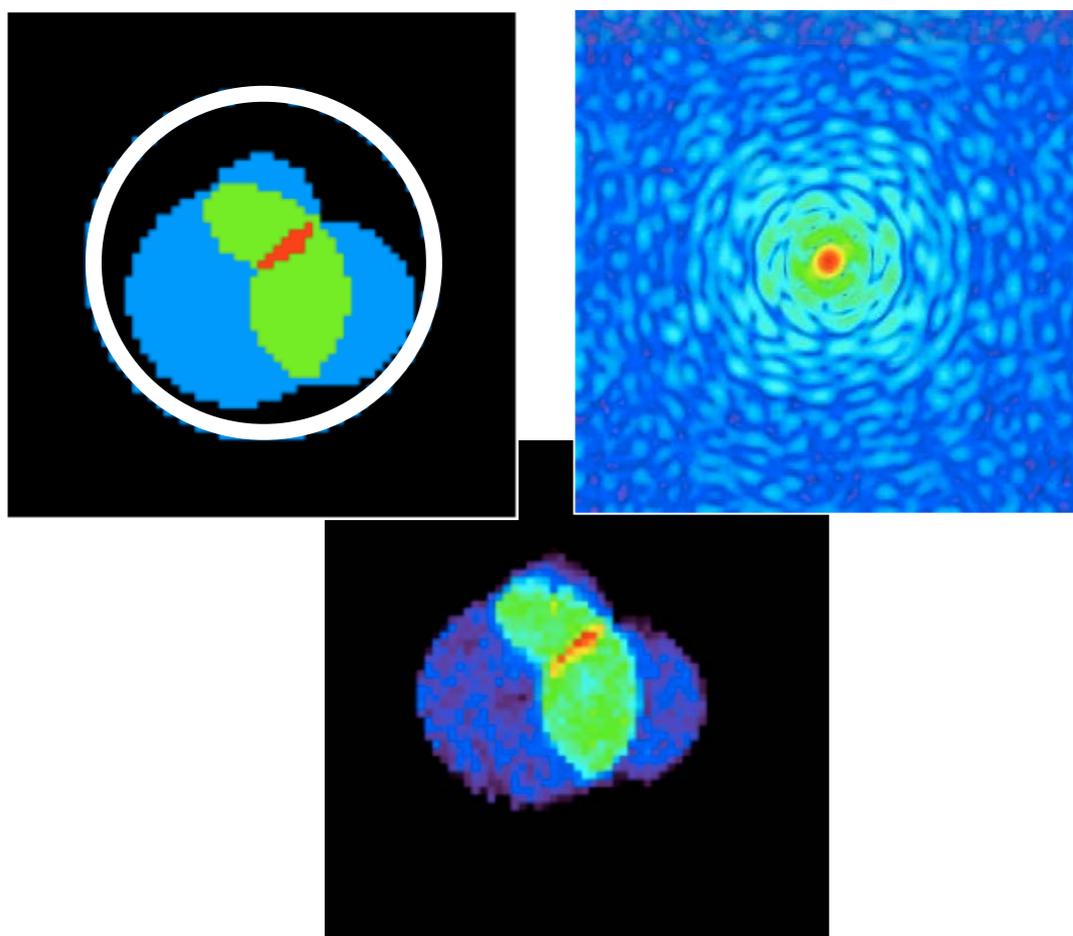
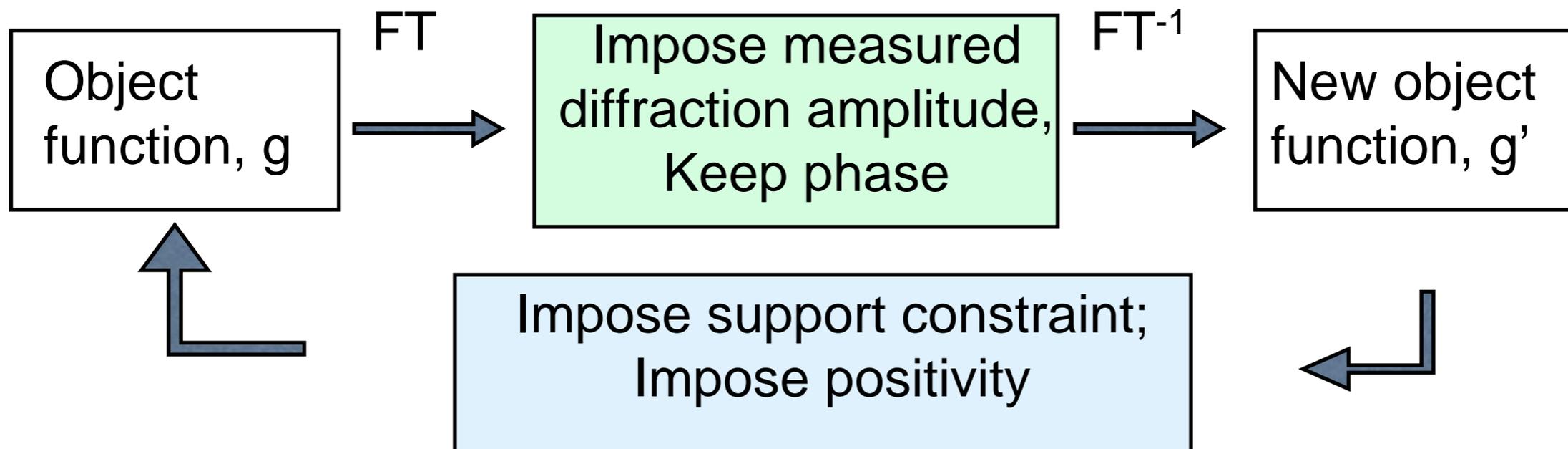
Janos Hajdu  
Keith Hodgson  
Henry Chapman

1. How short is short enough to outrun radiation damage?
2. How can you get single molecules into the X-ray beam?
3. How can you determine orientation from noisy diffraction?

# Single particles give rise to continuous diffraction patterns



# Phase retrieval can be accomplished with iterative transform algorithms



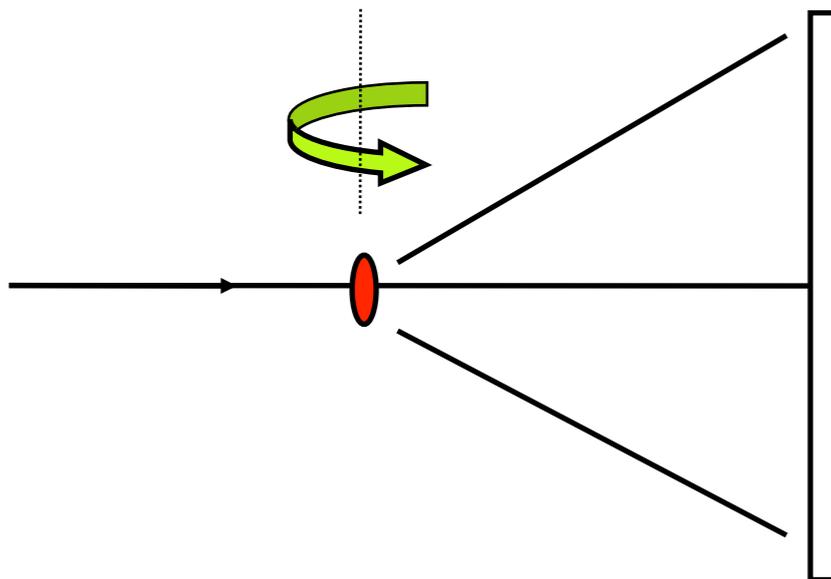
# We reconstructed a 3D X-ray image of a non-crystalline object at 10 nm resolution

Coherent X-ray diffraction data  $\lambda = 1.6$  nm, from a sample of 50-nm gold spheres arranged on a pyramid on a *synchrotron*

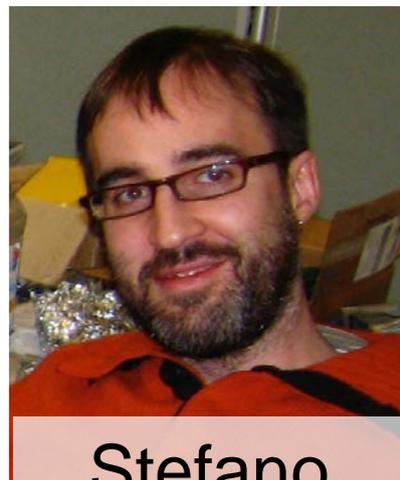
Complete image reconstruction achieved, without any prior knowledge, using our “**shrinkwrap**” algorithm, **parallelized** for 3D on 32-CPU cluster. Resolution = 10 nm



Coherent X-ray diffraction data, rotating the sample -70 to +70 degrees ( $5 \cdot 10^8$  data points)

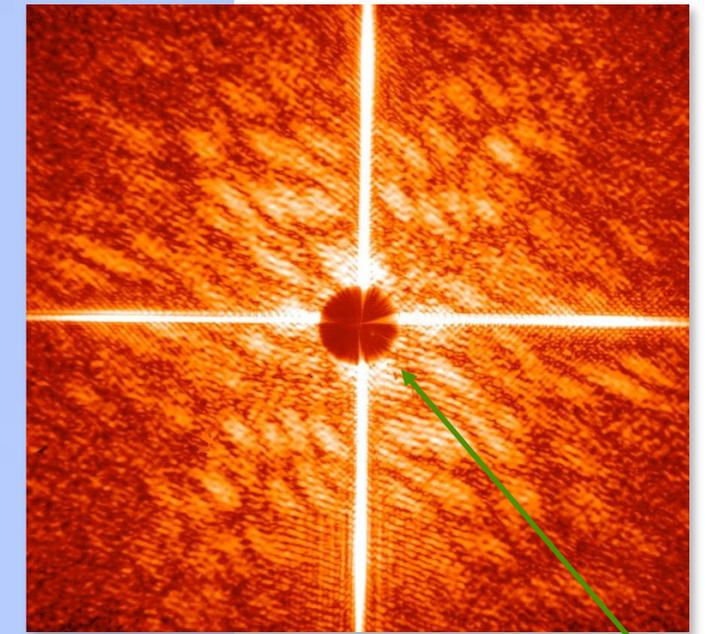
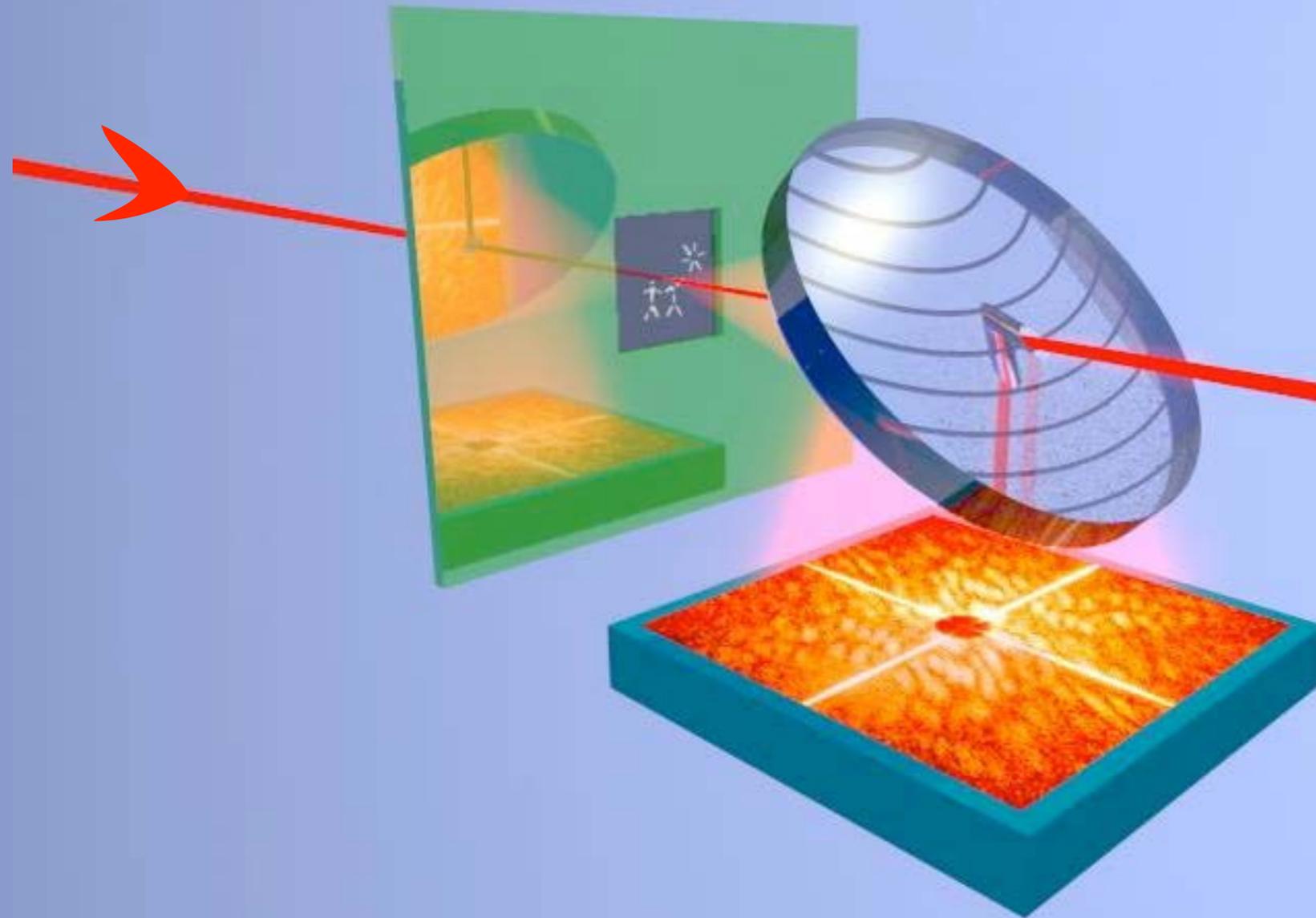


Anton Barty

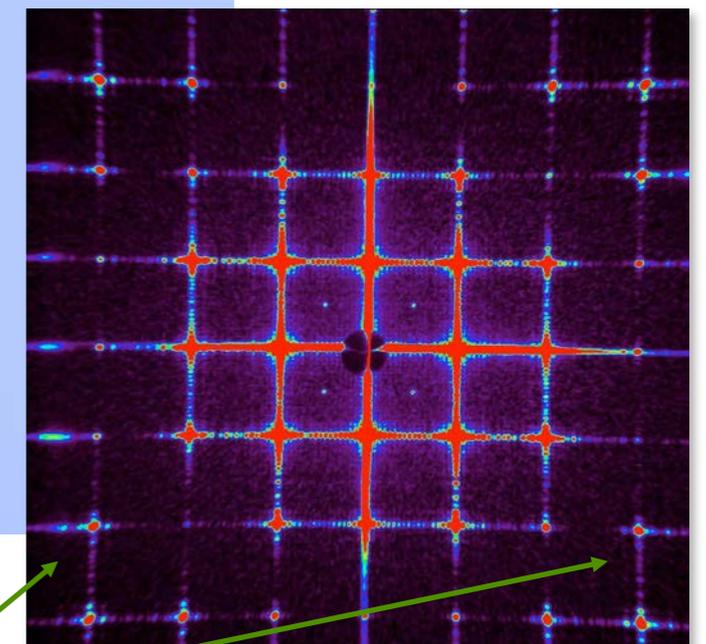


Stefano Marchesini

# Our diffraction camera can measure forward scattering close to the direct soft-X-ray FEL beam

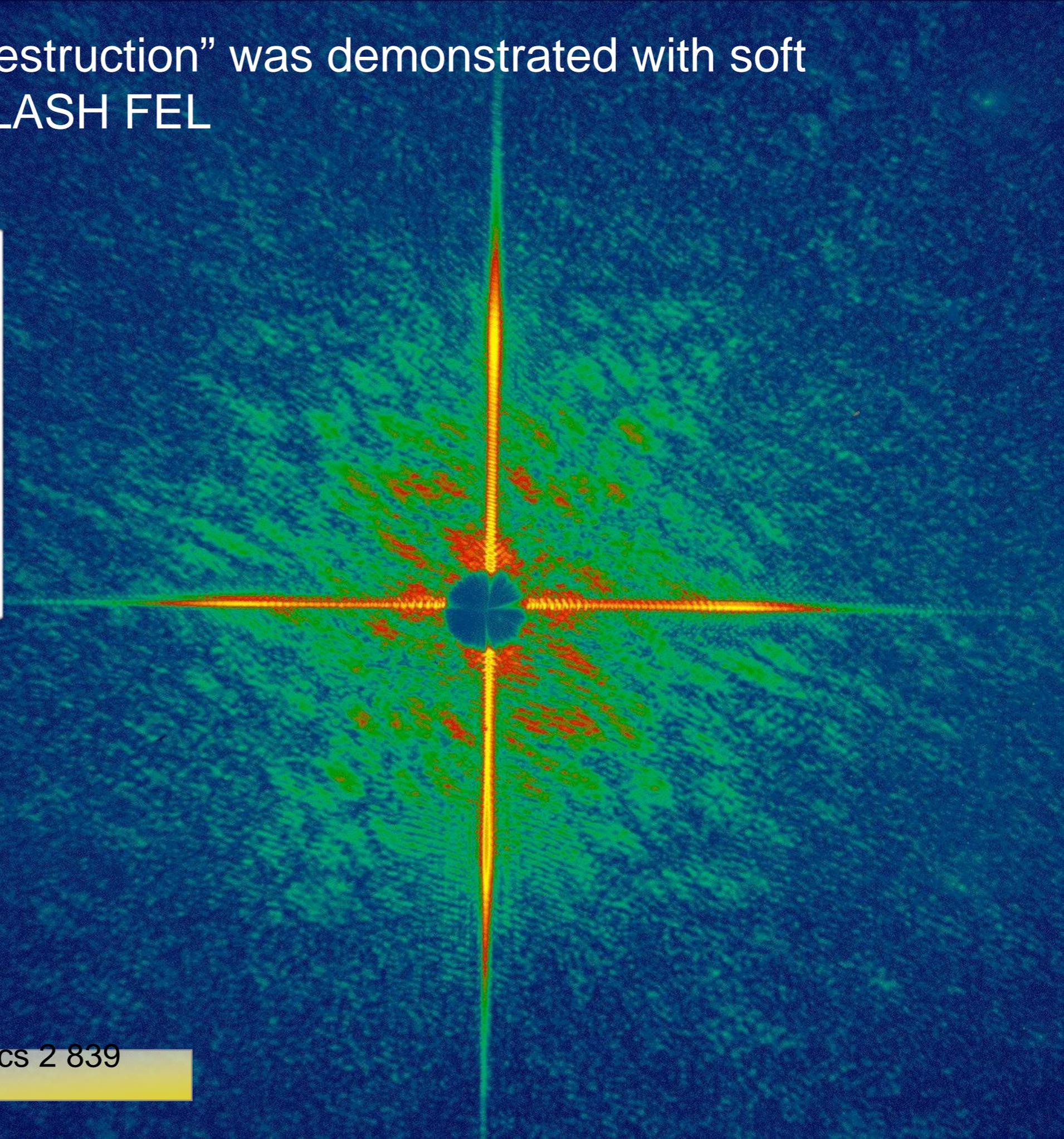
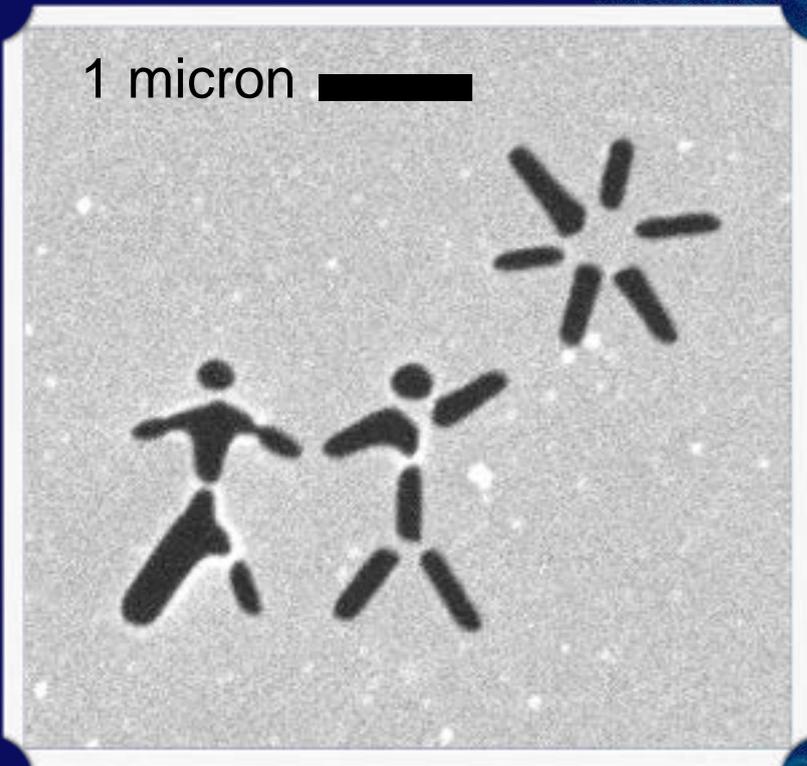


“Soft edge” prevents any scatter from the hole

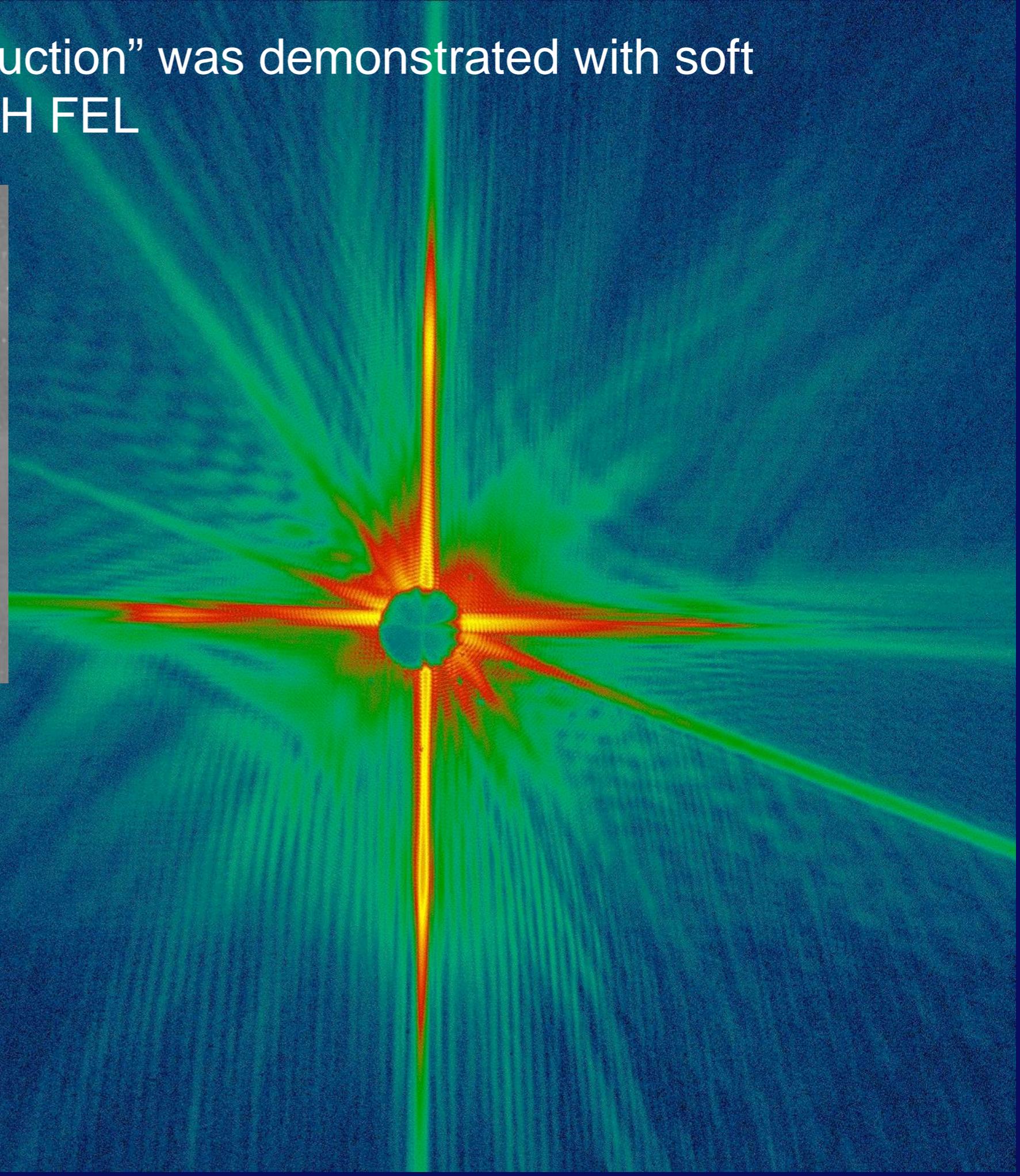
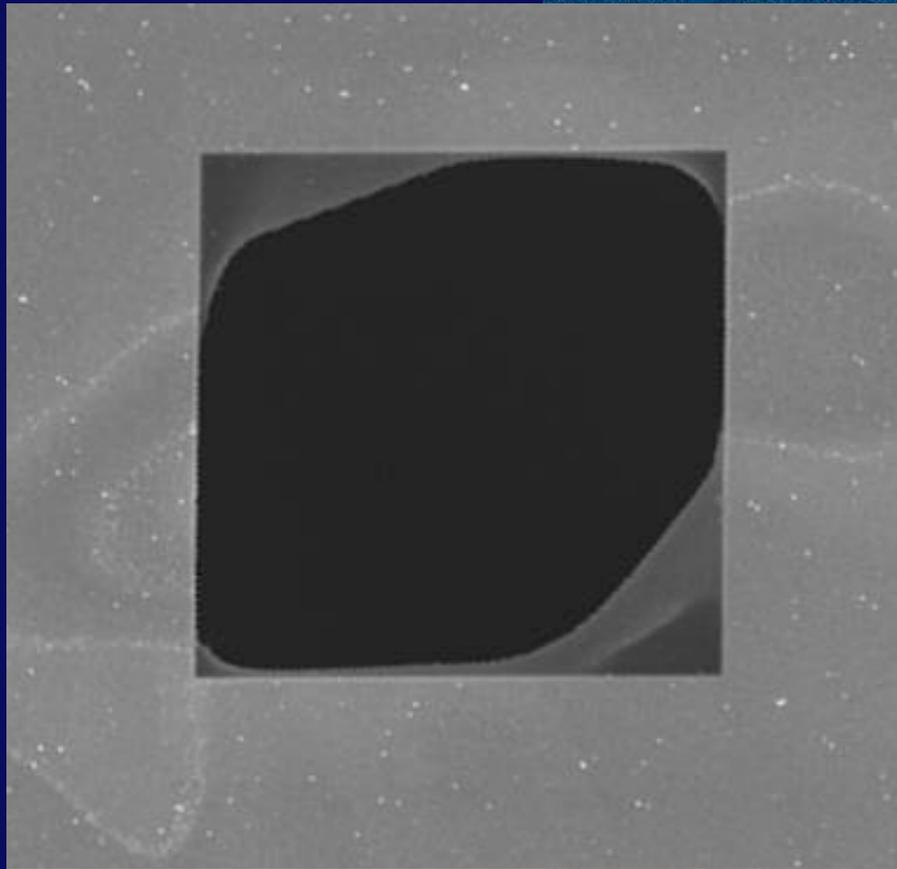


Multilayer reflectivity is uniform across the  $30^\circ$  to  $60^\circ$  gradient

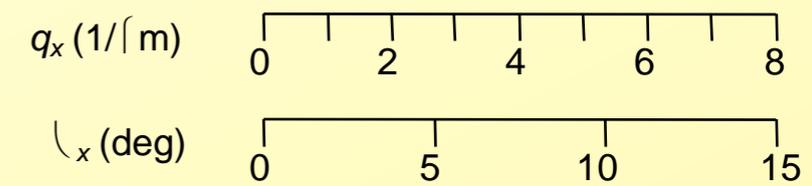
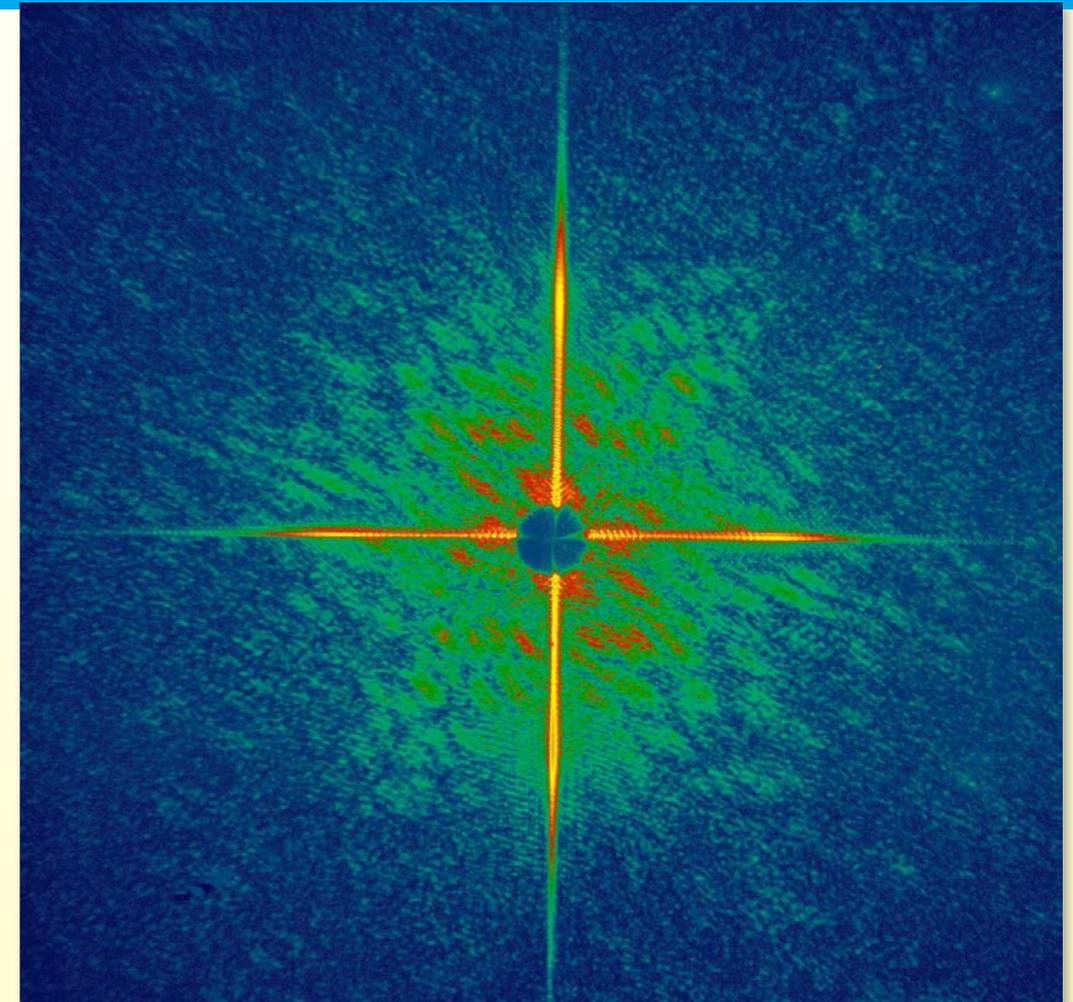
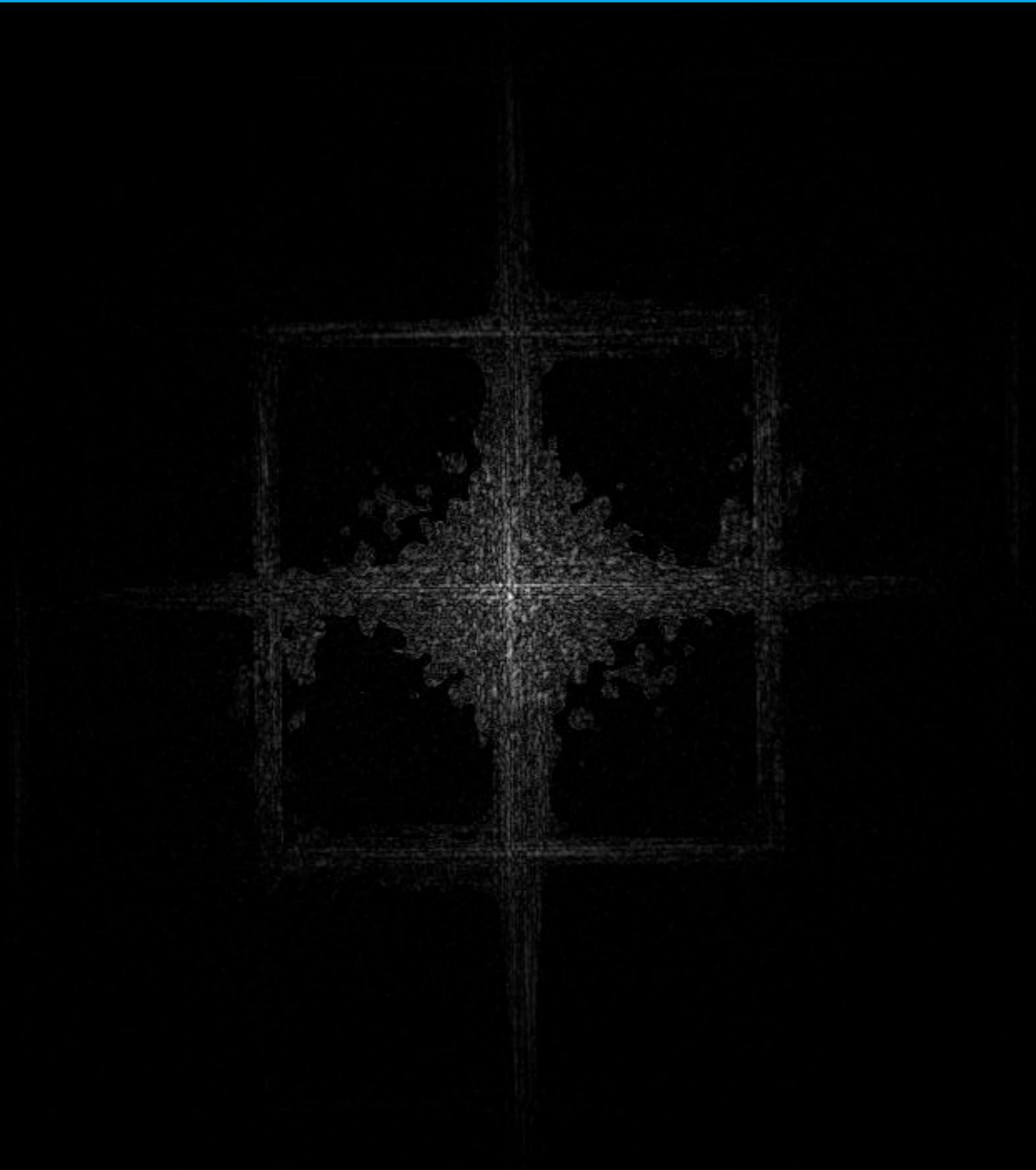
“Diffraction before destruction” was demonstrated with soft X-rays at DESY’s FLASH FEL



“Diffraction before destruction” was demonstrated with soft X-rays at DESY’s FLASH FEL



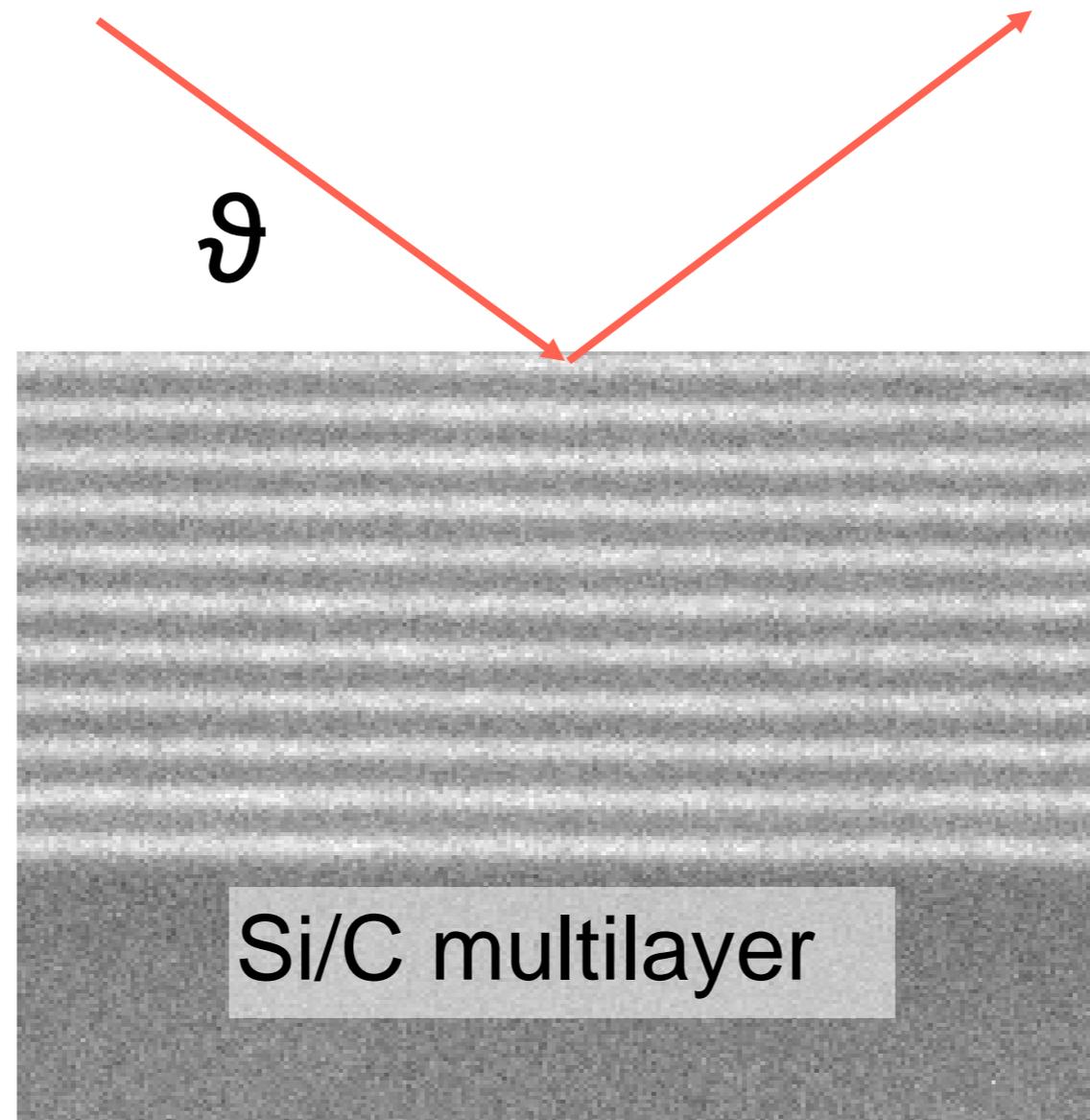
# We perform ab initio image reconstruction with our “Shrinkwrap” algorithm



S. Marchesini et al. Phys Rev B 68 140101  
(2003)

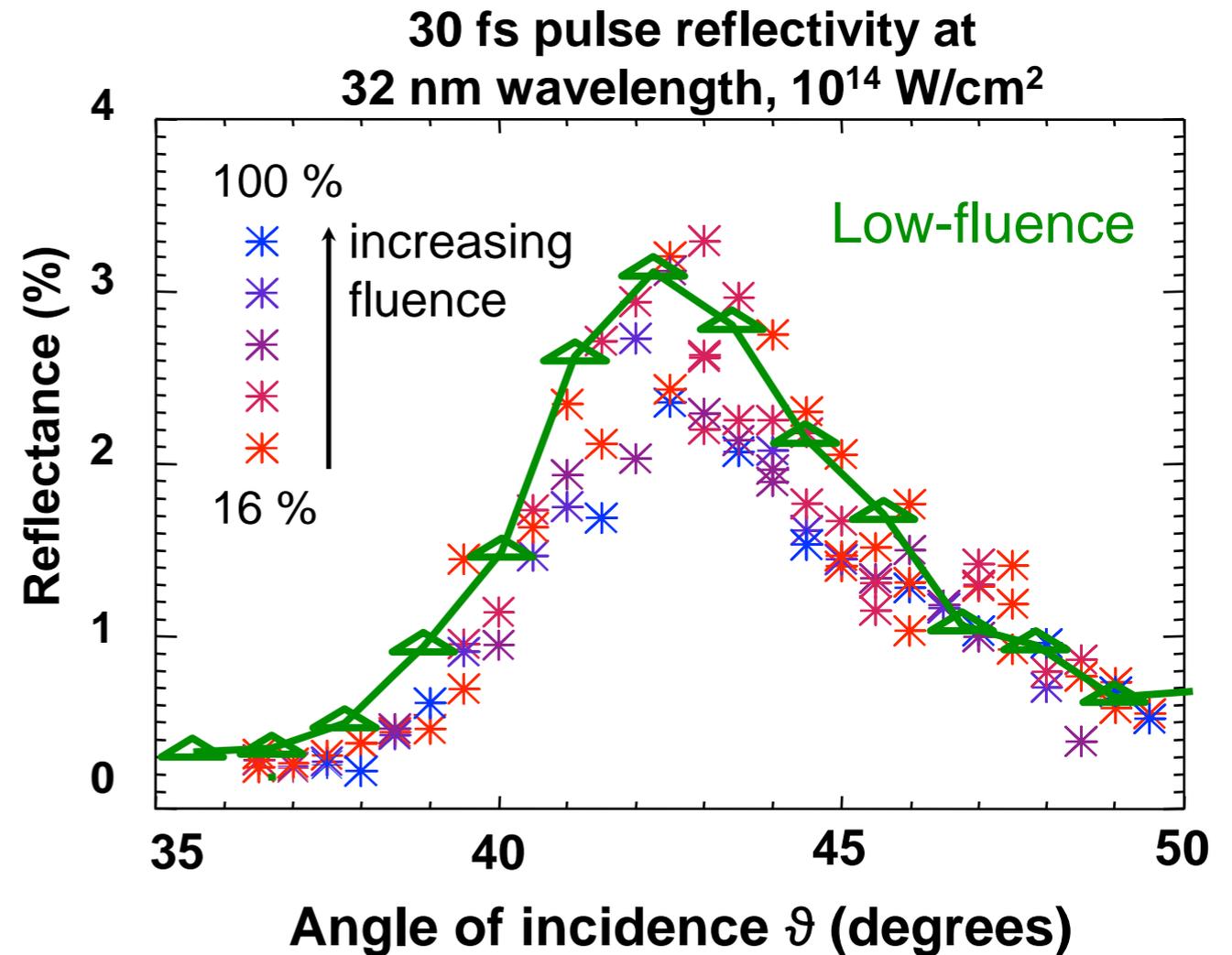
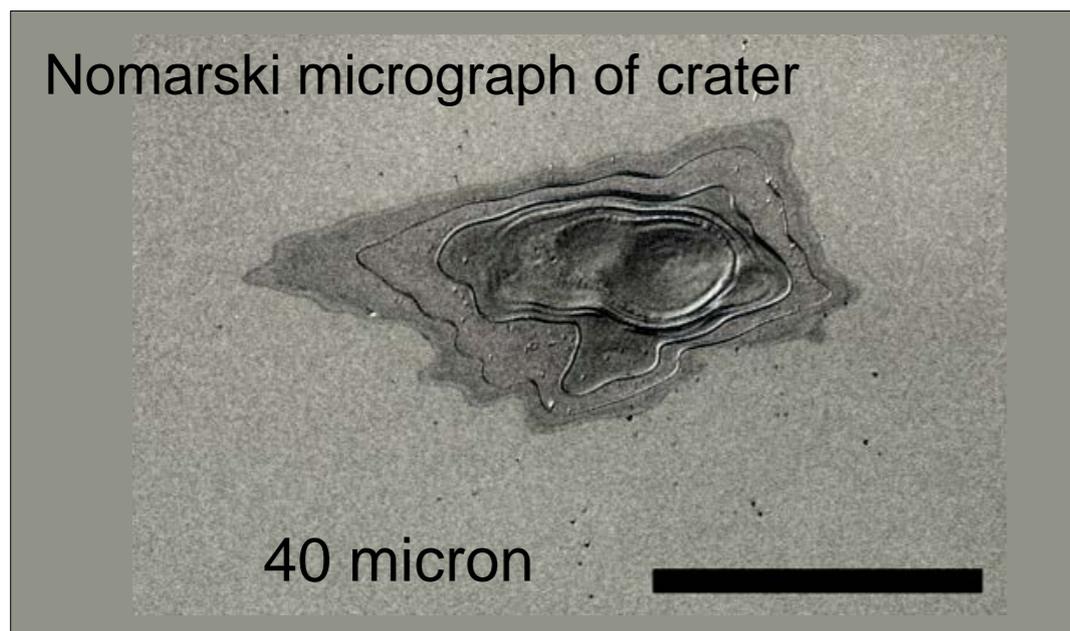
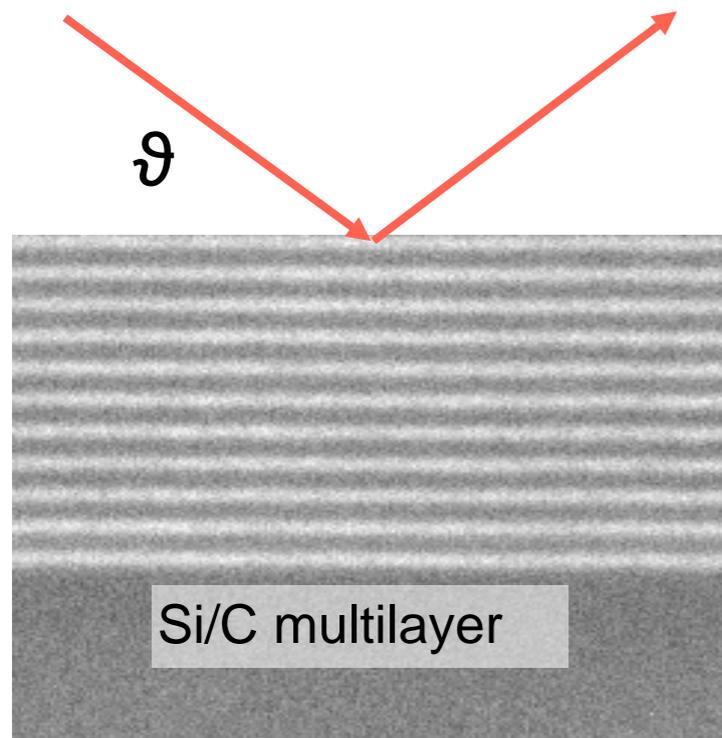
# Our first experiment was actually a bit simpler...

30 fs pulse ( $10^{14}$  W cm<sup>-2</sup>)  
32 nm wavelength



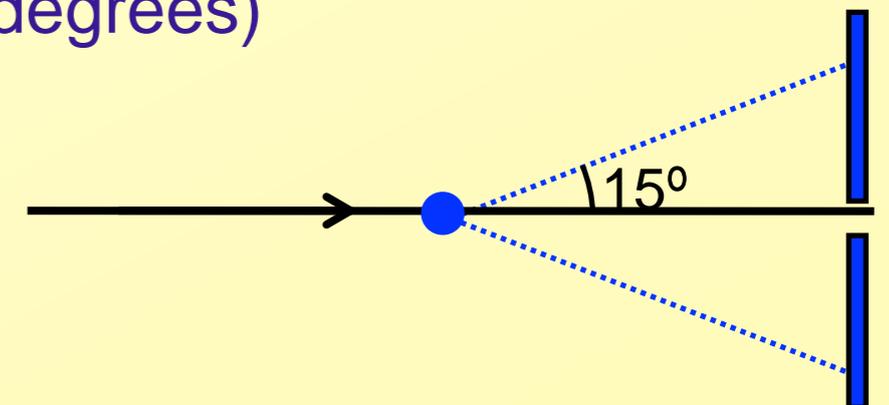
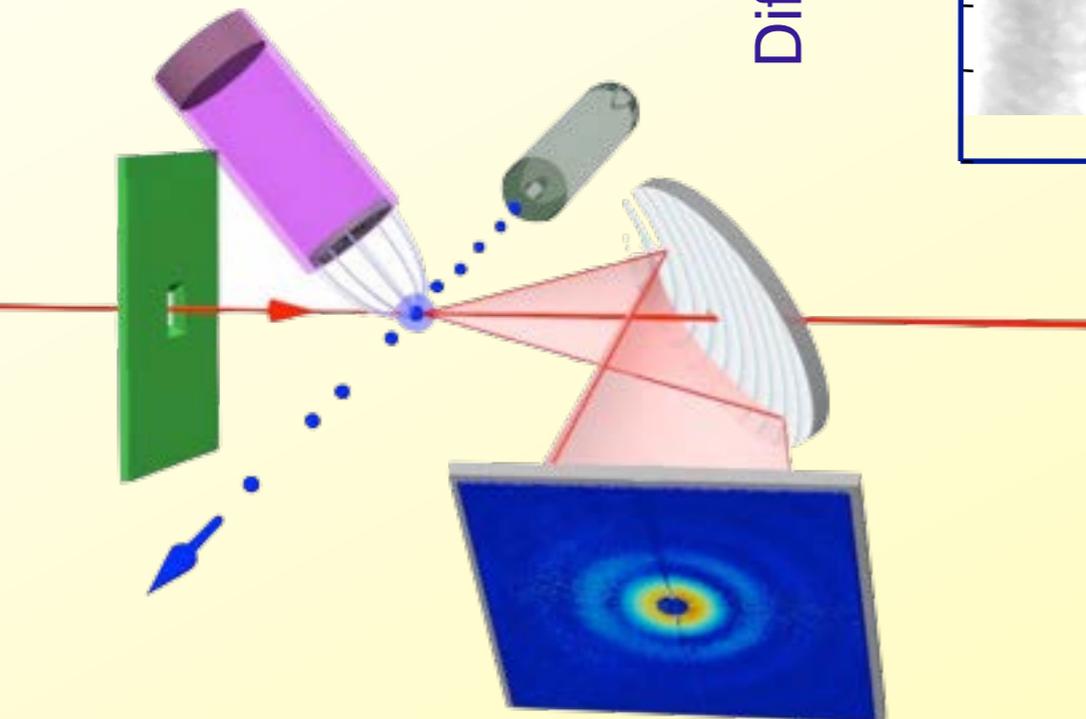
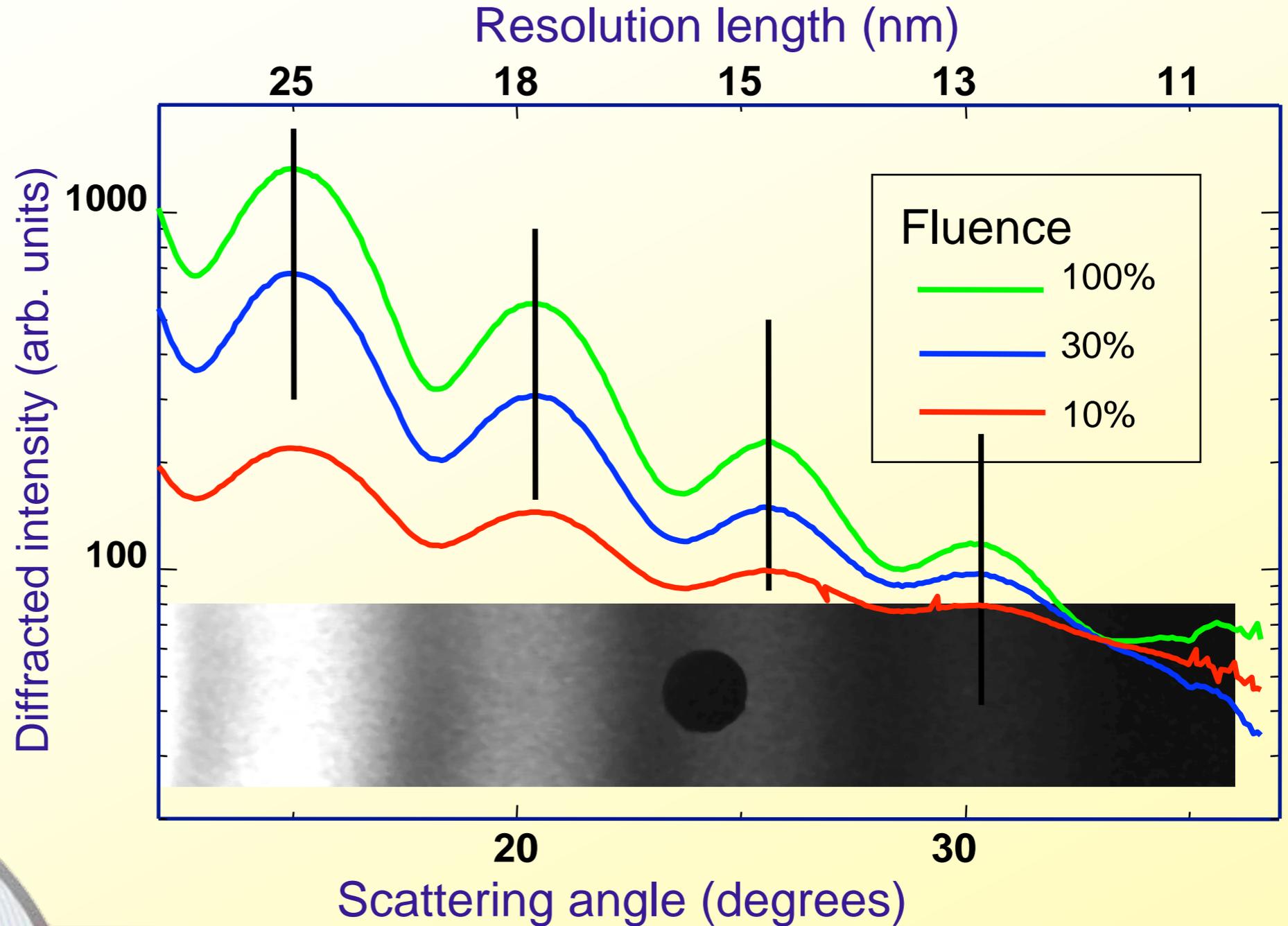
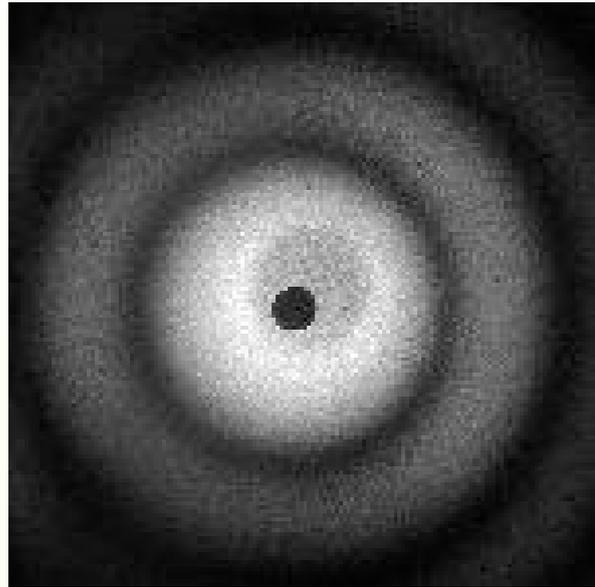
Saša Bajt

# First EUV-FEL experiments show that structural information can be obtained before destruction



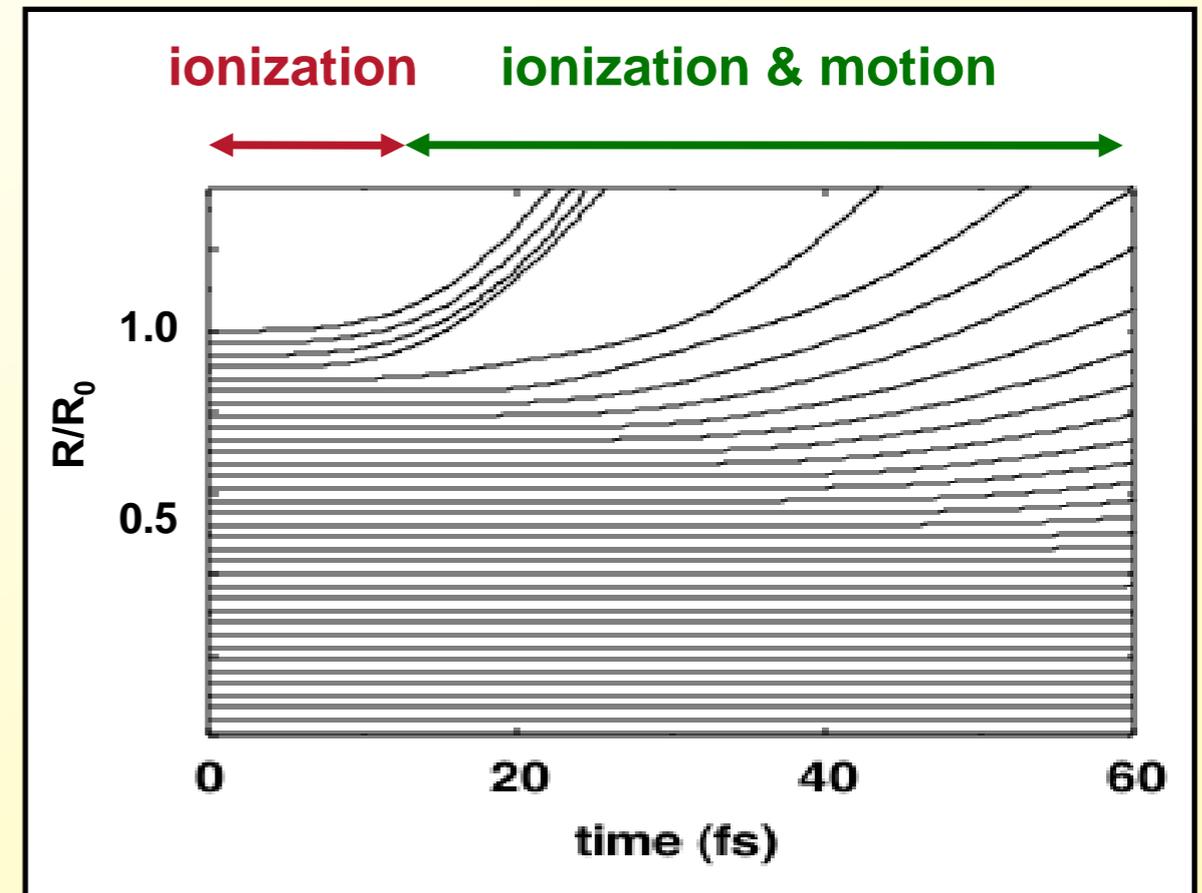
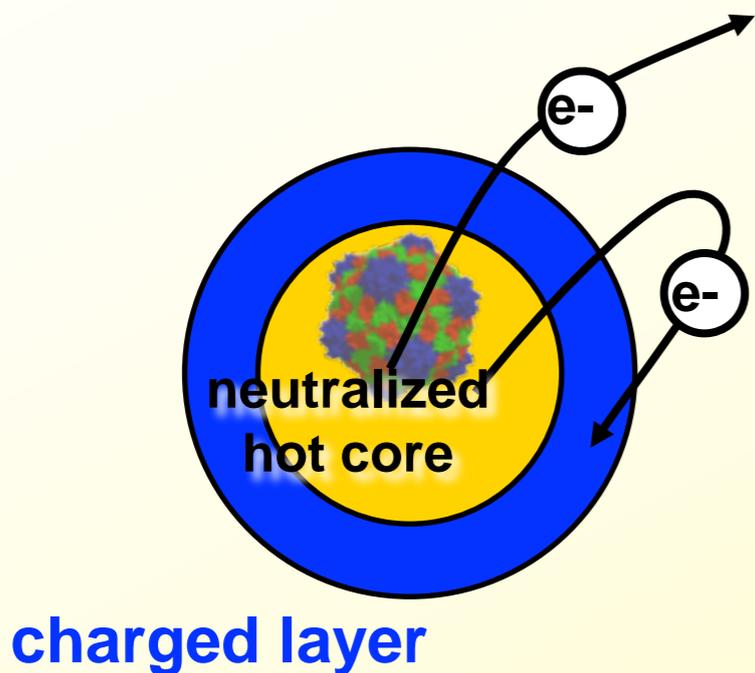
Reflectivity unchanged  
Multilayer  $d$  spacing not changed by more than 0.3 nm

# Initial high-angle diffraction shows no change in structure of particles greater than 12 nm

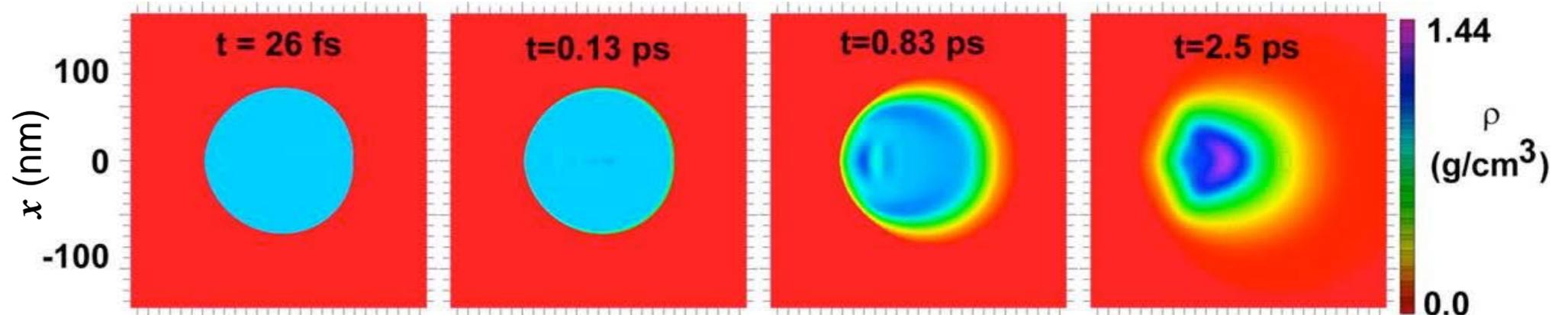


# XFEL diffraction of molecules and clusters is modified (damaged) by photoionization and motion of atoms

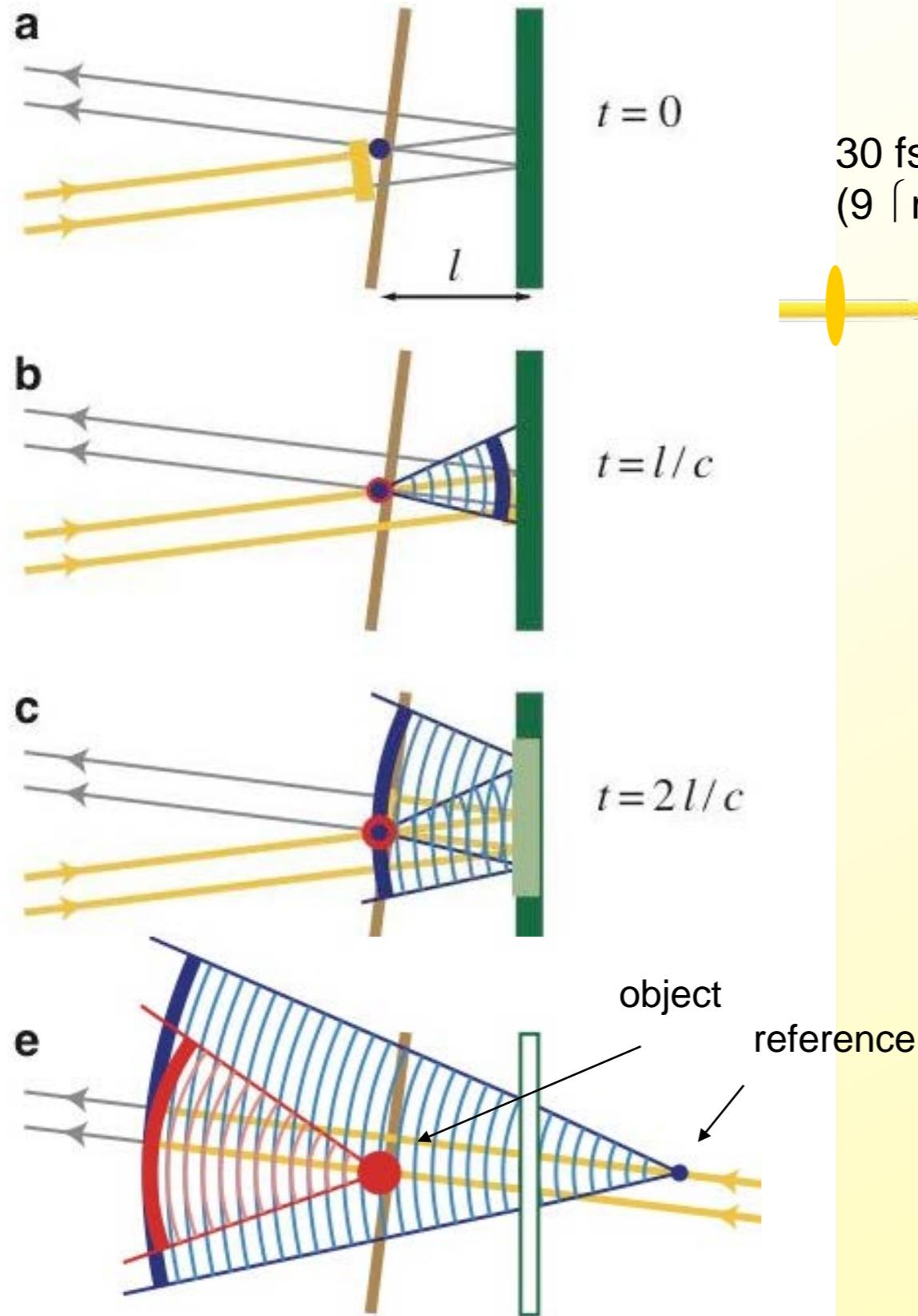
- ⑩ Photoionization (and subsequent collisional ionization) releases charges from the free molecule which lead to Coulomb explosion.
- ⑩ After  $\sim 10$  fs, charges are trapped and neutralize the core of the particle
- ⑩ Nuclear motion occurs on outer layers first



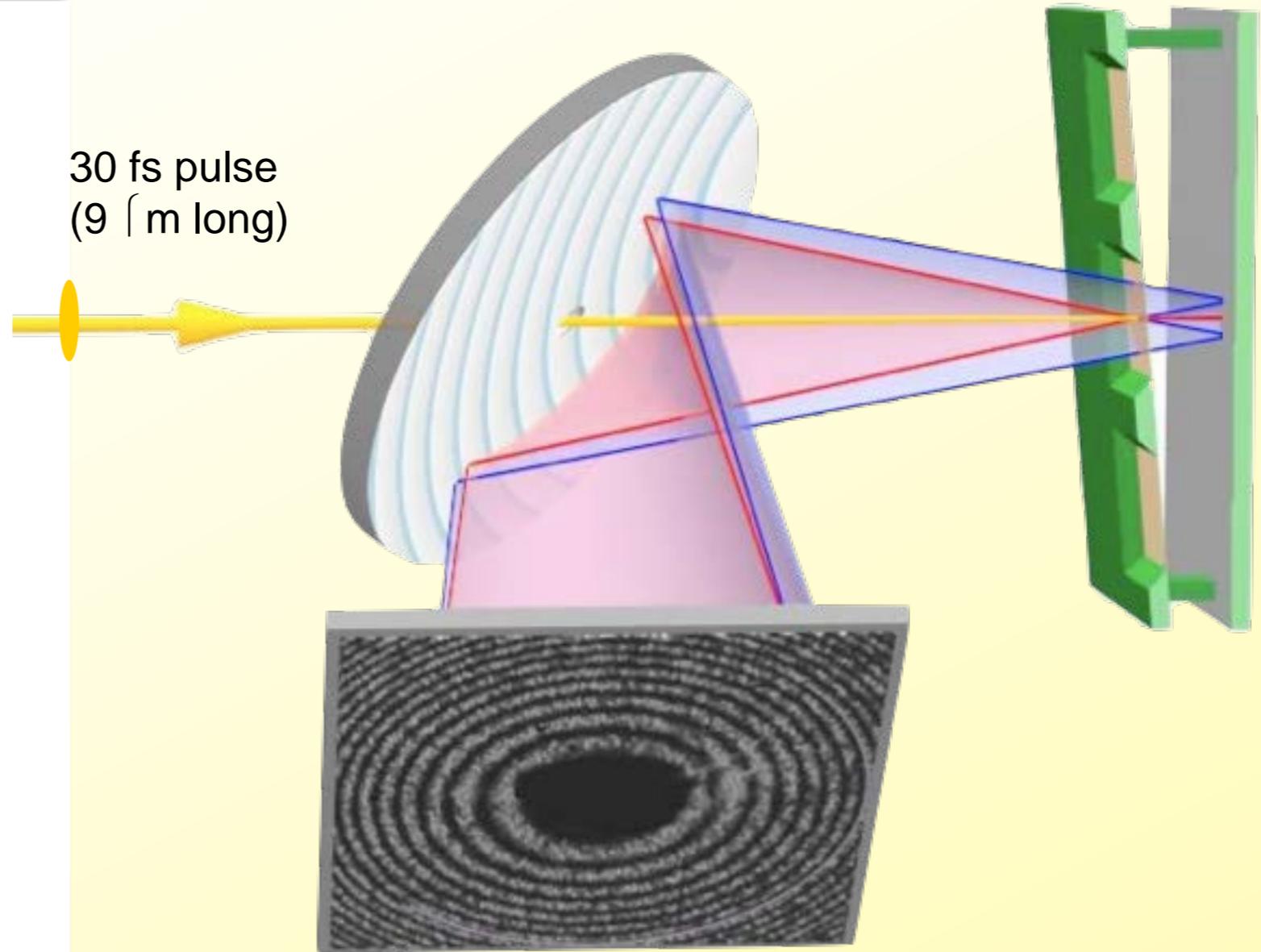
*Hydrodynamic simulations of nanostructures*



# We invented a new method called femtosecond time-delay holography



30 fs pulse  
(9  $\mu\text{m}$  long)

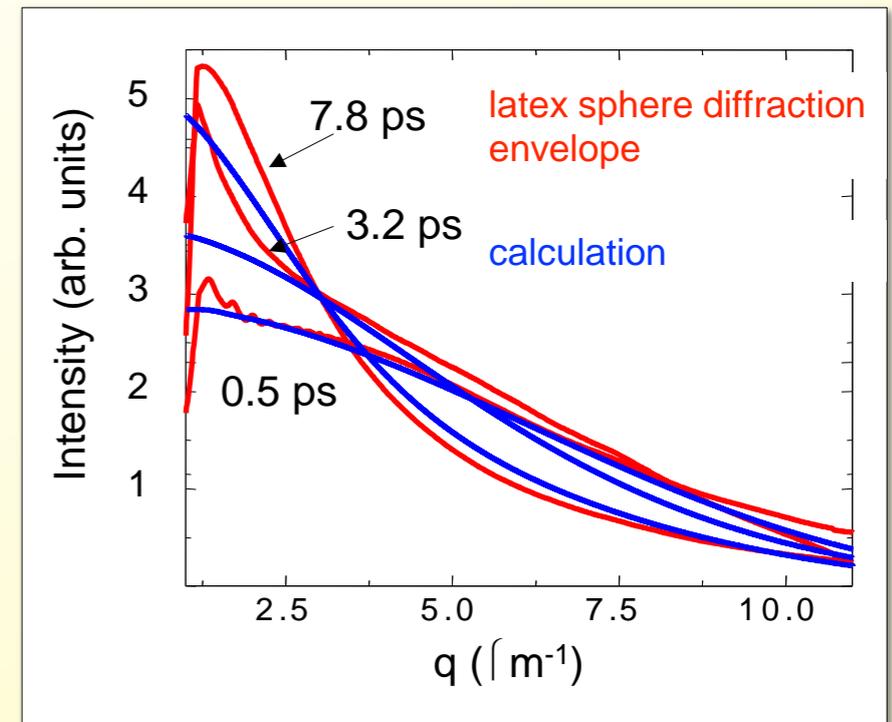


— Prompt diffraction  
— Delayed diffraction

Time delay  $2l/c$

H. Chapman et al., Nature 448 676 (2007)

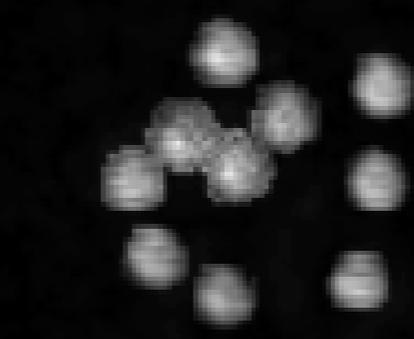
# Time-delay holography with 3 fs time resolution indicates the particle explosion



$<4\text{\AA} / (30 \text{ fs})$

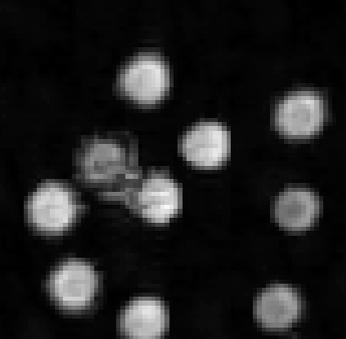
Single shot ultrafast time-delay X-ray hologram, with 300 fs delay

without tamper



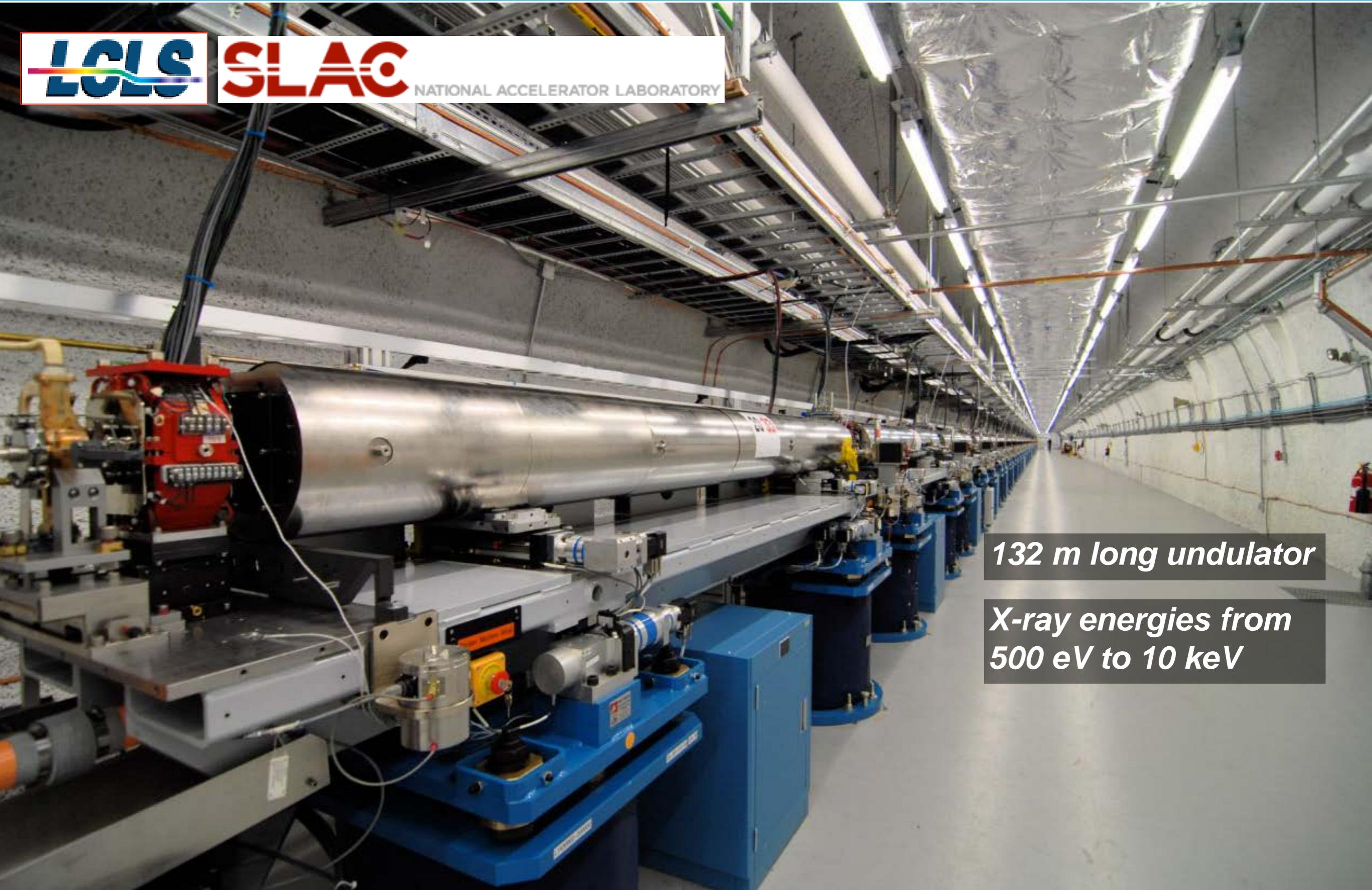
1  $\mu\text{m}$

with tamper



13 ps delay

The Linac Coherent Light Source has been in operation since 2009

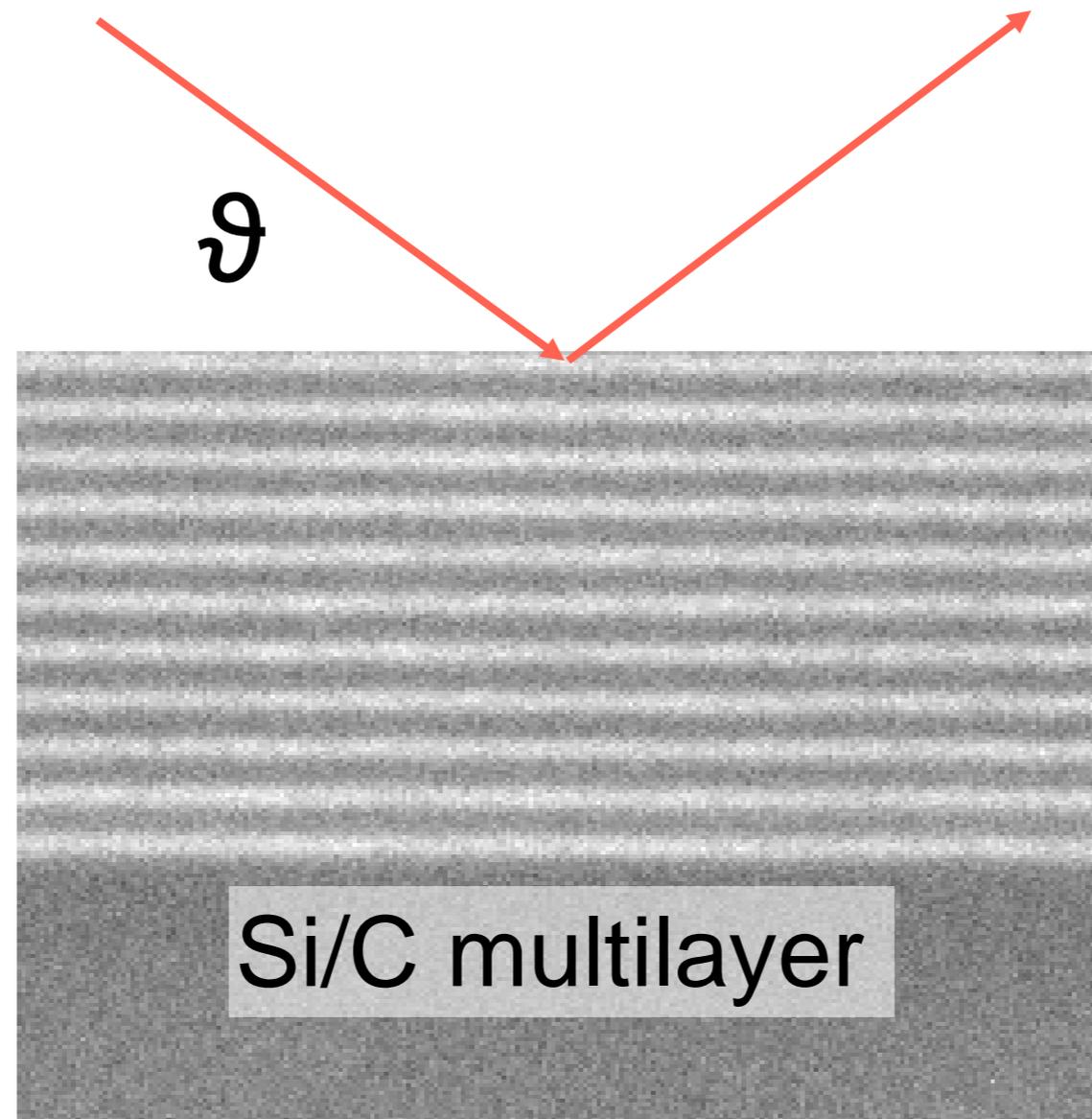


*132 m long undulator*

*X-ray energies from  
500 eV to 10 keV*

# Bragg diffraction is a good indicator of structural integrity

30 fs pulse ( $10^{14}$  W cm<sup>-2</sup>)  
32 nm wavelength



# Hard X-ray experiments at LCLS show high-resolution diffraction

## Photosystem I

9.3 keV

Single shot pattern

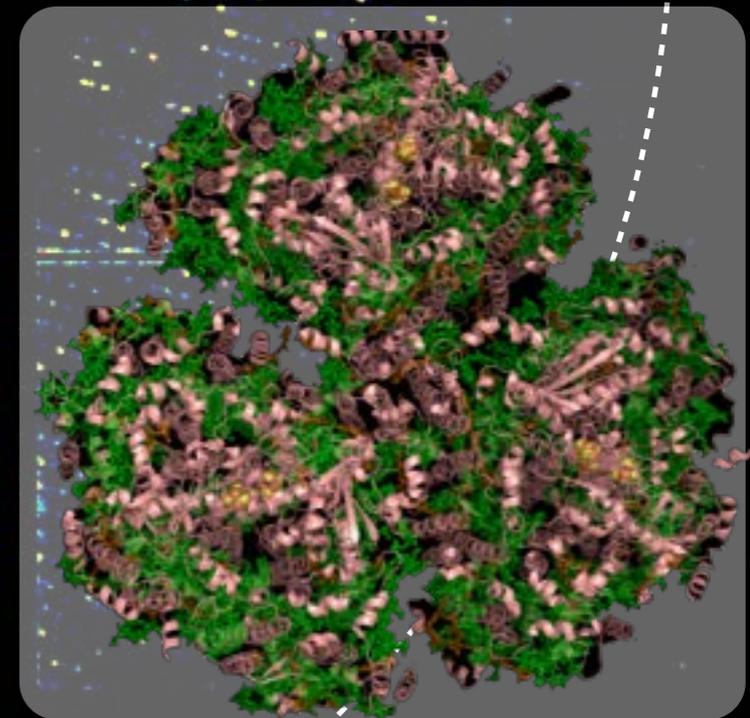
$\sim 1$  mJ ( $5 \times 10^{11}$  photons)

40 fs

$2 \times 10^{17}$  W/cm<sup>2</sup>

25 GW X-ray pulse

3.0 Å resolution



crystals prepared  
by Petra Fromme

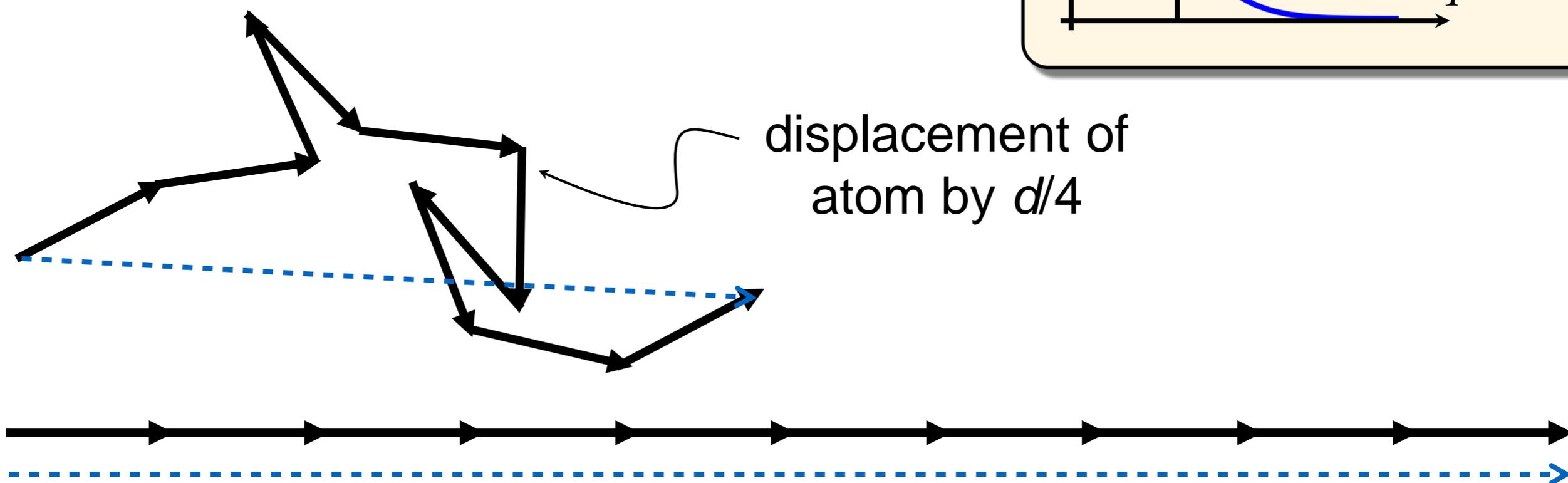
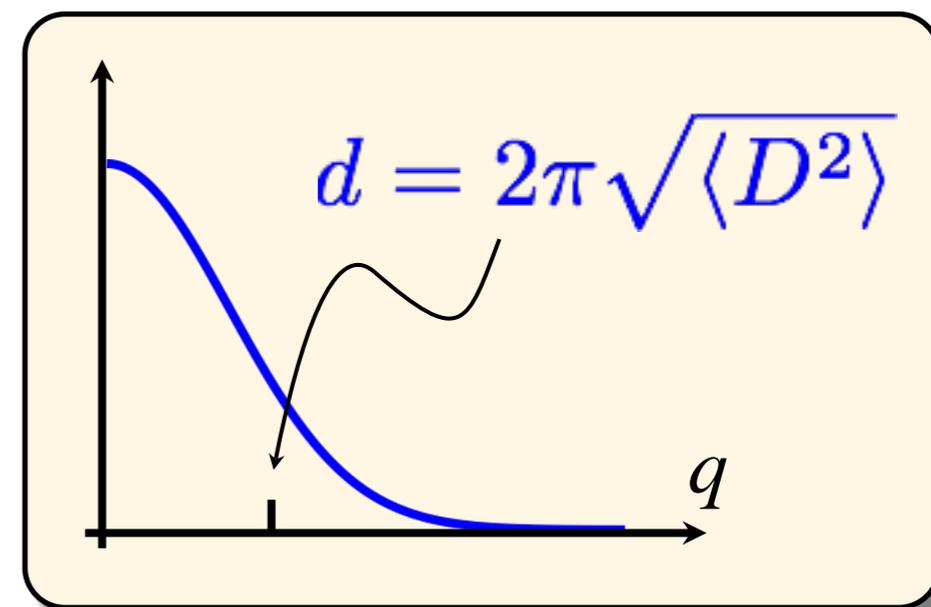
# Crystal diffraction is sensitive to atomic displacements

$$I(\mathbf{q}) = |f(\mathbf{q})|^2 = \left| \sum_i f_i \exp(i\mathbf{q} \cdot \mathbf{x}_i) \right|^2$$

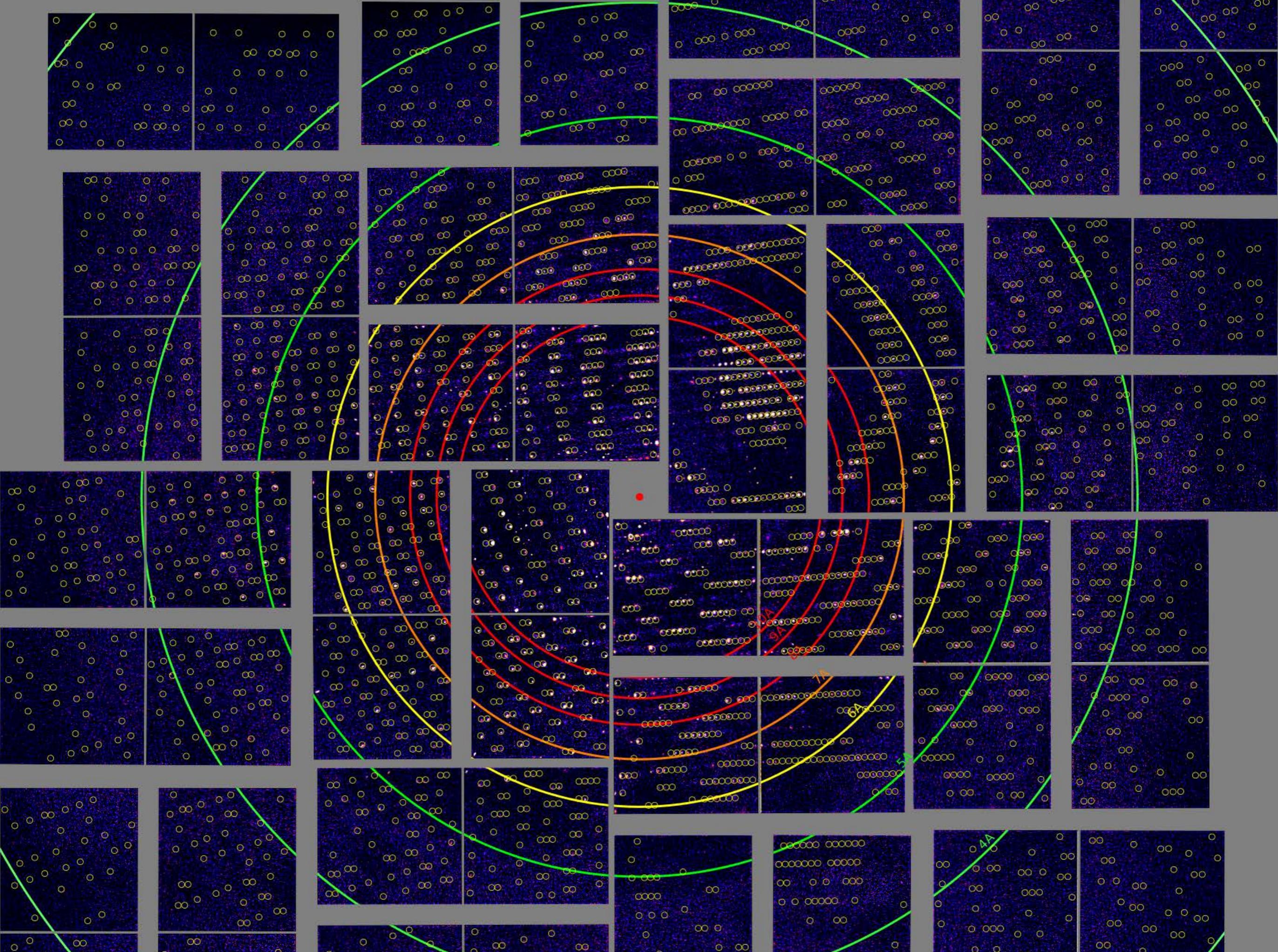
$\mathbf{x}_i \rightarrow \mathbf{x}_i + \mathbf{D}_i \quad \langle \mathbf{D}_i \rangle = 0$

$$|\mathbf{q}| = \frac{2\pi}{d}$$

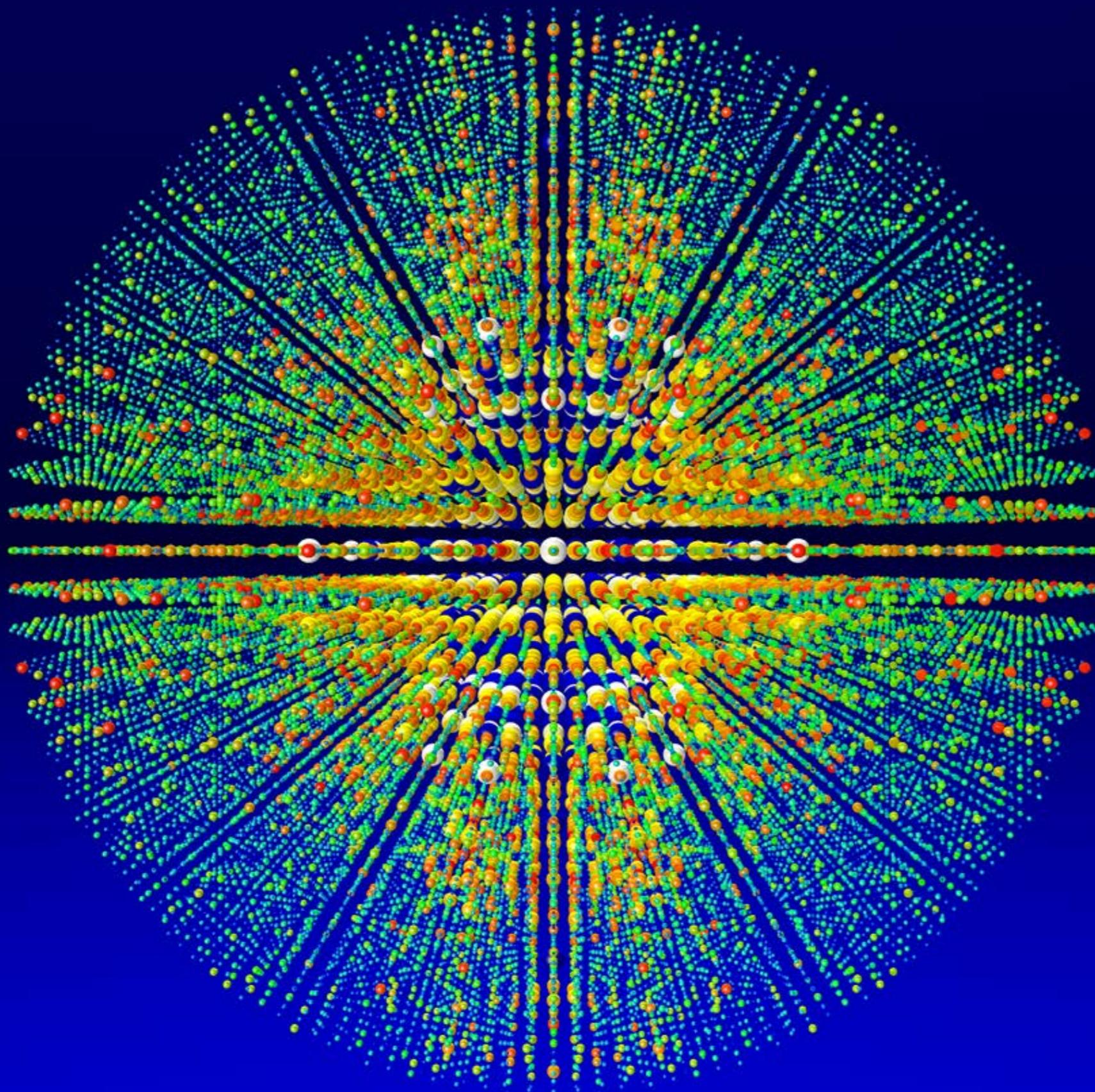
$$= |f(\mathbf{q})|^2 \exp(-q^2 \langle D^2 \rangle) + \sum_i f_i^2$$



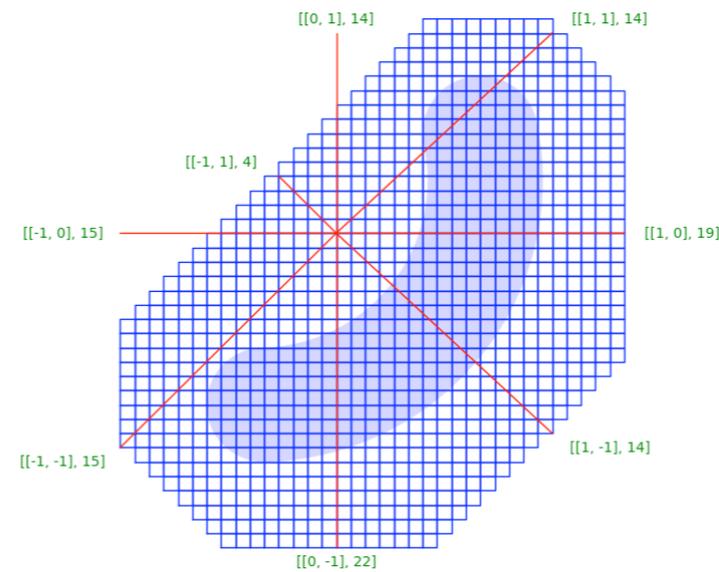
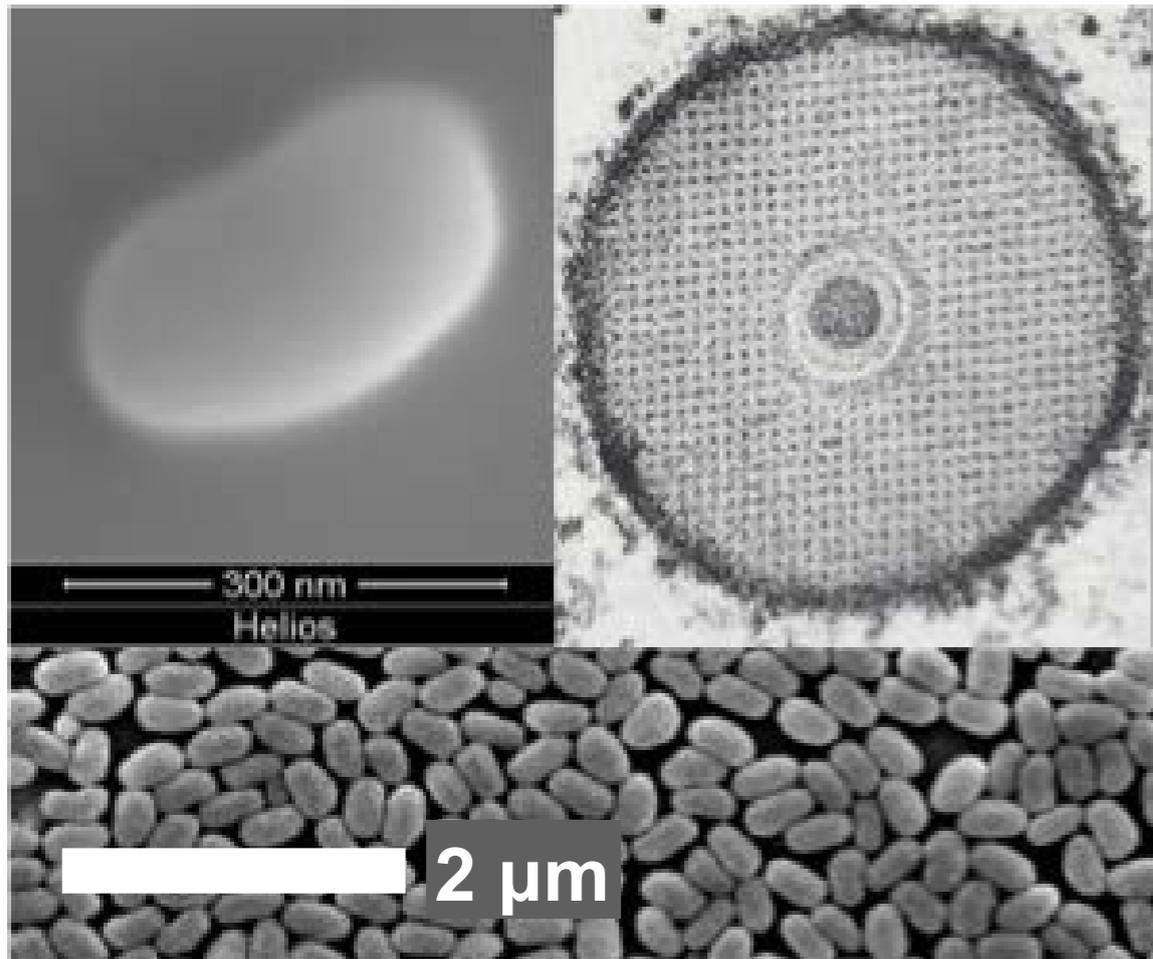




Intensities are merged into a “3D powder” pattern



# 2.1 Å resolution structure of polyhedrin obtained from single Granulovirus particles



## Virus body

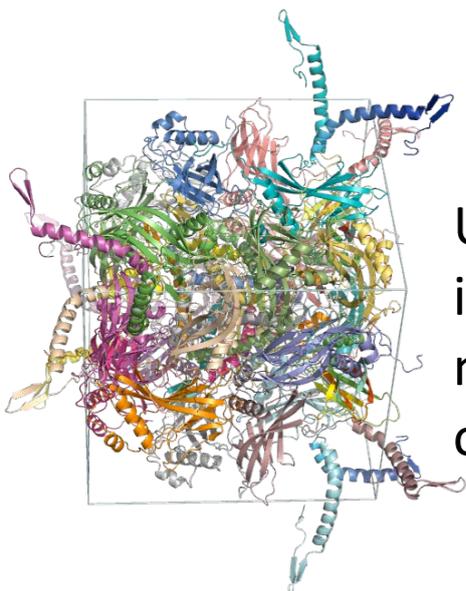
8,000 unit cells,

$a, b, c = 100 \text{ \AA}$

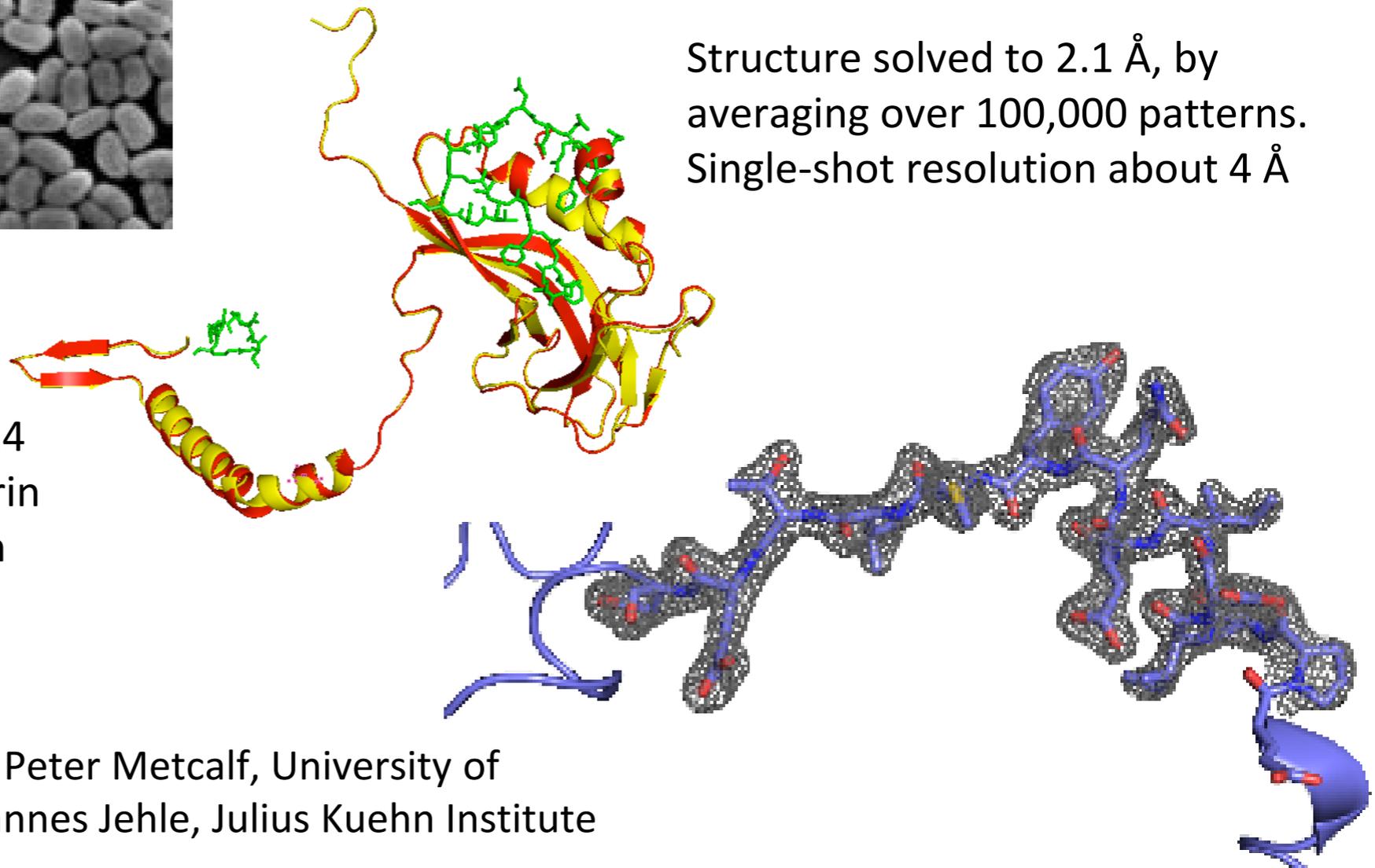
Volume of crystalline part:  
 $0.008 \mu\text{m}^3$

Dose: 2 GGy

Structure solved to 2.1 Å, by averaging over 100,000 patterns. Single-shot resolution about 4 Å

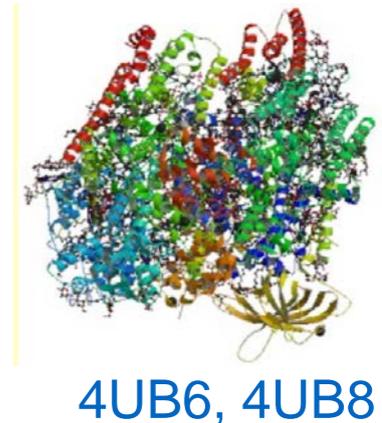
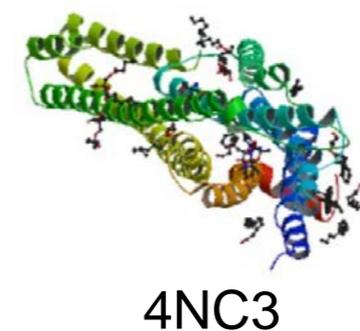
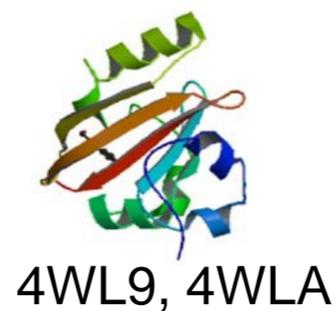
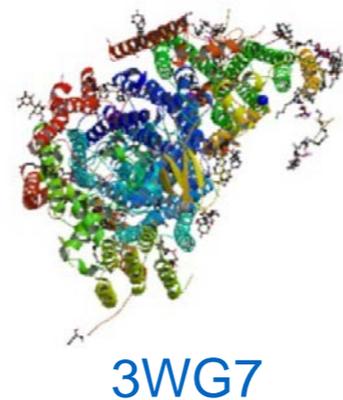
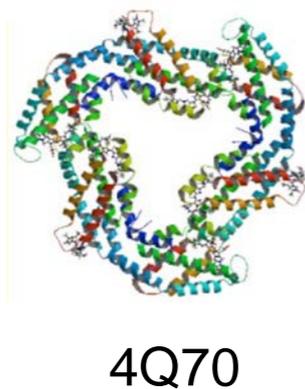
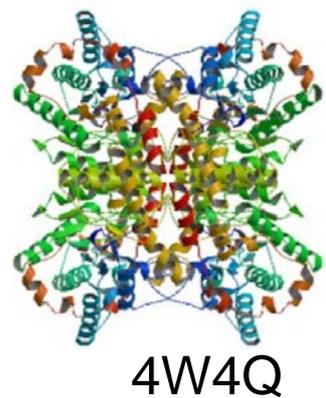
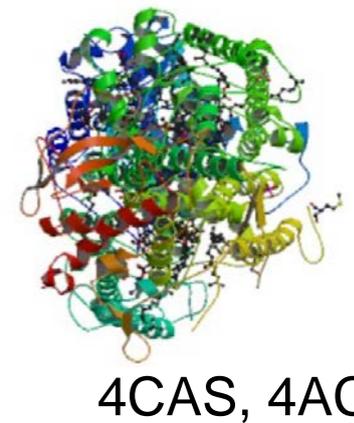
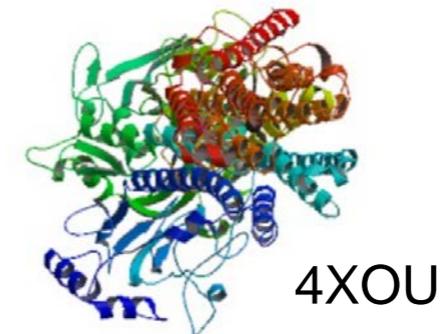
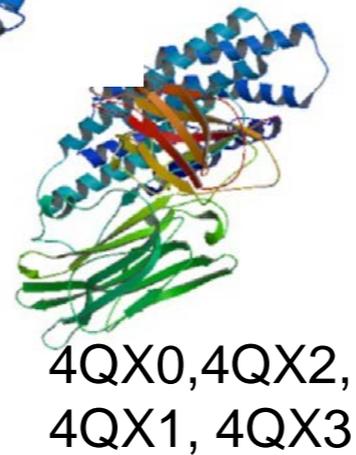
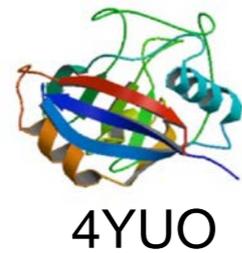
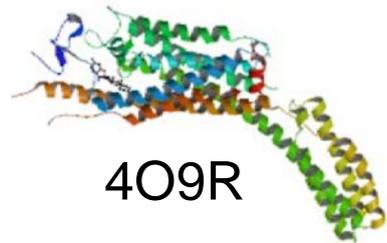
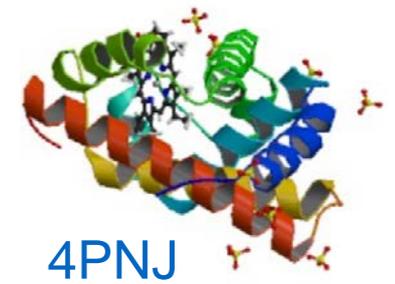
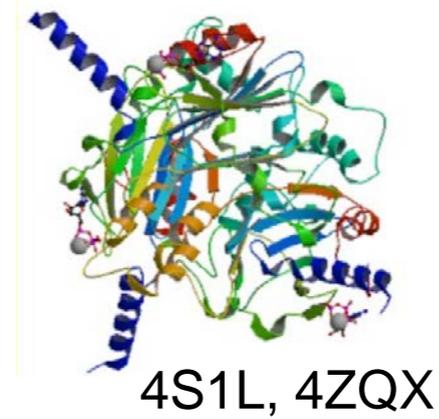
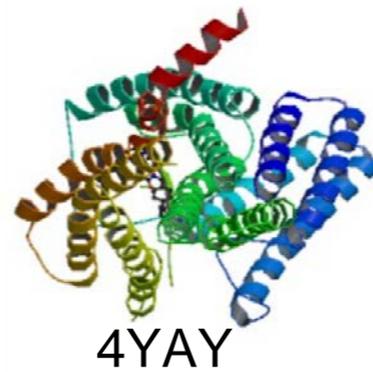
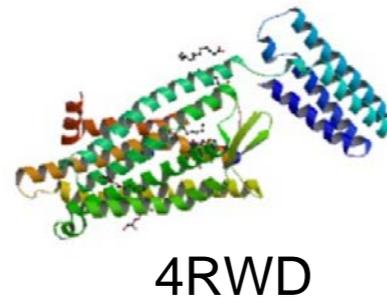
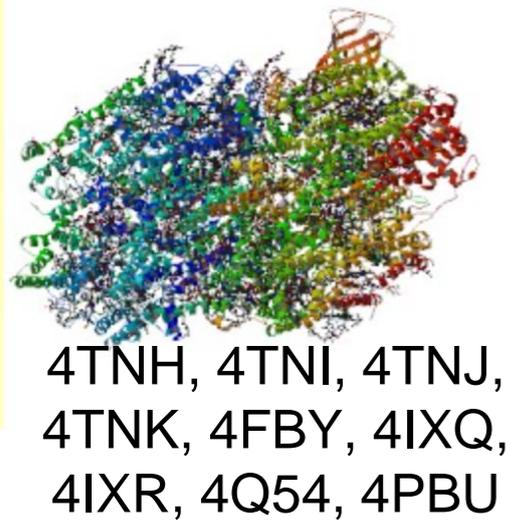
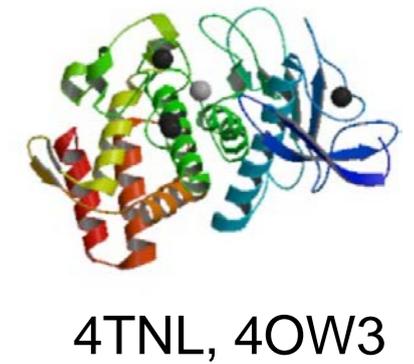
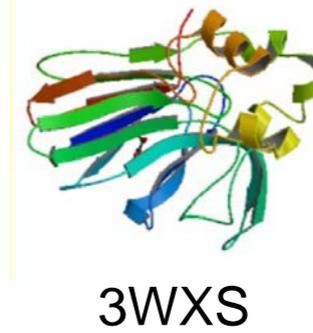
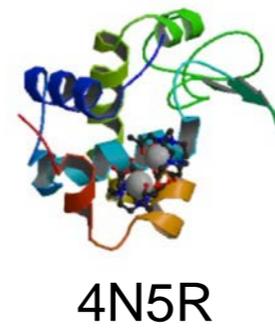
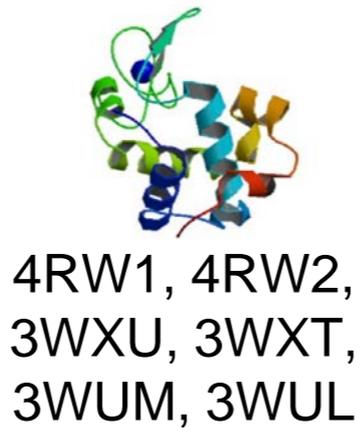
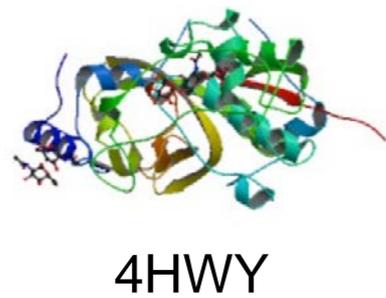
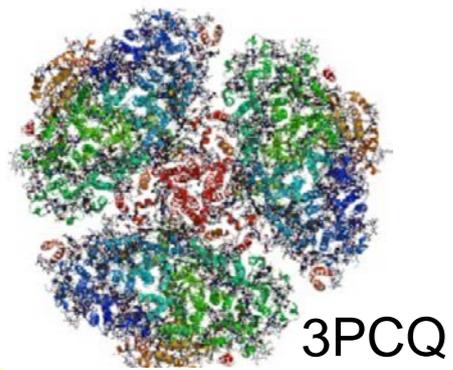


Unit cell consists of 24 interlocking polyhedrin molecules. Evolution optimised the crystal

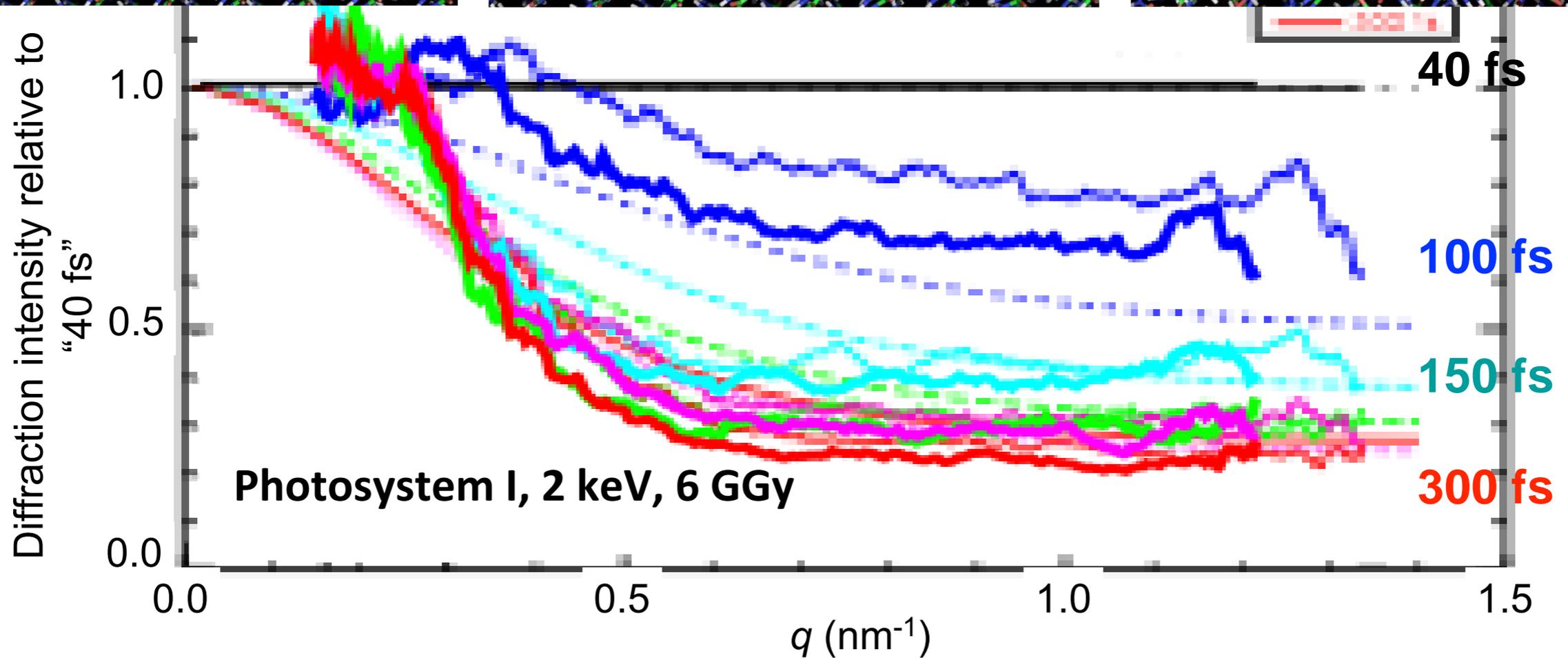
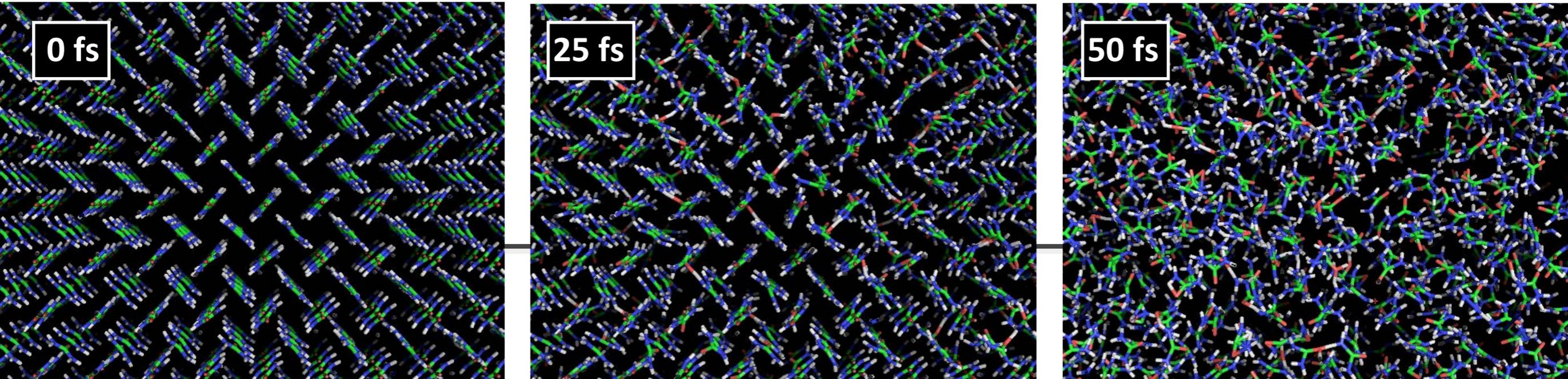


C. Gati, CFEL, with Peter Metcalf, University of Auckland and Johannes Jehle, Julius Kuehn Institute

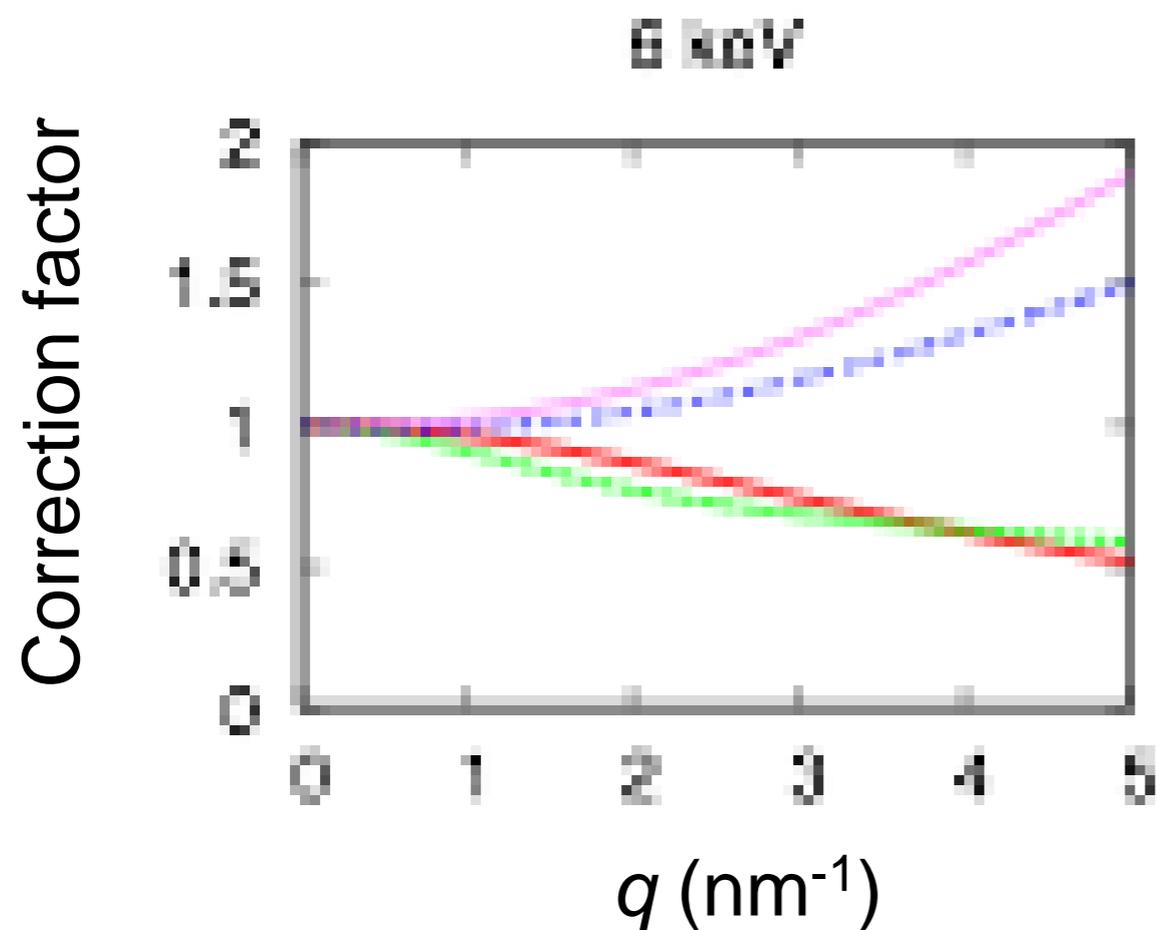
# There are now 44 FEL depositions in the protein databank



# A crystal only gives Bragg diffraction when it is a crystal! Selecting Bragg peaks filters the data



# At fast timescales the ionisation gates the diffraction rather than nuclear motion

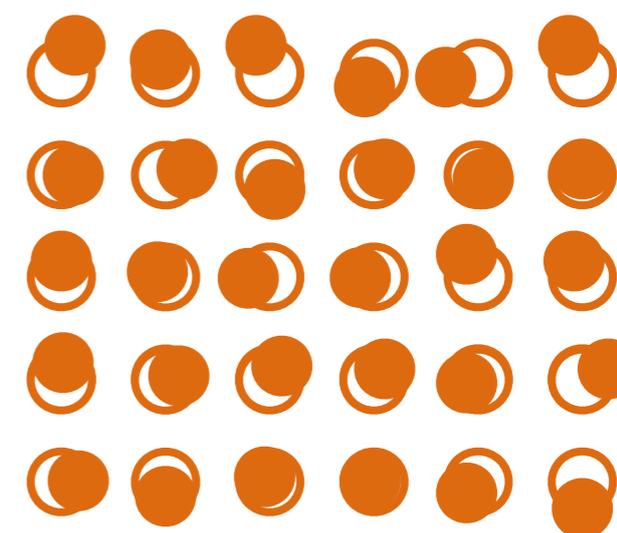
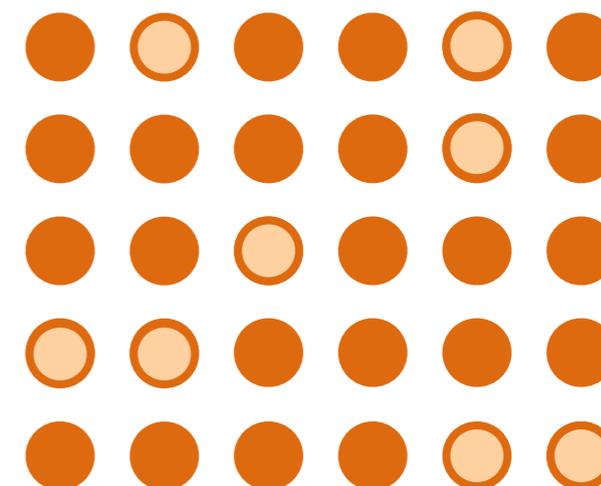


$10^{20}$  W/cm<sup>2</sup>

$10^{19}$  W/cm<sup>2</sup>

$10^{18}$  W/cm<sup>2</sup>

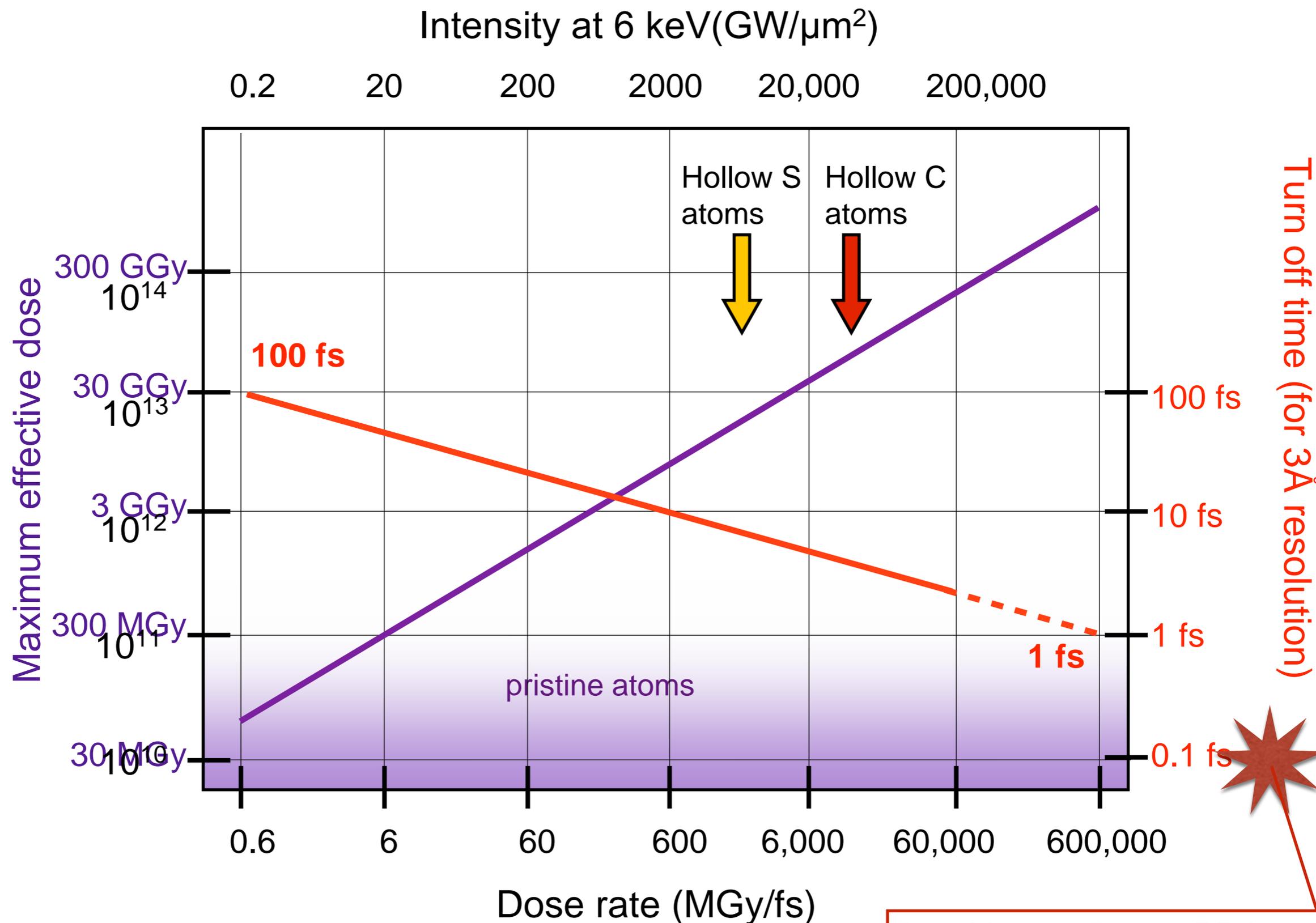
$10^{17}$  W/cm<sup>2</sup>



# Higher dose rates (i.e. higher X-ray intensities) should give larger Bragg signals

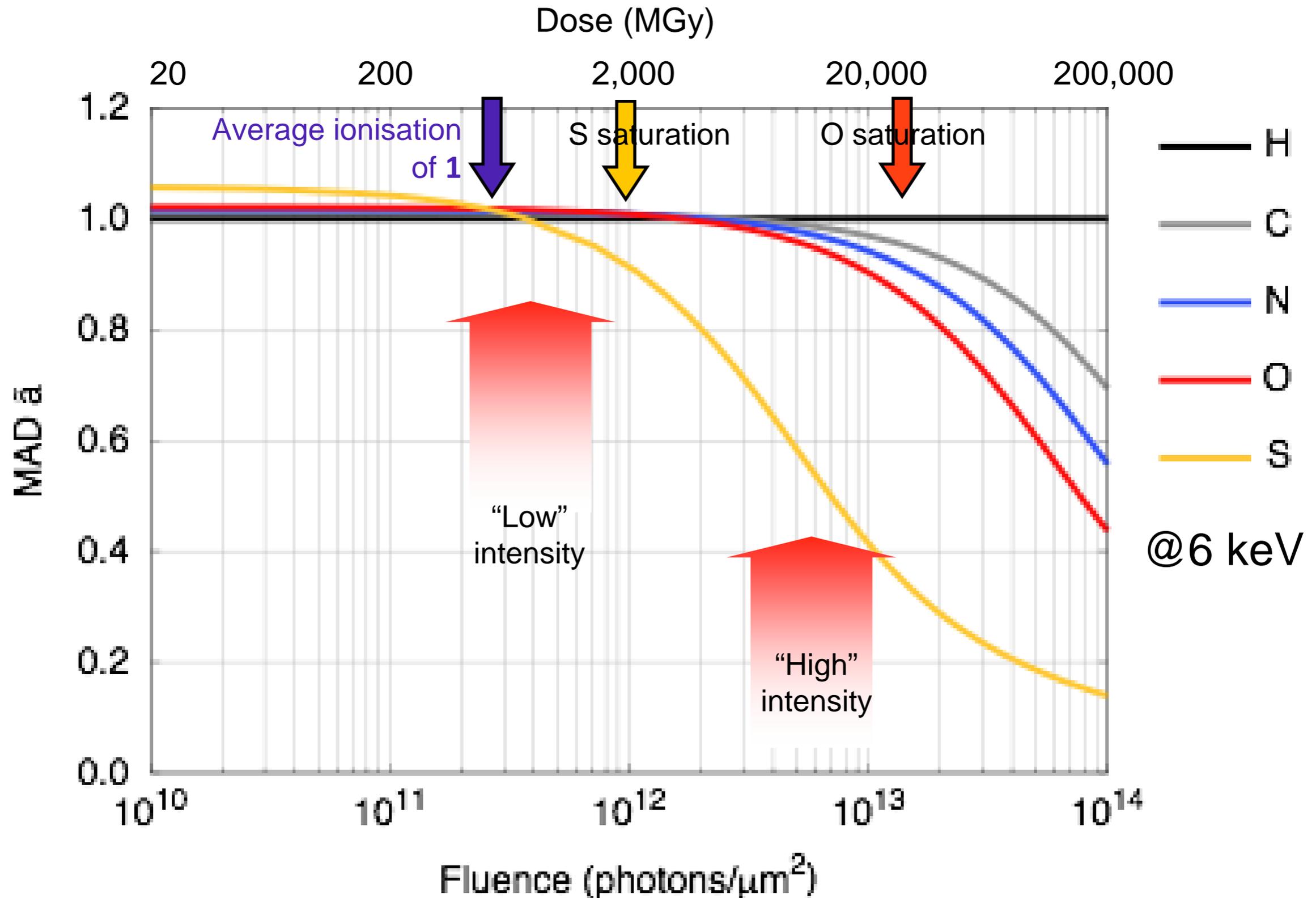


Effective fluence at 6 keV ( $\text{ph}/\mu\text{m}^2$ )

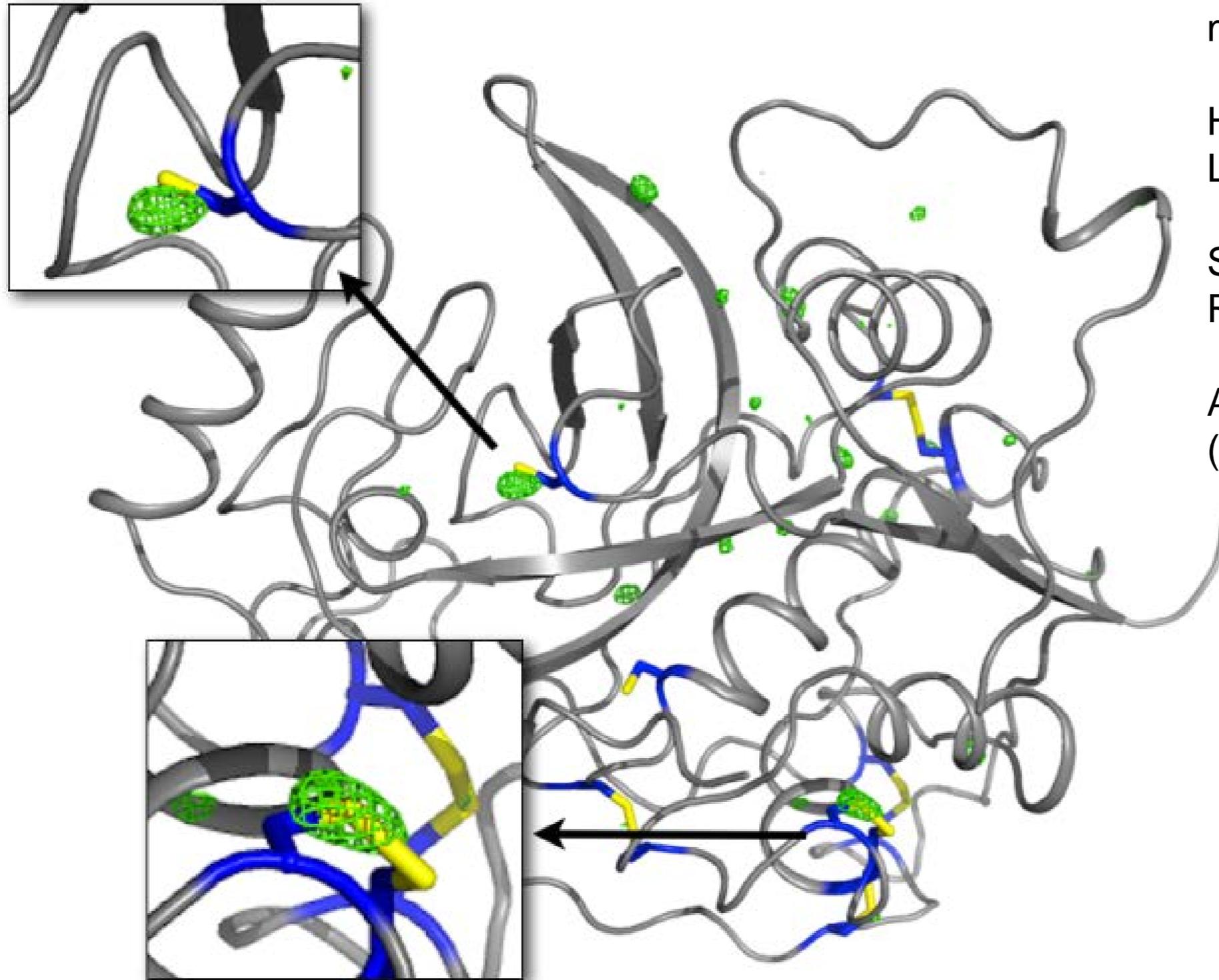


Son, Young, Santra PRA 2011

# We propose to use the fluence dependence of heavier element scattering factors for phasing



# Difference electron density between high and low fluences reveals the positions of sulfur atoms



Difference map: High intensity minus low intensity

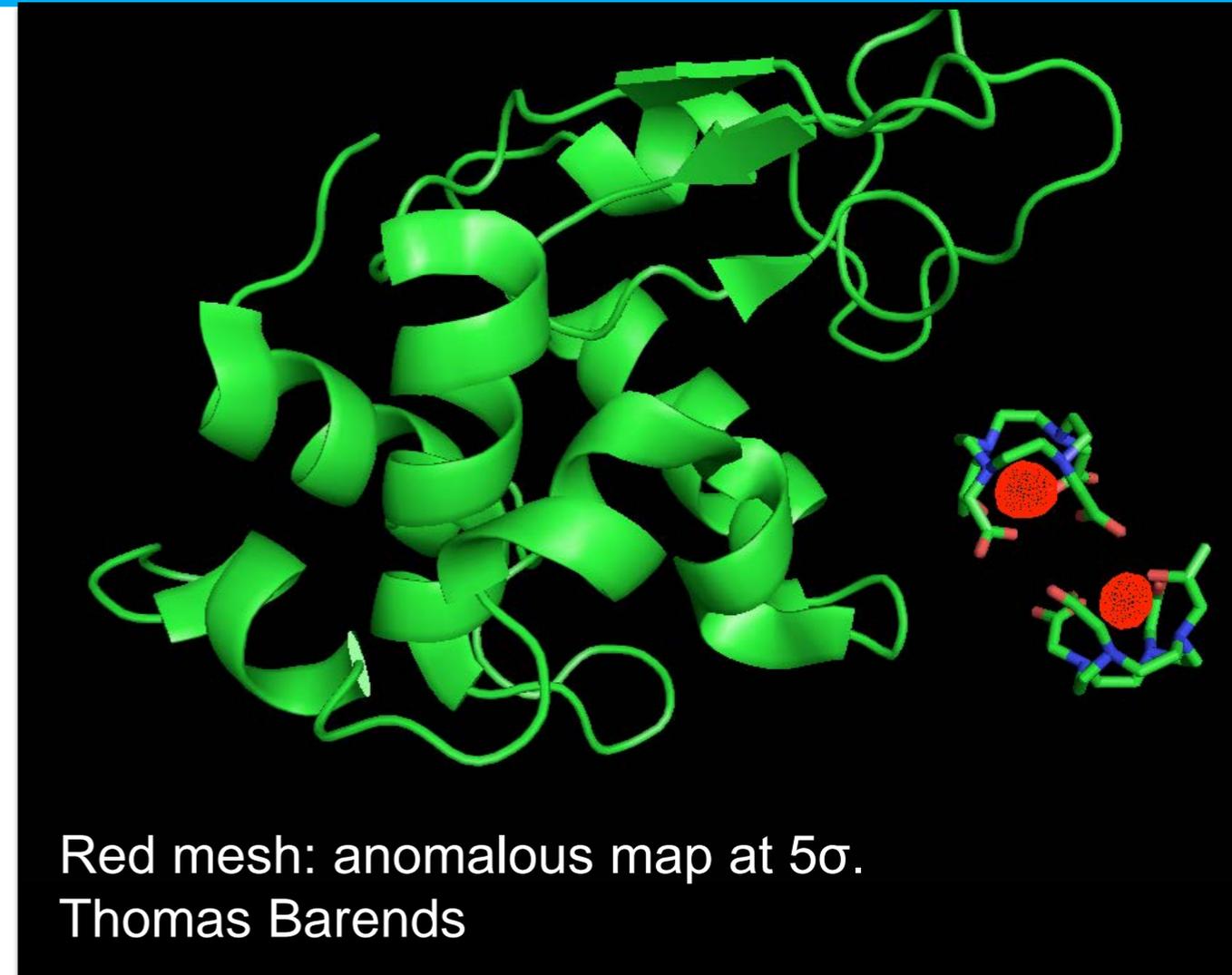
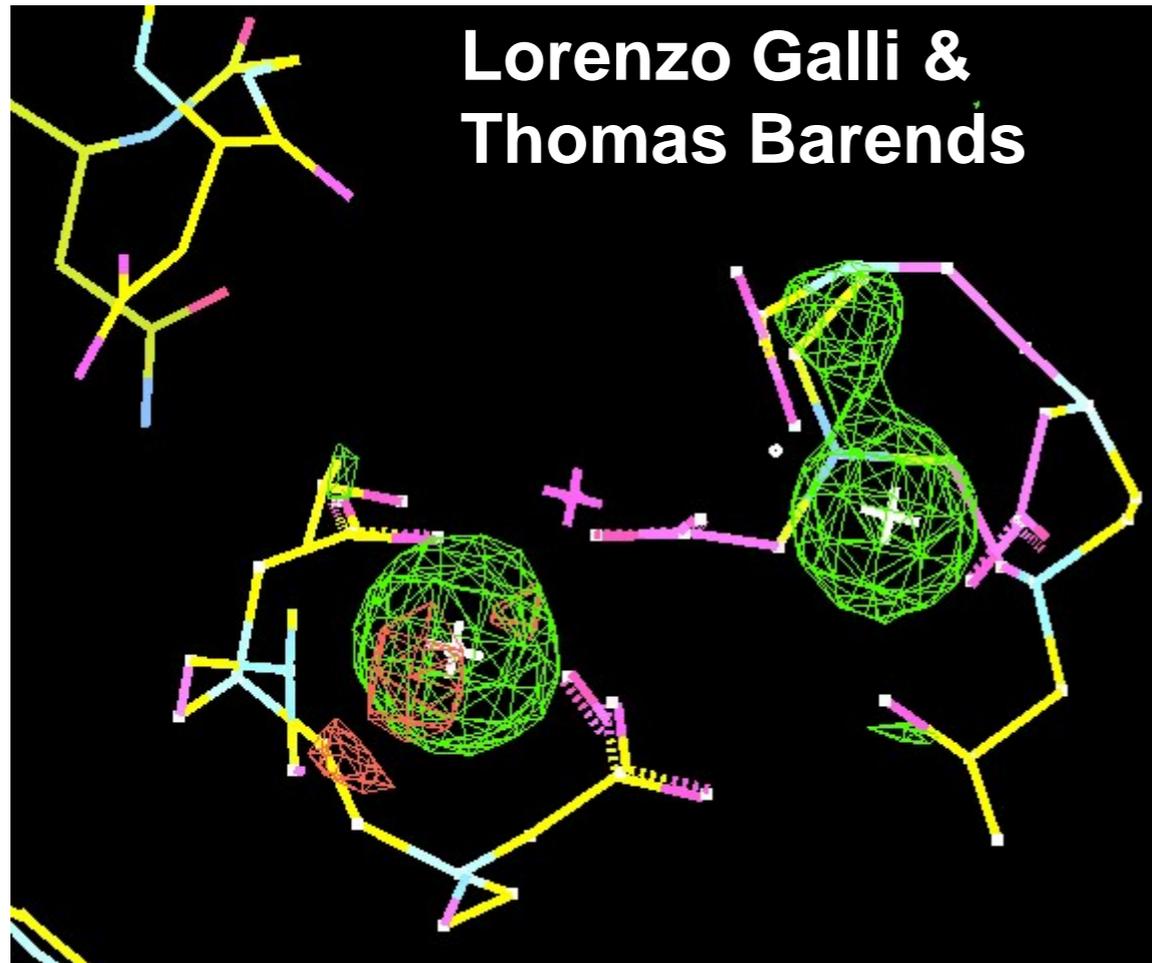
High intensity: ~20 GGy dose

Low intensity: ~2 GGy dose

Sample: Cathepsin B (Lars Redecke)

Analysis: **Lorenzo Galli** (CFEL) & Max Nanao (ESRF)

# The Gd electron density is reduced at high fluence



Red mesh: anomalous map at 5σ.  
Thomas Barends

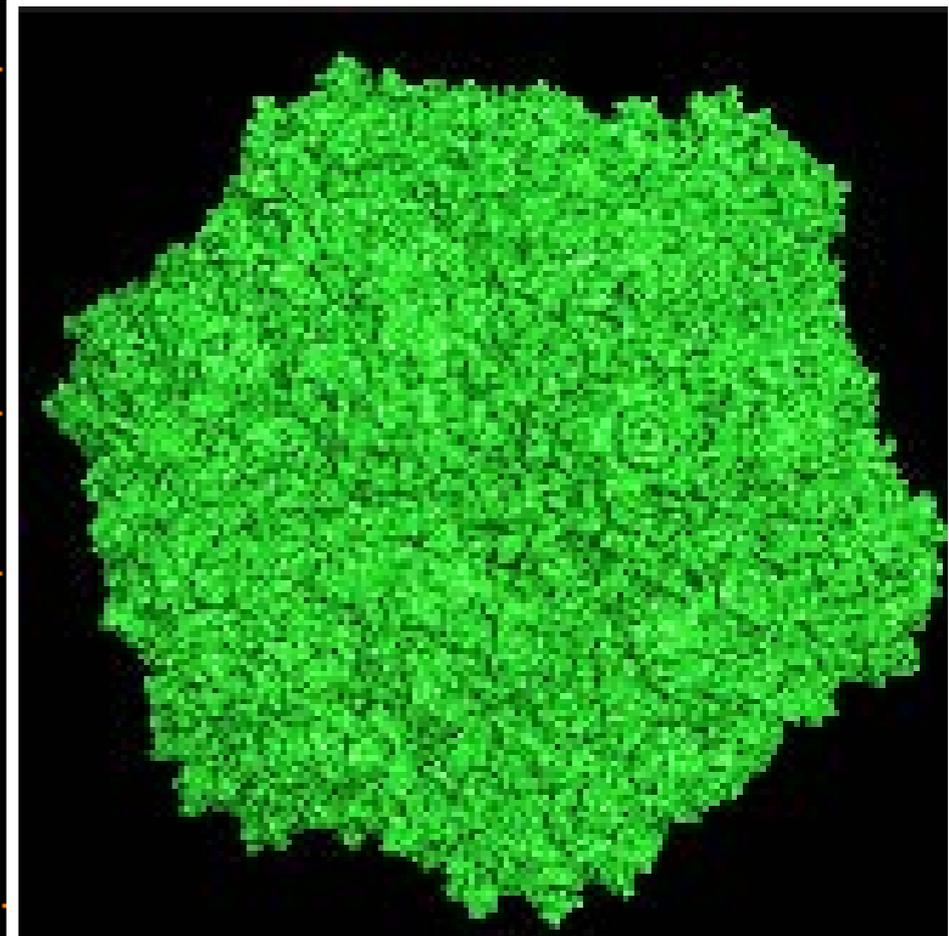
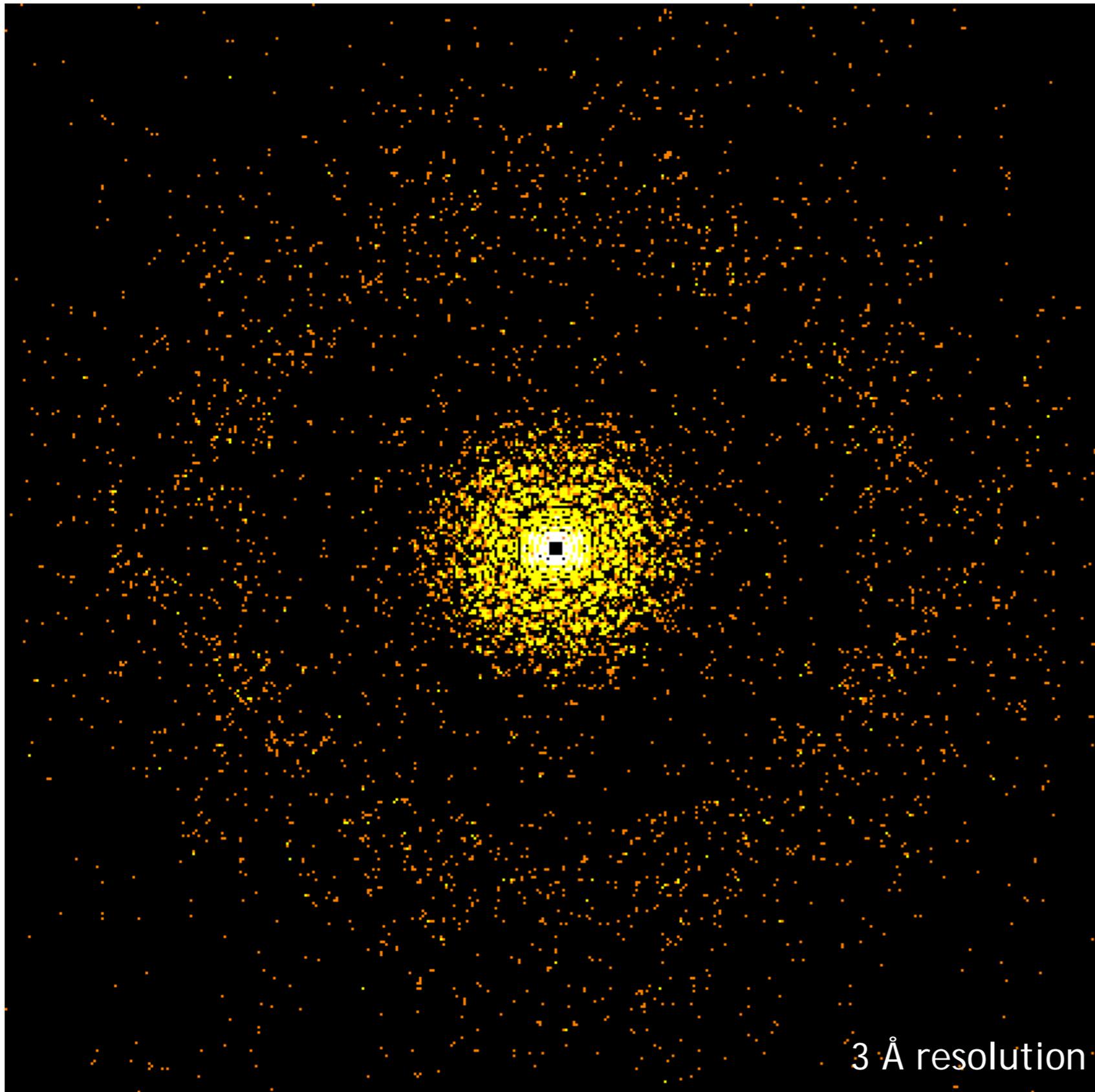
High fluence:  $10^{13}$  ph/ $\mu\text{m}^2$  (10 GGy)

Low fluence:  $2 \times 10^{11}$  ph/ $\mu\text{m}^2$  (200 MGy)

Difference: ~4 electrons in Gd (and surroundings)

see also Barends et al  
Nature **505** (2014)

# Atomic-resolution diffraction from single particles should be possible with $10^{14}$ ph/ $\mu\text{m}^2$



← 28 nm →

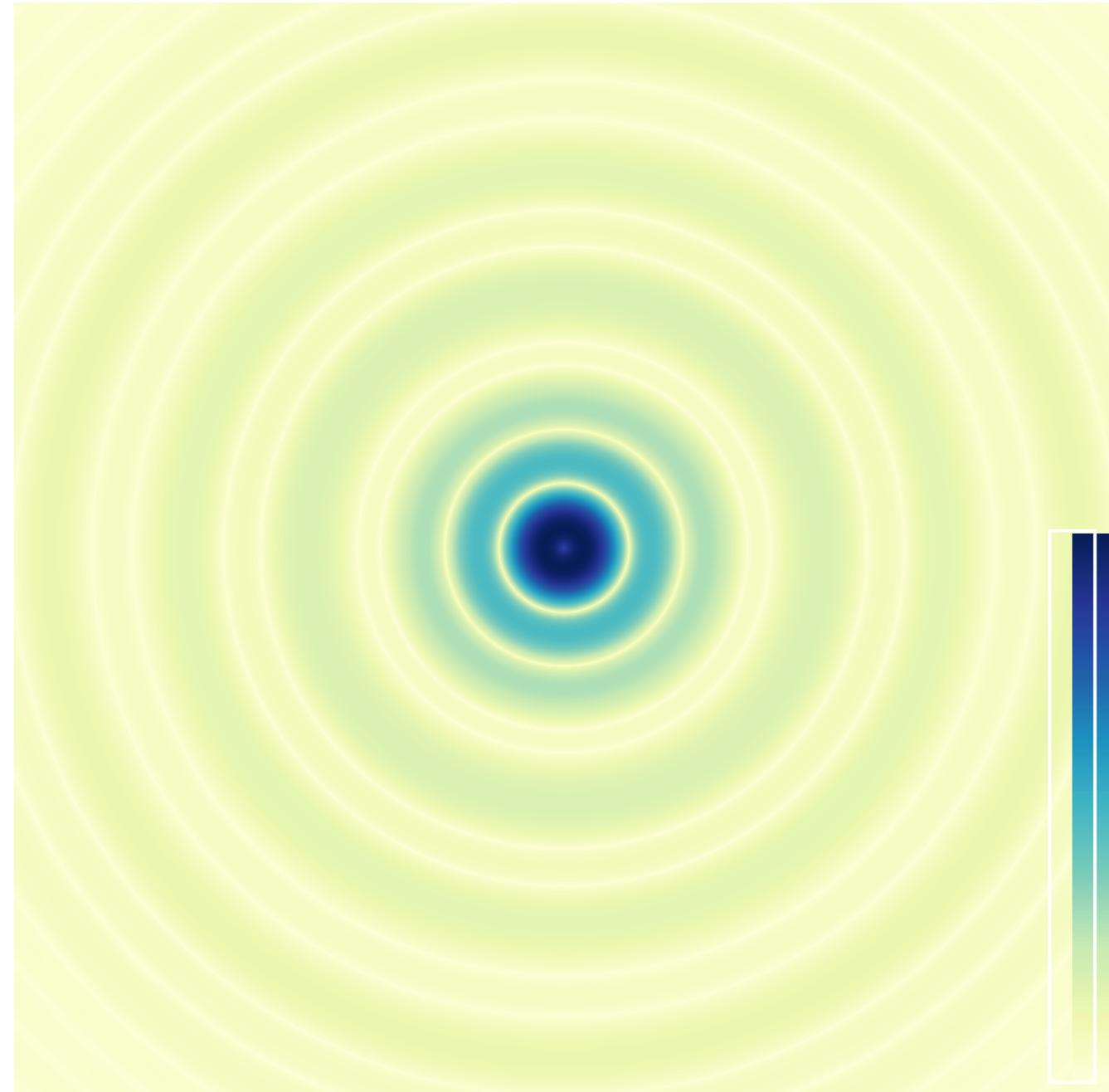
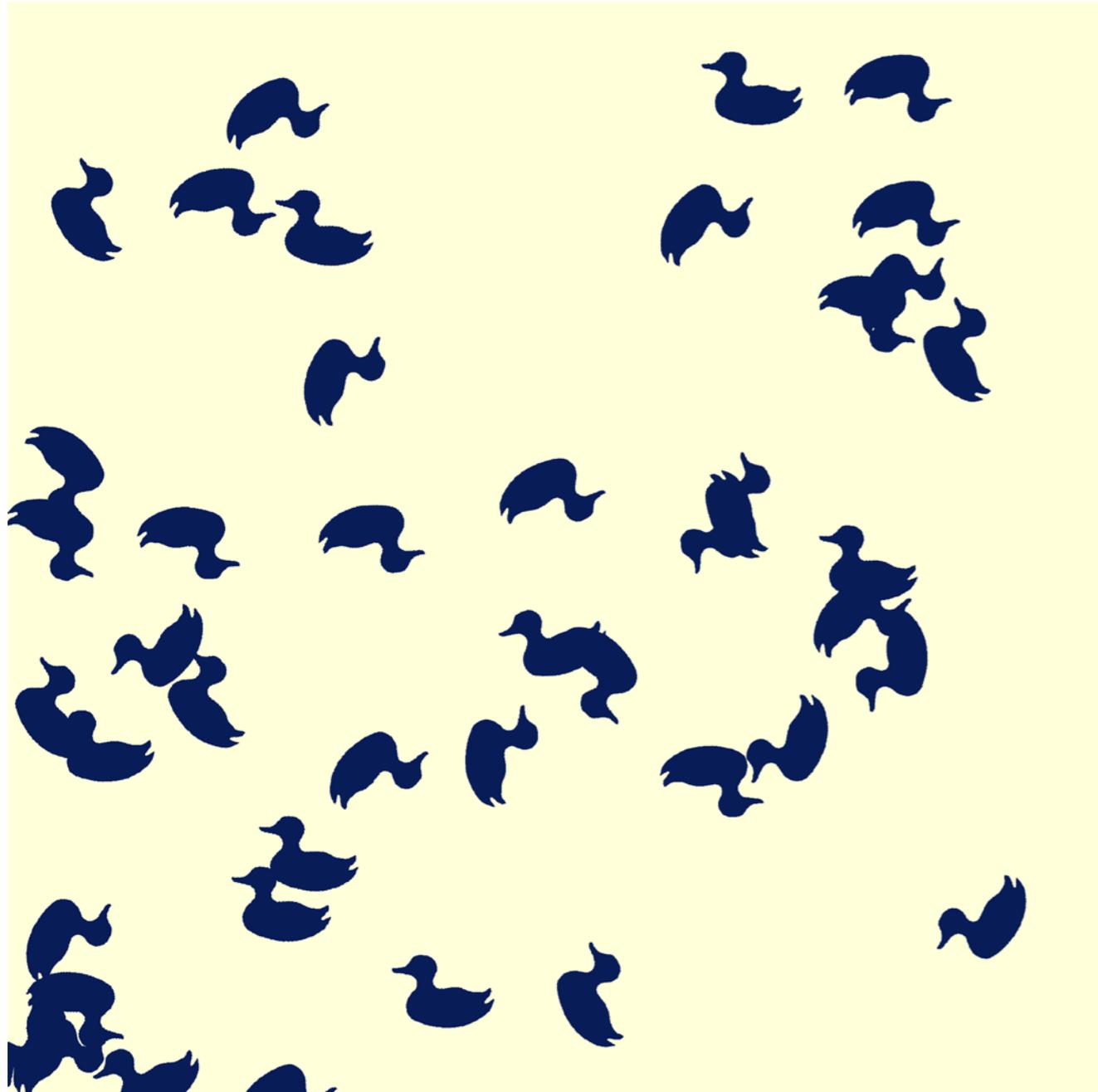
$10^{14}$  ph/ $\mu\text{m}^2$

60 GGy

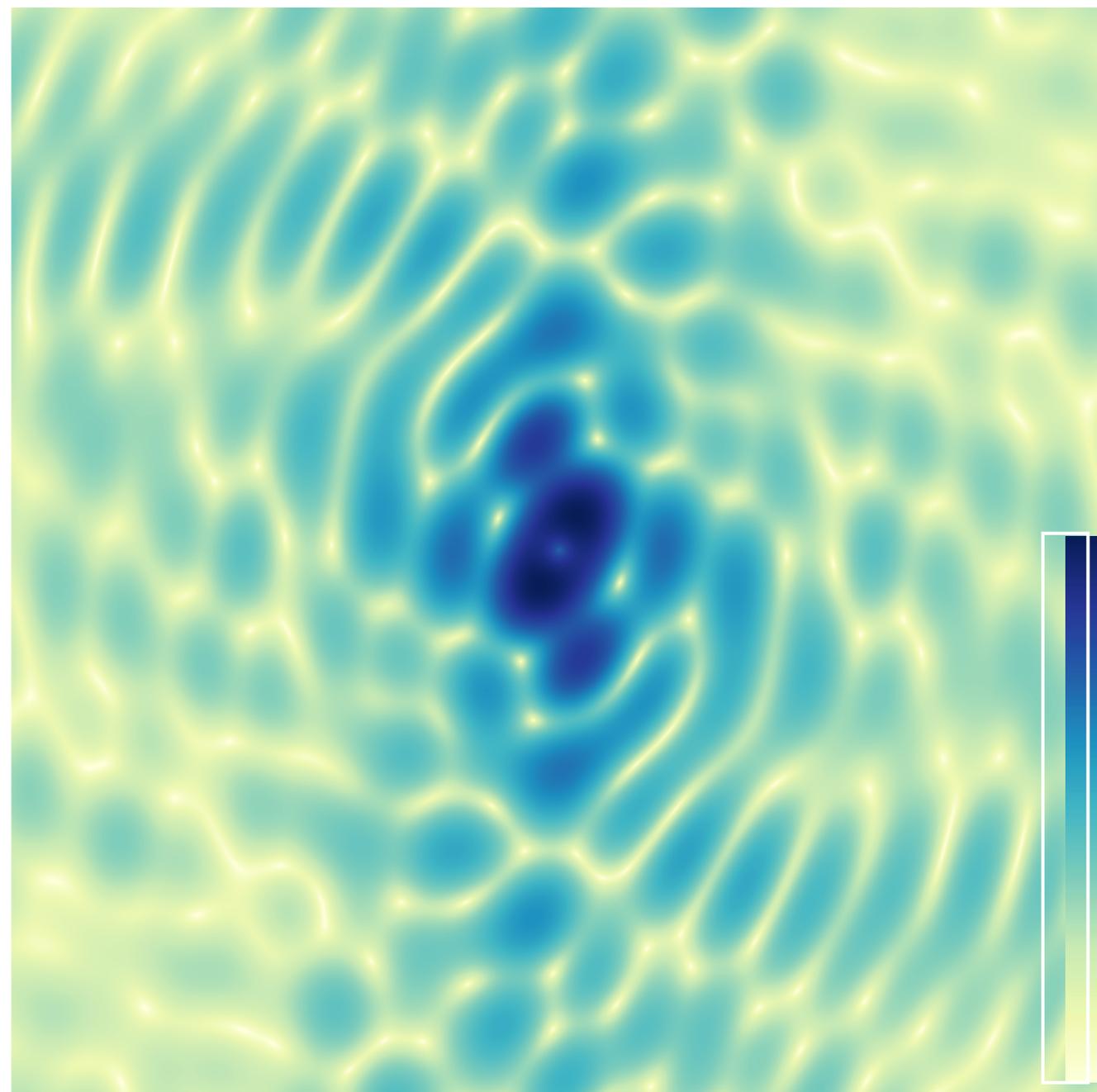
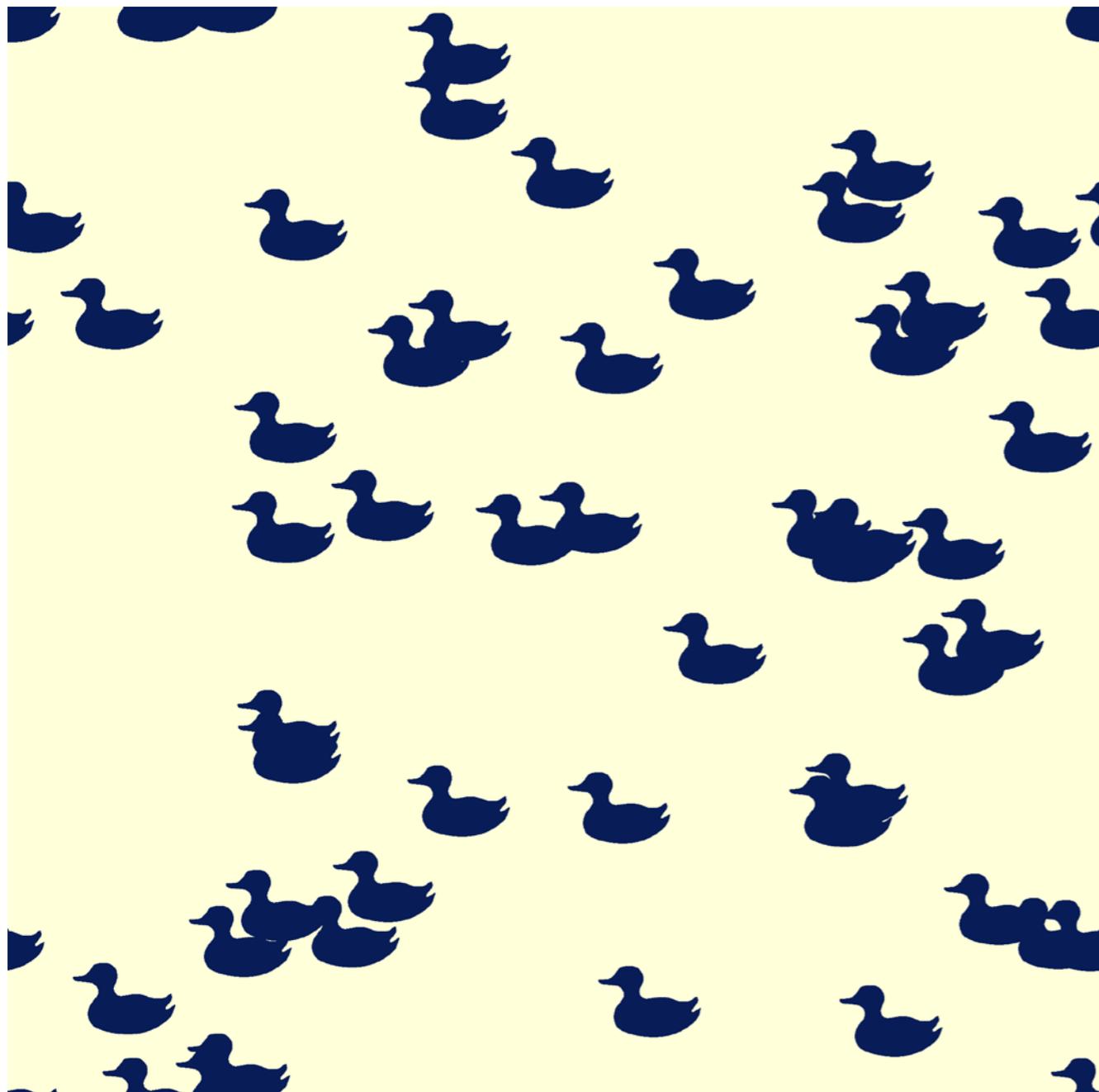
6000 MGy/fs  $\times$  10 fs

RMS displacement: 0.5 Å  
half electrons ionized

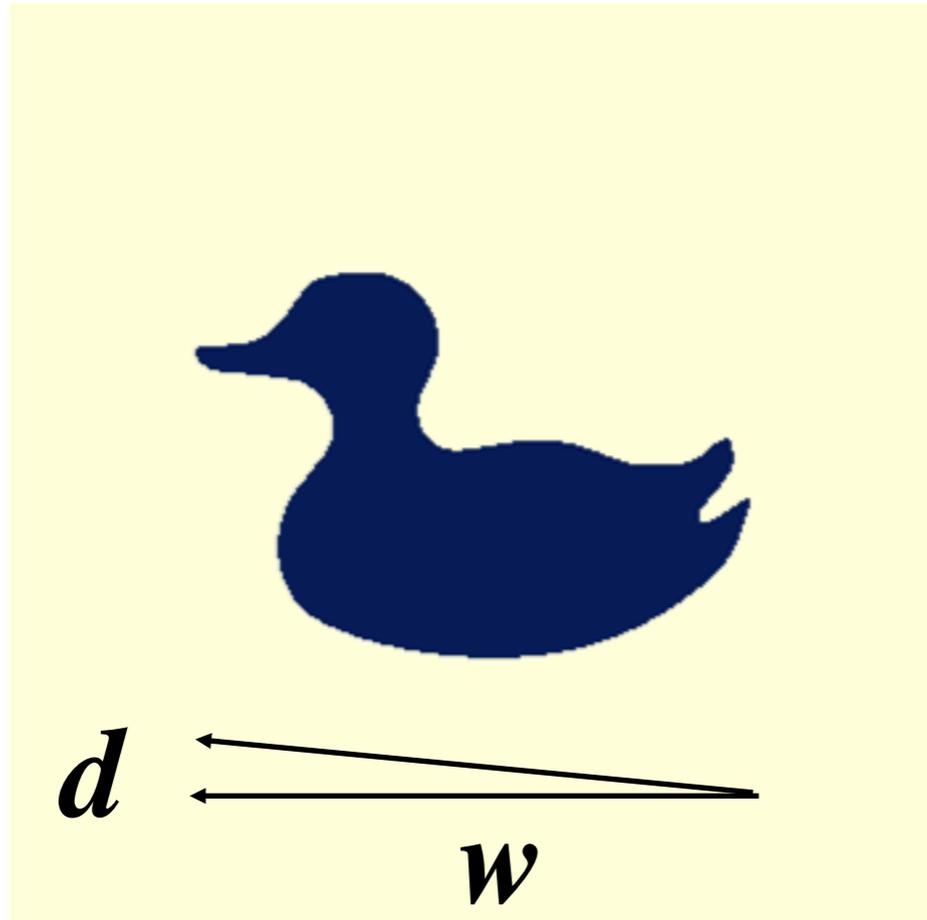
# Solution scattering gives single-molecule diffraction, but orientationally averaged



# Aligned molecules yield a single-molecule pattern



# How well aligned do you need?



$$\Delta\phi = d/w$$

photosystem II

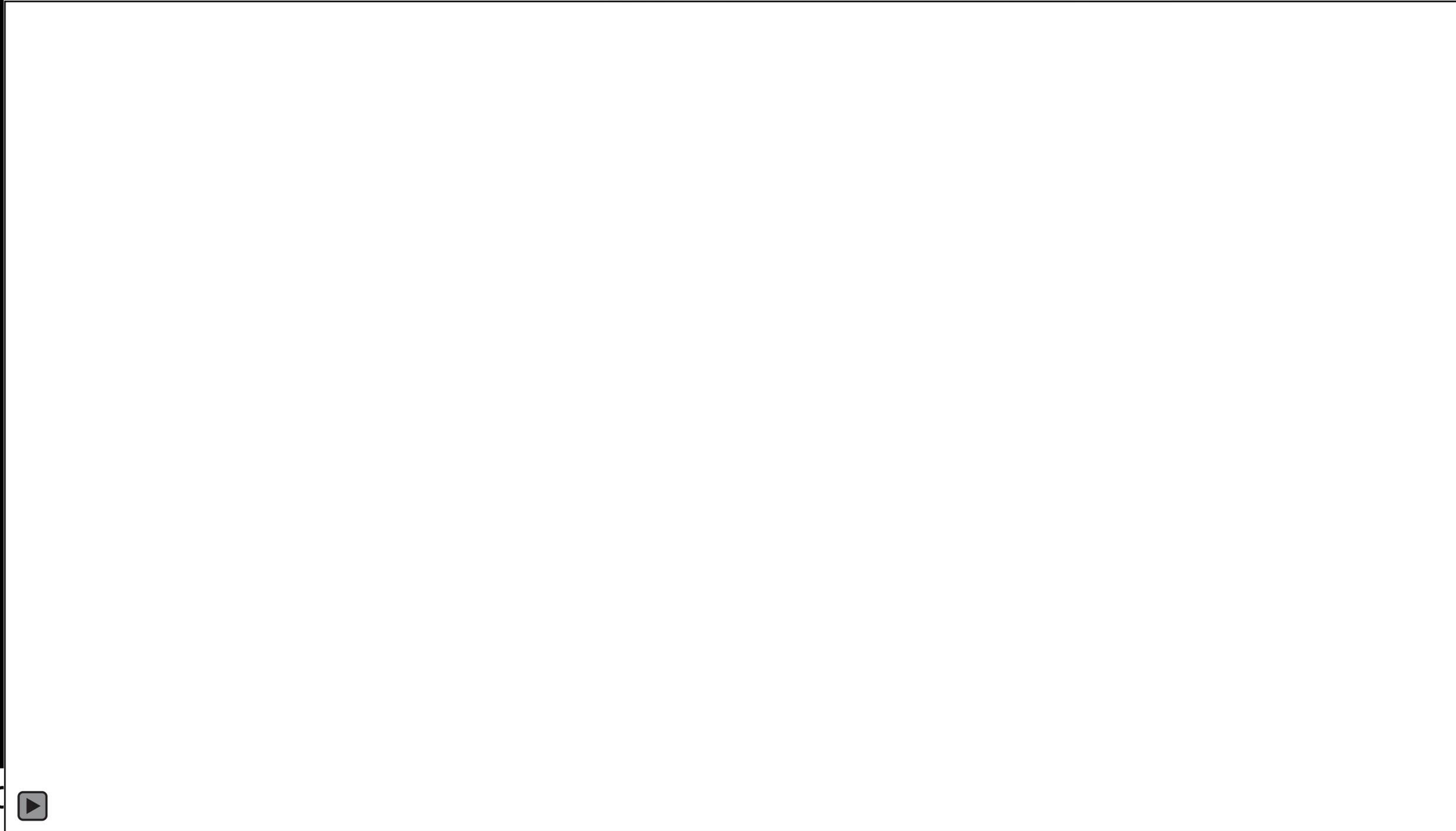


$$d = 3 \text{ \AA}$$

$$w = 160 \text{ \AA}$$

$$\Delta\phi = 1.1^\circ$$

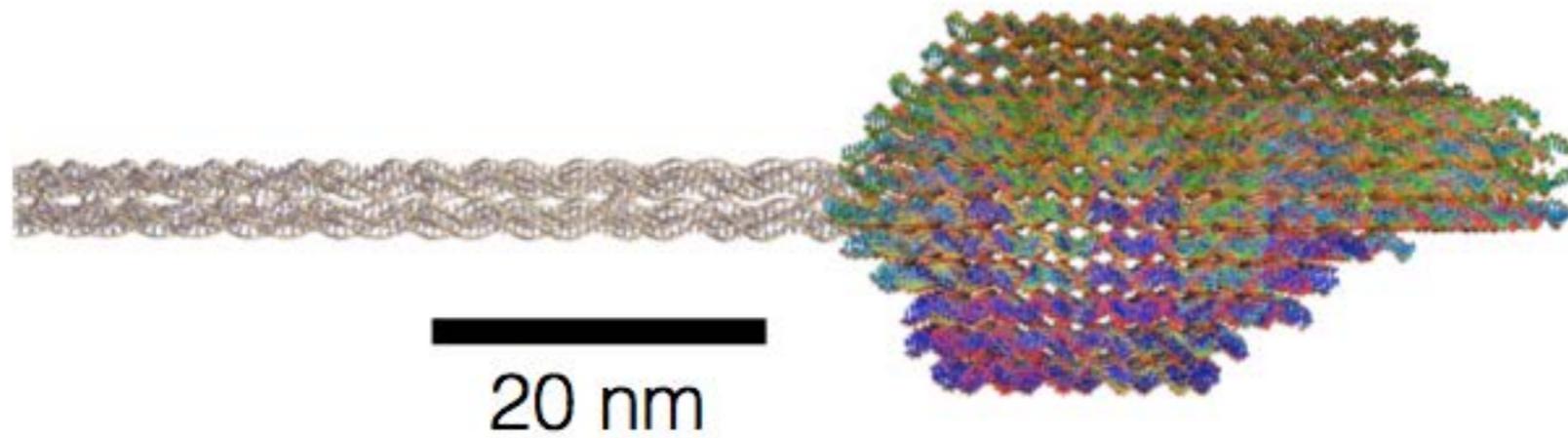
# Needle-like objects align in the jet



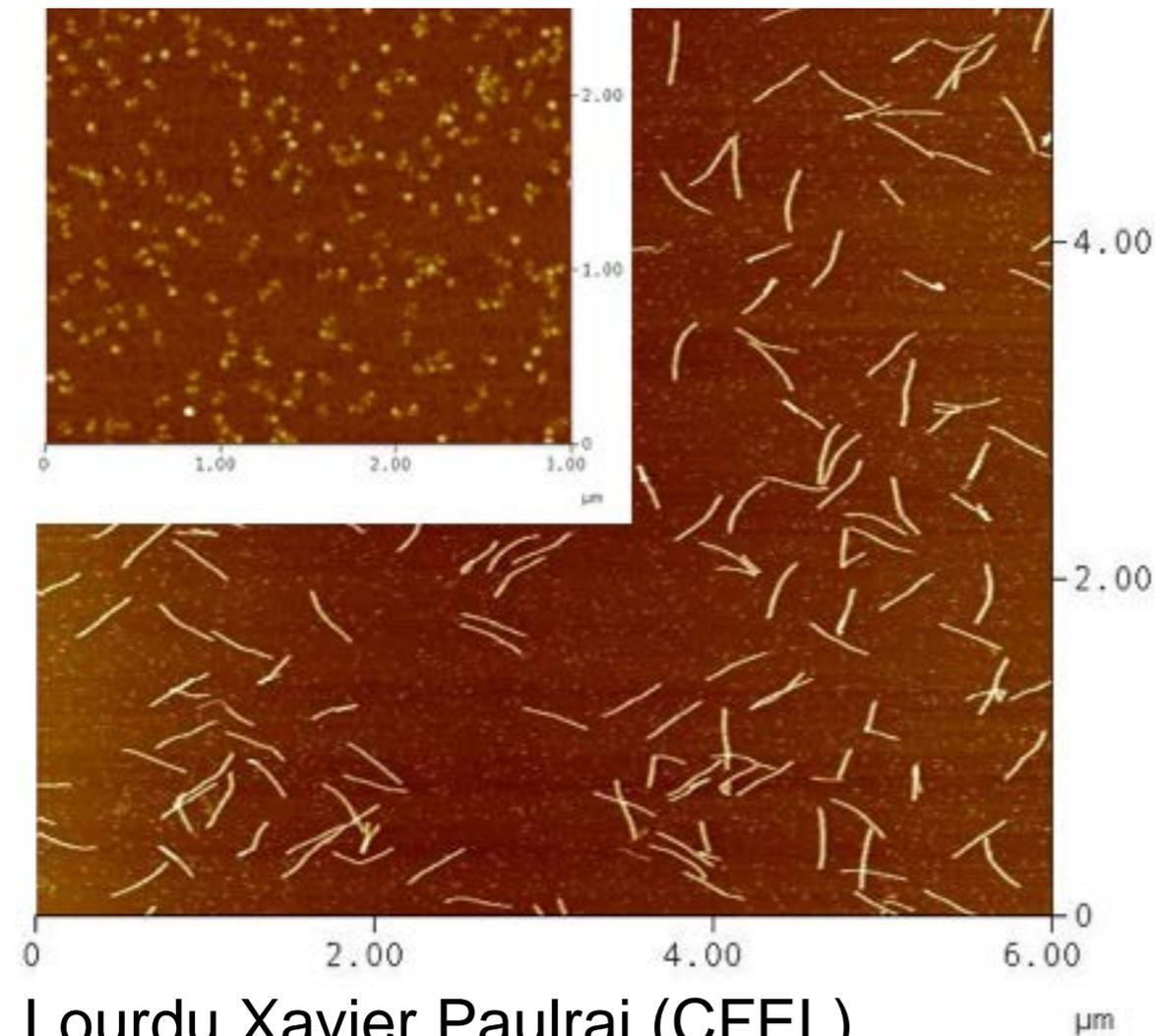
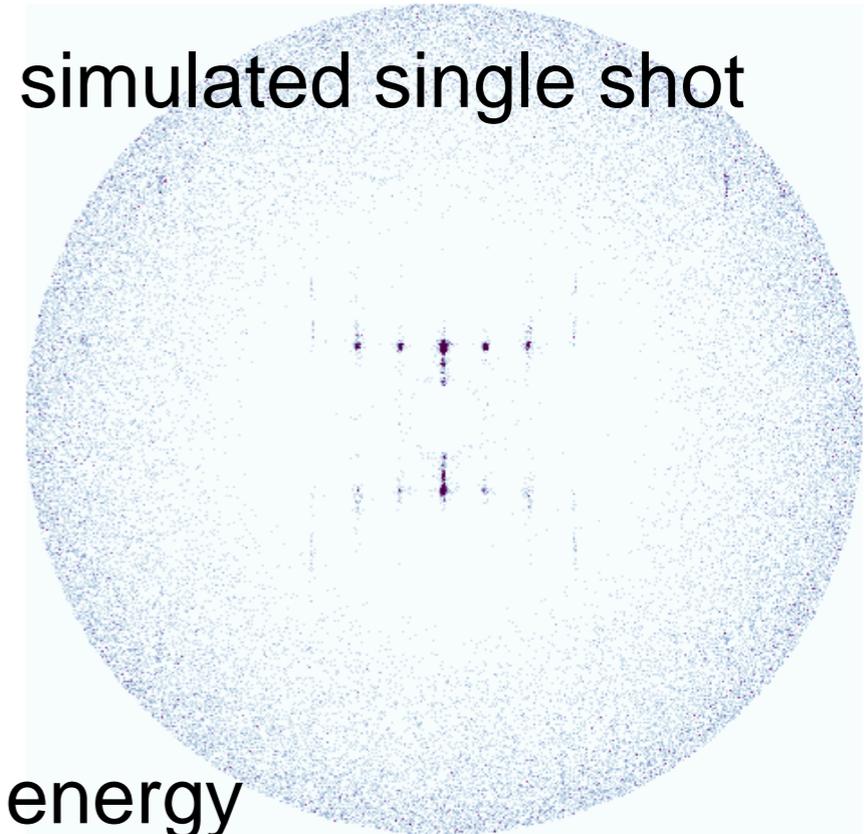
Gas foc 

Dan Deponate ASU

# Adding DNA “kite tails” may align arbitrarily-shaped molecules

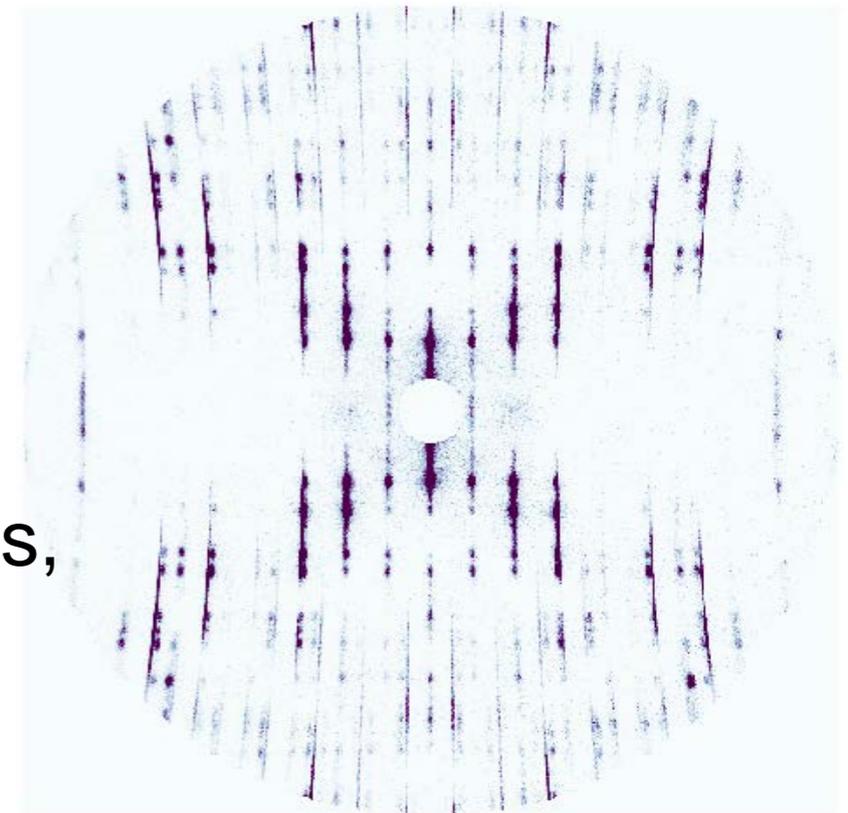


simulated single shot



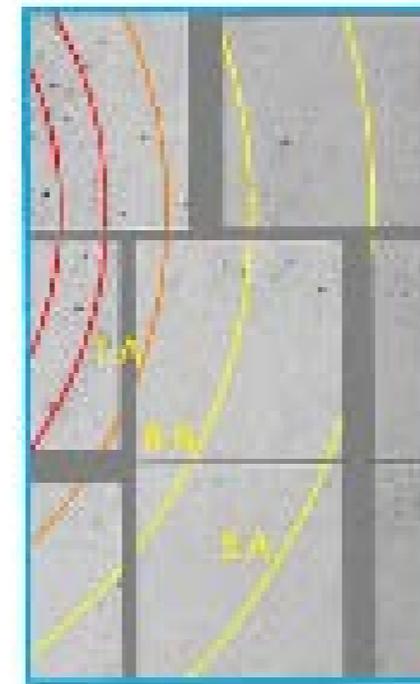
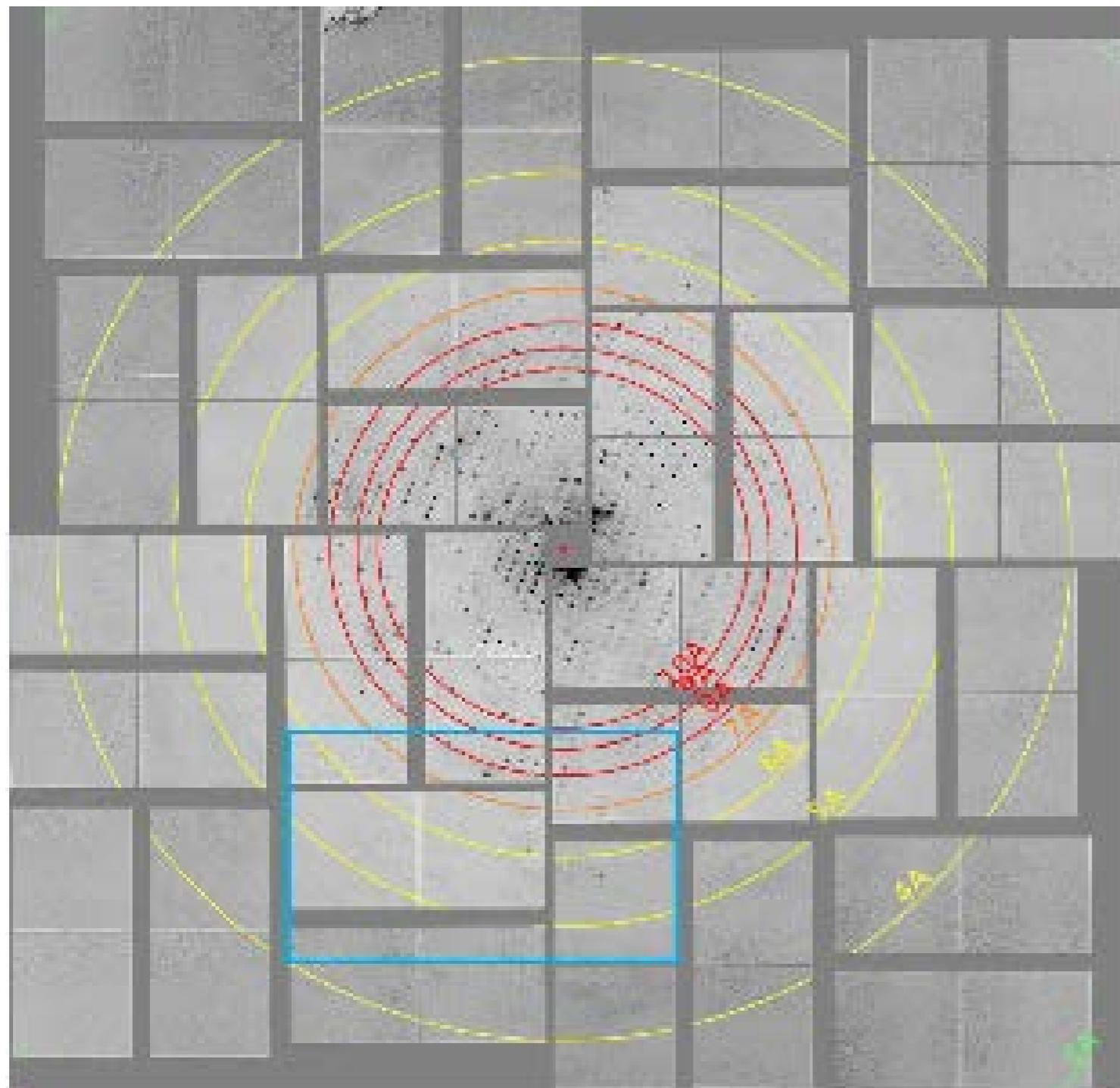
6 keV photon energy  
 $10^{12}$  ph/ $\mu\text{m}^2$   
(1 GGy)

simulated  
1000 shots,  
axially  
aligned



Lourdu Xavier Paulraj (CFEL)  
Ned Seeman (NYU)

# Even bad crystals should attain the required level of alignment



$$d = 2\pi\sqrt{\langle D^2 \rangle}$$

$$d = 5\text{\AA}$$

$$\sqrt{\langle D^2 \rangle} = 0.8\text{\AA}$$

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Galli



Valerio  
Mariani



Tom  
White



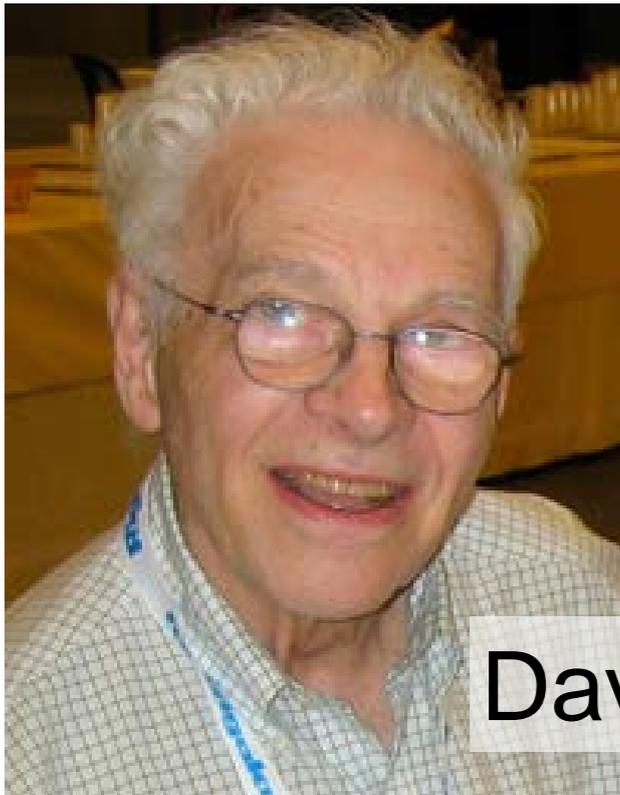
European Research Council  
Established by the European Commission



Bundesministerium  
für Bildung  
und Forschung



# Phasing diffraction of periodic structures is challenging because of the information deficit



David Sayre

*Acta Cryst.* (1952). **5**, 843

**Some implications of a theorem due to Shannon.** By D. SAYRE, *Johnson Foundation for Medical Physics, University of Pennsylvania, Philadelphia 4, Pennsylvania, U. S. A.*

(Received 3 July 1952)

Shannon (1949), in the field of communication theory, has given the following theorem: If a function  $d(x)$  is known to vanish outside the points  $x = \pm a/2$ , then its Fourier transform  $F(X)$  is completely specified by the values which it assumes at the points  $X = 0, \pm 1/a, \pm 2/a, \dots$ . In fact, the continuous  $F(X)$  may be filled in merely by laying down the function  $\sin \pi a X / \pi a X$  at each of the above points, with weight equal to the value of  $F(X)$  at that point, and adding.

Now the electron-density function  $d(x)$  describing a single unit cell of a crystal vanishes outside the points  $x = \pm a/2$ , where  $a$  is the length of the cell. The reciprocal-lattice points are at  $X = 0, \pm 1/a, \pm 2/a, \dots$ , and hence the experimentally observable values of  $F(X)$  would suffice, by the theorem, to determine  $F(X)$  everywhere, if the phases were known. (In principle, the necessary points extend indefinitely in reciprocal space, but by using, say, Gaussian atoms both  $d(x)$  and  $F(X)$  can be effectively confined to the unit cell and the observable region, respectively.)

For centrosymmetrical structures, to be able to fill in the  $|F|^2$  function would suffice to yield the structure, for sign changes could occur only at the points where  $|F|^2$  vanishes. The structure corresponding to the  $|F|^2$  function is the Patterson of a single unit cell. This has

twice the width of the unit cell, and hence to fill in the  $|F|^2$  function would require knowledge of  $|F|^2$  at the half-integral, as well as the integral  $h$ 's. This is equivalent to a statement made by Gay (1951).

I think the conclusions which may be stated at this point are:

1. Direct structure determination, for centrosymmetric structures, could be accomplished as well by finding the sizes of the  $|F|^2$  at half-integral  $h$  as by the usual procedure of finding the signs of the  $F$ 's at integral  $h$ .

2. In work like that of Boyes-Watson, Davidson & Perutz (1947) on haemoglobin, where  $|F|^2$  was observed at non-integral  $h$ , it would suffice to have only the values at half-integral  $h$ .

The extension to three dimensions is obvious.

#### References

- BOYES-WATSON, J., DAVIDSON, E. & PERUTZ, M. F. (1947). *Proc. Roy. Soc. A*, **191**, 83.  
GAY, R. (1951). Paper presented at the Second International Congress of Crystallography, Stockholm.  
SHANNON, C. E. (1949). *Proc. Inst. Radio Engrs., N.Y.* **37**, 10.

Current phasing methods for crystal diffraction:

- Molecular replacement
- Anomalous diffraction
- Isomorphous replacement (and things like RIP)
- Direct methods (atomic resolution)
- Density modification