

Topological Insulators and Quantum Anomalous Hall Effect

Qi-Kun Xue

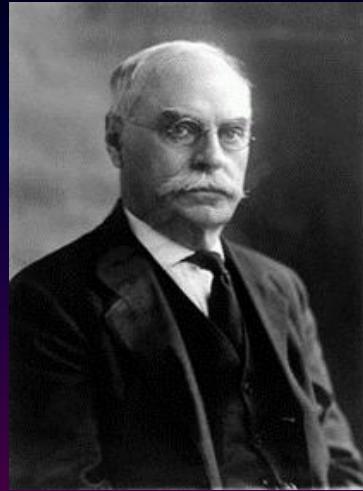
Tsinghua University



OUTLINE

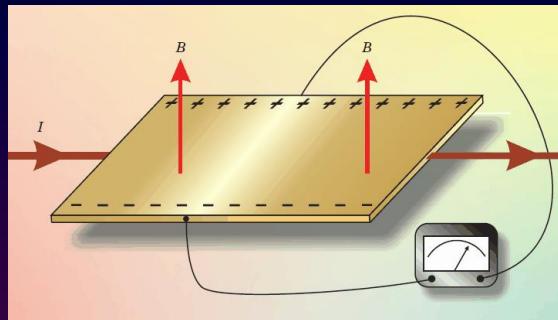
- Introduction
- MBE-STM-ARPES of topological insulators
- Realization of Quantum Anomalous Hall Effect
- Summary

Hall Effect and Anomalous Hall Effect

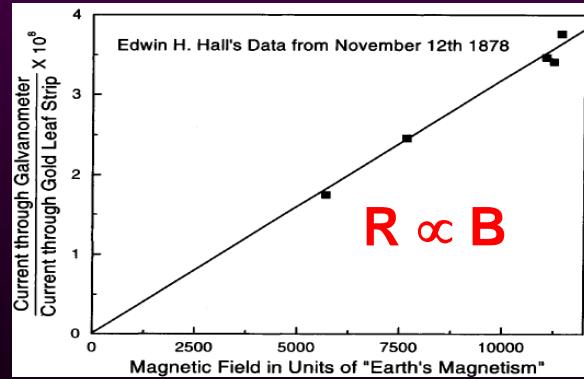


Hall Effect: 1879

(non-magnetic materials)



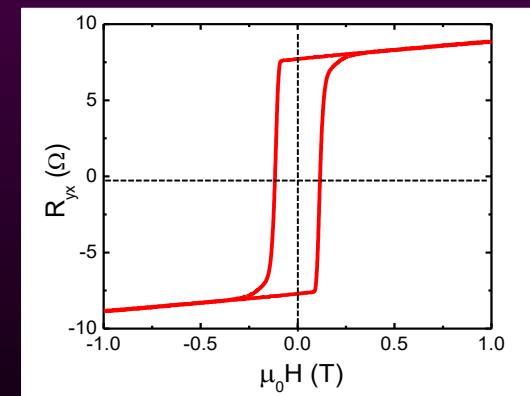
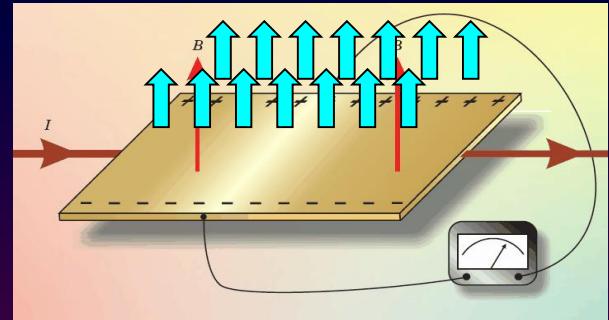
Edwin H. Hall



Linear dependence

Anomalous Hall Effect: 1881

(magnetic materials)



Magnetic property

Anomalous Hall Effect: Mechanism

*Nagaosa, Sinova, Onoda, MacDonald, Ong,
Review of Modern Physics 2009*

$$\sigma_{\text{AH}} = (\sigma_{\text{int}} + \sigma_{\text{sk}} + \sigma_{\text{sj}})$$

Spin-orbit coupling: intrinsic

R. Karplus, J. M. Luttinger, Phys. Rev. 95, 1154 (1954)

$$\rho_{\text{int}} \propto \rho_{xx}^2$$

Skew scattering: extrinsic

J. Smit, Physica 24, 39 (1958)

$$\rho_{\text{sk}} \propto \rho_{xx}$$

Side jump: extrinsic

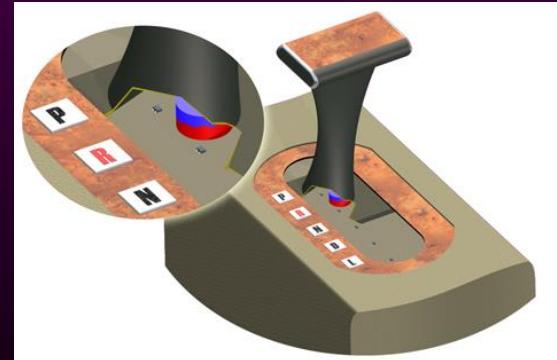
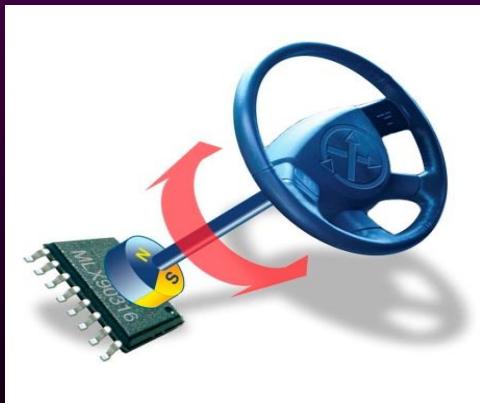
L. Berger, Phys. Rev. B2, 4559 (1970)

$$\rho_{\text{sj}} \propto \rho_{xx}^2$$

Applications



Hall effect
+ IC

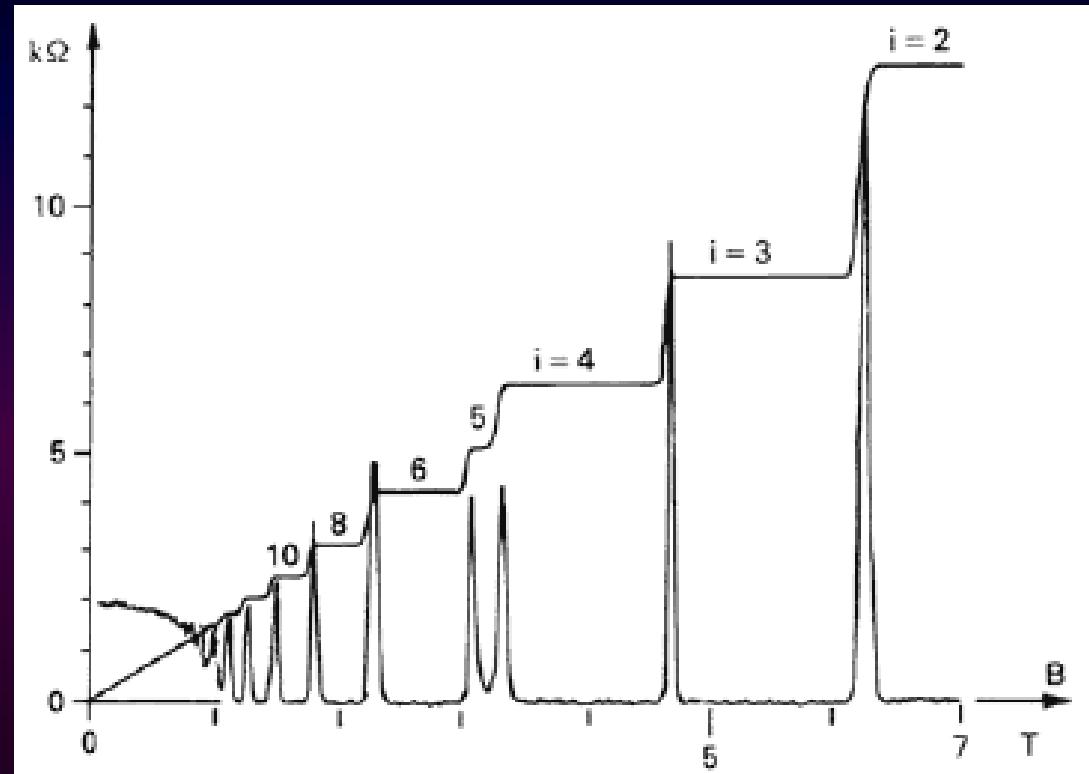


H



Integer Quantum Hall Effect (1980)

2D electron gas



Klaus von Klitzing

$$\rho_{xy} = h / ie^2$$
$$\rho_{xx} = 0$$



Tsui

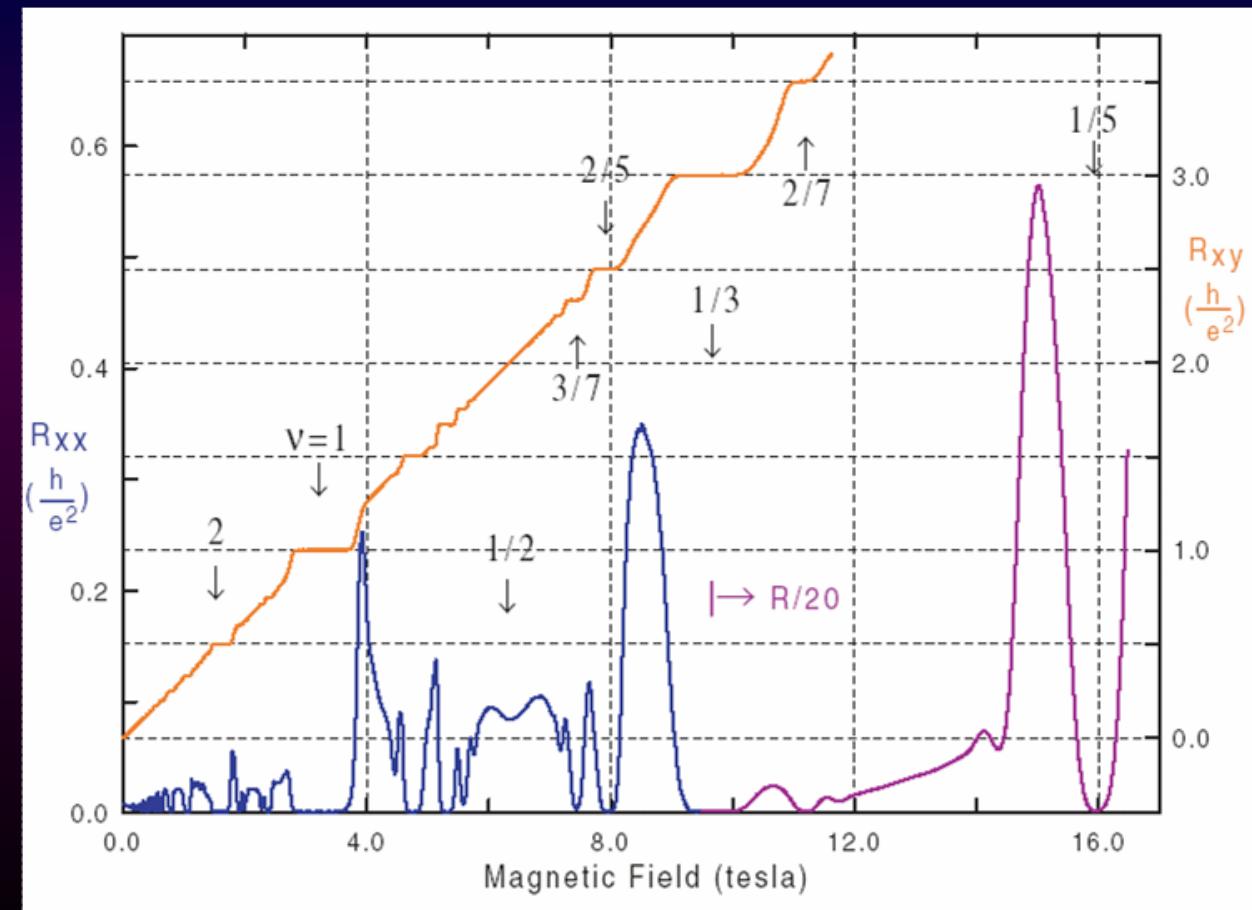


Stormer

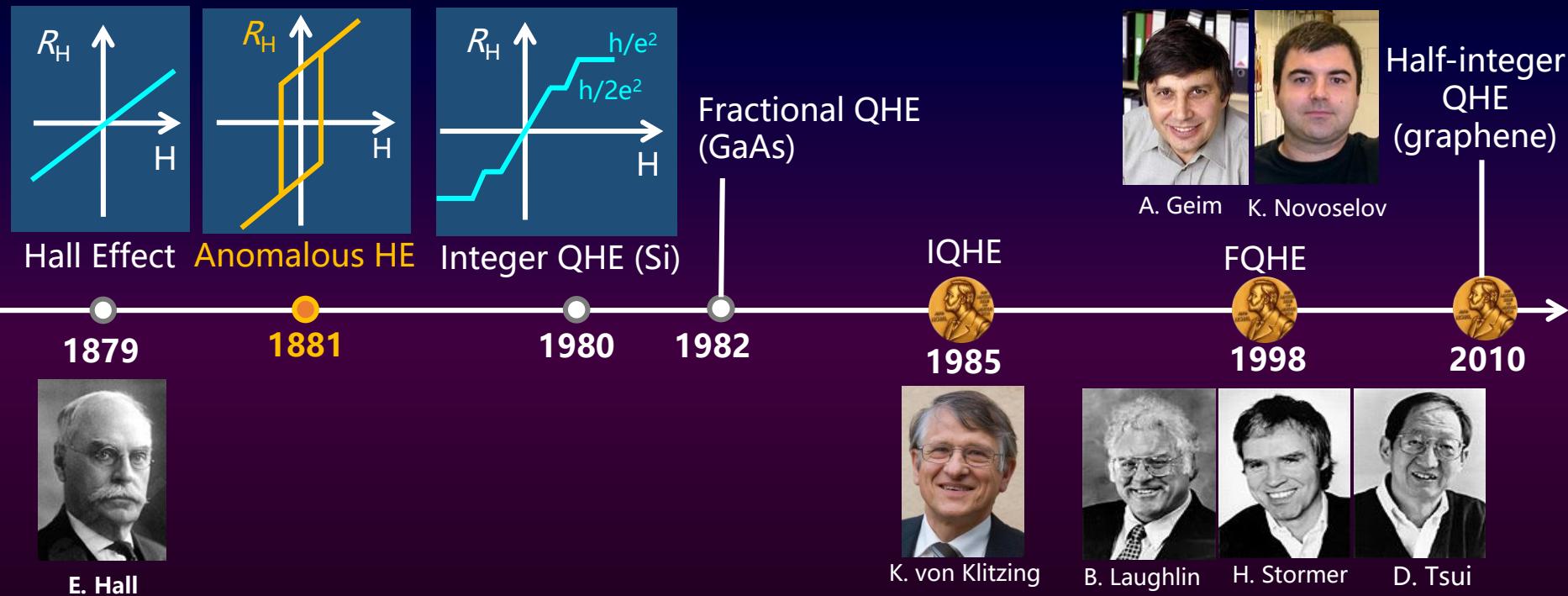


Laughlin

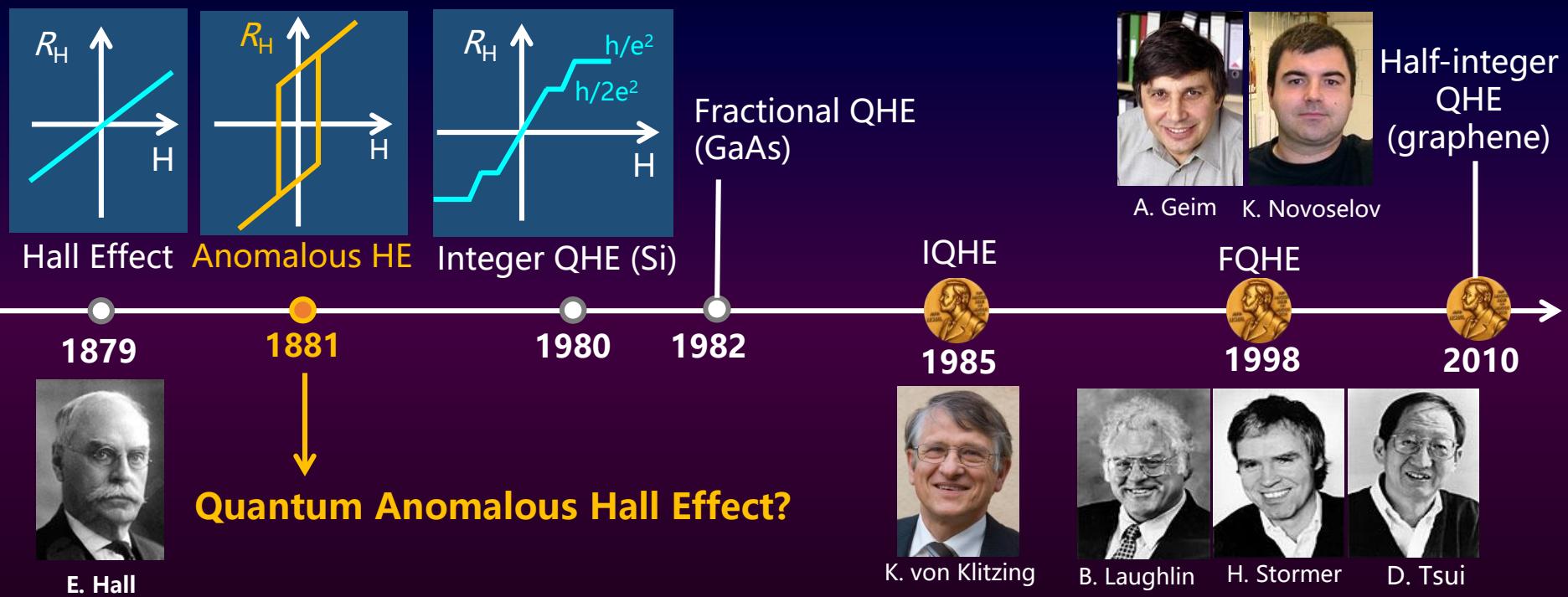
Fractional Quantum Hall Effect (1982)



From Hall Effect to Quantum Hall Effects (QHE)



From Hall Effect to Quantum Hall Effects (QHE)



The first Theoretical Proposal for Quantum Hall Effect without Magnetic Field

VOLUME 61, NUMBER 18

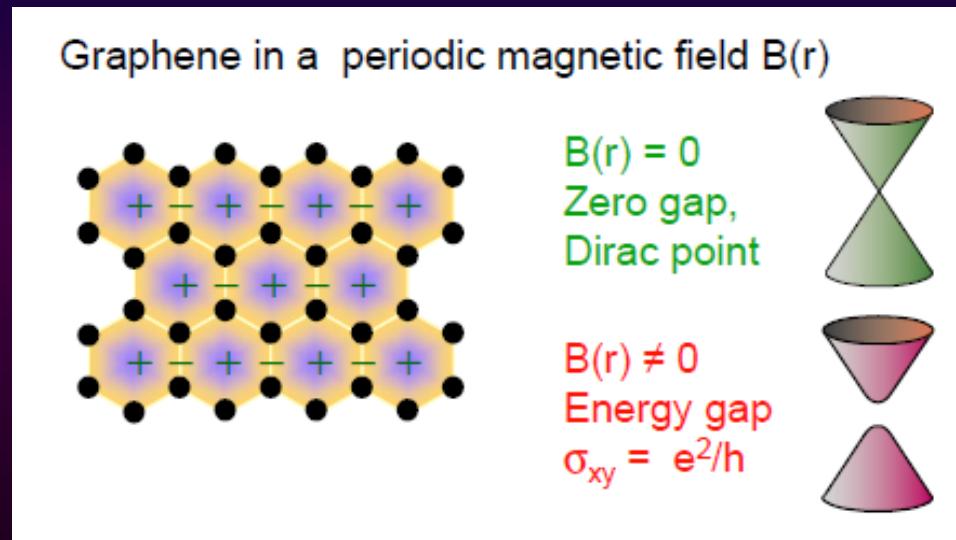
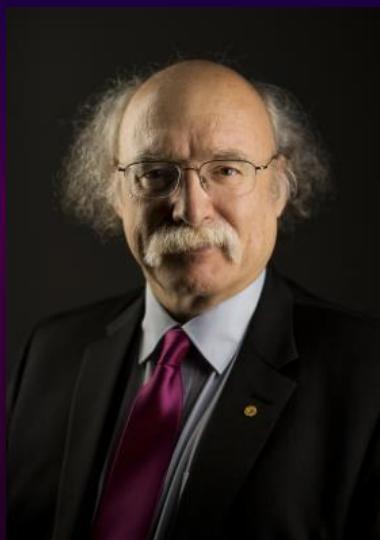
PHYSICAL REVIEW LETTERS

31 OCTOBER 1988

Model for a Quantum Hall Effect without Landau Levels: Condensed-Matter Realization of the “Parity Anomaly”

F. D. M. Haldane

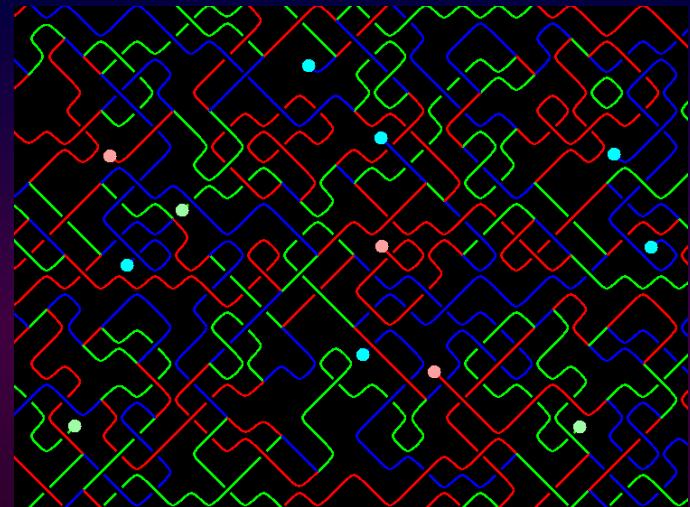
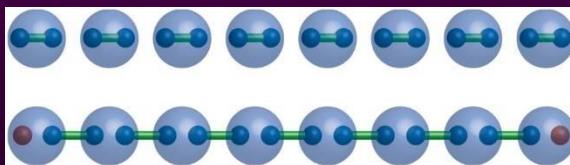
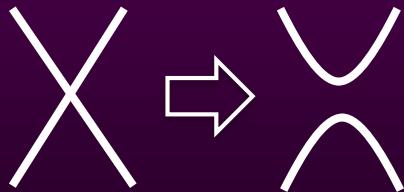
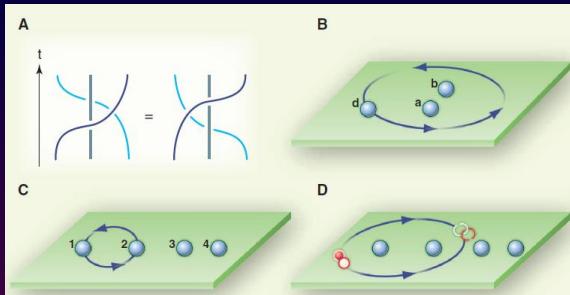
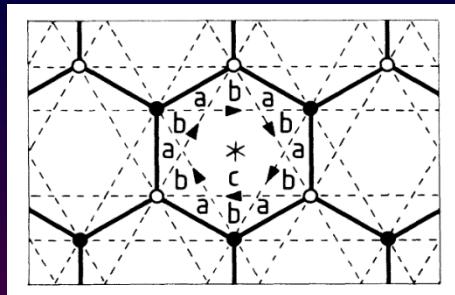
Graphene with broken TRS



- Haldane conceived a model that will show QHE in zero magnetic field, it is now called the “Chern insulator”
- It is very abstract and way ahead of its time, but it is highly influential about 20 years later in the field of topological insulators

Topological States of Matter

Quantum anomalous Hall effect, Haldane phase, Non-abelion anyons, Topological order, String-net condensation.....



Zoo of quantum-topological phases of matter

X. –G. Wen Rev. Mod. Phys. 89, 041004 (2017)



Haldane



X.-G. Wen



S.-C Zhang



Kitaev



Moore



Read

...

Topology



$\chi = 2$

$\chi = 0$

$$\frac{1}{2\pi} \oint_S K dA = \chi$$

K : Gauss curvature

χ : Euler number

Gauss-Bonnet theorem

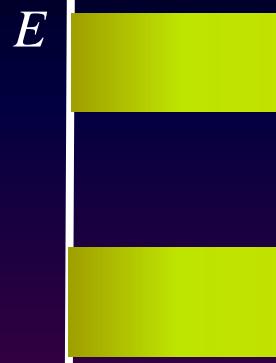


Gauss



Bonnet

Topological property of the electronic structure of a 2D insulator

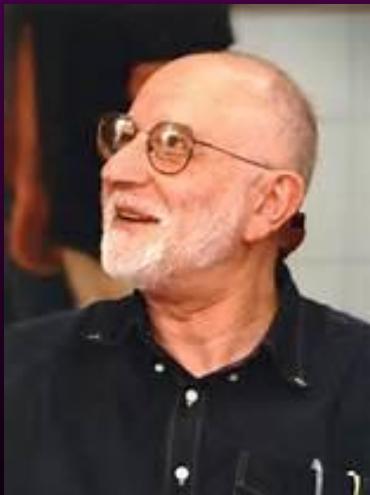


$C = 0$

$C = 1$



“TKNN”
T: Thouless
Nobel laureate
in Physics 2016



Berry



Chern

$$\frac{1}{2\pi} \oint_{BZ} \Omega d\mathbf{k} = C$$

Ω : Berry's curvature

C : Chern number

2005: Topological Insulators



Topological Insulators (2005—)

Hasan & Kane: Rev. Mod. Phys. 2010

Qi & Zhang: Rev. Mod. Phys. 2011



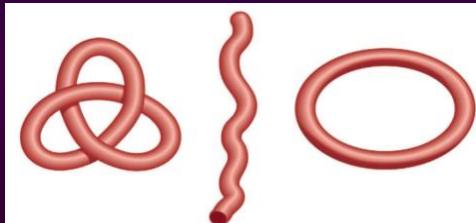
Quantum Anomalous Hall Effect

Quantum Spin Hall Effect

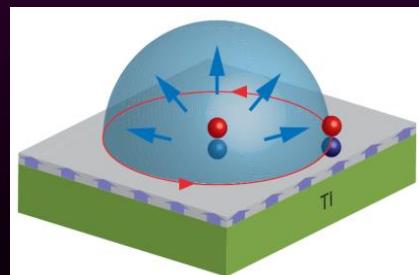
Majorana Fermions

Magnetic Monopole and Dyon

TME Effect and Axion

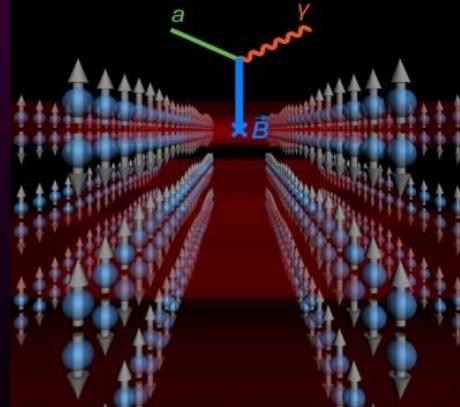


J. Moore, Nature 2010



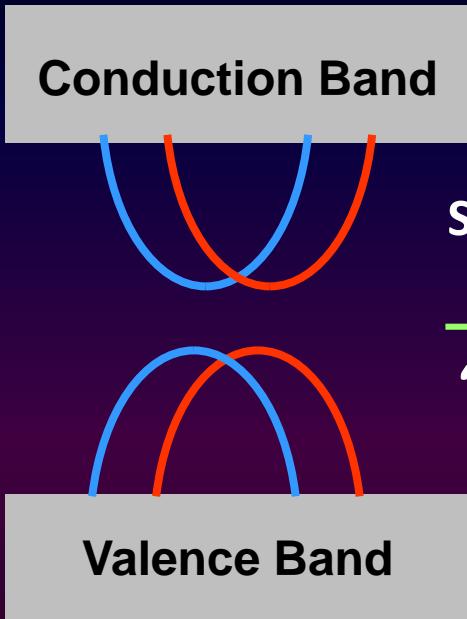
Qi & Zhang, Science 2009

Dark matter on
desktop
Wilczek, Nature 2009



Ordinary versus Topological Insulators

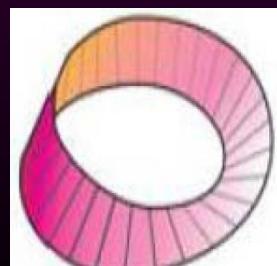
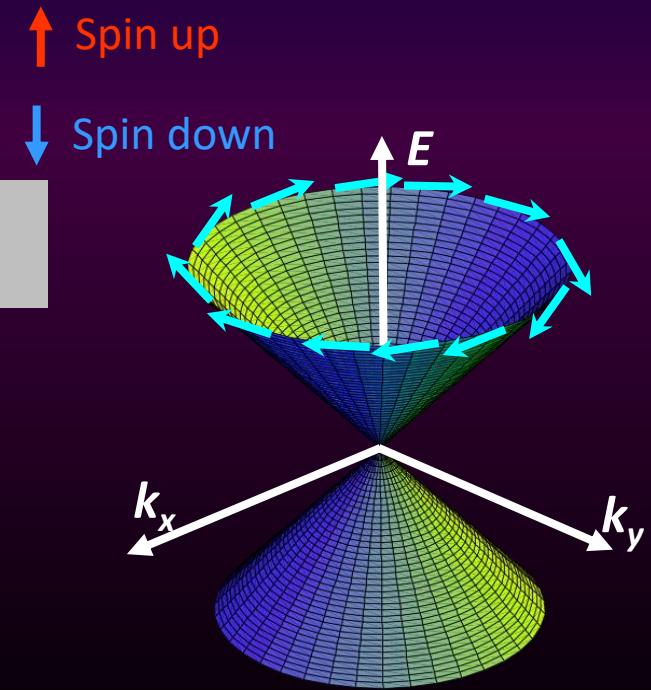
Ordinary Insulator



Topological Insulator



$$H = c \vec{\alpha} \bullet \vec{p} + mc^2 \beta$$
$$H = c \vec{\sigma} \bullet \vec{p} \quad (m=0)$$



Classification of Materials (new)

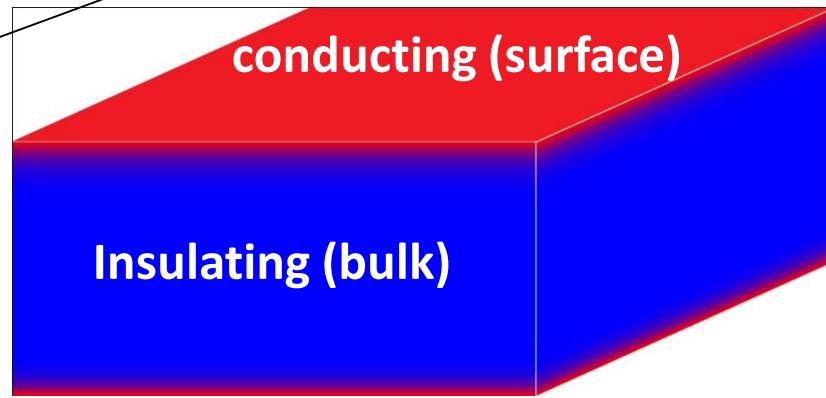
Conductor



Topological
Insulator

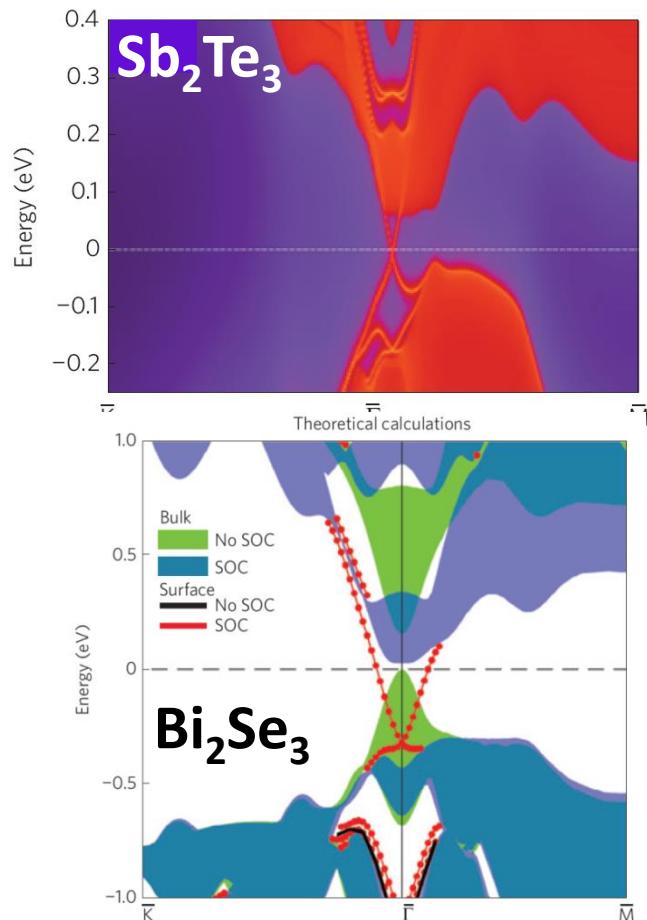


Insulator



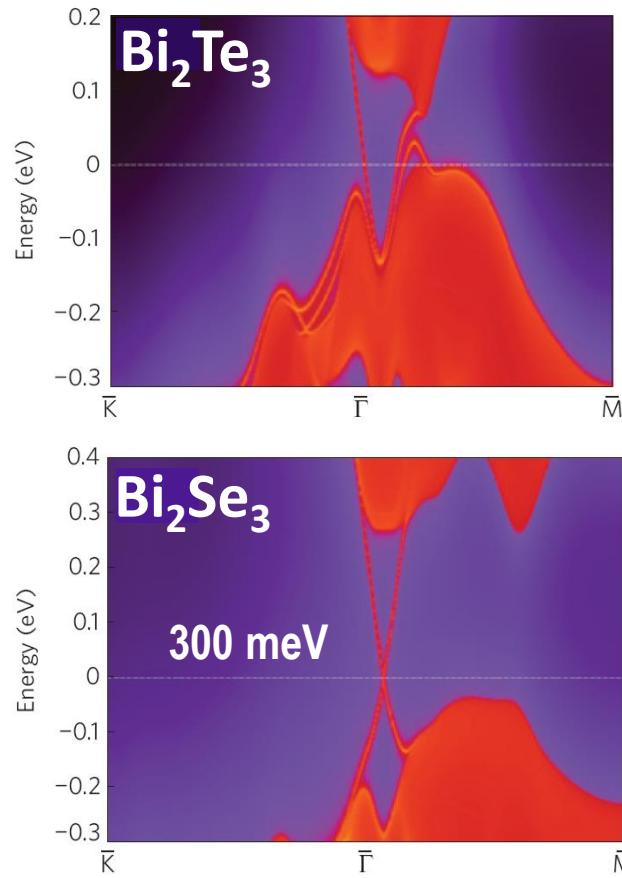
Spin-Orbital
Coupling

3D Topological Insulators: Bi_2Se_3 , Bi_2Te_3 , Sb_2Te_3



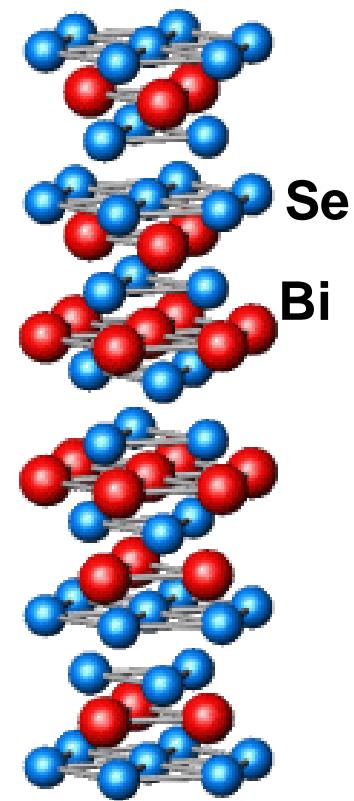
Xia et al., Nat. Phys. 5, 398 (2009)

Hasan group



Zhang et al., Nat. Phys. 5, 438 (2009)

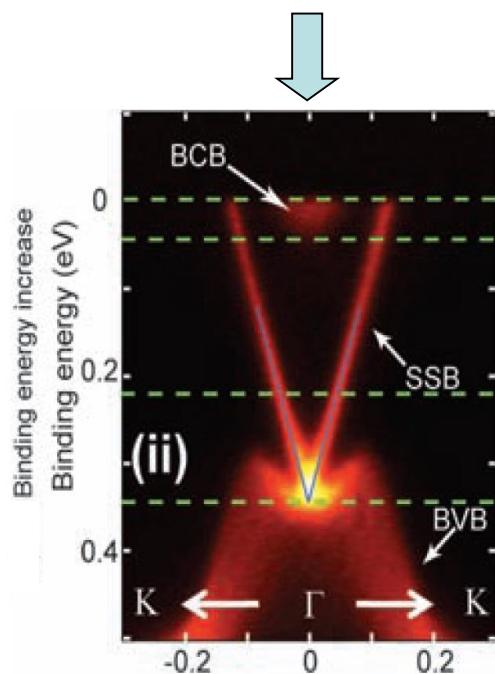
Shoucheng Zhang group



Electron Band Structure of 3D TI by ARPES

Bi_2Te_3

Fisher (Stanford)

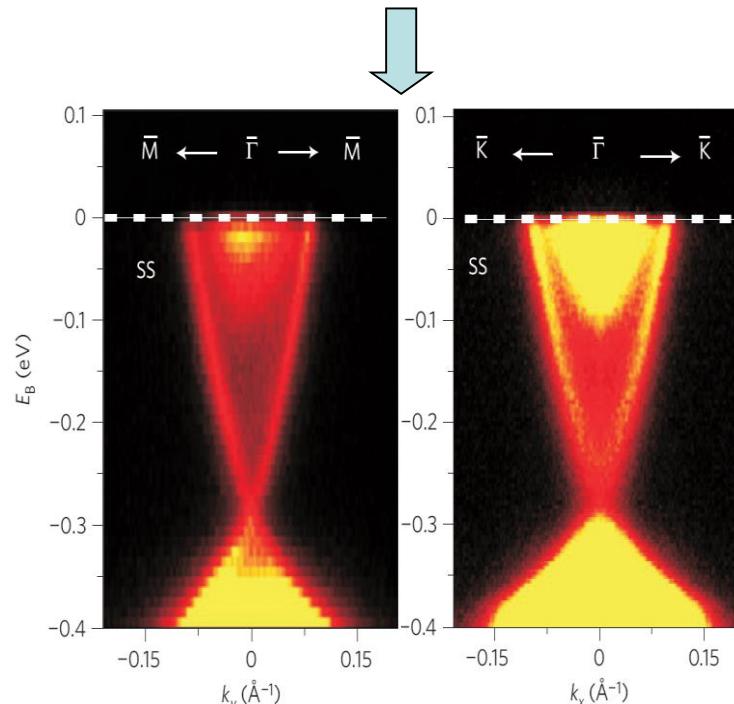


Chen et al., Science 2009

Zhixun Shen (Stanford)

Bi_2Se_3

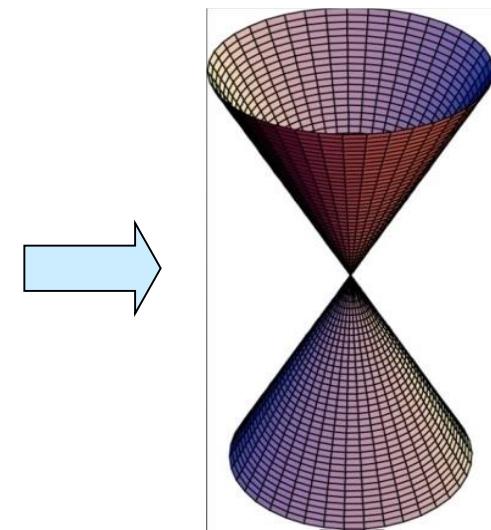
Cava (Princeton)



Xia et al., Nat. Phys. 2009

Hasan (Princeton)

n-type conductor
(Se vacancies)
(Similar to that in ZnO)



Dirac
Cone

Topological Insulator Material

“insulator” by definition: Bulk insulating
Surface metallic (2D)

bulk

(real space)

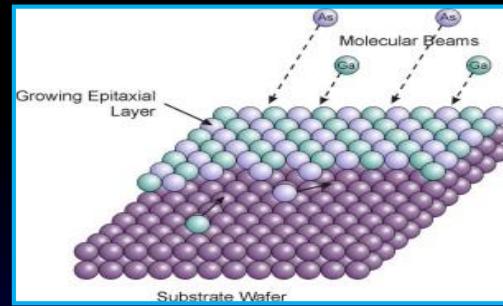
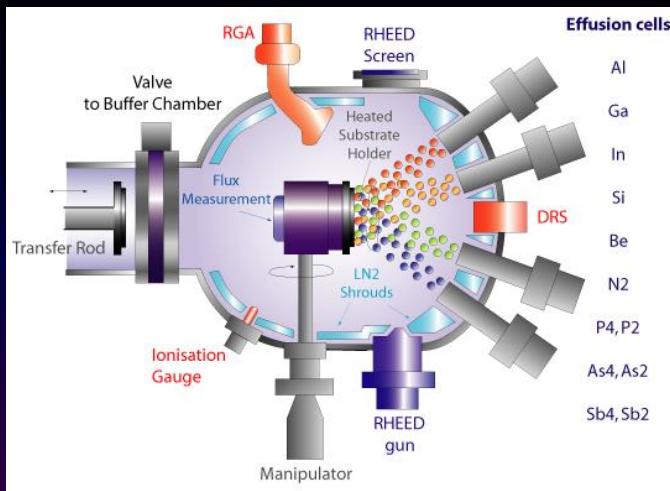
If the bulk is conducting, it is difficult to measure the transport property of its surface with exotic topological property.



High quality:
low defect/impurity
density

Molecular Beam Epitaxy (MBE)

(Cho & Arthur, 1970)



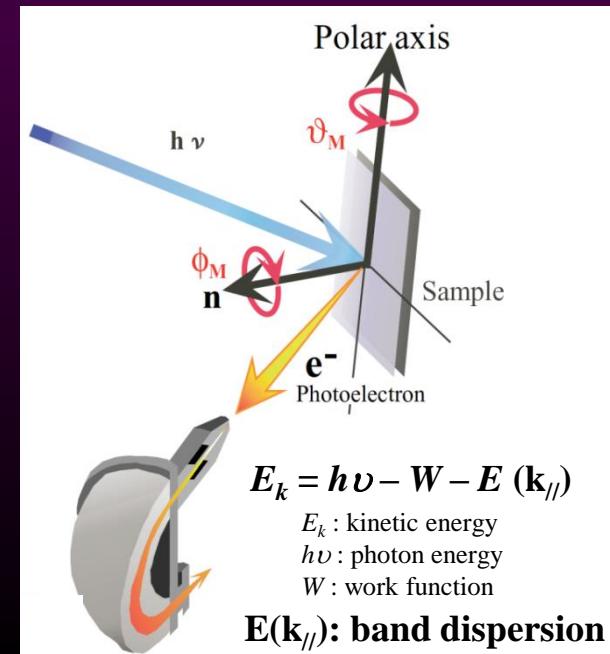
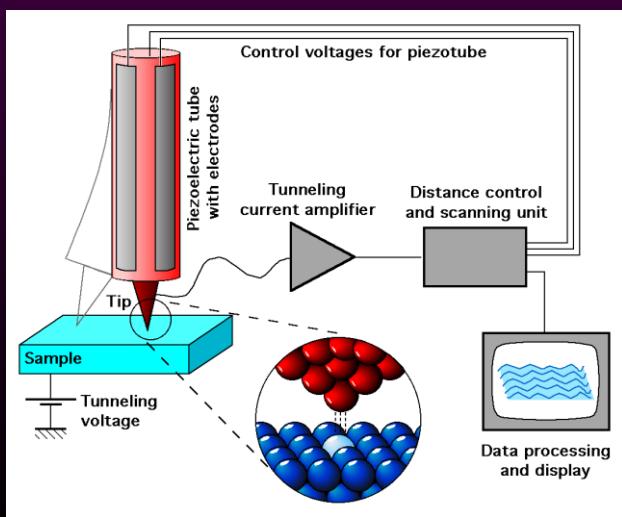
Atomic-Level

+

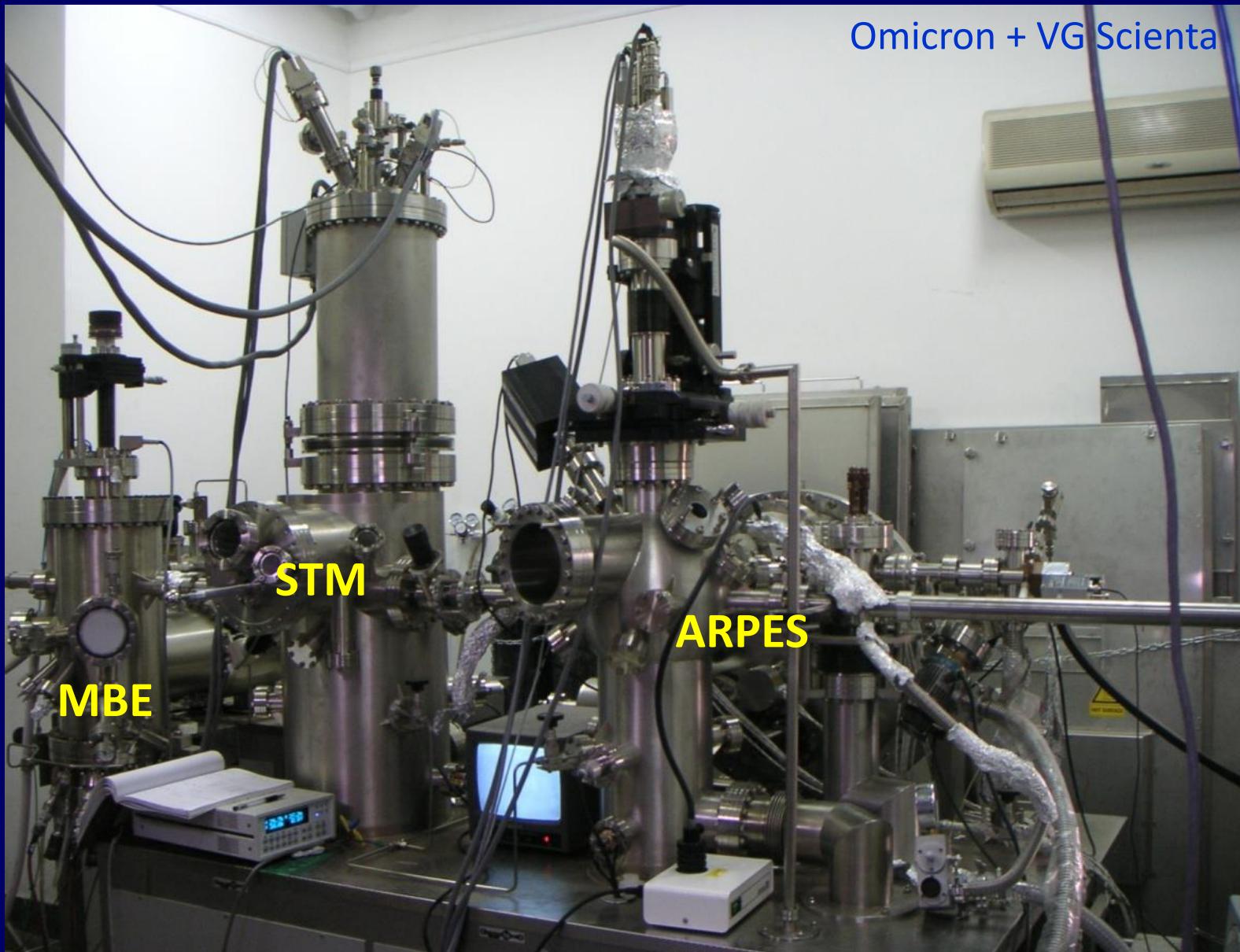
Angle-Resolved Photoemission Spectroscopy (ARPES)

Scanning Tunneling Microscope (STM)

(Binnig & Rohrer, 1981)



MBE-STM-ARPES



OUTLINE

- Introduction
- MBE-STM-ARPES of topological insulators

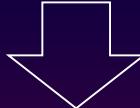
- Realization of Quantum Anomalous Hall Effect
- Summary

Establishment of MBE growth conditions

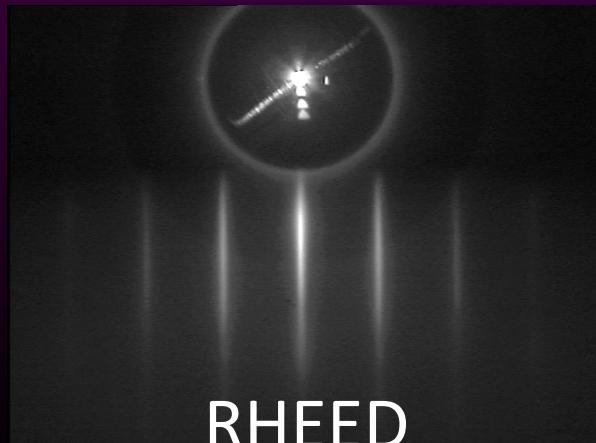
Y. Y. Li et al., Adv. Mater. 2010

Growth rules:

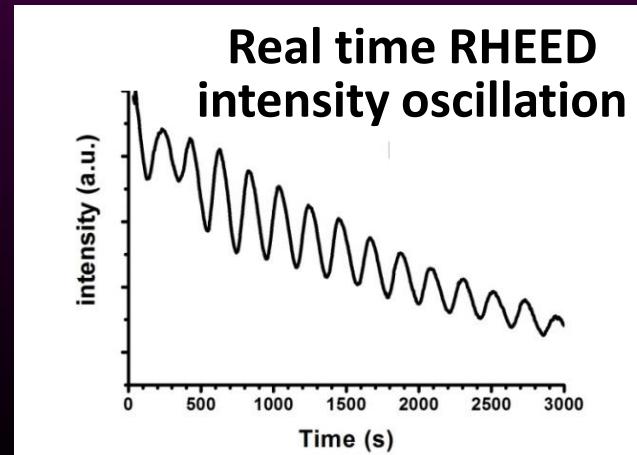
High VI (Te/Se) flux
 $T_{Bi} \gg T_{Sub} > T_{Te/Se}$



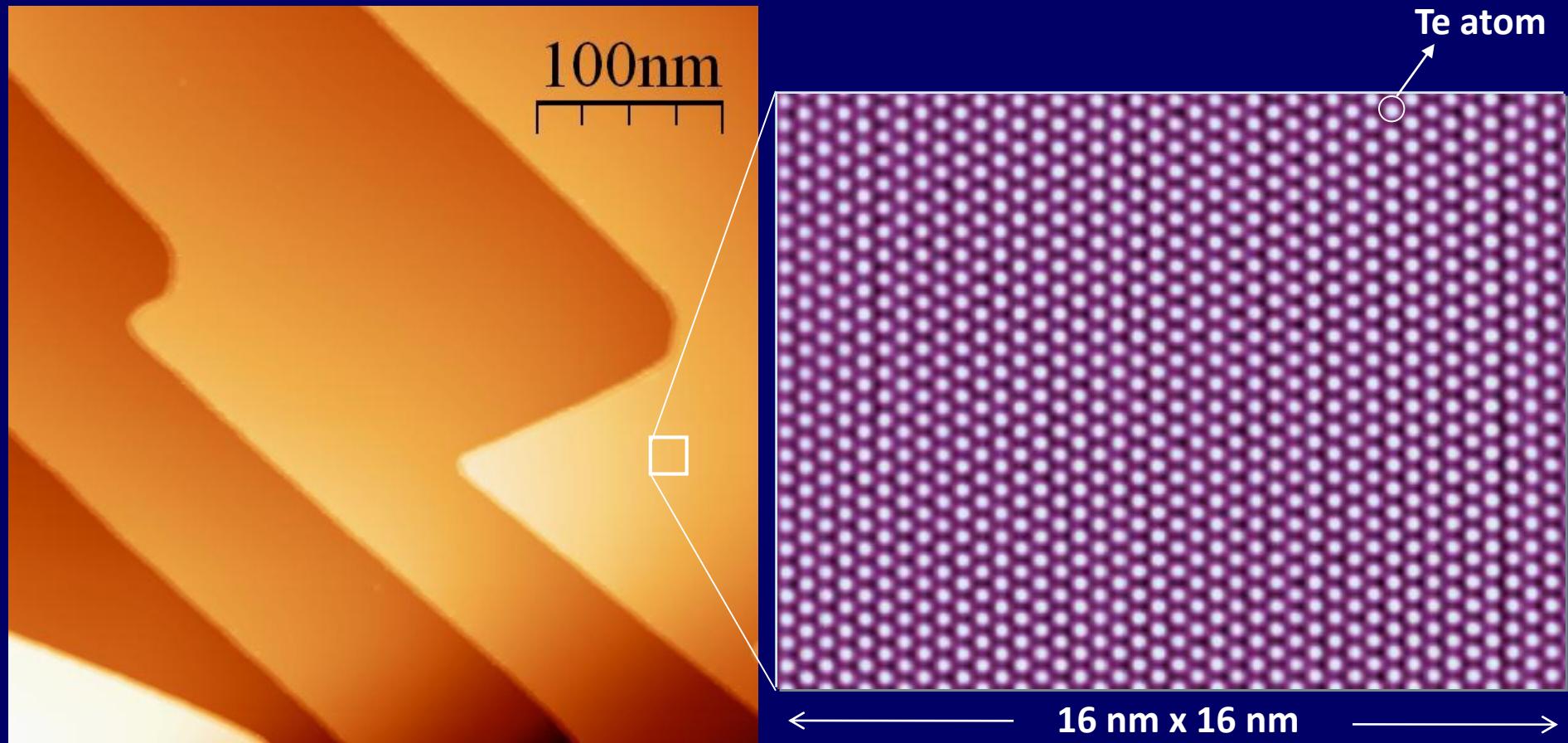
- (1) Stoichiometric: low impurities
- (2) Layer-by-layer: flat & single crystalline



RHEED



Atomically flat Bi_2Te_3 films by MBE

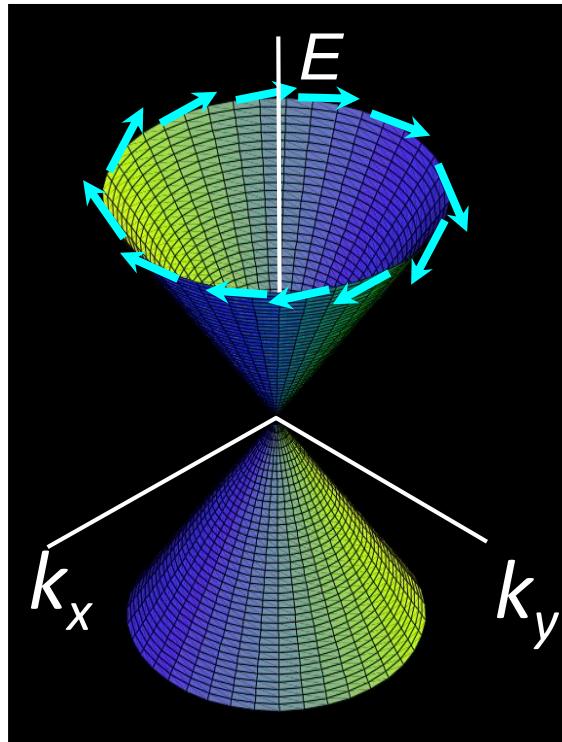
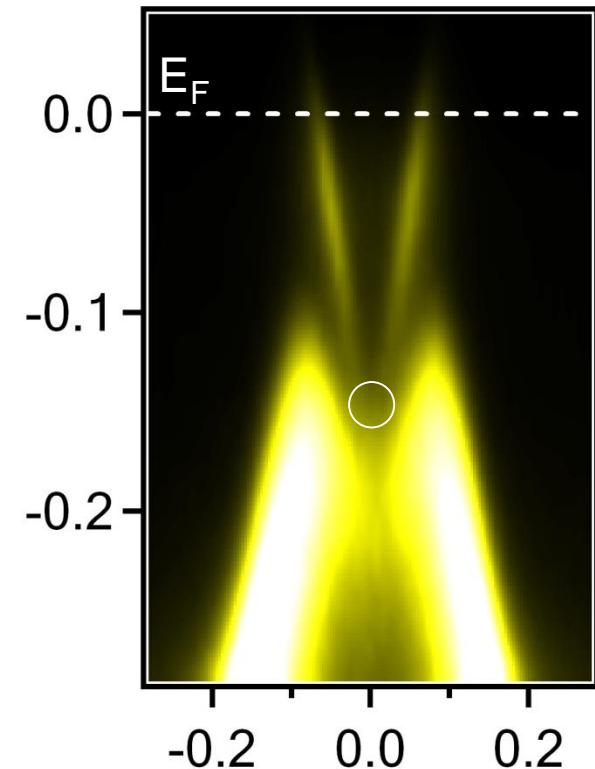


Y. Y. Li et al., Adv. Mater. (2010)

G. Wang et al., Adv. Mater. (2011)

X. Chen et al., Adv. Mater. (2011)

ARPES: Bi_2Te_3 band structure

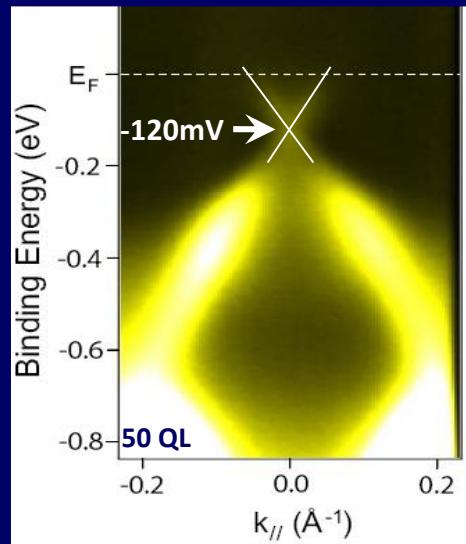
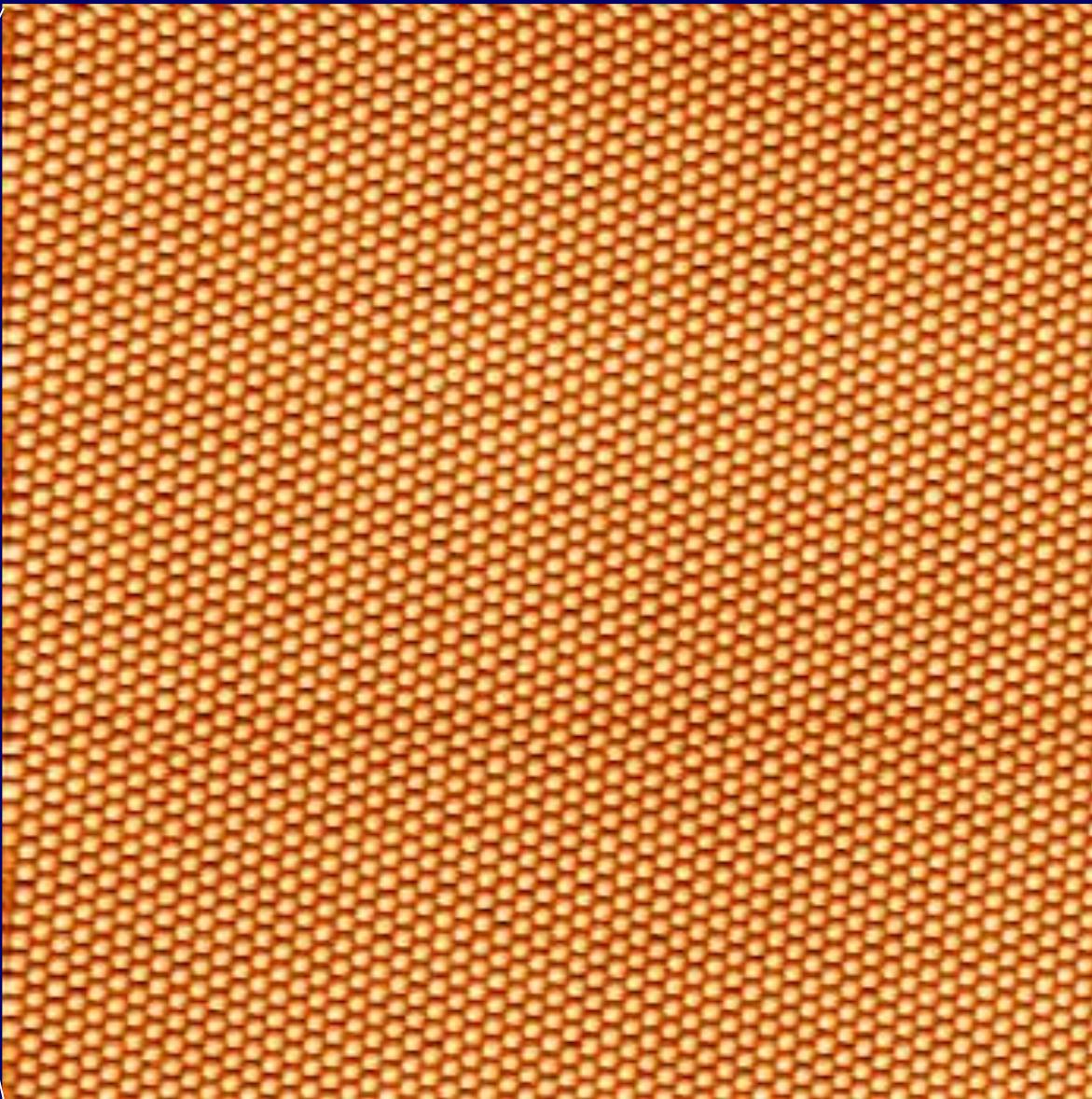
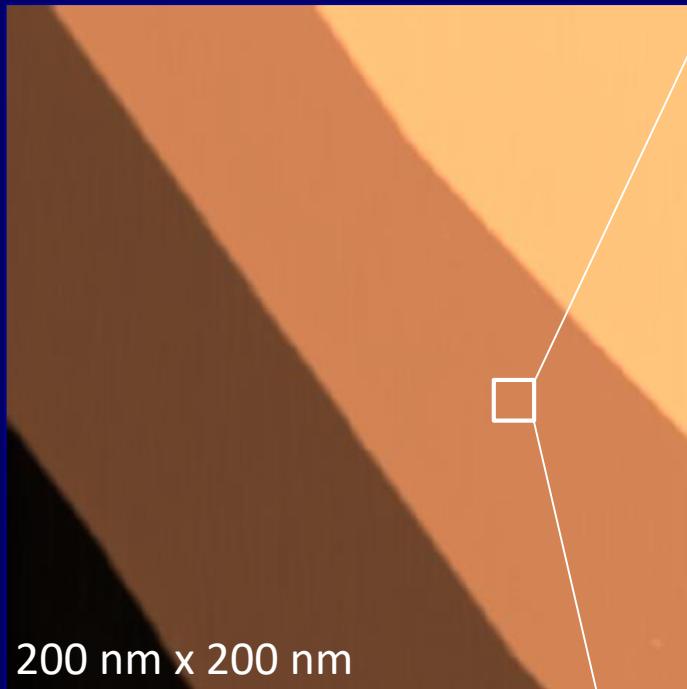


Experimentally confirmed:
Massless Dirac Cone



Insulating topological insulator

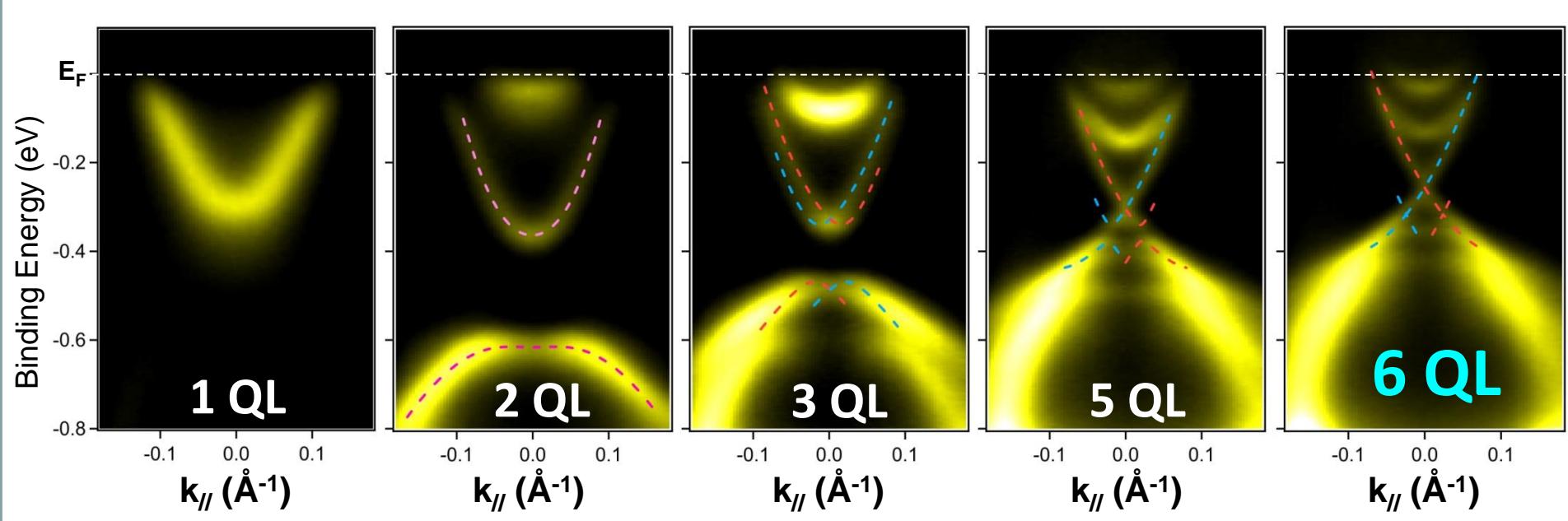
Atomically flat Bi_2Se_3 films on graphene by MBE



Yi Zhang et al., Nature Physics 6, 584 (2010)

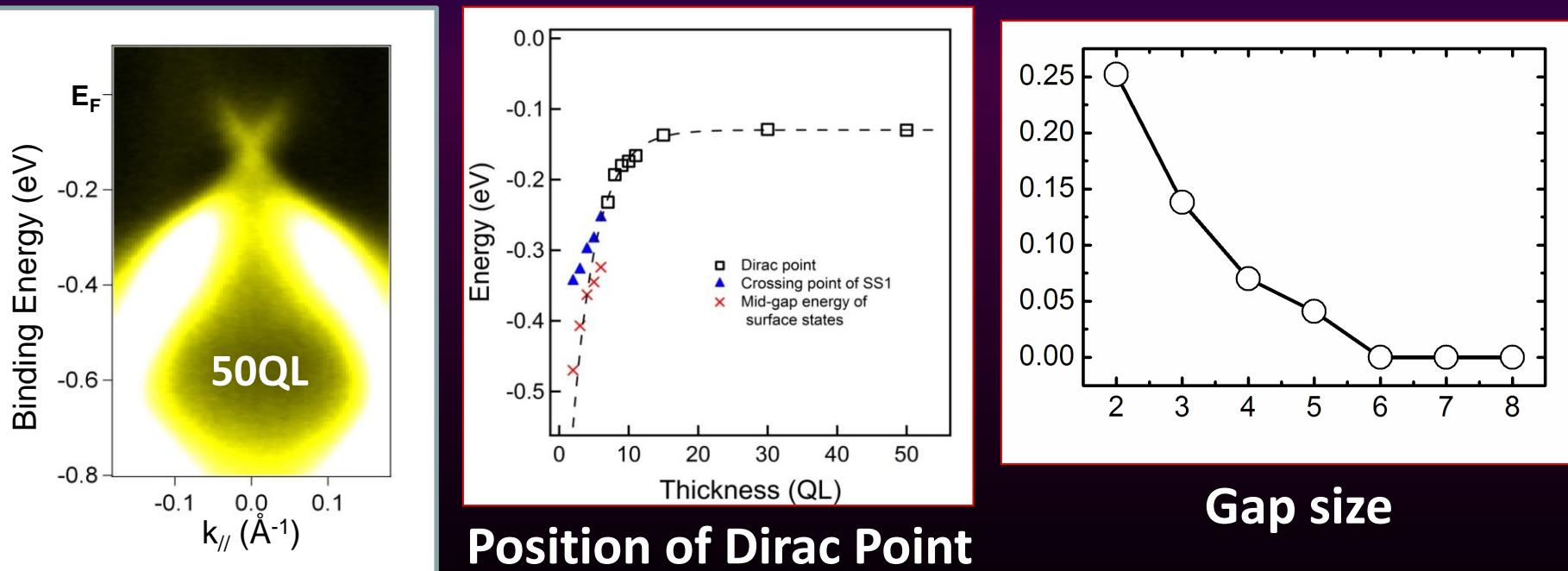
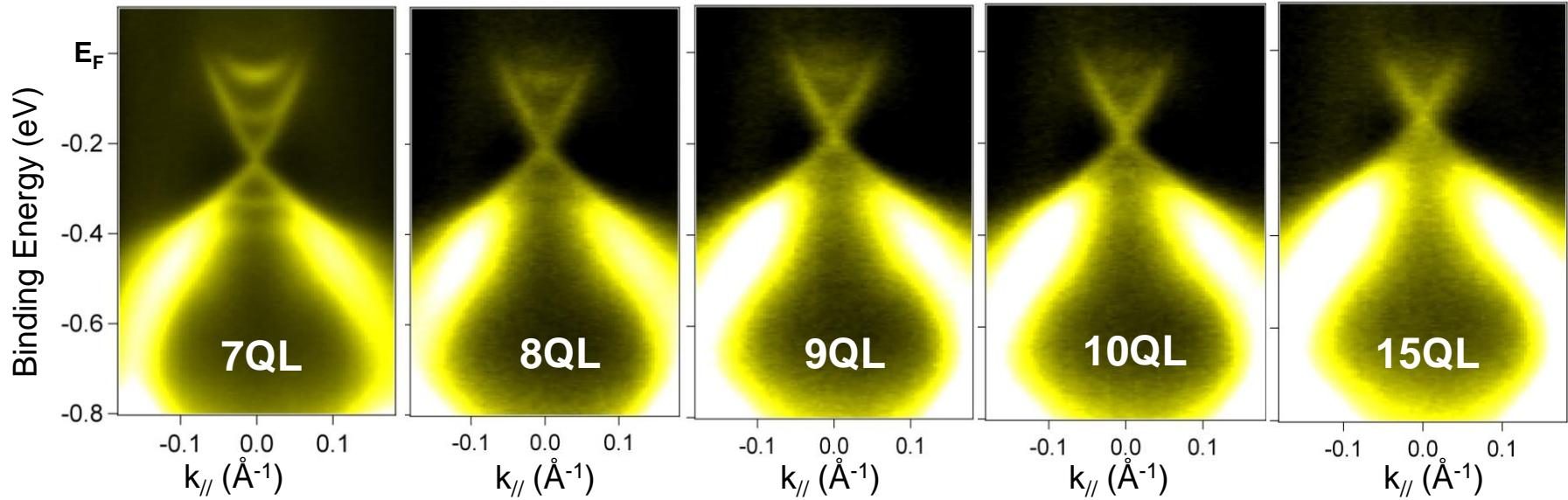
Bi_2Se_3 Band Structure: layer-by-layer

Yi Zhang et al., Nature Phys. 6, 584 (2010)

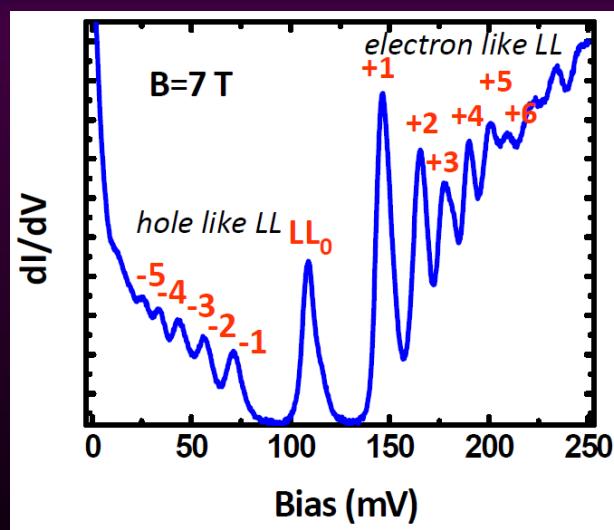
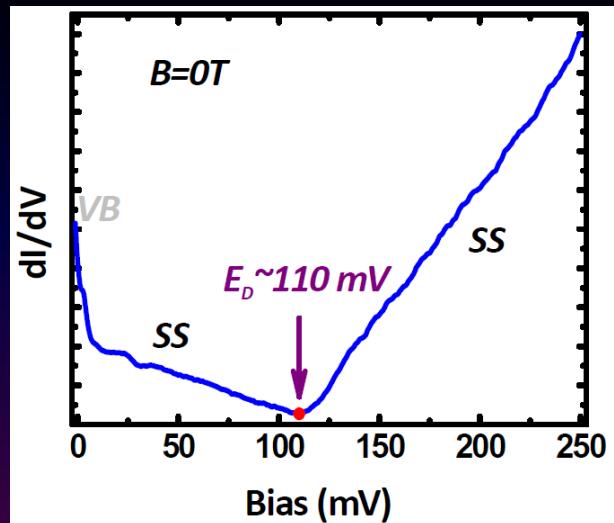
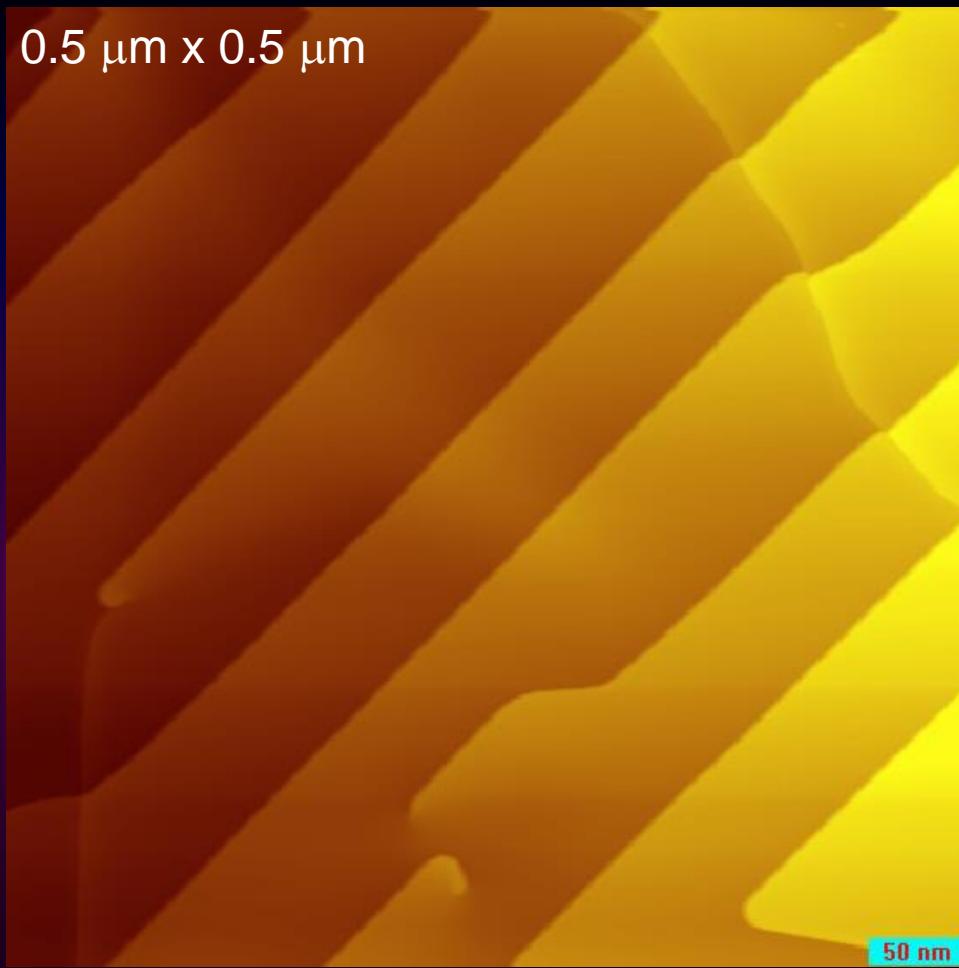


- The thickness and band structure can be controlled with atomic-layer precision by MBE
- Applied to FeSe , MoSe_2 and other layered materials

↑
Critical
thickness



Sb_2Te_3



Y. P. Jiang, PRL 108, 016401 (2012)

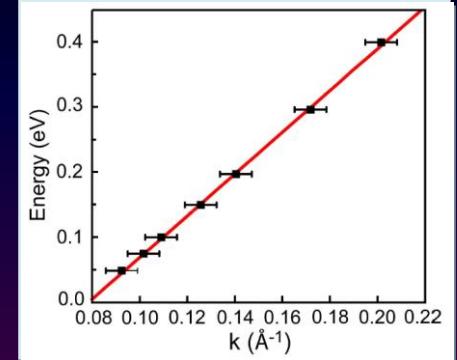
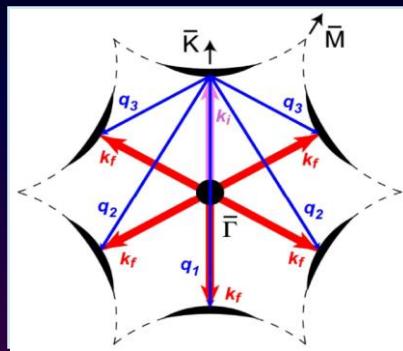
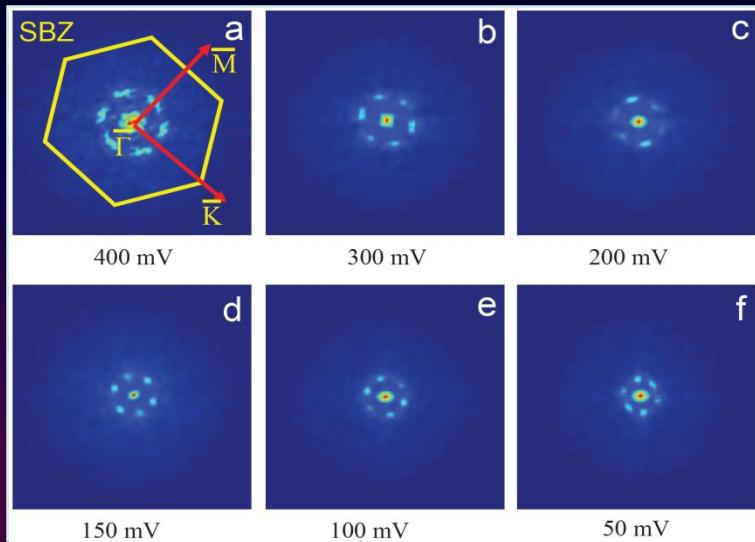
Y. P. Jiang PRL 108, 066809 (2012)

STM study of fundamental properties of TIs

Quantum Interference



Absence of backscattering



Zhang et al., PRL 103, 266803 (2009)

Jiang et al., PRL 108, 016401 (2012)

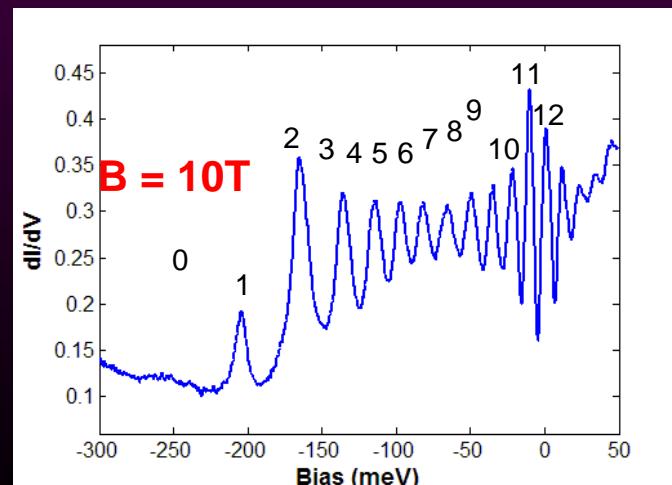
Massless Dirac fermion
(Landau Quantization)

Cheng et al., PRL 105, 076801 (2010)

Jiang et al., PRL 108, 066809 (2012)

Chang et al., PRL 115, 066809 (2015)

Song et al., PRL 114, 176602 (2015)



**With MBE-STM, we are able to prepare high quality
epitaxial thin films and demonstrate their exotic
electronic structure...**

New Effect or Law!

OUTLINE

- Introduction
- MBE-STM-ARPES of topological insulators
- Realization of Quantum Anomalous Hall Effect
- Summary

QAHE in magnetic topological insulator

PRL 101, 146802 (2008)

PHYSICAL REVIEW LETTERS

week ending
3 OCTOBER 2008

Quantum Anomalous Hall Effect in $Hg_{1-y}Mn_yTe$ Quantum Wells

Chao-Xing Liu,^{1,2} Xiao-Liang Qi,² Xi Dai,³ Zhong Fang,³ and Shou-Cheng Zhang²

¹*Center for Advanced Study, Tsinghua University, Beijing, 100084, China*

Chaoxing Liu et al. proposed that a 2D topological insulator with ferromagnetic order, but this compound cannot be made ferromagnetic

Journal of the Physical Society of Japan
Vol. 71, No. 1, January, 2002, pp. 19–22
©2002 The Physical Society of Japan

Term: QAHE

Topological Nature of Anomalous Hall Effect in Ferromagnets

Masaru ONODA * and Naoto NAGAOSA^{1,†}

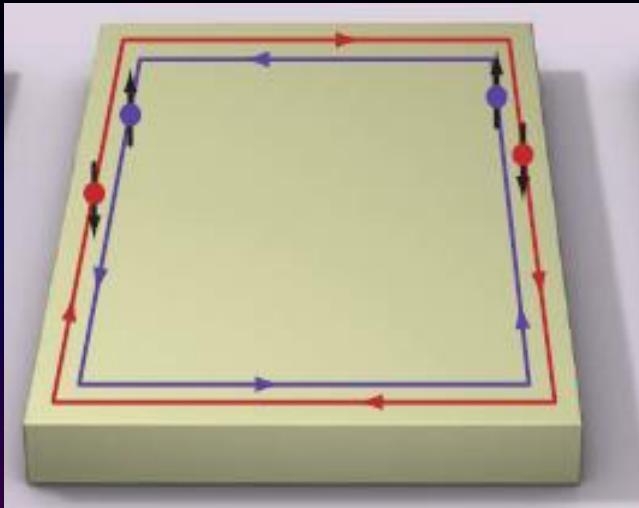
Quantized Anomalous Hall Effect in Magnetic Topological Insulators

Rui Yu,¹ Wei Zhang,¹ Hai-Jun Zhang,^{1,2} Shou-Cheng Zhang,^{2,3} Xi Dai,^{1,*} Zhong Fang^{1*}

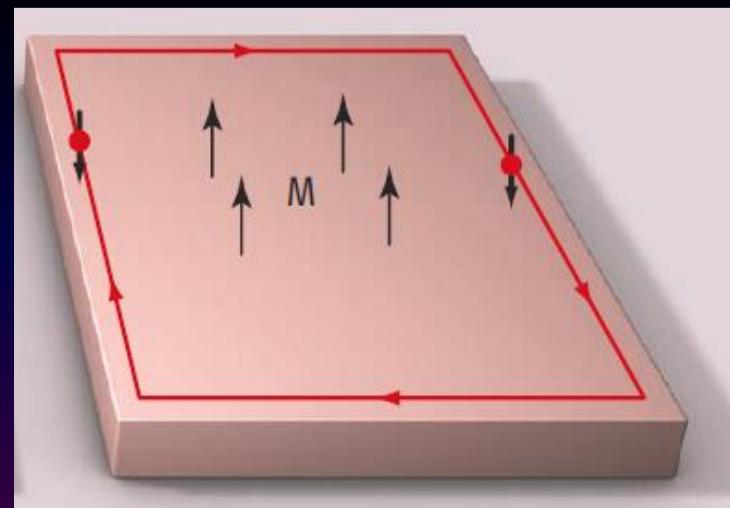
Science (2010)

- TI could remain ferromagnetic when it is insulating (van Vleck mechanism)
- The Bi_2Se_3 family topological insulator was proposed to be perfect candidate

QAHE in 2D magnetic TIs



2D TI: helical edge states



QAHE: chiral edge state

Requirements for QAHE: 2D Ferromagnetic Topological Insulator

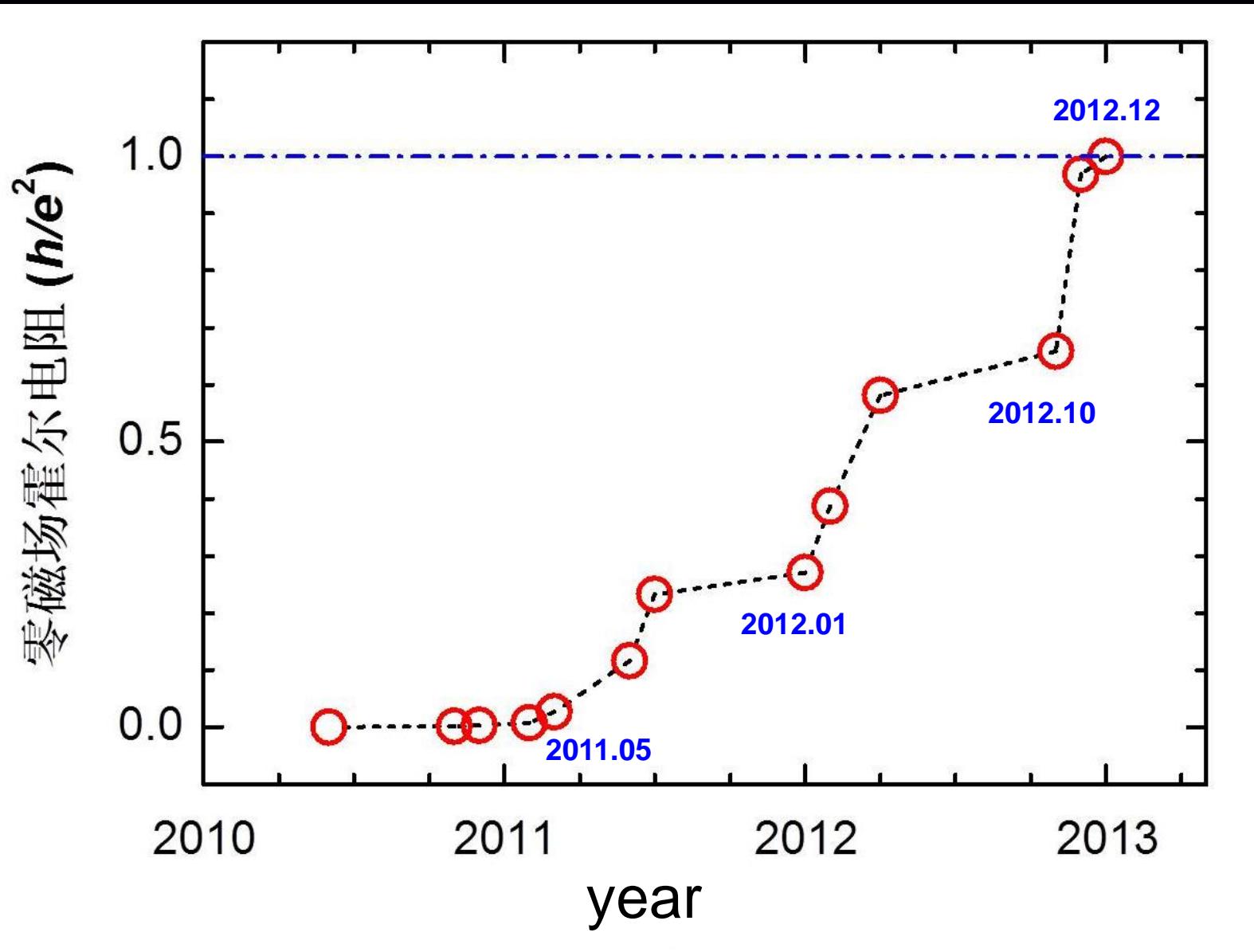
- It must be *magnetic*, so there is anomalous Hall effect at $B = 0$
- It must be *topological*, so there are spontaneous edge states
- It must be *insulating*, so there is only edge state transport

QAHE in 2D magnetic TIs

The QAHE puts stringent requirements for materials:

- Most ferromagnetic materials are metallic
- Magnetic order is difficult to realize in 2D
- Magnetism and topology may be against each other

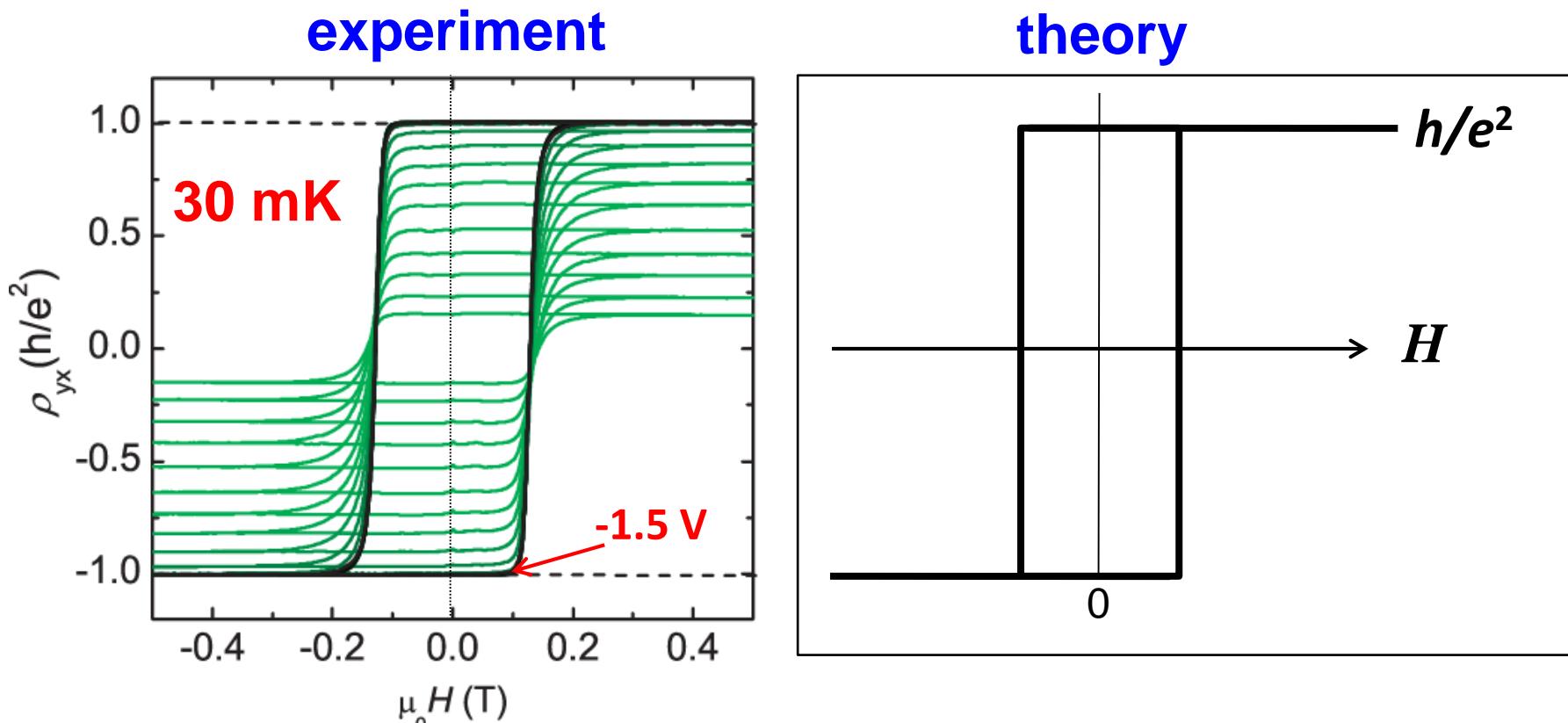
$$R_H = h/e^2 = 25812.807449 \Omega$$



- Sharpen your tools
- Work hard

Quantum Anomalous Hall Effect in $\text{Cr}_{0.15}(\text{Bi}_{0.1}\text{Sb}_{0.9})_{1.85}\text{Te}_3$

C. Z. Chang et al., Science 340, 167 (2013)



- 20 samples at $T = 1.5 \text{ K}$
- 6 samples at $T = 90 \text{ mK}$ (zero-field $\rho = 0.87$ to 0.98 h/e^2)
- 2 samples at $T = 30 \text{ mK}$ (full quantization at h/e^2)

QAHE by other groups

nature
physics

LETTERS

PUBLISHED ONLINE: 17 AUGUST 2014 | DOI: 10.1038/NPHYS3053

Trajectory of the anomalous Hall effect towards
the quantized state in a ferromagnetic
topological insulator

J. G. Checkelsky^{1*}, R. Yoshimi¹, A. Tsukazaki², K. S. Takahashi³, Y. Kozuka¹, J. Falson¹, M. Kawasaki^{1,3}
and Y. Tokura^{1,3}

PRL 113, 137201 (2014)

PHYSICAL REVIEW LETTERS

week ending
26 SEPTEMBER 2014

Y. Tokura (Tokyo/RIKEN)

K. L. Wang (UCLA)

nature
materials

LETTERS

PUBLISHED ONLINE: 2 MARCH 2015 | DOI: 10.1038/NMAT4204

High-precision realization of robust quantum
anomalous Hall state in a hard ferromagnetic
topological insulator

Cui-Zu Chang^{1*}, Weiwei Zhao^{2*}, Duk Y. Kim², Haijun Zhang³, Badih A. Assaf², Don Heiman⁴,
Shou-Cheng Zhang³, Chaoxing Liu², Moses H. W. Chan² and Jagadeesh S. Moodera^{1,5*}

J. Moodera (MIT)

PRL 114, 187201 (2015)

Selected for a Viewpoint in Physics
PHYSICAL REVIEW LETTERS

week ending
8 MAY 2015

D. Goldhaber-Gordon (Stanford)

Precise Quantization of the Anomalous Hall Effect near Zero Magnetic Field

A. J. Bestwick,^{1,2} E. J. Fox,^{1,2} Xufeng Kou,³ Lei Pan,³ Kang L. Wang,³ and D. Goldhaber-Gordon^{1,2,*}

QUANTUM MECHANICS

Large discrete jumps observed in the transition
between Chern states in a ferromagnetic
topological insulator

Minhao Liu,¹ Wudi Wang,¹ Anthony R. Richardella,² Abhinav Kandala,² Jian Li,¹ Ali Yazdani,¹
Nitin Samarth,² N. Phuan Ong^{1*}

N. P. Ong (Princeton)

PRL 118, 246801 (2017)

N. Sarmath (Penn State)

PHYSICAL REVIEW LETTERS

week ending
16 JUNE 2017

Scaling of the Quantum Anomalous Hall Effect as an Indicator of Axion Electrodynamics



TOPOLOGICAL PHASE TRANSITIONS AND TOPOLOGICAL PHASES OF MATTER

compiled by the Class for Physics of the Royal Swedish Academy of Sciences



D. Thouless



F. Haldane



J. Kosterlitz

The great importance of the Thouless *et al.* result is that it opens up the possibility of having a Hall conductance even in the absence of a magnetic field. It would, however, be another six years before this conceptually very important step was taken by Haldane [22], who realized that the important thing is to break the invariance under time-reversal and have an energy band,

This phase of matter described by Haldane is now called a *Chern insulator*, and twentyfive years later, in 2013, a quantized Hall effect was observed in thin films of Cr-doped $(\text{Bi},\text{Sb})_2\text{Te}_3$ at zero magnetic field, thus providing the first experimental detection of this phase of matter [15]. In Fig. 6 we see a clear plateau in the Hall resistance ρ_{yx} at a density (regulated by the gate voltage) corresponding to a filled band. The later development of *topological band theory* will be discussed in the concluding section.

Topological Insulators (2005–present)

(Dirac/Weyl semimetals)

Reviews: Qi & Zhang: *Phys. Today* 2009

Hasan & Kane: *Rev. Mod. Phys.* 2010

Qi & Zhang: *Rev. Mod. Phys.* 2011

Quantum Anomalous Hall Effect

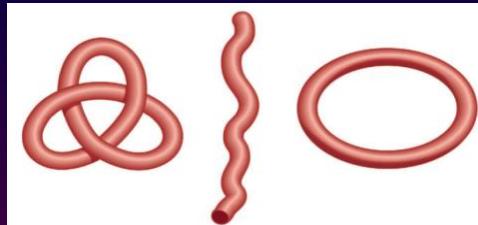
Quantum Spin Hall Effect

Majorana Fermions

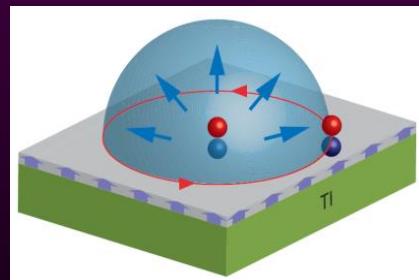
Magnetic Monopole and Dyon

TME Effect and Axion

.....

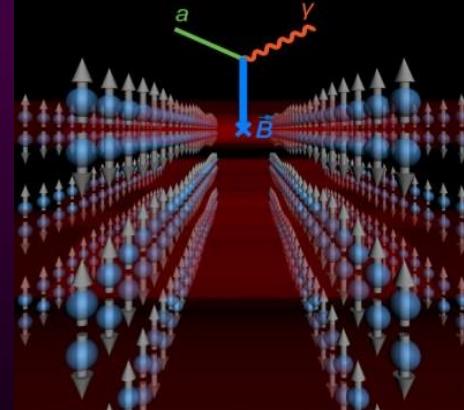


J. Moore, *Nature* 2010



Qi & Zhang, *Science* 2009

Dark matter on
desktop
Wilczek, *Nature* 2009



Anomalous Hall Effect: Mechanism

*Nagaosa, Sinova, Onoda, MacDonald, Ong,
Review of Modern Physics 2009*

$$\sigma_{\text{AH}} = (\sigma_{\text{int}} + \sigma_{\text{sk}} + \sigma_{\text{sj}})$$

Spin-orbit coupling: intrinsic

R. Karplus, J. M. Luttinger, Phys. Rev. 95, 1154 (1954)

$$\rho_{\text{int}} \propto \rho_{xx}^2$$

Skew scattering: extrinsic

J. Smit, Physica 24, 39 (1958)

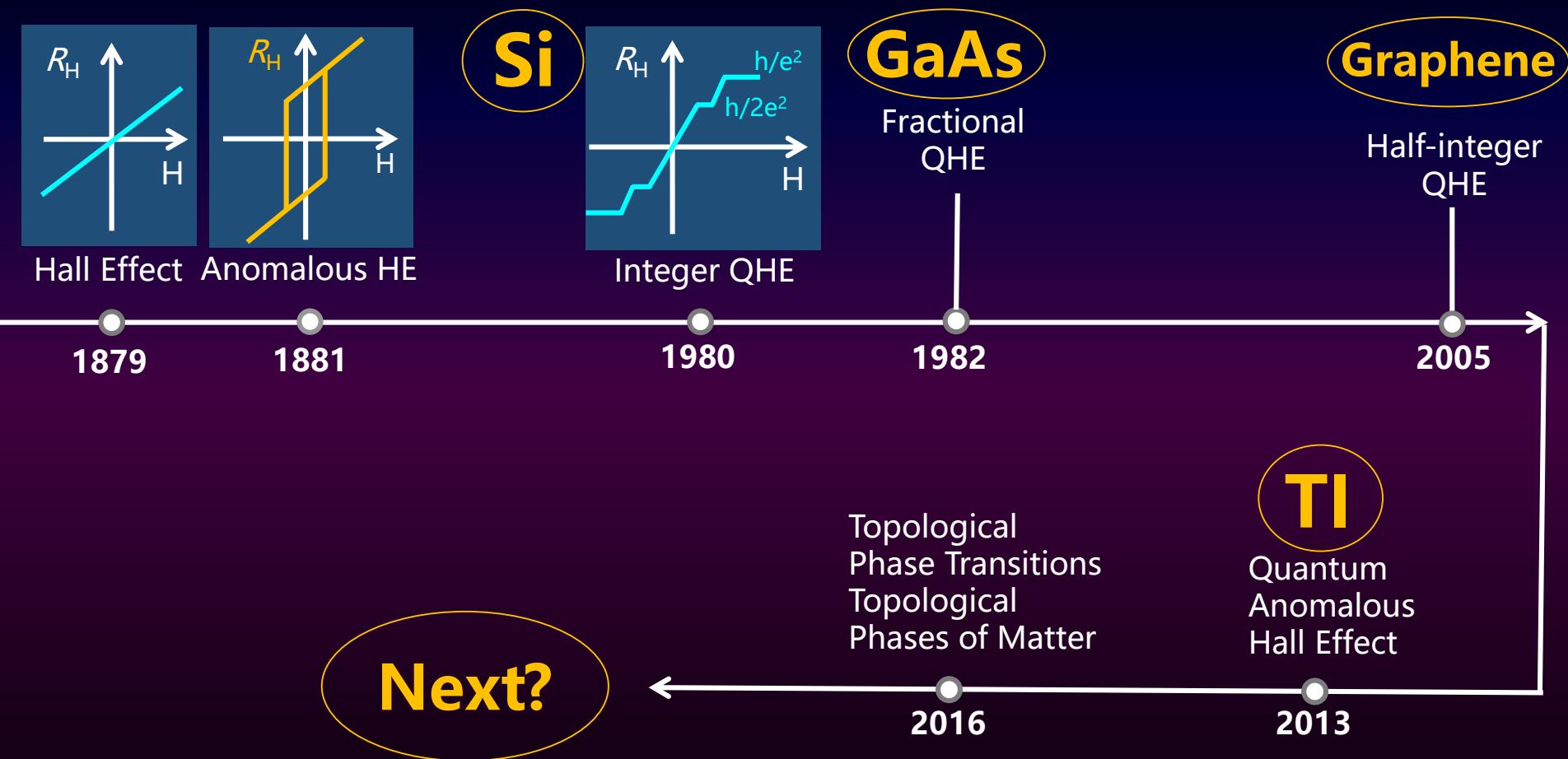
$$\rho_{\text{sk}} \propto \rho_{xx}$$

Side jump: extrinsic

L. Berger, Phys. Rev. B2, 4559 (1970)

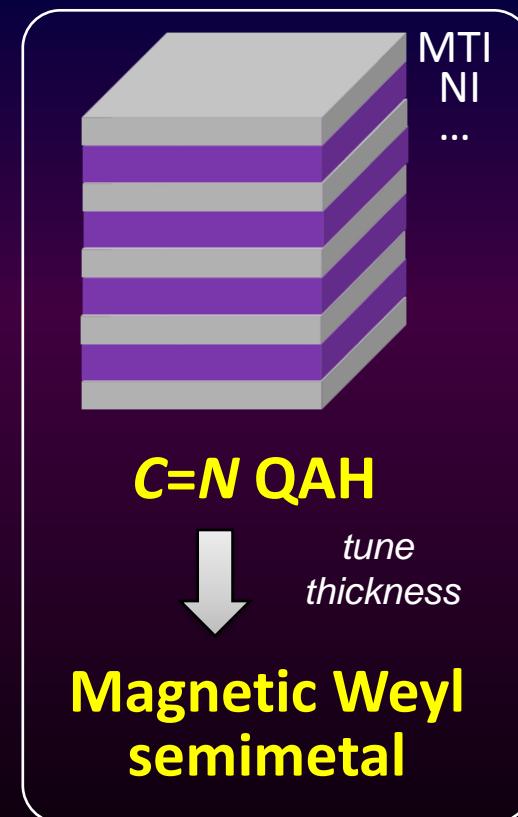
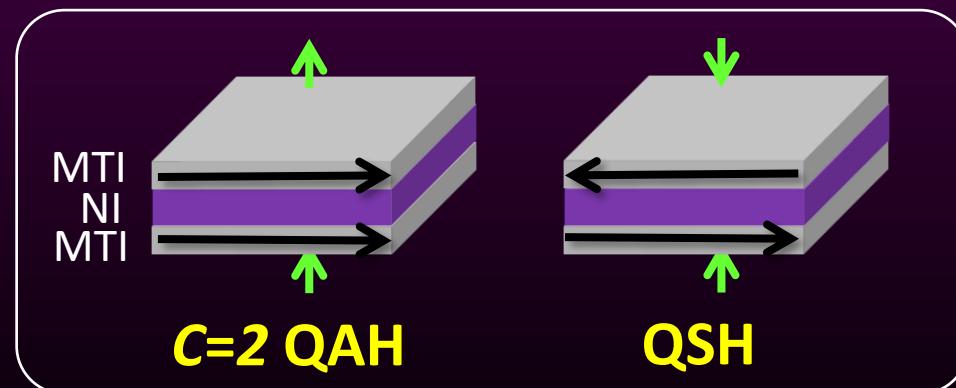
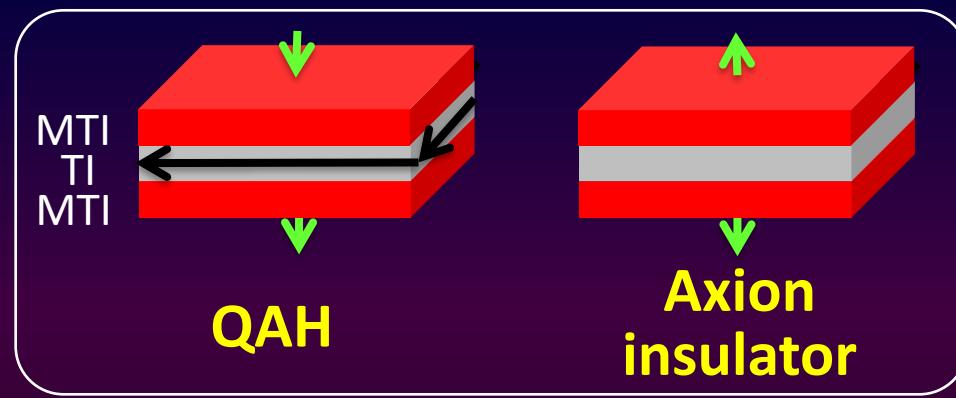
$$\rho_{\text{sj}} \propto \rho_{xx}^2$$

Material Driven Discoveries



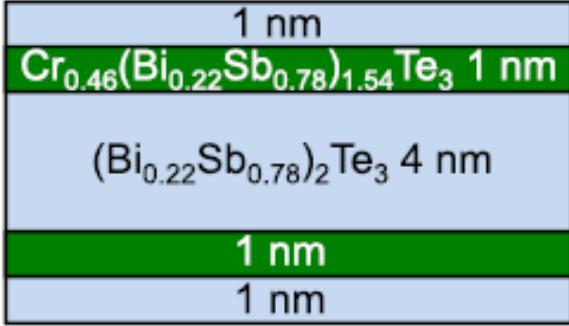
New progresses in QAHE

- QAHE at higher temperatures
- Other novel topological states of matter

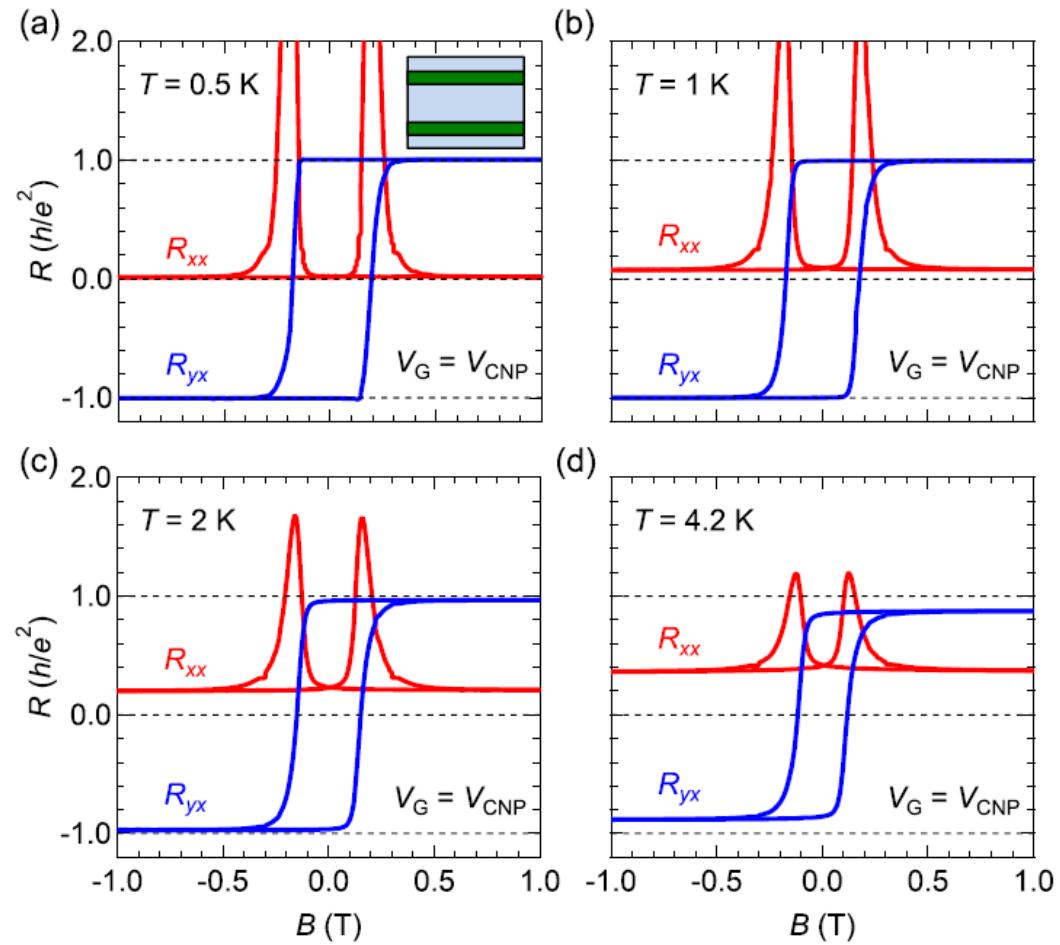


“Penta-layer” Cr-doped $(\text{Bi},\text{Sb})_2\text{Te}_3$

penta-layer



Perfect quantization
at 0.5 K and zero field



Quantized Anomalous Hall Effect in V-Sb₂Te₃

nature
materials

LETTERS

PUBLISHED ONLINE: 2 MARCH 2015 | DOI: 10.1038/NMAT4204

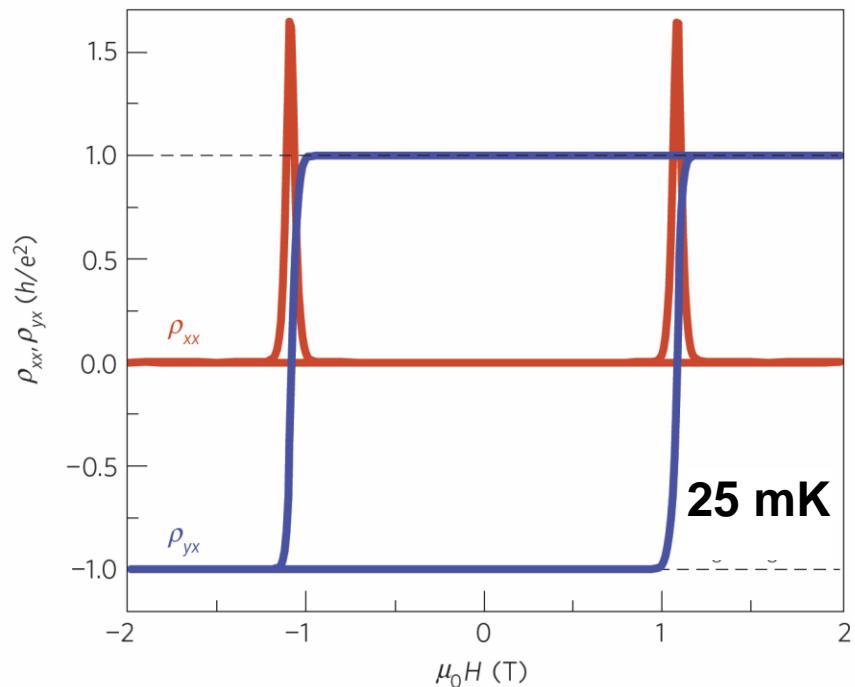
High-precision realization of robust quantum anomalous Hall state in a hard ferromagnetic topological insulator

MIT/PSU/Stanford

Cui-Zu Chang^{1*}, Weiwei Zhao^{2*}, Duk Y. Kim², Haijun Zhang³, Badih A. Assaf⁴, Don Heiman⁴, Shou-Cheng Zhang³, Chaoxing Liu², Moses H. W. Chan² and Jagadeesh S. Moodera^{1,5*}

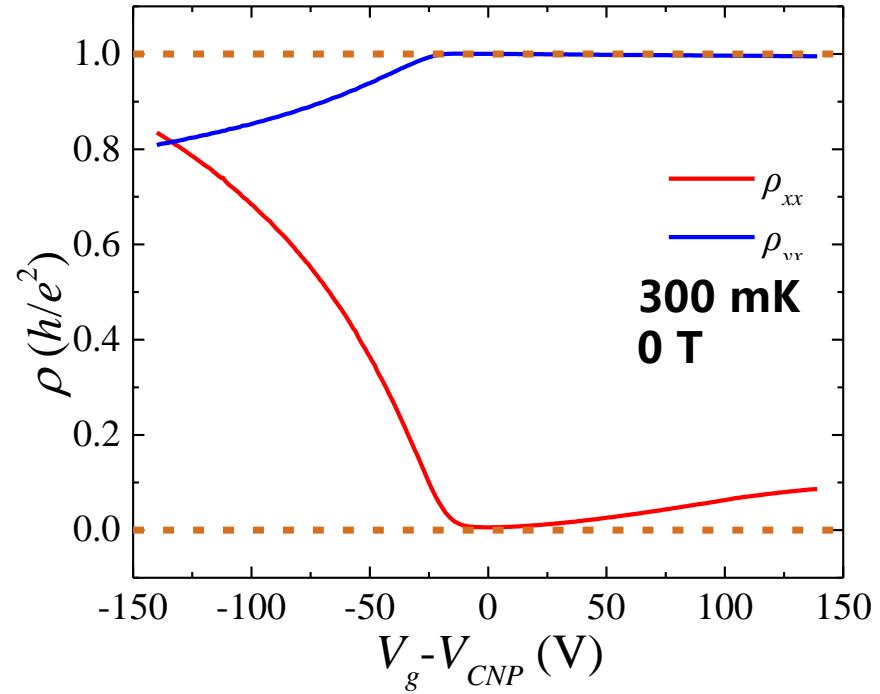
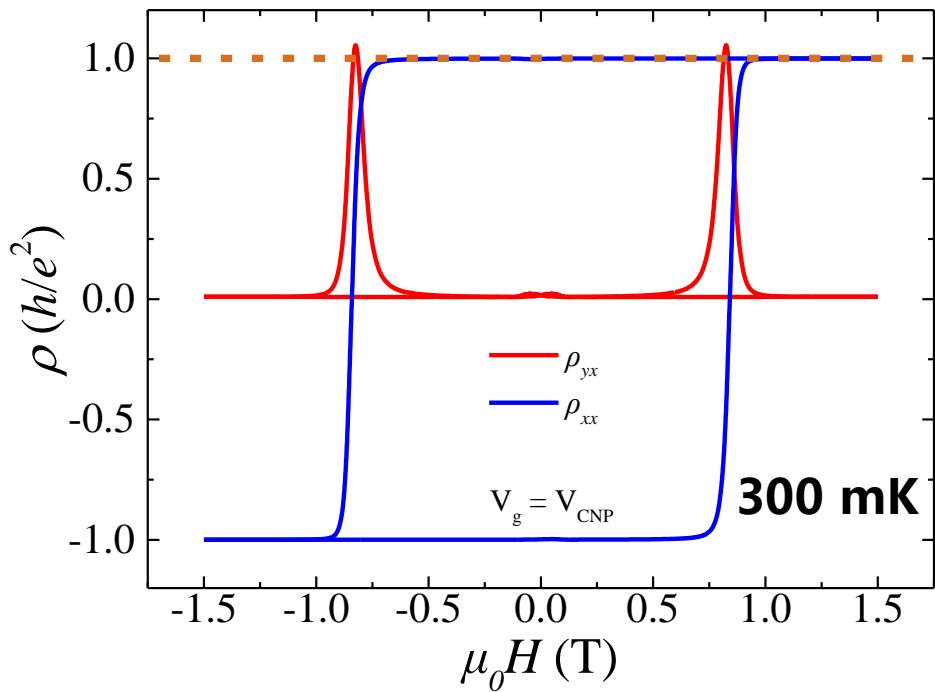
V-doped Sb₂Te₃
(~4%)

Moodera Group (MIT)



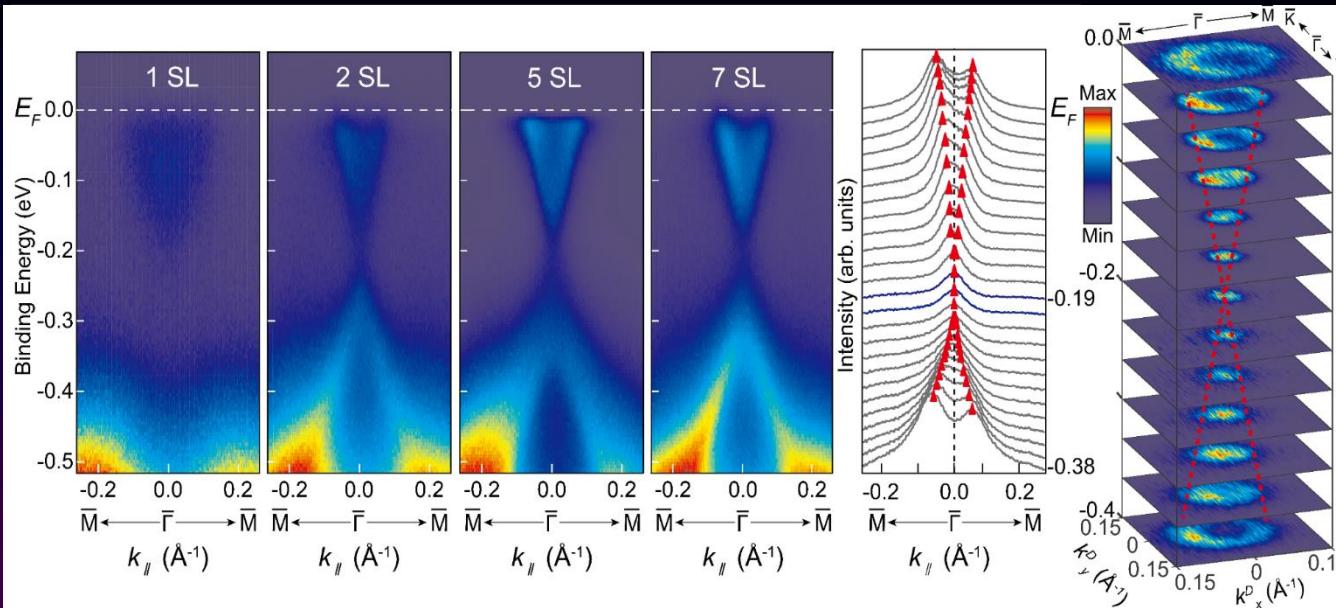
QAHE at higher T

Cr+V co-doped $(\text{BiSb})_2\text{Te}_3$



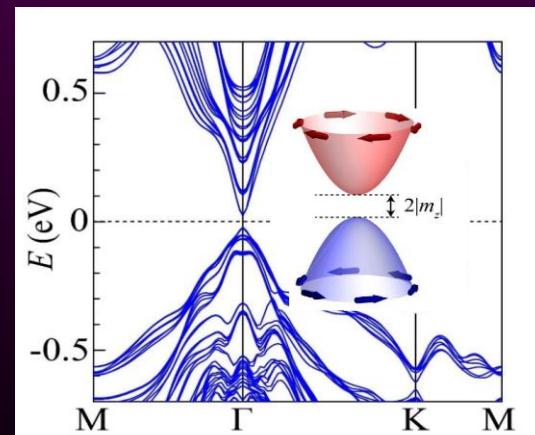
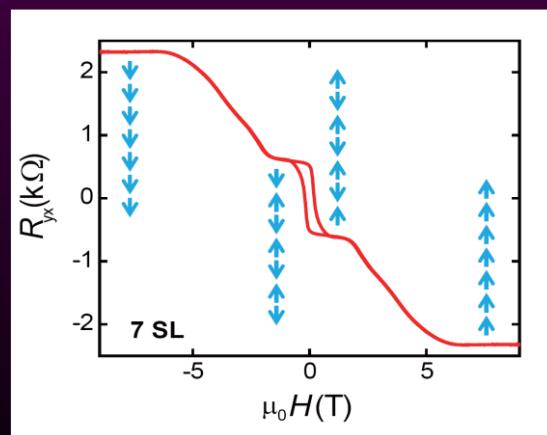
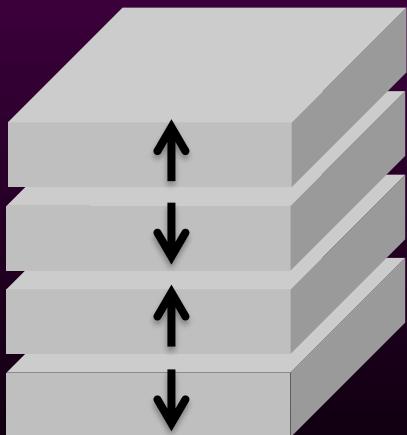
Perfect quantization at **T = 300 mK**

MnBi₂Te₄: 3D TI by MBE

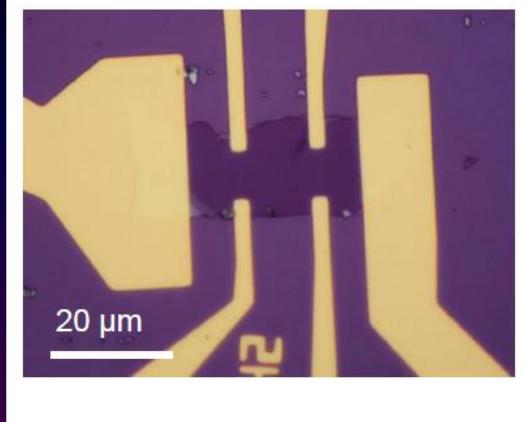


- 5SL MnBi₂Te₄:
- Chern No. =1
 - Gap: ~52meV

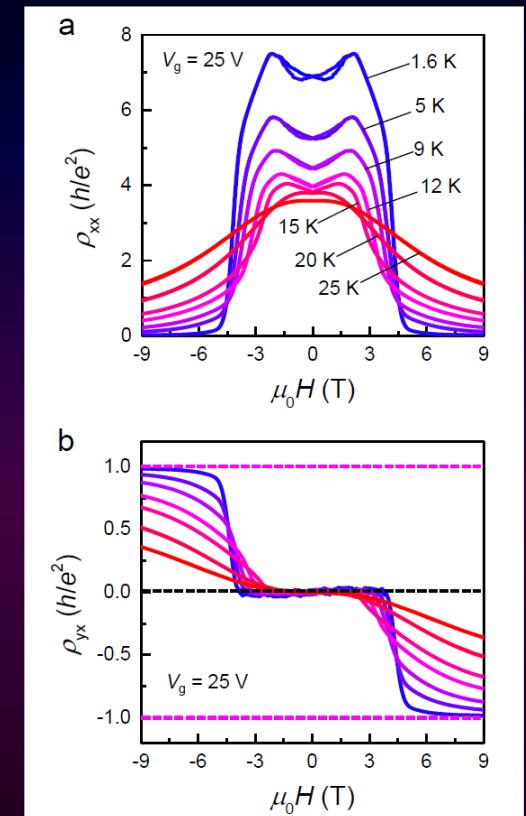
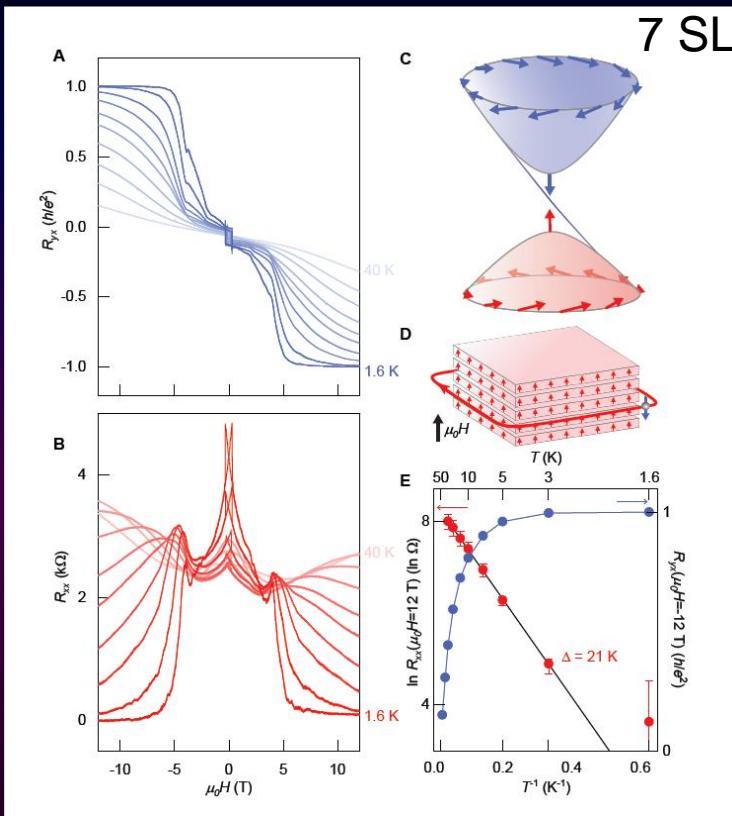
QAHE



QAHE in single crystal flakes of MnBi_2Te_4



Requires a strong magnetic field



Xianhui Chen (USTC) and Yuanbo Zhang (Fudan): arXiv: 1904.11468
Yayu Wang (Tsinghua): arXiv: 1905.00715

“Spin valve” based on QAH edge states

Sample
Structure

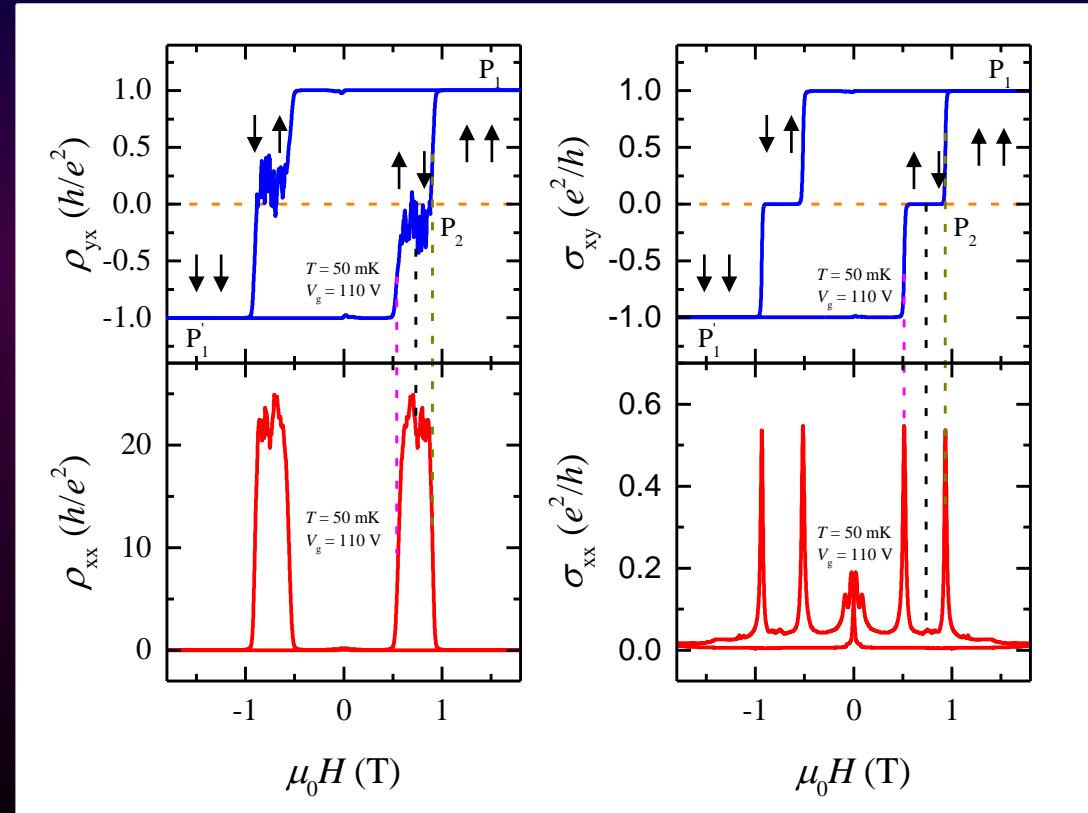


MTI (Cr/V: 0.16/0.84—larger coercivity)
TI (non-magnetic)
MTI (Cr/V: 0.4/0.6—smaller coercivity)

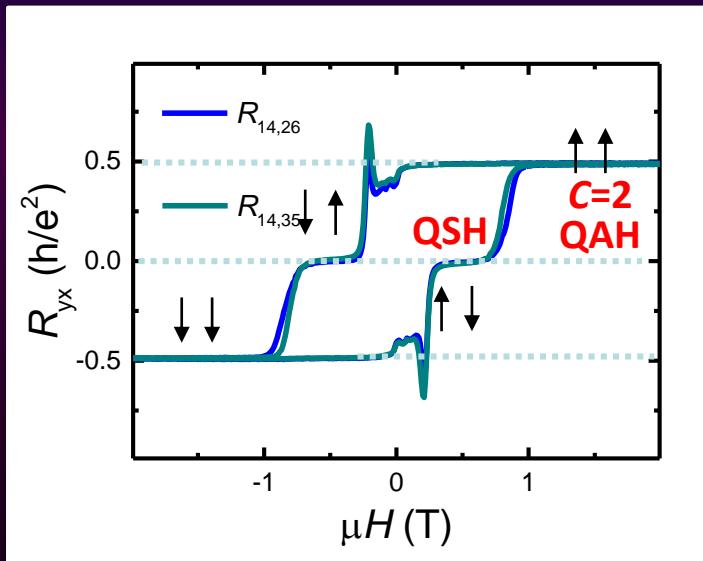
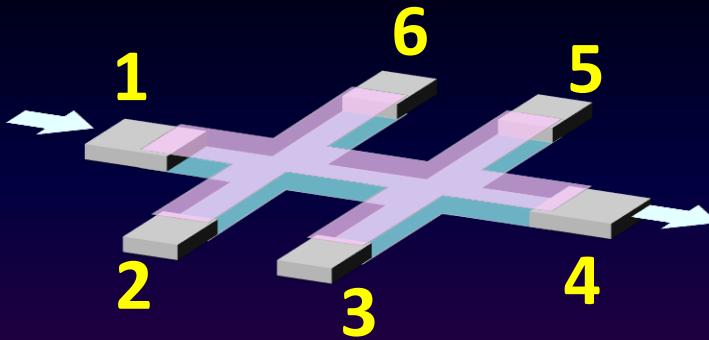
- When the magnetization directions of the top and bottom layers are parallel, QAH ($\rho_{xx}=0$, $\rho_{xy}=h/e^2$).
- Its longitudinal resistance becomes very large ($\rho_{xx}>20 h/e^2$) when anti-parallel.



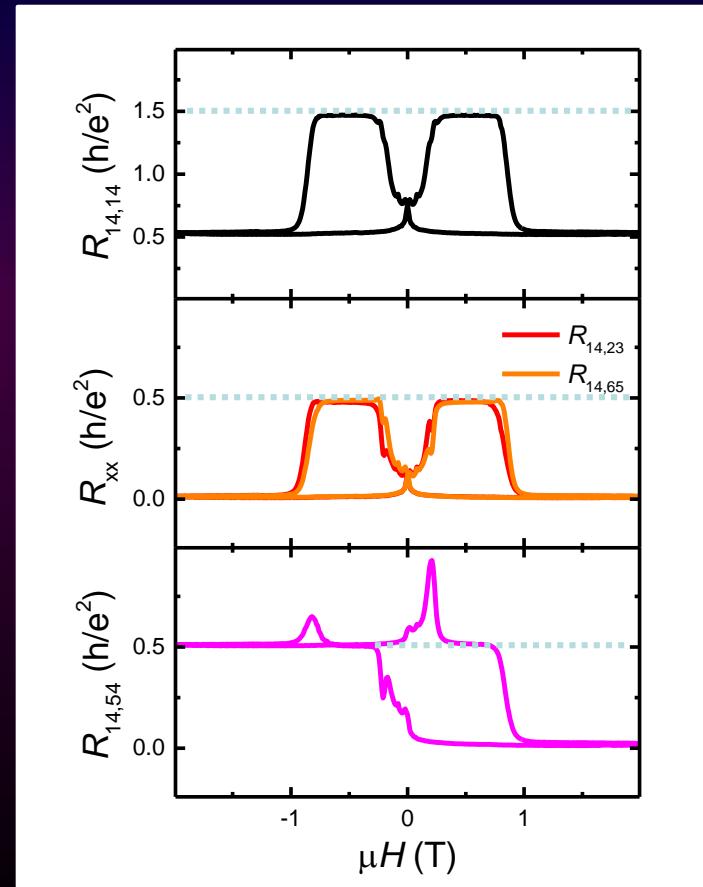
Spin valve



Synthetic Quantum Spin Hall Effect



- When two QAH sub-systems have the same magnetization direction (strong field), the system become a QAH insulator with Chern number 2.
- In the case of opposite magnetization, it becomes a QSH system.



Summary

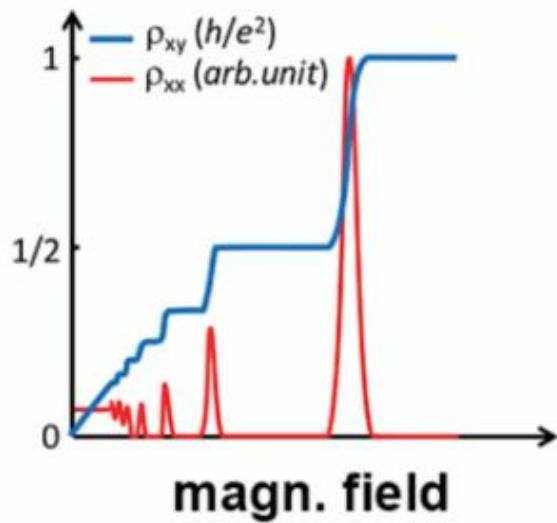
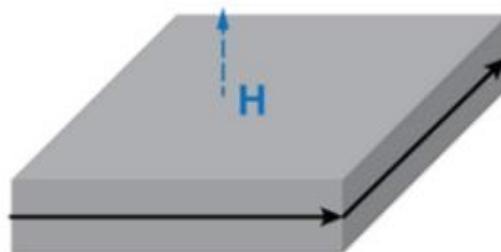
- QAHE is well-established quantum state of matter, independently realized by many groups.
- QAHE forms a platform for other exotic states of matter.

Hall Effect	1879	Anomalous Hall Effect	1881
IQHE	1980	QAHE	2013
FQHE	1982		

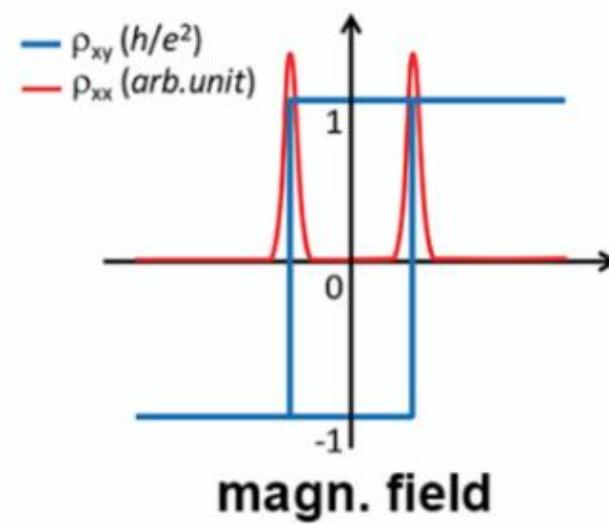
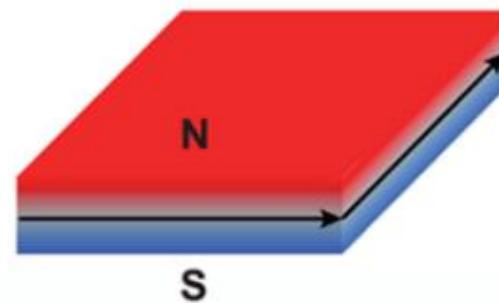
 with Magnetic Field

 w/o Magnetic Field

QHE



QAHE



science is art

Acknowledgements

Group Members:

Ke He, Xucun Ma, Xi Chen, Lili Wang, S. H. Ji (Tsinghua/IOP)
Jinfeng Jia (Shanghai Jiao-Tong Univ.)

Transport: Yayu Wang (Tsinghua), Li Lv, Y. Q. Li (IOP)

Theory: Shoucheng Zhang (Stanford)

**Bangfen Zhu, Wenhui Duan (Tsinghua), Zhong Fang, Xi Dai (IOP),
X. L. Qi (Stanford), C. X. Liu (Penn State), Shengbai Zhang (RPI),
X. C. Xie (PKU), S. Q. Shen (Hong Kong), Feng Liu (Utah)**

\$\$\$: **NSF, MOST, MOE of China**

Thank you very much!