

# Looking for strong EW phase transitions

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Electroweak Phase Transition

Based on works done with  
M. Carena, M. Quirós, C. Wagner, A. Wulzer

# Outline

- 1 EWBG Introduction
- 2 Effective Theory
  - Matching conditions at  $\tilde{m}$
  - RGE
- 3 Light Higgs and light Stop Masses
- 4 EW phase transition and Baryogenesis
- 5 EWBG vs Unification
- 6 Conclusions first part
- 7 Another possibility: RS
  - Supercooling
  - AdS-S/RS phase transition
- 8 Conclusions second part

# The Question: Why this asymmetry?

The Universe is matter dominated. Natural  $\bar{p}$  in the cosmic rays, but compatible with secondary production.

BBN and CMB furnish independently:

$$\eta \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.11 \pm 0.19) \times 10^{-10}$$

Why this strange number? Why not zero?

Possible mechanisms attempting to produce  $\eta$  must contain the ingredients [Sakharov,1967]

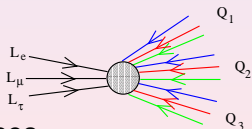
- 1 B violation
- 2 C and CP violation
- 3 Departure from thermal equilibrium

## An answer: EWBG in the SM

Kuzmin et al.,85; ...

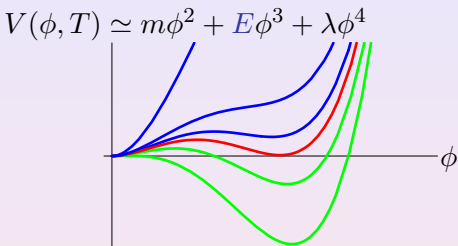
The SM contains the Sakharov conditions:

- 1 B number is non-perturbative violated at  $T \neq 0$  (sphalerons) [t Hooft,76]
- 2 CKM matrix contains CP violating phases
- 3 EWPT (when of 1<sup>st</sup> order) proceeds by bubble nucleation. Expanding bubbles break the thermal equilibrium.



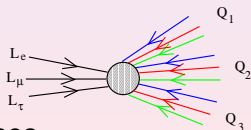
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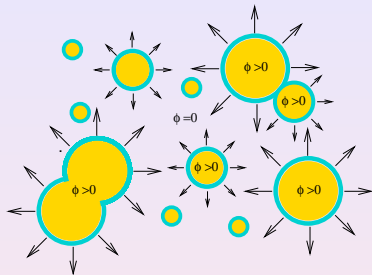
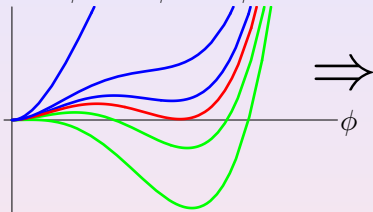
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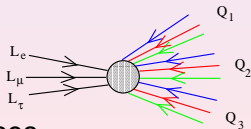
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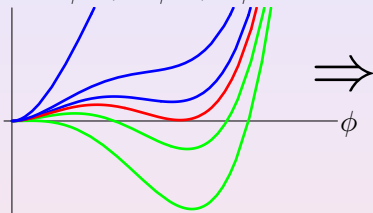
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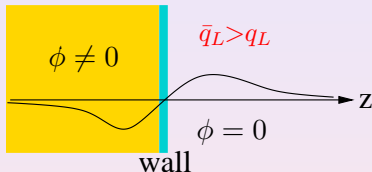
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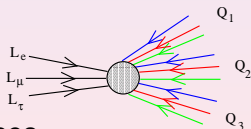


CP asymmetry



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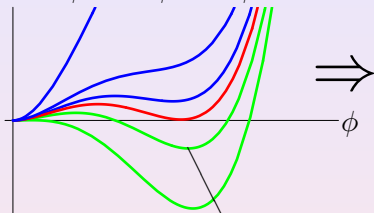
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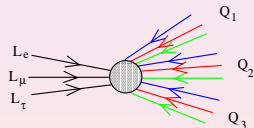
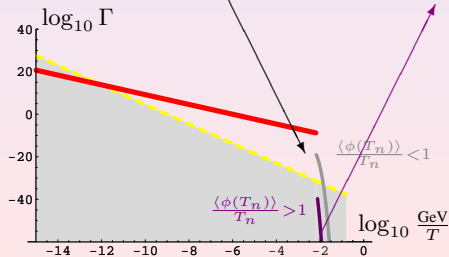
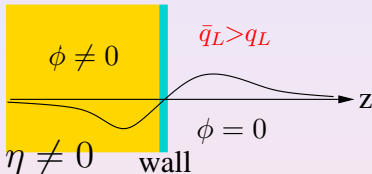
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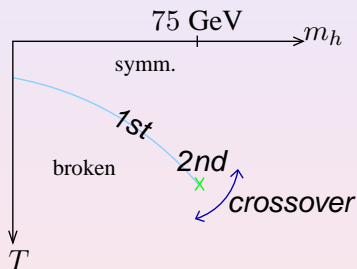




# Another answer: EWBG in the MSSM

Unluckily, EWBG in the SM does not work: the EWPT is **not strong** enough ( $\frac{\langle \phi(T_n) \rangle}{T_n} < 1$ ) since  $m_h > 114.4$  GeV [LEP].

[Kajantie et al.,97]



$\Rightarrow$  New physics to modify the  $V(\phi, T)$ .

Well motivated possibility: EWBG in the **MSSM**.

## State of the art ( < 2008)

In the MSSM the EWPT was strong enough in the **Light Stop Scenario** ( $m_{\tilde{t}_R} < m_t$ ) [Carena et al.,96;Delepine et al.,96;Cline et al.,98], but the analysis was performed for  $m_h \gtrsim 65$  GeV.

In the case of large  $m_A$  (SM-like Higgs), the parameter region useful for  $v(T)/T \gtrsim 1$  can be translated in a window of  $m_{\tilde{t}_R}$  versus  $m_h$ .

Some considerations about that window are relevant:

- If  $M_Q$  is a **few TeV**, the window is **jeopardized** by the present Higgs experimental bound ( $m_h > 114.4$  GeV).
- $m_h$  was calculated in the **1-loop** approximation.



*Thesis aim: what happens whether*

More precision in the  $m_h$  calculation?

Larger  $M_Q$ ?

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# LSS Framework

The main features of the LSS spectrum are:

- Fermions are at the EW scale (gluino may be a bit heavy)
- The  $\tilde{t}_R$  is lighter than the top quark
- The other scalars  $M_Q \simeq m_A \simeq \dots \equiv \tilde{m} \gg \text{few TeV}$
- $A_t \ll \tilde{m}$  (motivated by the strength of the EWPT)

(A sort of light-stop scenario in SS)

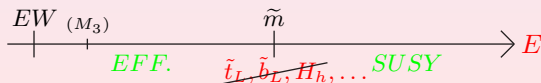


## LOW ENERGY EFFECTIVE THEORY

## LE Lagrangian

The effective Lagrangian is

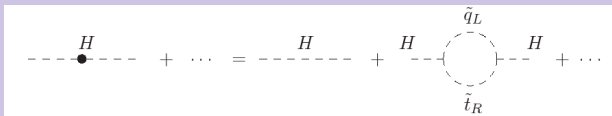
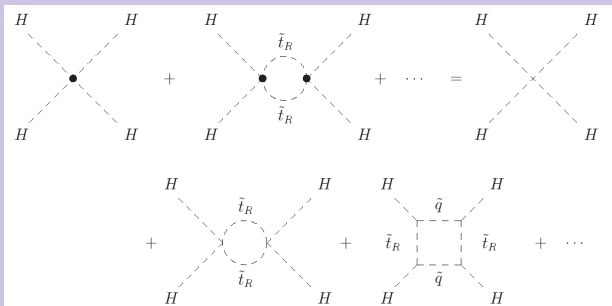
$$\begin{aligned}
 \mathcal{L}_{eff} = & m^2 H^\dagger H - \frac{\lambda}{2} (H^\dagger H)^2 - h_t [\bar{q}_L \epsilon H^* t_R] + Y_t \left[ \bar{H}_u \epsilon q_L \tilde{t}_R^* \right] \\
 & - \sqrt{2} G \Theta_{\tilde{g}} \tilde{t}_R \tilde{g}^a \bar{T}^a \bar{t}_R + \sqrt{2} J \tilde{t}_R^* \tilde{B} t_R - \frac{1}{6} K \tilde{t}_{R\omega}^* \tilde{t}_{R\omega} \tilde{t}_{R\gamma}^* \tilde{t}_{R\gamma} - Q |\tilde{t}_R|^2 |H|^2 \\
 & + \frac{H^\dagger}{\sqrt{2}} \left( g_u \sigma^a \tilde{W}^a + g'_u \tilde{B} \right) \tilde{H}_u + \frac{H^T \epsilon}{\sqrt{2}} \left( -g_d \sigma^a \tilde{W}^a + g'_d \tilde{B} \right) \tilde{H}_d + \text{h.c.} \\
 & - \frac{M_3}{2} \Theta_{\tilde{g}} \tilde{g}^a \tilde{g}^a - \frac{M_2}{2} \tilde{W}^A \tilde{W}^A - \frac{M_1}{2} \tilde{B} \tilde{B} - \mu \tilde{H}_u^T \epsilon \tilde{H}_d - M_U^2 \tilde{t}_R^* \tilde{t}_R
 \end{aligned}$$



# Matching conditions at $\tilde{m}$

(One-loop:  $\overline{MS}$  - dim. regular. - Landau gauge - 4-dim. ops.)

$$\lambda(\tilde{m}) - \Delta\lambda = \frac{g^2(\tilde{m}) + g'^2(\tilde{m})}{4} \cos^2 2\beta \left( 1 - \frac{1}{2} \Delta Z_\lambda \right)$$



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$$\lambda(\tilde{m}) - \Delta\lambda = \frac{g^2(\tilde{m}) + g'^2(\tilde{m})}{4} \cos^2 2\beta \left(1 - \frac{1}{2}\Delta Z_\lambda\right)$$

$$h_t(\tilde{m}) - \Delta h_t = \lambda_t(\tilde{m}) \sin \beta \left(1 - \frac{1}{2}\Delta Z_{h_t}\right)$$

$$Q(\tilde{m}) - \Delta Q = \left(\lambda_t^2(\tilde{m}) \sin^2 \beta - \frac{1}{3} g'^2 \cos 2\beta\right) \left(1 - \frac{1}{2}\Delta Z_Q\right)$$

$$Y_t(\tilde{m}) - \Delta Y_t = \lambda_t(\tilde{m}) \left(1 - \frac{1}{2}\Delta Z_{Y_t}\right)$$

$$K(\tilde{m}) - \Delta K = \left(g_3^2(\tilde{m}) + \frac{4}{3} g'^2(\tilde{m})\right) \left(1 - \frac{1}{2}\Delta Z_K\right)$$

$$G(\tilde{m}) - \Delta G = g_3(\tilde{m}) \left(1 - \frac{1}{2}\Delta Z_G\right)$$

$$J(\tilde{m}) = \frac{2}{3} g'(\tilde{m}), \quad g_u(\tilde{m}) = g(\tilde{m}) \sin \beta, \quad g_d(\tilde{m}) = g(\tilde{m}) \cos \beta,$$

$$g'_u(\tilde{m}) = g'(\tilde{m}) \sin \beta, \quad g'_d(\tilde{m}) = g'(\tilde{m}) \cos \beta$$

## RGE

For the adimensional couplings...

$$(4\pi)^2 \beta_\lambda = 12\lambda^2 + 6Q^2 - 12h_t^4 + 12h_t^2\lambda$$

$$(4\pi)^2 \beta_{h_t} = h_t \left( \frac{9}{2}h_t^2 + \frac{1}{2}Y_t^2 + \frac{4}{3}G^2 - 8g_3^2 \right)$$

$$(4\pi)^2 \beta_Q = -\frac{32}{3}G^2 h_t^2 - 4Y_t^2 h_t^2 + Q \left( K + 3\lambda + 4Q + 6h_t^2 + 4Y_t^2 + \frac{16}{3}G^2 - 8g_3^2 \right)$$

$$(4\pi)^2 \beta_{Y_t} = \frac{1}{2}Y_t \left( h_t^2 + 8Y_t^2 + \frac{16}{3}G^2 - 8g_3^2 \right)$$

$$(4\pi)^2 \beta_K = 12Q^2 + 13g_3^4 - \frac{88}{3}G^4 - 24Y_t^4 + K \left( \frac{14}{3}K + 8Y_t^2 + \frac{32}{3}G^2 - 16g_3^2 \right)$$

$$(4\pi)^2 \beta_G = \frac{1}{2}G (9G^2 + 2h_t^2 - 26g_3^2 + 4Y_t^2)$$

$$(4\pi)^2 \beta_J = J \left( h_t^2 + 2Y_t^2 + \frac{12}{3}G^2 - 4g_3^2 \right)$$

$$(4\pi)^2 \beta_{g_u(\prime)} = g_u(\prime) \left( 3h_t^2 + \frac{3}{2}Y_t^2 \right), \quad (4\pi)^2 \beta_{g_d(\prime)} = 3g_d(\prime) h_t^2,$$



## RGE

... and for the mass terms

$$(4\pi)^2 \beta_{M_1} = 0$$

$$(4\pi)^2 \beta_{M_2} = 0$$

$$(4\pi)^2 \beta_m = -6Q m_U^2 + 6m^2 h_t^2$$

$$(4\pi)^2 \beta_\mu = \frac{3}{2} \mu Y_t^2$$

$$(4\pi)^2 \beta_{M_3} = M_3 (-18g_3^2 + G^2)$$

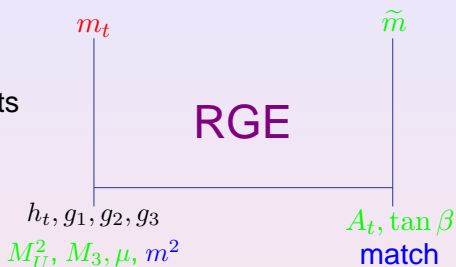
$$(4\pi)^2 \beta_{M_U^2} = M_U^2 \left( \frac{8}{3} K + 4Y_t^2 + \frac{16}{3} G^2 - 8g_3^2 \right) - \frac{32}{3} M_3^2 G^2 - 4m^2 Q - 4Y_t^2 \mu^2$$

- Checked by the SUSY and SS limits

# Higgs mass calculation

INPUTS:

- Experimental LE inputs
- Theoretical inputs
- Free parameters

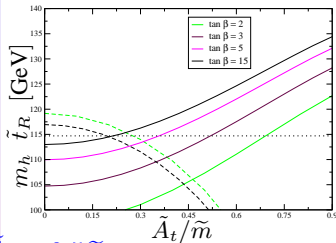


HIGGS MASS:

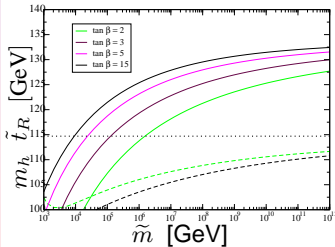
by the 1-loop effective potential in the LE theory improved by the 1-loop RGE resummation (necessary to resum large logs for large values of  $M_Q$ )

## Higgs and stop mass

$$\tilde{m} = 100 \text{ TeV}$$

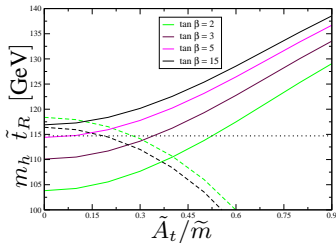


$$\tilde{A}_t = 0.5\tilde{m}$$



$$M_U^2 = -(100)^2 \text{ GeV}^2$$

$$\tilde{m} = 1000 \text{ TeV}$$



$$m_h \lesssim 133 \text{ GeV}$$

$$m_{\tilde{t}_R} \lesssim 120 \text{ GeV}$$

( $\tilde{m} < 10 \text{ TeV} + \tan\beta < 5 + \text{EWBG}$ ) difficult

# Why $M_U^2 < 0$ ? Basic idea [Carena et al.,96]

To obtain a **strong** 1<sup>st</sup> order EW transition ( $\langle \phi(T_n) \rangle > T_n$ ), the Higgs potential ( $V(\phi, T) \simeq m\phi^2 + E\phi^3 + \lambda\phi^4$ ) has to develop a **large barrier** ( $E \uparrow$ ), increased by the “**cubic term**” produced by **bosons**.

Unlike in the SM (developing a small cubic term), in our LE theory the Stop could strengthen the EW transition. Its **spurious** cubic term appears as

$$\left[ M_U^2 + \frac{Q}{2} \phi^2 + \Pi(T) \right]^{3/2} \quad Q \sim (1 - \tilde{A}_t/\tilde{m})$$

To strengthen the transition  $M_U^2 \approx -\Pi(T_c)$  so that  $[\dots]^{3/2} \sim E\phi^3$

The theory then has two minima!

EWB  
 $\langle h, \hat{t} \rangle = (v, 0)$

CB  
 $\langle h, \hat{t} \rangle = (0, u)$

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**CB**

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# Potentials and possible transitions

Starting from the symmetric phase (SP), since  $M_U^2 < 0$ :

- If  $(T_{SP \rightarrow CB}^n > T_{SP \rightarrow EWB}^n) + (\langle V_h \rangle > \langle V_{\tilde{t}} \rangle)$  NO
- If  $(T_{SP \rightarrow CB}^n > T_{SP \rightarrow EWB}^n) + (\langle V_h \rangle < \langle V_{\tilde{t}} \rangle)$  NO [Cline et al,99]
- If  $(T_{SP \rightarrow CB}^n < T_{SP \rightarrow EWB}^n) + (\langle V_h \rangle < \langle V_{\tilde{t}} \rangle)$  OK
- If  $(T_{SP \rightarrow CB}^n < T_{SP \rightarrow EWB}^n) + (\langle V_h \rangle > \langle V_{\tilde{t}} \rangle)$  ?

At  $T \neq 0$  we consider the 2-loop effective potential in the LE theory taking into account only the effective couplings  $\sim g_3, \lambda_t$ .

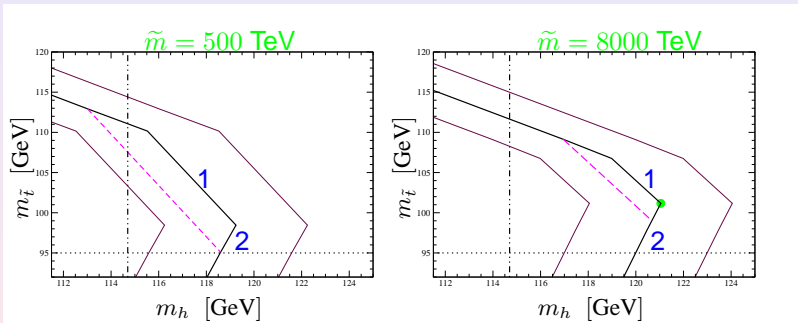


tree-level:  $m_h, m_{\tilde{t}}, m_U^2$  ( $Q, \lambda$ )  
 radiative: other couplings

# Higgs-Stop window $\langle \phi(T_c) \rangle / T_c > 0.9$ ( $\mu = 100, M_3 = 500$ )

Condt. 1:  $\tan \beta \lesssim 15$  good for EDM and BAU.

Condt. 2: If  $T_h^c \geq T_{\tilde{t}}^c + 1.6 \text{ GeV} \Rightarrow T_{SP \rightarrow CB}^n < T_{SP \rightarrow EWB}^f$



Only effect. parameters are important

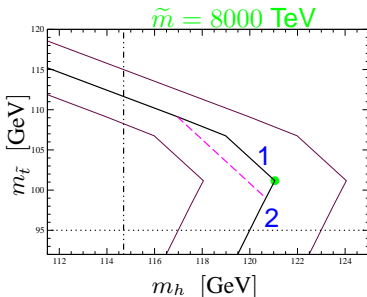
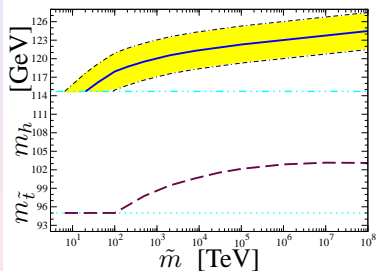
Condt. 1 strongly restricts the window, but the similar  $(m_h, m_{\tilde{t}}, M_U^2)$  can be often obtained by lower  $\tan \beta$  in a higher  $\tilde{m}$  scenario where only less important couplings are different



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EWBG bounds (upper uncertainty):

$$m_h \lesssim 127 \text{ GeV}$$

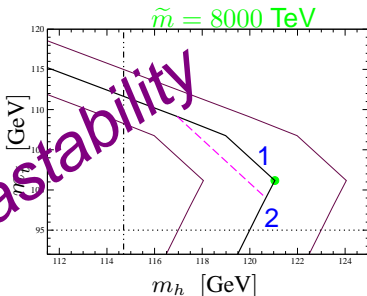
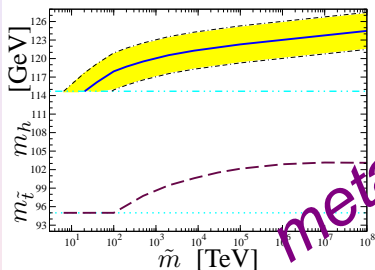
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$$\tilde{m} \gtrsim 7 \text{ TeV}$$

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$$\tilde{m} \gtrsim 7 \text{ TeV}$$

# Condition 1: $\tan \beta \leq 15$

- EDM: one-loop predominates ( $\tilde{m} \gtrsim 10$  TeV), roughly [Chang et al.,99]

$$d_e \lesssim d_e^{exp} \tan \beta / 15 \quad (\tilde{m} \approx 10 \text{ TeV})$$

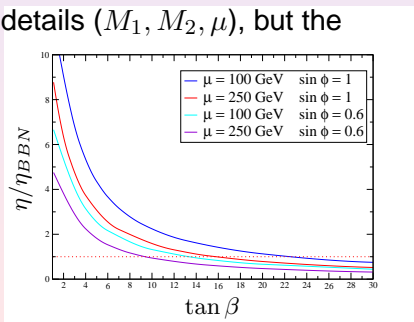
- BAU: fixing  $\langle h \rangle_{T_n} / T_n = 1$  [Carena et al.,01]

Calculation strongly depends on details ( $M_1, M_2, \mu$ ), but the windows do weakly depend



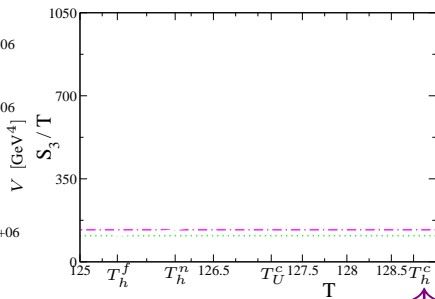
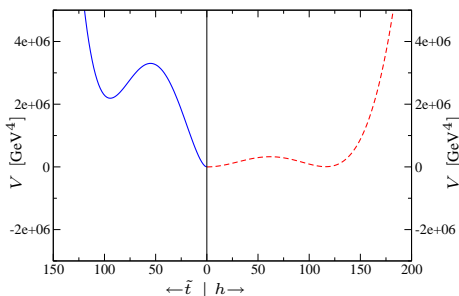
Good choice:  $\tan \beta \leq 15$

Very conservative:  $\tan \beta \leq 5$



$$\text{Condition 2: } T_h^c \geq T_{\tilde{t}}^c + 1.6 \text{ GeV} \Rightarrow T_{SP \rightarrow CB}^n < T_{SP \rightarrow EWB}^f$$

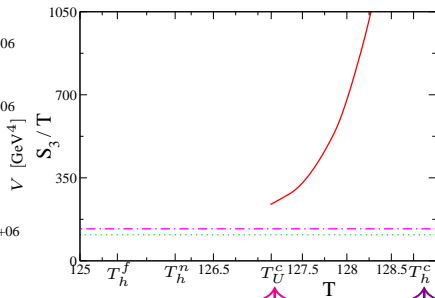
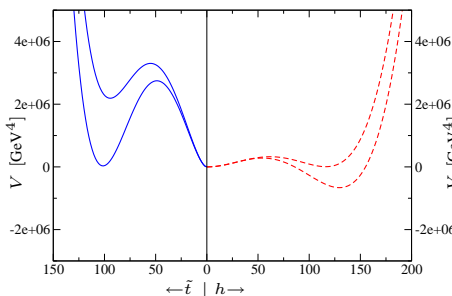
$$\text{Nucl: } S_3/T \approx 135 \quad \text{End: } S_3(T_f)/T_f \approx 110$$



- At  $T = T_c^{EWB} = 128.7$  GeV:  $S_{SP \rightarrow EWB}$  and  $S_{SP \rightarrow CB}$  are infinite
- 
- 
-

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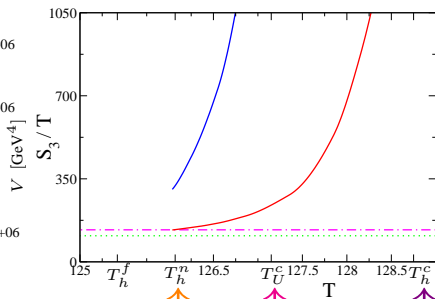
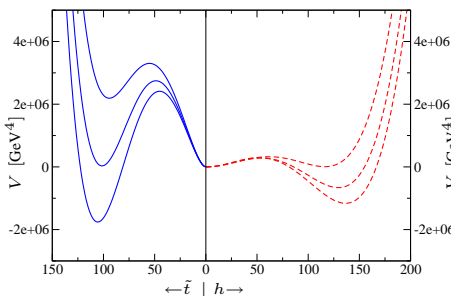
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- At  $T = T_c^{CB} = 127.1 \text{ GeV}$ :  $S_{SP \rightarrow CB}$  too large and  $S_{SP \rightarrow CB}$  infinite
- 
-

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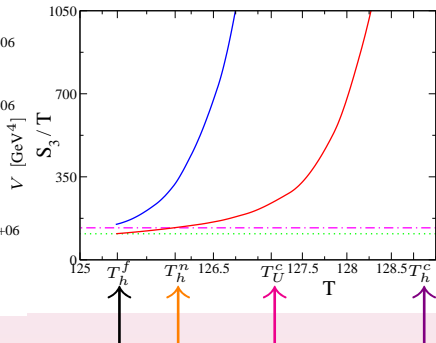
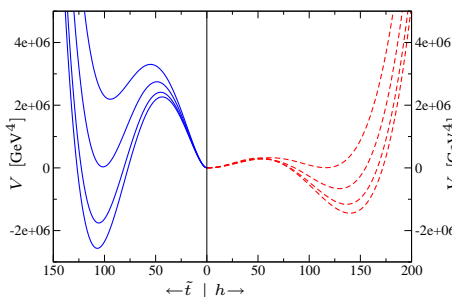
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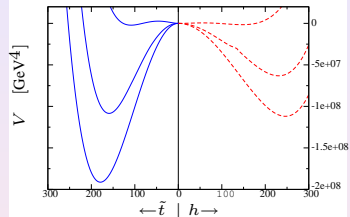
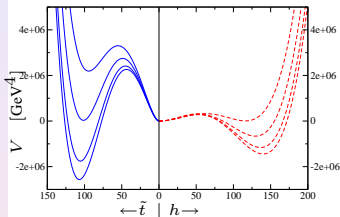
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- At  $T = T_f = 125.4 \text{ GeV}$ :  $S_{SP \rightarrow EWB} = 110$  and  $S_{SP \rightarrow CB} > 135$

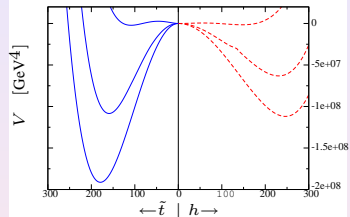
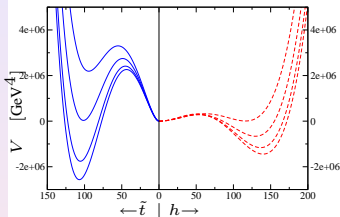
# Metastability

Is the transition  $\text{EWB} \rightarrow \text{CB}$  possible ?



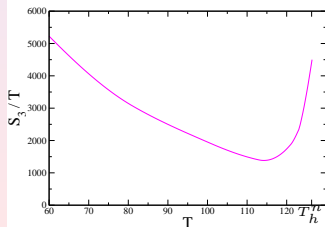


## Metastability

Is the transition  $EWB \rightarrow CB$  possible ? NO

$$S_{EWB \rightarrow CB} \gg 135$$

IT DOESN'T DECAY !



# Gauge Coupling Unification

EWBG suggests  $\tilde{m} \gg \text{TeV}$ . Large modif. from the usual parameter region of the MSSM, which unifies.

EWBG compatible with unification?

$$(4\pi)^2 \frac{d}{dt} g_i = g_i^3 b_i + \frac{g_i^3}{(4\pi)^2} \left[ \sum_{j=1}^3 B_{ij} g_j^2 - d_i^u h_t^2 - d_i^G G^2 - d_i^J J^2 - \dots \right]$$

$$g_1^2 = (5/3) g'^2$$

$$b^{LSS} = \left( \frac{143}{30}, -\frac{7}{6}, -\frac{41}{6} + 2\Theta_{\tilde{g}} \right)$$

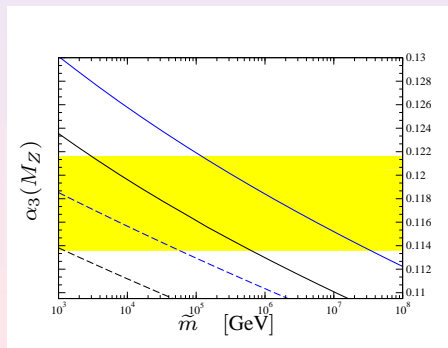
$$b^{SUSY} = \left( \frac{33}{5}, -2, -3 \right)$$

$m_Z$   
 $\tilde{m}$   
 $M_{GUT}$

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EWBG compatible with unification? YES



1- $\sigma$  prediction:

$$M_3 = 500 \text{ GeV:}$$

$$\tilde{m} = 10^{3.3 \pm 0.6} \text{ TeV}$$

$$M_3 = 150 \text{ GeV:}$$

$$\tilde{m} = 10^{1.6 \pm 0.6} \text{ TeV}$$

# Conclusions first part

## Effective Theory

- By using appropriate RGE and matching conditions, we have computed the LE effective theory in the LSS in a reliable manner for very high  $\tilde{m}$ .
- We have calculated  $m_h$  using the effective potential improved by the RGE and we find  $m_h \lesssim 133$  GeV for  $M_U^2 < 0$ .

## EWBG

- We have improved on the determination of the  $m_h - m_{\tilde{t}}$  strong-transition window that permits to explore higher scales  $\tilde{m}$ .
- We observe that for  $\tilde{m} \gtrsim 7$  TeV the window is in agreement with BAU.
- The parameters for EWBG imply an EW metastable vacuum that we have checked not to decay.
- Bounds:  $m_h \lesssim 127$  GeV and  $m_{\tilde{t}_R} \lesssim 120$  GeV.
- EWBG in the LSS compatible with GUT.

## Another possibility

If we are not able to modify the barrier of the Higgs effective potential...

...we try to change the nucleation temperature of the EWPT !

## Another possibility

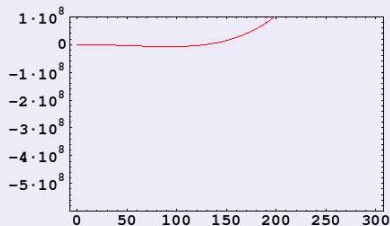
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## ...if there would be a supercooling...

If supercooling is efficient, in the SM  $\langle\phi(T)\rangle \rightarrow v$  when  $T \ll T_{EWPT}$  and easily  $\langle\phi(T)\rangle/T \gg 1$ .

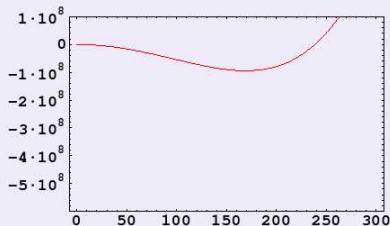
At one-loop with  $m_H = 250\text{GeV}$ ,  $T \simeq 305\text{GeV}$  and  $\langle\phi(T)\rangle/T \sim 0.3$



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At one-loop with  $m_H = 250\text{GeV}$ ,  $T \simeq 250\text{GeV}$  and  $\langle\phi(T)\rangle/T \sim 0.7$

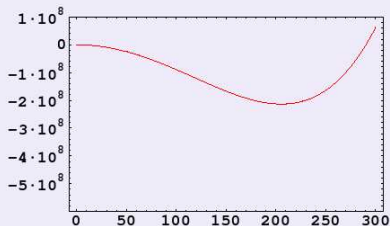




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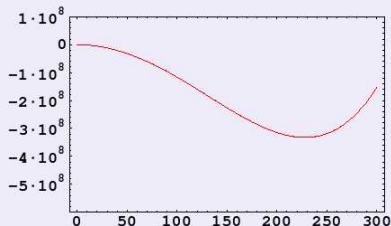
At one-loop with  $m_H = 250\text{GeV}$ ,  $T \simeq 200\text{GeV}$  and  $\langle\phi(T)\rangle/T \sim 1$



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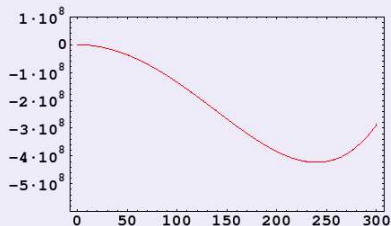
At one-loop with  $m_H = 250\text{GeV}$ ,  $T \simeq 150\text{GeV}$  and  $\langle\phi(T)\rangle/T \sim 1.5$



## ...if there would be a supercooling...

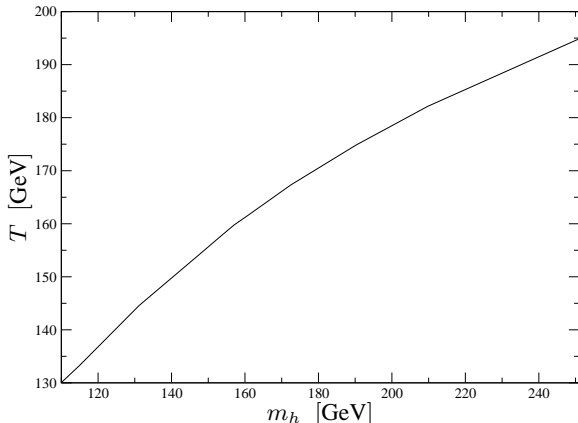
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At one-loop with  $m_H = 250\text{GeV}$ ,  $T \simeq 100\text{GeV}$  and  $\langle\phi(T)\rangle/T \sim 2.4$



## ...if there would be a supercooling...

If supercooling is efficient, in the SM  $\langle\phi(T)\rangle \rightarrow v$  when  $T \ll T_{EWPT}$  and easily  $\langle\phi(T)\rangle/T \gg 1$ .



# AdS-S/RS phase transition

Another possibility appears in **warped spaces** with the Higgs localized in the IR brane

- The **radion**  $\mu(x)$  VEV which fixes the distance between the UV and IR branes will play a major role in the phase transition
- At **high temperatures** ( $\mu \sim 0$ ) the space is AdS and the IR brane is replaced by a **black hole horizon** (AdS-S) [Witten,98]

## AdS/CFT correspondence

At high  $T$  IR brane does not exist  $\Leftrightarrow$  Deconfined (phase) Higgs [ $\sim h$  does not exist]

- At temperature  $T_n$  ( $\mu \neq 0$ ) the IR brane is nucleated from the horizon and the space is RS

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IR brane nucleated  $\Leftrightarrow$  Confined (phase) Higgs [ $\sim h$  exists]

For earlier studies of the radion phase transition see <sup>1</sup>

### Essential observation

At the typical nucleation temperatures  $T_n$  the SM potential is a little perturbation of the radion potential and should not alter the bounce solution and the corresponding Euclidean action that governs the radion phase transition.

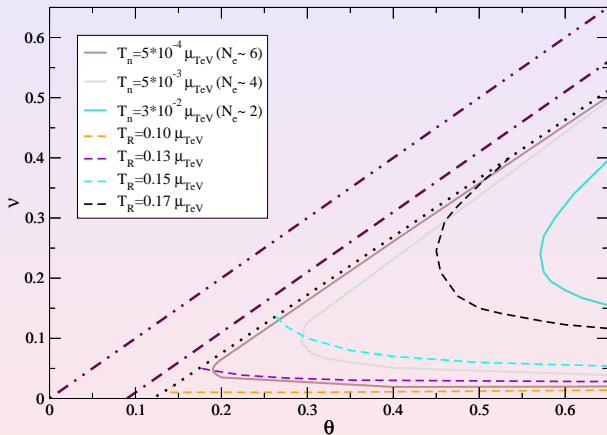
The radion potential has a large barrier and its transition transition is supercooled  $T_n \ll T_c \lesssim \mu_{TeV}$ .

Since  $T_n < T_{EW}$ , the Higgs “appears” when  $\langle \phi(T) \rangle > T$ . The EWPT is supercooled!

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<sup>1</sup>Creminelli et al.,01; Randall et al.,06; Kaplan et al.,06. 



Example: parameter region for  $N=3$ 

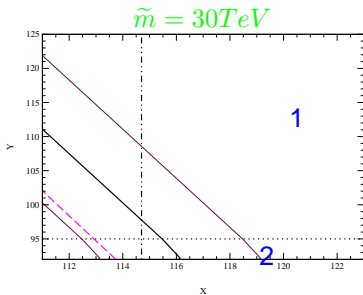
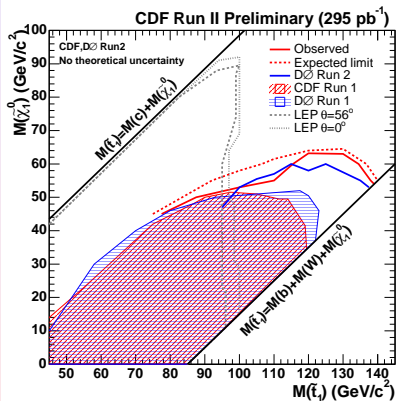
# Conclusion second part

- Supercooling strengthens the EWPT appreciably
- In RS (with GW) the EWPT is strong
- ...more details during the discussion of the next week or privately

# Higgs-Stop window $\langle h \rangle_{T_c} / T_c > 1$ ( $\mu = 100, M_3 = 500$ )

Condt. 1:  $\tan \beta \lesssim 10$  good for EDM and BAU.

Condt. 2: If  $T_h^c \geq T_{\tilde{t}}^c + 2 \text{ GeV} \Rightarrow T_{SP \rightarrow CB}^n < T_{SP \rightarrow EWB}^n$



to  $m_h \approx 127 \text{ GeV}!!!$

low, but the same  $(m_h, m_{\tilde{t}}, M_U^2)$   
 $\beta$  in a higher  $\tilde{m}$  scenario where

only less important couplings are different

THANKS FOR  
THE  
ATTENTION