

## Screening Dark Energy

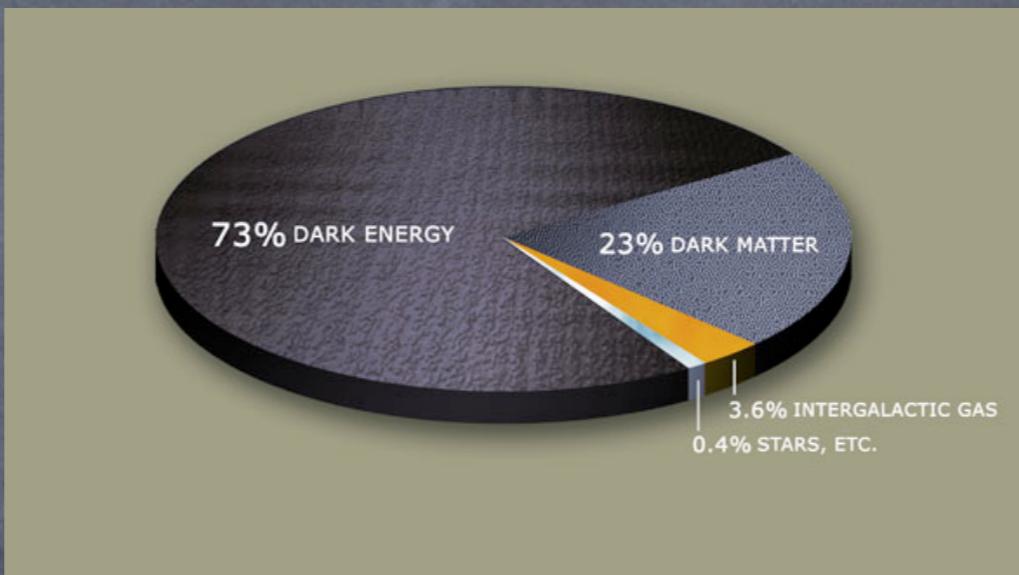
Justin Khoury (UPenn)

K. Hinterbichler & J. Khoury, Phys. Rev. Lett. 104, 231301 (2010)

B. Jain & J. Khoury, Annals Phys. 325, 1479 (2010)

A. Levy, A. Matas, K. Hinterbichler and J. Khoury, in progress

# The Era of Precision Uncertainty

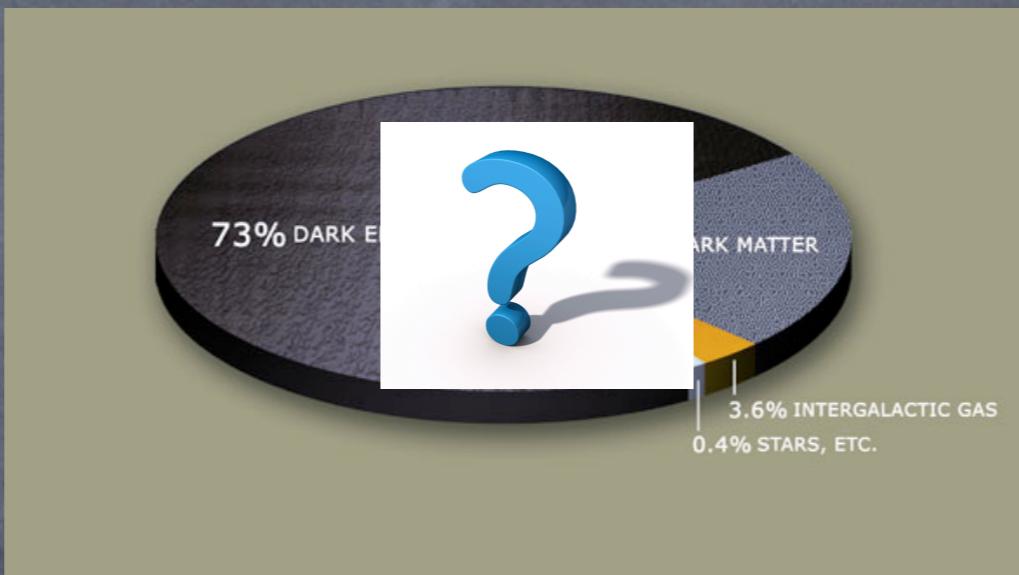


$$\Omega_b h^2 = 0.02260 \pm 0.0053; \quad \Omega_c h^2 = 0.1123 \pm 0.0035;$$

$$\Omega_\Lambda = 0.728 \pm 0.016 \quad n_s = 0.963 \pm 0.012;$$

$$\tau = 0.087 \pm 0.014; \quad \Delta_{\mathcal{R}}^2 = (2.441 \pm 0.090) \times 10^{-9}$$

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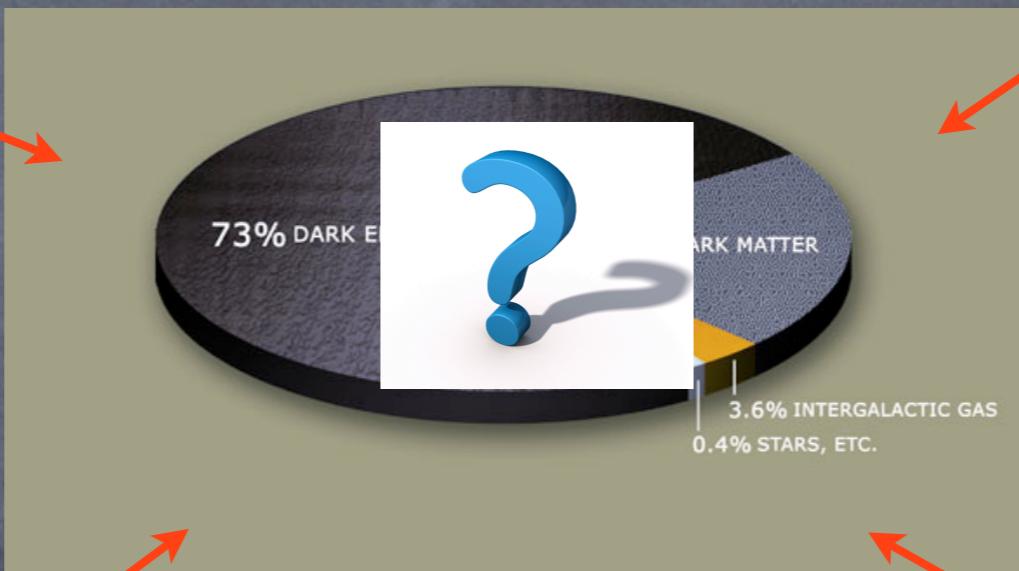
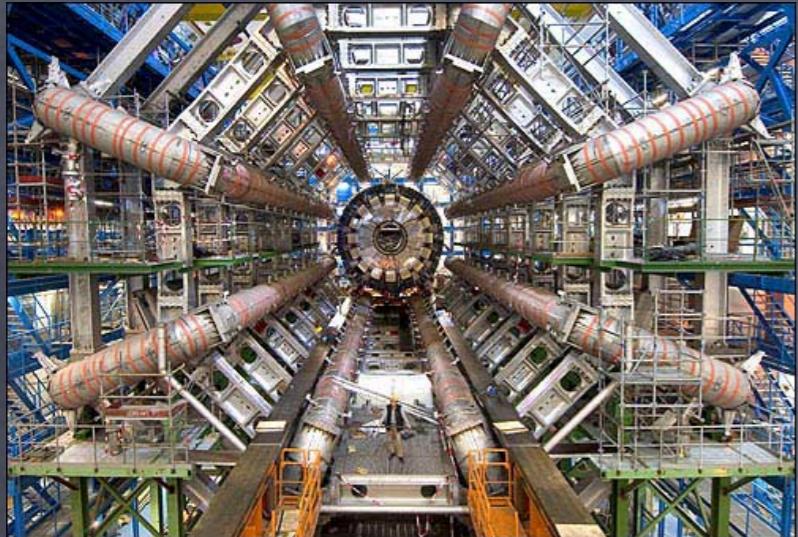


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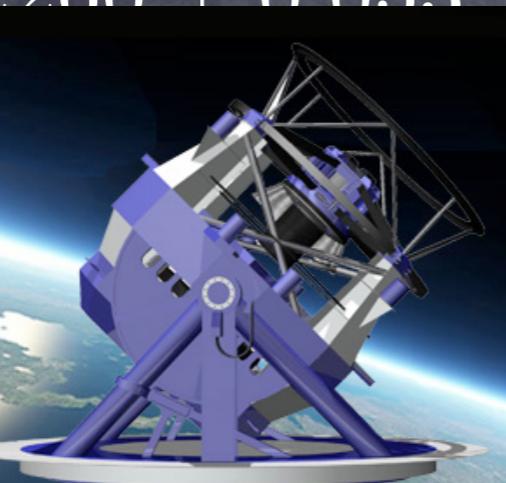
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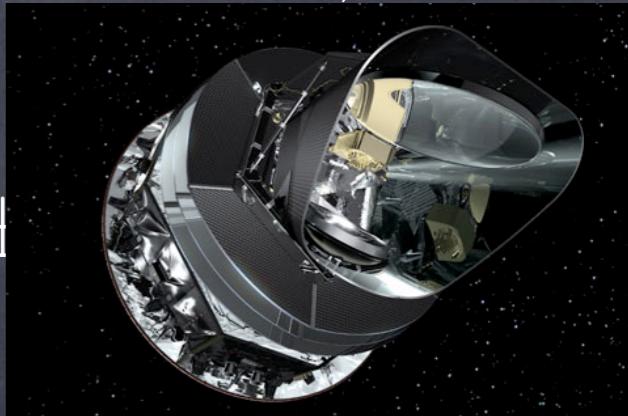
# The Era of Precision Uncertainty



$$\Omega_b h^2 = 0.02260 + 0.053 \cdot$$



$$\Omega_m h^2 = 0.1192 \pm 0.0035;$$



# The end of cosmology?

30 Oct 1998

## IS COSMOLOGY SOLVED? An Astrophysical Cosmologist's Viewpoint

P. J. E. Peebles

*Joseph Henry Laboratories, Princeton University,  
and Princeton Institute for Advanced Study*

### ABSTRACT

We have fossil evidence from the thermal background radiation that our universe expanded from a considerably hotter denser state. We have a well defined, testable, and so far quite successful theoretical description of the expansion: the relativistic Friedmann-

“Does  $\Lambda$ CDM signify completion of the fundamental physics that will be needed in the analysis of ... future generations of observational cosmology? Or might we only have arrived at the simplest approximation we can get away with at the present level of evidence?”

- Prof. P. J. E. Peebles



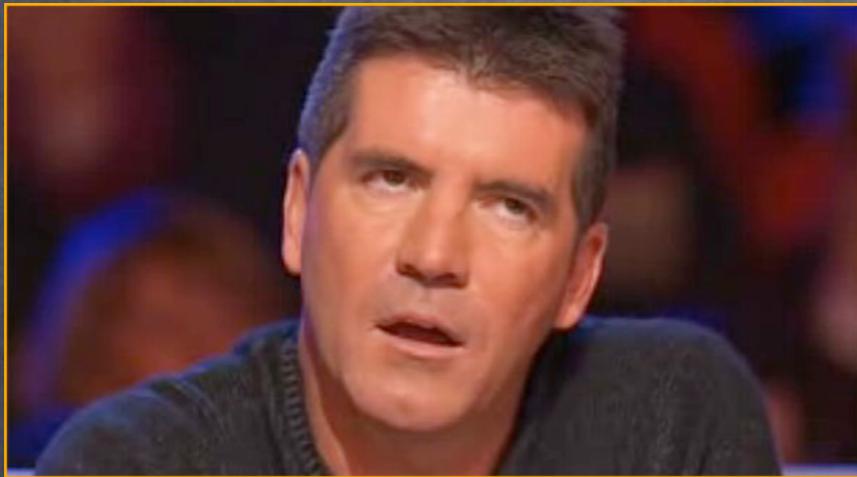
Said differently...

...will convergence to  $\Lambda$ CDM continue?

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...will convergence to  $\Lambda$ CDM continue?

Or are we in for a BIG surprise?



Cosmologist



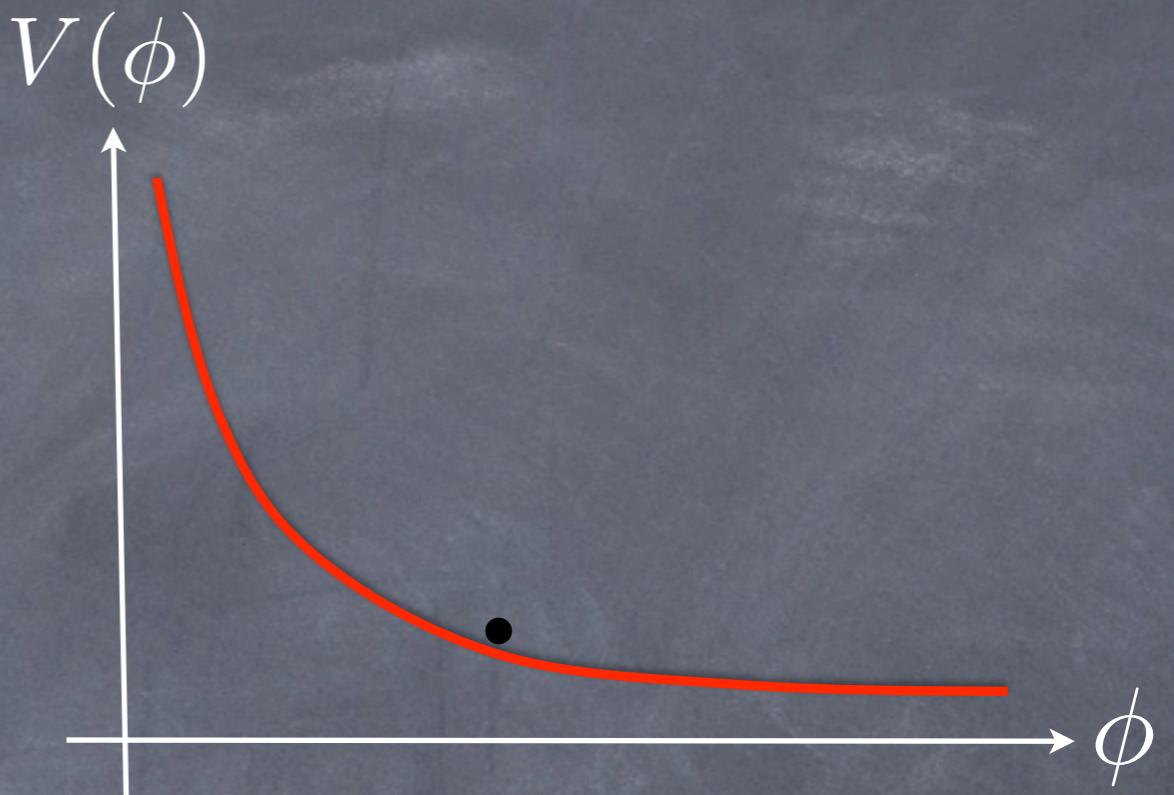
Mother Nature

# A Richer Dark Sector

- Dark energy candidates:

$\Lambda$ , quintessence...

Ratra & Peebles (1988); Wetterich (1988);  
Caldwell, Dave & Steinhardt (1998)

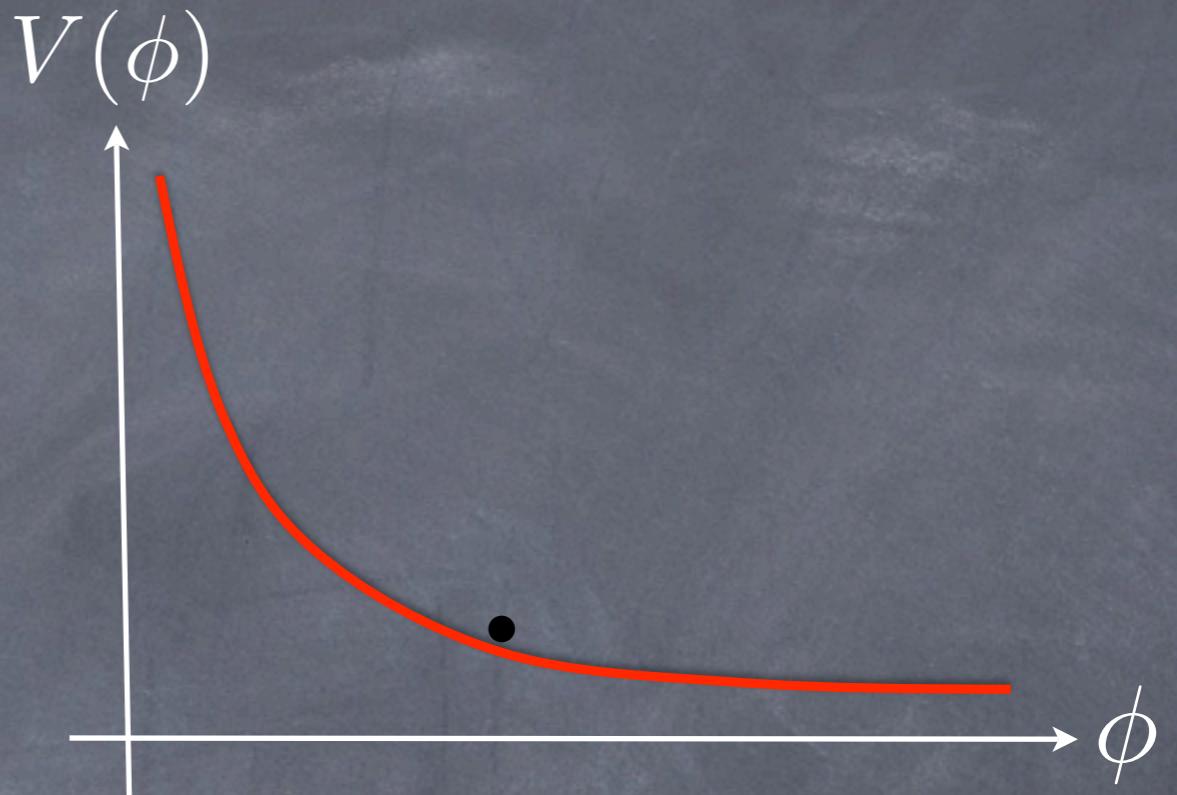


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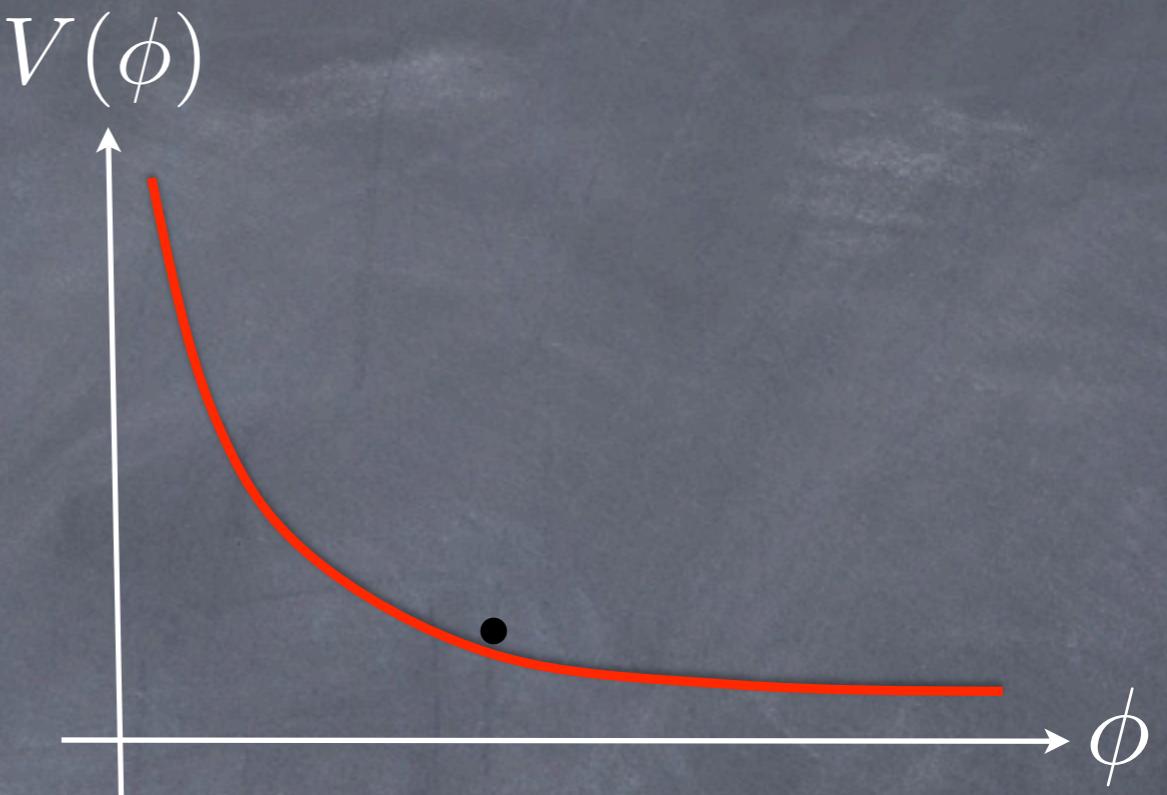
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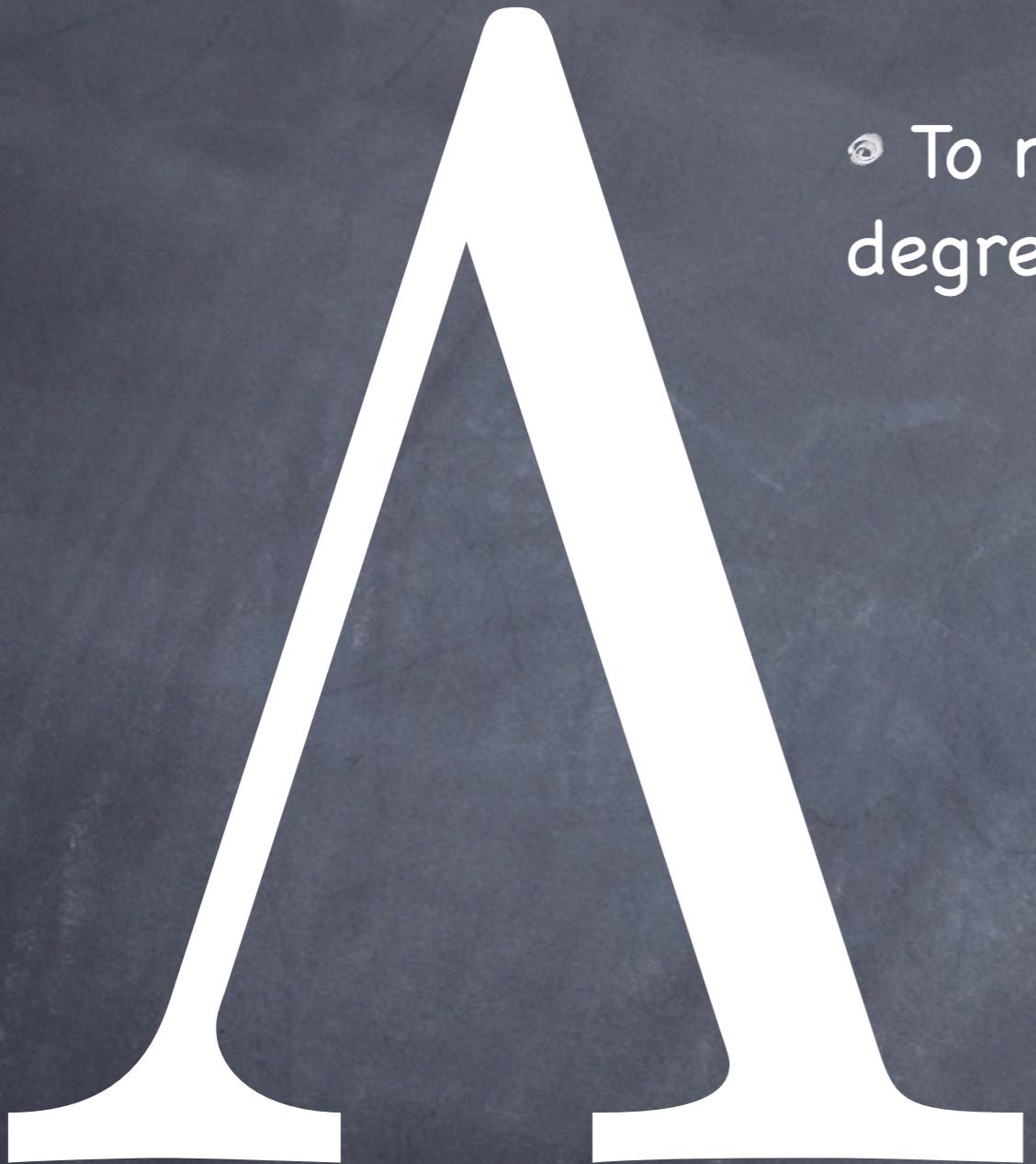
Not so fast. Scalar fields can “hide” themselves from local experiments through **screening mechanisms**

$$\rho_{\text{here}} \sim 10^{30} \rho_{\text{cosmos}}$$

New Scale = New Physics?



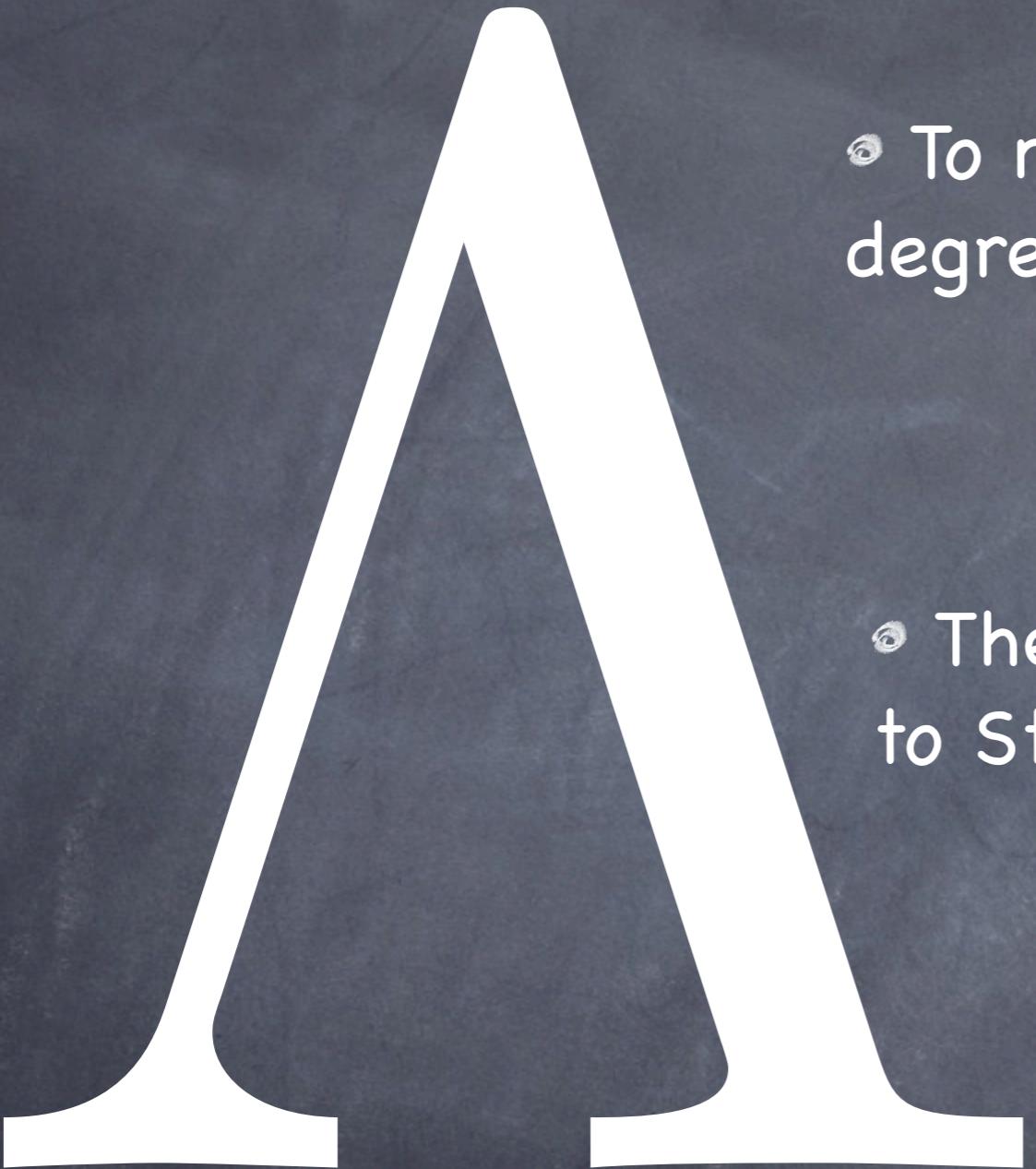
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$$m_\phi \lesssim H_0$$

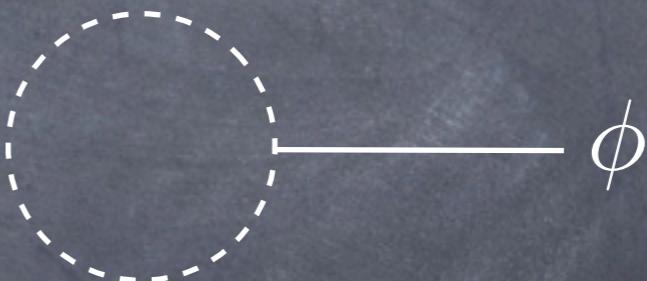
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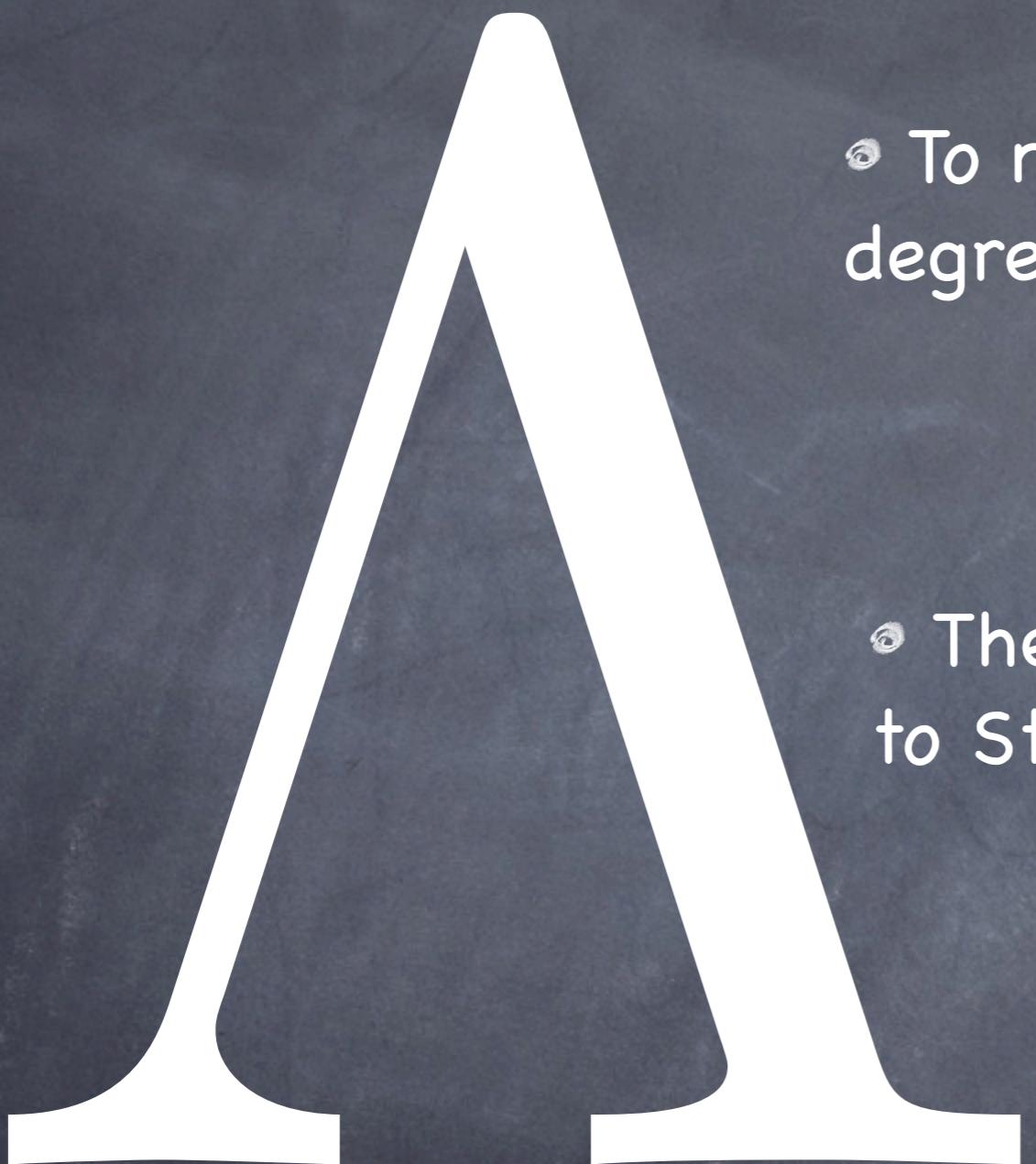
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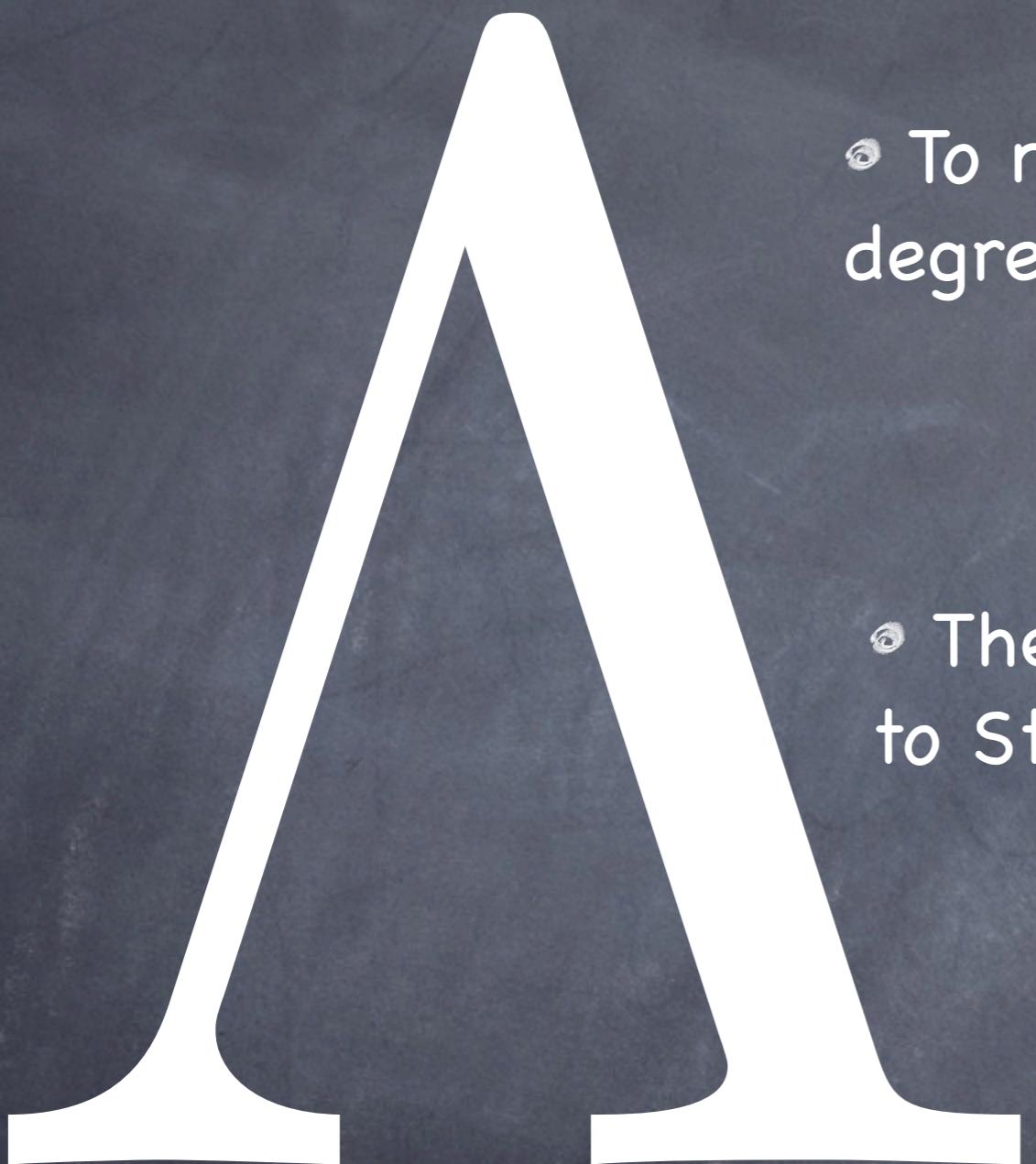
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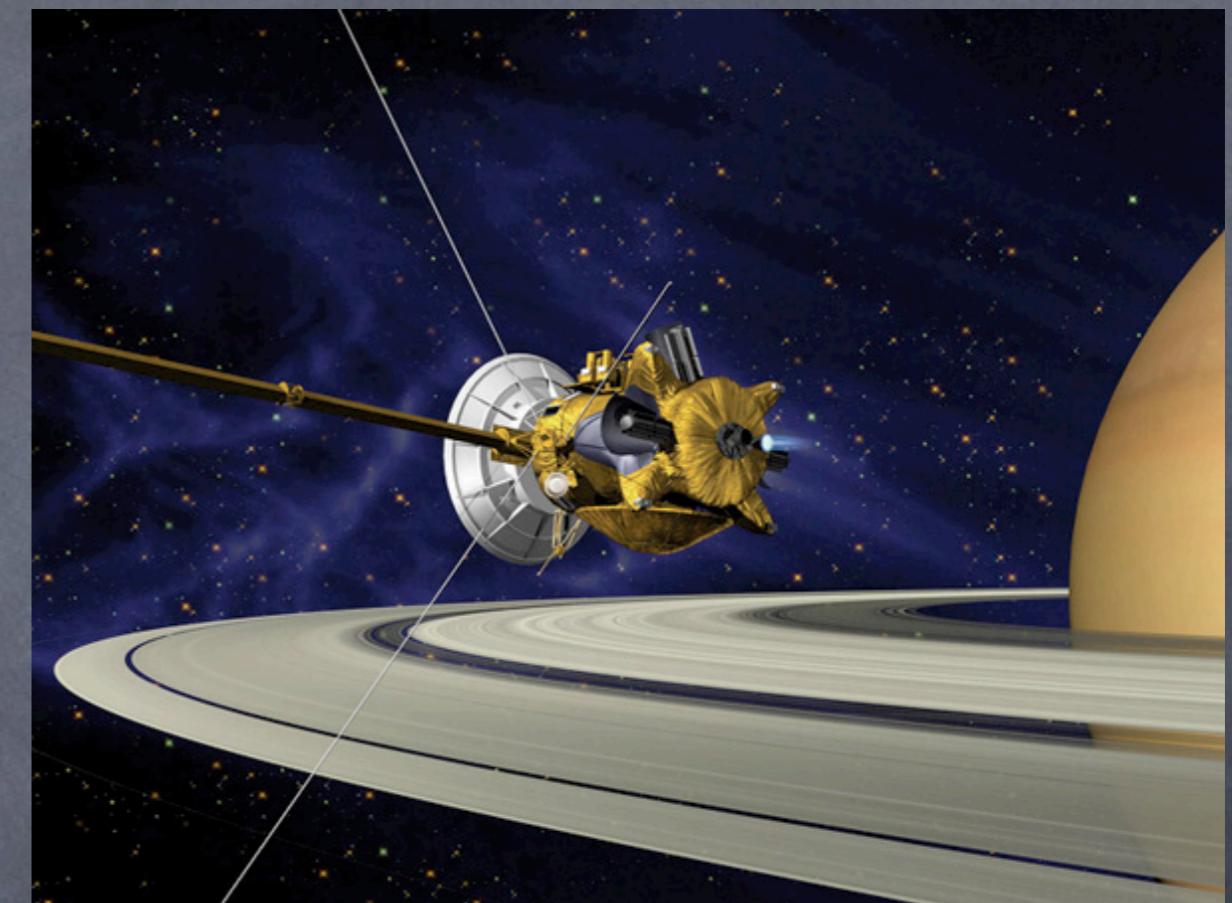
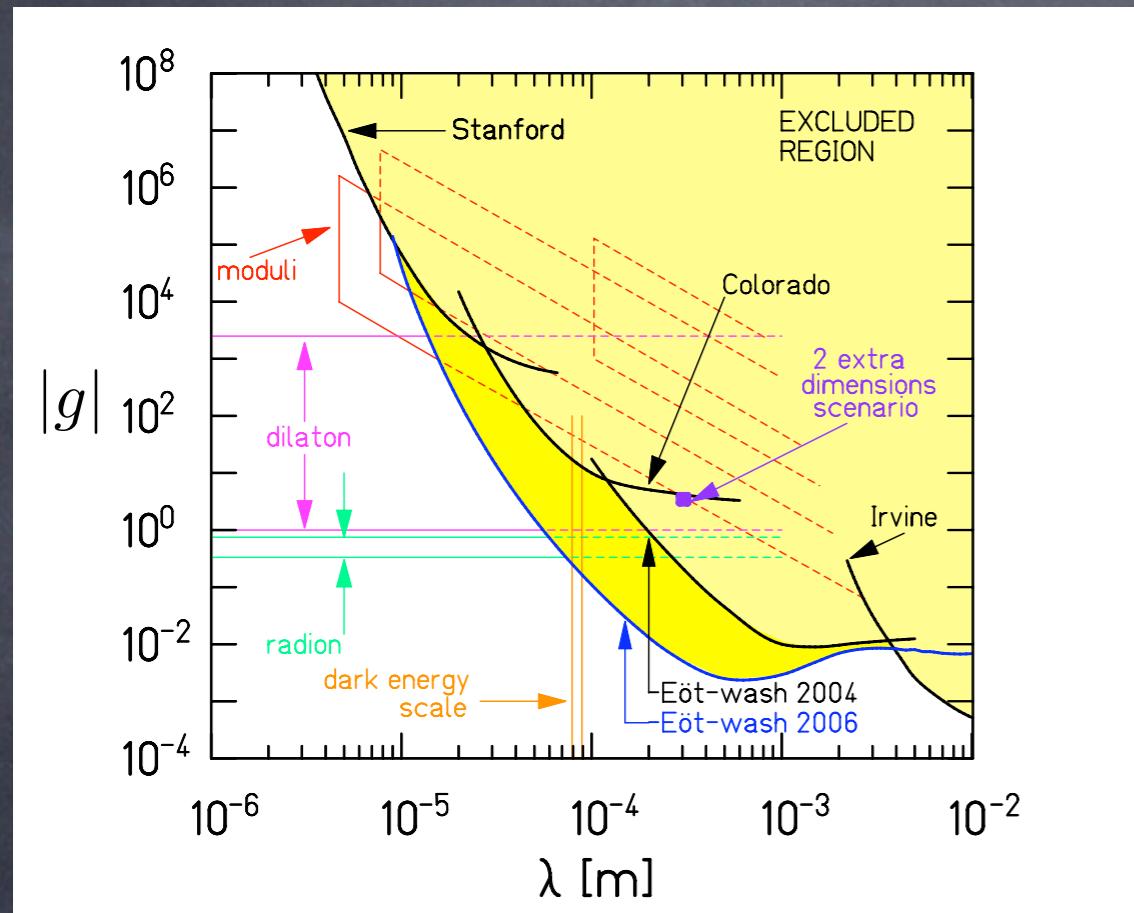
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Must rely on screening mechanism for consistency with local tests of GR

# Experimental Program

$$U(r) = -g \frac{M}{8\pi M_{\text{Pl}}^2} \frac{e^{-r/\lambda}}{r}$$



**Screening mechanisms** invariably lead to small but potentially measurable effects in the solar system and/or in the lab

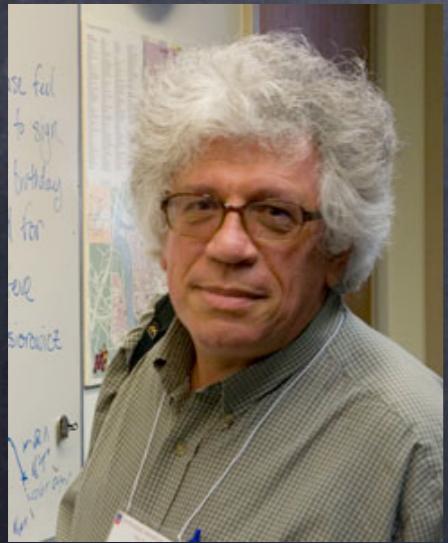
$$\nabla^2\phi+m^2\phi=-\frac{g}{M_{\rm Pl}}T^\mu{}_\mu$$

$$\nabla^2\phi+m^2\phi=\frac{g}{M_{\rm Pl}}\rho$$

$$\nabla^2 \phi + M^2(\rho) \phi = -\frac{g}{M_{\text{Pl}}} \rho$$



$$K(\rho) \nabla^2 \phi + m^2 \phi = \frac{g}{M_{\text{Pl}}} \rho$$



$$\nabla^2 \phi + m^2 \phi = \frac{g(\rho)}{M_{\text{Pl}}} \rho$$



symmetron

# Chameleon Mechanism

J. Khouri & Weltman, Phys. Rev. Lett. (2004);  
Gubser & J. Khouri, (2004)



Consider scalar field  $\phi$  with potential  $V(\phi)$  and conformally-coupled to matter:

$$\mathcal{L} = -\frac{1}{2}(\partial\phi)^2 - V(\phi) + g\frac{\phi}{M_{\text{Pl}}}T_{\mu}^{\mu}$$

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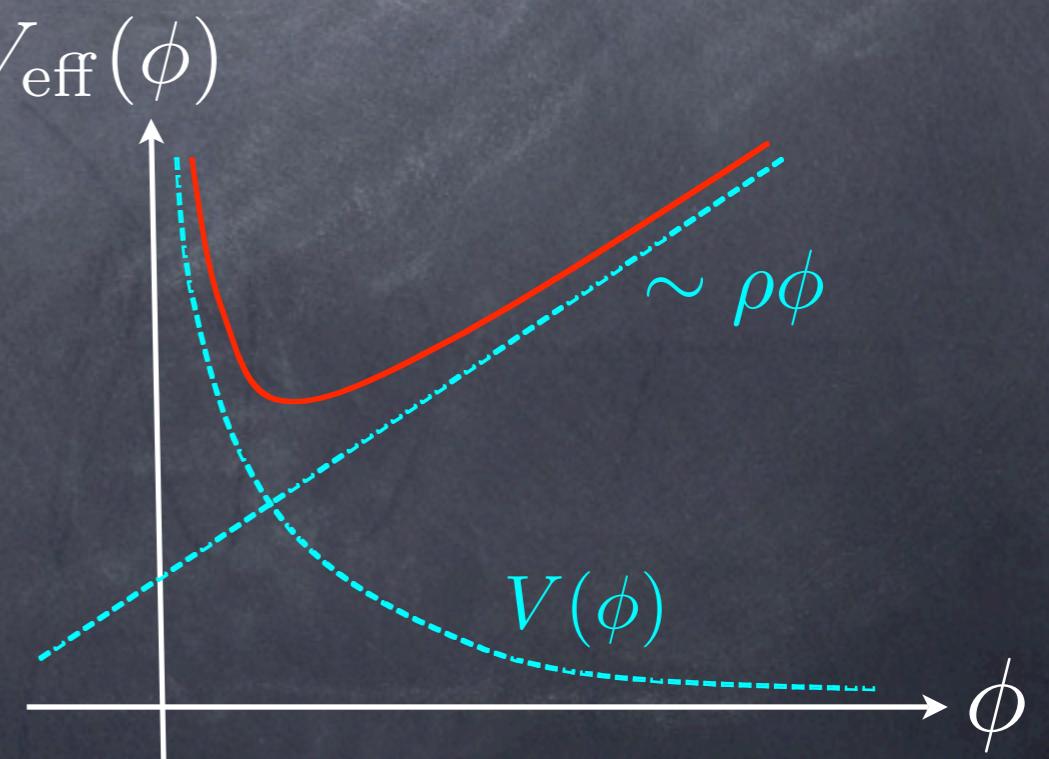
where  $T^\mu_\mu$  is stress tensor of all matter (Baryonic and Dark)

For non-relativistic matter,  $T^\mu_\mu \approx -\rho$ , hence

$$\nabla^2 \phi = V_{,\phi} + \frac{g}{M_{\text{Pl}}} \rho$$

$\implies$

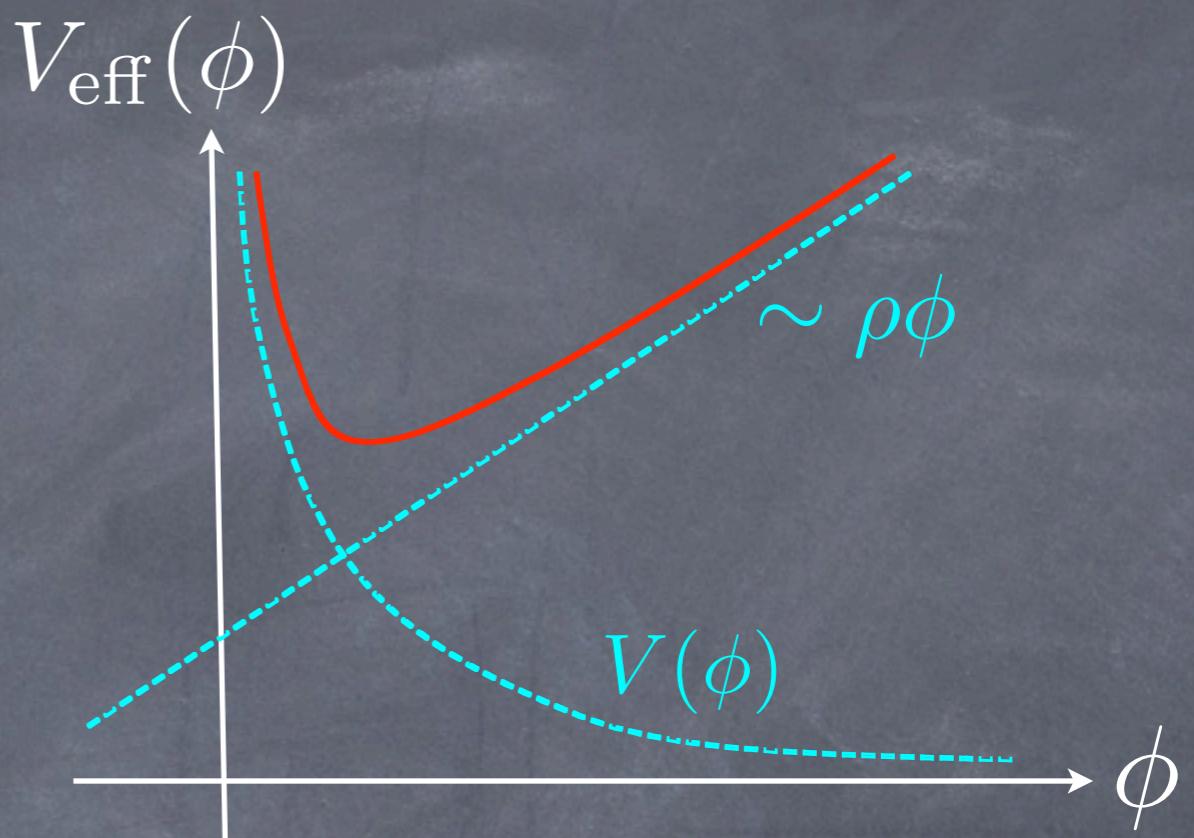
$$V_{\text{eff}}(\phi) = V(\phi) + g \frac{\phi}{M_{\text{Pl}}} \rho$$



# Density-dependent mass

$$V_{\text{eff}}(\phi) = V(\phi) + g \frac{\phi}{M_{\text{Pl}}} \rho$$

e.g.  $V(\phi) = \frac{M^5}{\phi}$



Thus  $m = m(\rho)$  increases with increasing density

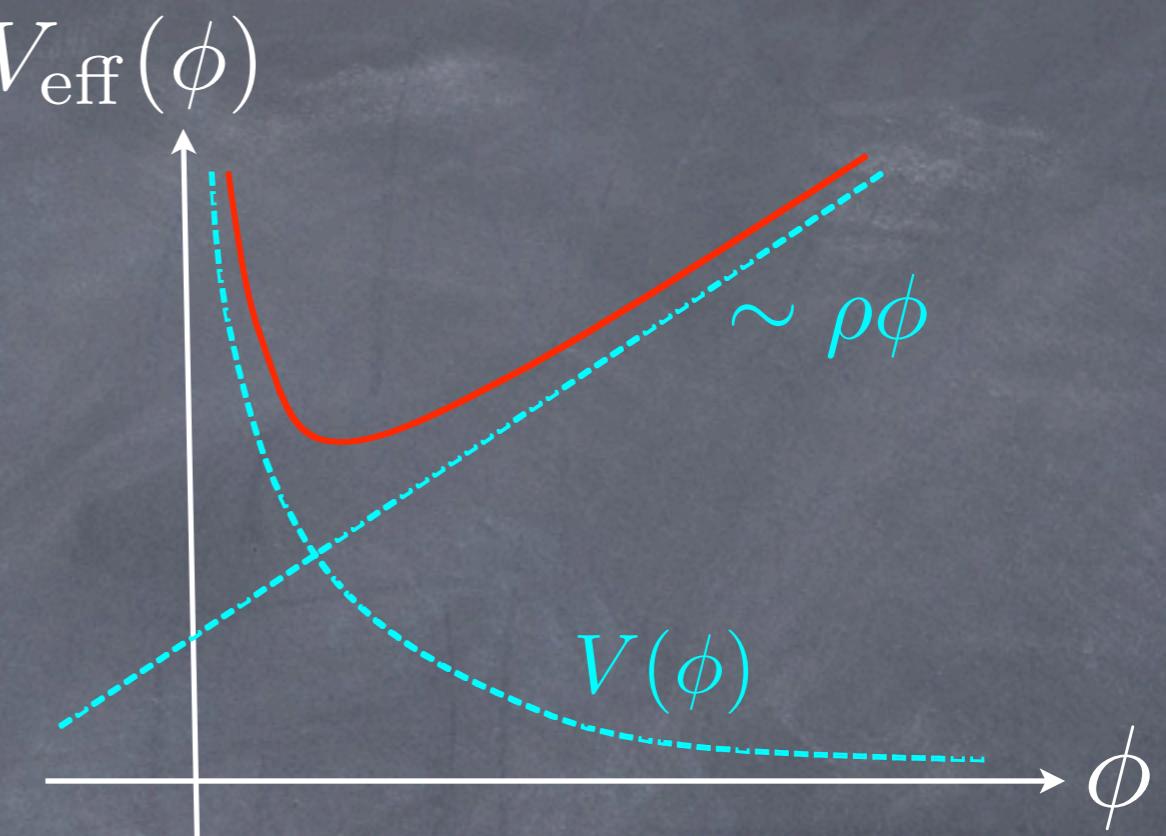
Laboratory tests => set  $m^{-1}(\rho_{\text{local}}) \lesssim \text{mm}$

Generally implies:  $m^{-1}(\rho_{\text{cosmos}}) \lesssim \text{Mpc}$

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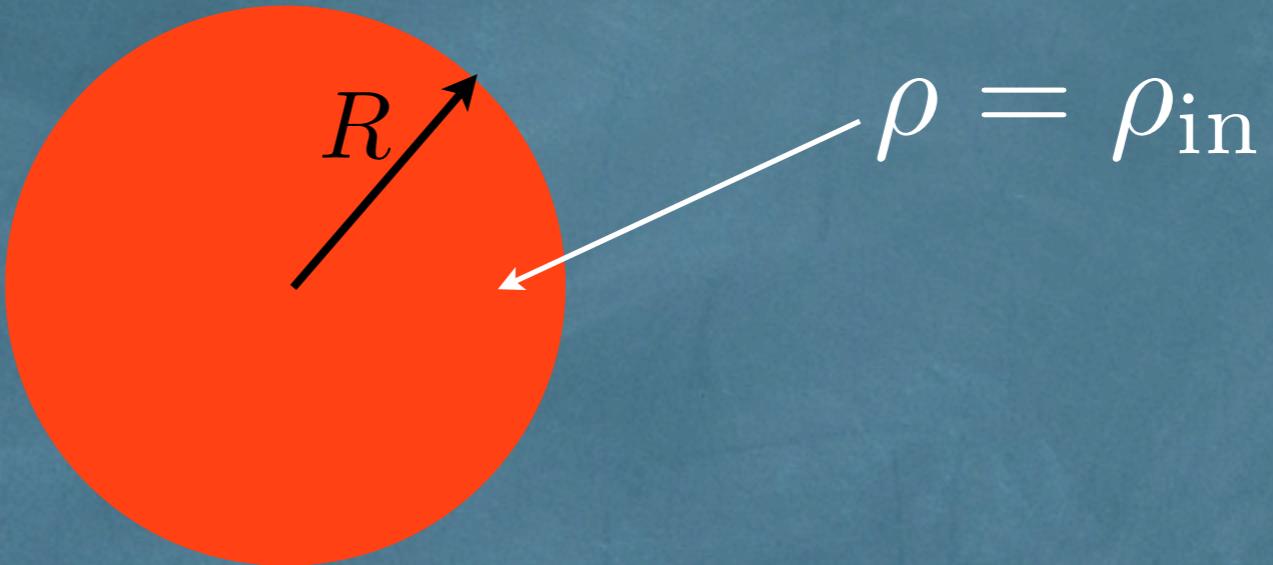
Generally implies:  $m^{-1}(\rho_{\text{cosmos}}) \lesssim \text{Mpc}$

Meanwhile,  $m^{-1}(\rho_{\text{solar system}}) \lesssim 10 - 10^4 \text{ AU}$

→ ruled out by post-Newtonian tests?

# Thin-shell screening

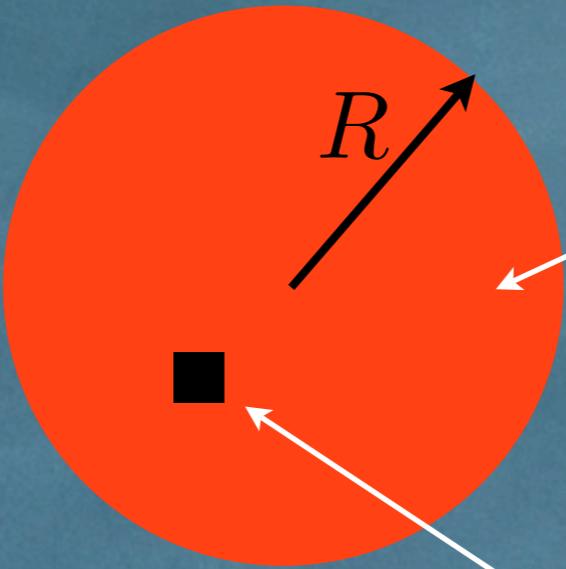
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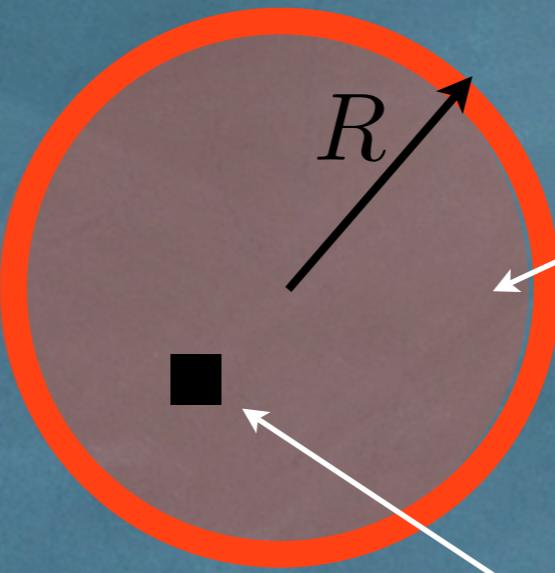


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$$\delta\phi \sim \frac{\delta\mathcal{M}}{r} e^{-mr}$$

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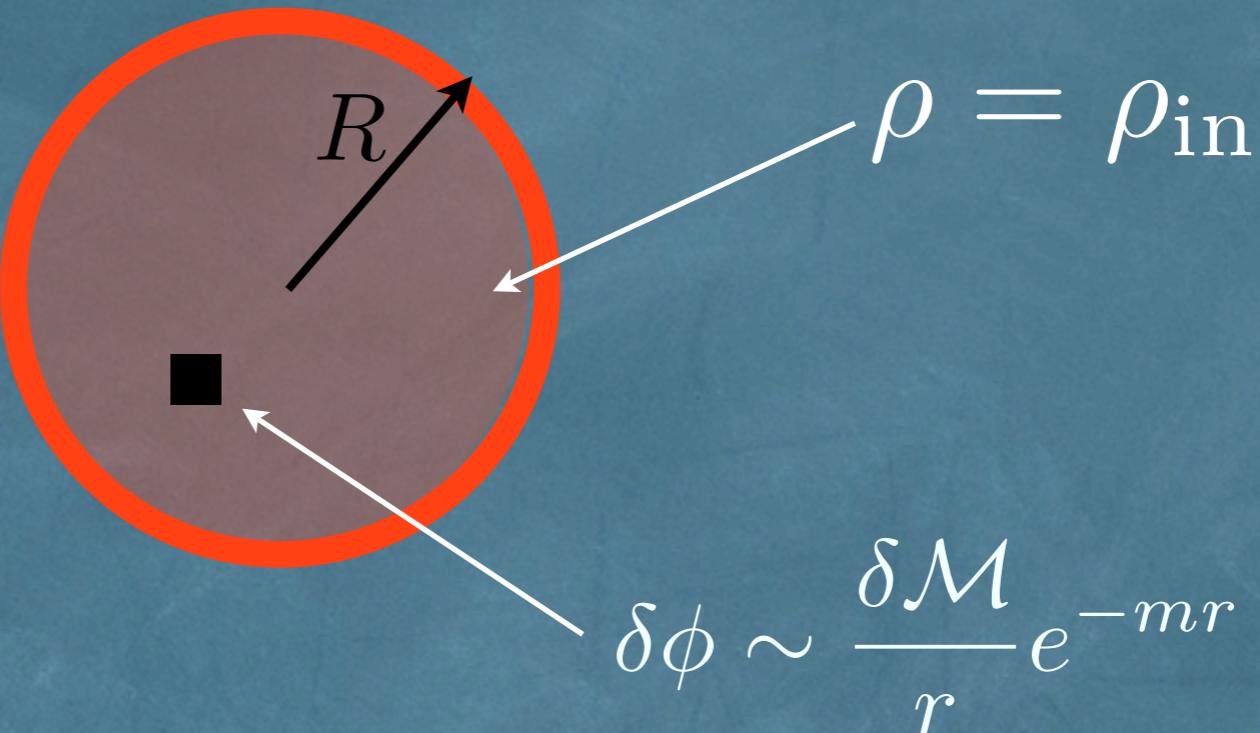


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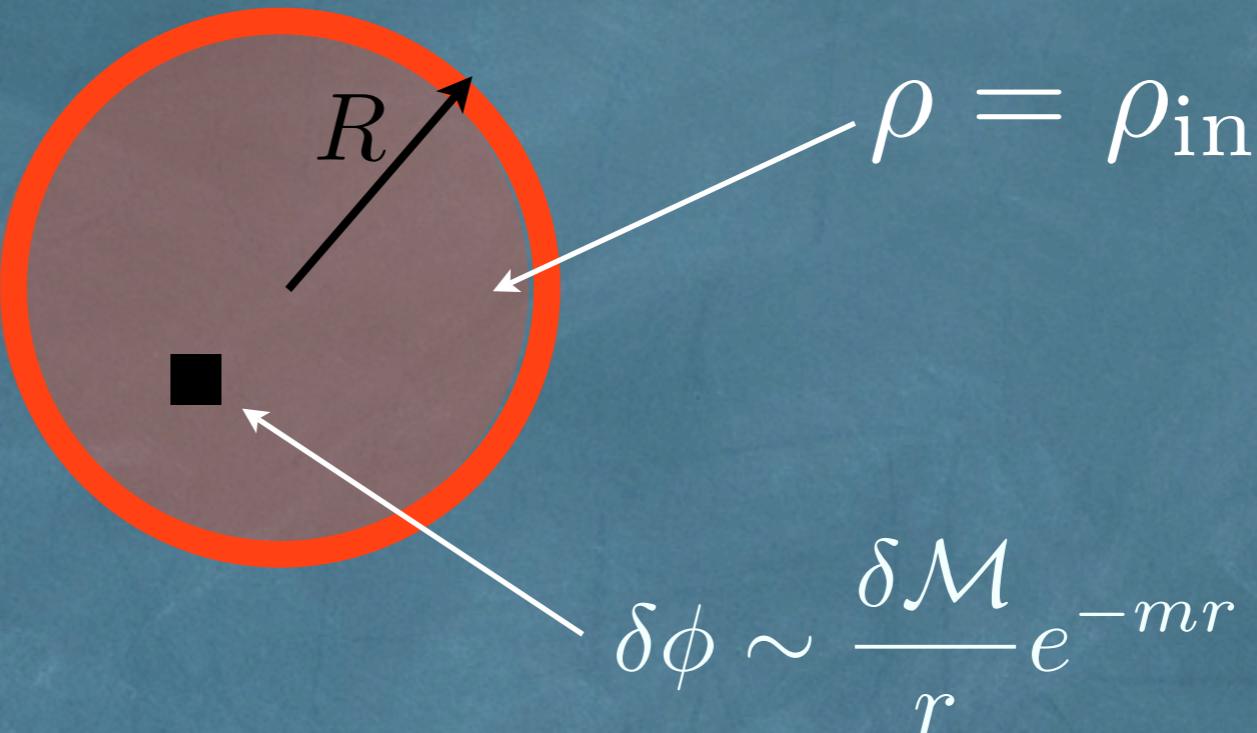
$$\delta\phi \sim \frac{\delta\mathcal{M}}{r} e^{-mr}$$

$$\implies \boxed{\phi(r > R) \sim \frac{\Delta R}{R} \times \frac{g G_N M}{r}}$$

where  $\frac{\Delta R}{R} = \frac{\phi_{\text{out}} - \phi_{\text{in}}}{6gM_{\text{Pl}}\Phi_N} \ll 1 \implies \text{thin-shell screening}$

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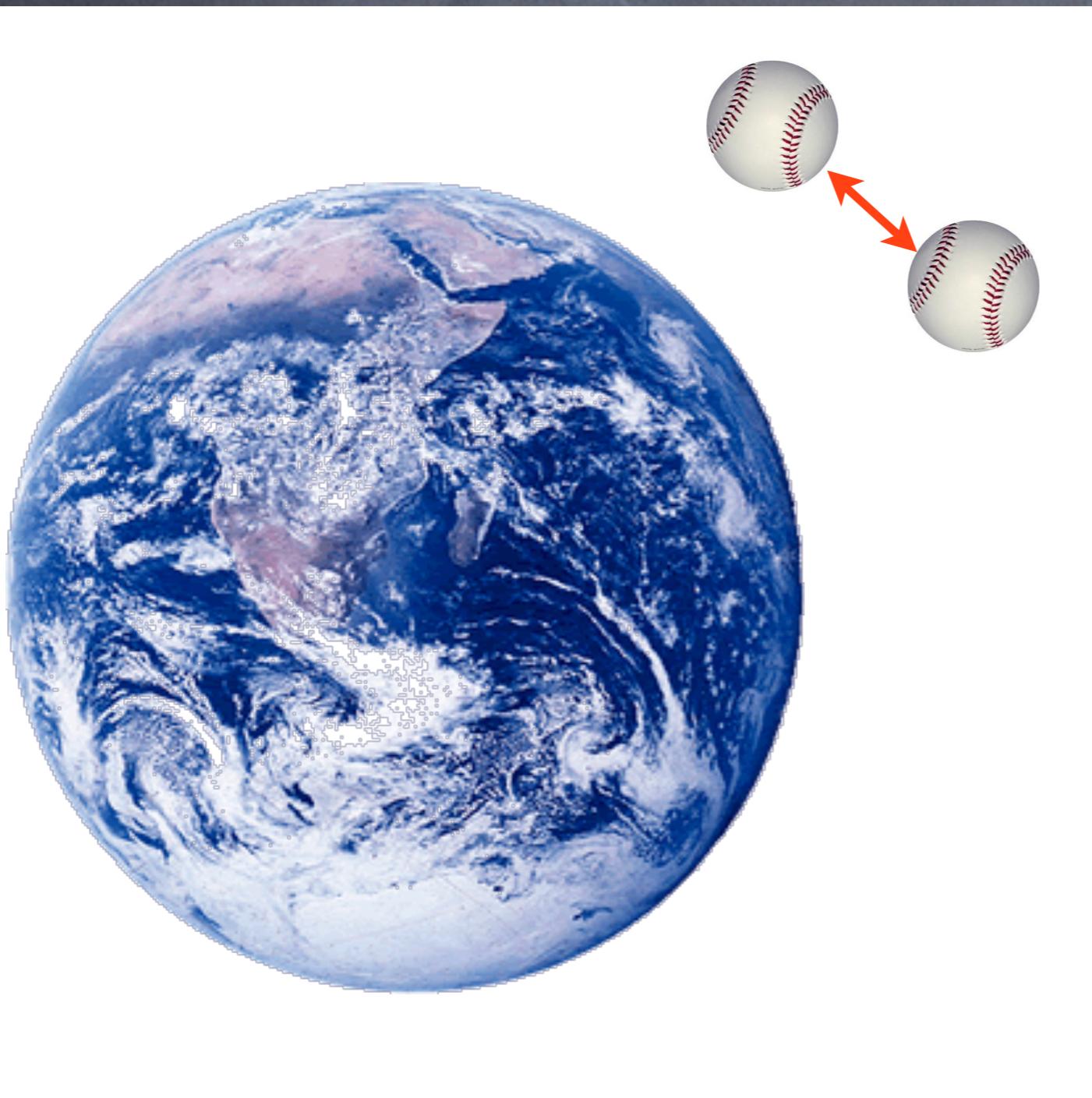
But small objects  $\implies$  no thin-shell

Thin-shell condition depends on environment!

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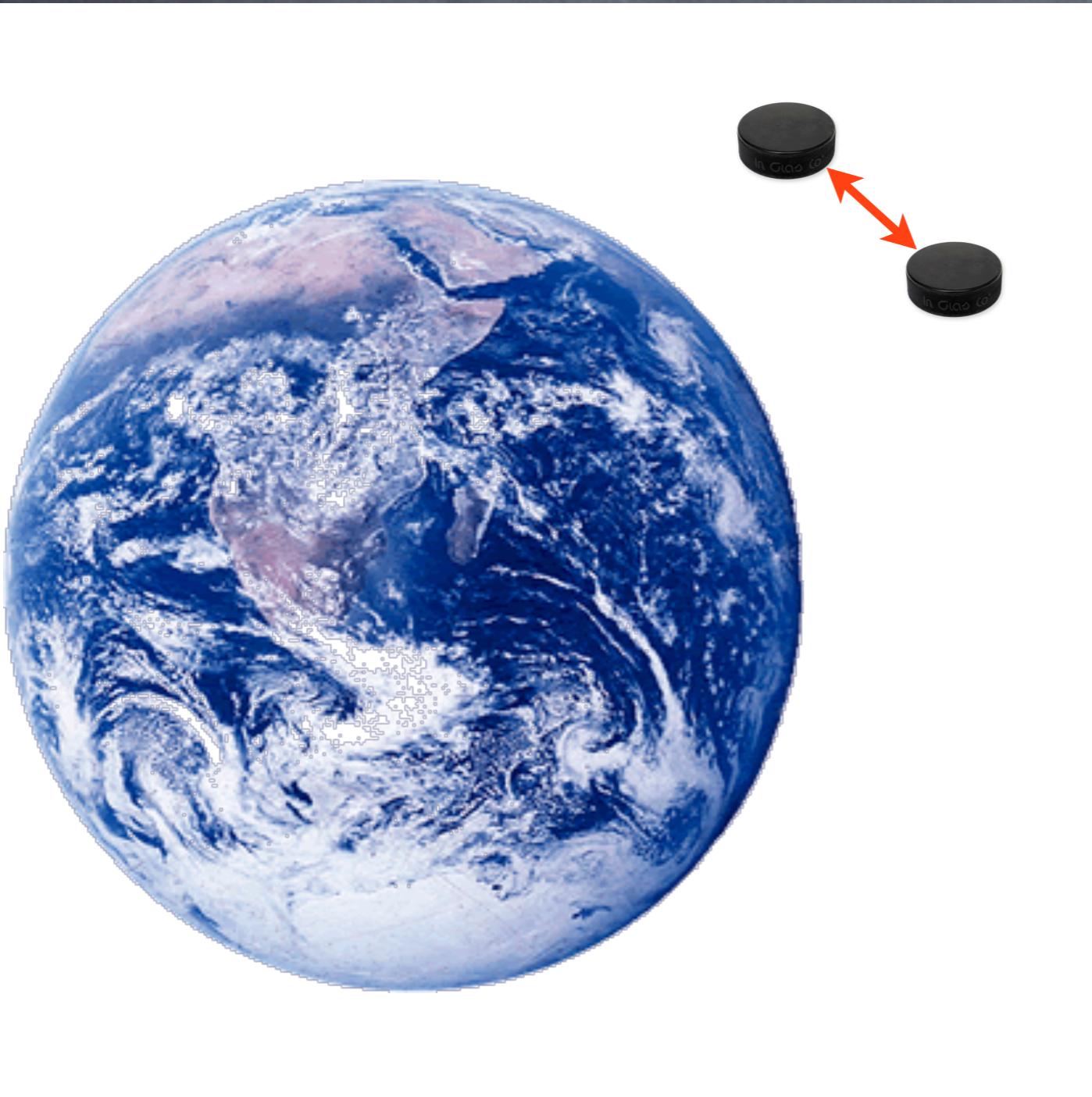
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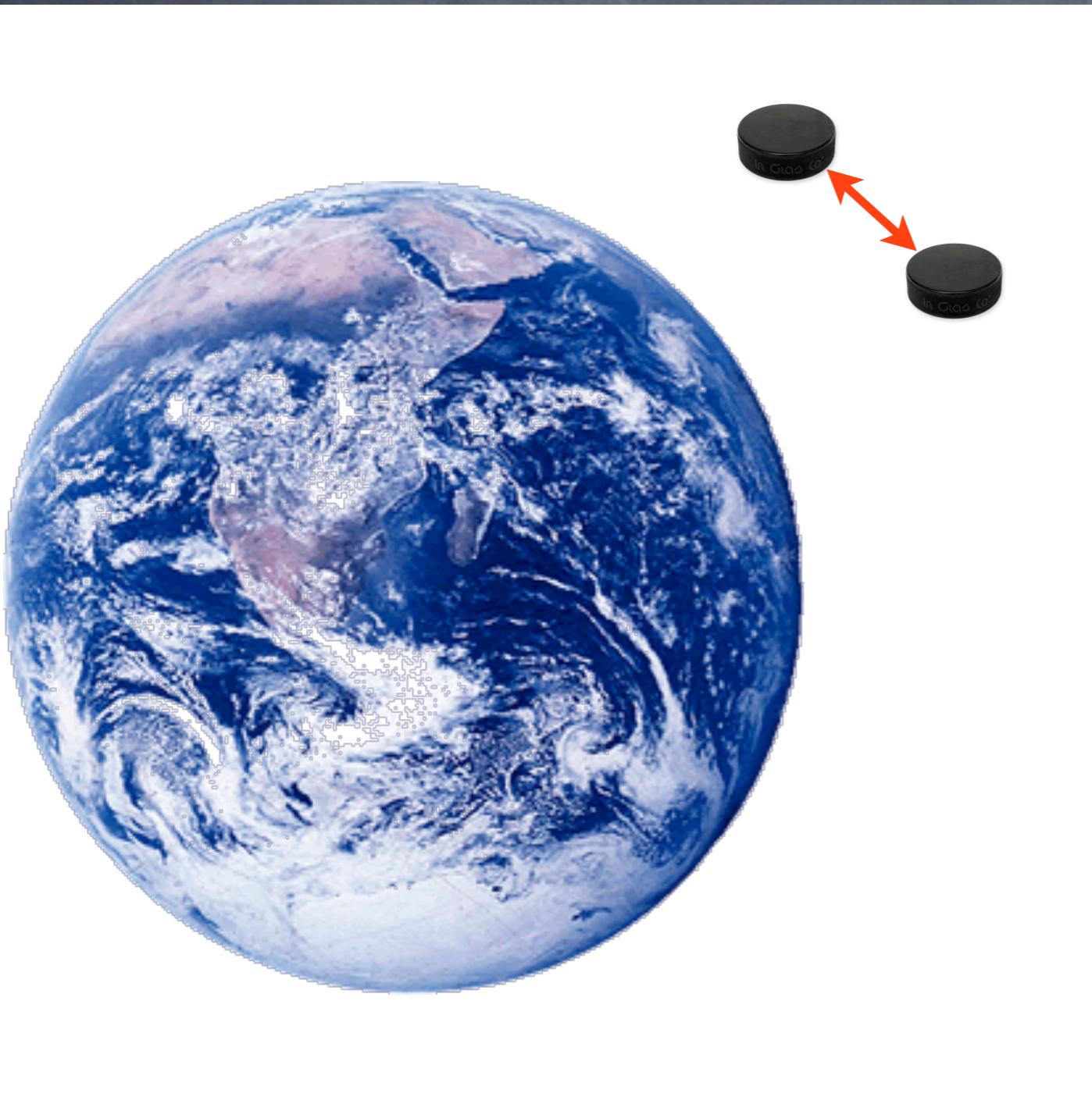
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$G_N^{\text{eff}} = G_N(1 + 2g^2)$   
**between small objects  
in space !**

# Smoking Guns

- Satellite Test of the Equivalence Principle (STEP)

$$\frac{\Delta G_N}{G_N} < 10^{-6}$$



$$\frac{\Delta G_N}{G_N} \sim \mathcal{O}(1)$$

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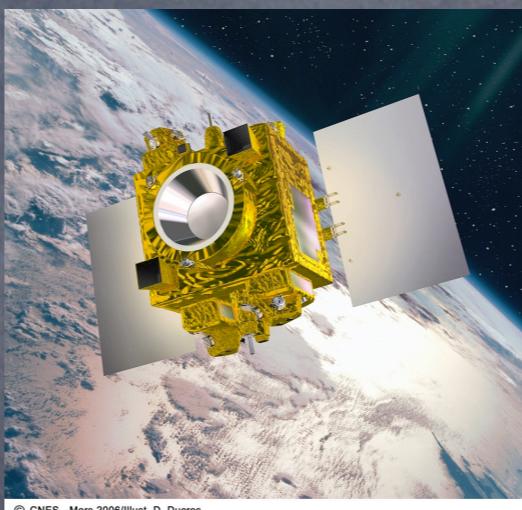
$$\frac{\Delta G_N}{G_N} < 10^{-6}$$

$$\frac{\Delta a}{a} < 10^{-18}$$



- MICROSCOPE (2012)

$$\frac{\Delta a}{a} < 10^{-15}$$



- Galileo Galilei (???)

$$\frac{\Delta a}{a} < 10^{-17}$$



$$\frac{\Delta G_N}{G_N} \sim \mathcal{O}(1)$$

$$\frac{\Delta a}{a} > 10^{-13}$$

# Strong coupling?

J. Khoury, A. Upadhye & W. Hu, to appear

$$V(\phi) = \frac{M^5}{\phi} \quad M = 10^{-3} \text{ eV}$$

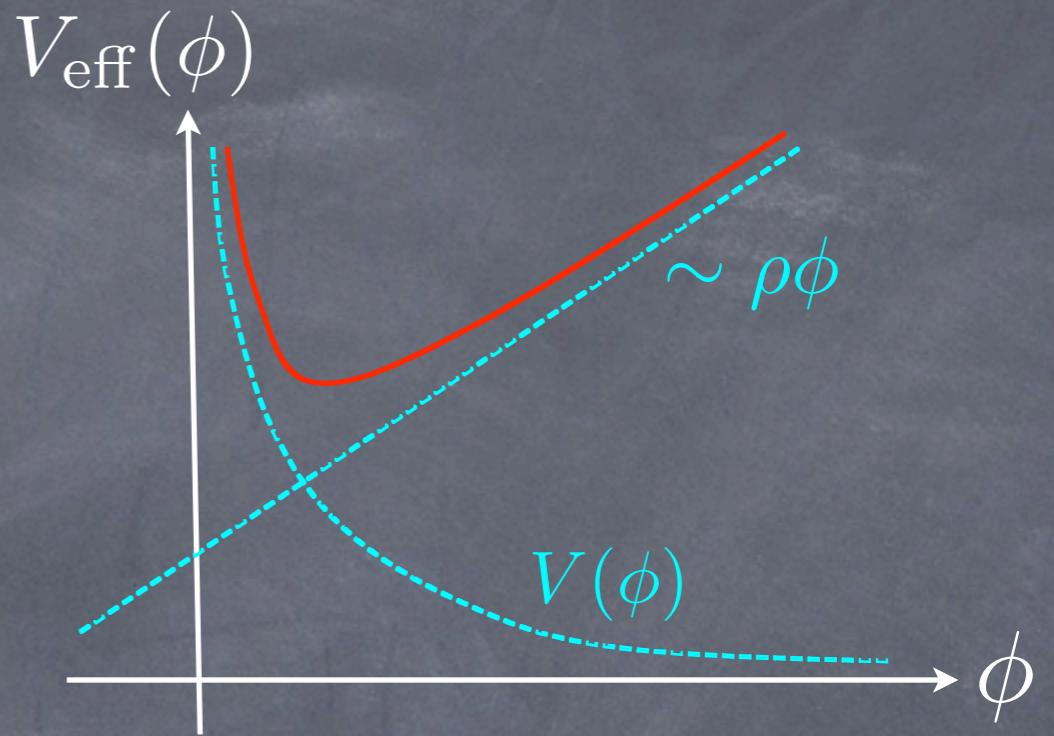
Perturb around minimum:

$$V = \bar{V} + \dots + \frac{\delta\phi^n}{\Lambda^{n-4}} + \dots$$

where

$$\frac{\Lambda}{M} = \left( \frac{\bar{\phi}}{M} \right)^{\frac{n+1}{n-4}} = \left( \frac{M^2}{m^2} \right)^{\frac{n+1}{3(n-4)}} > \left( \frac{M^2}{m^2} \right)^{\frac{1}{3}}$$

- Cosmologically:  $m \sim \text{Mpc}^{-1} \implies \Lambda \sim 10^5 \text{ GeV}$
- Lab:  $m \sim 10^{-3} \text{ eV} \implies \Lambda \sim 10^{-3} \text{ eV}$



# Relation to $f(R)$ gravity

Carroll, Duvvuri, Trodden & Turner (2004);  
Capozziello, Carloni & Troisi (2004)

$$S = \frac{M_{\text{Pl}}^2}{2} \int d^4x \sqrt{-\tilde{g}} f(\tilde{R}) + S_{\text{matter}}[\tilde{g}_{\mu\nu}]$$

Special case of chameleon theories:

$$S = \frac{M_{\text{Pl}}^2}{2} \int d^4x \sqrt{-\tilde{g}} \left\{ f(\psi) + \frac{df}{d\psi} (\tilde{R} - \psi) \right\} + S_{\text{matter}}[\tilde{g}_{\mu\nu}]$$

Varying wrt to  $\psi \implies \psi = \tilde{R}$

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**Field redefinitions:**  $g_{\mu\nu} = \frac{df}{d\psi} \tilde{g}_{\mu\nu} ; \phi = -\sqrt{\frac{3}{2}} M_{\text{Pl}} \log \frac{df}{d\psi}$

$$\implies S = \int d^4x \sqrt{-g} \left( \frac{M_{\text{Pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) \right) + S_{\text{matter}} \left[ g_{\mu\nu} e^{\sqrt{2/3}\phi/M_{\text{Pl}}} \right]$$

**where**  $V = \frac{M_{\text{Pl}}^2 \left( \psi \frac{df}{d\psi} - f \right)}{2 \left( \frac{df}{d\psi} \right)^2} .$

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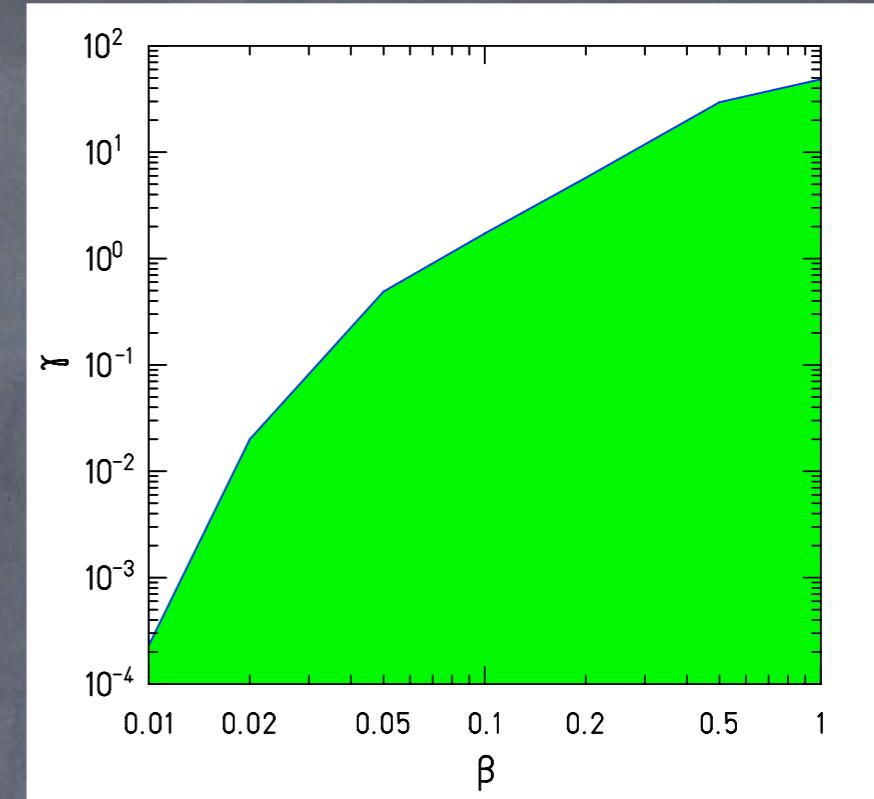
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# Chameleon Searches

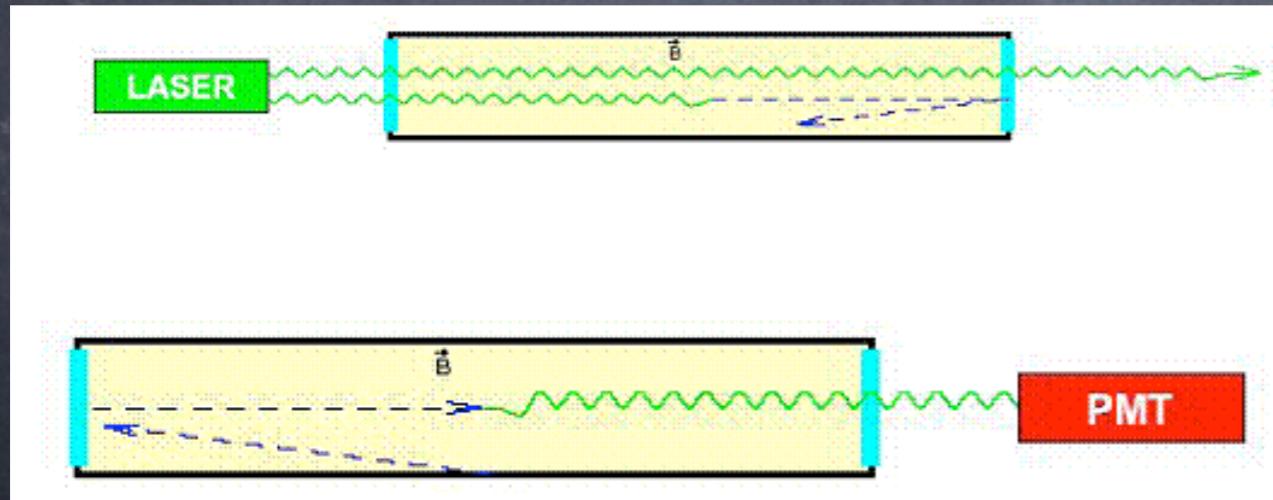
- Eot-Wash

Adelberger et al.,  
Phys. Rev. Lett. (2008)



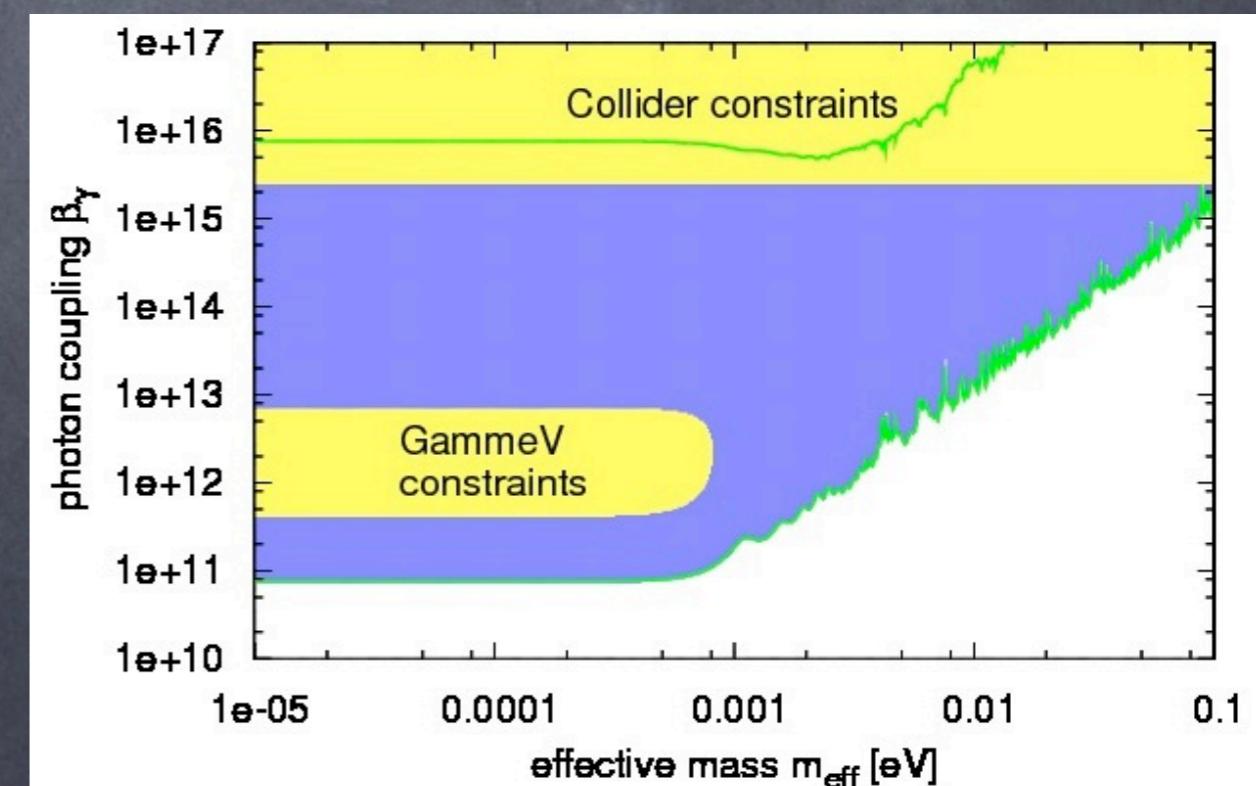
- CHameleon Afterglow SSearch (CHASE), Fermilab

Chou et al., Phys. Rev. Lett. (2008,2010)



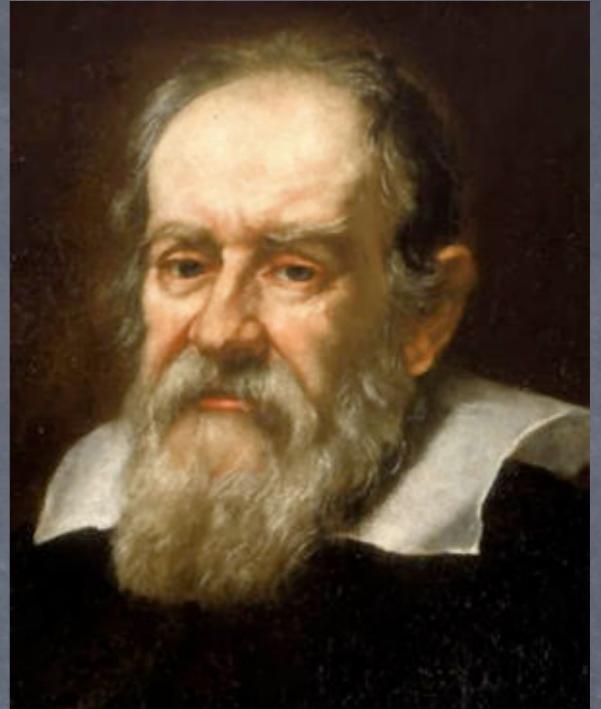
See also ADMX expt

P. Sikivie & co., Phys. Rev. Lett. (2010)



# Vainshtein/Galileon Mechanism

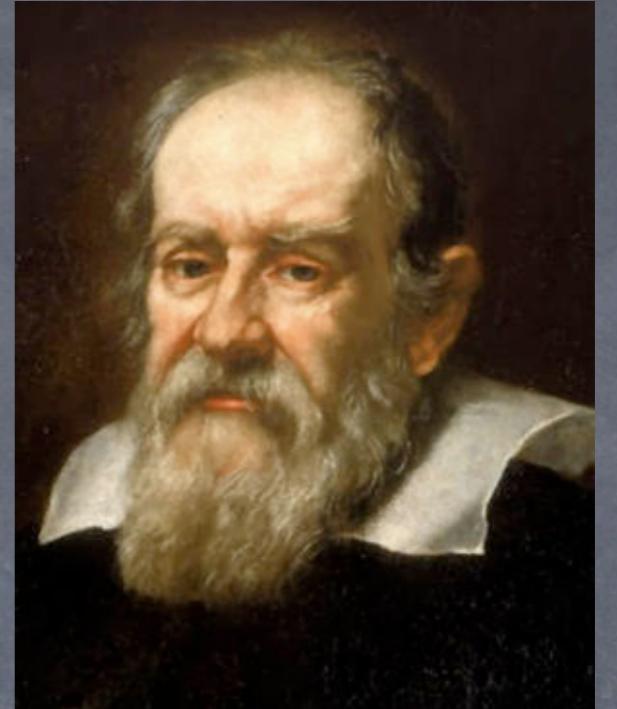
Vainshtein (1972); Deffayet, Dvali, Gabadadze &  
Vainshtein (2002); Luty, Poratti & Rattazzi (2003);  
Nicolis & Rattazzi (2004)



$$\mathcal{L} = -\frac{1}{2}(\partial\phi)^2 - \frac{L^2}{6\sqrt{6}M_{\text{Pl}}}(\partial\phi)^2\square\phi + \frac{\phi}{\sqrt{6}M_{\text{Pl}}}T^\mu_\mu$$

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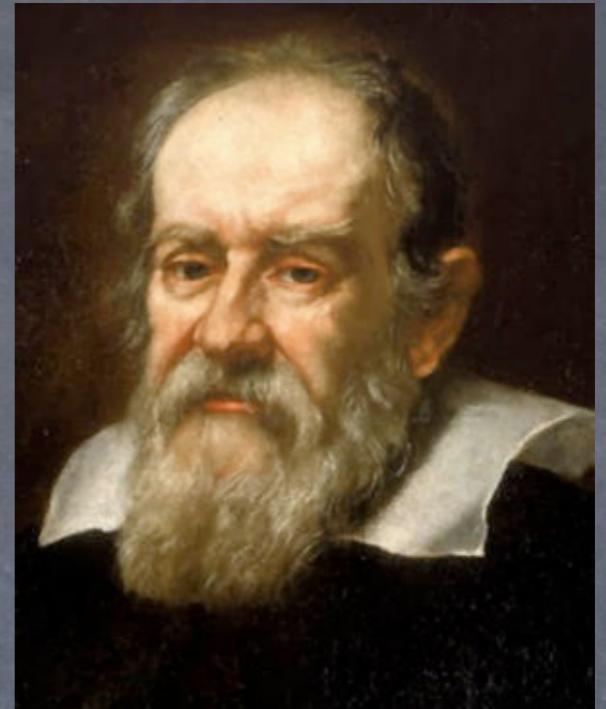


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Enjoys “Galilean” symmetry:  $\phi \rightarrow \phi + c + b_\mu x^\mu$

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Nicolis & Rattazzi (2004)



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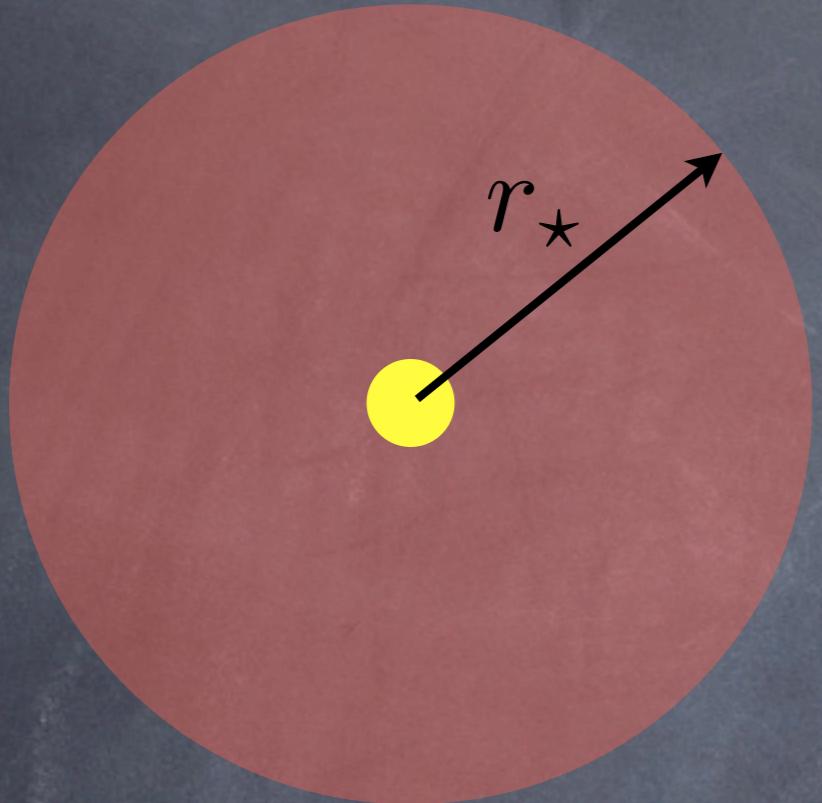
Enjoys “Galilean” symmetry:  $\phi \rightarrow \phi + c + b_\mu x^\mu$

Leads to 2nd order eqns of motion:

$$\Box\phi + \frac{L^2}{3\sqrt{6}M_{\text{Pl}}} \left[ (\Box\phi)^2 - (\partial_\mu\partial_\nu\phi)^2 \right] = \frac{T^\mu_\mu}{\sqrt{6}M_{\text{Pl}}}$$

For a spherically-symmetric source,

$$\nabla^2 \phi + \frac{L^2}{3\sqrt{6}M_{\text{Pl}}} \left[ (\nabla^2 \phi)^2 - (\nabla_i \nabla_j \phi)^2 \right] = \frac{\rho}{\sqrt{6}M_{\text{Pl}}}$$

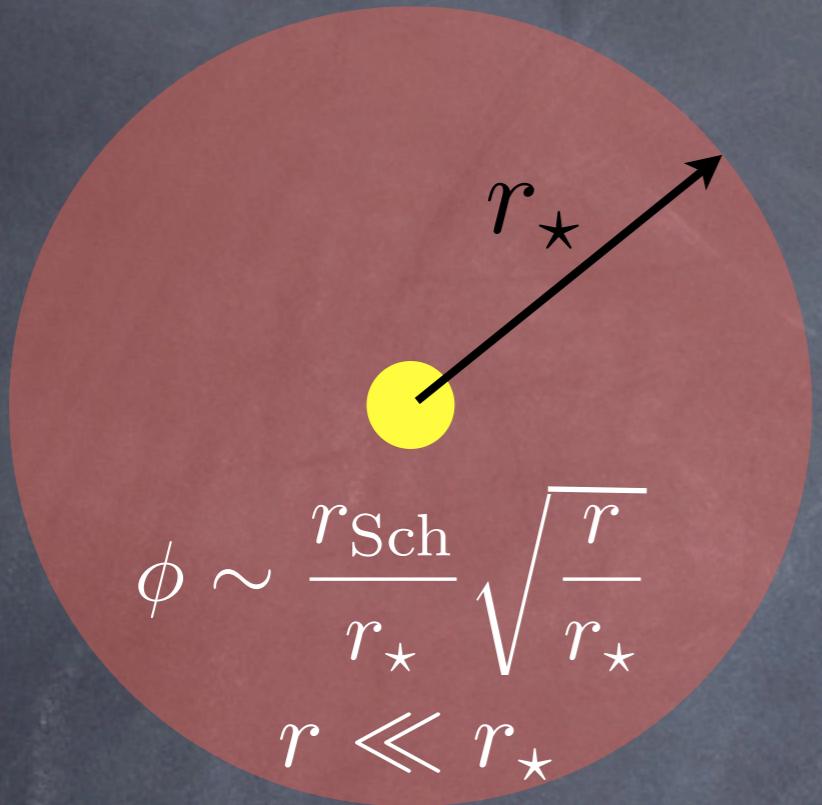


$$\phi \sim \frac{r_{\text{Sch}}}{r} \quad \text{where} \quad r \gg r_\star$$

$$r_\star = (r_{\text{Sch}} L^2)^{1/3}$$

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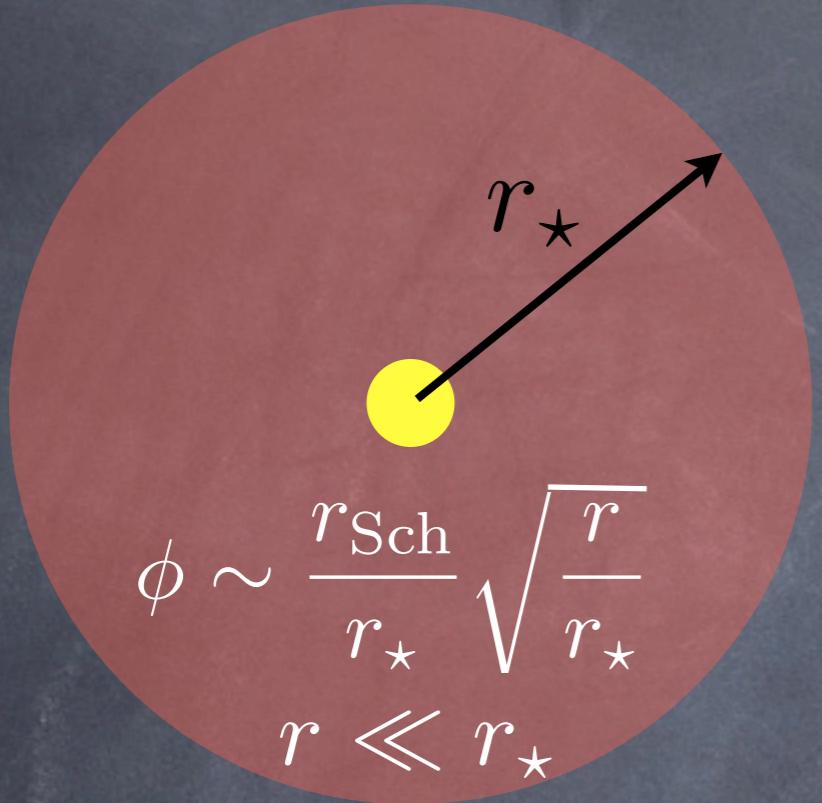
$$\phi \sim \frac{r_{\text{Sch}}}{r_\star} \sqrt{\frac{r}{r_\star}}$$
$$r \ll r_\star$$

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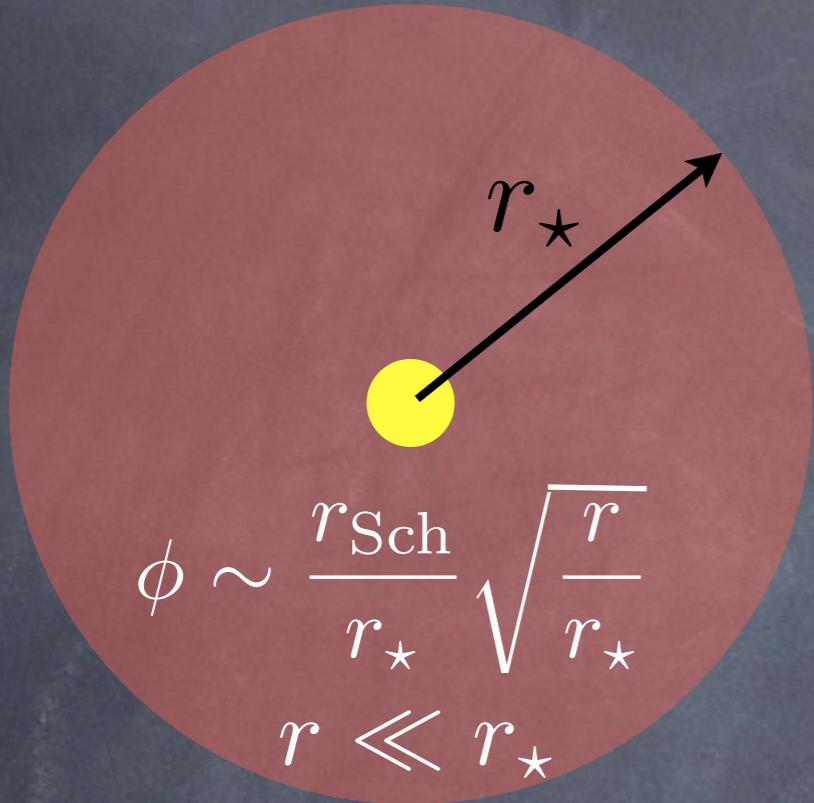
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e.g.  $L = 3000 \text{ Mpc}$

$$r_\star|_\odot \simeq 0.1 \text{ kpc}$$
$$\Rightarrow r_\star|_{\text{gal}} \simeq \text{Mpc}$$
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$$r_*|_{\odot} \simeq 0.1 \text{ kpc}$$

$$\Rightarrow r_*|_{\text{gal}} \simeq \text{Mpc}$$

$$r_*|_{\text{clus}} \simeq 10 \text{ Mpc}$$

For  $r \gg r_*$ , gravity enhanced:

$$G_{\text{N}}^{\text{eff}} = G_{\text{N}} \left( 1 + \frac{1}{3} \right)$$

Note: Deviations from GR are largest on scales  $\gtrsim 1 - 10 \text{ Mpc}$

Kinetic screening:

Consider perturbations  $\phi = \bar{\phi}(r) + \delta\phi$

$$\begin{aligned}\mathcal{L}_{\text{pert}} = & -\frac{1}{2}(\partial\delta\phi)^2 \left( 1 + \frac{L^2}{M_{\text{Pl}}} \bar{\phi}''(r) \right) \\ & - \frac{L^2}{6\sqrt{6}M_{\text{Pl}}} (\partial\delta\phi)^2 \square\delta\phi + \frac{\delta\phi}{\sqrt{6}M_{\text{Pl}}} \delta T\end{aligned}$$

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The non-linear coupling scale is also raised.

Lunar Laser Ranging:

Dvali, Gruzinov and Zaldarriaga (2002)

$$\frac{\delta\Phi_N}{\Phi_N} \sim \left(\frac{r}{r_\star}\right)^{3/2} \simeq 10^{-12}$$



# Symmetron Mechanism

K. Hinterbichler and J. Khoury, Phys. Rev. Lett. (2010)

Instead of  $m(\rho)$ , here it is the coupling to matter that depends on density.

$$\mathcal{L} = -\frac{1}{2}(\partial\phi)^2 - V(\phi) + \frac{\phi^2}{2M^2}T^\mu_\mu$$

where  $T^\mu_\mu$  is stress tensor of all matter (Baryonic and Dark)

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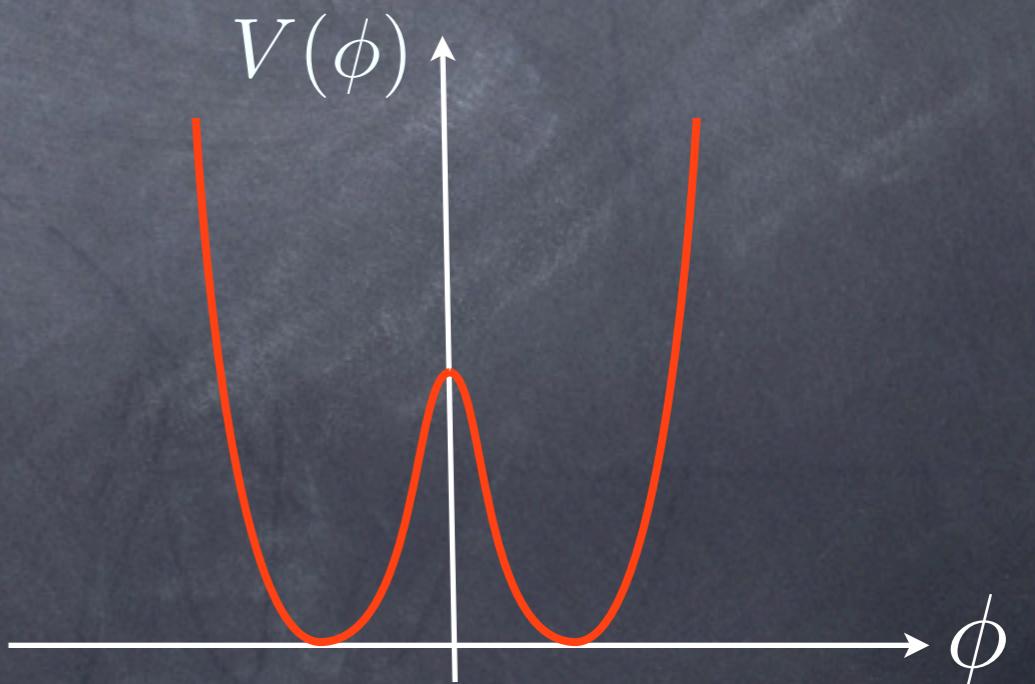
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Potential is of the spontaneous-symmetry-breaking form:

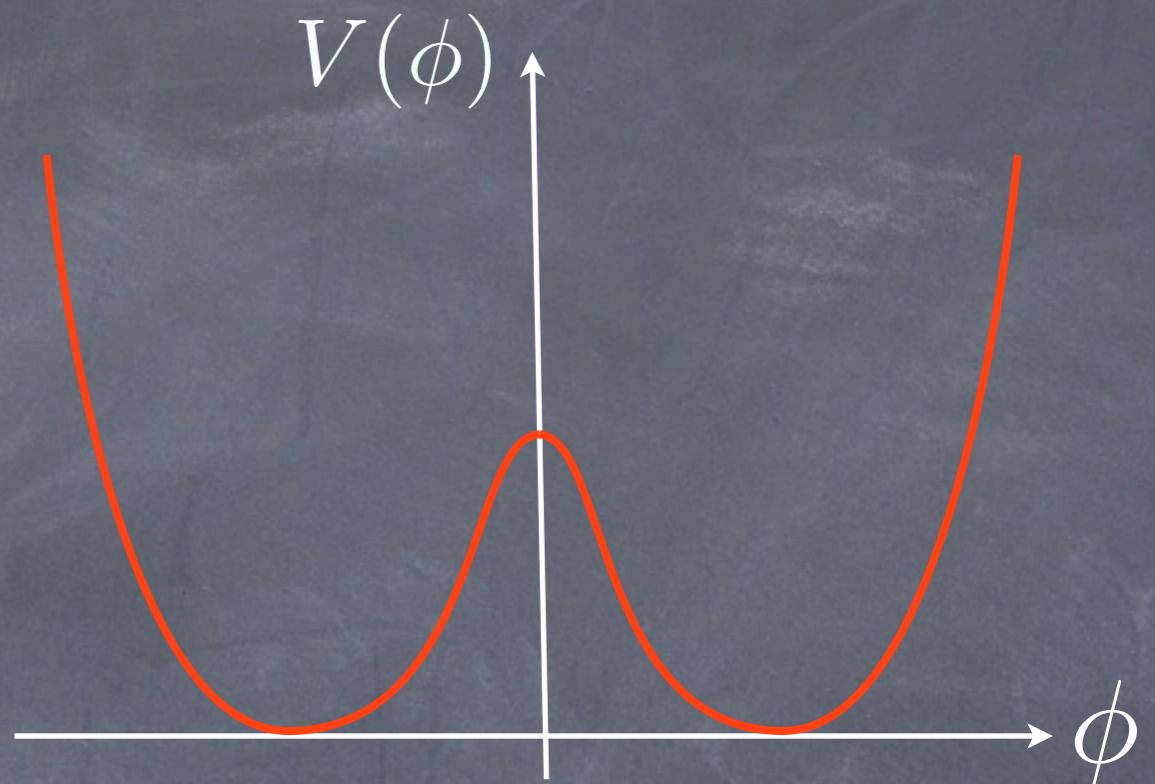
$$V(\phi) = -\frac{1}{2}\mu^2\phi^2 + \frac{1}{4}\lambda\phi^4$$

Most general renormalizable potential with  $\phi \rightarrow -\phi$  symmetry.



# Effective Potential

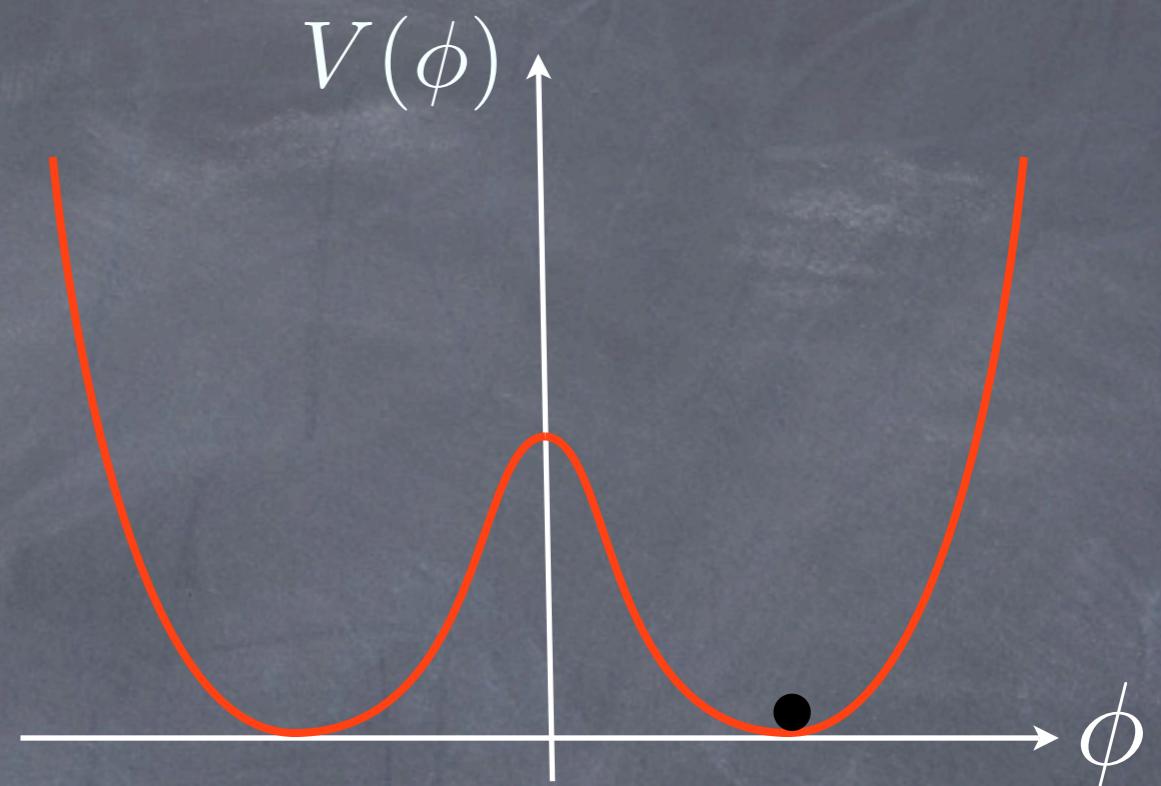
$$V_{\text{eff}}(\phi) = \frac{1}{2} \left( \frac{\rho}{M^2} - \mu^2 \right) \phi^2 + \frac{1}{4} \lambda \phi^4$$



∴ Whether symmetry is broken or not depends on local density

# Effective Potential

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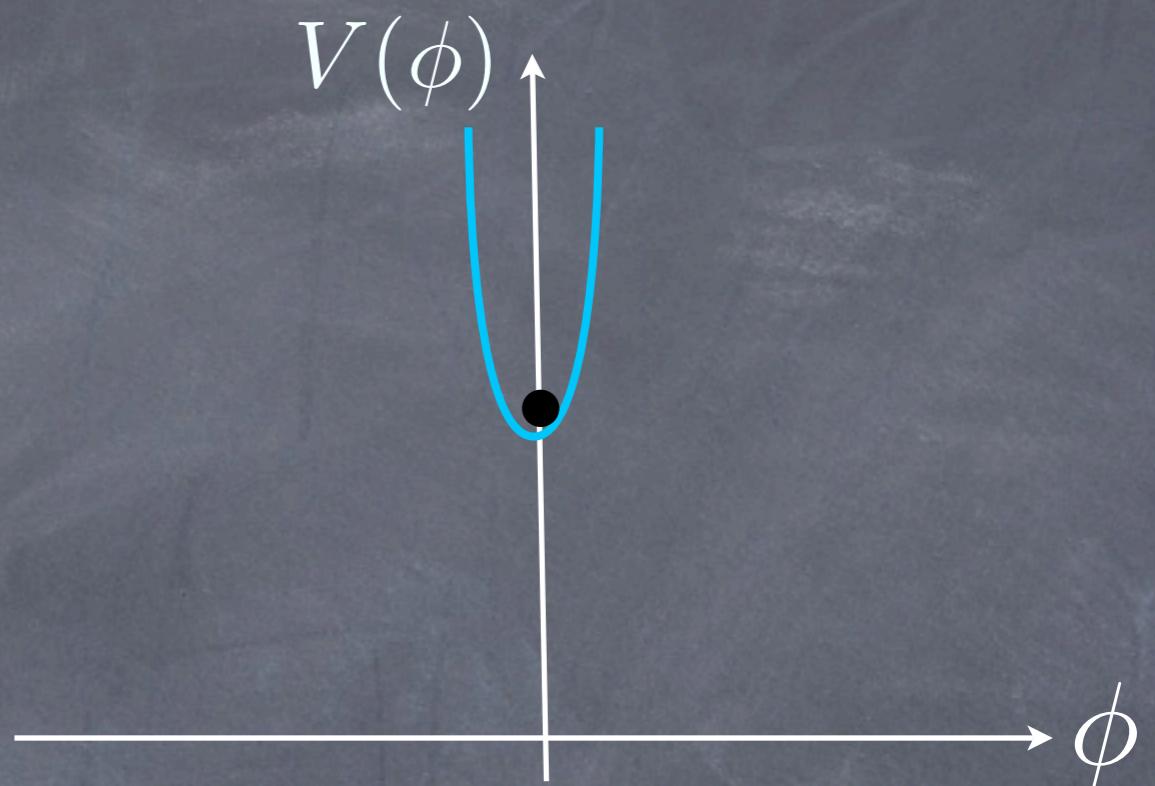


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- Outside source,  $\rho = 0$ , symmetron acquires VEV and symmetry is spontaneously broken.

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∴ Whether symmetry is broken or not depends on local density

- Outside source,  $\rho = 0$ , symmetron acquires VEV and symmetry is spontaneously broken.
- Inside source, provided  $\rho > \mu^2 M^2$ , the symmetry is restored.

# Effective Coupling

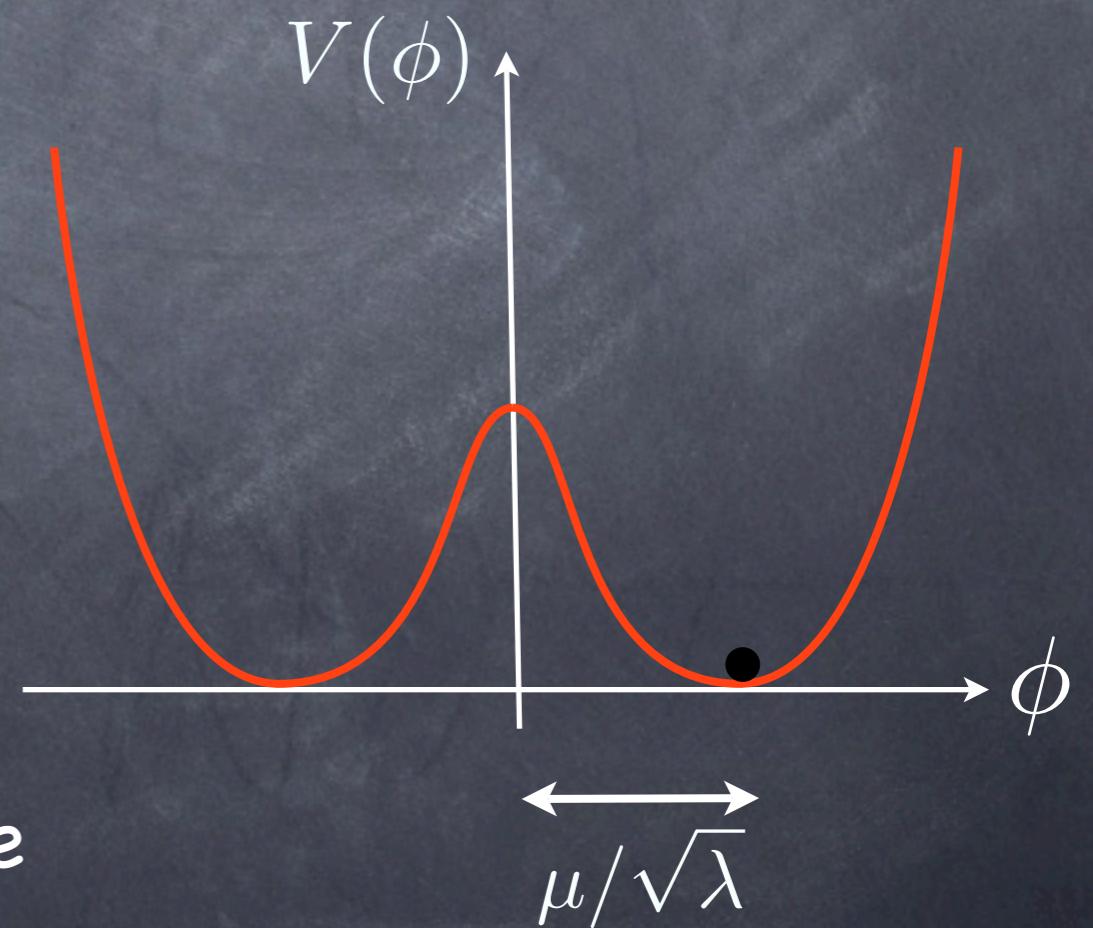
Perturbations  $\delta\phi$  around local background value couple as:

$$\mathcal{L}_{\text{coupling}} \sim \frac{\bar{\phi}}{M^2} \delta\phi \rho$$

- Symmetron flctns decouple in high-density regions
- In voids, where  $Z_2$  symmetry is broken,

$$\mathcal{L}_{\text{coupling}} \sim \frac{\mu}{\sqrt{\lambda} M^2} \delta\phi \rho$$
$$\sim \frac{\delta\phi}{M_{\text{Pl}}} \rho$$

gravitational strength



- Gravitational-strength, Mpc-range
- 5th force in voids.

Inspiration...

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Symmetron Couch  
(\$9500.00)

"NASA-style gravity reduction."

"Offers a unique multi-phase wave experience."

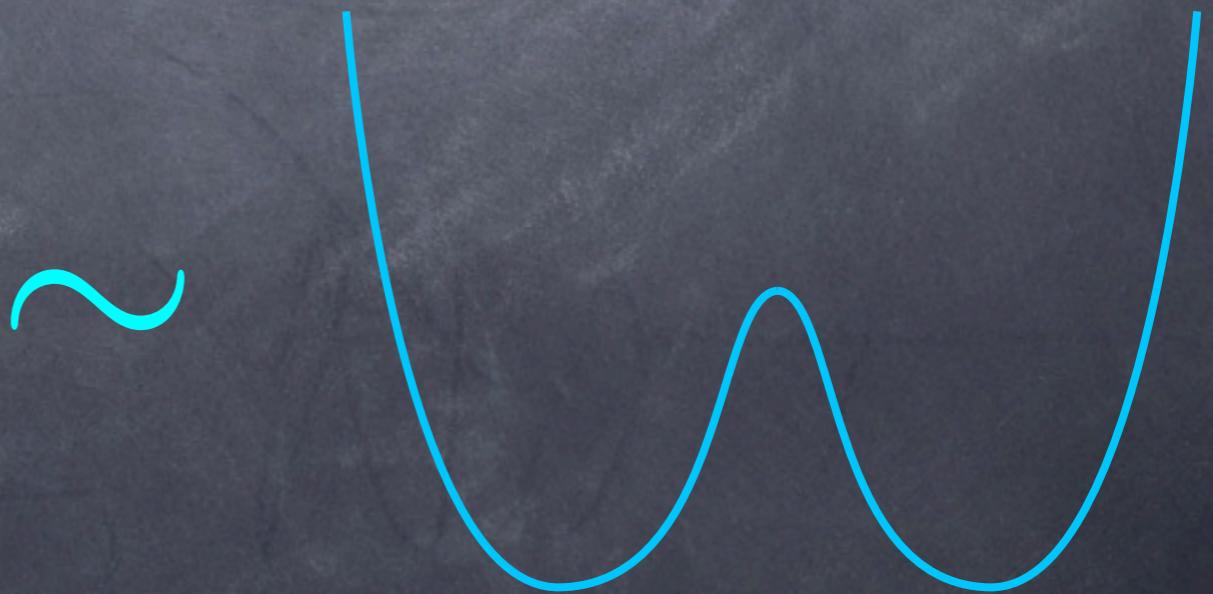


# Inspiration...

## Symmetron Couch (\$9500.00)

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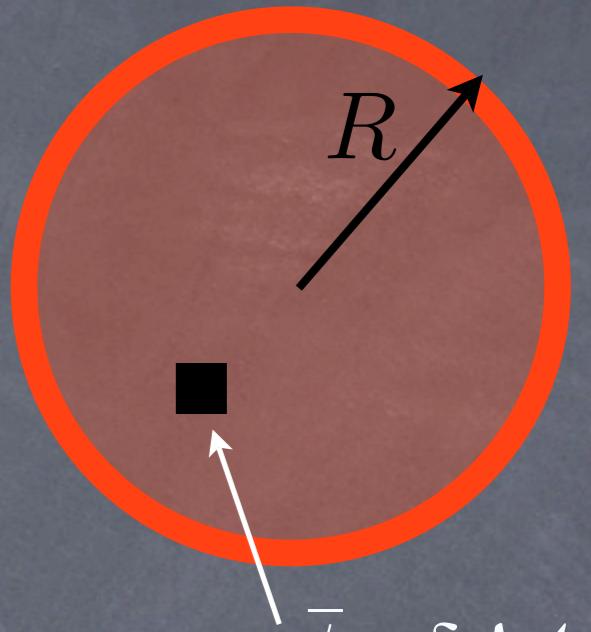
"Offers a unique multi-phase wave experience."



# Thin-Shell Screening Effect

Behavior of solution depends on

$$\alpha \equiv \frac{\rho R^2}{M^2} = 6 \frac{M_{\text{Pl}}^2}{M^2} \Phi_N$$



- For sufficiently massive objects, such that  $\alpha \gg 1$ , solution is suppressed by thin-shell effect:

$$\phi_{\text{exterior}}(r) \sim \frac{1}{\alpha} \frac{\mathcal{M}}{M_{\text{Pl}}^2 r} + \phi_0$$

- For small objects,  $\alpha \ll 1$ , we find  $\phi \approx \phi_0$  everywhere

$$\implies \phi_{\text{exterior}}(r) \sim \frac{\mathcal{M}}{M_{\text{Pl}}^2 r} + \phi_0$$

# Parameter Constraints

$$\mathcal{L} = -\frac{1}{2}(\partial\phi)^2 + \frac{1}{2}\mu^2\phi^2 - \frac{1}{4}\lambda\phi^4 + \frac{\phi^2}{2M^2}T^\mu_\mu$$

Necessary (and sufficient) condition is that Milky Way has thin shell:

$$\alpha_G = 6 \frac{M_{Pl}^2}{M^2} \Phi_G \gtrsim 1$$

$$\Phi_G \sim 10^{-6}$$



$$\implies M \lesssim 10^{-3} M_{Pl}$$

$$\implies \mu \sim \frac{M_{Pl}}{M} H_0 \gtrsim \text{Mpc}^{-1} \quad \lambda \sim \frac{M_{Pl}^4 H_0^2}{M^6} \gtrsim 10^{-100}$$

# Predictions for Tests of Gravity

Test	Effective parameter	Current bounds
Time delay/light deflection	$ \gamma - 1  \approx 10^{-5}$	$ \gamma - 1  \approx 10^{-5}$
Nordvedt effect	$ \eta_N  \sim 10^{-4}$	$ \eta_N  \sim 10^{-4}$
Mercury perihelion shift	$ \gamma - 1  \approx 4 \cdot 10^{-4}$	$ \gamma - 1  \approx 10^{-3}$
Binary pulsars	$\omega_{\text{BD}}^{\text{eff}} \gtrsim 10^6$	$\omega_{\text{BD}}^{\text{eff}} \gtrsim 10^3$

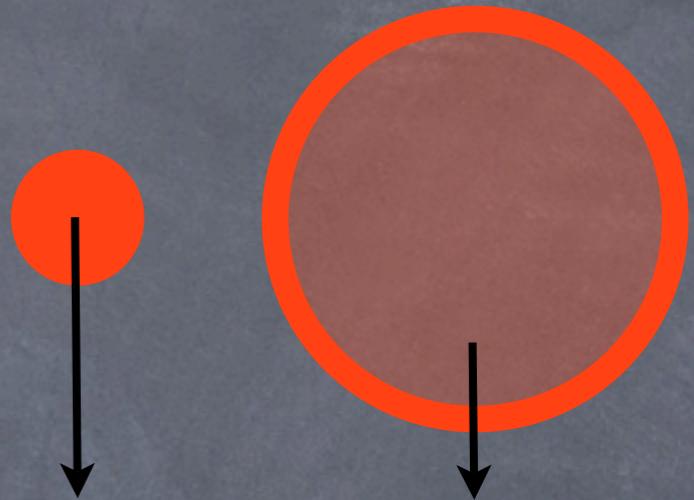
# Observational Tests

# Macroscopic Violations of Equivalence Principle

Khoury & Weltman (2003); Hui, Nicolis and Stubbs (2009)

Because of thin-shell screening, macroscopic objects fall with different acceleration in g-field

$$\vec{a} = -\vec{\nabla}\Phi + \epsilon \frac{\phi}{M^2} \vec{\nabla}\phi$$



- Unscreened objects ( $\epsilon = 1$ ) feel gravity + symmetron forces
- Screened objects ( $\epsilon = 0$ ) only feel gravity

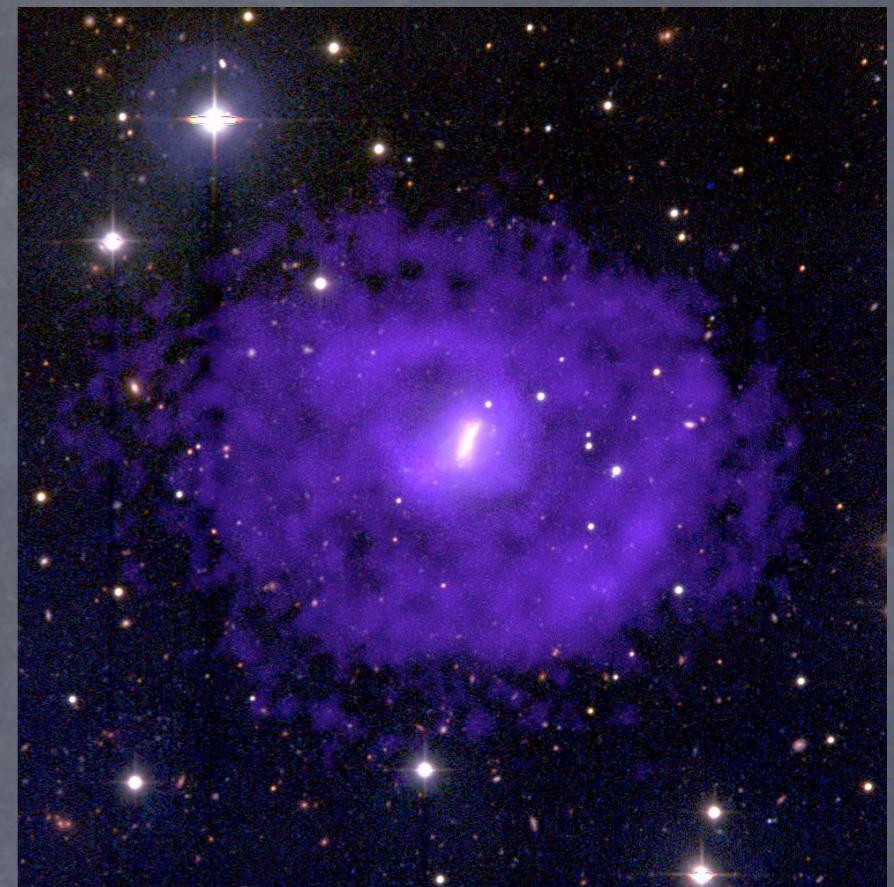
To maximize effect, look for

- large ( $\sim$  Mpc) void regions, so that symmetry is broken and  $\bar{\phi}/M^2 = 1/M_{Pl}$
- look for unscreened objects (i.e.  $\Phi < 10^{-7}$  ) in these voids

# Astrophysical signatures

Hui, Nicolis and Stubbs (2009)

- Look at dwarf galaxies in voids
- Stars are screened ( $\Phi \sim 10^{-6}$ ), but hydrogen gas is unscreened. (Gas itself has only  $\Phi \sim 10^{-11}$ .)
- Should find systematic  $O(1)$  discrepancy in the mass estimates based on these two tracers.



NOTE: Applies to chameleons and symmetrons, but not galileons.

# The Mpc barrier

Wang, Hui & J. Khoury, to appear

Chameleons/Symmetrons:  $\mathcal{L} = -\frac{1}{2}(\partial\phi)^2 - V(\phi) + A(\phi)T_\mu^\mu$

Can we ever obtain  $m_0 \sim H_0$  ? NO: Mpc is the best you can do.

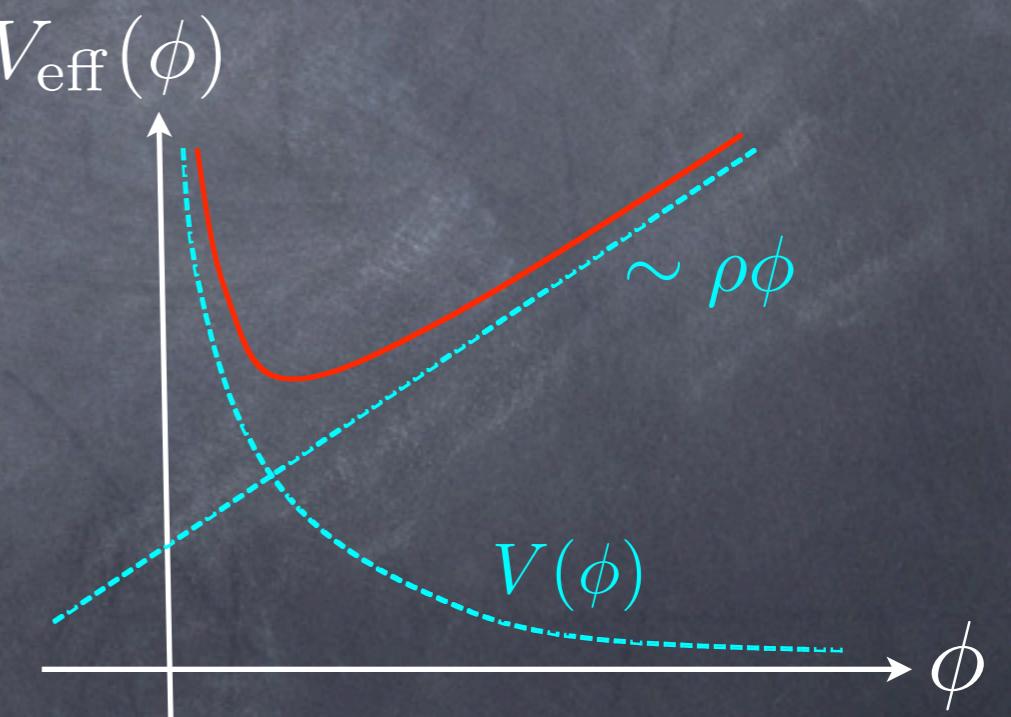
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Proof: Take chameleon with  $A(\phi) \simeq 1 + g\frac{\phi}{M_{\text{Pl}}}$



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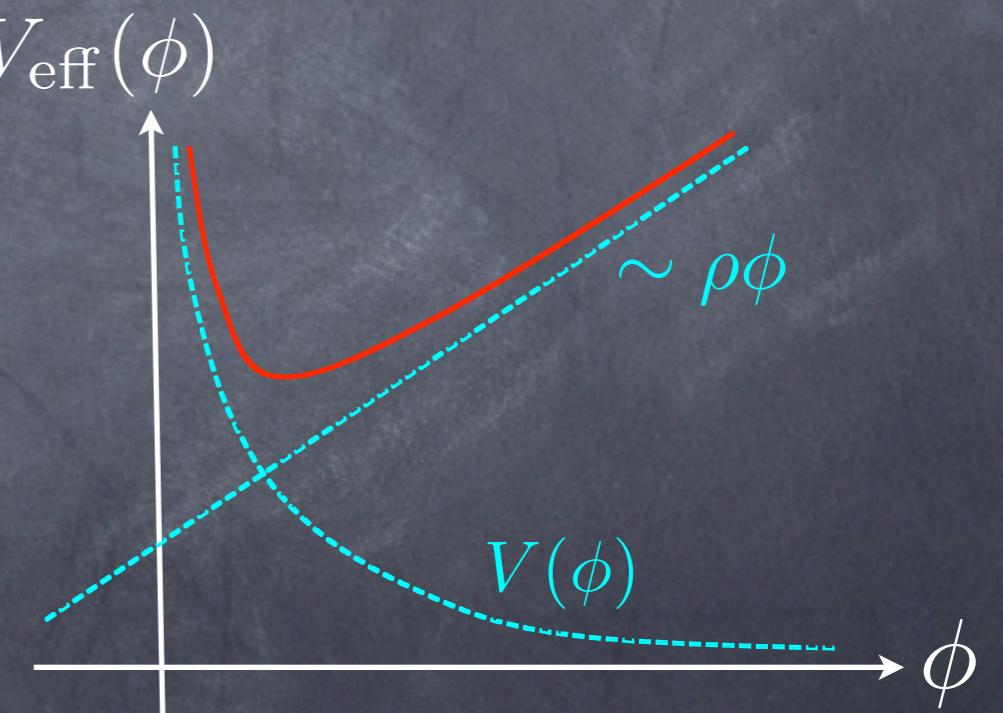
• Screening condition:

$$\frac{\Delta R}{R} \approx \frac{\phi_0}{6gM_{\text{Pl}}\Phi_N} < 1$$

Milky Way has  $\Phi_N \sim 10^{-6}$

$\implies$

$$\phi_0 \lesssim 10^{-6} M_{\text{Pl}}$$



- Cosmological evolution:

$$\ddot{\phi} + 3H\dot{\phi} = -\frac{dV}{d\phi} - \frac{g}{M_{Pl}}\rho$$

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 $\therefore$  Pretty large force!

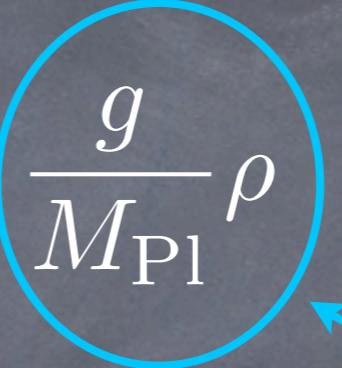
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Hence  $dV/d\phi$  &  $g\rho/M_{Pl}$  must cancel to good accuracy

• Cosmological evolution:

$$\ddot{\phi} + 3H\dot{\phi} = -\frac{dV}{d\phi} - \frac{g}{M_{Pl}}\rho$$


simply  $H^2 M_{Pl}$

∴ Pretty large force!

Hence  $dV/d\phi$  &  $g\rho/M_{Pl}$  must cancel to good accuracy

Cancellation must hold over last Hubble time:

$$\Delta \left( \frac{dV}{d\phi} + \frac{g}{M_{Pl}}\rho \right) \sim H_0^2 M_{Pl} \sim m_0^2 \Delta\phi$$

$$\implies m_0 \sim H_0 \sqrt{\frac{M_{Pl}}{\Delta\phi}} > 10^3 H_0$$

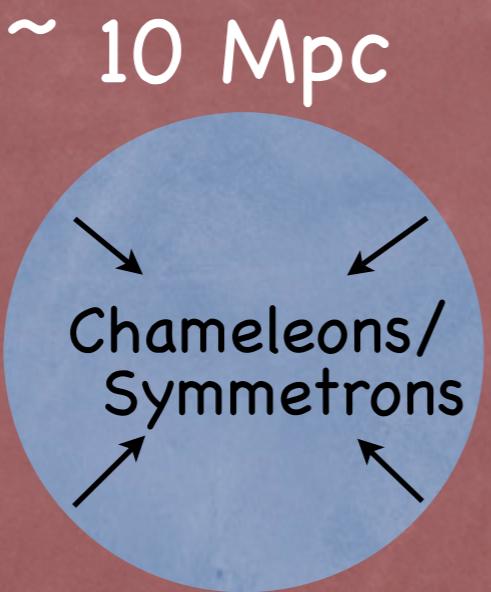
Argument generalizes to arbitrary chameleon/symmetron theories

# The Mpc divide

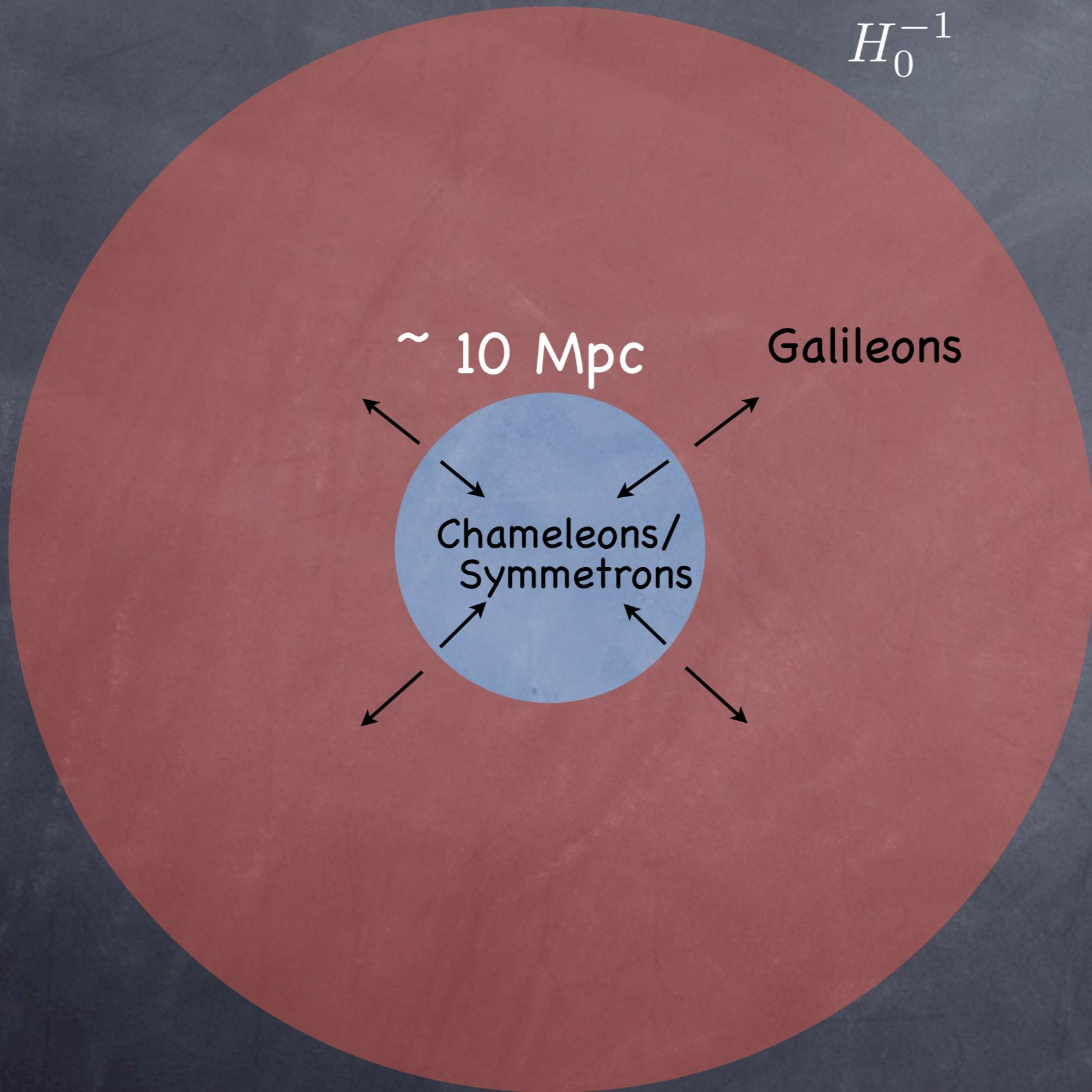
$$H_0^{-1}$$

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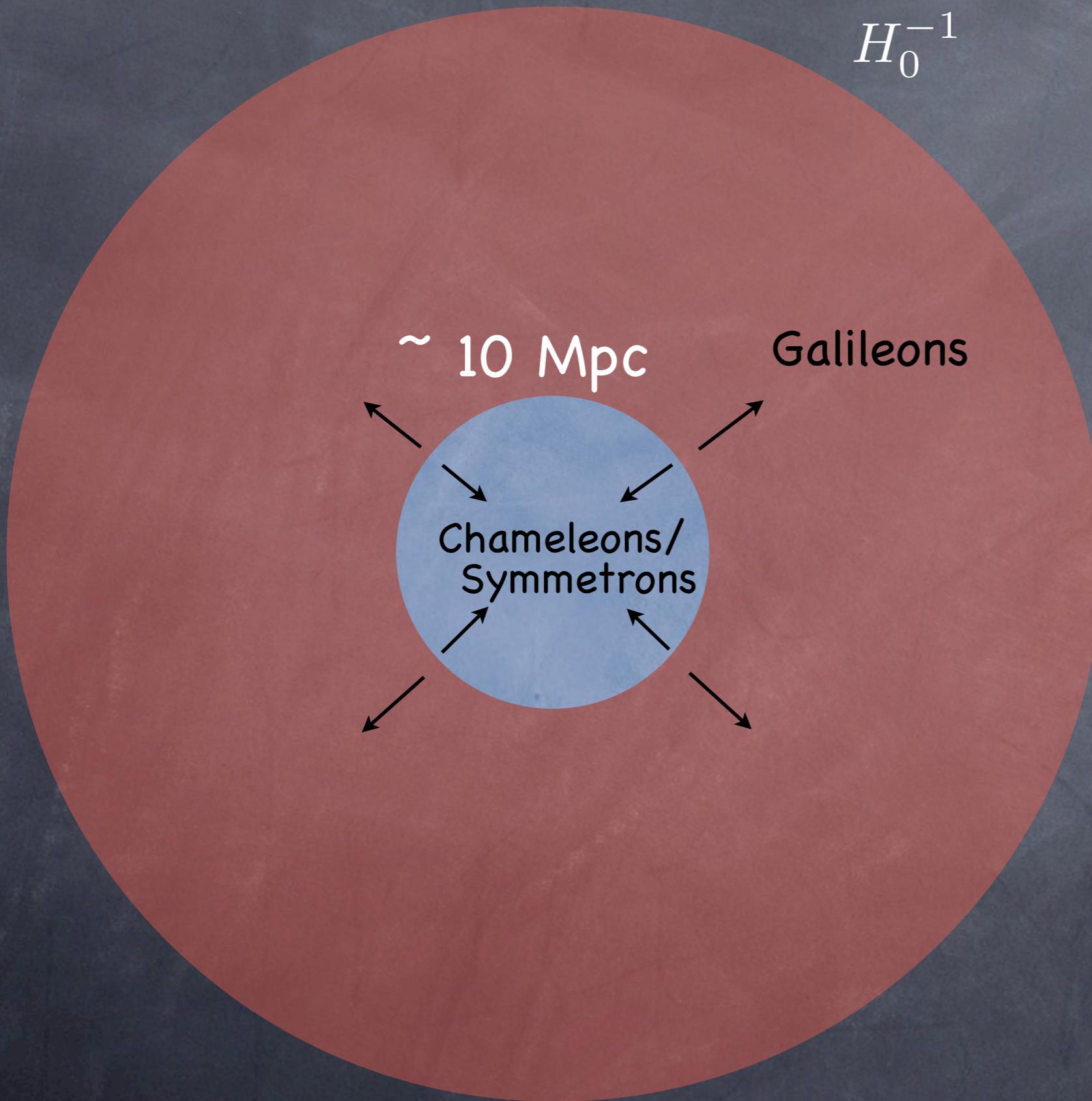
$$H_0^{-1}$$



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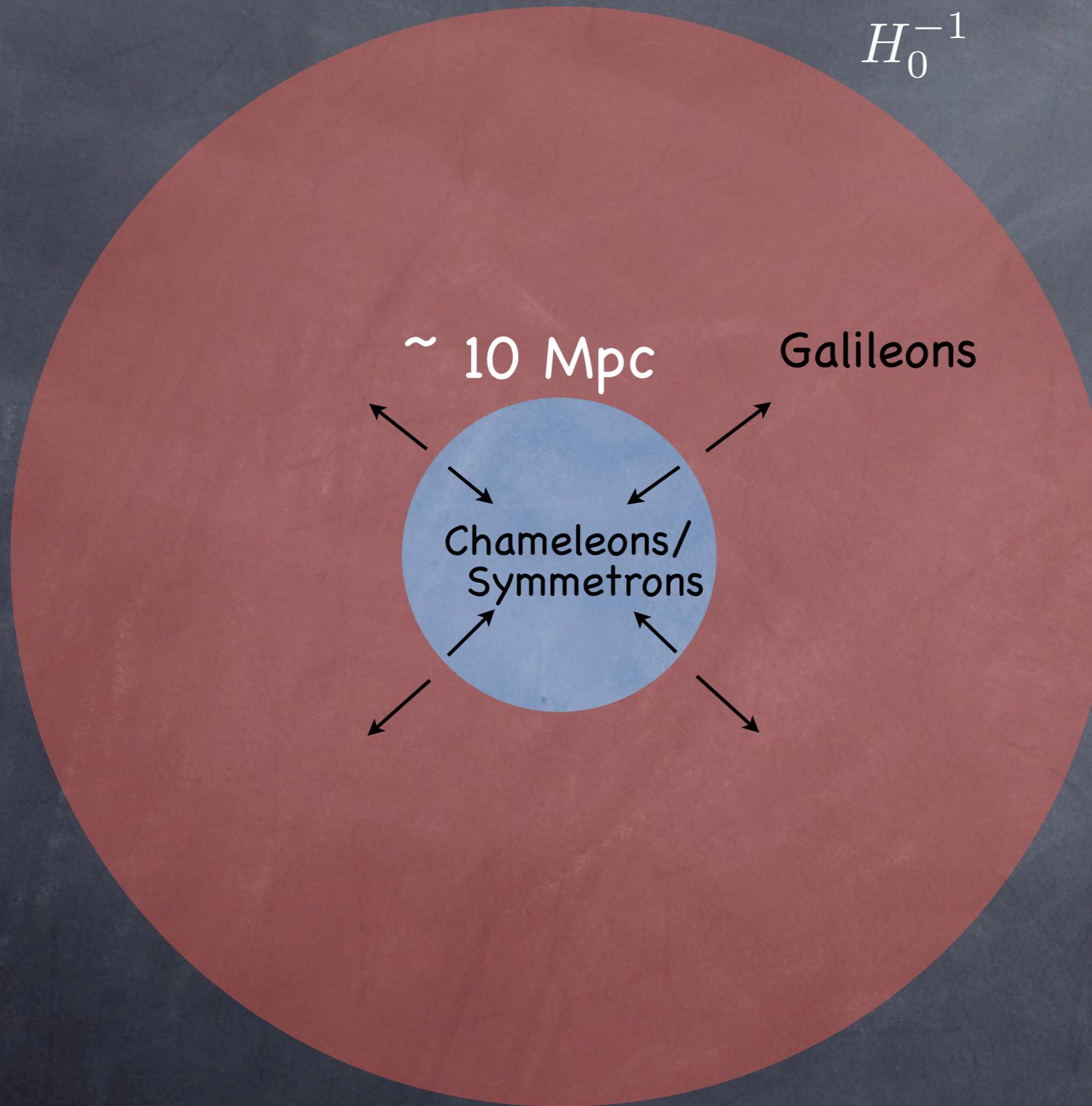


$$H_0^{-1}$$

- Galileons (DGP):  
Lombriser et al. (2009)

$L > 9000 \text{ Mpc}$

# The Mpc divide



$$H_0^{-1}$$

- ⦿ Galileons (DGP):  
[Lombriser et al. \(2009\)](#)

$$L > 9000 \text{ Mpc}$$

- ⦿ Chameleons/f(R):  
[Ferraro et al. \(2010\)](#)

$$m_0^{-1} < 10 - 100 \text{ Mpc}$$

# Tantalizing Hints?

Wyman & J. Khoury, PRD (2010)  
Lima, Wyman & J. Khoury, in progress

## i) Large Scale Bulk Flows

- Local bulk flow within  $50 h^{-1}\text{Mpc}$  is  $407 \pm 81 \text{ km/s}$   
Watkins, Feldman & Hudson (2008)
- LCDM prediction is  $\approx 180 \text{ km/s}$

Find:  $v < 240 \text{ km/s}$

## ii) Bullet Cluster (1E0657-57)

- Requires  $v_{\text{infall}} \approx 3000 \text{ km/s}$   
at  $5\text{Mpc}$  separation  
Mastropietro & Burkett (2008)  
Farrar & Rosen (2007)
- Probability in LCDM is between  $3.3 \times 10^{-11}$  and  $3.6 \times 10^{-9}$   
Lee & Komatsu (2010)



Find:  $10^4$  enhancement in prob.

### iii) Void phenomenon

Peebles, astro-ph/0712.2757  
Nusser, Gubser & Peebles, PRD (2005)

$$V(r) = -\frac{\beta G m^2}{r} e^{-r/r_s}$$

with  $\beta \sim \mathcal{O}(1)$ ;  $r_s \sim \text{Mpc}$

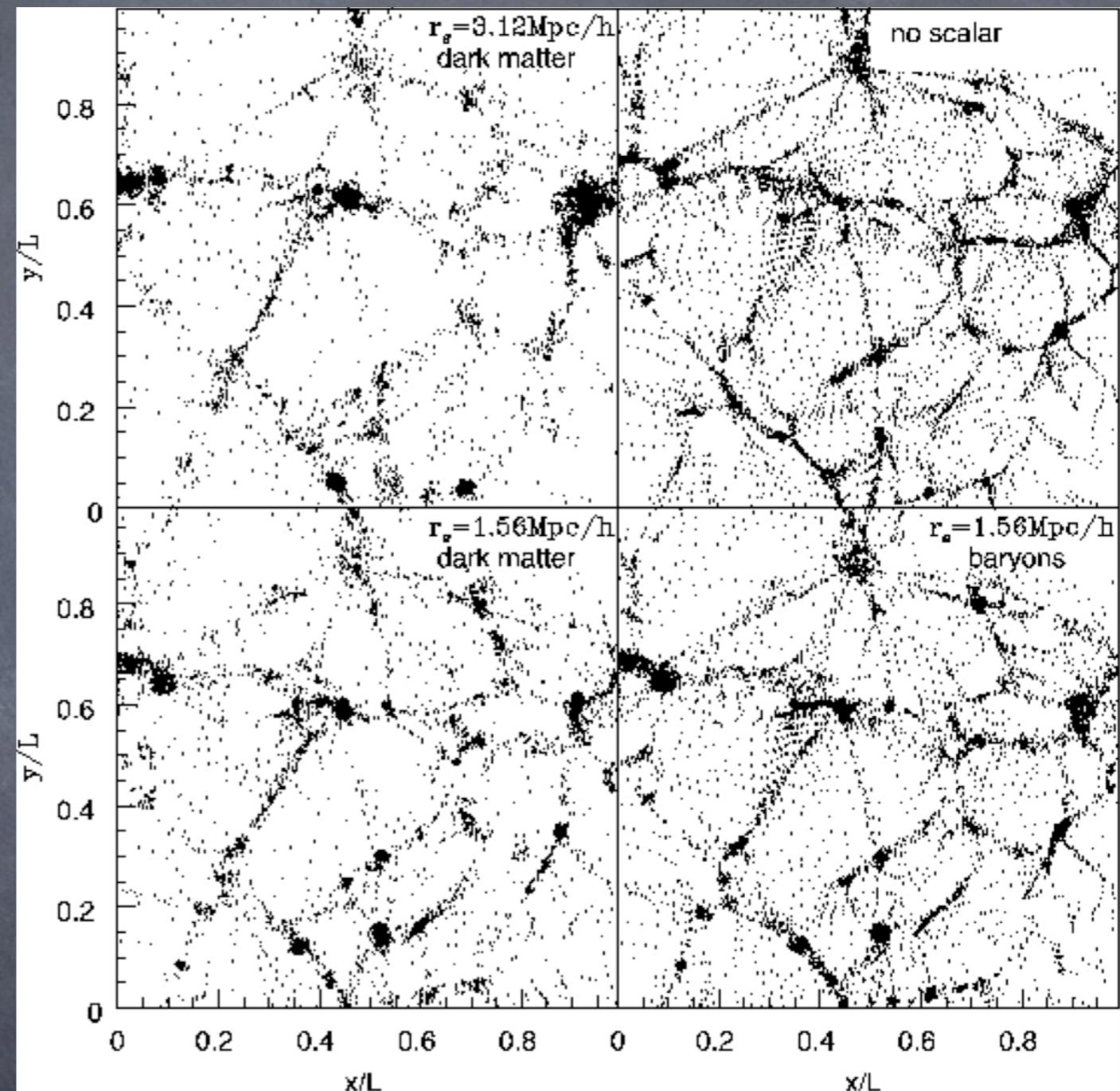
Between DM only!!!

\* However, Yukawa force is tightly constrained on galactic scales:

$$\beta < 0.1$$

Kesden & Kamionkowski, PRL (2007)

(See, however, Peebles et al. (2009).)



But screening mechanism circumvents Kesden-Kamionkowski because Milky Way is screened.



Thank you!