

Nernst effect in the cuprates



Stockholm, July 2010

Nernst effect in the cuprates

Andreas Hackl

(California Institute of Technology)



Cologne: Matthias Vojta

Harvard: Subir Sachdev

Contents

1) Nernst effect in the Cuprates (historical remarks)

Nernst effect due to quasiparticles/vortices

2) Nernst effect in the presence of stripe order

Stripe order enhances the Nernst effect

3) Nernst effect and rotational symmetry breaking

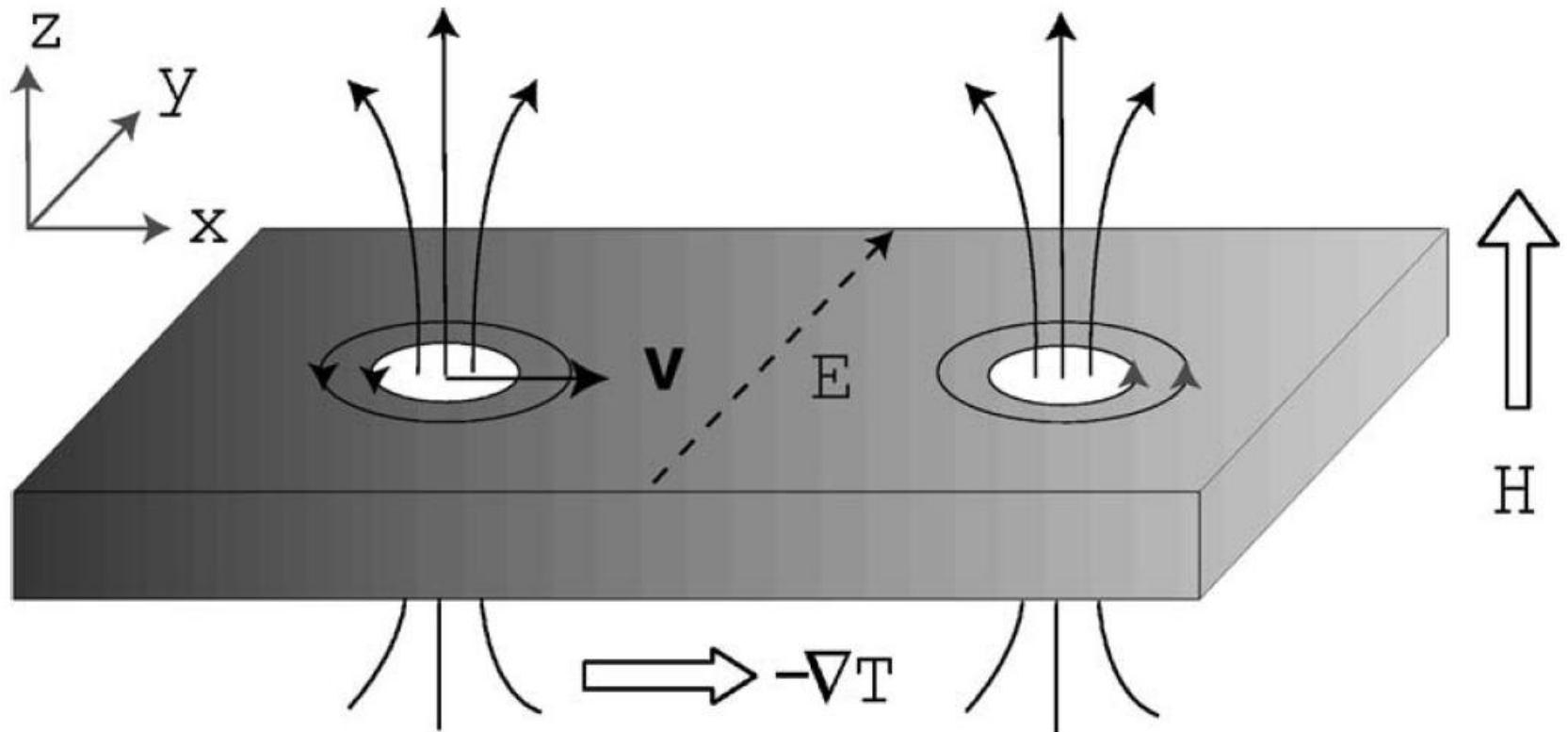
Important new insights into the pseudogap phase

Nernst effect and cuprates

The Nernst effect

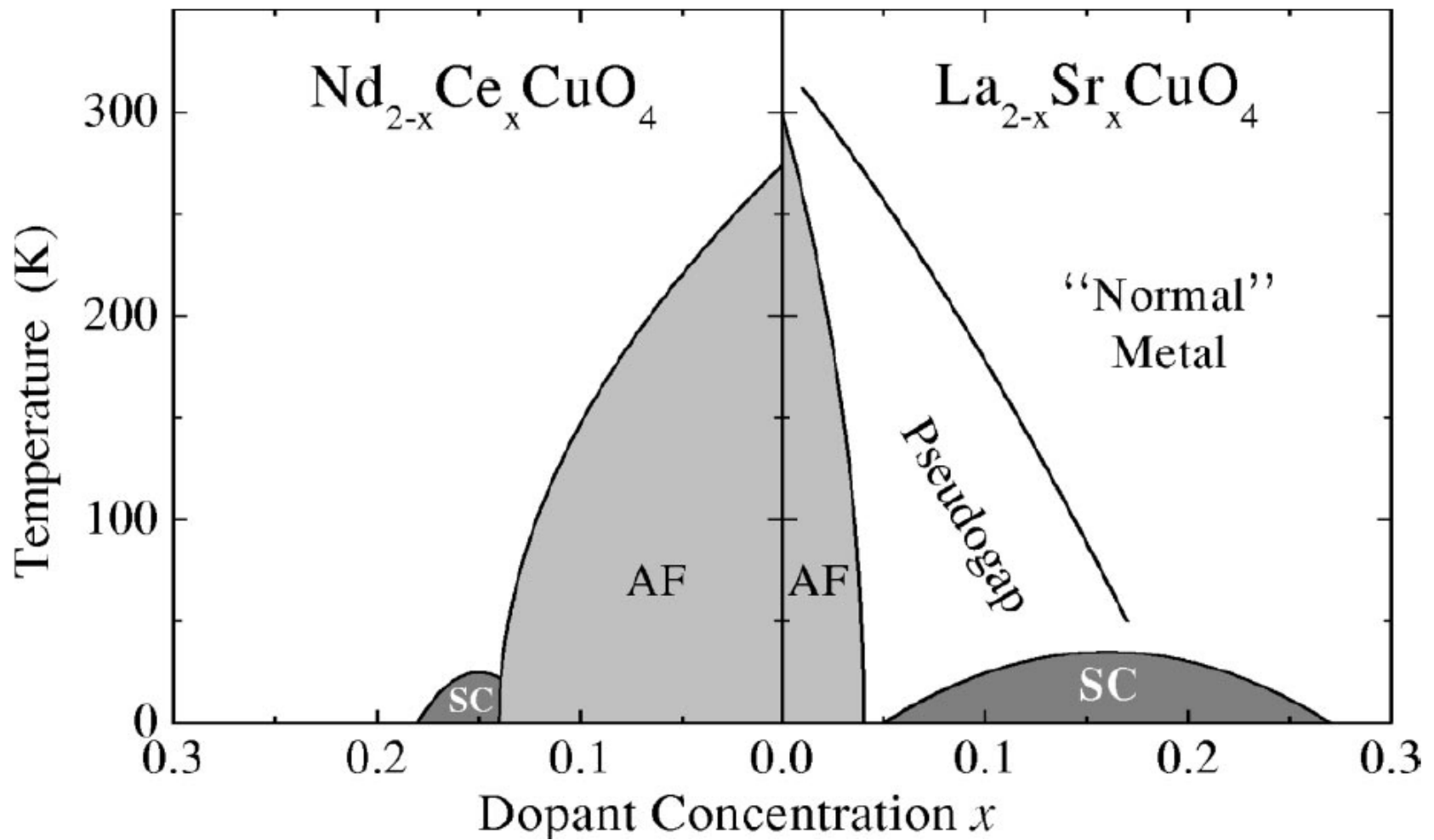
- Thermoelectric phenomenon observed in strong magnetic fields
- Very small and featureless in metals
- Important role for correlated electron systems only recently due to discovery of large Nernst signal in cuprate materials
- Potential of new insights into origin of cuprate phase diagram

Nernst effect

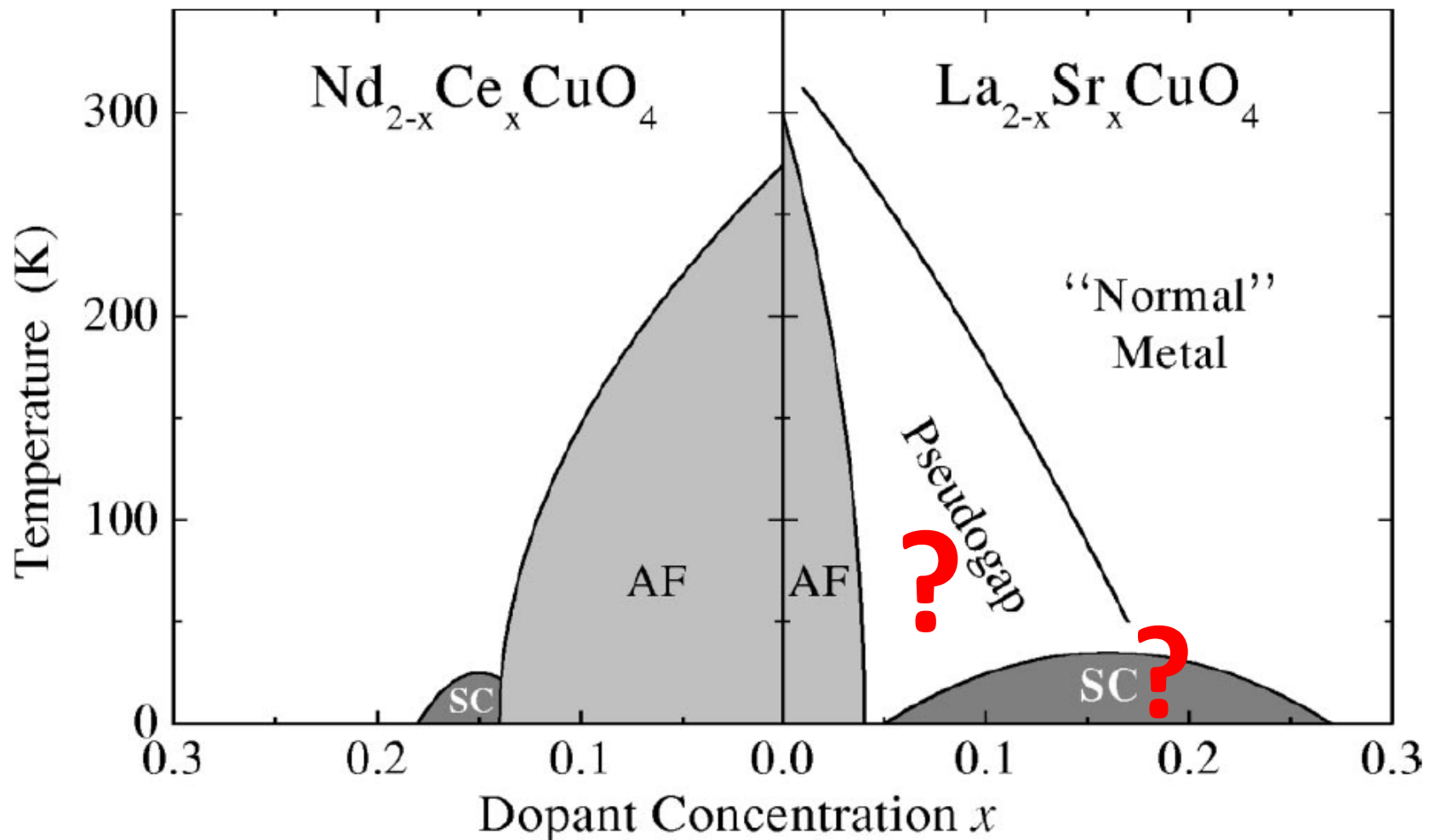


Thermal analogon to Hall effect

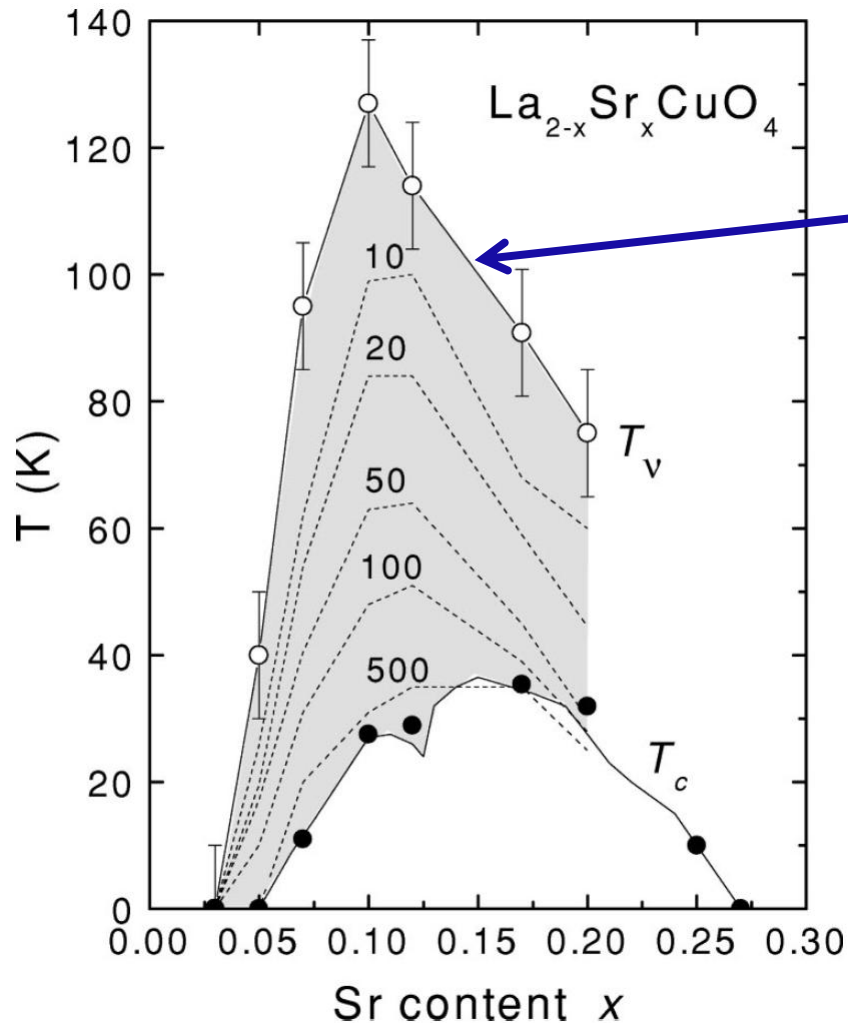
The cuprates



The cuprates



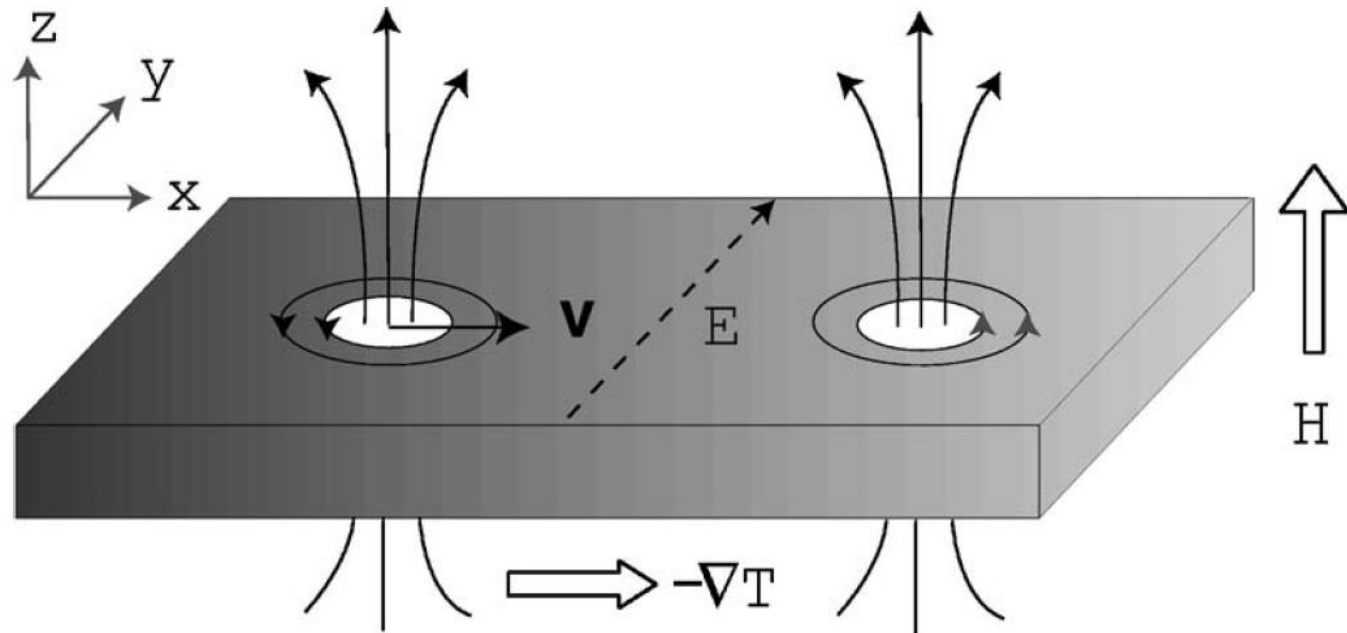
Nernst effect near superconducting dome



contours of constant v
[nV/KT]

Vortices in thermal
gradient produce
strong Nernst signal

Phenomenological explanation



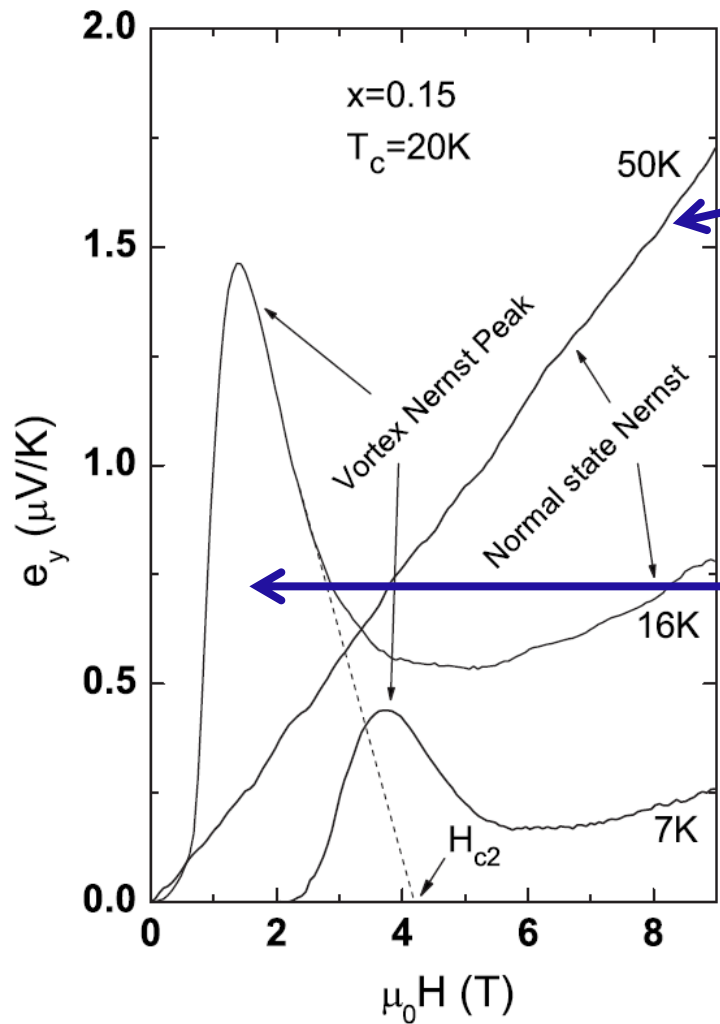
Josephson equation: $2eV_J = \hbar\dot{\Theta}$

of drifting vortices: $\dot{\Theta} = 2\pi\dot{N}_V$



Transverse Voltage

Quasiparticle Nernst effect



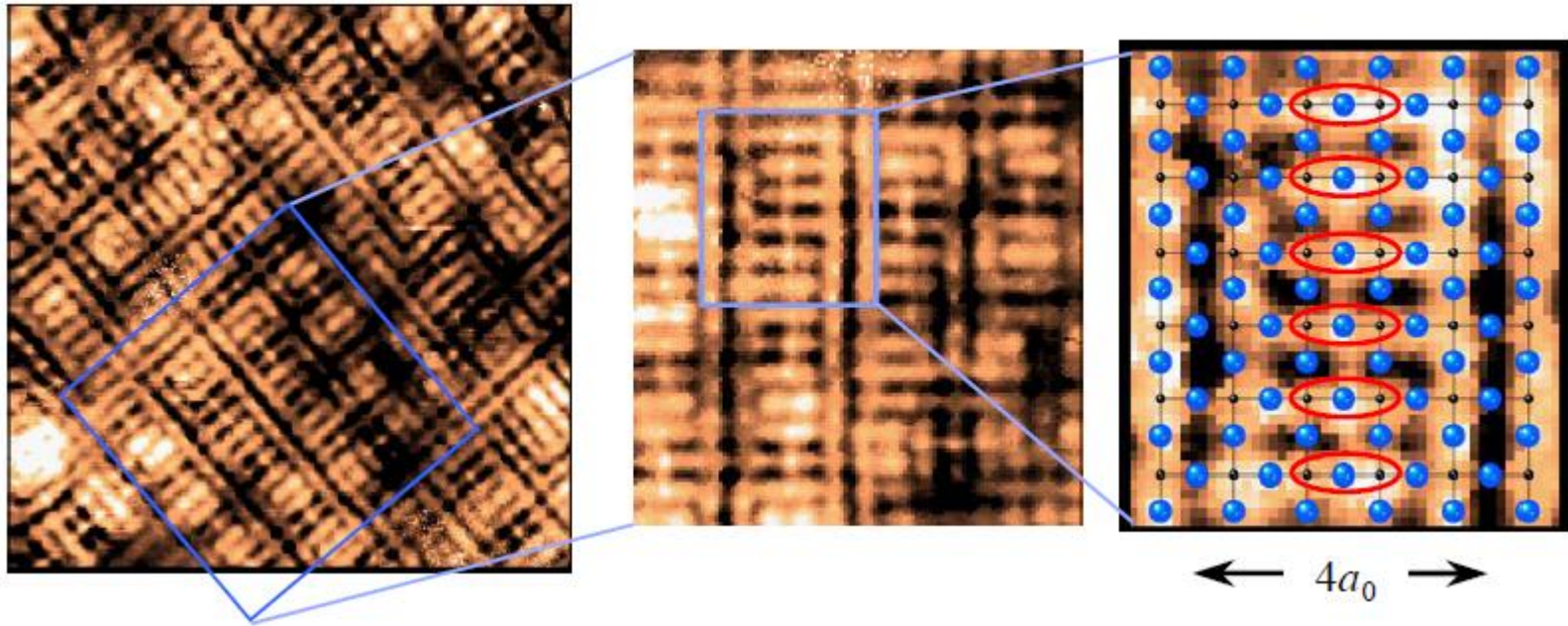
Nernst effect linear in magnetic field: normal state quasiparticles

Vortex Nernst effect, suppressed in strong magnetic fields

Nernst effect and stripe order

Stripe order

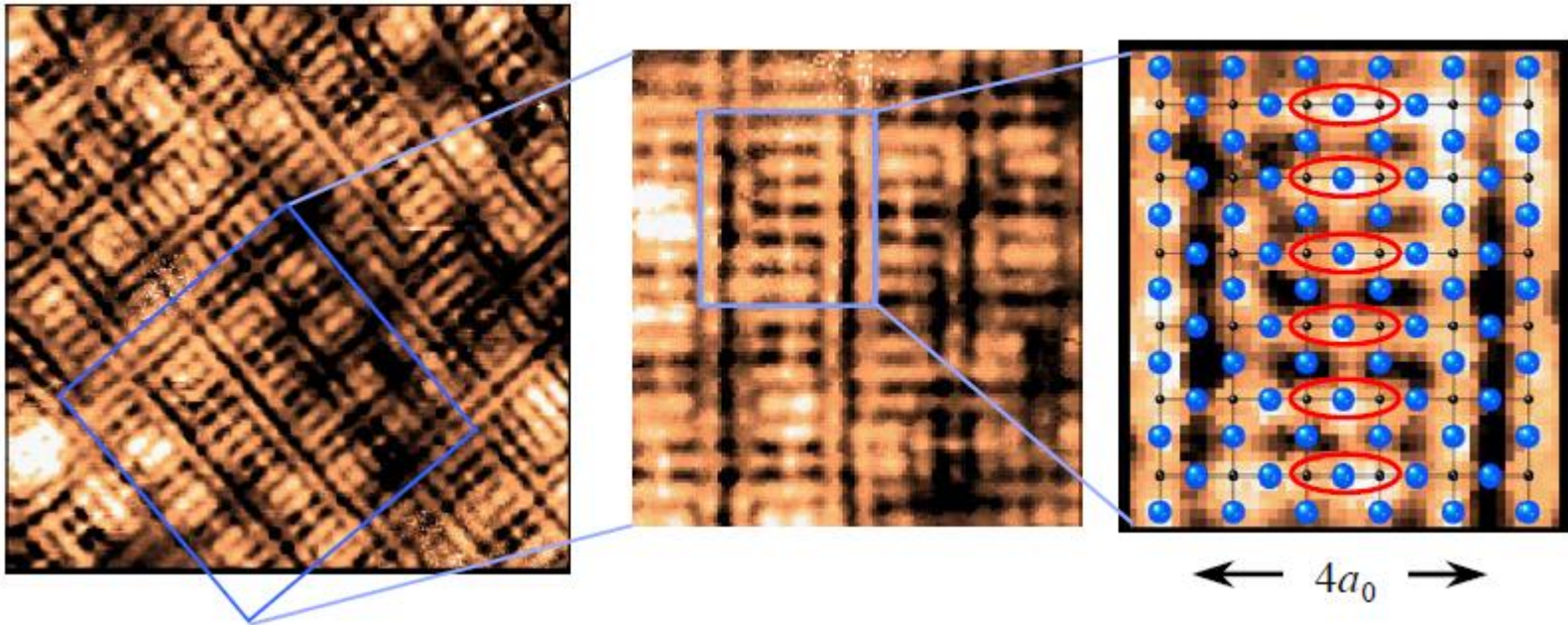
R map (asymmetry) at 150 meV



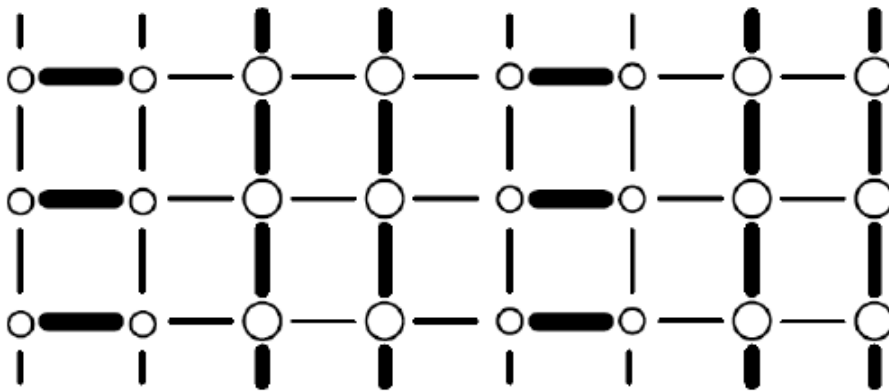
Kohsaka et al., Science **315**, 1380 (2007)

Stripe order

R map (asymmetry) at 150 meV



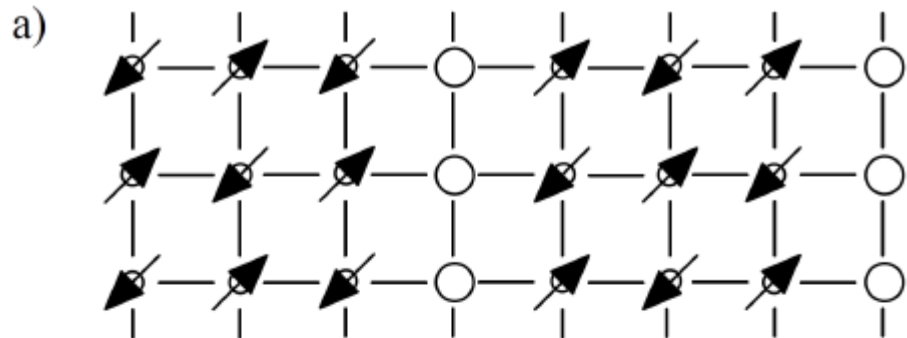
Kohsaka et al., Science **315**, 1380 (2007)



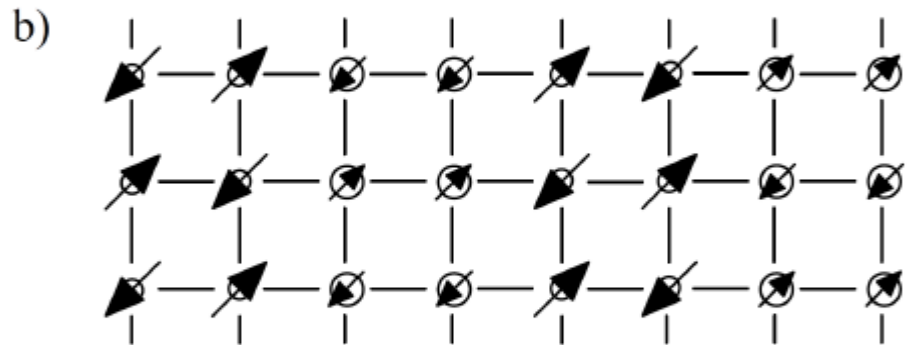
Unconventional order:
„d-wave“ stripes

Vojta / Rösch, PRB **77**, 094504 (2008)

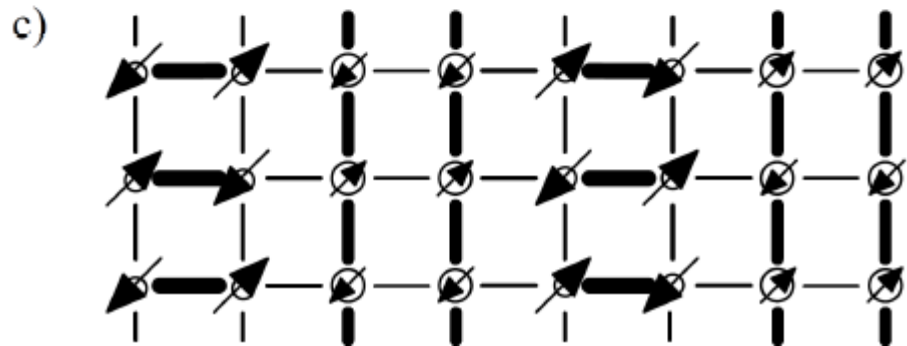
Stripe order



On mean-field level:
provides scattering potential
for quasiparticles



$$\hat{V}_{s,c} = \sum_{\vec{k}\sigma} V_{s,c}(\vec{k}) c_{\vec{k}+\vec{Q}_{s,c}\sigma}^\dagger c_{\vec{k}\sigma} + h.c.$$



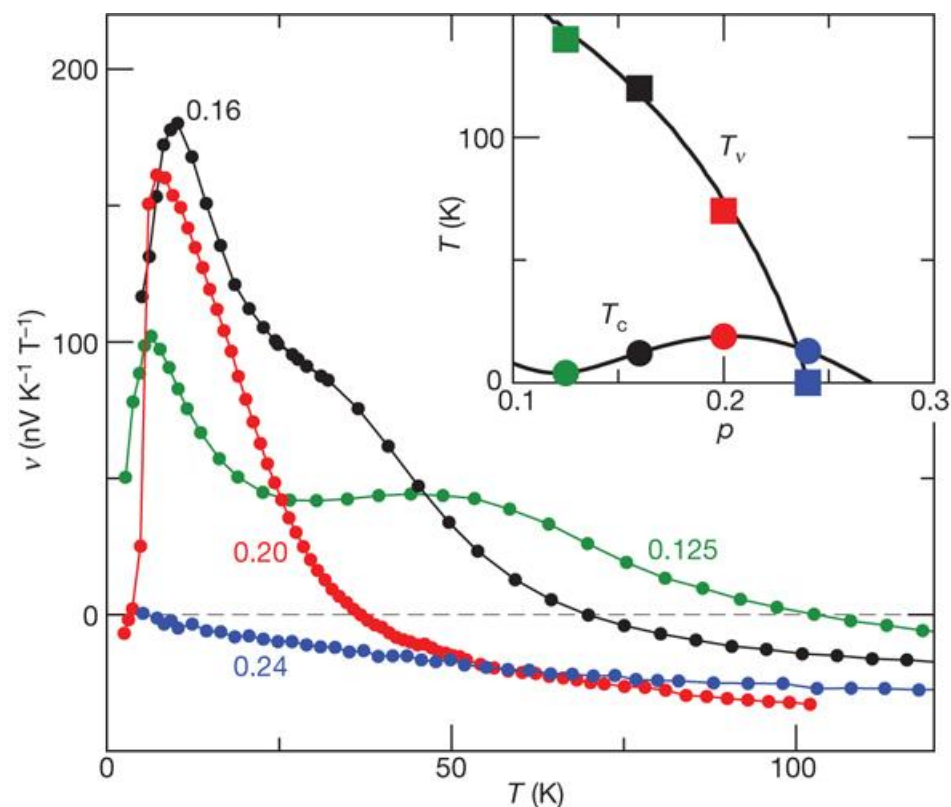
LETTERS

Eu-LSCO
Nd-LSCO**Enhancement of the Nernst effect by stripe order in a high- T_c superconductor**

Olivier Cyr-Choinière^{1*}, R. Daou^{1*}, Francis Laliberté¹, David LeBoeuf¹, Nicolas Doiron-Leyraud¹, J. Chang¹, J.-Q. Yan^{2†}, J.-G. Cheng², J.-S. Zhou², J. B. Goodenough², S. Pyon³, T. Takayama³, H. Takagi^{3,4}, Y. Tanaka^{5,3} & Louis Taillefer^{1,6}

Nernst signal shows two „peaks“:

- 1) Superconducting fluc. at low T
- 2) Fermi surface reconstruction at higher T



Cyr-Choiniere Nature **458**, 743 (2009)

Theoretical question:

To what extent can this peak structure of the Nernst effect be explained in terms of normal state quasiparticles?

Semiclassical calculation

Quasiparticle Hamiltonian

$$H = \sum_{\vec{k}\sigma} \epsilon_{\vec{k}} c_{\vec{k}\sigma}^{\dagger} c_{\vec{k}\sigma} + \sum_{\vec{k}\sigma} V_{s,c}(\vec{k}) c_{\vec{k}+\vec{Q}_{s,c}\sigma}^{\dagger} c_{\vec{k}\sigma} + h.c.$$

Boltzmann equation

$$\left[-\frac{e}{\hbar c} (\mathbf{v}_{\mathbf{k}} \times \mathbf{B}) \cdot \nabla_{\mathbf{k}} + \frac{1}{\tau(\epsilon_{\mathbf{k}})} \right] g_{\mathbf{k}} = \left[-e \mathbf{v}_{\mathbf{k}} \mathbf{E} - (\epsilon_{\mathbf{k}} - \mu) \mathbf{v}_{\mathbf{k}} \frac{\nabla_r T}{T} \right] \left(-\frac{\partial f_{\mathbf{k}}^0}{\partial \epsilon_{\mathbf{k}}} \right)$$

$$g(\mathbf{k}) = f(\mathbf{k}) - f_0(\mathbf{k})$$

Semiclassical calculation

Linear response

$$\begin{pmatrix} \vec{J} \\ \vec{Q} \end{pmatrix} = \begin{pmatrix} \hat{\sigma} & \hat{\alpha} \\ T\hat{\alpha} & \hat{\kappa} \end{pmatrix} \begin{pmatrix} \vec{E} \\ -\vec{\nabla}T \end{pmatrix}$$

Nernst signal:

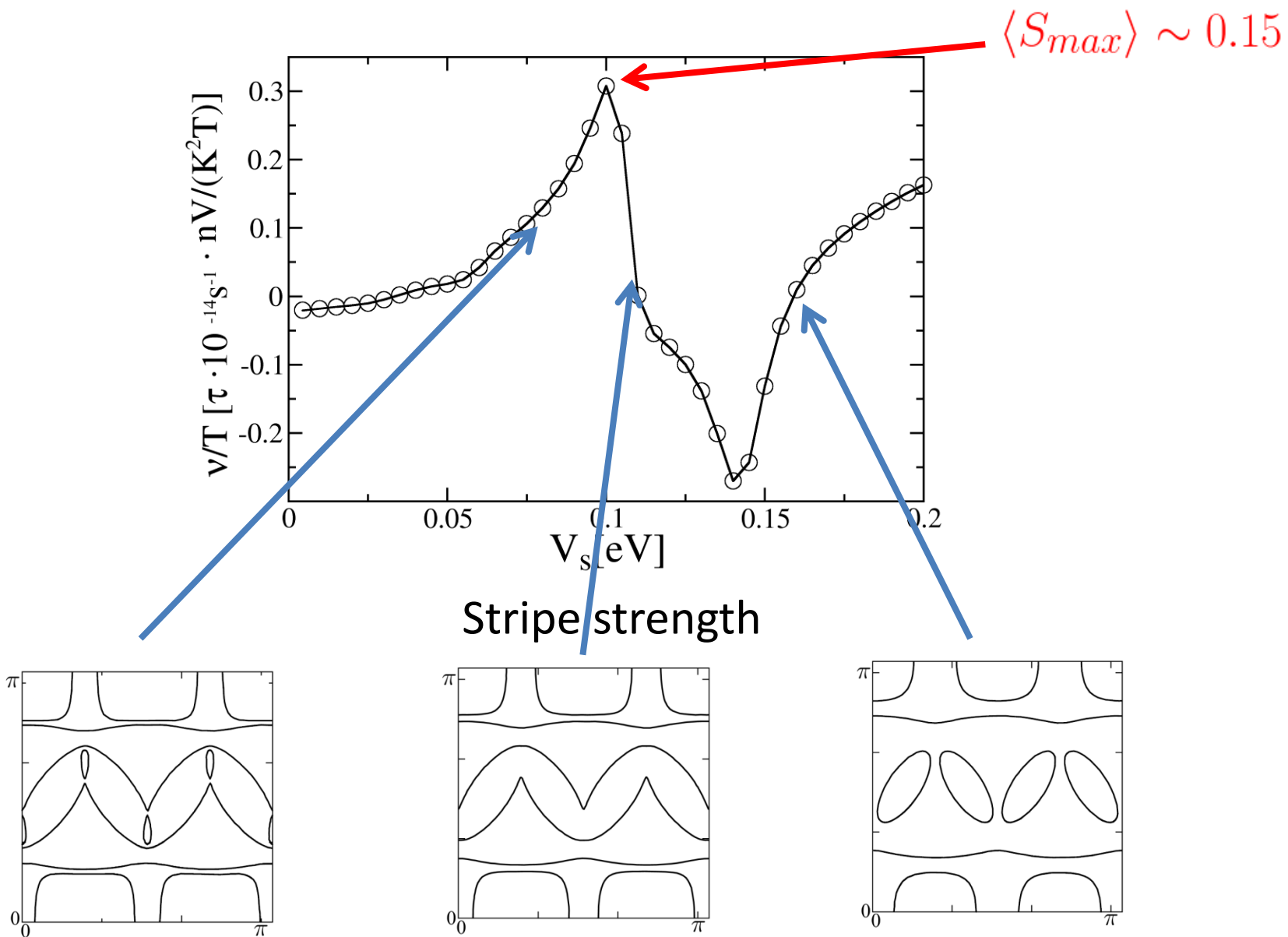
$$\vec{E} = -\hat{\vartheta} \nabla T \quad (\text{no charge current, } B \text{ field } \parallel z)$$

$$\vartheta_{yx} = -\frac{\sigma_{xx}\alpha_{yx} - \sigma_{yx}\alpha_{xx}}{\sigma_{xx}\sigma_{yy} - \sigma_{xy}\sigma_{yx}}$$

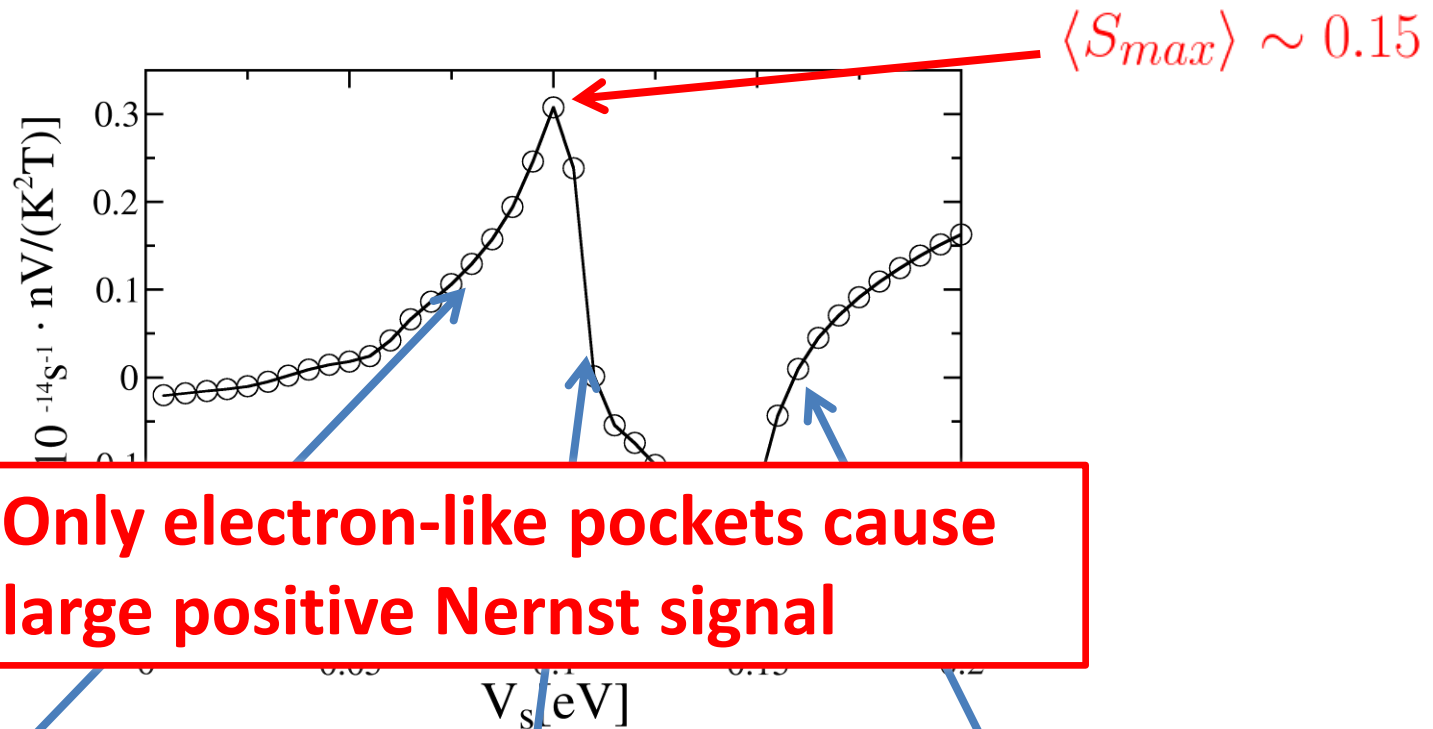
Nernst coefficient:

$$\nu = \vartheta_{yx}/B \quad (\sim T \text{ at low } T)$$

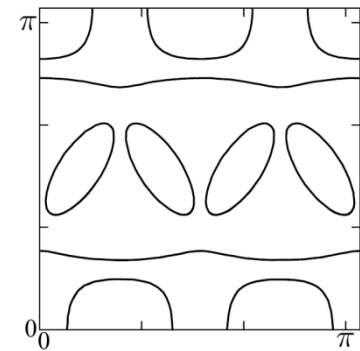
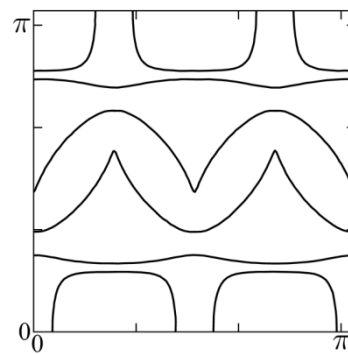
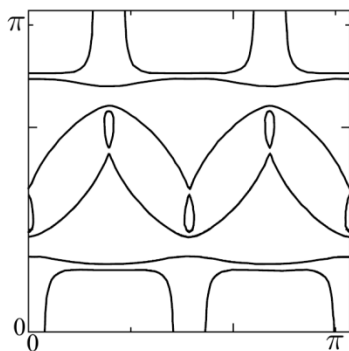
Nernst signal for CDW+SDW (period 8)



Nernst signal for CDW+SDW (period 8)



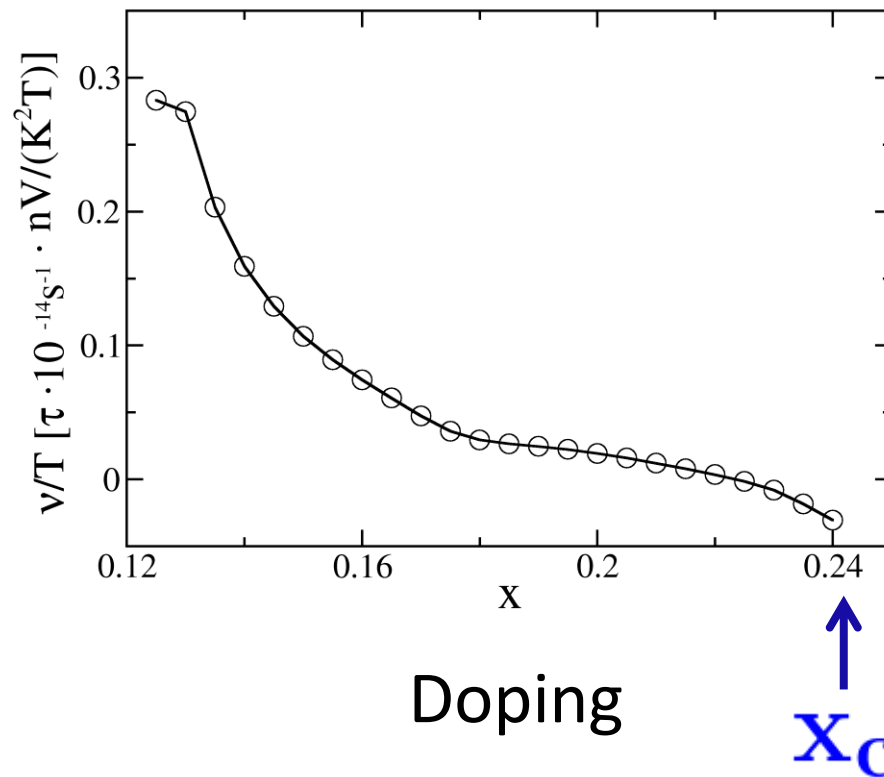
Only electron-like pockets cause large positive Nernst signal



Nernst signal for CDW+SDW (period 8)

Assuming a mean-field dependence of the stripe order parameter on doping:

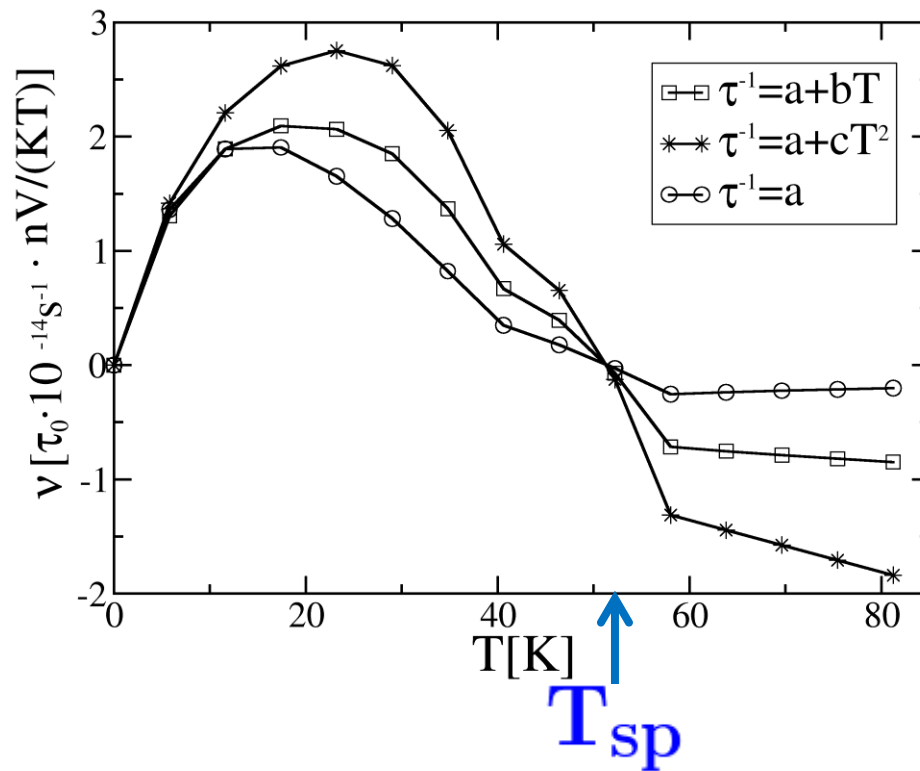
$$V_s(x) = V_0 \sqrt{1 - x/x_c}$$



Nernst signal for CDW+SDW (period 8)

Assuming a mean-field dependence of the stripe order parameter on temperature:

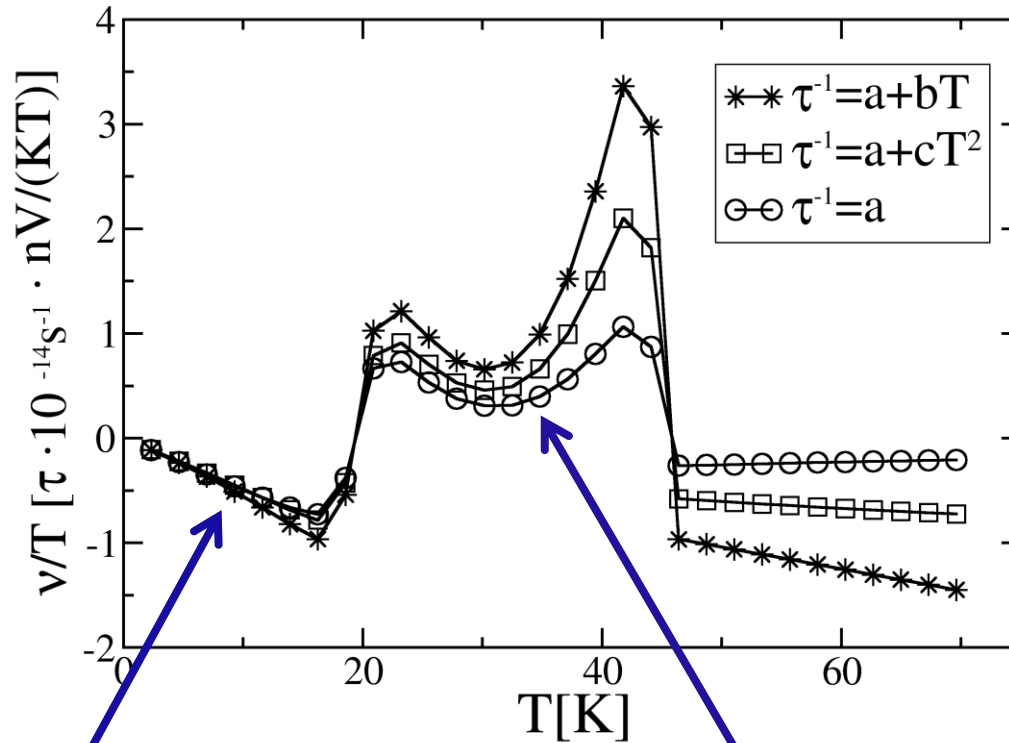
$$V_s(T) = V_0 \sqrt{1 - T/T_{sp}}$$



Nernst signal for CDW+SDW (period 10)

Period-10 stripe order with

$$V_s(T) = V_0 \sqrt{1 - T/T_{sp}}$$



Only hole pockets

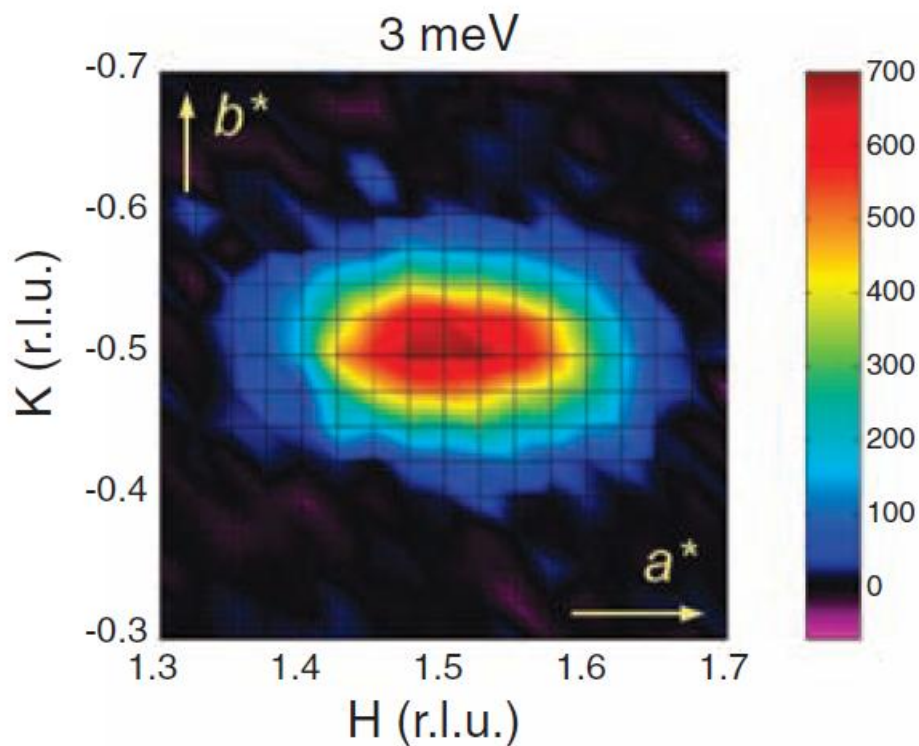
Electron pockets

Intermediate conclusions

- Fermi surface reconstruction due to stripe order in agreement with enhanced positive Nernst signal
- Sign changes of Nernst signal as function of temperature predicted in underdoped region
- Further experiments for different dopings needed to check theoretical results

Nernst effect and rotational symmetry breaking

Electron nematic order in cuprates

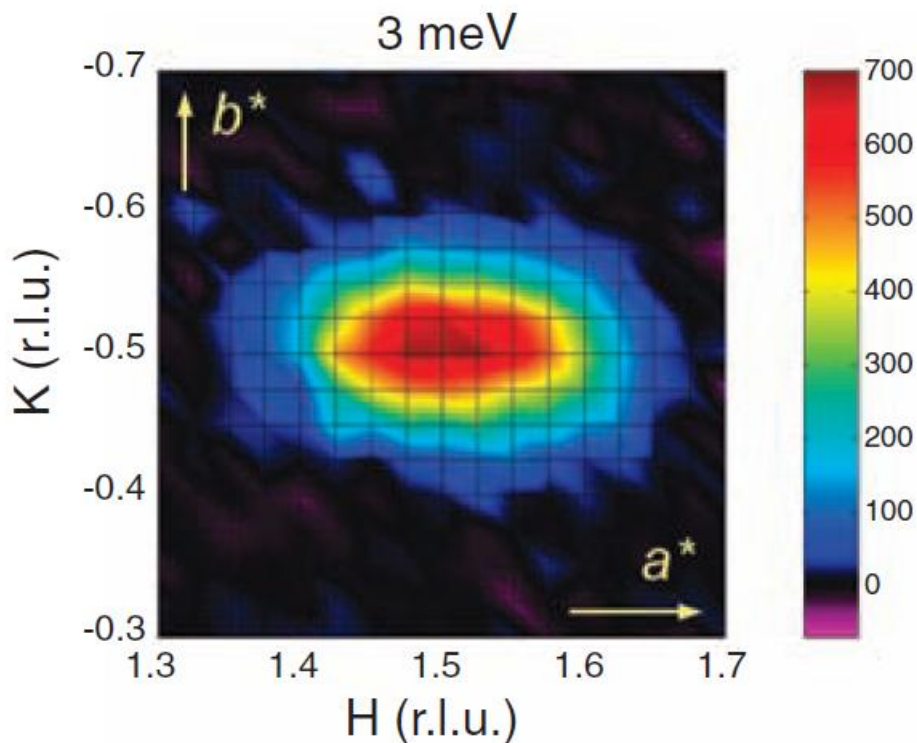


Electronic Liquid Crystal State in the High-Temperature Superconductor $\text{YBa}_2\text{Cu}_3\text{O}_{6.45}$

V. Hinkov,^{1*} D. Haug,¹ B. Fauqué,² P. Bourges,² Y. Sidis,² A. Ivanov,³
C. Bernhard,⁴ C. T. Lin,¹ B. Keimer¹

Anisotropic spin
fluctuations detected

Electron nematic order in cuprates



Electronic Liquid Crystal State in the High-Temperature Superconductor YBa₂Cu₃O_{6.45}

V. Hinkov,^{1*} D. Haug,¹ B. Fauqué,² P. Bourges,² Y. Sidis,² A. Ivanov,³
C. Bernhard,⁴ C. T. Lin,¹ B. Keimer¹

Anisotropic spin
fluctuations detected

**Electronic liquid-crystal
phases of a doped
Mott insulator**

S. A. Kivelson*, E. Fradkin† & V. J. Emery‡

Proposed theoretically
years before

Is the pseudogap phase a nematic phase?

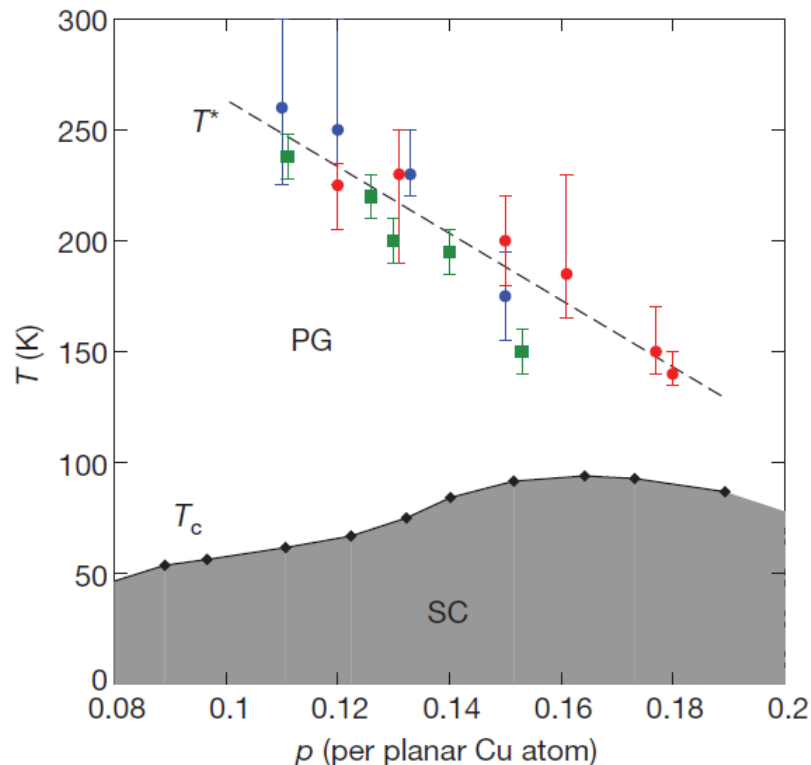
Vol 463 | 28 January 2010 | doi:10.1038/nature08716

nature

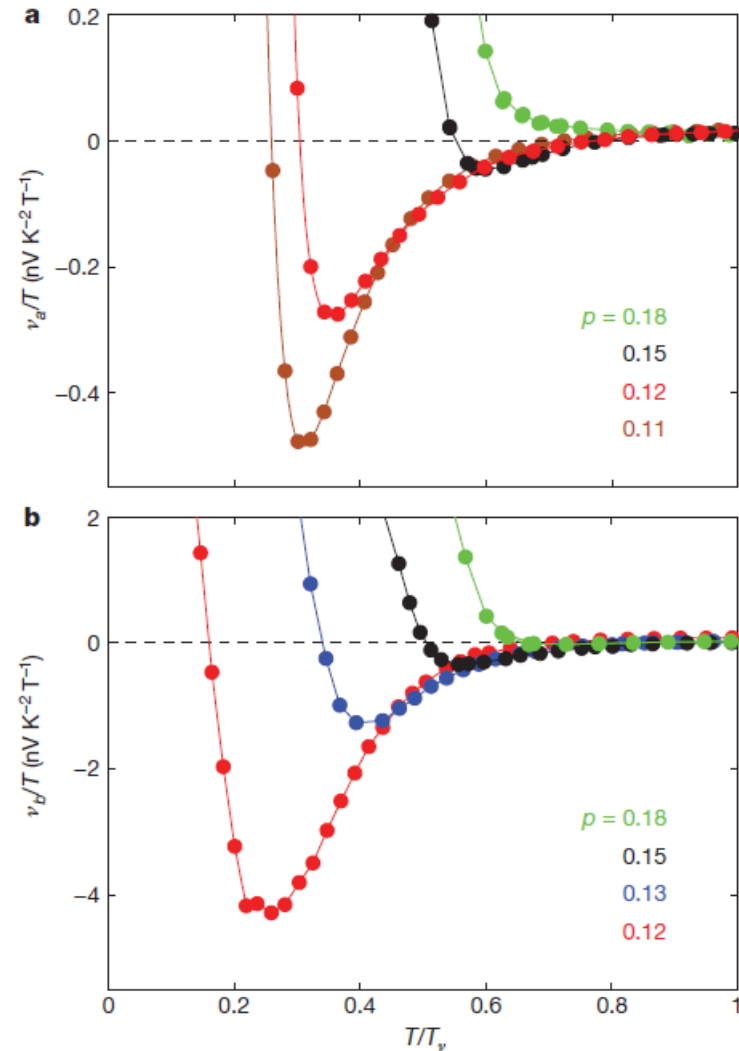
LETTERS

Broken rotational symmetry in the pseudogap phase of a high- T_c superconductor

R. Daou¹†, J. Chang¹, David LeBoeuf¹, Olivier Cyr-Choinière¹, Francis Laliberté¹, Nicolas Doiron-Leyraud¹, B. J. Ramshaw², Ruixing Liang^{2,3}, D. A. Bonn^{2,3}, W. N. Hardy^{2,3} & Louis Taillefer^{1,3}



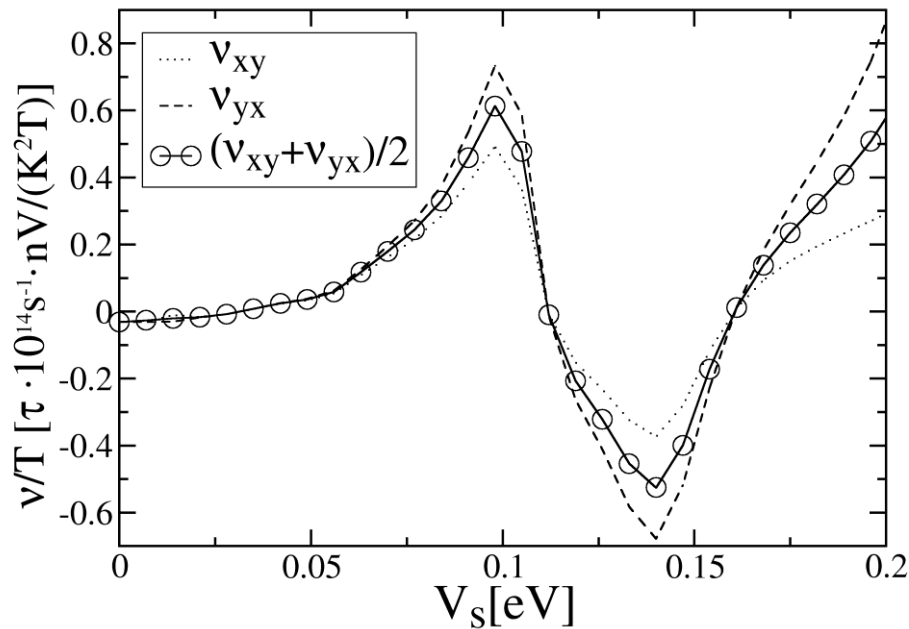
Nernst signal



Stripe order is not enough

Anisotropy ratio too small (≤ 2 for relevant stripe potential strengths)

Example: period 8 stripe order



Electron nematic order

Nematic order distorts band structure

here: $d_{x^2-y^2}$ symmetry

(e.g., precursor of stripe phase)

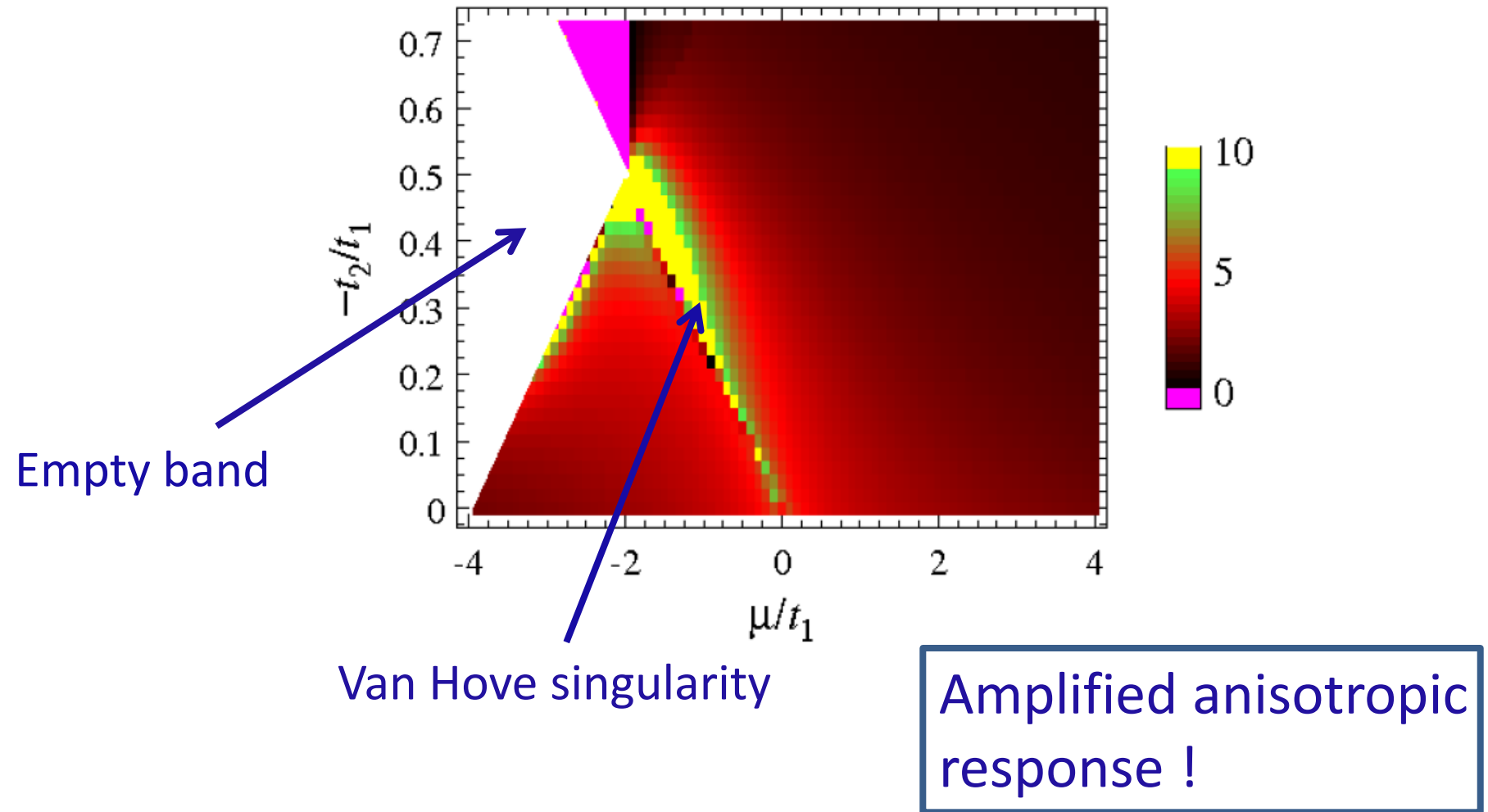
distorted hoppings:

$$\begin{aligned}t_{1x,y} &= (1 \pm \epsilon/2)t_1 \\ t_{3x,y} &= (1 \pm \epsilon/2)t_3\end{aligned}$$

Lattice symmetry: $C_4 \longrightarrow C_2$

Anisotropic Nernst effect

$$d(\nu_{yx} - \nu_{xy})/(\nu d\epsilon)$$

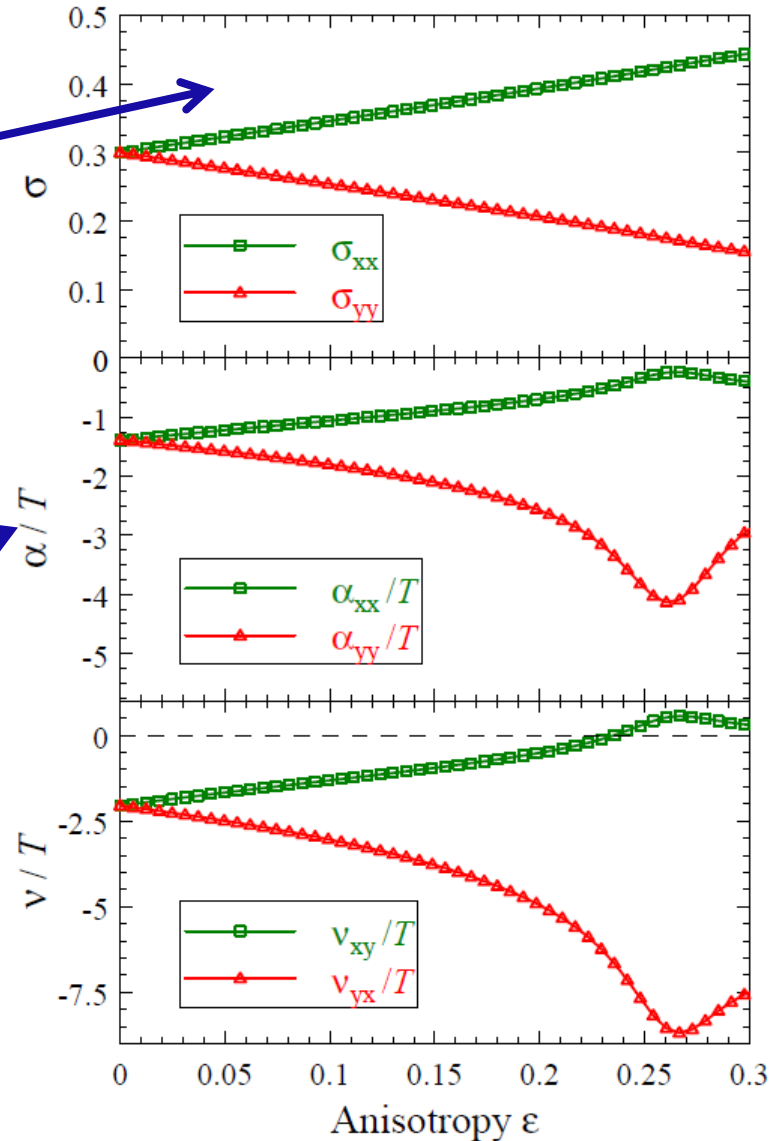


Anisotropic Nernst effect

Typical cuprate parameters;

Small anisotropy

Large anisotropy



Summary

Summary

- Strong enhancement of quasiparticle Nernst effect in strongly stripe ordered cuprates at doping $x=1/8$, qualitative agreement with experiment
- Proposed Nernst signal as unique tool for detection of broken rotational symmetry, e.g. also in $\text{Sr}_3\text{Ru}_2\text{O}_7$
- Results strengthen proposal of the identification of pseudogap phase as nematically ordered state