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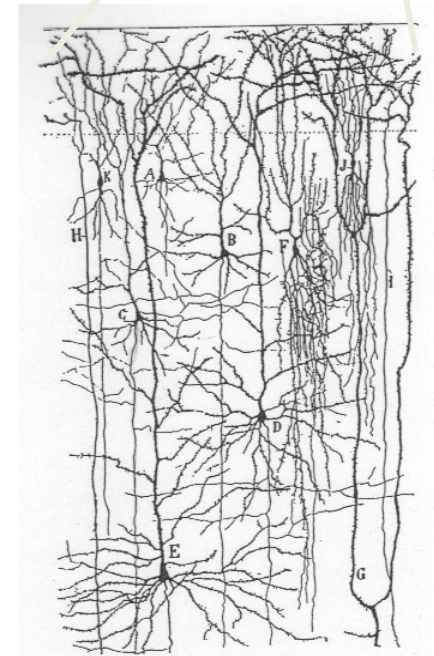
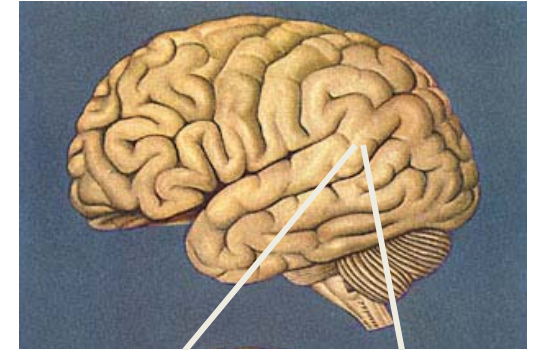
# Very large-scale brain simulations using supercomputers

**Anders Lansner**

**Dept of Computational Biology  
KTH and Stockholm University**

# Our brain = "alien technology"

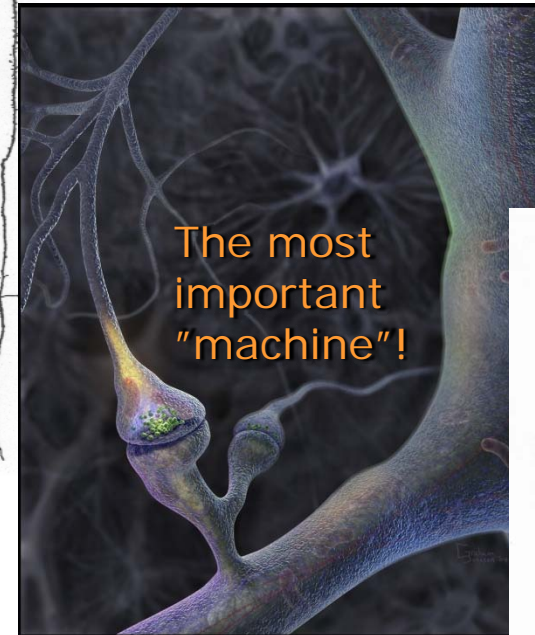
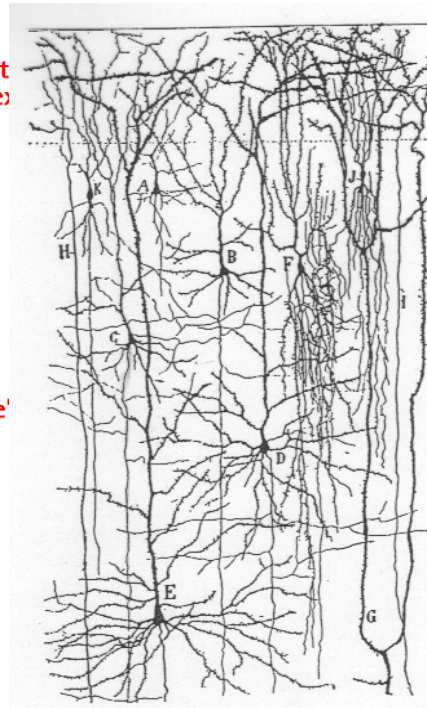
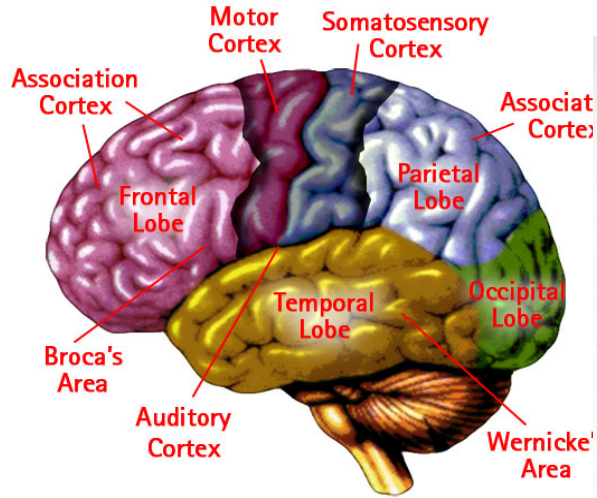
- **Volume: 1.5 liters**
- **Cortex (80%)**
  - Dimension: 0,3 cm × 2400 cm<sup>2</sup>
  - N:o nerve cells: 20 billion
  - N:o connections (synapses):  $\sim 2 \cdot 10^{14}$
- **Power: 25 W, ~PC-processor**
- **1 rack BG/L: 35 kW**
- **Fiber length: 10 million km**
  - > 20 × Earth – Moon distance
  - > 6000km/cm<sup>2</sup>
  - 90 nm chip: 10 km/cm<sup>2</sup>
- **N:o messages/s:  $2 \cdot 10^{13}$**
- **"Alien technology"**
  - Scientific challenge to understand!
  - ... and to model/simulate/emulate



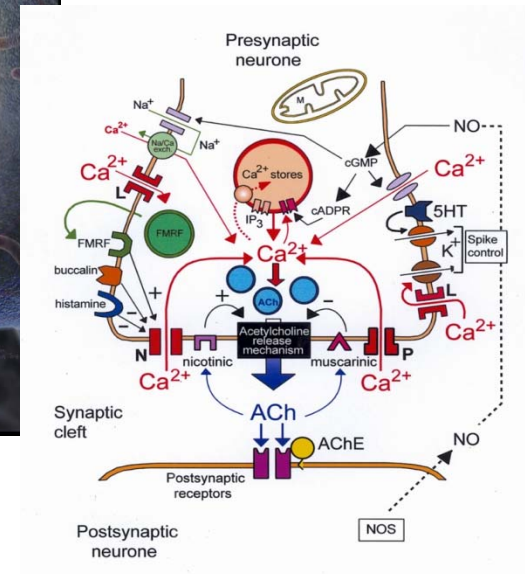
# Brain simulation

## A multi-scale problem

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Graham Johnson Medical  
Media, Boulder, Colorado





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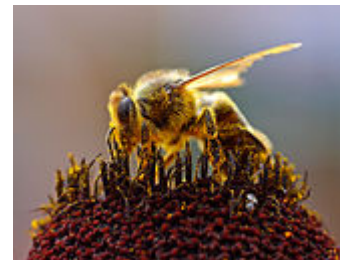
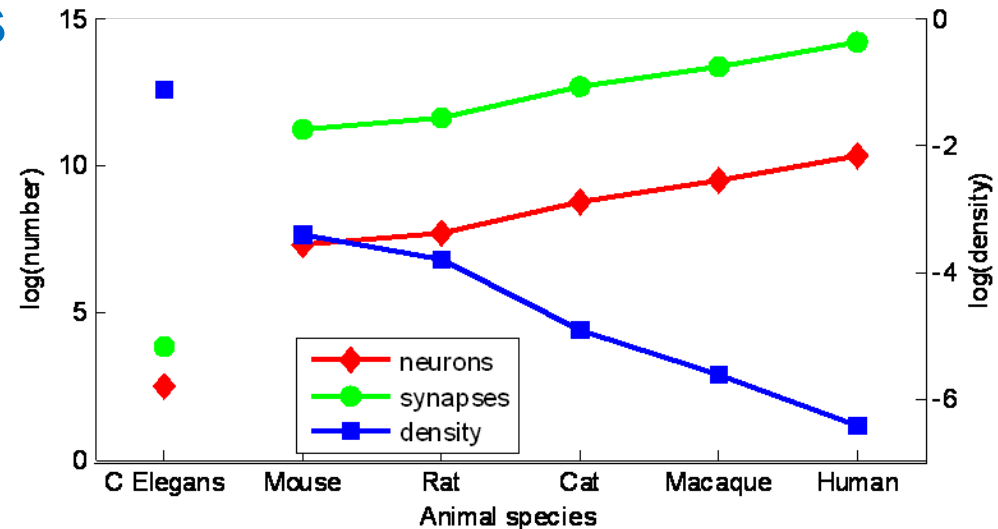


# Why simulate the brain?

- To undercover the mystery
- To understand function and dysfunction
- To be able to interface with the brain
- To design brain-inspired technology
  - "Cognitive computing"

# Why use HPC?

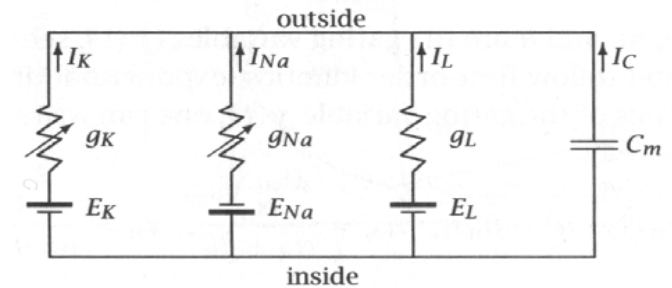
- Many neurons and synapses in reality
- Network is key
- Simulating small networks distorts results
- Distributed representation and processing for technical applications
- 1000 neurons on PC slow





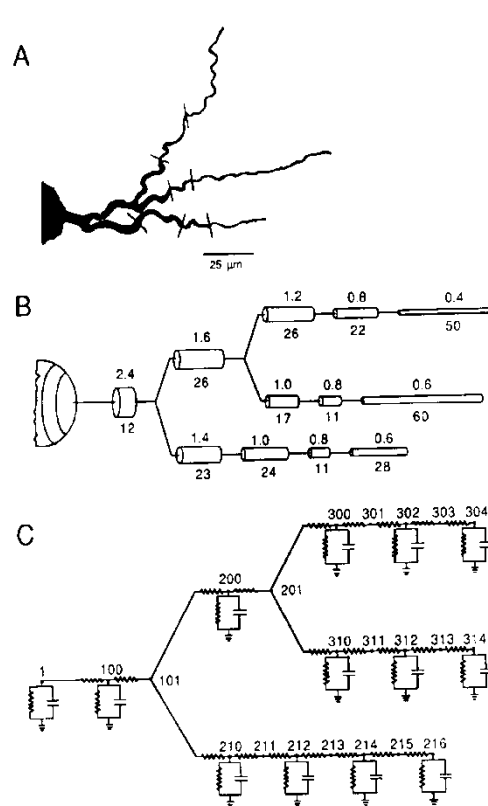
# Single cell modeling

- Connectionist/Mesosopic
- Integrate-and-fire
- Hodgkin-Huxley
  - Single/multiple compartment
- Equivalent electrical circuit

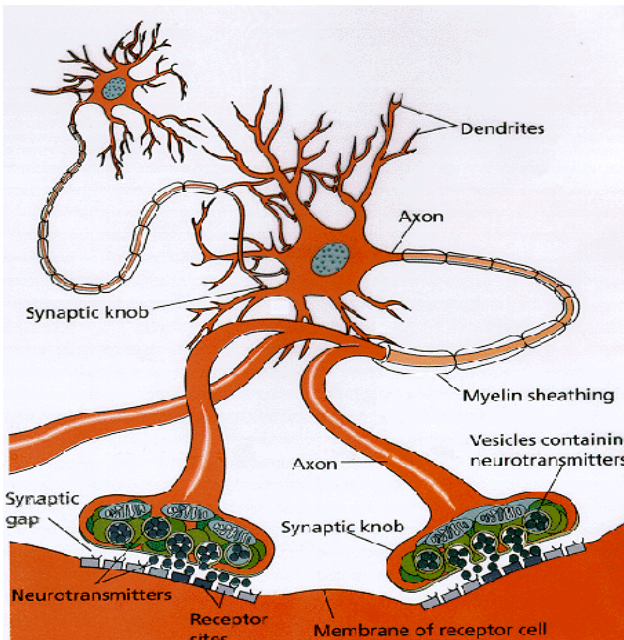


- Hodgkin-Huxley formalism
  - Na, K,  $K_{Ca}$ , Ca-channels
  - $Ca_{AP}$  and  $Ca_{NMDA}$  pools
  - ...

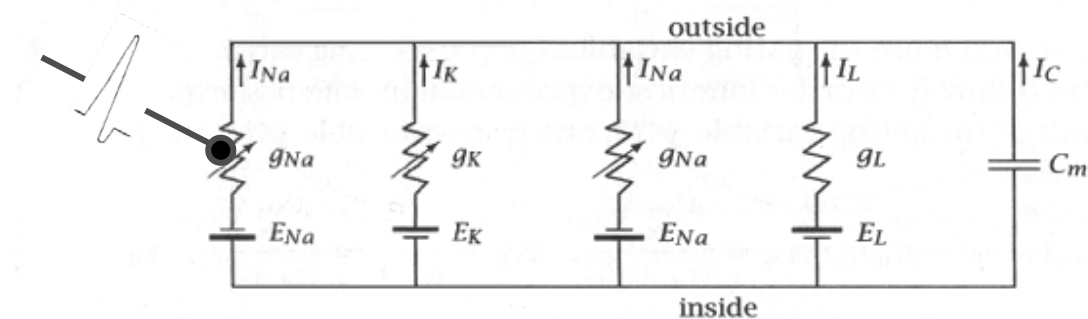
- Quantitative fit possible
- IBM-EPFL Blue Brain project



# Synaptic transmission and plasticity



- Conduction delay
- Synaptic conductance, kinetics, PSP-shape
- Reversal potential
  - Glutamate (AMPA&NMDA)
  - $GABA_A$



- Quantitative fit possible
- Synaptic plasticity
  - Fast: Facilitation, Depression
  - LTP/LTD: STDP
    - Biochemistry

## APPENDIX MODEL HODGKIN–HUXLEY NEURON EQUATIONS

This Hodgkin–Huxley implementation was based on Ekeberg et al. (1991). With the membrane potential  $V$  and the Nernst potential  $E_i$  for  $i \in \{\text{Na}, \text{K}, \text{Ca}, \text{K}_{\text{Ca}}\}$  and given Ohm's law:

$I_i = g_i(V - E_i)$  combined with Kirchhoff's laws, yields:

$$I_m = C_m \frac{dV}{dt} + g_{\text{Na}}(V, t)(V - E_{\text{Na}}) + g_{\text{K}}(V, t)(V - E_{\text{K}}) + g_{\text{Ca}}(V, t)(V - E_{\text{Ca}}) + g_{\text{K}_{\text{Ca}}}(V, t)(V - E_{\text{K}_{\text{Ca}}}) + g_{\text{Leak}}(V - E_{\text{Leak}})$$

Where  $t$  is time,  $g_{\text{Leak}}$  is the constant leak conductance and  $E_{\text{Leak}}$  is the leak equilibrium potential. Parameter values are given in **Table A1**. The dynamic conductance  $g_i(V, t)$  can be expressed with a gating model for individual ion channels. Hodgkin and Huxley (1952) discovered these dynamics for  $\text{Na}^+$  and  $\text{K}^+$  ion channels (but not  $\text{Ca}^{2+}$ ) after analyzing empirical data on action potentials in squid neurons. This resulted in the Hodgkin–Huxley equation:

$$I_m = C \frac{dV}{dt} + \bar{g}_{\text{Na}} m^3 h (V - E_{\text{Na}}) + \bar{g}_{\text{K}} n^4 (V - E_{\text{K}}) + g_{\text{Leak}} (V - E_{\text{Leak}})$$

Where  $\bar{g}$  is the maximal conductance when a channel is open. Gating variable  $m$  is  $\text{Na}^+$  channel activation,  $h$  is  $\text{K}^+$  channel activation and  $n$  is  $\text{Na}^+$  channel inactivation. The gating variables can be expressed as the following differential equations:

$$\begin{aligned} \frac{dm}{dt} &= \alpha_m(1-m) - \beta_m m & \text{with} & \quad \alpha_m = \frac{A(V-B)}{1-e^{(B-V)/C}} \quad \beta_m = \frac{A(B-V)}{1-e^{(V-B)/C}} \\ \frac{dh}{dt} &= \alpha_h(1-h) - \beta_h h & \text{with} & \quad \alpha_h = \frac{A(B-V)}{1-e^{(V-B)/C}} \quad \beta_h = \frac{A}{1+e^{(B-V)/C}} \\ \frac{dn}{dt} &= \alpha_n(1-n) - \beta_n n & \text{with} & \quad \alpha_n = \frac{A(V-B)}{1-e^{(B-V)/C}} \quad \beta_n = \frac{A(B-V)}{1-e^{(V-B)/C}} \end{aligned}$$

Where constants  $A$ ,  $B$  and  $C$  are independently defined for  $\alpha$  and  $\beta$  of each channel.  $\text{Ca}^{2+}$  is treated differently, because  $\text{Ca}^{2+}$  pools are assumed to be inside the cell near the cell membrane and can activate  $\text{K}_{\text{Ca}}$  channels to achieve hyperpolarization. Using  $q$  to represent  $\text{Ca}^{2+}$  activation, a relation similar to the  $\text{Na}^+$  channel activation ( $m$ ) holds:

$$\frac{dq}{dt} = \alpha_q(1-q) - \beta_q q \quad \text{with} \quad \alpha_q = \frac{A(V-B)}{1-e^{(B-V)/C}} \quad \beta_q = \frac{A(B-V)}{1-e^{(V-B)/C}}$$

change in concentration  $[\text{Ca}_{\text{AP}}]$  is equivalent to the rate of ions entering the pool less the ions leaving the pool:

$$\frac{d[\text{Ca}_{\text{AP}}]}{dt} = (E_{\text{Ca}} - V)Q_{\text{AP}} q^5 - \delta_{\text{AP}} [\text{Ca}_{\text{AP}}]$$

Where  $Q_{\text{AP}}$  is the rate of  $[\text{Ca}^{2+}]$  influx and  $\delta_{\text{AP}}$  is the rate of decay. The concentration  $[\text{Ca}_{\text{AP}}]$  occurs in the soma of neurons and will activate  $\text{K}_{\text{Ca}}$  channels inside the cell membrane with the following current:

$$I_{\text{K(Ca)AP}} = \bar{g}_{\text{K(Ca)AP}} (E_{\text{K}} - V) [\text{Ca}_{\text{AP}}]$$

After sustained firing activity, calcium buildup in the neuron will cause hyperpolarization and a reduction in the firing rate (adaptation).

## SYNAPTIC EQUATIONS

Like voltage-gated ion channels, the neurotransmitter-gated synaptic channels have ionic current produced by a voltage driving force, maximum conductance  $\bar{g}_{\text{syn}}$  and synaptic activation level  $s$  with 1 being the most active. Given this, the synaptic AMPA and  $\text{GABA}_{\text{A}}$  inward currents are:

$$I_{\text{syn}} = \bar{g}_{\text{syn}} (E_{\text{syn}} - V) s \quad 0 \leq s \leq 1$$

All synapses are saturating as defined by Lytton (1996) and depressing as defined by Varela et al. (1997). The combination of saturation and depression implemented in the same synapse (using NEURON) was not found in previous publications and appears to be new. Each pre-synaptic spike results in neurotransmitter release into post-synaptic receptors with a binding rate  $\alpha$ , unbinding rate  $\beta$ , and synaptic conductance  $r$ . During neurotransmitter release  $C_{\text{dur}}$ ,  $r = r_{\text{on}}$  and conductance increases to  $R_{\infty} = \alpha/(\alpha + \beta)$  with a time constant  $\tau_{\text{on}} = 1/(\alpha + \beta)$ . After  $C_{\text{dur}}$ ,  $r = r_{\text{off}}$  and conductance decays to zero with a time constant  $\tau_{\text{off}} = 1/\beta$ . With  $\Delta t$  being time since a spike, the dynamics are as follows:

$$\frac{dr_{\text{on}}}{dt} = (\alpha + \beta)(R_{\infty} - r_{\text{on}}) \quad \Delta t \leq C_{\text{dur}}$$

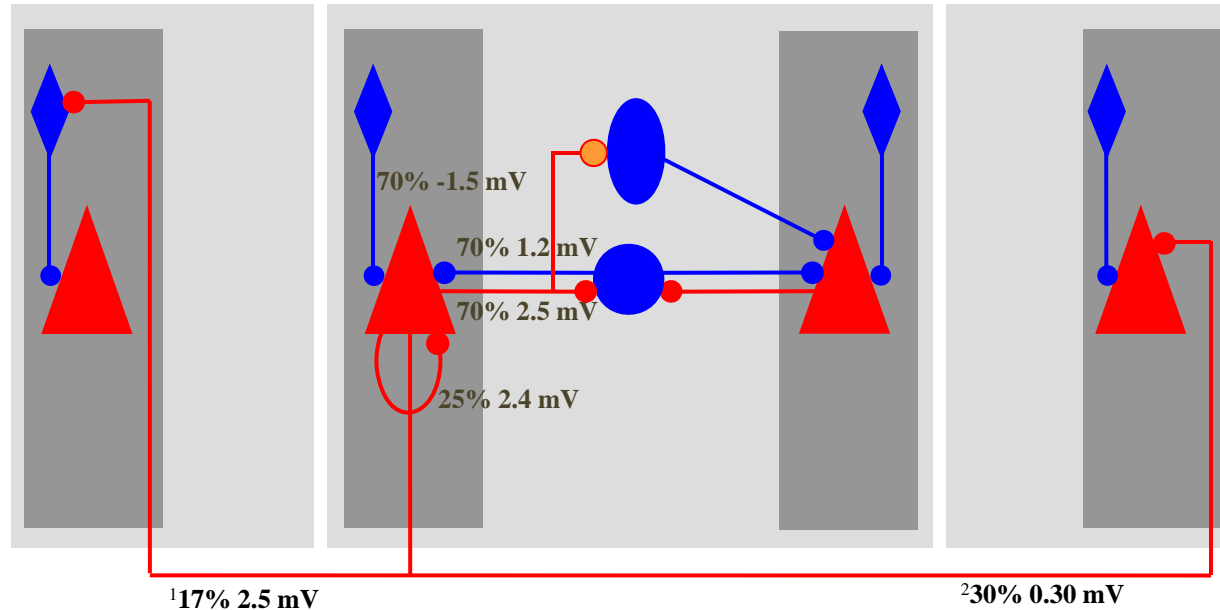
$$\frac{dr_{\text{off}}}{dt} = -\beta r_{\text{off}} \quad \Delta t > C_{\text{dur}}$$

$$s = \frac{r_{\text{on}} + r_{\text{off}}}{R_{\infty}}$$



# A layer 2/3 cortex model

## Microcircuit layout “Icecube - Potts” like

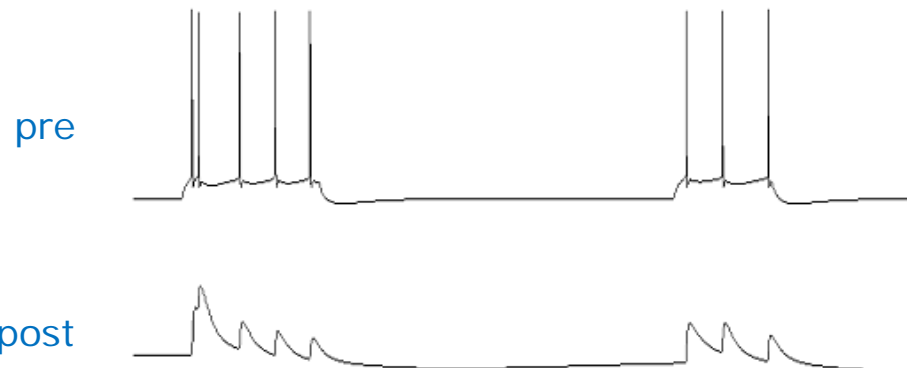
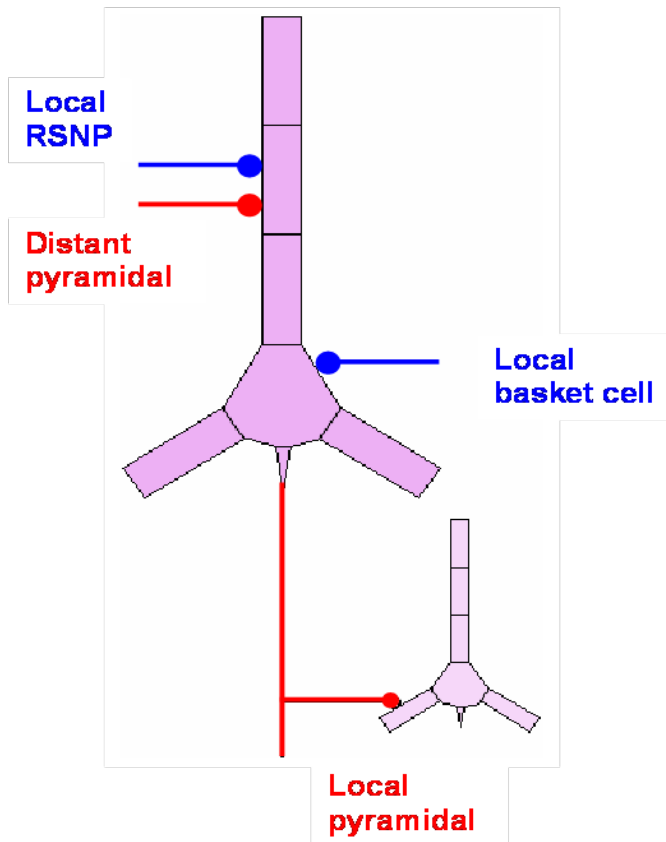


- **Minicolumns/local sub-networks with**
  - 30 pyramidal cells, connected 25%
  - 2 dendritic targeting, vertically projecting inhibitory interneurons
    - RSNP, e.g. Double bouquet
- **Hypercolumns (soft WTA modules) with**
  - Pool of Basket cells
  - Martinotti cells, with facilitating synapses from pyramidal cells
  - Large models: 100 minicolumns, 200 basket + Martinotti cells per hypercolumn
- **Currently rudimentary layers 4 and 5**

# The layer 2/3 cortex model

## Synaptic properties and connectivity

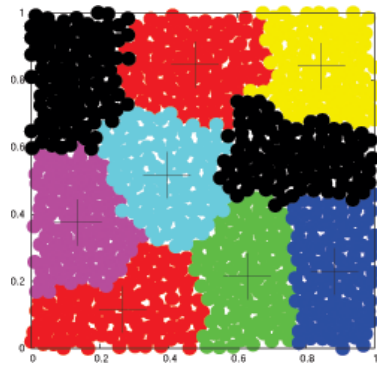
- **Synaptic transmission**
  - Glutamate (AMPA & voltage dependent NMDA)
  - Depressing synapses
  - GABA<sub>A</sub>
- **Synaptic targeting of soma and dendrites**
- **3D geometry  $\Rightarrow$  delays**
  - 0.1 - 1m/s conduction speed
- **Realistic amplitude of PSP:s in larger network models**



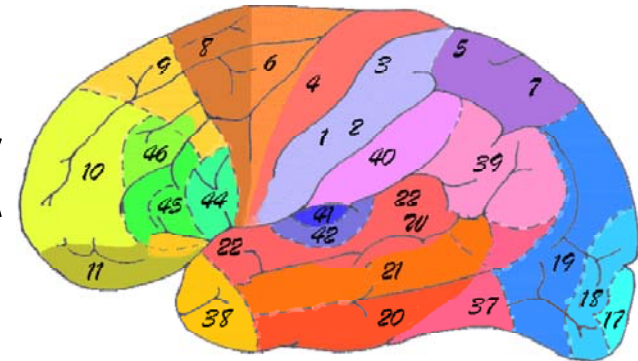
Pyramidal-pyramidal fast synaptic depression  
[Tsodyks, Uziel, Markram 2000]

# Conceptual model of Neocortex

Hypercolumns



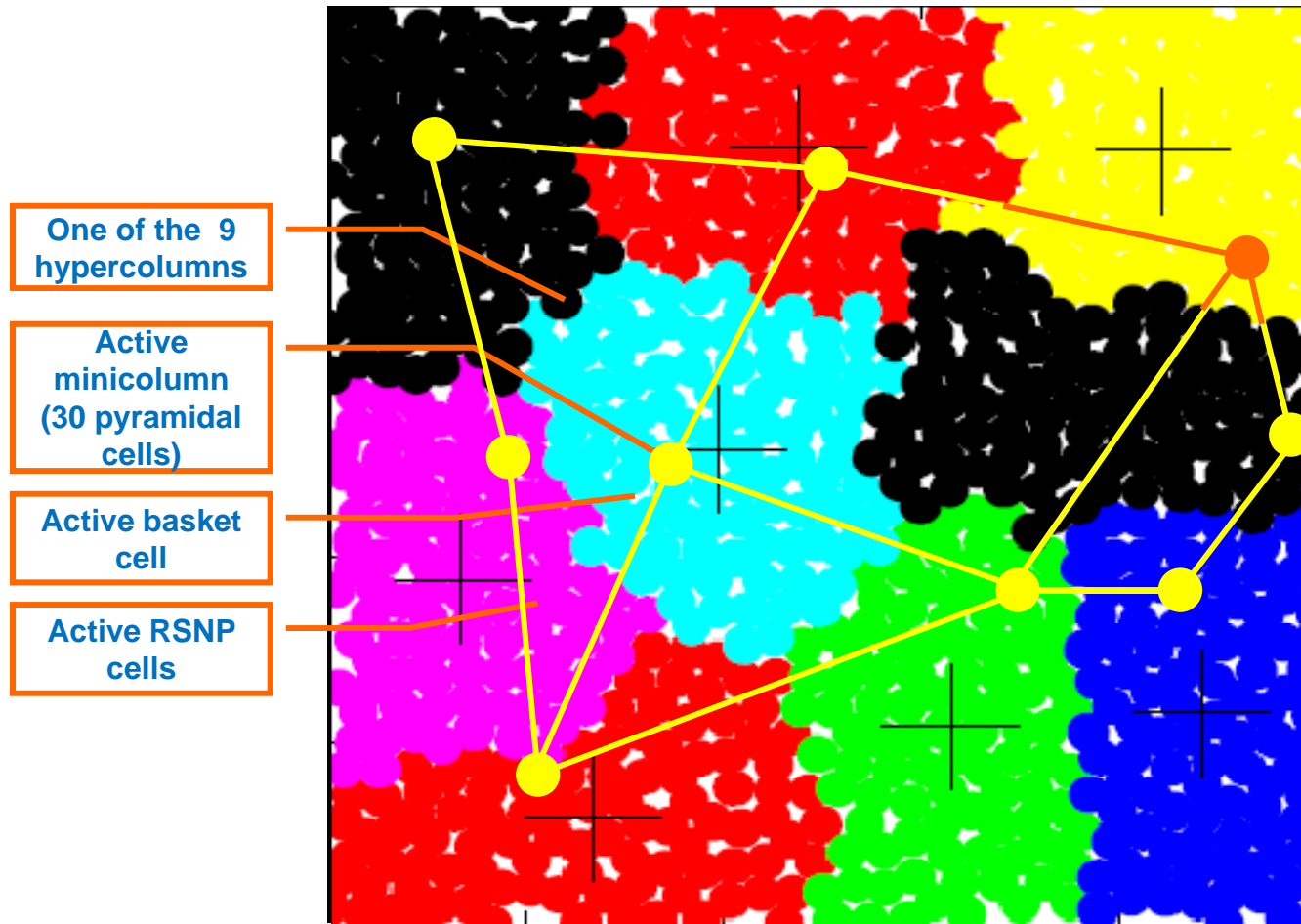
Cortical areas



- Hypercolumns are grouped into cortical areas of various sizes
  - Human V1 has ~40000 hypercolumns
- Human neocortex has about 110 cortical areas (Kaas, 1987)

# Simulation model network layout

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- 1x1 mm patch
- 9 hypercolumns
- Each hypercolumn
  - 100 minicolumns
  - 100 basket cells
- 29700 neurons
- 15 million synapses
- 100 patterns stored
- W trained offline
- (A-)symmetric



# 9 hypercolumns

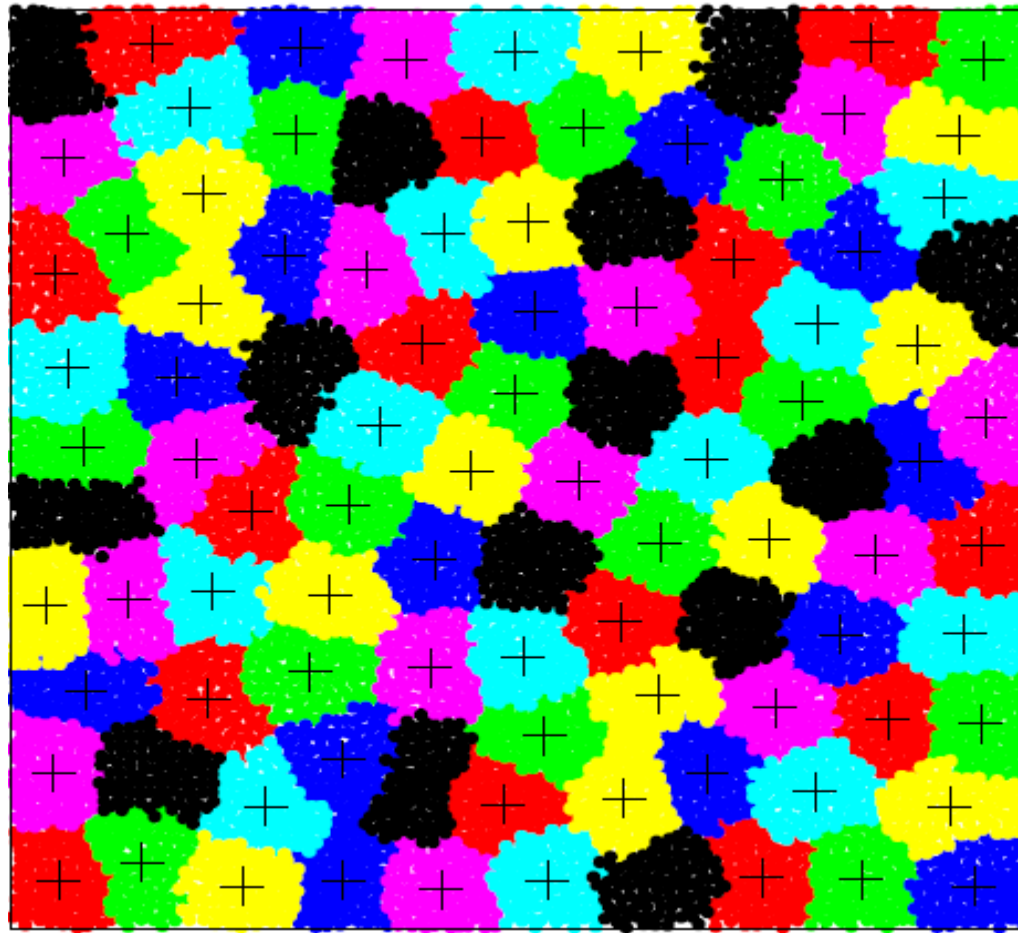
## Spontaneous activity



- 1x1 mm patch
- 9 hypercolumns
- Each hypercolumn
  - 100 minicolumns
  - 100 basket cells
- 29700 neurons
- 15 million synapses
- 100 patterns stored
- Non-symmetric W

# 100 hypercolumns

## Spontaneous activity

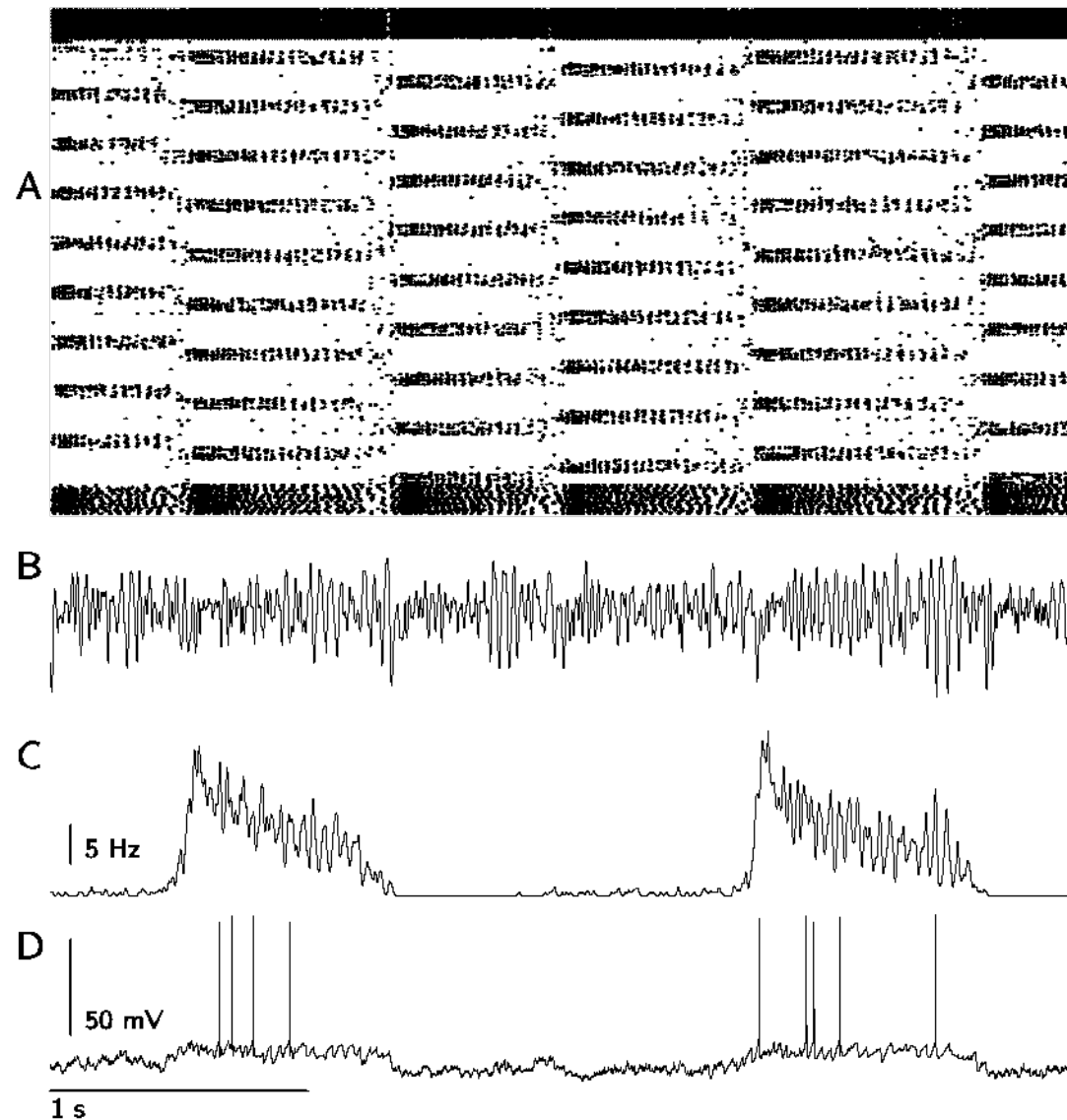


- 330000 neurons
- 161 million synapses

≈ 4x4 mm

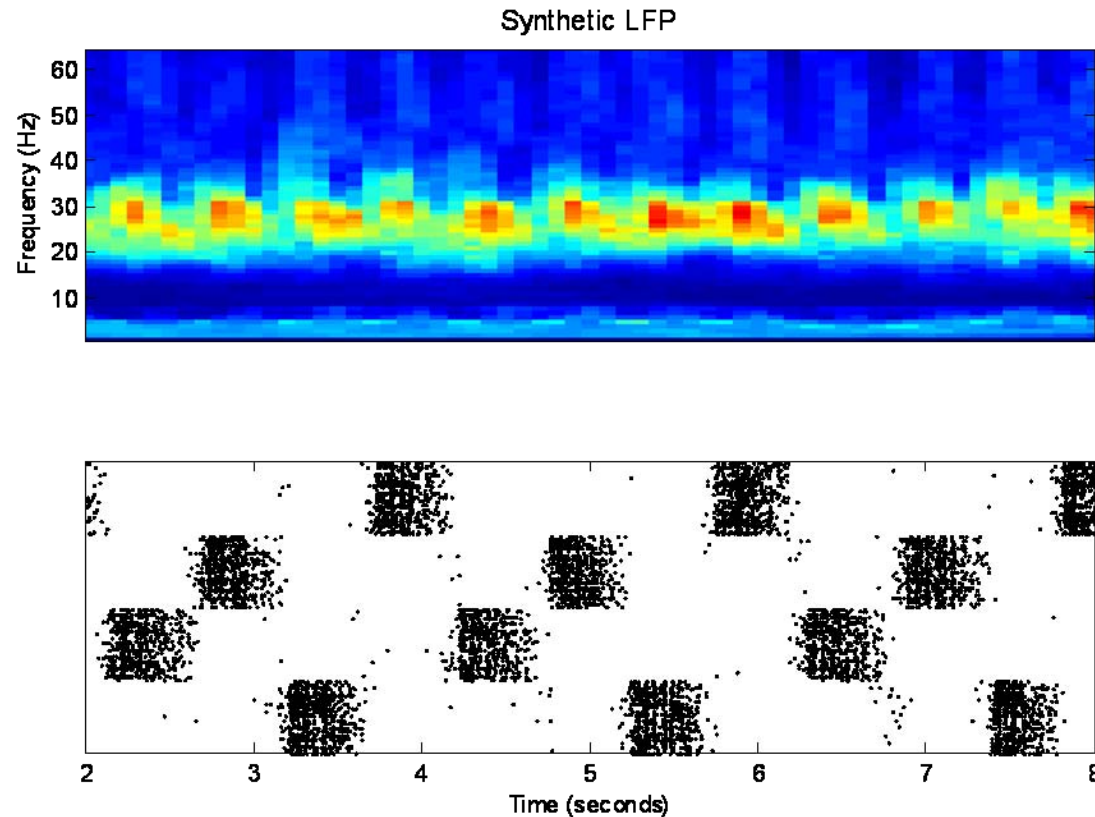
- 2000+ neurons
- 250000+ synapses

Spontaneous  
"resting activity"  
Tsodyks, Grinvald  
et al. 1999



Lundqvist M, Rehn M, Djurfeldt M and Lansner A (2006). Attractor dynamics in a modular network model of the neocortex. *Network: Computation in Neural Systems*: 17, 253-276

# Spontaneous attractor "hopping"



Can be  
compared to  
experimental  
data

- Memory replay at theta
  - Fuentemilla et al. Curr Biol 2010





# Computational demands

## Mouse brain $\approx 1/1000$ Human brain



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- Number of state variables in model neurons (6 compartments)  $\approx 30$
- Flops per neuron update:  $\approx 100$
- Number of state variable in model synapses:  $\approx 3$
- Flops per synapse update:  $\approx 20$
- Number of neurons: 30 M
- Number of neurons: 100 G
- Memory  $30 \cdot 4B \cdot 30M + 3 \cdot 4B \cdot 100G \approx 1TB$
- Simulation time step:  $50 \mu s$
- Flops/simulated second:  $(100 \cdot 30M + 20 \cdot 100G) / (50 \cdot 10^{-6}) \approx 4 \cdot 10^{16}$
- Simulation time per simulated second (1 Pflop) = 40 sec



# Parallelization of brain simulations



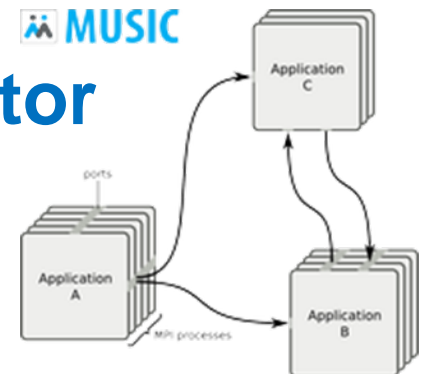
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- **Distributed processing, local memory (synapses mostly)**
- **Very sparse connectivity (human cortex  $10^{-6}$ )**
- **Spiking (event based) communication**
  - **Some graded interactions**
- **$\Rightarrow$  Readily parallelized**

# Available HPC simulators

- **SPLIT** (Hammarlund, Ekeberg 1998)
- **PGENESIS**, Parallel Genesis (Bower, ...)
- **PNEURON**, Parallel Neuron (Hines, ...)
- **NEST** (NEST Initiative)
- **MOOSE** (Bhalla, ...,  $\beta$ -version)
  - Integrated subcellular dynamics

- **MUSIC – MultiSimulation Coordinator**



- **GPU simulators**

# 8 rack BG/L simulation

October 2006

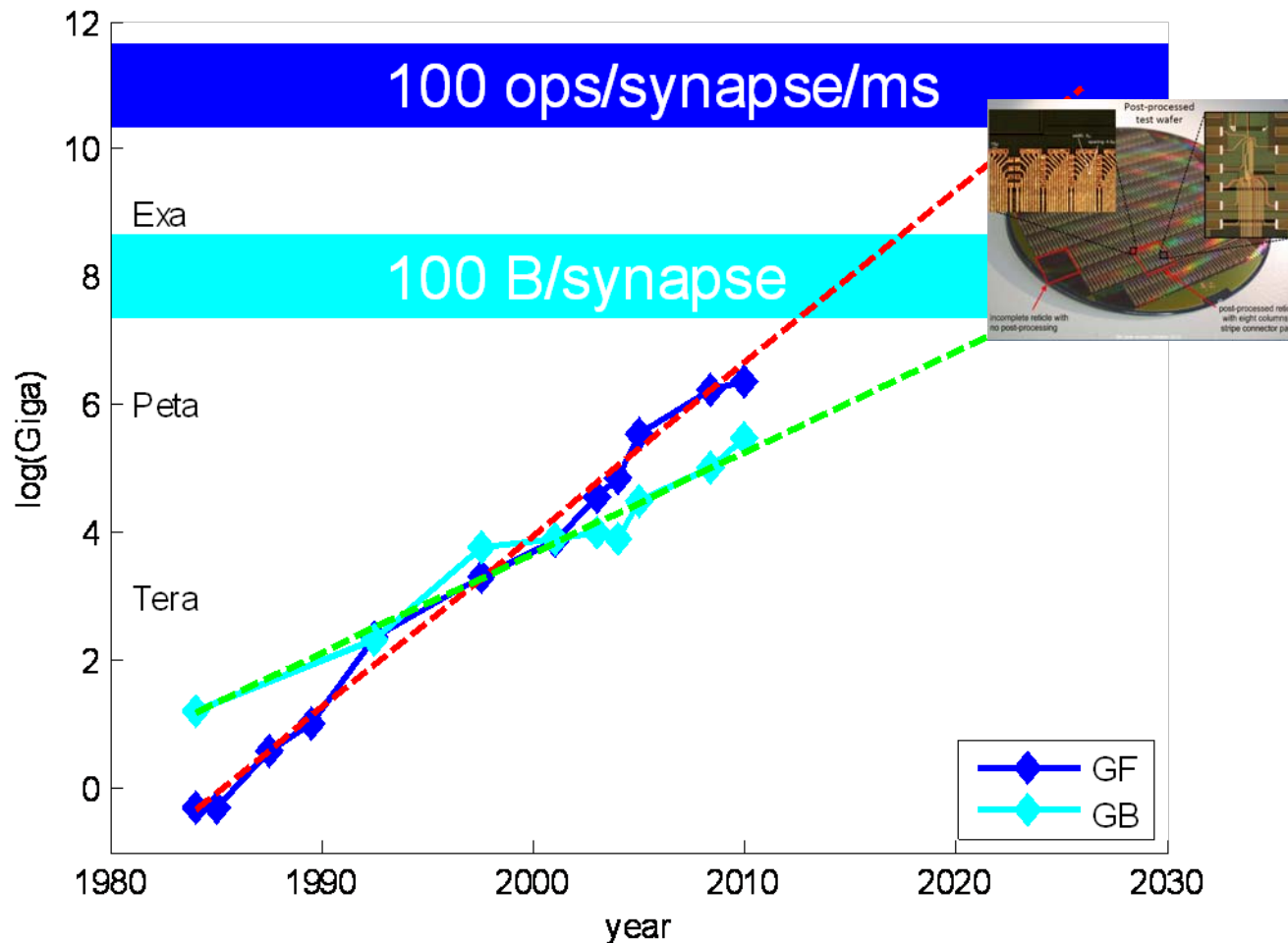
- **22x22 mm cortical patch**
  - 22 million cells, 11 billion synapses
- **SPLIT simulator by KTH**
- **8K nodes, co-processor mode**
  - used 360 MB memory/node
- **Setup time = 6927 s**
- **Simulation time = 1 s in 5942 s**
- **Massive amounts of output data**
  - Network operation similar as smaller versions of the model
- **77 % estimated speedup**
  - Point-point communication slows (?)
  - Linear speedup to 4K nodes



Djurfeldt M, Lundqvist M, Johansson C, Rehn M, Ekeberg Ö, and Lansner A (2008): Brain-scale simulation of the neocortex on the Blue Gene/L supercomputer. IBM J R&D 52:31-41



# When can we simulate the human brain in real time?





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# Simulation output pre-post processing



- **Preprocessing**
  - Setting up simulation model
    - Predefined networks of neurons and synapses
    - W files may be large!
  - Building/Growing network
    - E.g. By self-organization
    - From Large datasets
- **Postprocessing**
  - TB output files ...
  - Sub-sampling of output, online postprocessing
  - Synthesis of measurements
    - VSD, LFP, EEG, MEG, BOLD
    - Spike analysis
  - 3D visualization



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# HPC results overview

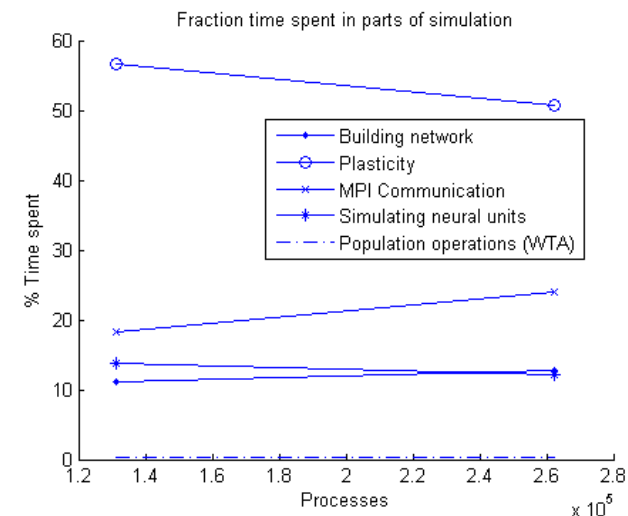
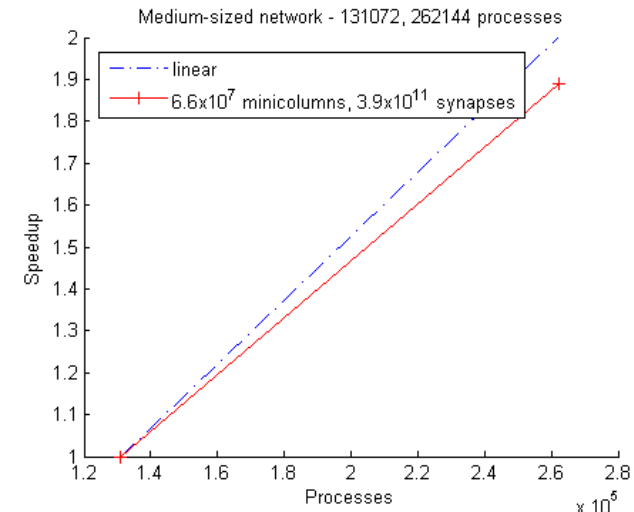
- **Full scale lamprey swimming simulations**
- **First (?) parallelizing Hodgkin-Huxley brain simulator**
- **Largest ever Hodgkin-Huxley cortex network models**
  - with David Silverstein
  - Brain simulation, Cortex modelling
  - Currently scaling up (JUGENE) using NEURON
- **Most parallel ever spiking and non-spiking neural network simulations**
  - with Simon Benjaminsson
  - February 2011 on JUGENE
    - Largest multi-core installation (294912 cores)
- **Brain imaging data analysis**

# Recent scaling experiments: ANSCore program

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TRITA-CSC-CB 2011:01

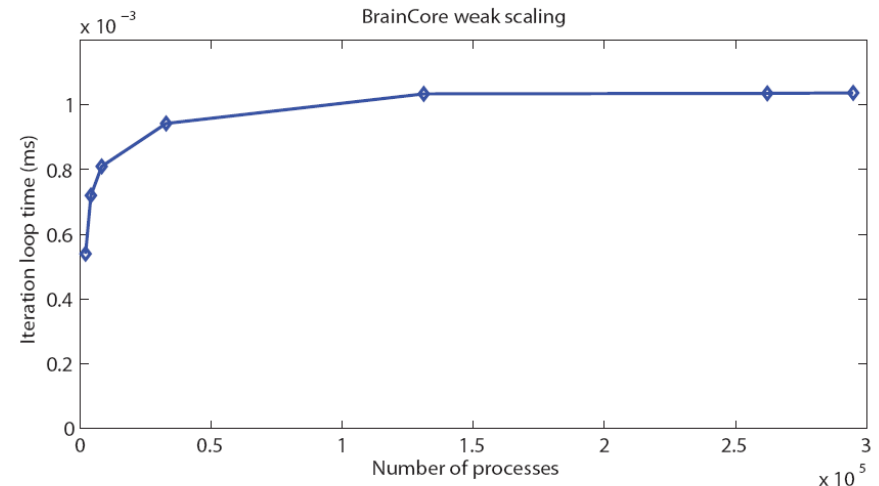
- **ANSCore on full machine**
  - Non-spiking ANS code (Simon Benjaminsson)
  - Collective communication
  - ANSCore good strong scaling
    - $N = 66\text{M}$  (non-spiking units, “minicolumns”)
    - $C = 390\text{G}$
    - Inner loop time = 2200 ms (w/o plasticity)
- **Recent tests on Cray XE6 (ANSCore)**
  - 6000 cores, 4-5 times faster than JUGENE, 3 times ← faster clock ...?



# Recent scaling experiments. BrainCore program

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- **BRAINCore on full JUGENE**
  - >29M spiking units, event based communication
    - MPI point-point communication
    - Largest network 0.034 % processor-processor communication
      - ... as in the real brain
  - >295G trainable connections
  - Perfect weak scaling
    - Inner loop time < 1 ms (real time learning and recall)
    - Size  $\approx$  mouse brain
    - Complexity  $\ll$  mouse brain
  - Remember:
    - 25x25x2 m machine
    - 1 MW







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# What difficulties we encountered?



- **MPI programming**
  - Mapping problem to parallel architecture
  - Debugging, profiling
- **New methodology/Technology for optimal use of resources**
  - Scripting, temporary saves, ...
  - Model fitting possibilities
- **Queing Policy – different user groups needs**
  - We use MANY cores but currently run short jobs ...
- **Hard to build large networks**
  - Public simulators not programmable enough
  - Need input from file (W) – large!
- **Potentially huge simulations output**
  - Subsampling, postprocessing necessary



# Conclusions and Outlook

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- **Next generation simulators for brain simulation**
  - Rapidly growing HPC activities
  - Multi-scale
  - Complex multi-network brain-like architecture
- **What would have been ‘good to get’ from HPC in future?**
  - Exascale computers will allow full scale human brain simulation with considerable detail
    - Need one on desktop ...
  - Expert support on
    - MPI programming
    - Data postprocessing
    - 3D visualization



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# Thanks for listening!