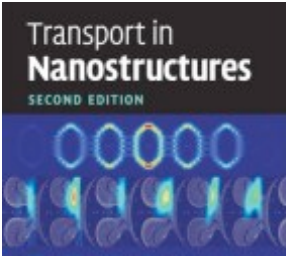


# GENERAL ASPECTS OF MESOSCOPIC TRANSPORT: I

**Jonathan Bird**  
**Electrical Engineering,**  
**University at Buffalo,**  
**Buffalo NY, USA**

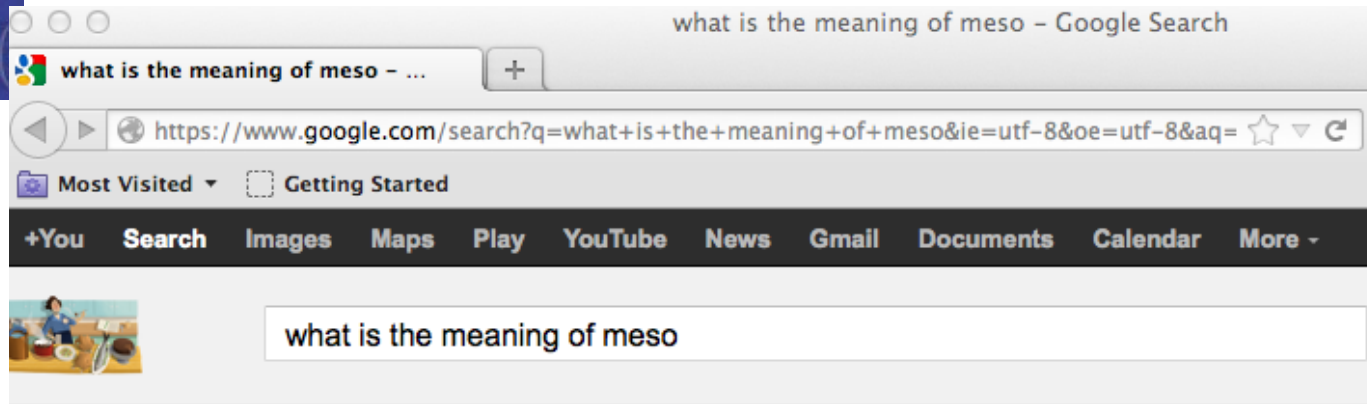
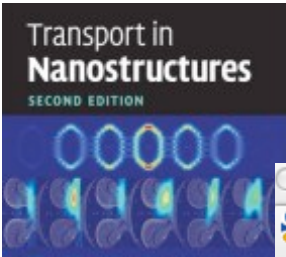




# GENERAL ASPECTS OF MESOSCOPIC TRANSPORT I

- **An Introduction to Mesoscopics**
- **Some Features of Mesoscopic Systems**
- **Some Common Mesoscopic Phenomena**
- **Realizing Mesoscopic Systems**
- **1-D Mesoscopic Systems**





## Search

About 2,460,000 results (0.26 seconds)

### Web

#### Definition for **meso**:

### Images

Web definitions: A Greek prefix meaning middle or mid; used with Latin, latinized, or Greek words to indicate the middle (often second) part of a structure..

### Maps

[hedgerowmobile.com/Glossaryparasitica.html](http://hedgerowmobile.com/Glossaryparasitica.html)

### Videos

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### News

[meso- - definition of meso- by the Free Online Dictionary, Thesauru...](#)

### Shopping

[www.thefreedictionary.com/meso-](http://www.thefreedictionary.com/meso-)

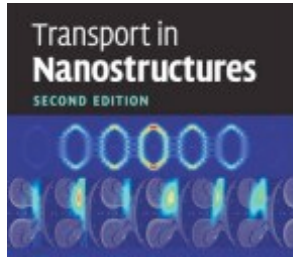
### More

1. In the middle; middle: mesoderm. 2. Intermediate: mesophyte. [Greek, from mesos, middle; see medhyo- in Indo-European roots.] **meso-** before a vowel, mes- ...

[Meso - Meso-appendix - Meso-ionic compound](#)

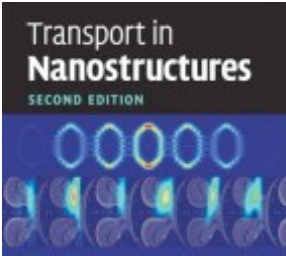
# What does "MESOSCOPIC" mean?





**MESOSCOPIC PHYSICS** – concerns the physical description of systems that are **INTERMEDIATE** between the macroscopic and microscopic realms

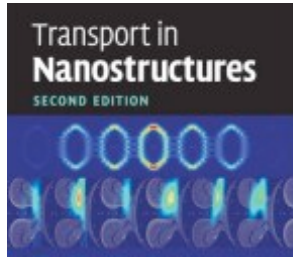




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# What are the **GENERAL FEATURES** of Mesoscopic Systems?

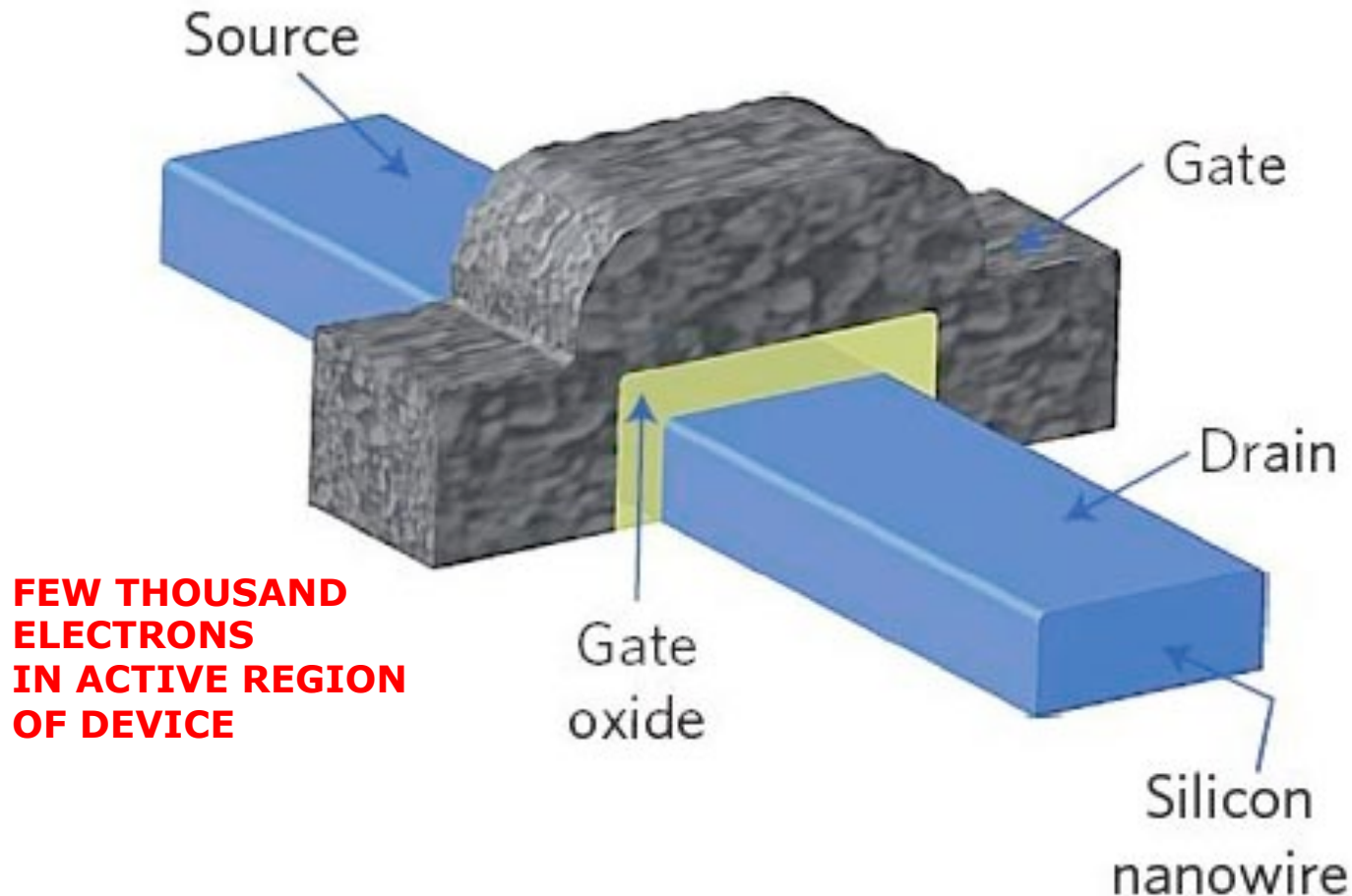
Typically (not always) contain **LARGE** numbers of particles – reminiscent of classical systems ...

... But, the **QUANTUM** character of these particles is strongly apparent

- Exhibit pronounced effects due to **QUANTUM INTERFERENCE & ENERGY QUANTIZATION**
- **MANY-BODY** effects ...



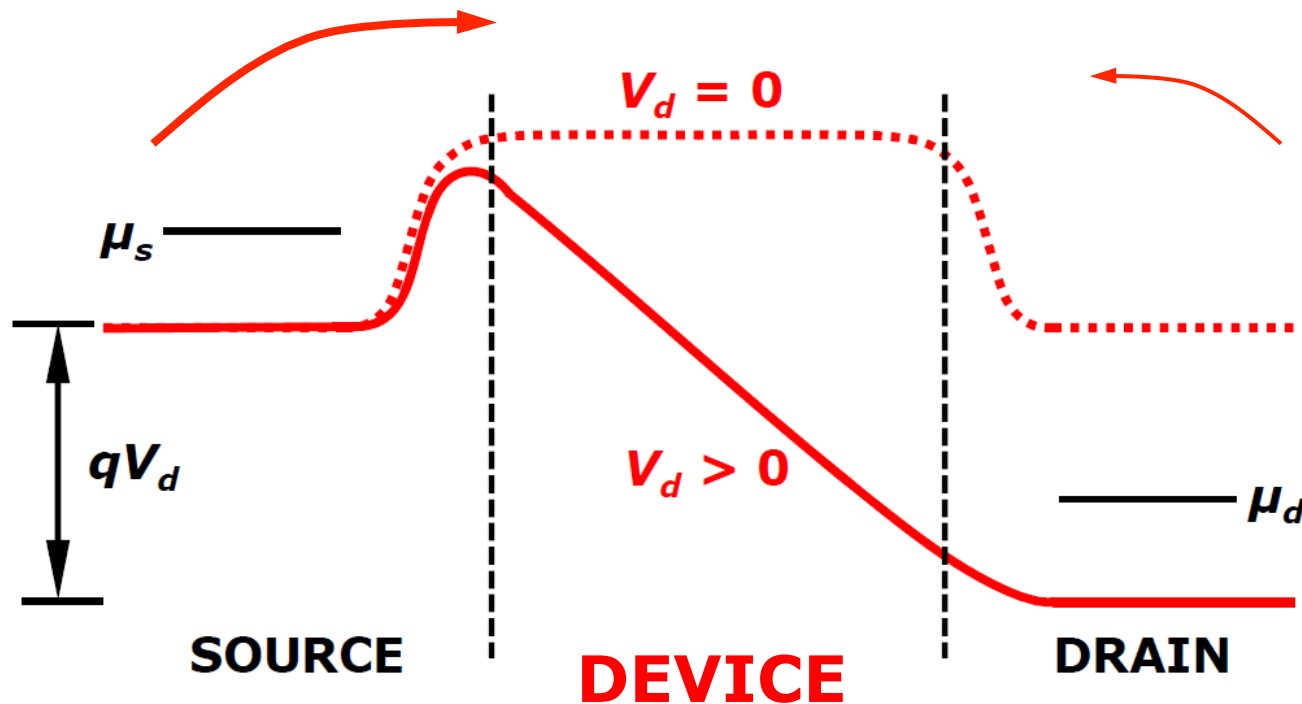
# Semiconductor devices: **ARCHETYPAL** mesoscopic system



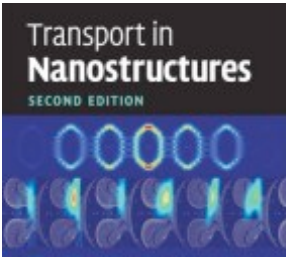
**FEW THOUSAND  
ELECTRONS  
IN ACTIVE REGION  
OF DEVICE**



# Device current calculated in a **TRANSMISSION** approach – the **LANDAUER** formula



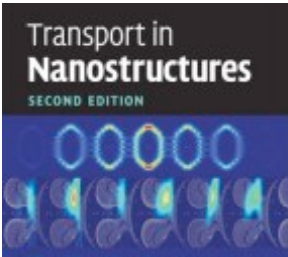




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# QUANTUM INTERFERENCE Due to **COHERENT** wave transport

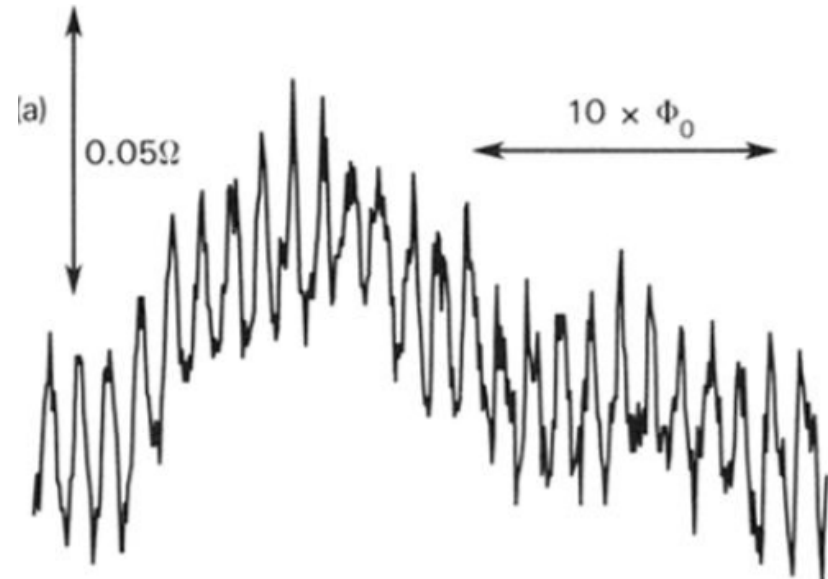
VOLUME 54, NUMBER 25

PHYSICAL REVIEW LETTERS

24 JUNE 1985

## Observation of $h/e$ Aharonov-Bohm Oscillations in Normal-Metal Rings

R. A. Webb, S. Washburn, C. P. Umbach, and R. B. Laibowitz  
*IBM Thomas J. Watson Research Center, Yorktown Heights, New York 10598*



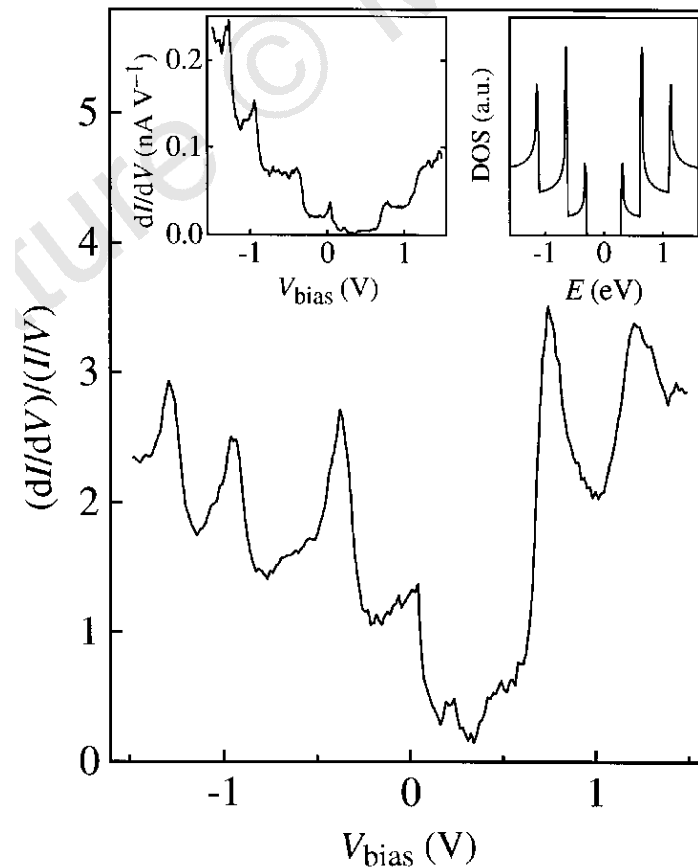
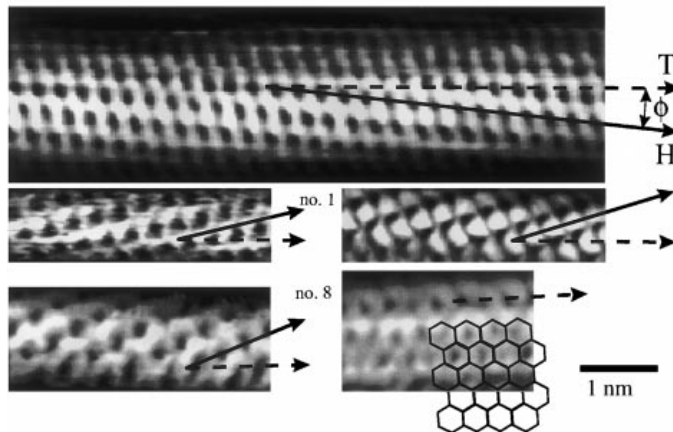
# ENERGY QUANTIZATION due to spatial confinement of carriers

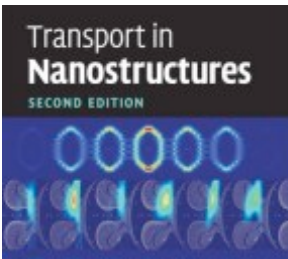
## Electronic structure of atomically resolved carbon nanotubes

Jeroen W. G. Wildöer\*, Liesbeth C. Venema\*,  
Andrew G. Rinzler†, Richard E. Smalley† & Cees Dekker\*

\* Department of Applied Physics and DIMES, Delft University of Technology,  
Lorentzweg 1, 2628 CJ Delft, The Netherlands

† Center for Nanoscale Science and Technology, Rice Quantum Institute,  
Departments of Chemistry and Physics, MS-100, Rice University, PO Box 1892,  
Houston, Texas 77251, USA





# SINGLE-ELECTRON control of currents in nanostructures

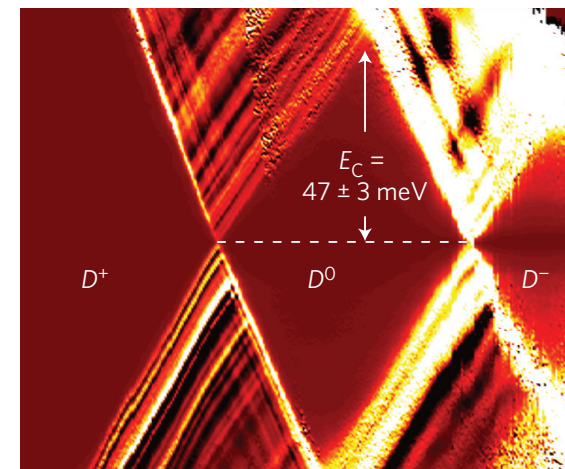
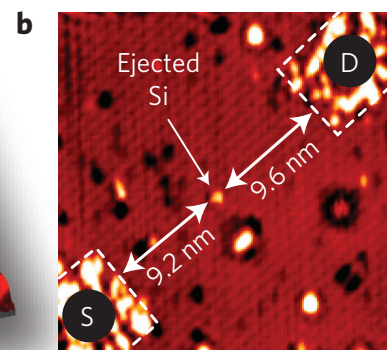
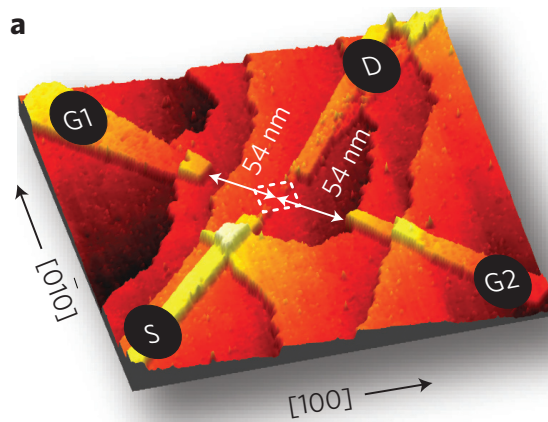
LETTERS

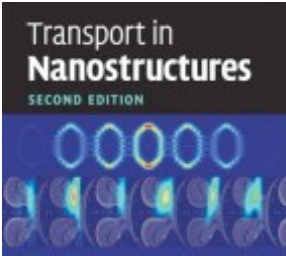
PUBLISHED ONLINE: 19 FEBRUARY 2012 | DOI: 10.1038/NNANO.2012.21

nature  
nanotechnology

## A single-atom transistor

Martin Fuechsle<sup>1</sup>, Jill A. Miwa<sup>1</sup>, Suddhasatta Mahapatra<sup>1</sup>, Hoon Ryu<sup>2</sup>, Sunhee Lee<sup>3</sup>,  
Oliver Warschkow<sup>4</sup>, Lloyd C. L. Hollenberg<sup>5</sup>, Gerhard Klimeck<sup>3</sup> and Michelle Y. Simmons<sup>1\*</sup>

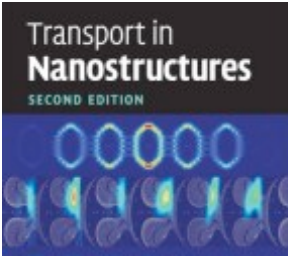




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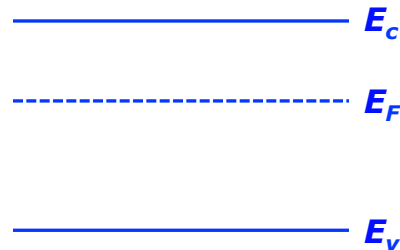
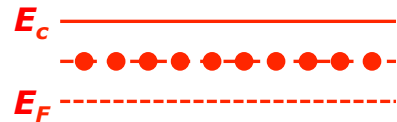
# Mesoscopic Devices Can Be Realized via **TWO** Distinct Approaches

**TOP-DOWN** methods utilize standard approaches of semiconductor micro-fabrication to perform **NANOSCALE** patterning of semiconductors or metals

**BOTTOM-UP** approaches exploit **NATURAL** nanostructures that form via **SELF-ASSEMBLY**



# TOP-DOWN Approaches: Two-Dimensional Electron Gas (2DEG)



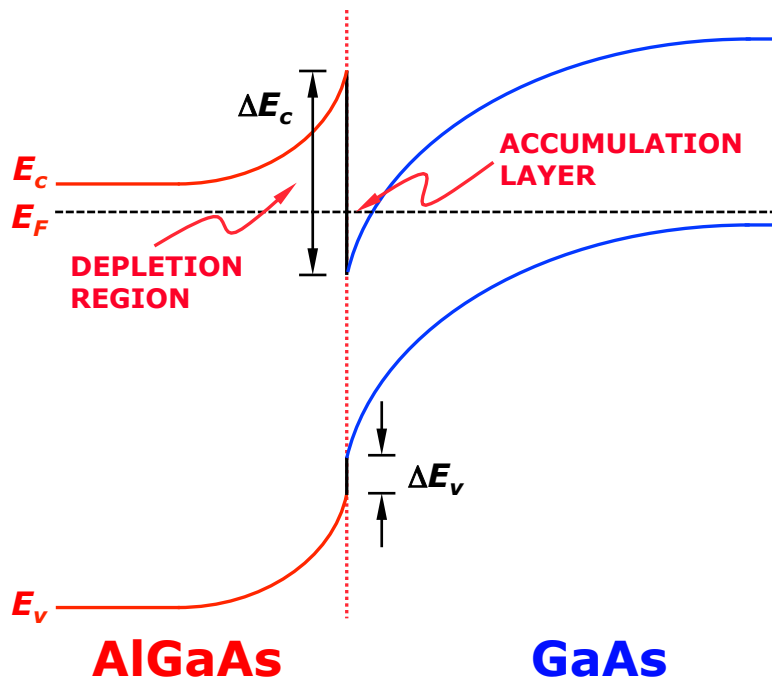
AlGaAs

GaAs

- MOST COMMONLY BASED ON **GaAs/AlGaAs HETEROJUNCTION**
- FORMED BY GROWING **AlGaAs** ON TOP OF **GaAs**
- AlGaAs HAS A **LARGER** BANDGAP THAN THAT OF GaAs AND IS **DOPED** *n*-TYPE WITH AN EXCESS OF ELECTRONS
- **PRIOR** TO HETEROJUNCTION FORMATION FERMİ LEVEL IN THE TWO MATERIALS IS **DIFFERENT**



# TOP-DOWN Approaches: Two-Dimensional Electron Gas (2DEG)

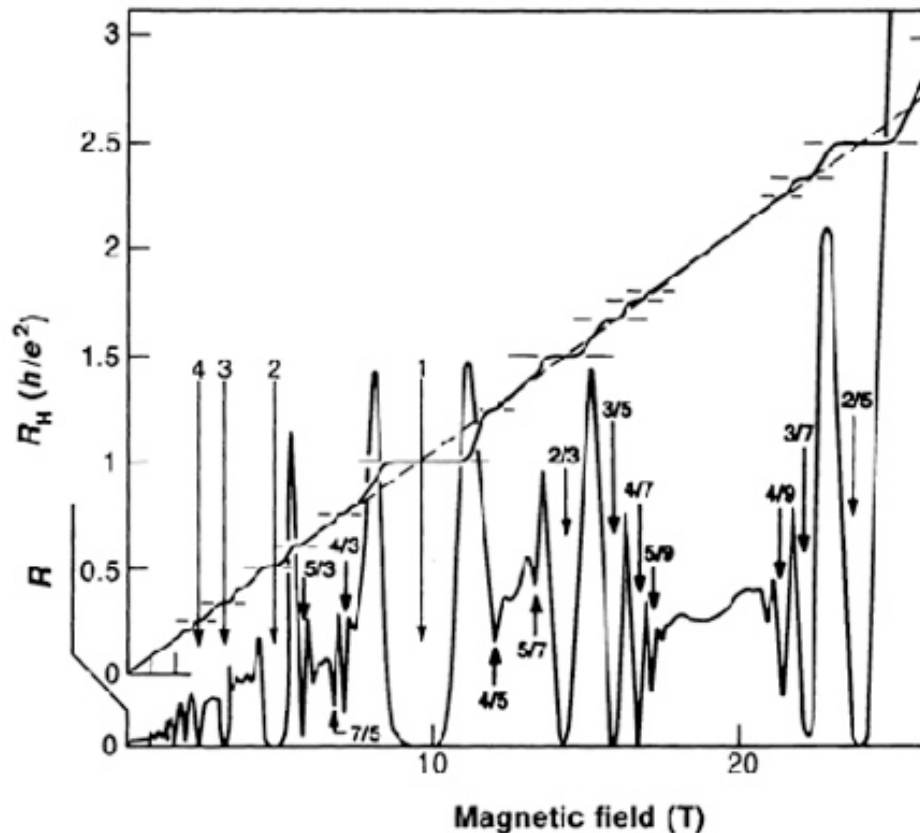


- AT **THERMAL EQUILIBRIUM** THE FERMIL LEVEL IS ALIGNED AT A **CONSTANT** POSITION ACROSS THE TWO MATERIALS
- THIS IS ACHIEVED BY THE **TRANSFER** OF ELECTRONS FROM THE AlGaAs TO THE GaAs
- THE RESULTING **BAND BENDING** – IN COMBINATION WITH THE BAND OFFSETS – RESULTS IN THE FORMATION OF A NARROW POTENTIAL WELL
- CARRIER MOTION IN THE WELL IS CONFINED NEAR THE INTERFACE FORMING A 2DEG



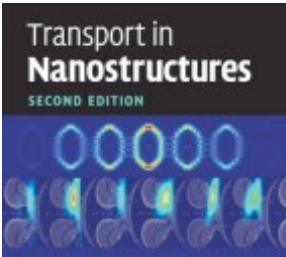


# TOP-DOWN Approaches: Two-Dimensional Electron Gas (2DEG)

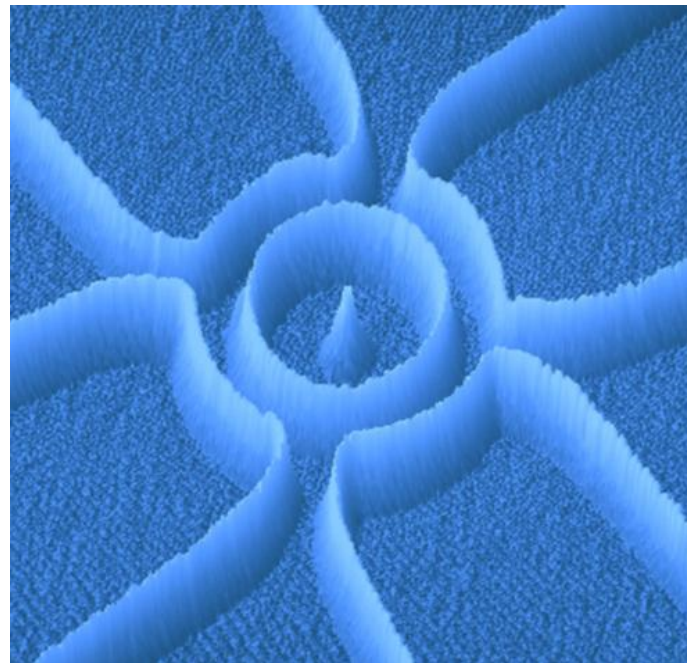


- THE 2DEG FORMED IN A HETEROJUNCTION CAN EXHIBIT **SUPERIOR** ELECTRICAL CHARACTERISTICS
- REMOVAL OF DOPANTS FROM CONDUCTING LAYER RESULTS IN **EXCELLENT** LOW-TEMPERATURE MOBILITY
- MEAN FREE PATH FOR TRANSPORT CAN EXCEED A **HUNDRED MICRONS** AT LOW TEMPERATURES!
- ALLOWS THE EXPLORATION OF A VARIETY OF **NOVEL** MESOSCOPIC TRANSPORT PHENOMENA





# **TOP-DOWN** Approaches: Two-Dimensional Electron Gas (**2DEG**)

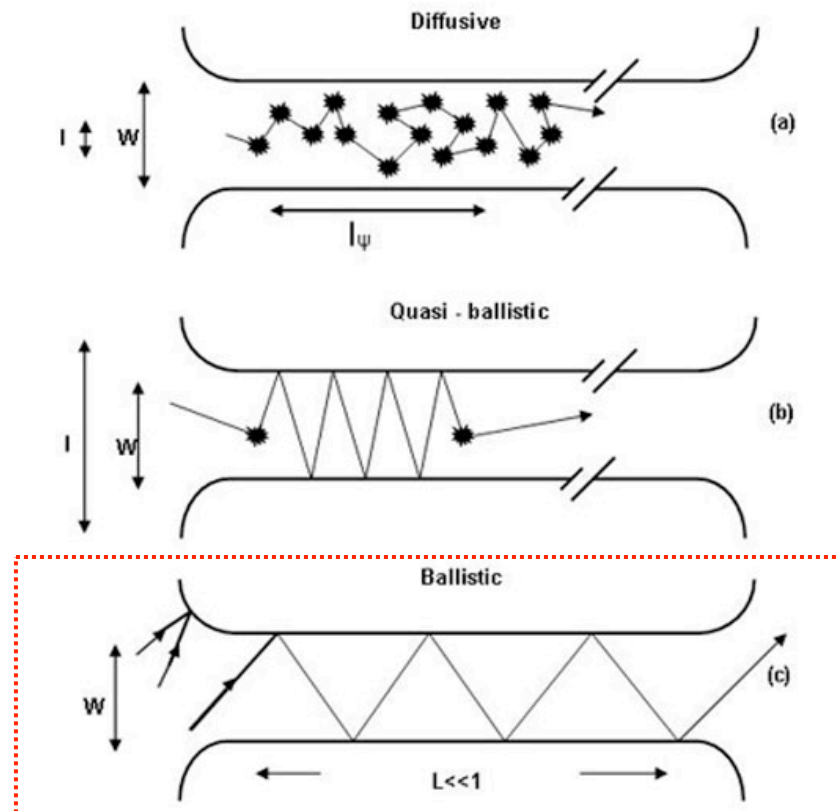


Ensslin Group  
ETH Zurich

## Easily **PATTERNED** to Form Mesoscopic Devices

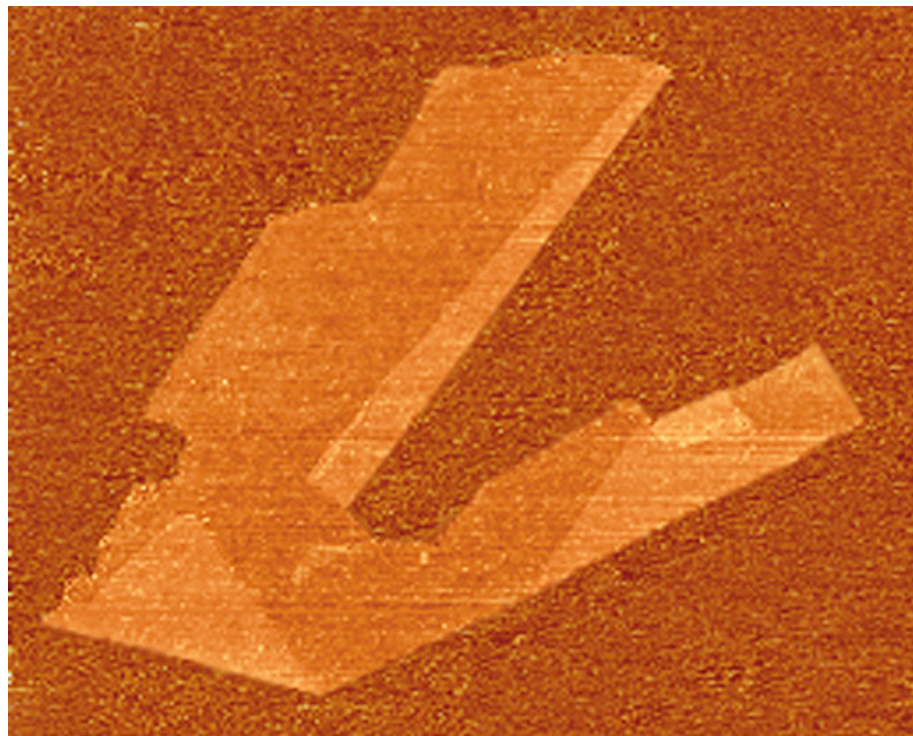
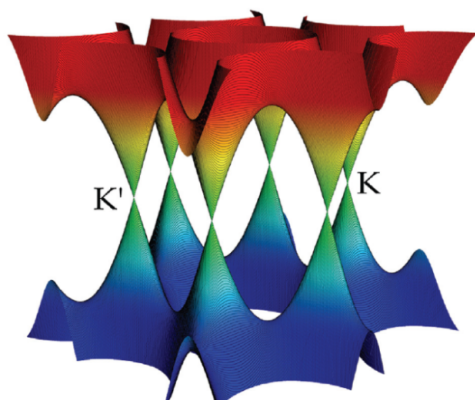
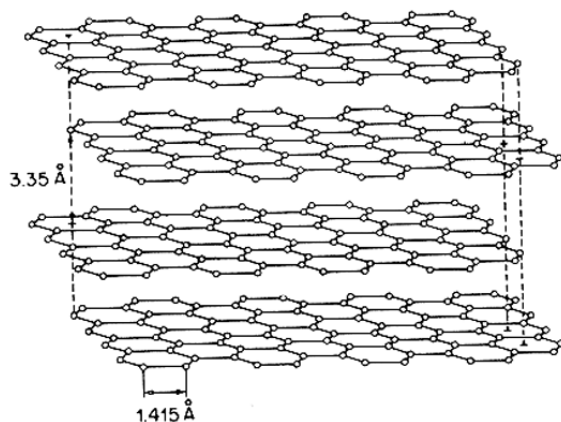


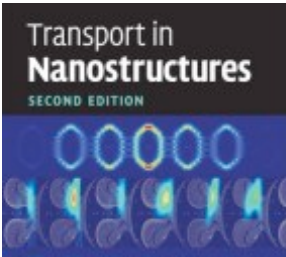
# LONG Mean-Free Path Allows **BALLISTIC** Transport





# BOTTOM-DOWN 2DEG: GRAPHENE

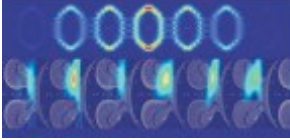




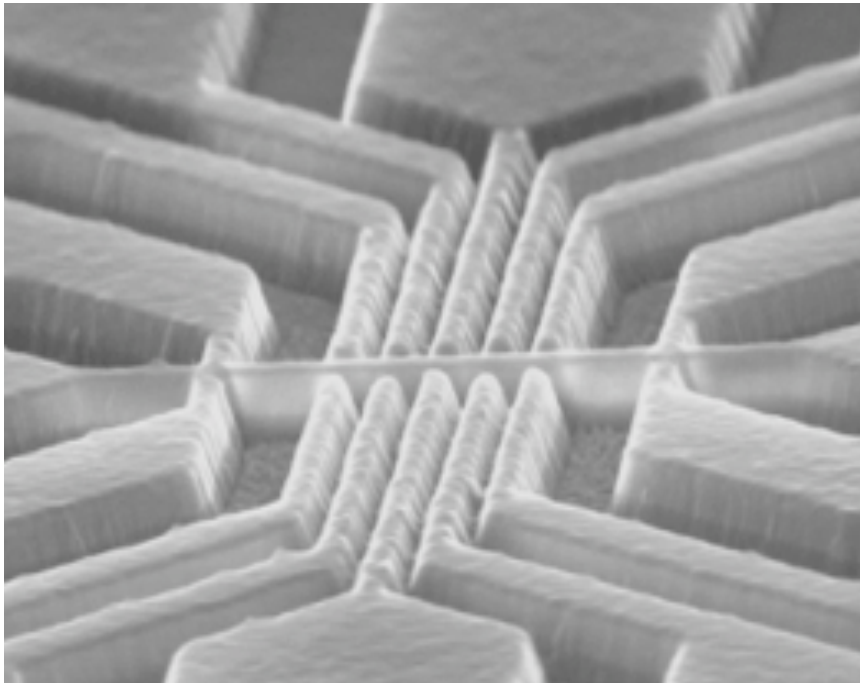
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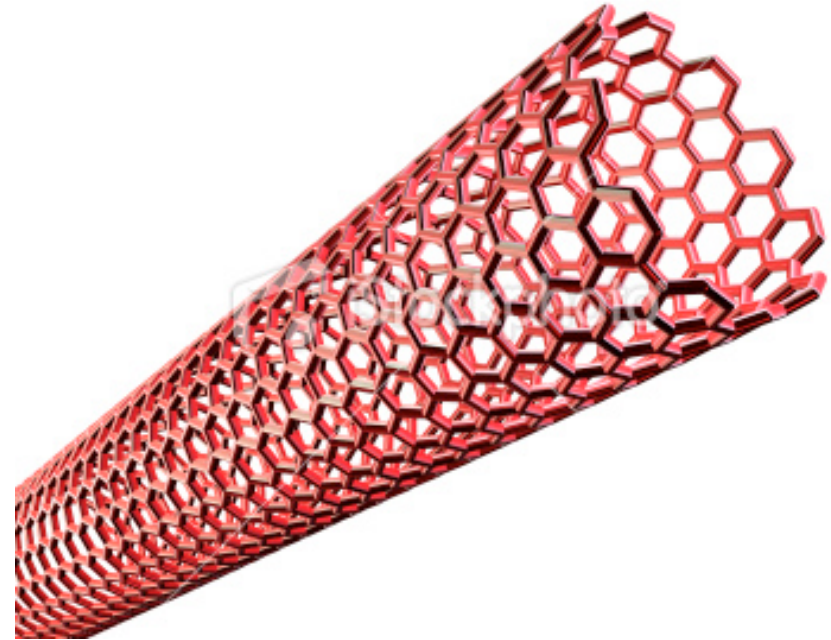




# 1-D Wires Can Be Realized By Top-Down **OR** Bottom-Up Methods



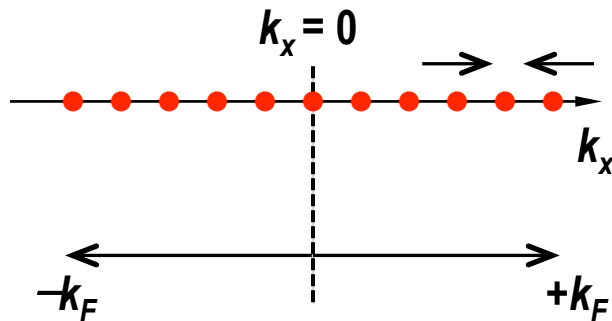
Etched Nanowire



Carbon Nanotube



# Exhibit **UNIQUE** Density of States That Governs Electrical & Optical Properties



$$k_x = \frac{2\pi}{L} n_x, \quad n_x = 0, \pm 1, \pm 2, \dots$$

$$dk_x = \frac{2\pi}{L}$$

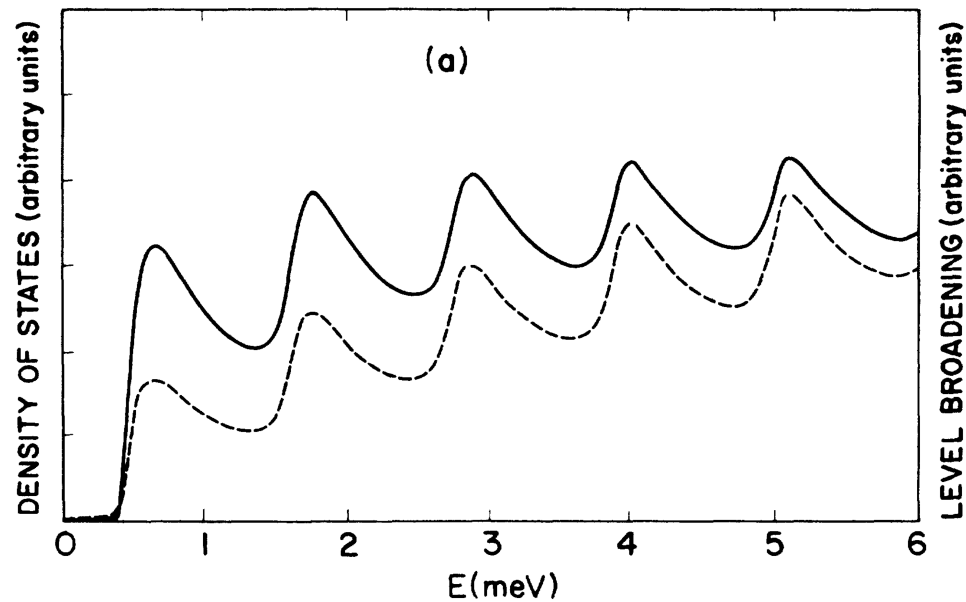
$$g_{1D}(E) = \left[ \frac{2m^*}{\pi^2 \hbar^2} \right]^{1/2} \frac{1}{\sqrt{E}}$$

**DoS OF PURELY 1-DIMENSIONAL –  
NON-INTERACTING - ELECTRONS**



# In Real Systems DoS Follows from a **SUM** Over Multiple **1-D SUBBANDS**

$$g_{1D}(E) = \left[ \frac{2m^*}{\pi^2 \hbar^2} \right]^{1/2} \sum_{E_n \leq E} \frac{1}{\sqrt{E - E_n}} \Theta(E - E_n)$$



K. F. Berggren et al.  
PRB **37**, 10118 (1988)

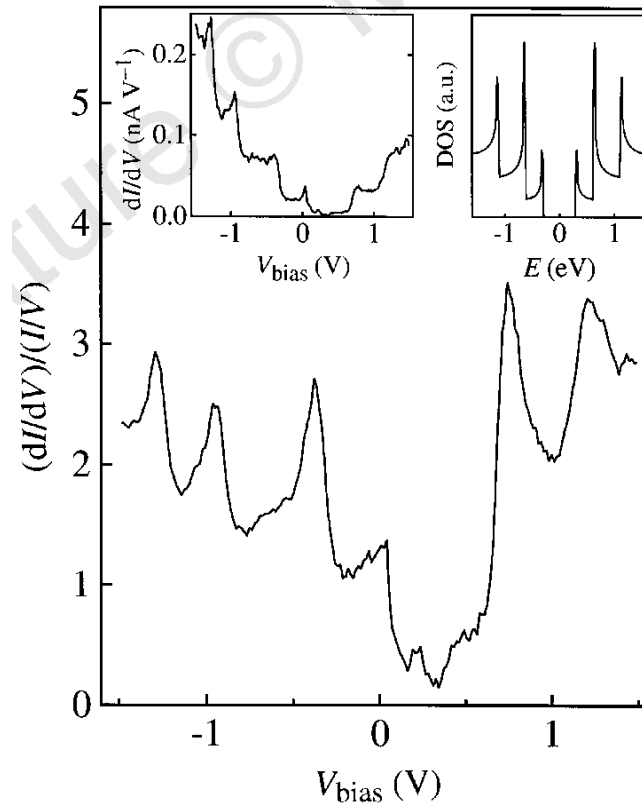
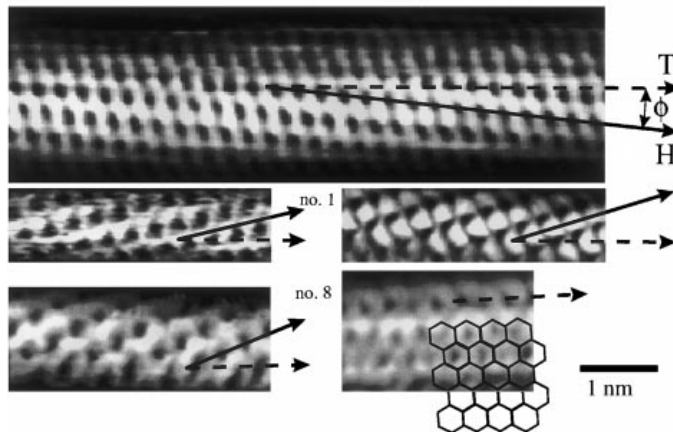




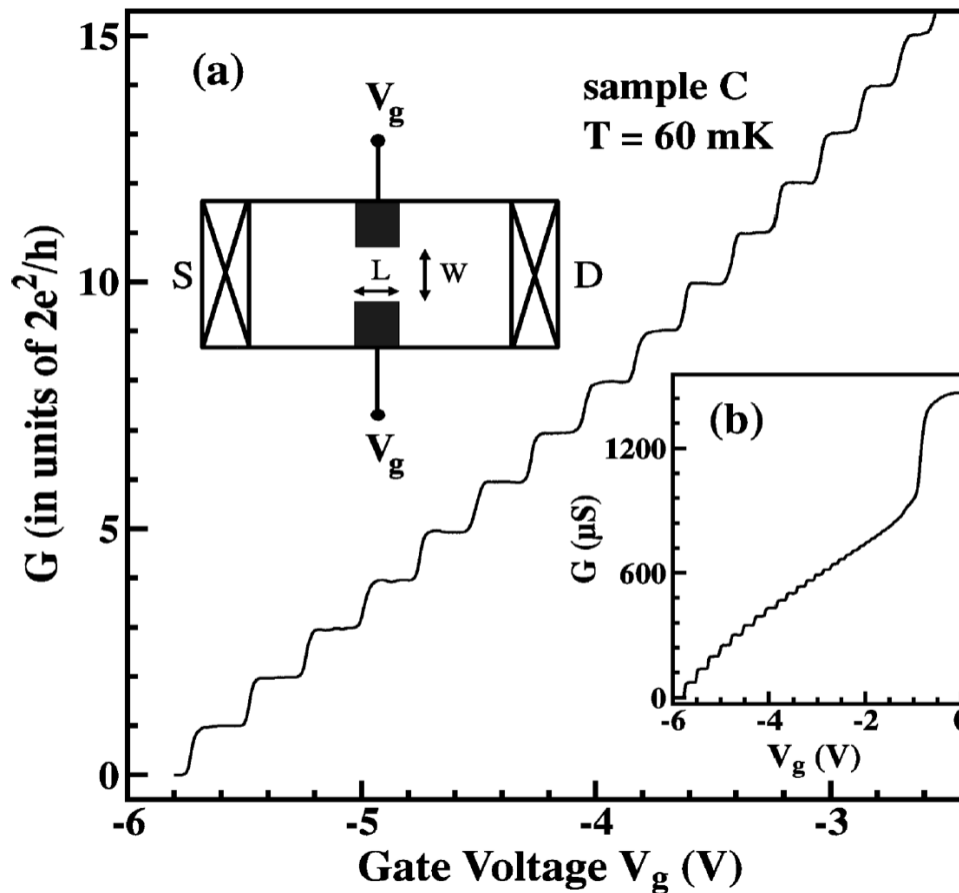
# In Real Systems DoS Follows from a **SUM** Over Multiple **1-D SUBBANDS**

## Electronic structure of atomically resolved carbon nanotubes

Jeroen W. G. Wildöer\*, Liesbeth C. Venema\*,  
Andrew G. Rinzler†, Richard E. Smalley† & Cees Dekker\*



# 1-D DoS Responsible for a Unique Conductance **QUANTIZATION**



Pepper Group  
Cambridge (U.K.)

