

# Ultracold atoms and neutron-rich matter in nuclei and astrophysics

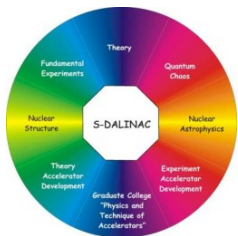
Achim Schwenk



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



**NORDITA program “Pushing the boundaries with cold atoms”**  
Stockholm, Jan. 23, 2013



**DFG**



*Minerva  
Stiftung*  
**ARCHES**  
Award for Research Cooperation and  
High Excellence in Science



Bundesministerium  
für Bildung  
und Forschung

# Outline

## Advances in nuclear forces

### 3N forces and neutron-rich nuclei

with J.D. Holt, J. Menendez, T. Otsuka, T. Suzuki



### 3N forces and neutron matter/stars

with K. Hebeler, T. Krüger, I. Tews,  
J.M. Lattimer, C.J. Pethick



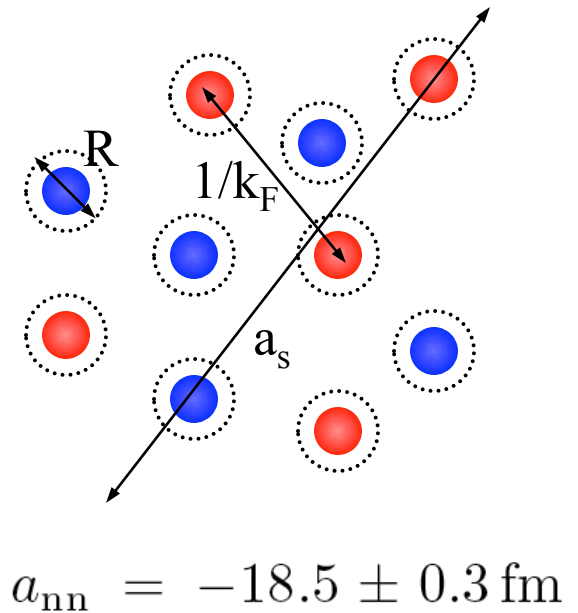
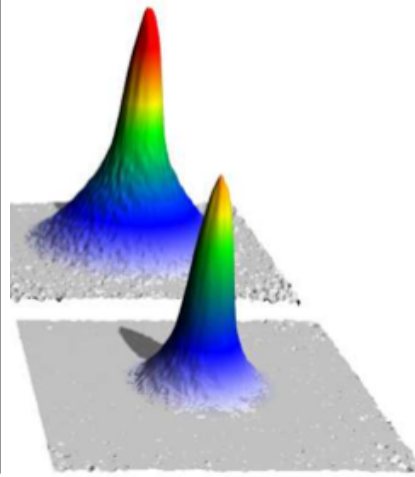
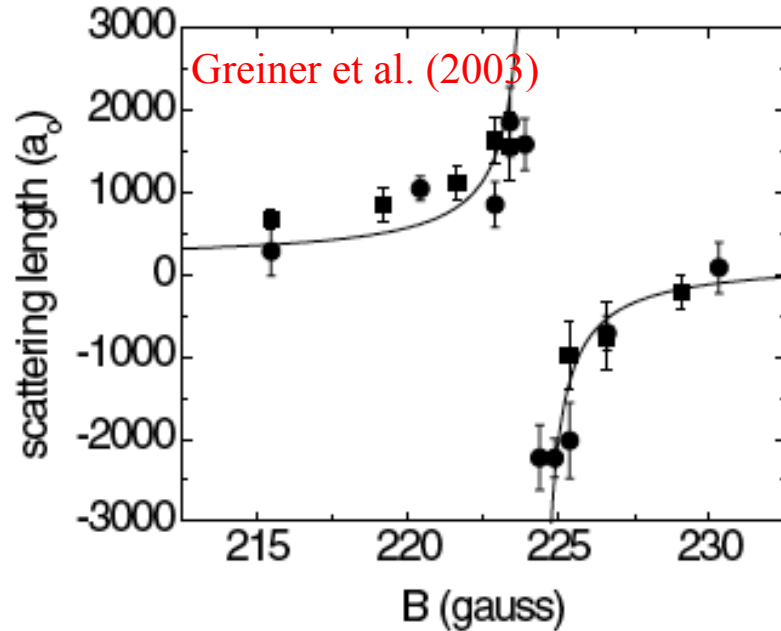
**NORDITA**

### Neutron polaron and density functionals

with M. Forbes, A. Gezerlis,  
K. Hebeler, T. Lesinski



# Large scattering lengths: Universal properties at low densities



strong interactions via Feshbach resonances

large for neutrons

dilute Fermi system with large scattering length has **universal properties**

$$0 \leftarrow 1/a_s \ll k_F \ll 1/r_e, 1/R, \dots \rightarrow \infty$$

strongly-interacting                      dilute




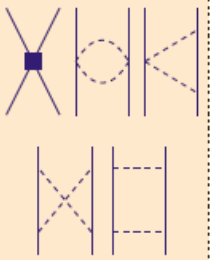


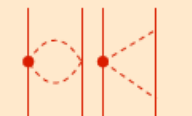
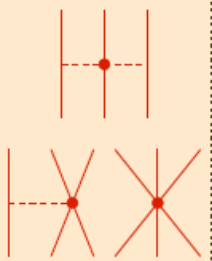



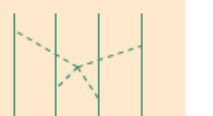
only Fermi momentum or density sets scale

physics is independent of interaction/system details:

from dilute neutron matter to resonant  ${}^6\text{Li}$  or  ${}^{40}\text{K}$  atoms in traps

# Chiral Effective Field Theory for nuclear forces

Separation of scales: low momenta  $\frac{1}{\lambda} = Q \ll \Lambda_b$  breakdown scale  $\sim 500$  MeV

	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N <sup>2</sup> LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N <sup>3</sup> LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$	 + ...	 + ...	 + ...

limited resolution at low energies,  
can expand in powers  $(Q/\Lambda_b)^n$

LO,  $n=0$  - leading order,  
NLO,  $n=2$  - next-to-leading order,...

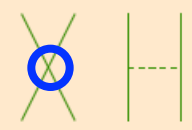


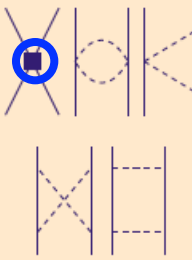


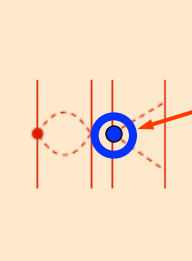
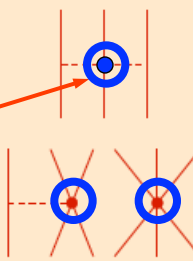

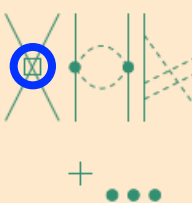
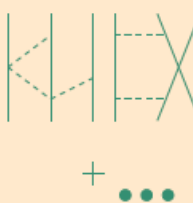
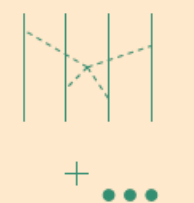
expansion parameter  $\sim 1/3$

(compare to multipole expansion  
for a charge distribution)



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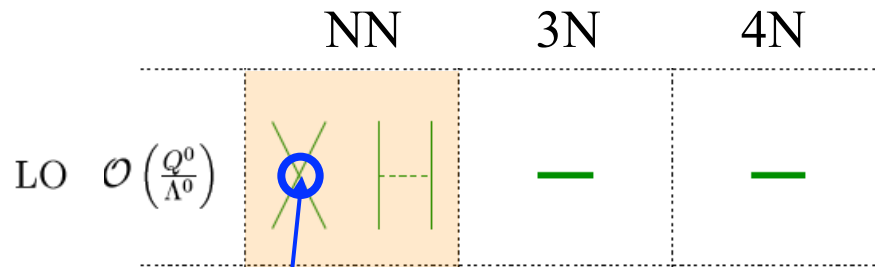
include long-range pion physics

few short-range couplings,  
fit to experiment once

systematic: can work to desired  
accuracy and obtain **error estimates**

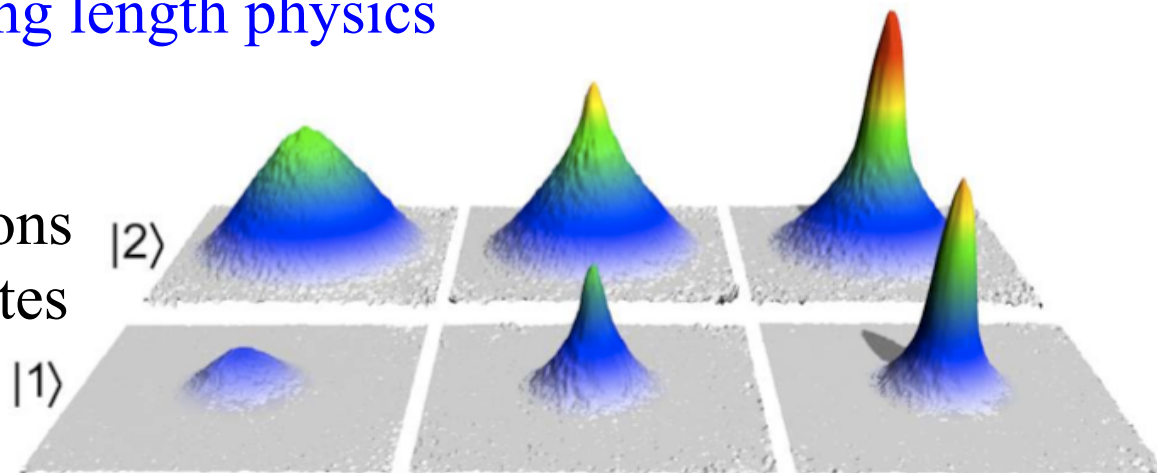
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large scattering length physics

${}^6\text{Li}$  fermions  
2 spin states

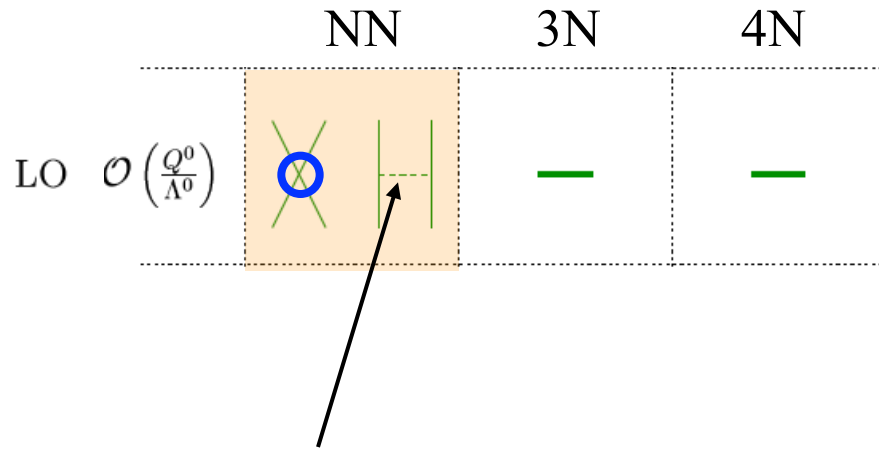


from M. Zwierlein

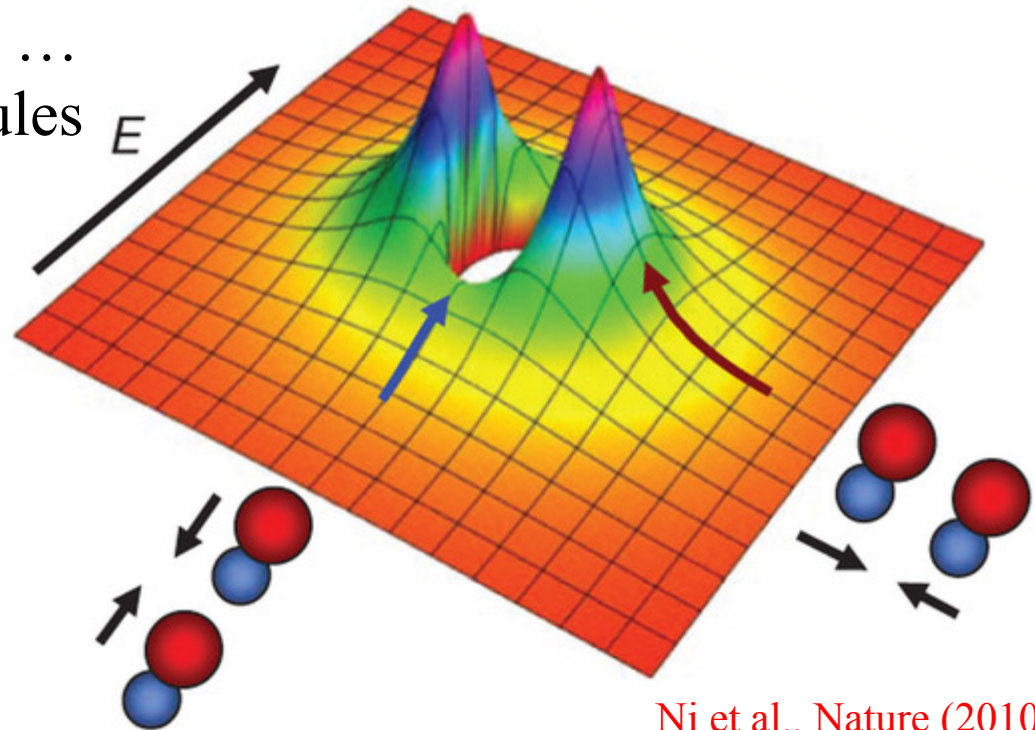
neutrons with same density, temperature and spin polarization  
have the same properties!

# Chiral Effective Field Theory for nuclear forces

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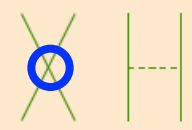


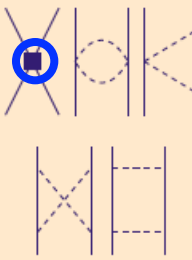


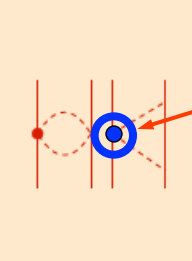
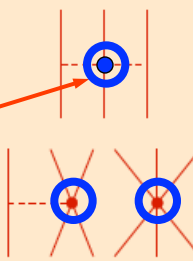

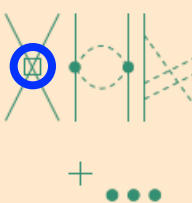
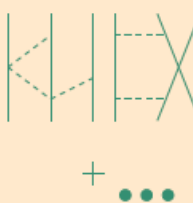
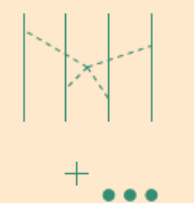


pion tensor/dipole interactions + ...  
 → compare to cold polar molecules



# Chiral Effective Field Theory for nuclear forces

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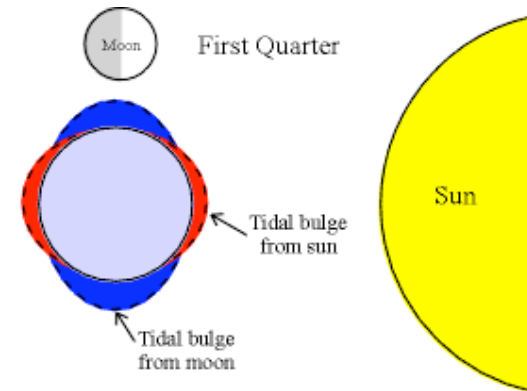
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include long-range pion physics

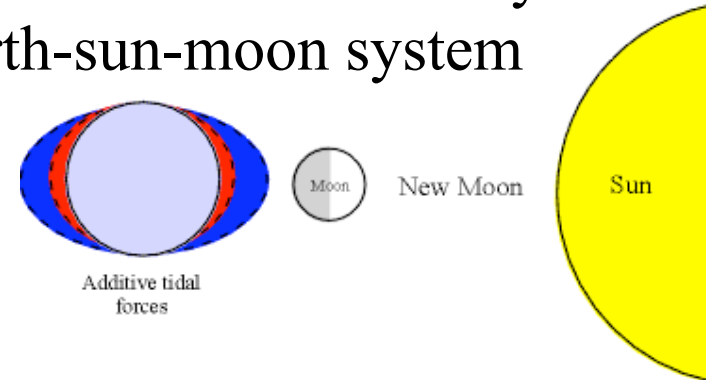
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systematic: can work to desired  
accuracy and obtain **error estimates**

# Why are there three-body forces?



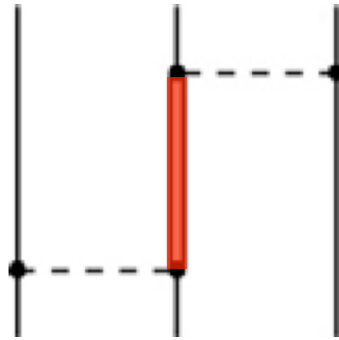
tidal effects lead to 3-body forces  
in earth-sun-moon system



# Why are there 3N forces?

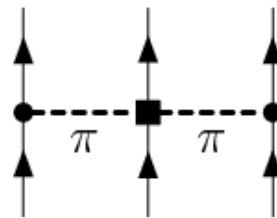
Nucleons are finite-mass composite particles,  
can be excited to resonances

dominant contribution from  $\Delta(1232 \text{ MeV})$

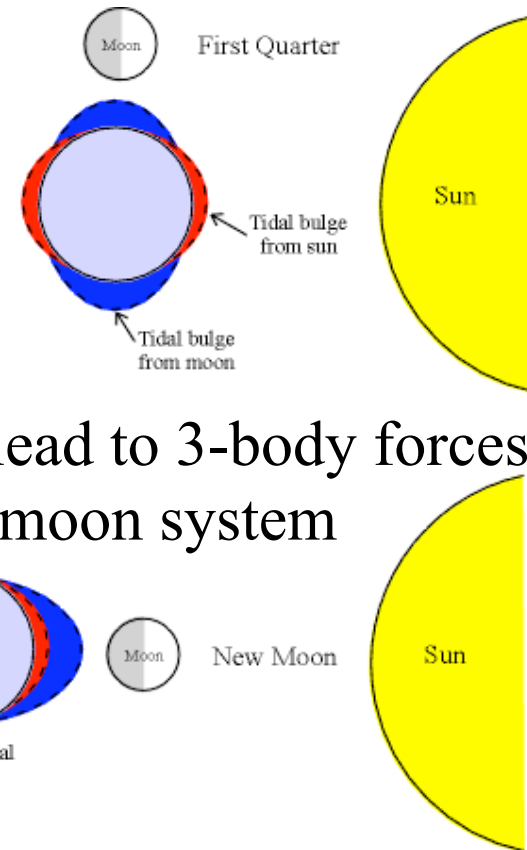


+ many shorter-range parts

chiral effective field theory (EFT)  
Delta-less ( $\Delta$  is treated as heavy):



+ shorter-range parts



tidal effects lead to 3-body forces  
in earth-sun-moon system

**EFT provides a systematic and powerful approach for 3N forces**

# Chiral Effective Field Theory and many-body forces

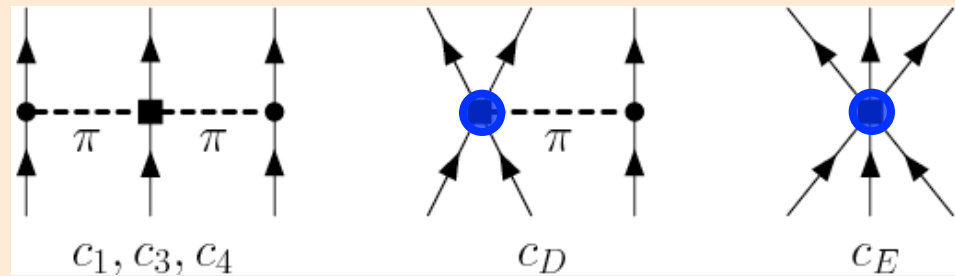
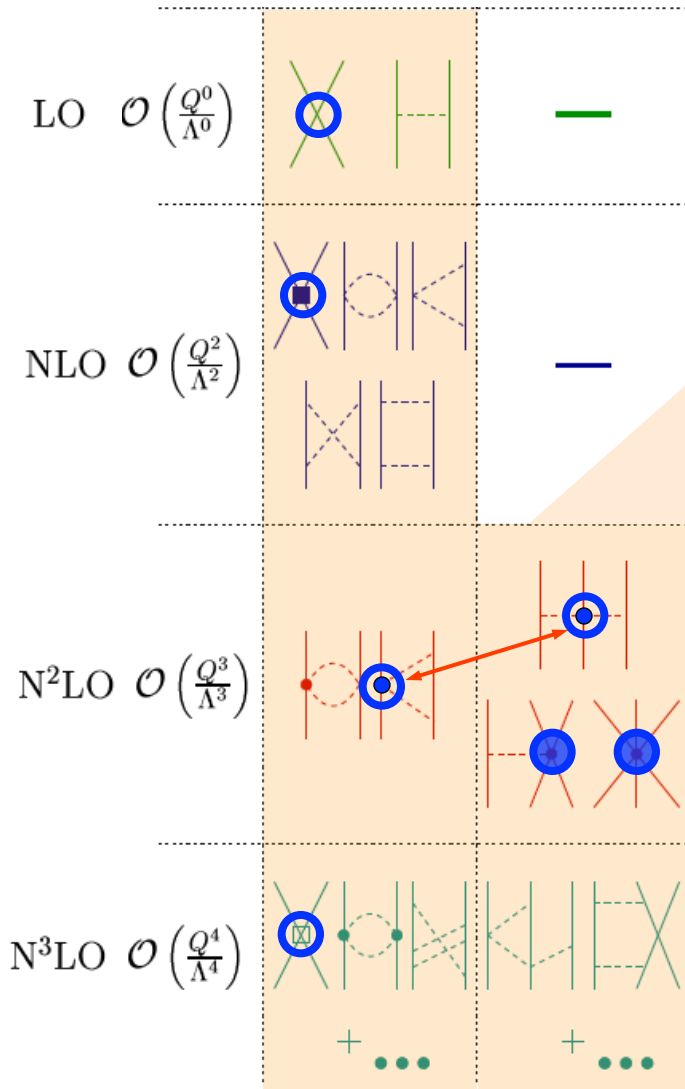
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NN

3N

consistent NN-3N interactions

3N,4N: only 2 new couplings to N<sup>3</sup>LO



$c_i$  from  $\pi$ N and NN Meissner et al. (2007)

$$c_1 = -0.9^{+0.2}_{-0.5}, \quad c_3 = -4.7^{+1.2}_{-1.0}, \quad c_4 = 3.5^{+0.5}_{-0.2}$$

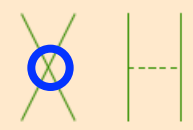


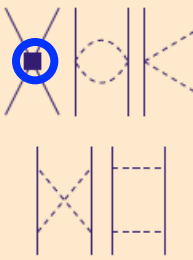

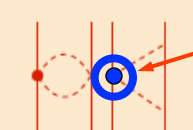
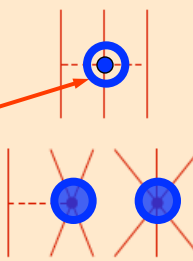
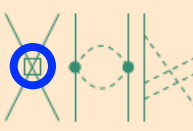
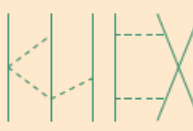
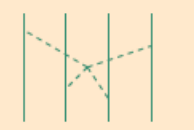
single- $\Delta$ :  $c_1=0$ ,  $c_3=-c_4/2=-3 \text{ GeV}^{-1}$

$c_D, c_E$  fit to  $^3\text{H}$ ,  $^4\text{He}$  properties only



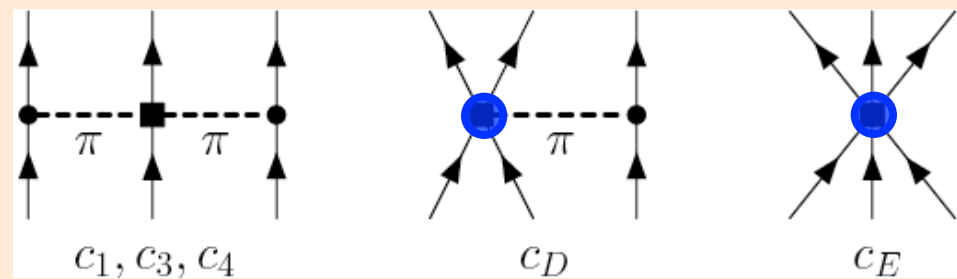
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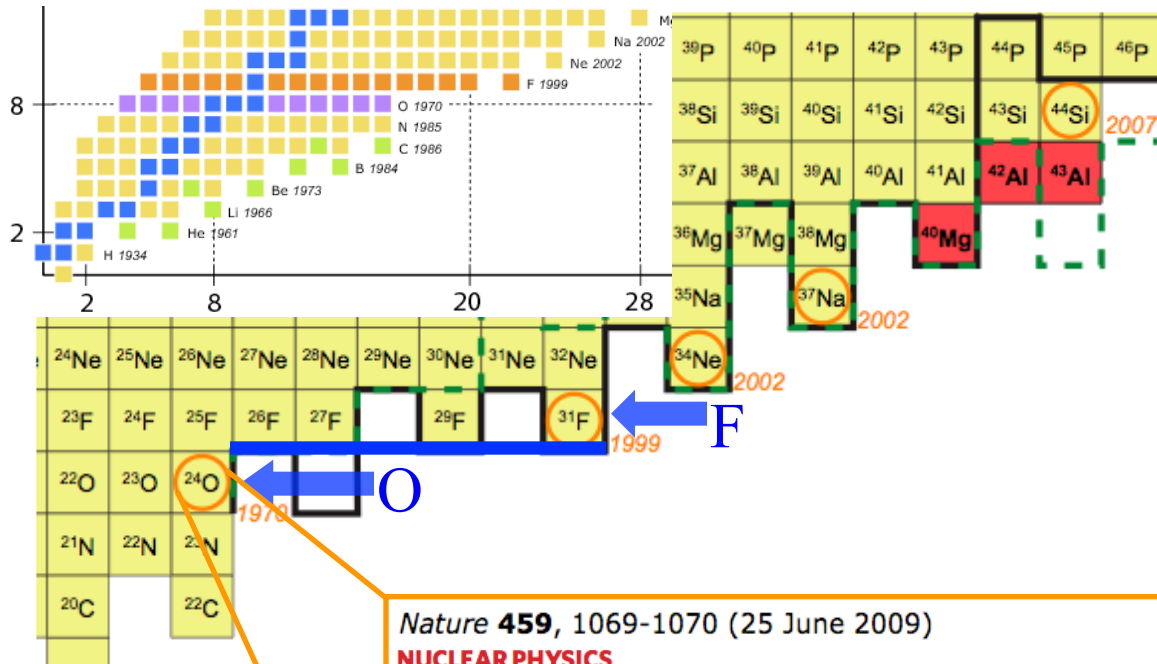
$c_D, c_E$  don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for  $c_4$

Hebeler, AS (2010)



**all 3- and 4-neutron forces are predicted to N<sup>3</sup>LO!**

# The oxygen anomaly



*Nature* **459**, 1069-1070 (25 June 2009)

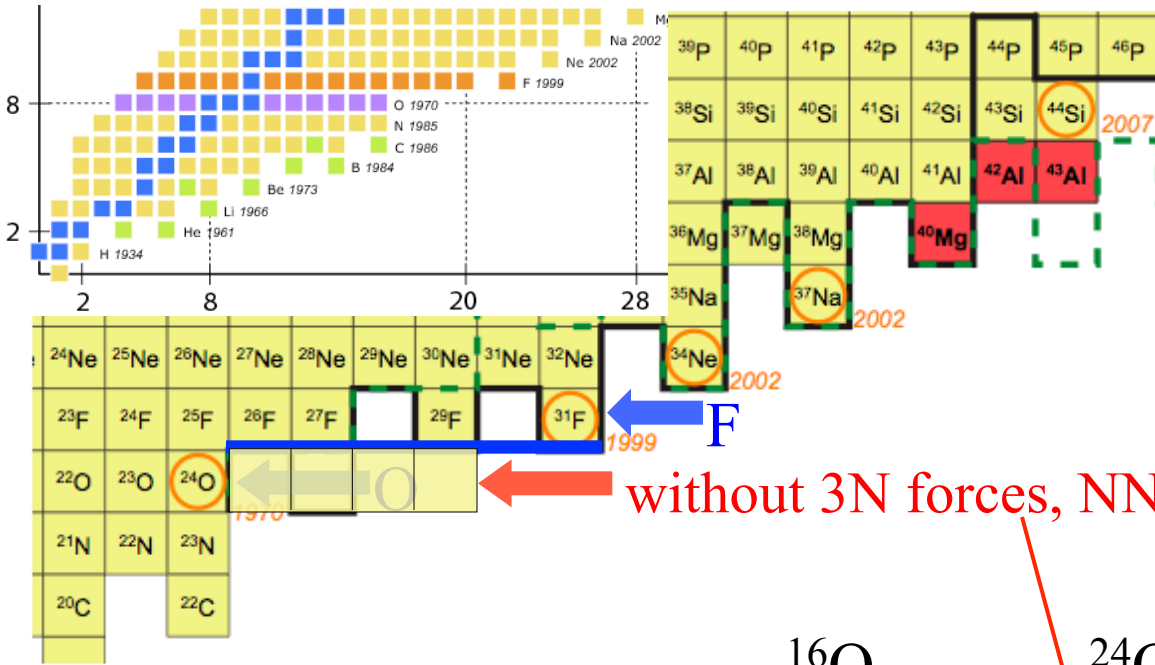
**NUCLEAR PHYSICS**

## Unexpected doubly magic nucleus

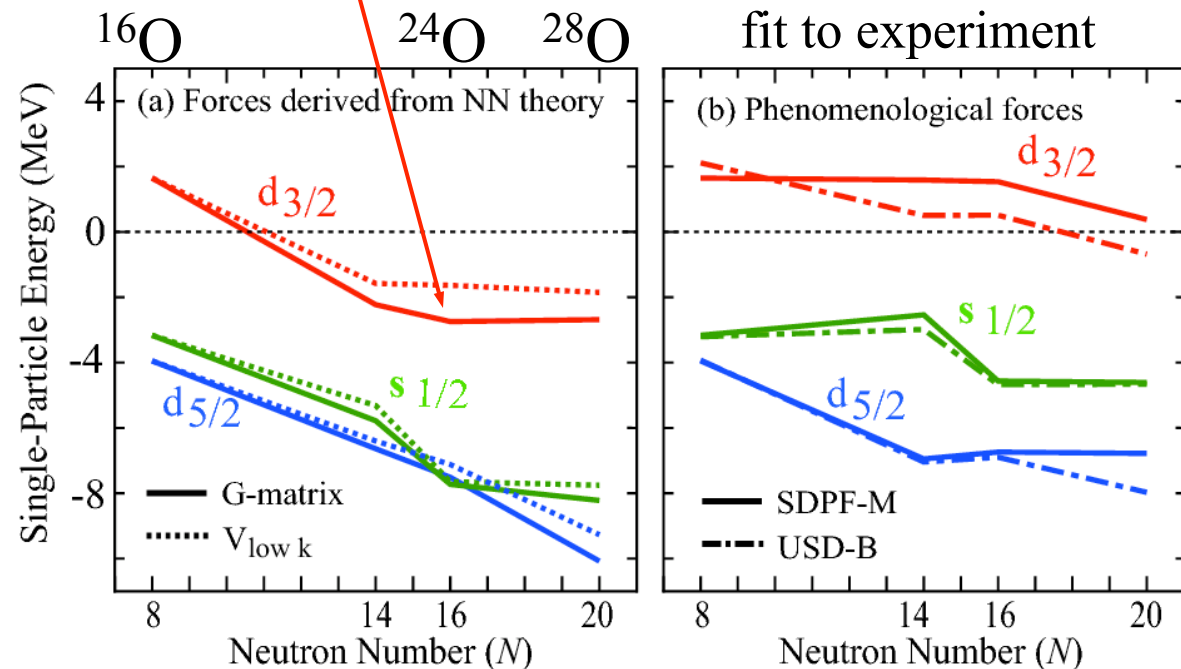
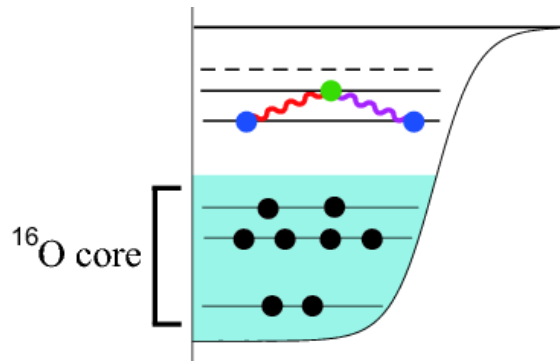
Robert V. F. Janssens

Nuclei with a 'magic' number of both protons and neutrons, dubbed doubly magic, are particularly stable. The oxygen isotope  $^{24}\text{O}$  has been found to be one such nucleus — yet it lies just at the limit of stability.

# The oxygen anomaly - not reproduced without 3N forces



many-body theory based  
on two-nucleon forces:  
drip-line incorrect at  $^{28}\text{O}$



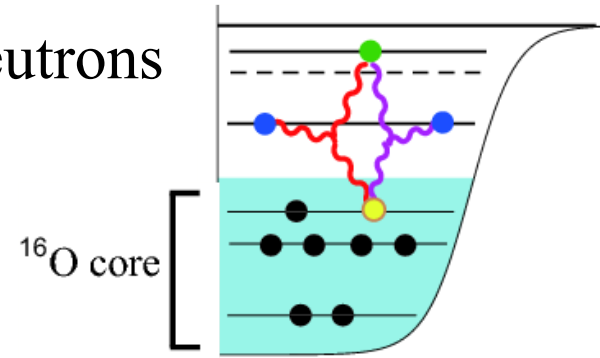
# The shell model - impact of 3N forces

include 'normal-ordered' 2-body part of 3N forces (enhanced by core A)

leads to repulsive interactions between valence neutrons

contributions from residual three valence-nucleon interactions suppressed by  $E_{\text{ex}}/E_{\text{F}} \sim N_{\text{valence}}/N_{\text{core}}$

Friman, AS (2011)



# Oxygen isotopes - impact of 3N forces

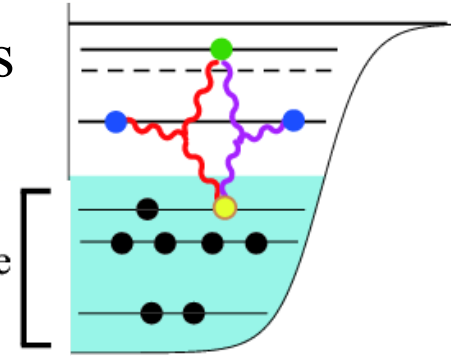
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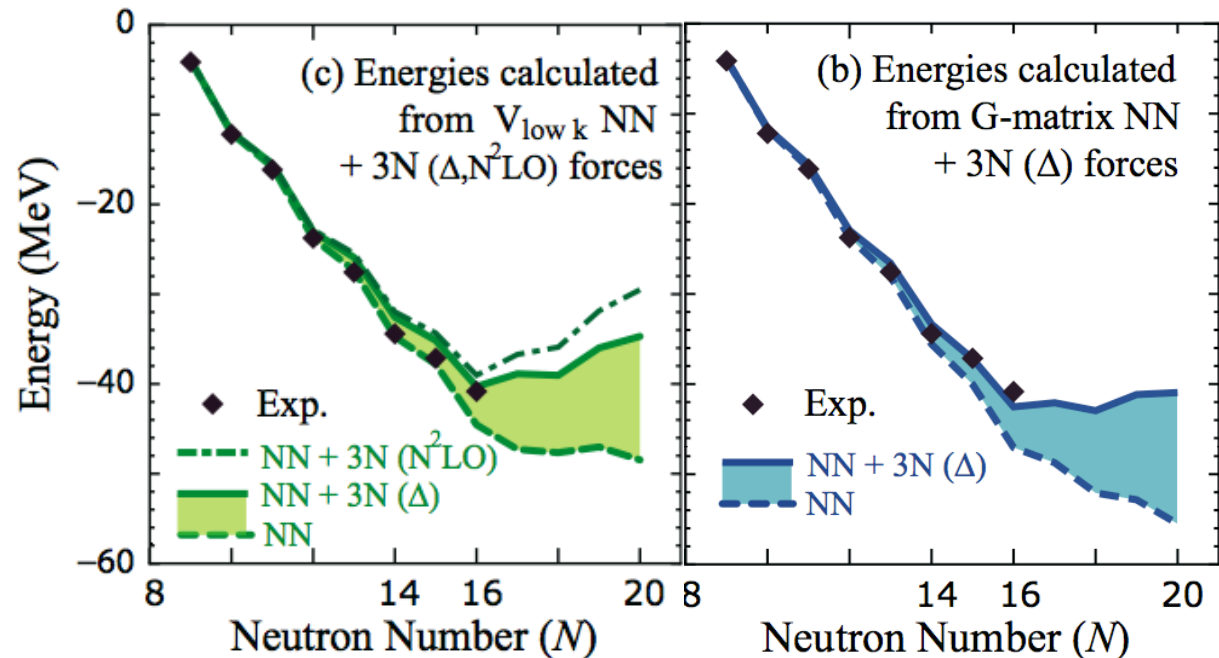
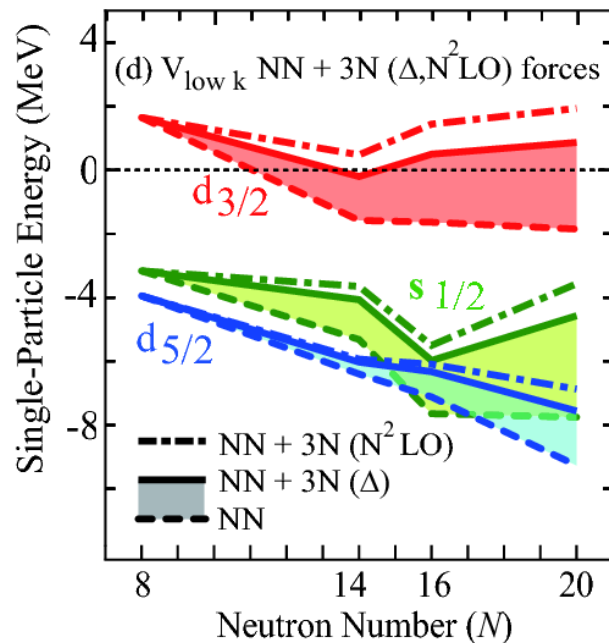
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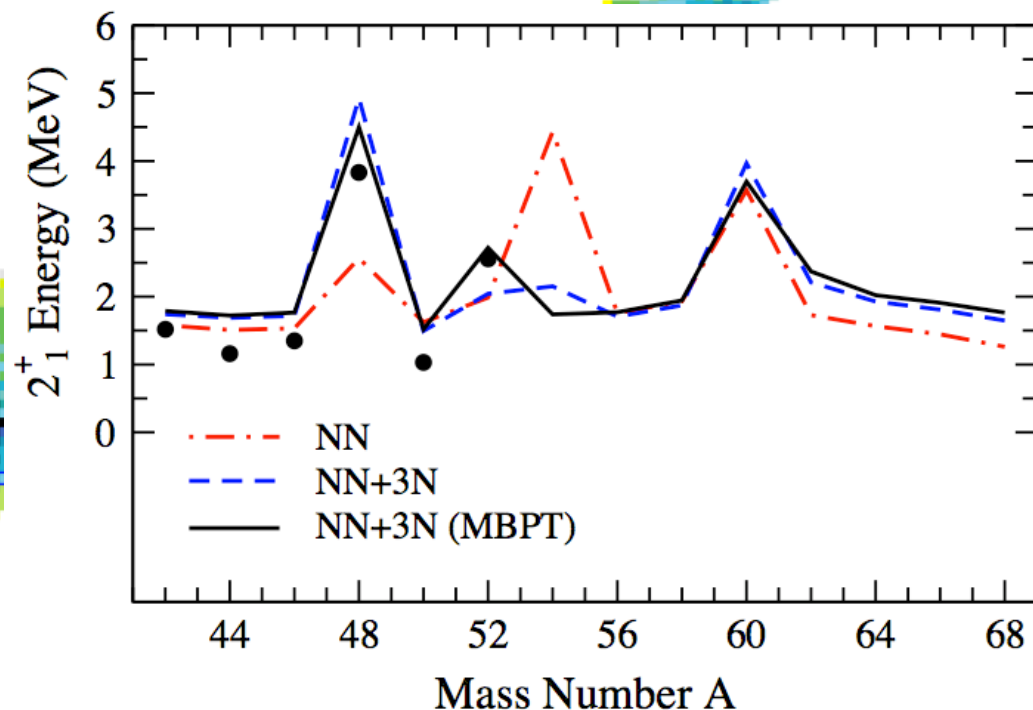
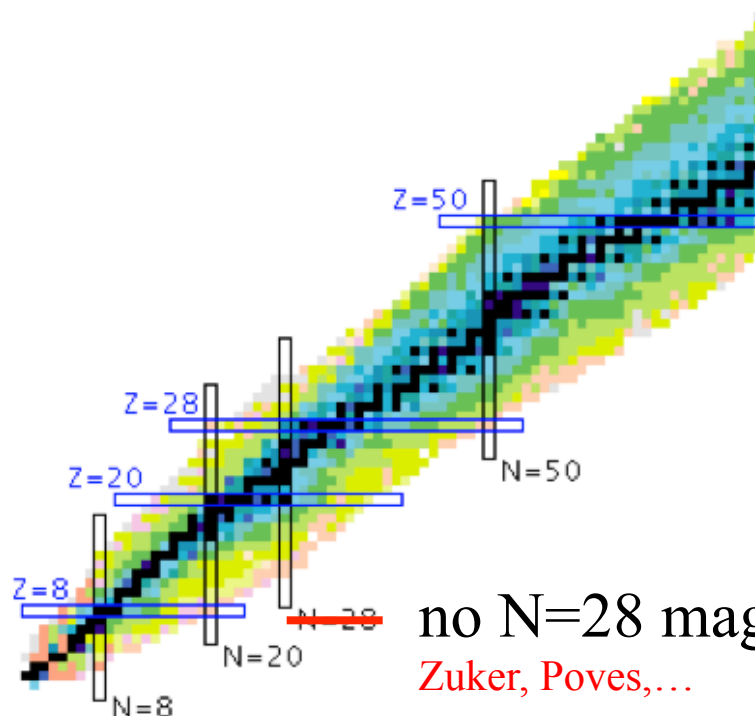


$d_{3/2}$  orbital remains unbound from  $^{16}\text{O}$  to  $^{28}\text{O}$



microscopic explanation of the oxygen anomaly Otsuka et al. (2010)

# Three-body forces and magic numbers



Holt et al. (2010), Holt, Menendez, AS, in prep.

no  $N=28$  magic number from microscopic NN forces

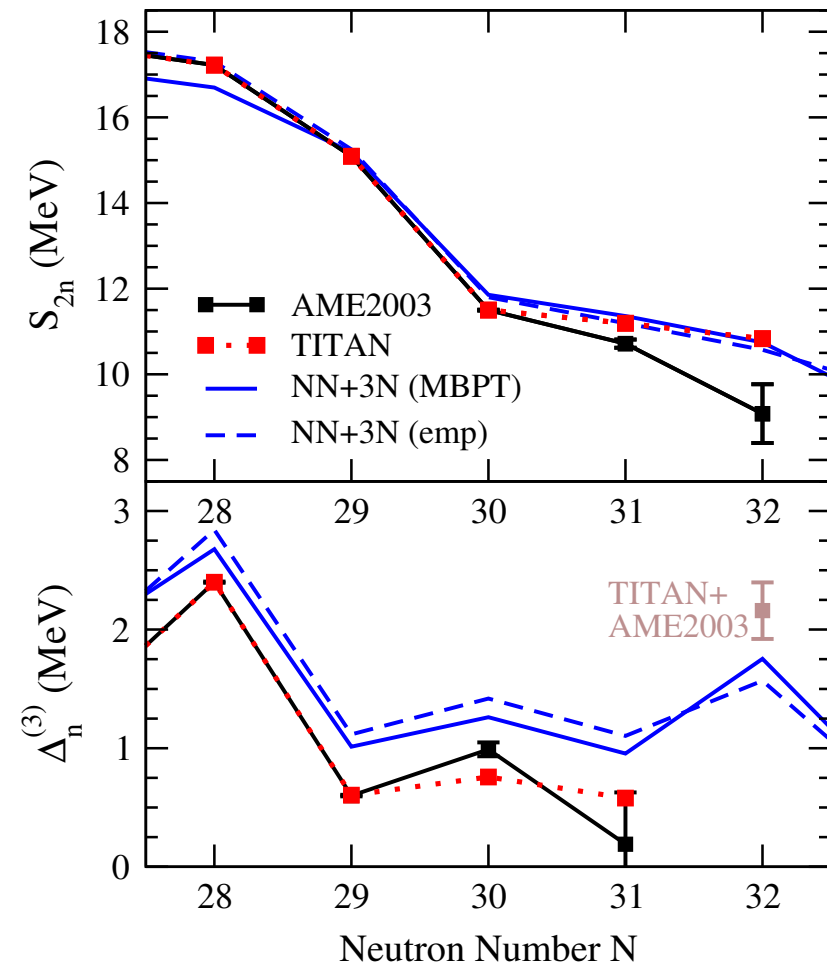
Zuker, Poves,...

# new $^{51,52}\text{Ca}$ TITAN measurements

$^{52}\text{Ca}$  is 1.75 MeV more bound  
compared to atomic mass evaluation

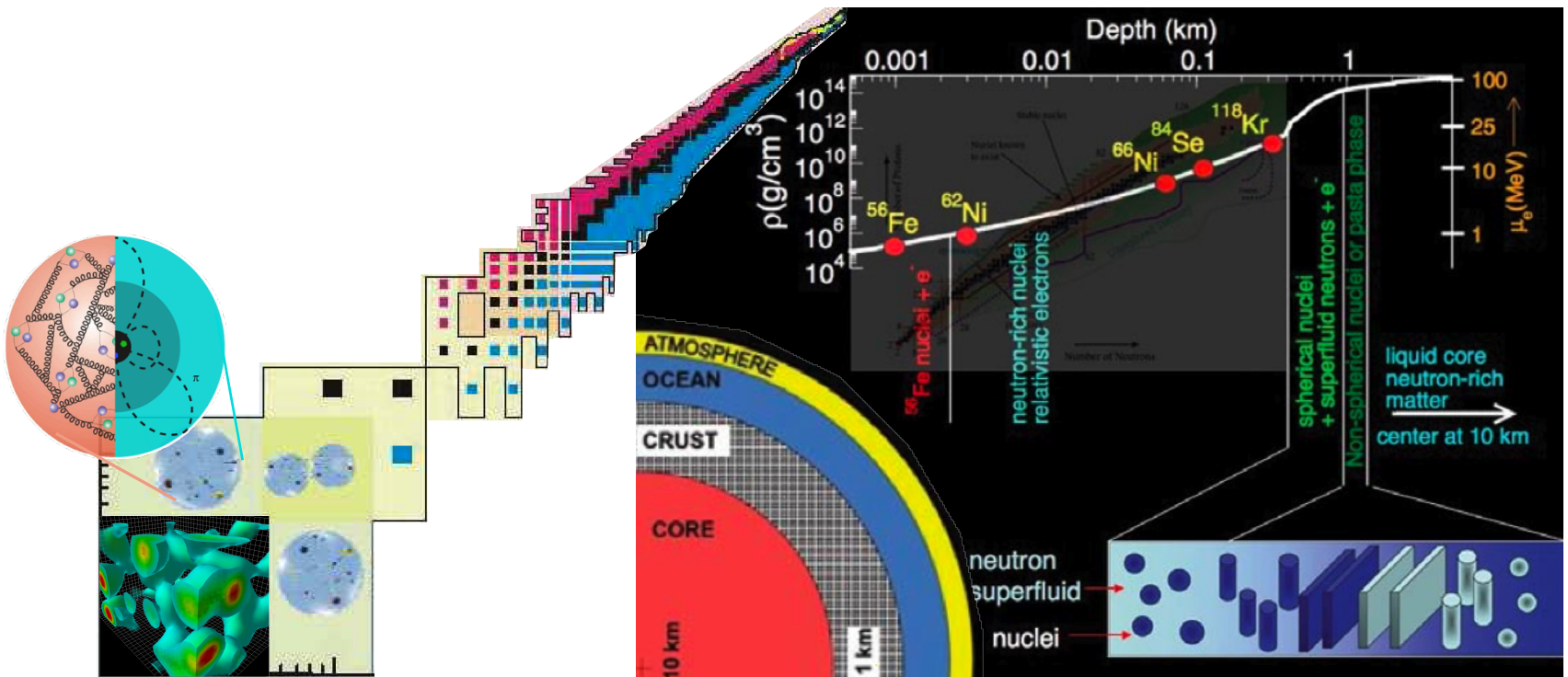
Gallant et al. (2012)

behavior of two-neutron separation  
energy  $S_{2n}$  and odd-even staggering  $\Delta_n$   
agrees with NN+3N predictions





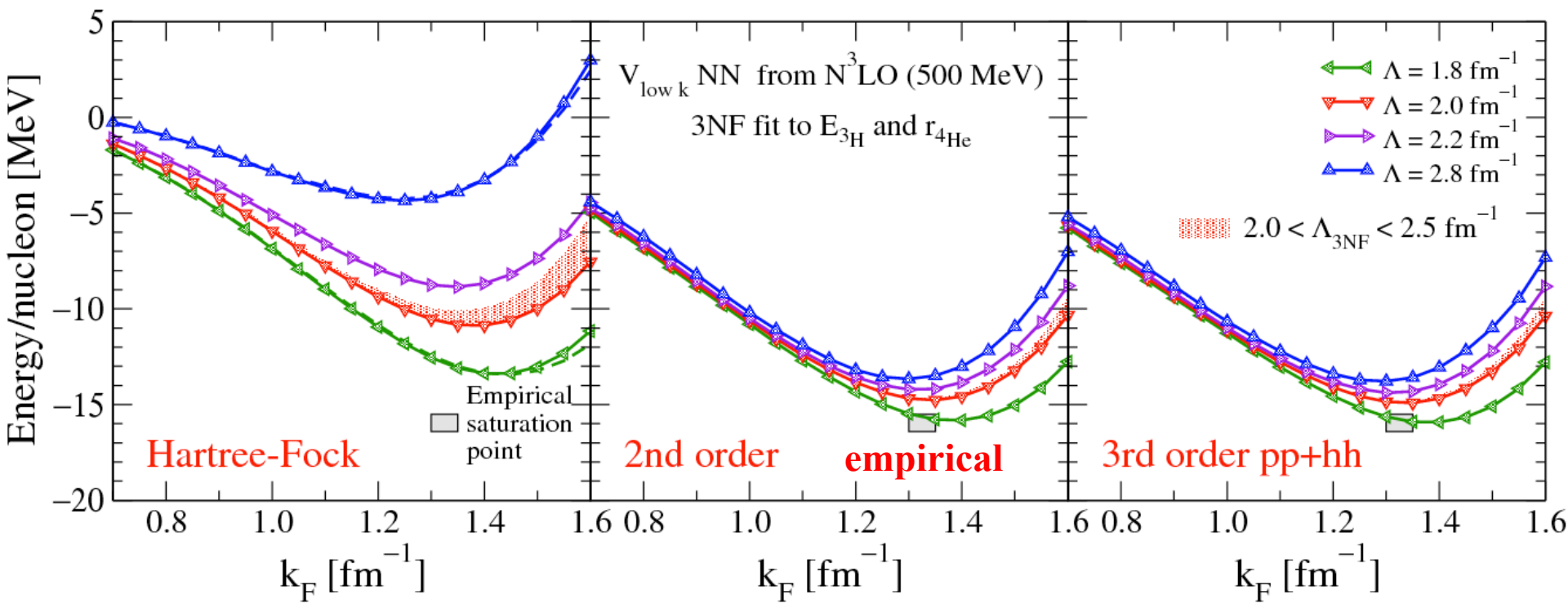
# Neutron matter and neutron stars



# Impact of 3N forces on nuclear matter

chiral 3N forces fit to light nuclei  
predict nuclear matter saturation  
with theoretical uncertainties

Hebeler et al. (2011), Bogner et al. (2005)

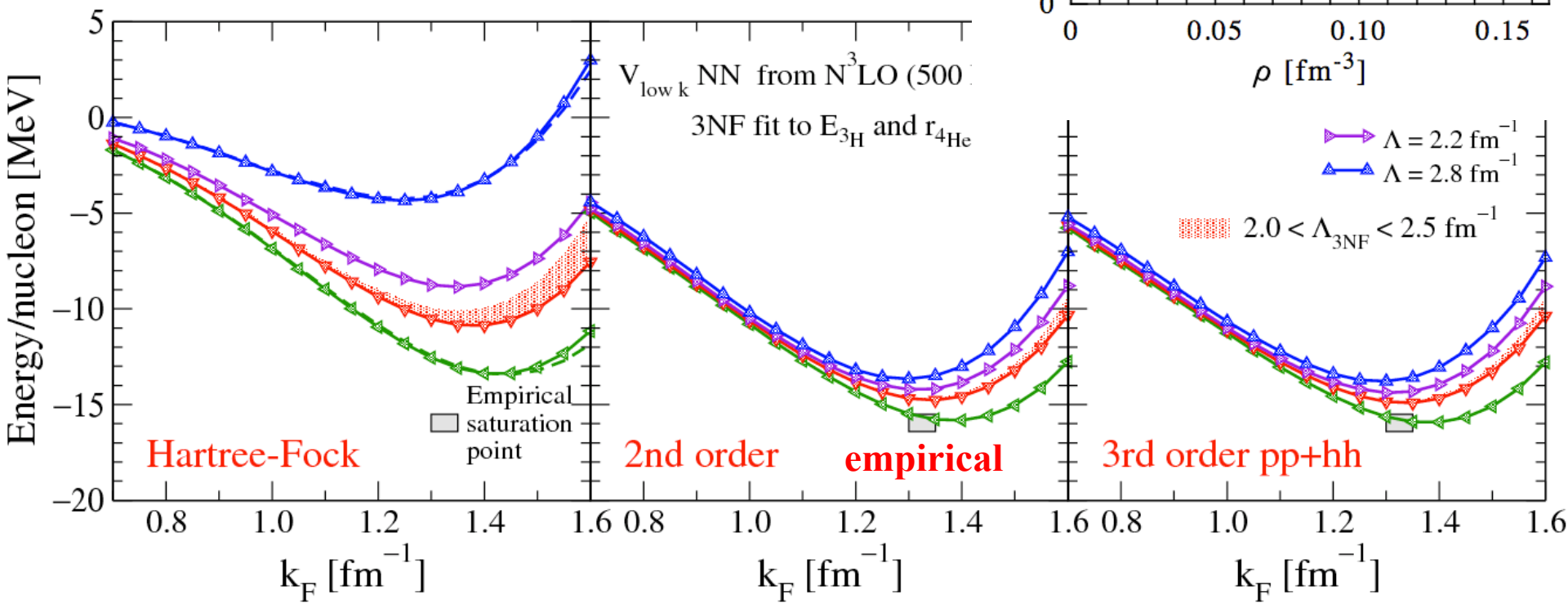
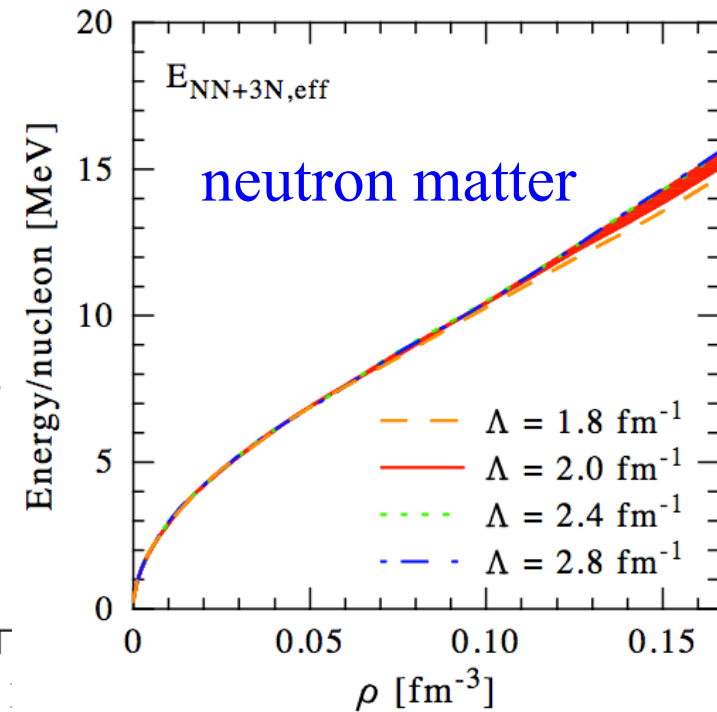


# Impact of 3N forces on neutron matter

neutron matter is simpler system,  
only long-range parts of 3N forces  
contribute ( $c_1$  and  $c_3$ )

Hebeler, AS (2010)

scales as in universal regime at low densities,  
cold atoms provide anchor point



# Chiral Effective Field Theory and many-body forces

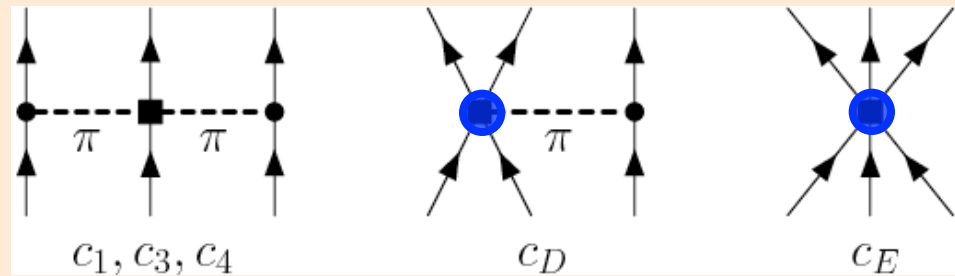
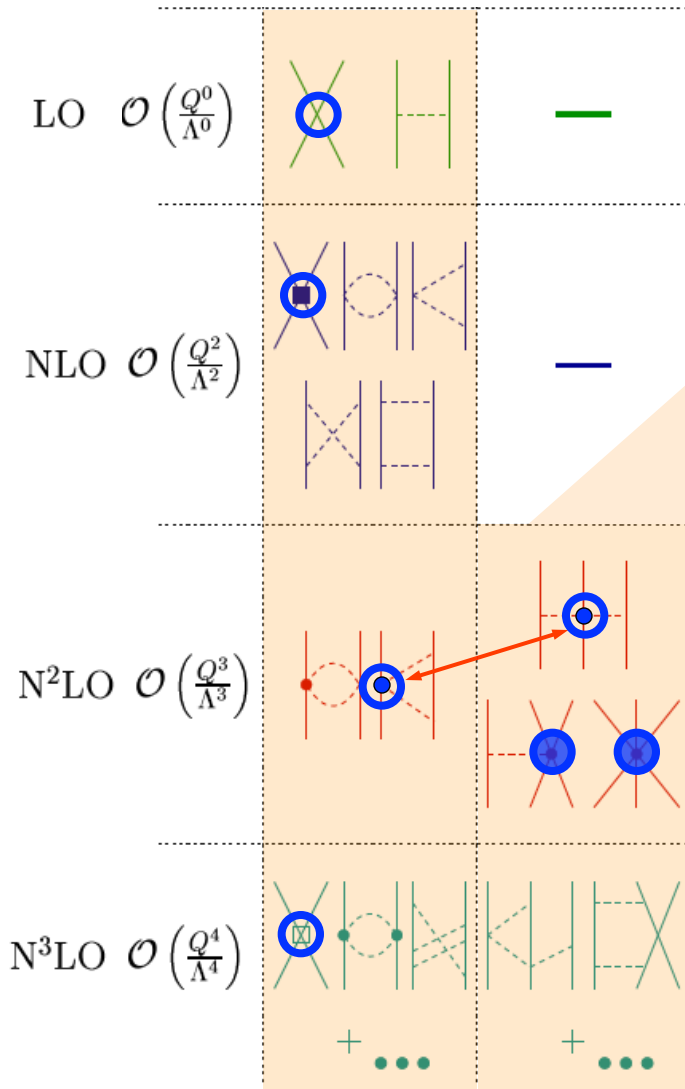
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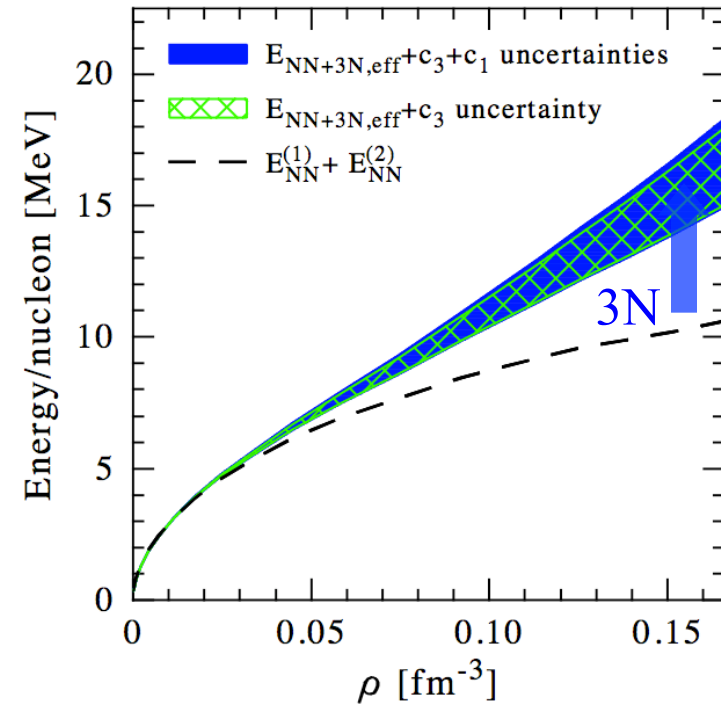
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neutron matter uncertainties

dominated by 3N forces ( $c_3$  coupling)

Hebeler, AS (2010)

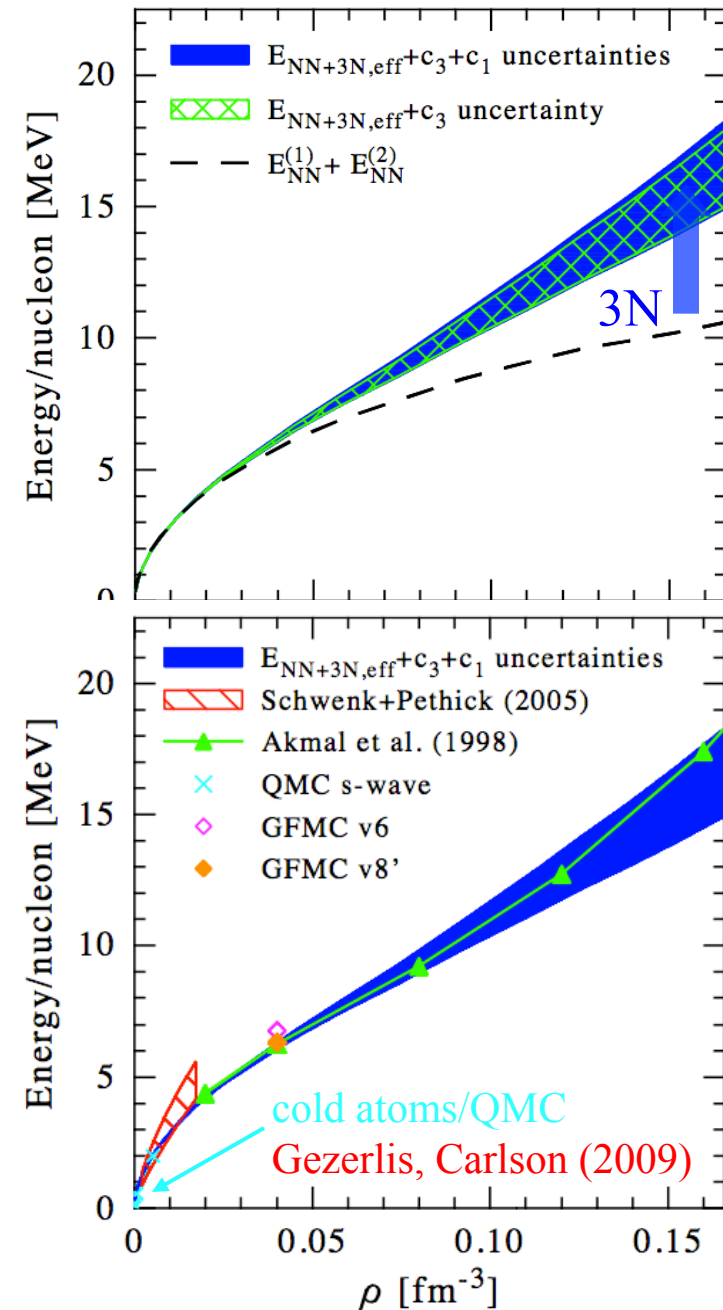


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Hebeler, AS (2010)

other microscopic calculations within band  
(but without uncertainties)



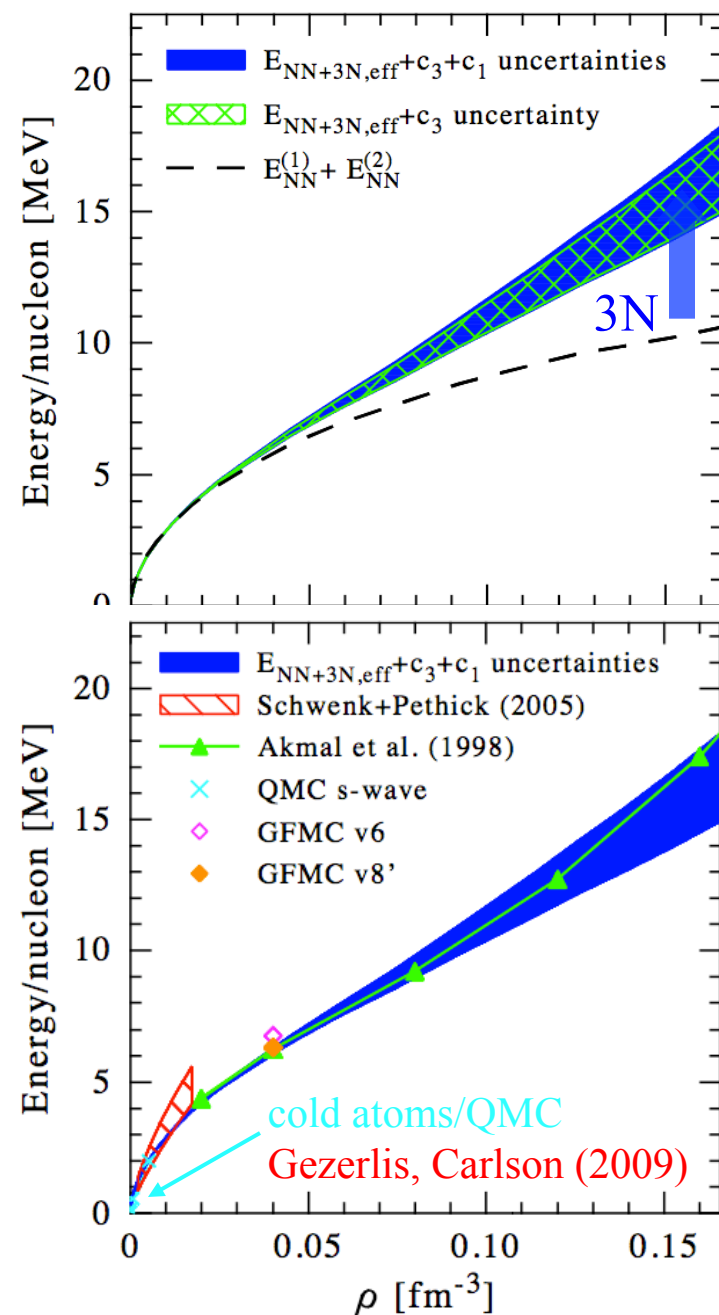
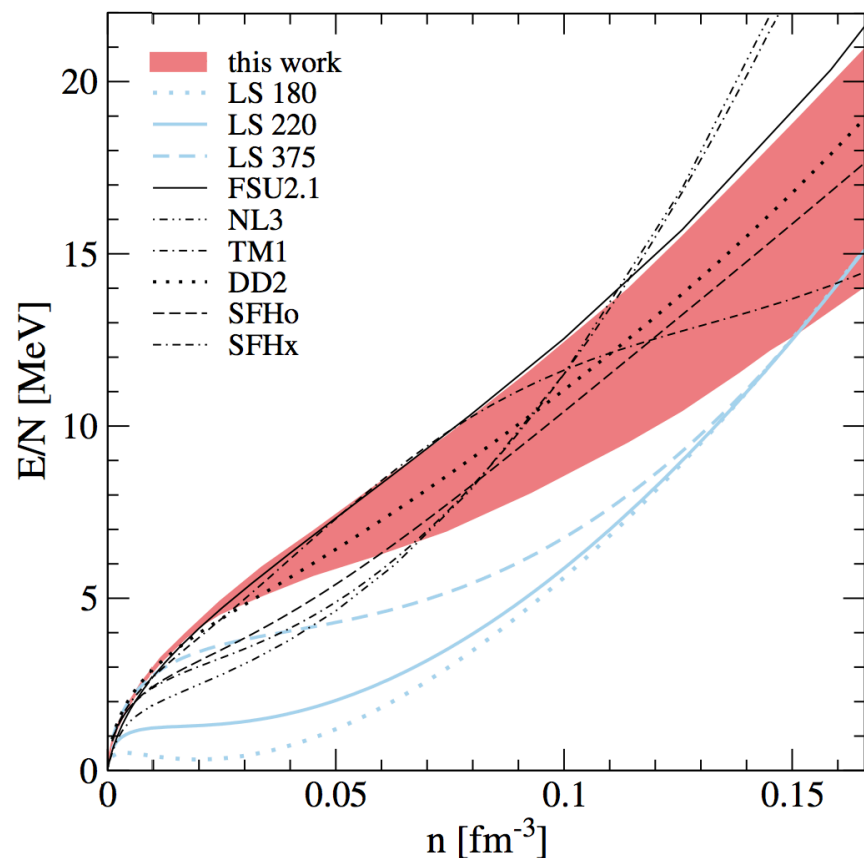
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neutron matter uncertainties

dominated by 3N forces ( $c_3$  coupling)

Hebeler, AS (2010)

Problem: many equations of state  
not consistent with neutron matter results





# Symmetry energy and pressure of neutron matter

neutron matter band predicts  
symmetry energy  $S_v$  and  
its density dependence  $L$

comparison to experimental  
and observational constraints

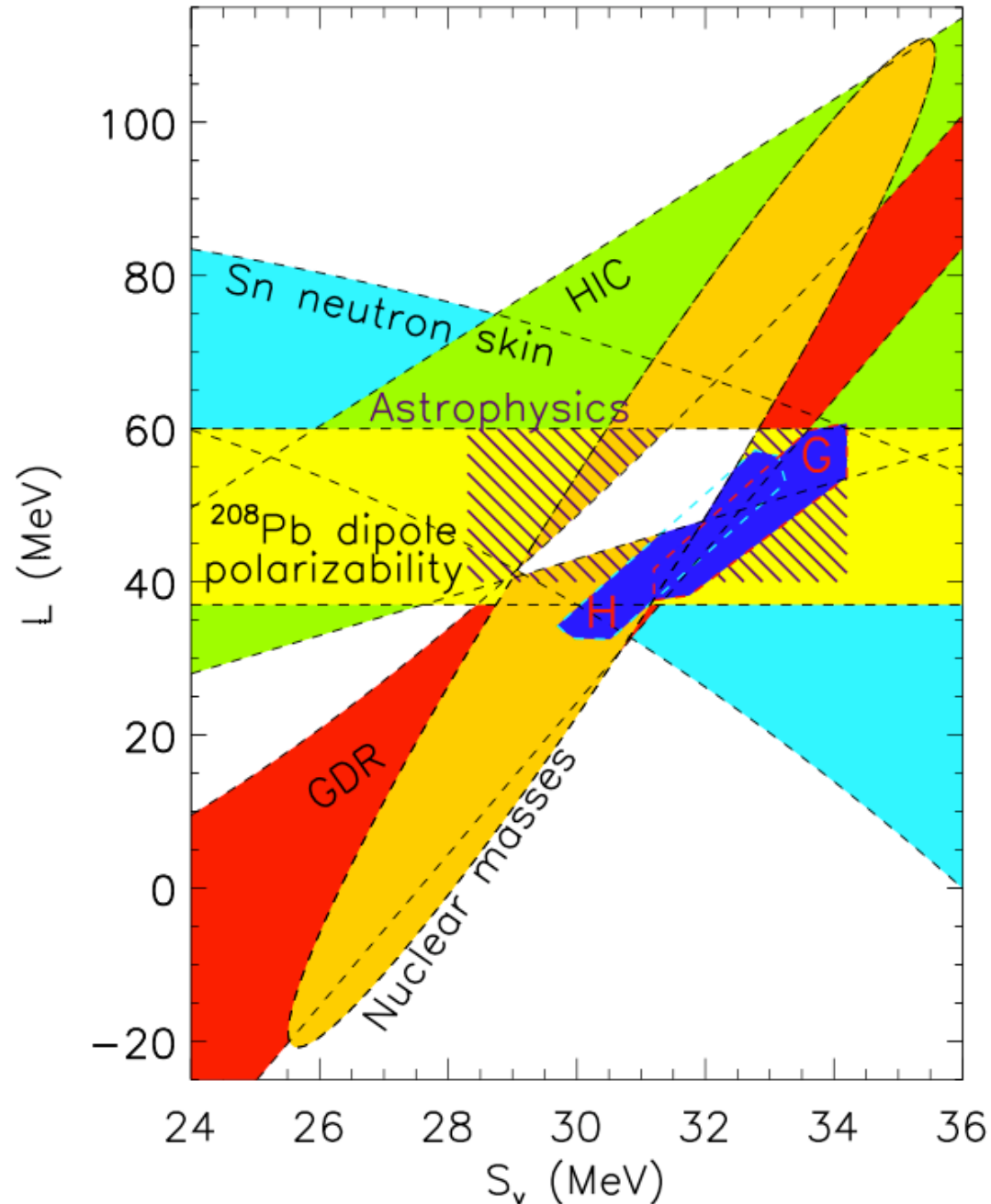
Lattimer, Lim (2012)

neutron matter constraints

H: Hebeler et al. (2010) and in prep.

G: Gandolfi et al. (2011)

predicts correlation  
but not range of  $S_v$  and  $L$



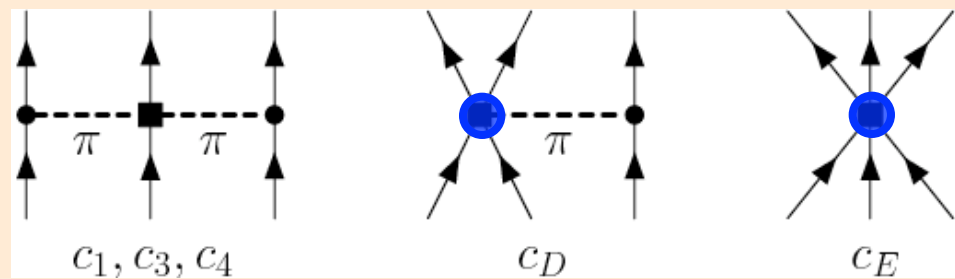
# Chiral Effective Field Theory for nuclear forces

Separation of scales: low momenta  $\frac{1}{\lambda} = Q \ll \Lambda_b$  breakdown scale  $\sim 500$  MeV

	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N <sup>2</sup> LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N <sup>3</sup> LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

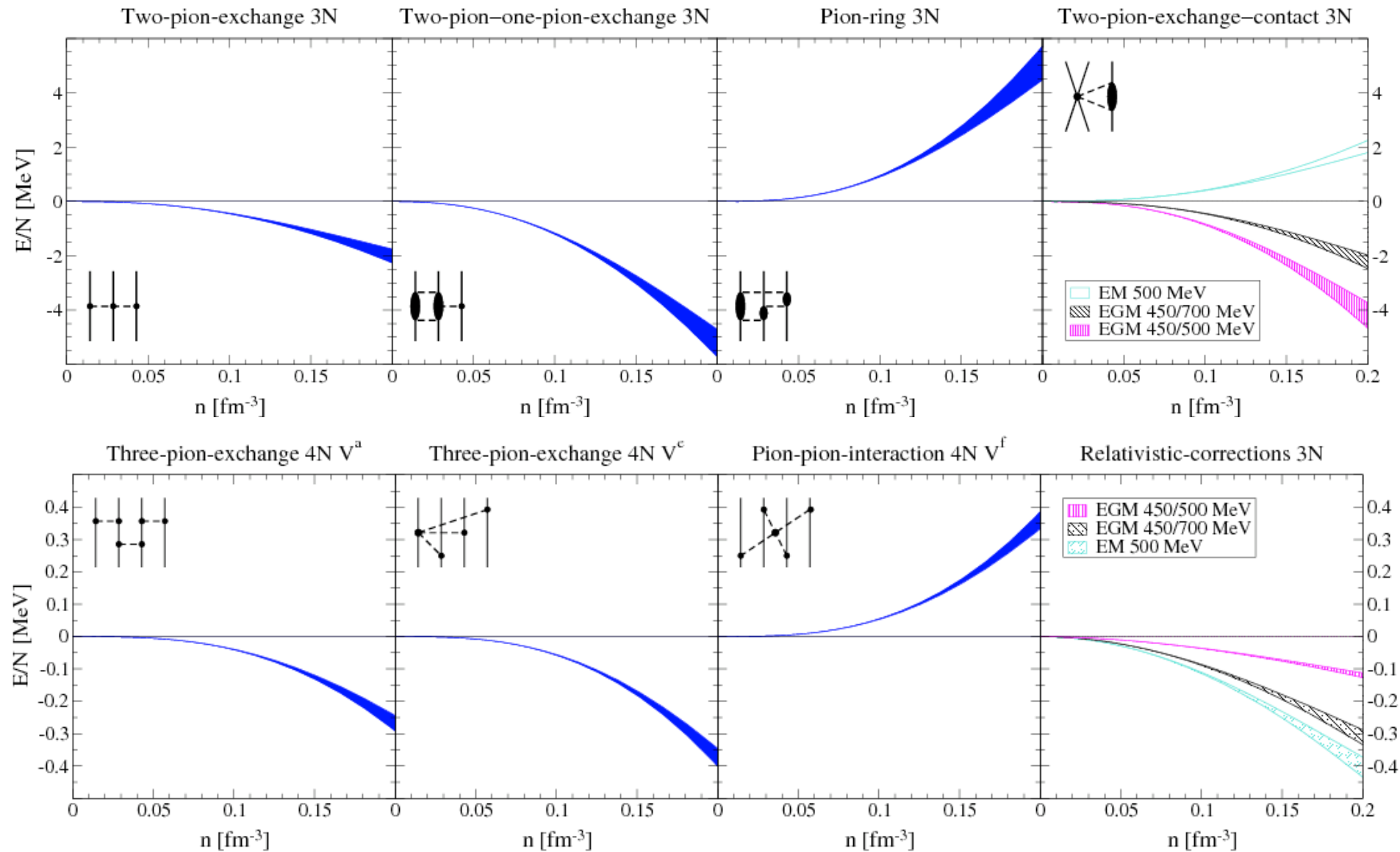
$c_D, c_E$  don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for  $c_4$

Hebeler, AS (2010)



**all 3- and 4-neutron forces are predicted to N<sup>3</sup>LO!**

# Complete N<sup>3</sup>LO calculation of neutron matter

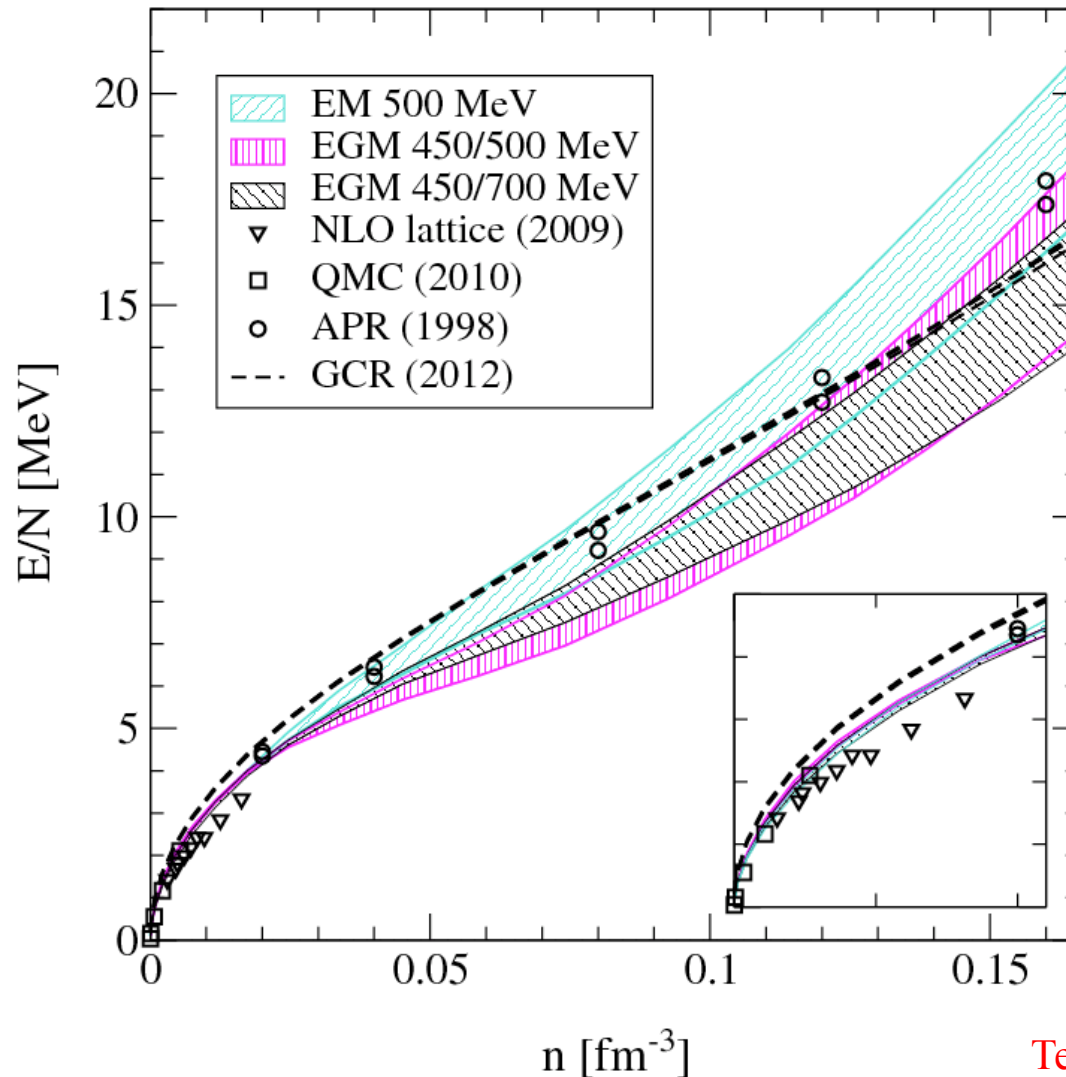


Tews, Krüger, Hebeler, AS (2013).

# Complete $N^3$ LO calculation of neutron matter

first complete  $N^3$ LO result

includes uncertainties from bare NN, 3N, 4N



Tews, Krüger, Hebeler, AS (2013).

# Discovery of the heaviest neutron star

## A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest<sup>1</sup>, T. Pennucci<sup>2</sup>, S. M. Ransom<sup>1</sup>, M. S. E. Roberts<sup>3</sup> & J. W. T. Hessels<sup>4,5</sup>

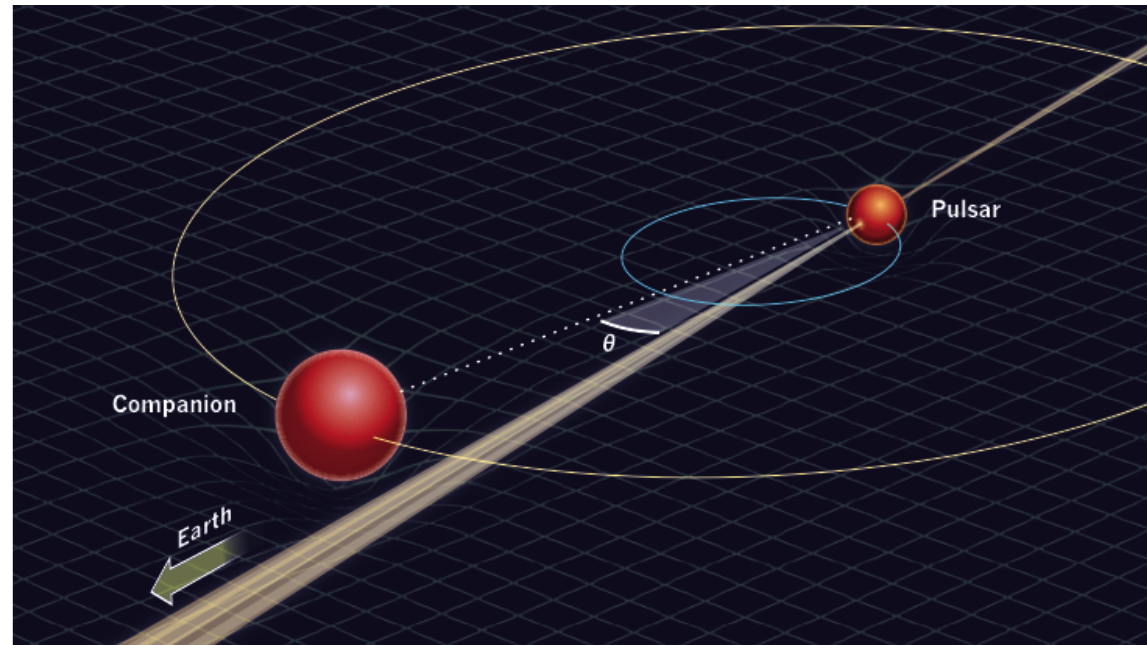
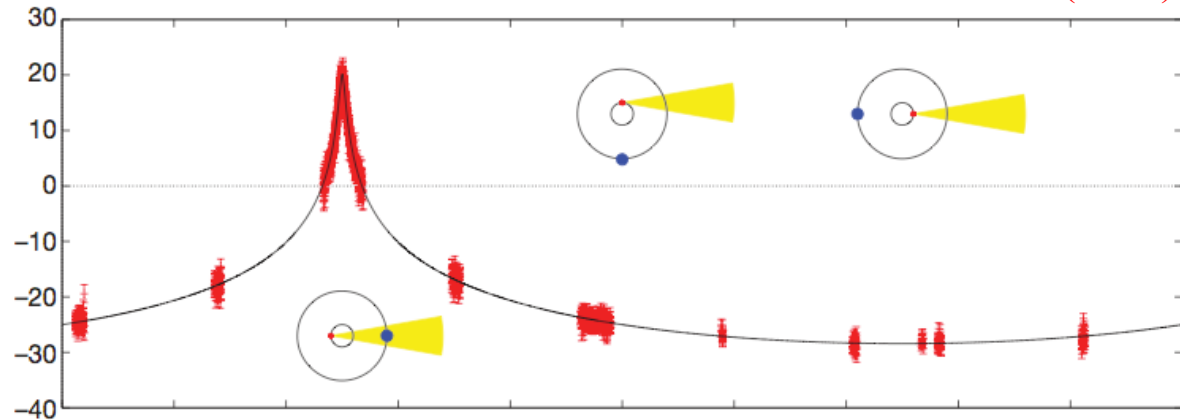
Nature (2010)

direct measurement of  
neutron star mass from  
increase in signal travel  
time near companion

J1614-2230

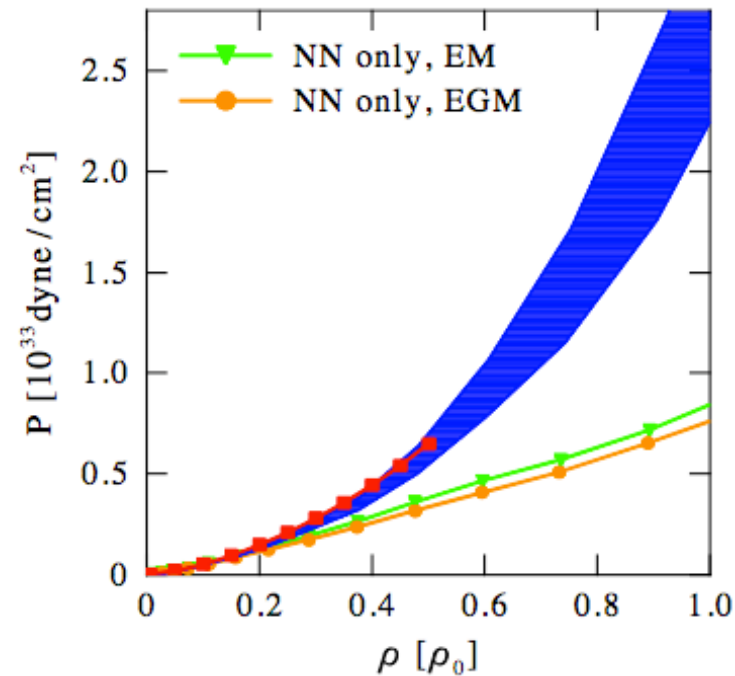
most edge-on binary  
pulsar known ( $89.17^\circ$ )  
+ massive white dwarf  
companion ( $0.5 M_{\text{sun}}$ )

heaviest neutron star  
with  $1.97 \pm 0.04 M_{\text{sun}}$



# Impact on neutron stars Hebeler et al. (2010) and in prep.

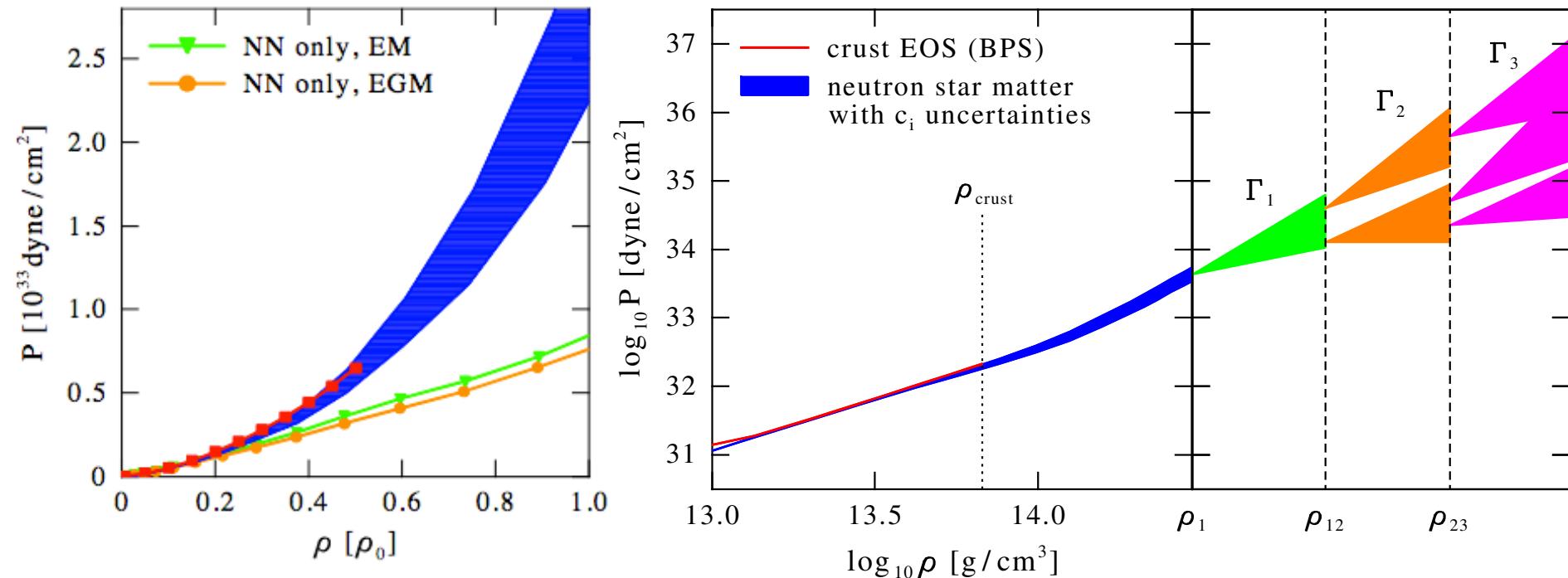
Equation of state/pressure for **neutron-star matter** (includes small  $Y_{e,p}$ )



pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

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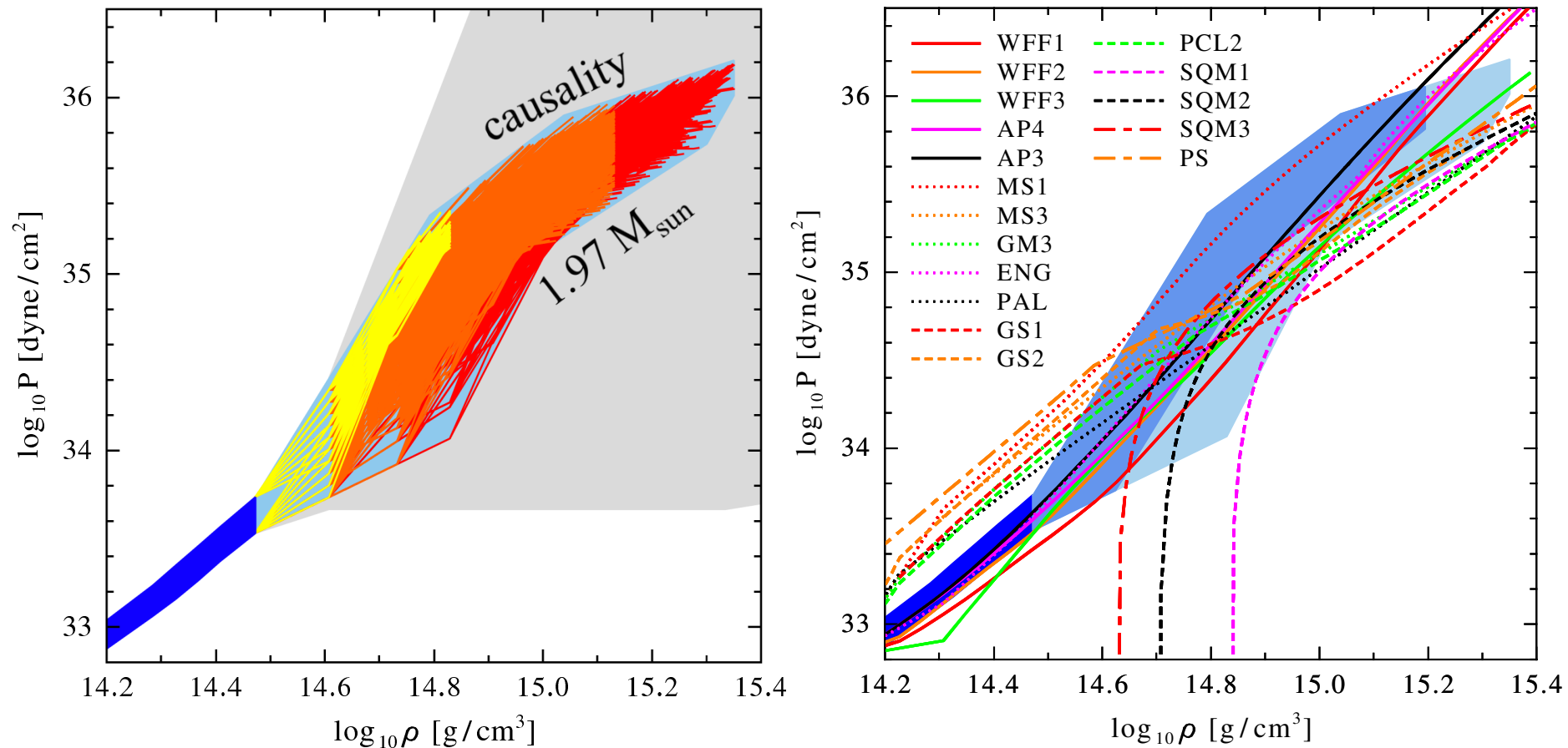
pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

extend uncertainty band to higher densities using piecewise polytropes  
allow for soft regions



# Pressure of neutron star matter

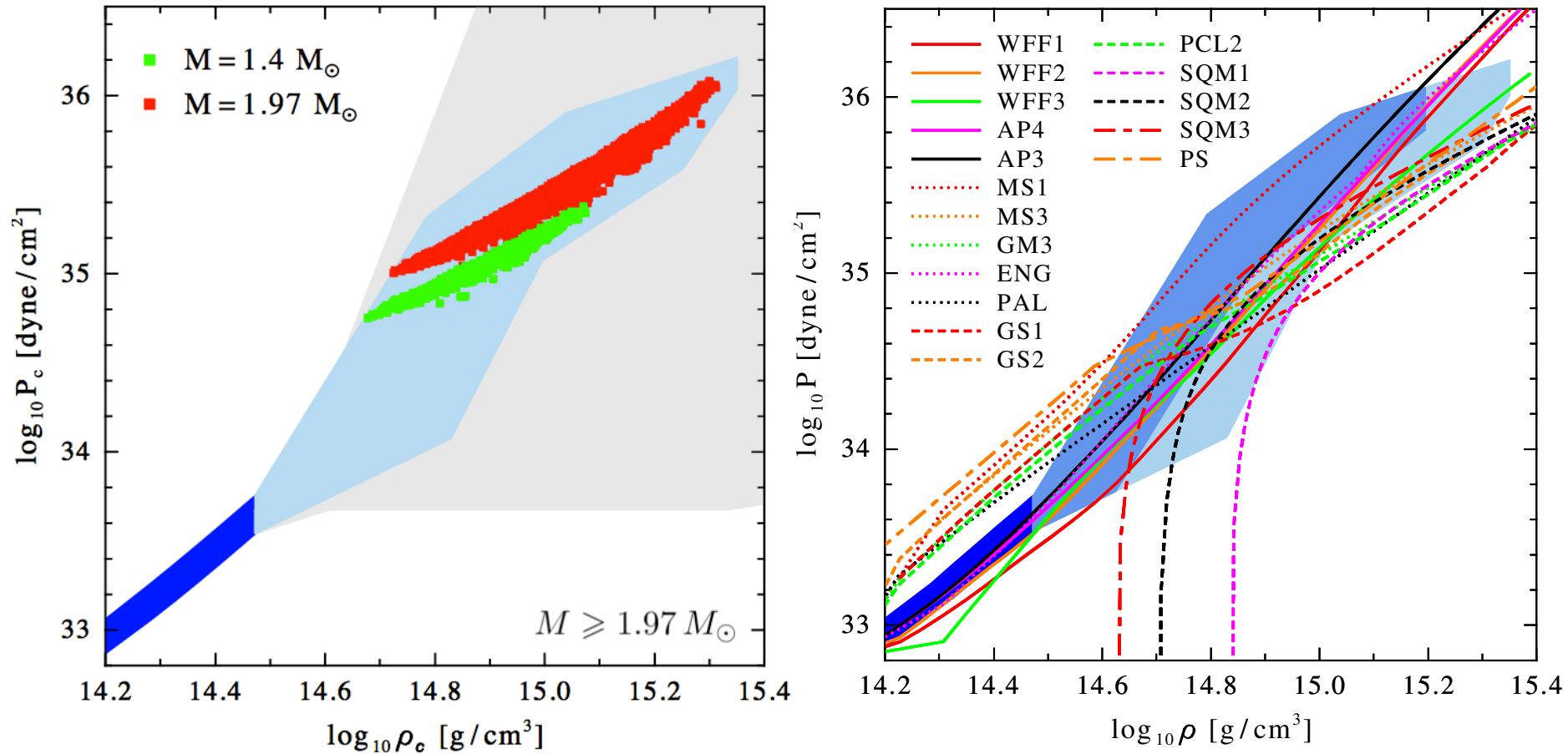
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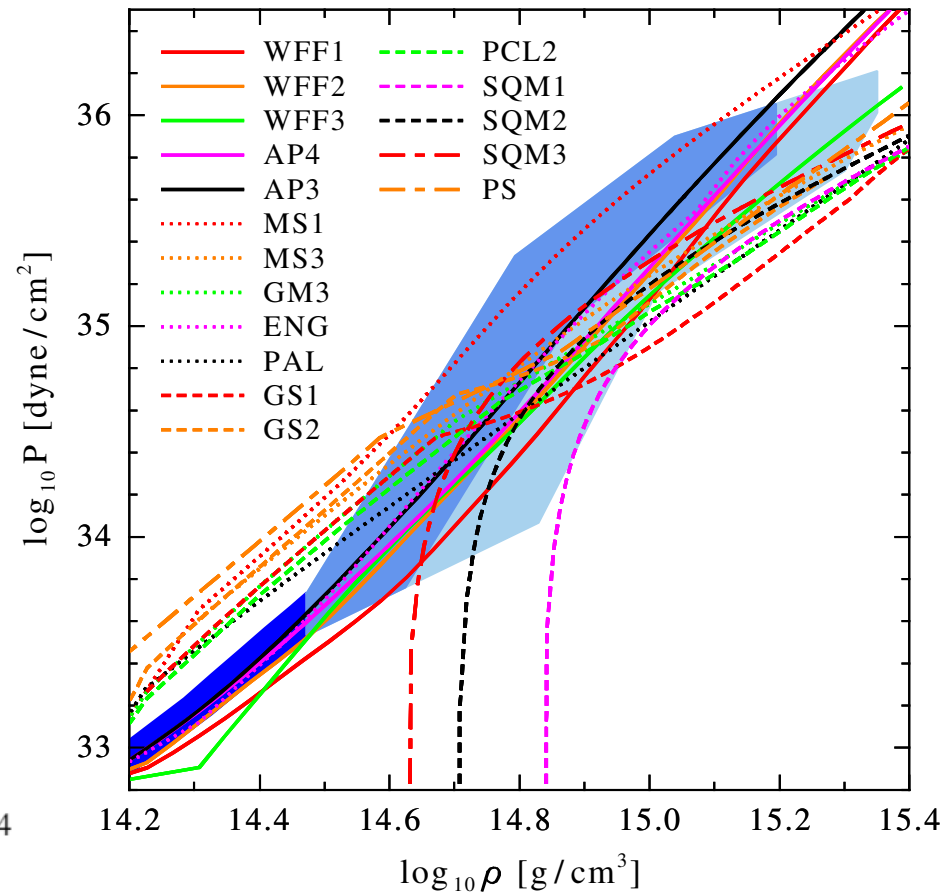
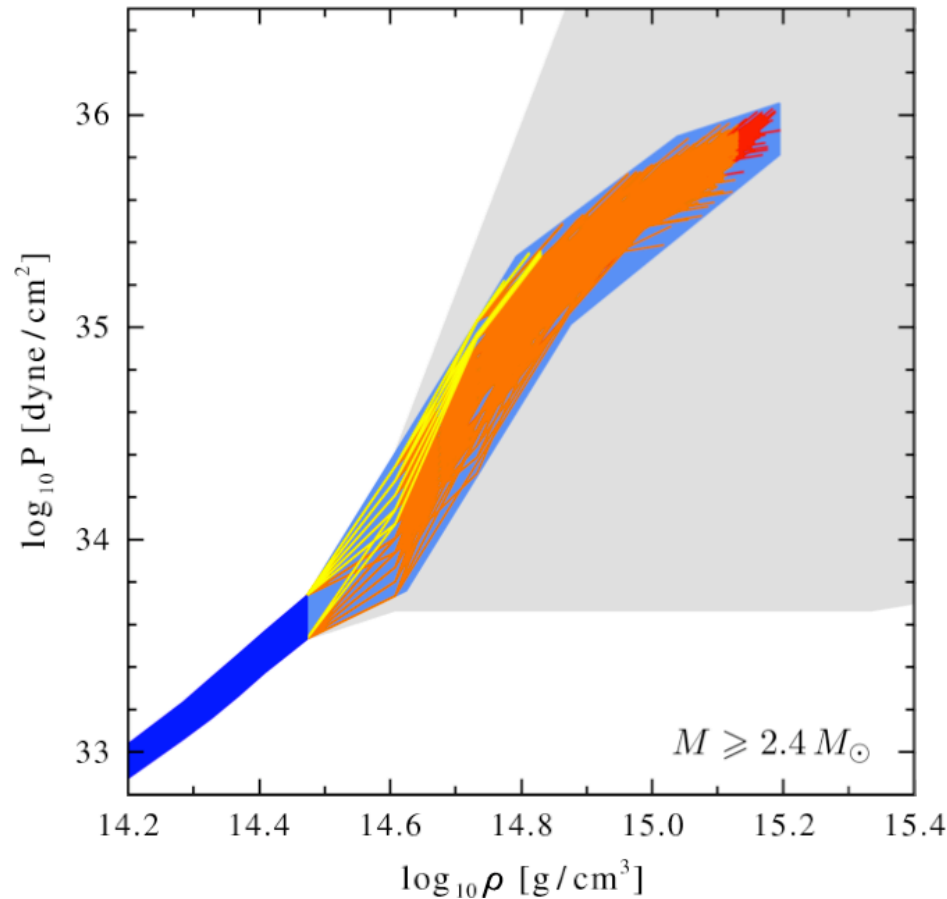


low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

**central densities for  $1.4 M_{\text{sun}}$  star:  $1.7\text{-}4.4 \rho_0$**

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constrain polytropes by causality and require to support  $1.97 M_{\text{sun}}$  star

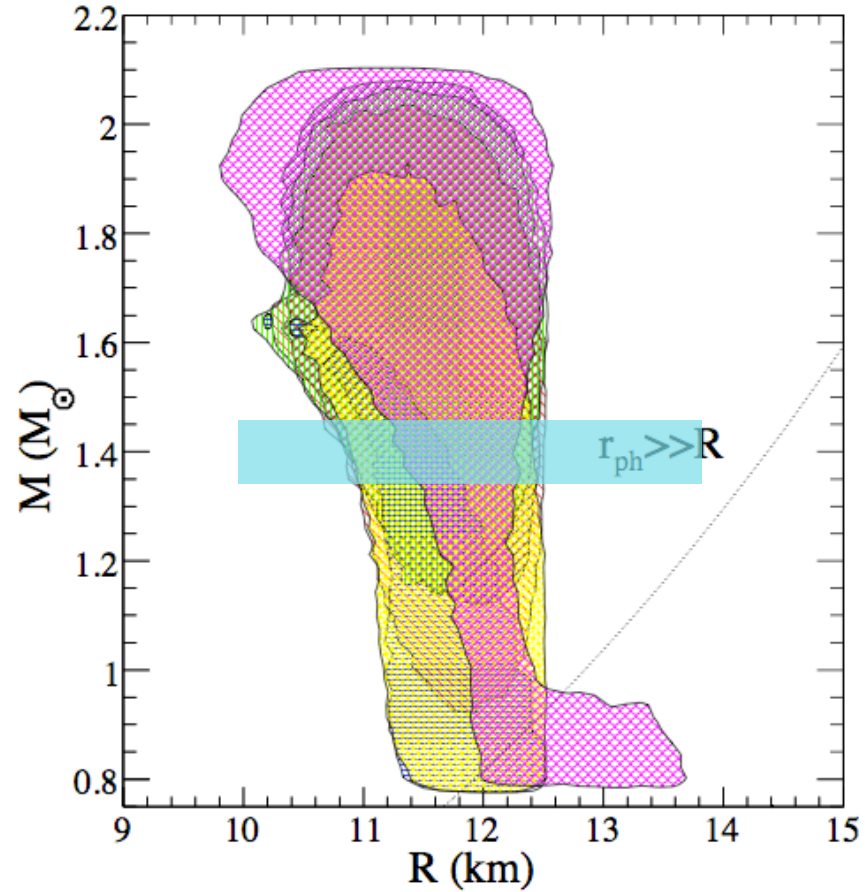
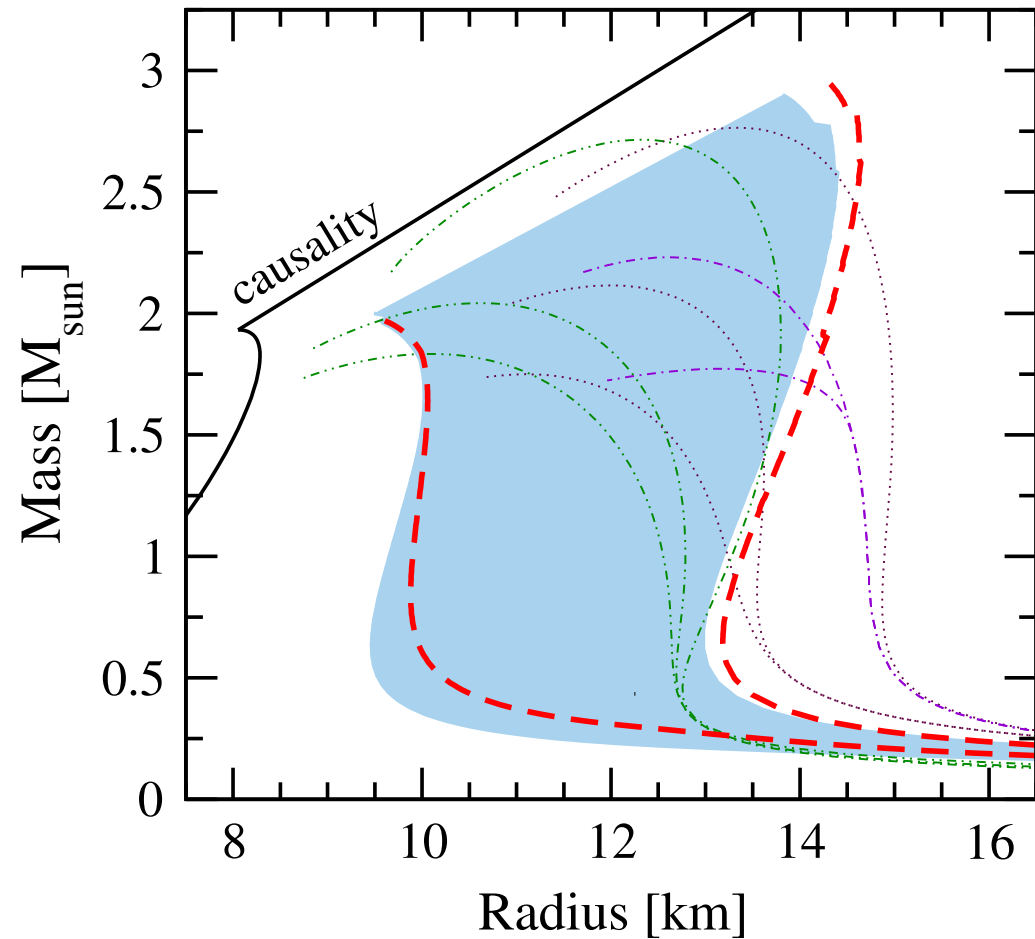


low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

darker blue band for  $2.4 M_{\text{sun}}$  star

# Neutron star radius constraints

uncertainty from many-body forces and general extrapolation



constrains neutron star radius: 9.9-13.8 km for  $M=1.4 M_{\text{sun}}$  ( $\pm 15\%$  !)

consistent with extraction from X-ray burst sources [Steiner et al. \(2010\)](#)

provides important constraints for EOS for core-collapse supernovae

# Neutron-star merger and gravitational waves

explore sensitivity to neutron-rich matter in neutron-star merger and gw signal

Bauswein, Janka (2012) and A. Bauswein et al., arXiv:1204.1888.

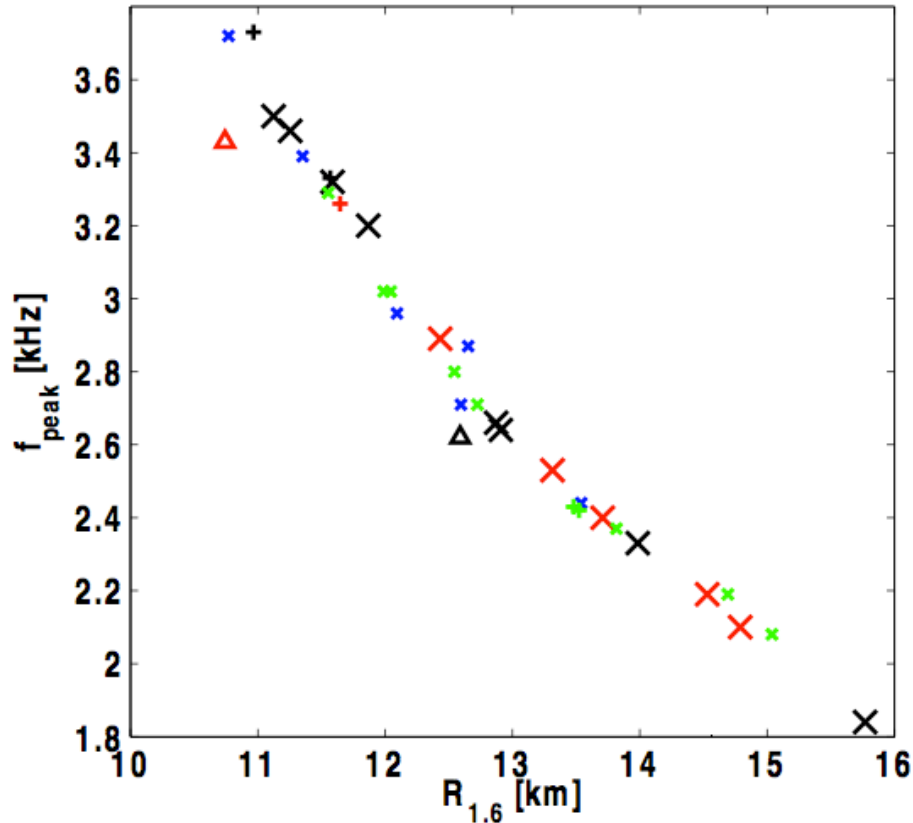
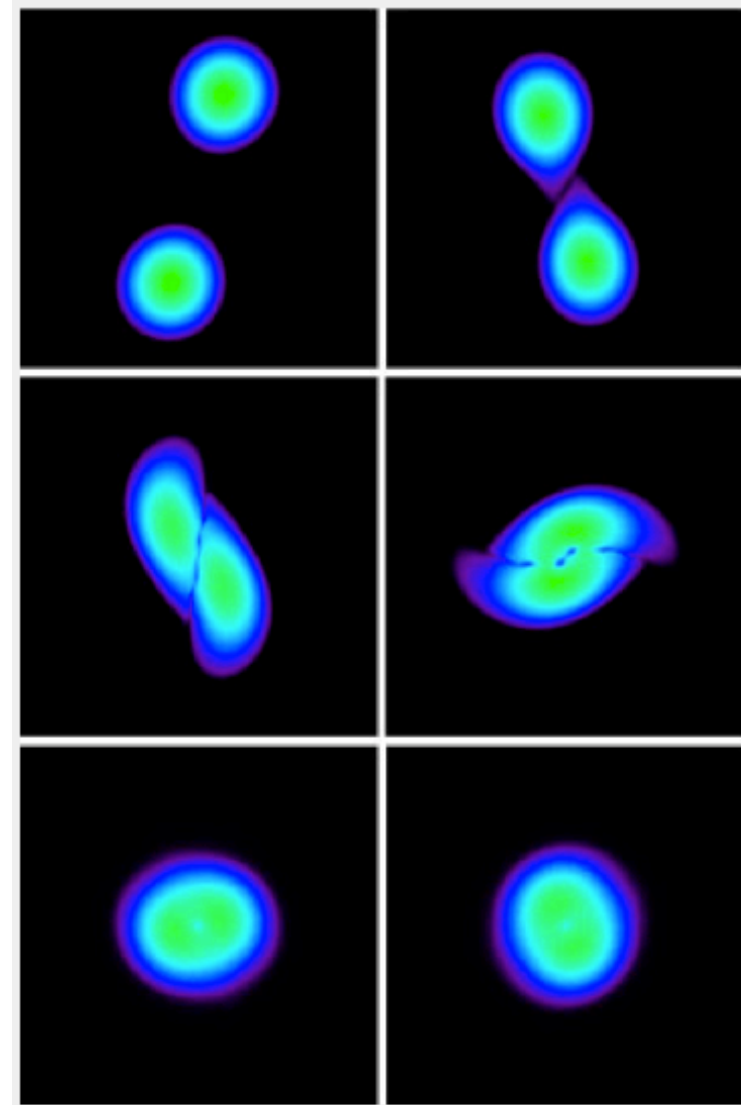


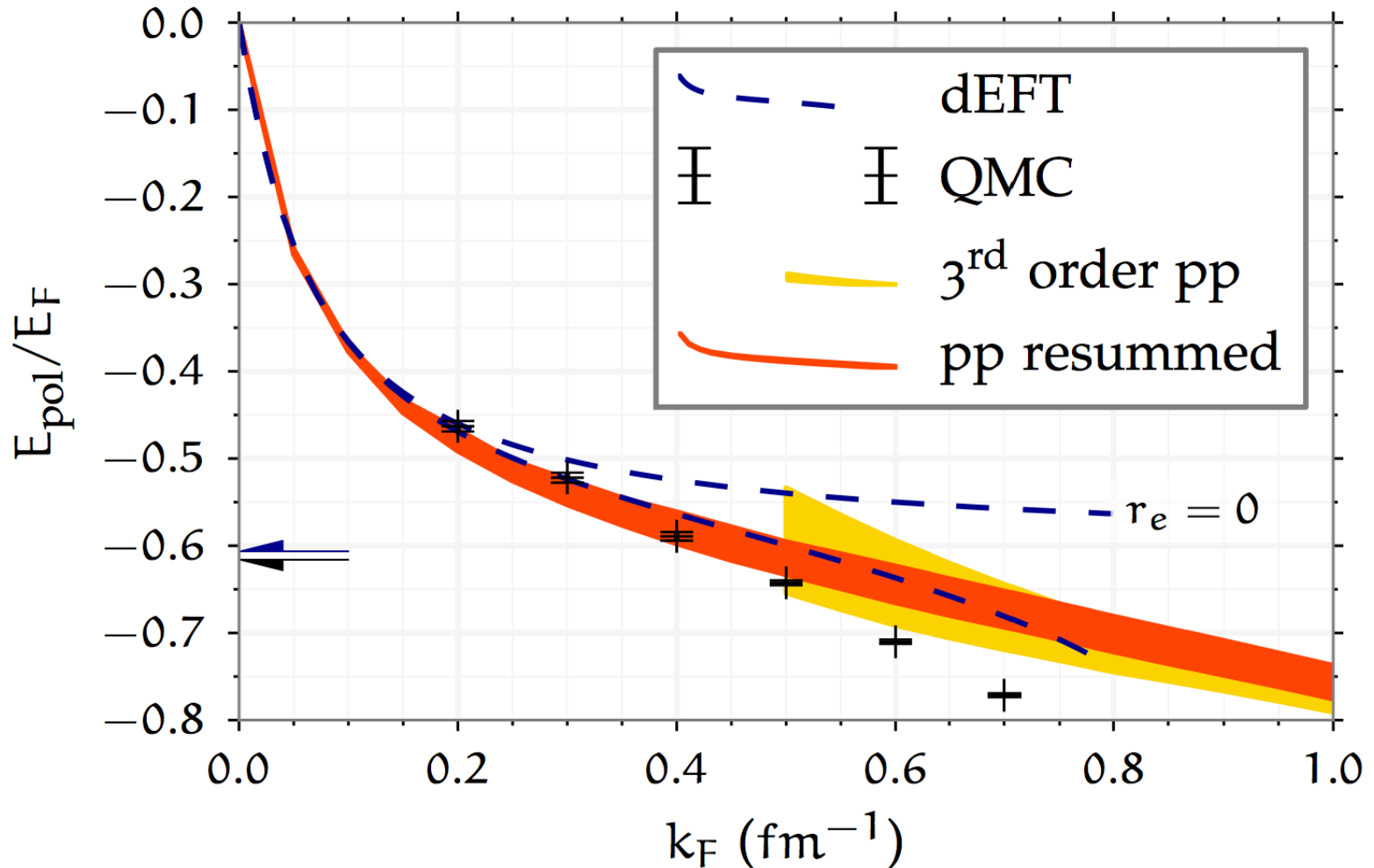
FIG. 10: Peak frequency of the postmerger GW emission versus the radius of a nonrotating NS with  $1.6 M_{\odot}$  for different EoSs. Symbols have the same meaning as in Fig. 8.



**Fig. 1:** Various snapshots of the collision of two neutron stars initially revolving around each other. The sequence simulated by the computer covers only 0.03 seconds. The two stars orbit each other counterclockwise (top left) and quickly come closer (top right). Finally they collide (centre left), merge (centre right), and form a dense, superheavy neutron star (bottom). Strong vibrations of the collision remnant are noticeable as deformations in east-west direction and in north-south direction (bottom panels). (Simulation: Andreas Bauswein and H.-Thomas Janka/MPA)

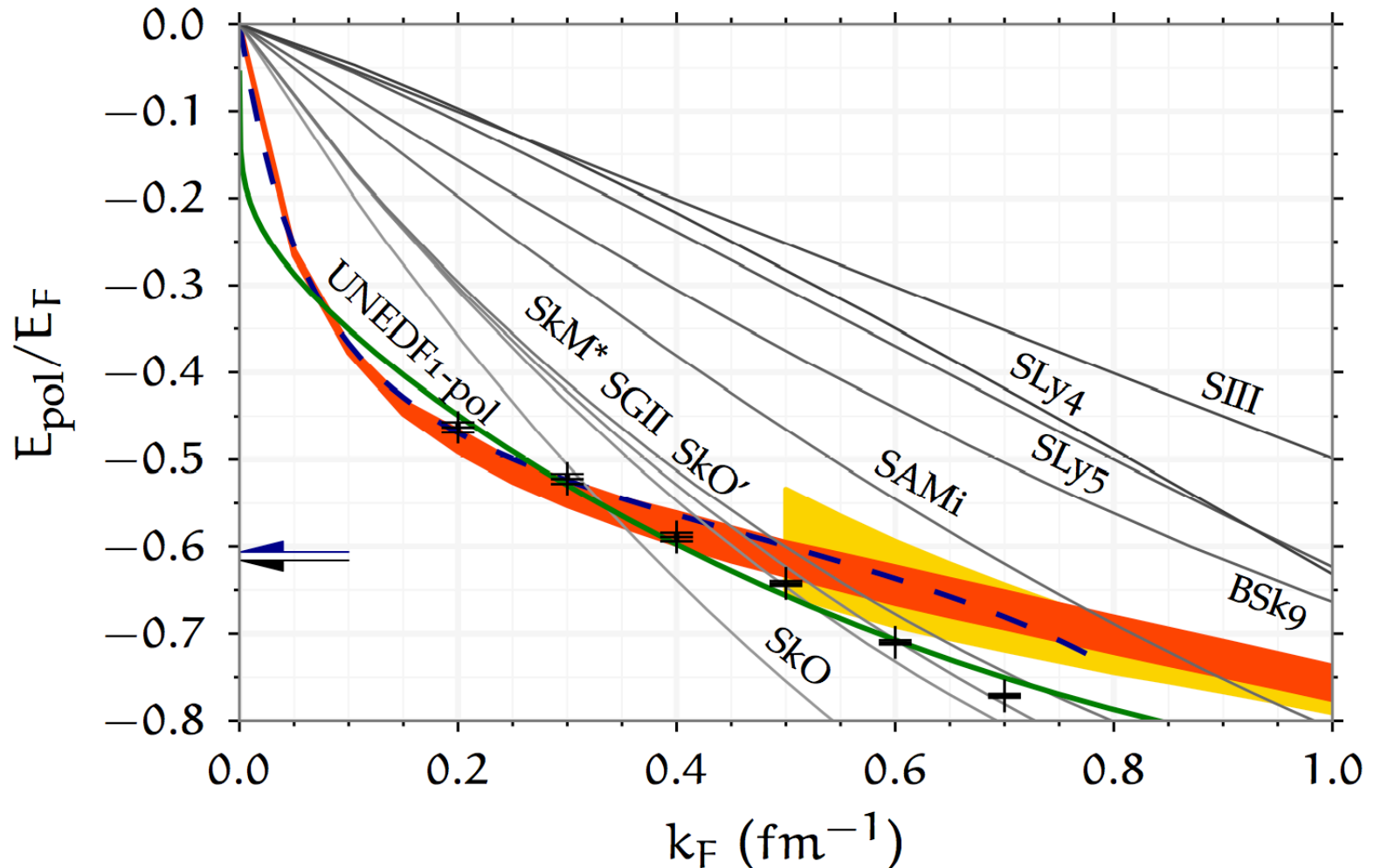
## Neutron polaron

calculated with QMC and effective field theory methods,  
polaron energy increases due to effective range



## Neutron polaron and density functionals

Neutron polaron provides constraints for nuclear density functional, most state-of-the-art functionals underpredict polaron energy



# Summary

Chiral effective field theory interactions provide strong constraints for neutron-rich nuclei/matter, 3N forces are a frontier

key to explain why  $^{24}\text{O}$  is the heaviest oxygen isotope

key for neutron-rich nuclei: Ca isotopes and magic numbers

3N forces are dominant uncertainty of neutron (star) matter below nuclear densities, constrains neutron-star radii and equation of state

neutron polaron constrains nuclear density functional

cold atoms provide anchor points at low densities