

Consistent long-term variation in the hemispheric asymmetry of solar rotation

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Differential rotation and magnetism across the HR diagram

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- Latitudinal differential rotation

$$\Omega = \Omega_0 - B \sin^2 \varphi$$

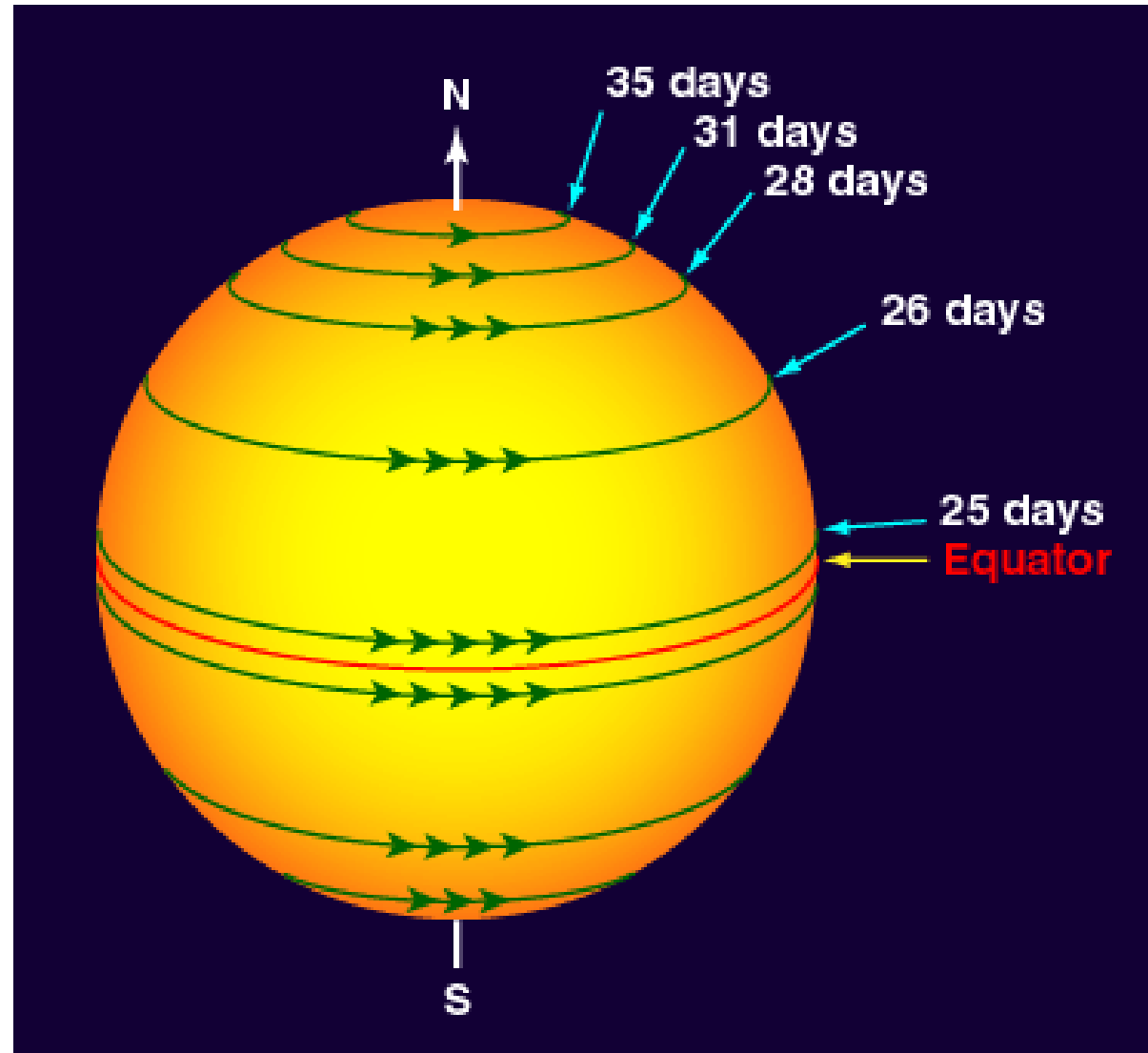
φ Latitude

Ω_0 Velocity of equator

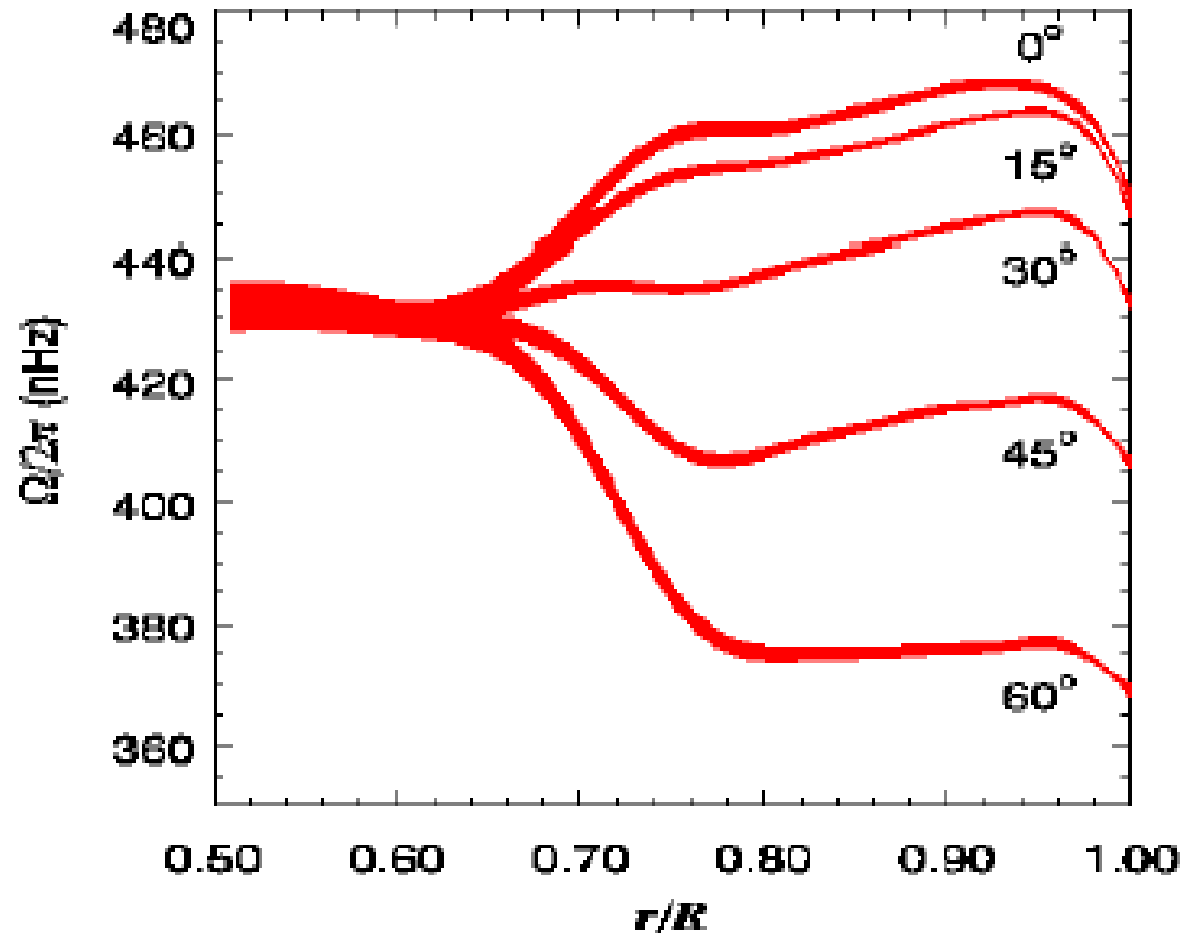
$$B = \Omega_0 - \Omega_{pole}$$

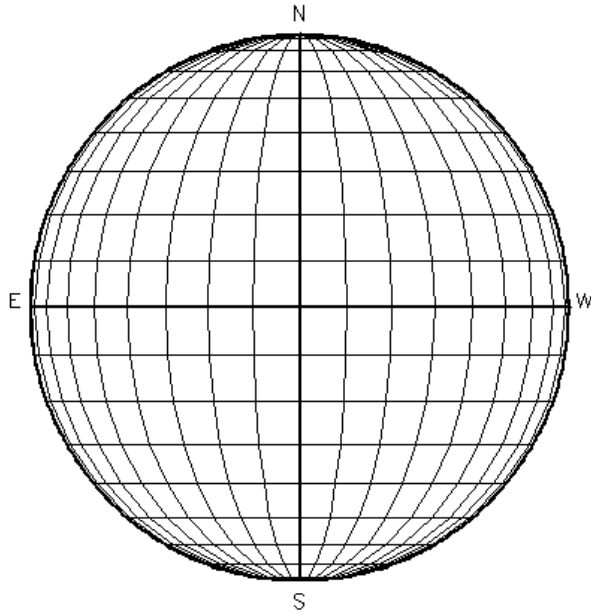
Rotational shear

Ω_0 and B vary with time



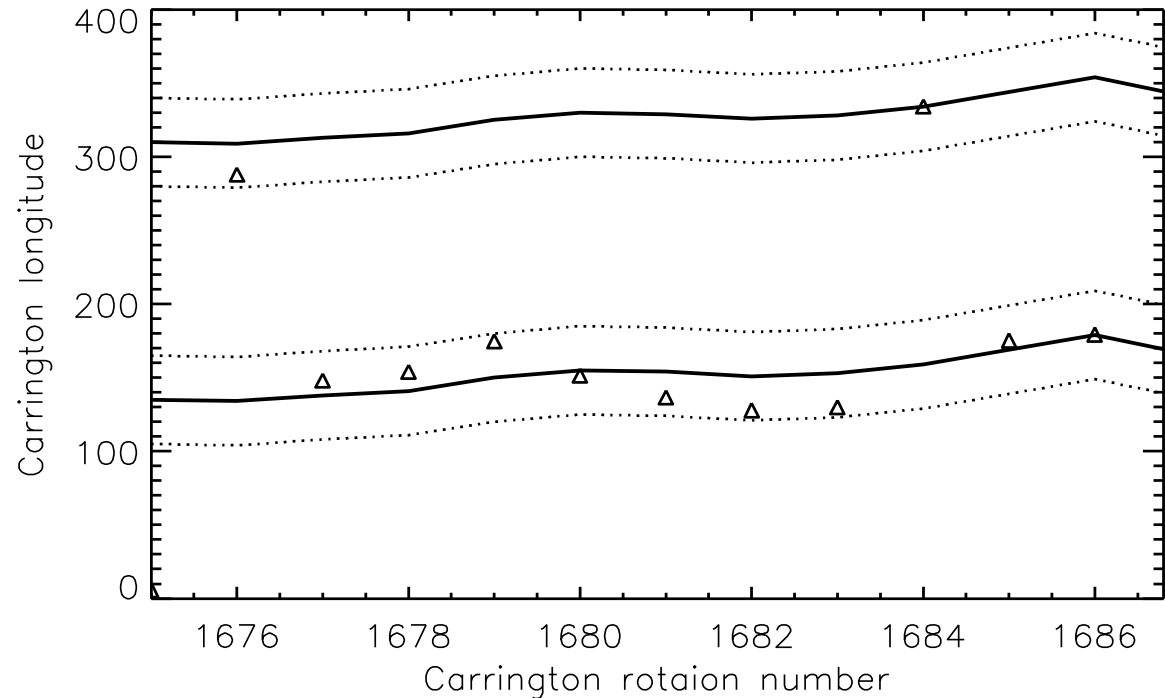
- Radial differential rotation





Carrington longitude
increases East 0 → West 360

$$\Omega_c = 14.18 \text{ deg/day}$$



ALs of X class flares in 1979

Two permanent ALs, 180° apart, were found by many authors, e.g., Usoskin, et al , 2005, A&A, 441, 347; Zhang, et al 2007, A&A, 471, 711

ALs migrate significantly in the Carrington reference frame when the rotation of the Sun deviates much from Ω_c .

- Least-square fitting method

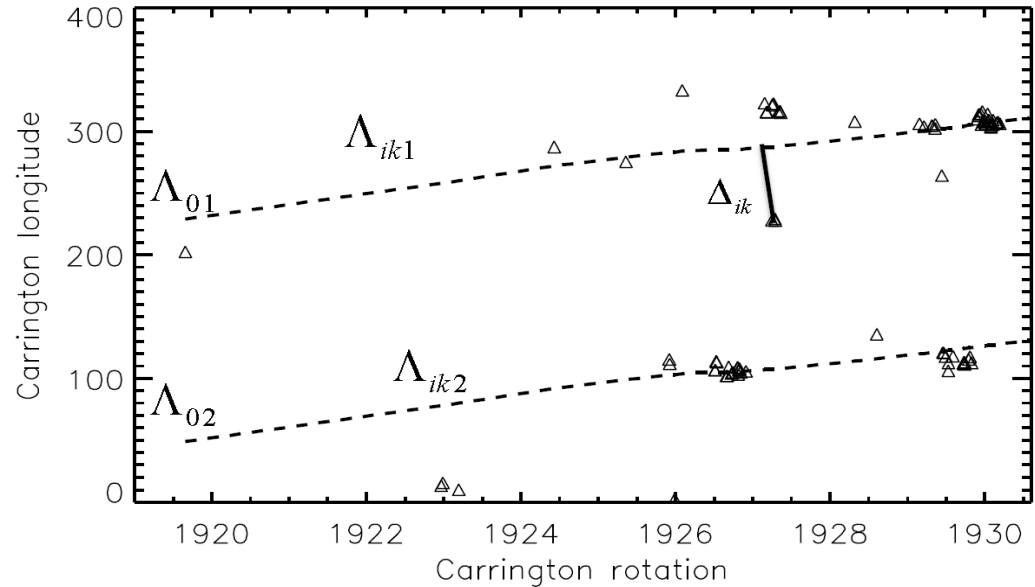
Assuming one AL in the beginning at Carrington longitude Λ_{01} , its rotation rate follows the differential rotation. It will move to Λ_{ik1} on the k th day of the i th rotation.

The other AL migrates to

$$\Lambda_{ik2} = \Lambda_{ik1} \pm 180^\circ$$

$$\varepsilon(\Lambda_{01}, A, B) = \frac{1}{n} \sum_i \sum_k \Delta_{ik}^2 \quad \text{merit function}$$

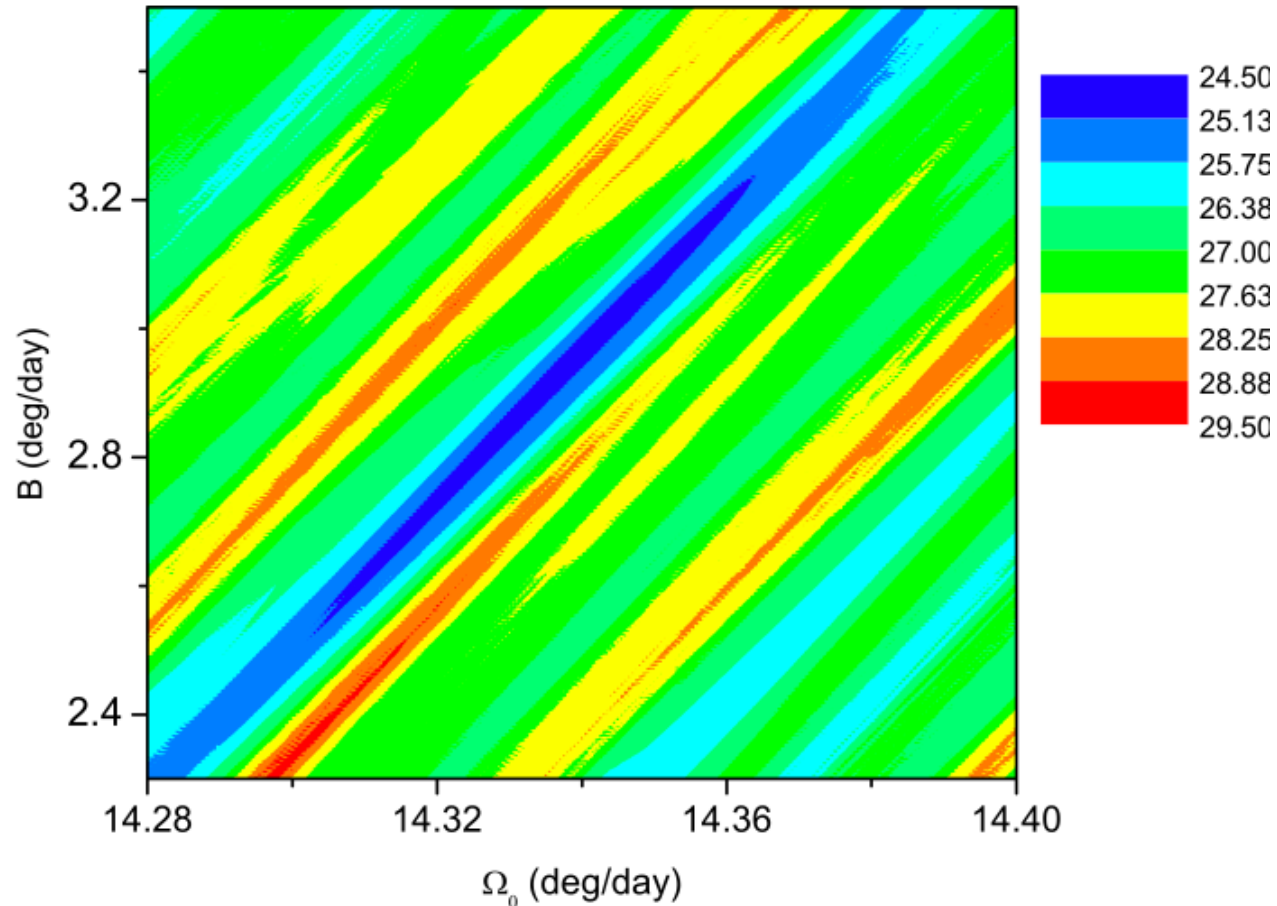
Search for the optimal values of the parameters



$$\Omega_\varphi = \Omega_0 - B \sin^2 \varphi$$

	step
Λ_{01} [0,360] (deg)	1
Ω_0 [13.5, 15.0] (deg/day)	0.001
B [0.0, 5.0] (deg/day)	0.001

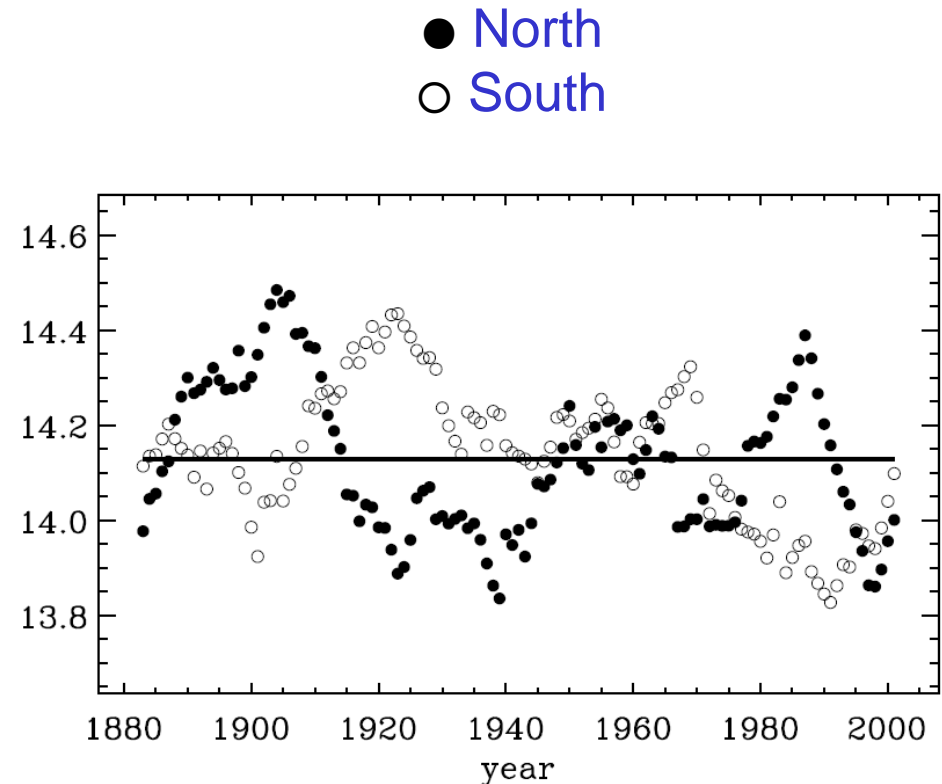
The **best fit values** are found at the center of an elongated area of small values of ε , and **their errors** are given by the horizontal and vertical extent of this area, respectively.



The rotation of sunspot groups in the northern and southern hemispheres at the reference latitude 17° .

The rotation rates vary around the mean by up to (3-4)%.

The two hemispheres show an anti-correlation and both have an 80-90-year quasi-periodicity.



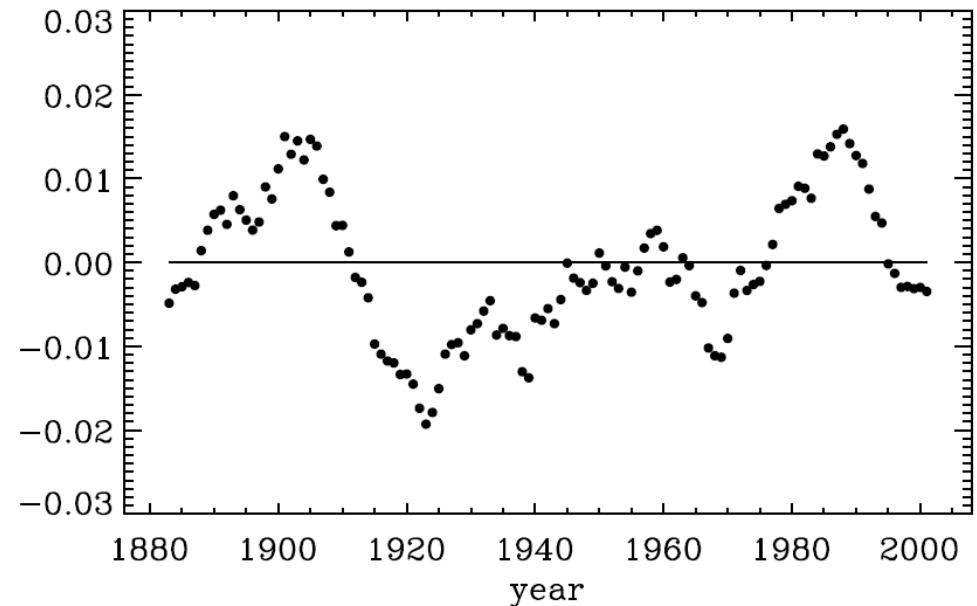
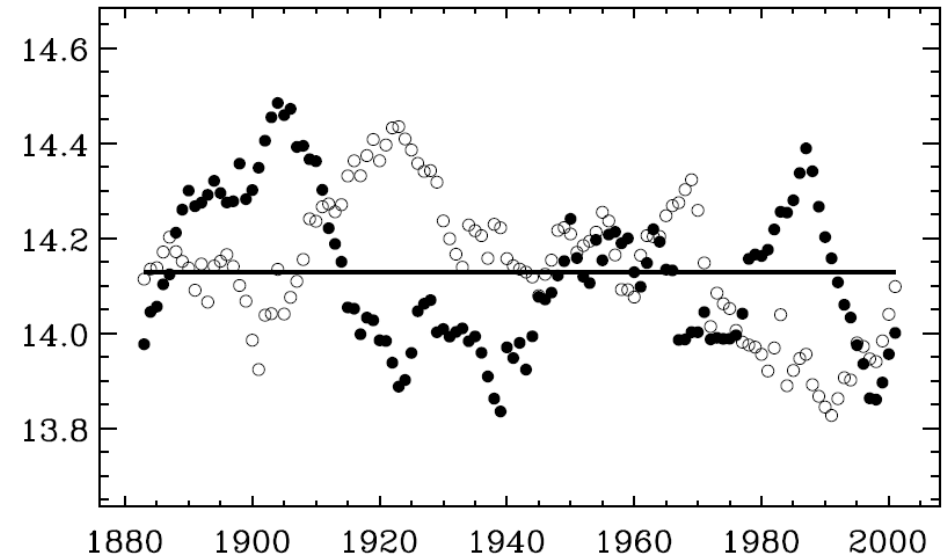
Using 3yr running and 1yr
step forward fit interval

(Zhang et al. A&A 552, A84)

North-south (N-S)
asymmetry:
 $(N - S) / (N + S)$

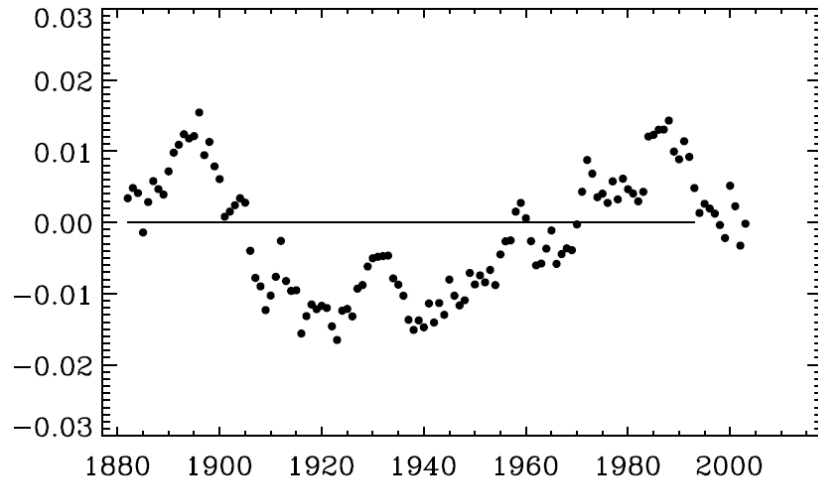
Rotation
● North
○ South

The N-S
asymmetry also
shows a 80-90-year
periodicity. N-S asymmetry
of solar rotation
(deg/day)

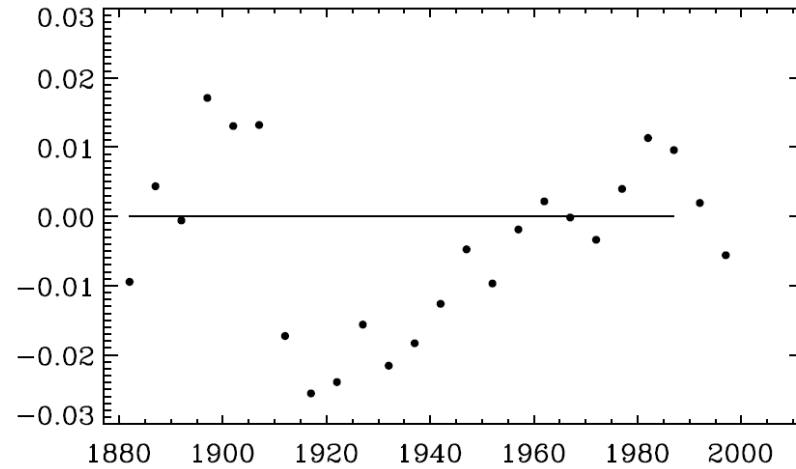


N-S asymmetry of rotation using 4 more fit intervals

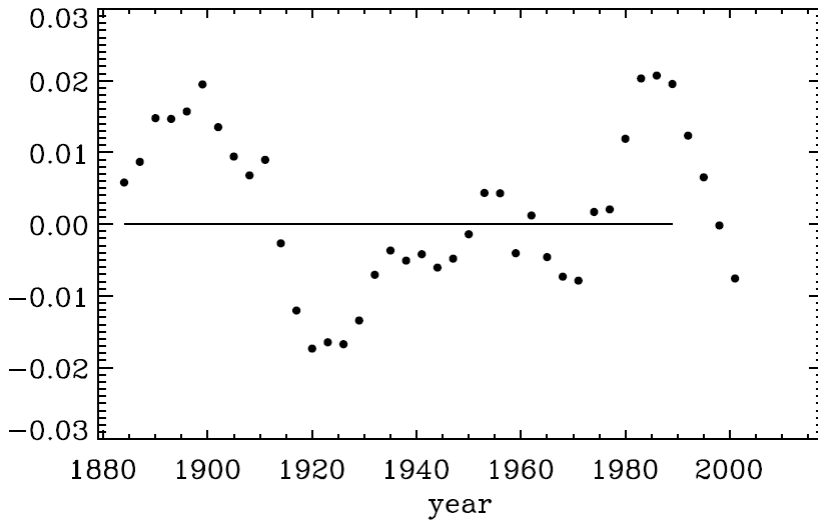
1yr



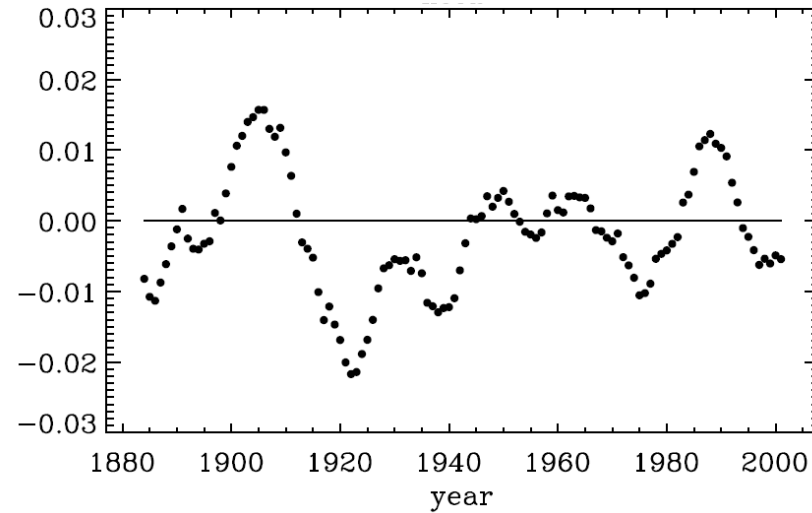
5yr



3yr



5yr running



Using sunspot area as weight in the merit function when searching for best fit parameters.

$$\varepsilon(\Lambda_{01}, A, B) = \frac{1}{n} \sum_i \sum_k W_{ik} \Delta_{ik}^2$$

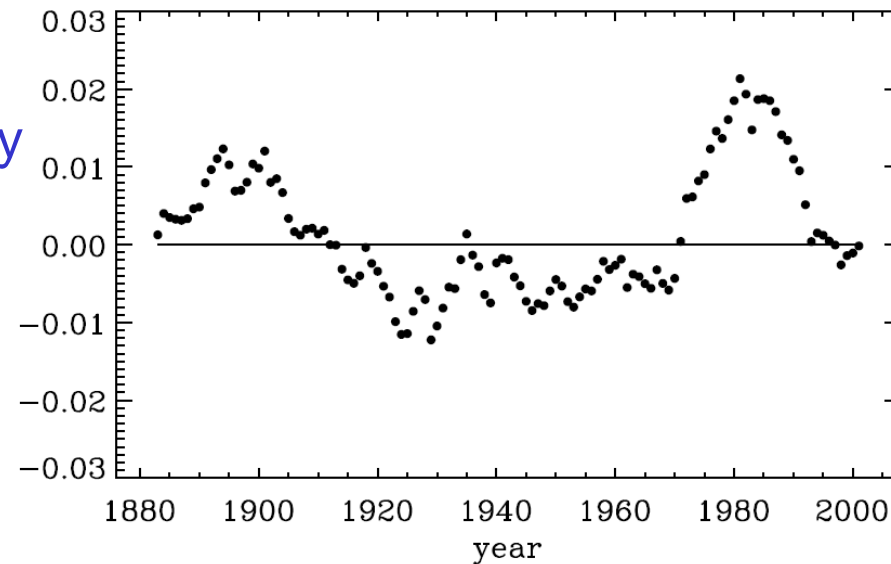
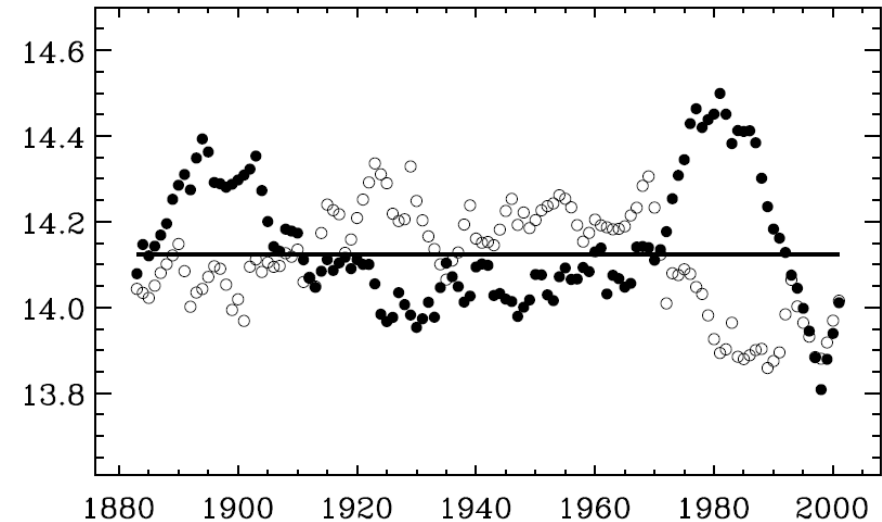
The weighting method also leads to an **anti-correlation** between the two hemispheres.

Rotation

● North

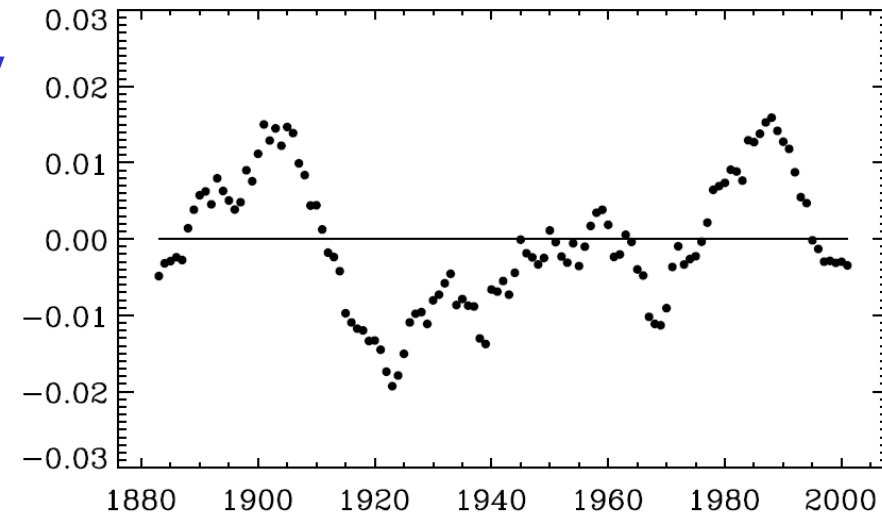
○ South

N-S asymmetry
of rotation
(deg/day)

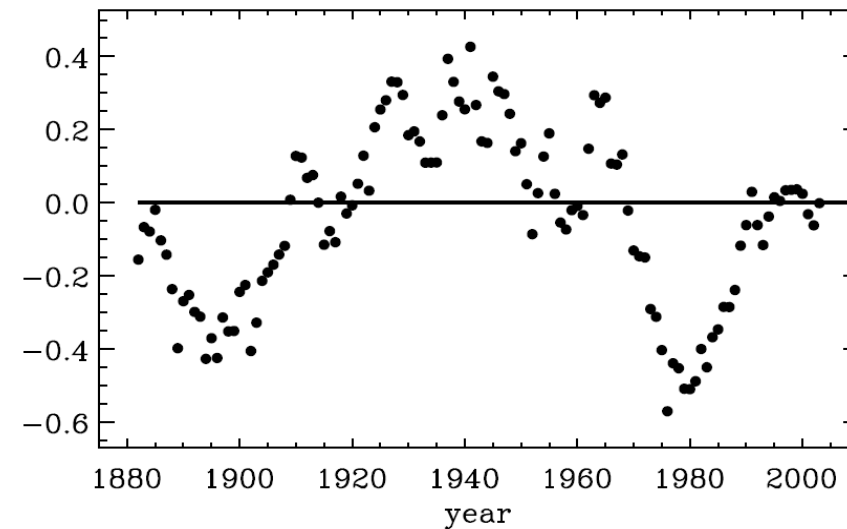


the N-S asymmetry of large sunspots shows a clear **anti-correlation** with the N-S asymmetry of solar surface rotation.
Large sunspots rotate more slowly than small sunspots.

N-S asymmetry of rotation (deg/day)



N-S asymmetry of sunspot area above 2000 μhem



All the results give strong evidence for **the anti-correlation** of the rotation of the two solar hemispheres.

The found long term oscillation of solar rotation suggests that **a systematic interchange of angular momentum** takes place between the two hemispheres at the period of about 80-90 years.