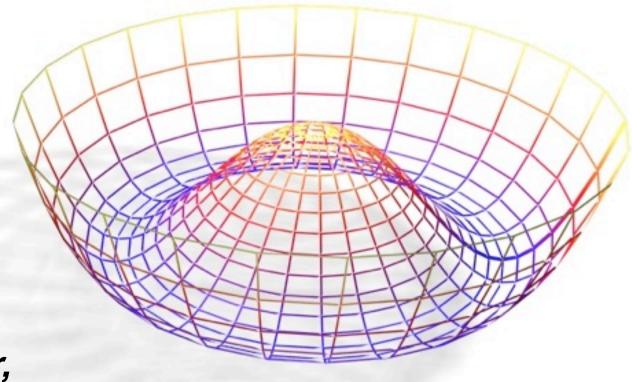


# Presenting LHC Results: A path forward



Kyle Cranmer,

**New York University** 

#### Introduction



#### After campaigning that we publish our likelihood functions

Searches for New Physics: Les Houches Recommendations for the Presentation of LHC Results

```
S. Kraml<sup>1</sup>, B.C. Allanach<sup>2</sup>, M. Mangano<sup>3</sup>, H.B. Prosper<sup>4</sup>, S. Sekmen<sup>3,4</sup> (editors), C. Balazs<sup>5</sup>, A. Barr<sup>6</sup>, P. Bechtle<sup>7</sup>, G. Belanger<sup>8</sup>, A. Belyaev<sup>9,10</sup>, K. Benslama<sup>11</sup>, M. Campanelli<sup>12</sup>, K. Cranmer<sup>13</sup>, A. De Roeck<sup>3</sup>, M.J. Dolan<sup>14</sup>, T. Eifert<sup>15</sup>, J.R. Ellis<sup>16,3</sup>, M. Felcini<sup>17</sup>, B. Fuks<sup>18</sup>, D. Guadagnoli<sup>8,19</sup>, J.F. Gunion<sup>20</sup>, S. Heinemeyer<sup>17</sup>, J. Hewett<sup>15</sup>, A. Ismail<sup>15</sup>, M. Kadastik<sup>21</sup>, M. Krämer<sup>22</sup>, J. Lykken<sup>23</sup> F. Mahmoudi<sup>3,24</sup>, S.P. Martin<sup>25,26,27</sup>, T. Rizzo<sup>15</sup>, T. Robens<sup>28</sup>, M. Tytgat<sup>29</sup>, A. Weiler<sup>30</sup>
```

**Recommendation 3c:** Additionally provide a digitized implementation of the likelihood that is consistent with the mathematical description.

#### I will start with the recommendation document and

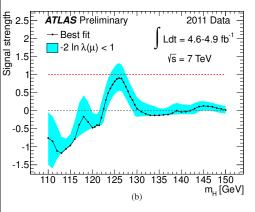
- provide some critical remarks
- discuss some reaction and reality
- outline our progress

Eur. Phys. J. C 72 (2012) [arXiv:1203.2489]

## An important point

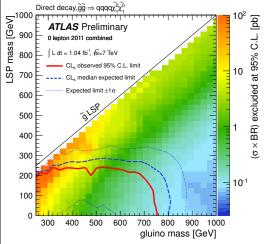


In the request to experiments to publish likelihood functions, we should have been making a fundamental distinction between:



#### 1. Parameters that modify cross sections and branching ratios

- keeping fixed the kinematics, acceptances, shapes
- the parametrization here is not up for debate, it is a simple scaling
- ie. 125 GeV, spin-0, CP-even "Higgs" with generic couplings



#### 2. Parameters that modify kinematics, acceptances, & shapes

- changing these parameters require detector simulation and discrete points and an interpolation algorithm between those points
- this is and will continue to be a controversial issue

I think we have some hope to see 1.

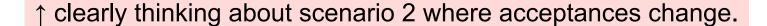
## Example feedback



**Recommendation 3c:** Additionally provide a digitized implementation of the likelihood that is consistent with the mathematical description.



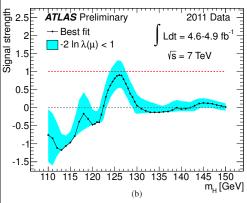
"...For the same reason, we have doubts about providing the final likelihood function (in parameterised or digitised form) - in practice, we have often found it better to follow the approach of giving grids of efficiencies, acceptances and excluded cross-sections over a parameter space of benchmark models (as also advocated in recommendation 4)."

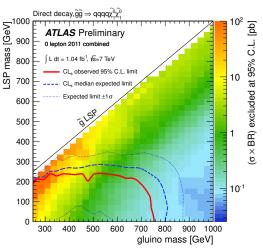


**Recommendation 2b:** Provide and maintain a public simulator developed by the collaboration, or provide official support of an existing one. The public simulator would provide the mapping from the pre-detector data to the post-reconstruction data.

- 2b: We don't think it is practical to provide a 'public simulator' which would provide a significantly more accurate result than that which can be obtained from simple fiducial cuts and efficiency maps / parameterisations.

- Rec 2b: "NO"





## Example feedback



**Recommendation 3a:** Provide all crucial numbers regarding the results of the analysis, preferably in tabulated form in the publication itself. Further relevant information, like fit functions or distributions, should be provided as auxiliary material.

In the case of a single-bin counting experiment these numbers include:

- D the number of observed events in the signal region,
- $\delta S$  the systematic error on the expected number of signal events across the parameter space of the new physics model considered,
- B the background estimate,
- $\delta B$  the estimated background uncertainty,
- $\mathcal{L}$  the integrated luminosity estimate, and
- $\delta \mathcal{L}$  the integrated luminosity uncertainty.

If the background estimate is the result of extrapolating from a control region (e.g, from a side-band) to the signal region, the following should also be provided (perhaps in the auxiliary information):

- ullet Q the observed number of events in the control region
- $\bullet$  Q' the expected number of events in the control region from simulations and its uncertainty
- k the ratio of expected background in the control region to the expected background in the signal region. If the uncertainty  $\delta k$  on k is not negligible, it should also be included.

In the case of a multi-bin analysis, the above numbers should be given for each bin.

**Recommendation 3b:** Provide a mathematical description of the <u>final</u> likelihood function in which experimental data and parameters are clearly distinguished, either in the publication or the auxiliary information.

- Addendum to 3a: "This is too complicated and often will be misinterpreted"
- Rec 3b: "this is hard to do and needs to be discussed"
- "The experiments have problems giving out information that in principle can't be used properly" -Yuri Gershtein (approximate)

#### Marked Poisson Process



**Channel**: a subset of the data defined by some selection requirements.

- eg. all events with 4 electrons with energy > 10 GeV
- n: number of events observed in the channel
- $\nu$ : number of events expected in the channel

Discriminating variable: a property of those events that can be measured and which helps discriminate the signal from background

- eg. the invariant mass of two particles
- f(x): the p.d.f. of the discriminating variable x

$$\mathcal{D} = \{x_1, \dots, x_n\}$$

#### **Marked Poisson Process:**

$$\mathbf{f}(\mathcal{D}|\nu) = \operatorname{Pois}(n|\nu) \prod_{e=1} f(x_e)$$

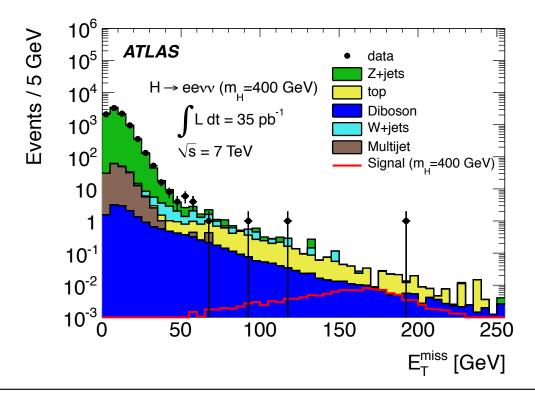
#### Mixture model



**Sample:** a sample of simulated events corresponding to particular type interaction that populates the channel.

• ie. components of a mixture model

$$f(x) = \frac{1}{\nu_{\text{tot}}} \sum_{s \in \text{samples}} \nu_s f_s(x) , \qquad \nu_{\text{tot}} = \sum_{s \in \text{samples}} \nu_s$$



## Parametrizing the model



Parameters of interest: parameters of the theory that modify the rates and shapes of the distributions

- ▶ eg. the unknown mass of the Higgs boson m<sub>H</sub>
- eg. "signal strength"  $\mu$ =0 no signal,  $\mu$ =1 predicted signal rate

Nuisance parameters: parameters associated to uncertainty in:

- systematic uncertainty in the response of the detector
- phenomenological model of interaction in non-perturbative regime

Lead to a parametrized model:  $\nu \to \nu(\alpha), f(x) \to f(x|\alpha)$ 

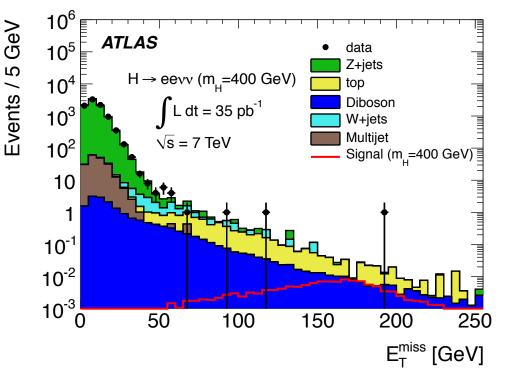
$$\mathbf{f}(\mathcal{D}|\boldsymbol{\alpha}) = \operatorname{Pois}(n|\boldsymbol{\alpha}) \prod_{e=1}^{n} f(x_e|\boldsymbol{\alpha})$$

## Incorporating Systematic Effects



Tabulate effect of individual variations of sources of systematic uncertainty

- typically one at a time evaluated at nominal and "± 1 σ"
- use some form of interpolation to parametrize  $i^{th}$  variation in terms of **nuisance parameter**  $\alpha_i$



	samp 1	samp 2	samp 3	
syst 1				
syst 2				

$$\mathbf{f}(\mathcal{D}|\boldsymbol{\alpha}) = \operatorname{Pois}(n|\boldsymbol{\alpha}) \prod_{e=1}^{n} f(x_e|\boldsymbol{\alpha})$$

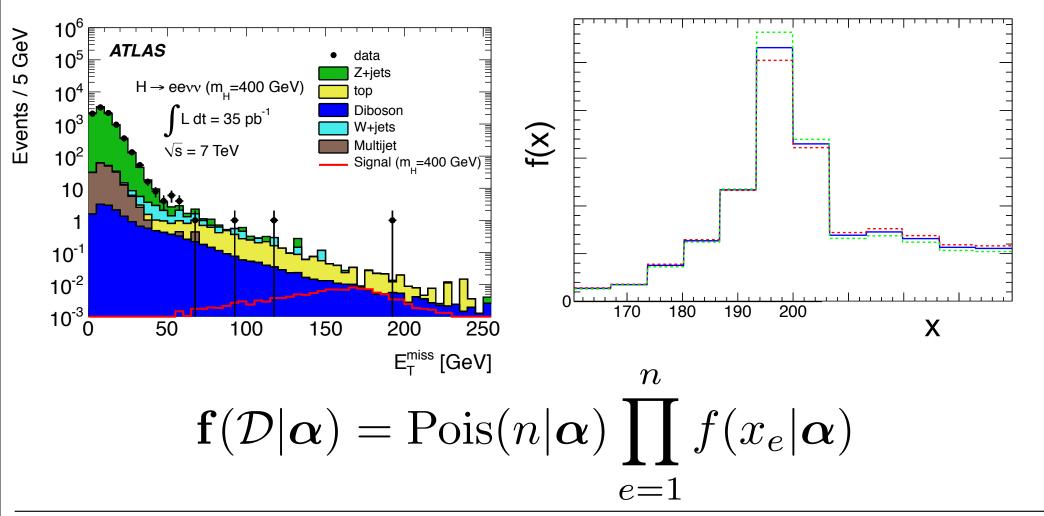
n

## Incorporating Systematic Effects



Tabulate effect of individual variations of sources of systematic uncertainty

- typically one at a time evaluated at nominal and "± 1 σ"
- use some form of interpolation to parametrize  $i^{th}$  variation in terms of **nuisance parameter**  $\alpha_i$

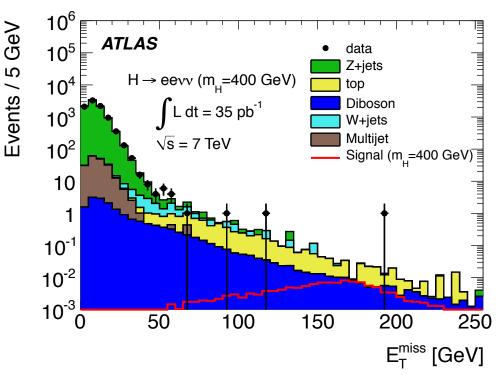


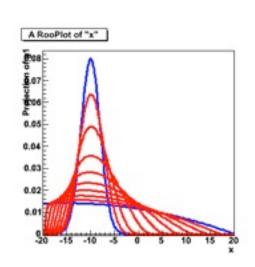
## Incorporating Systematic Effects



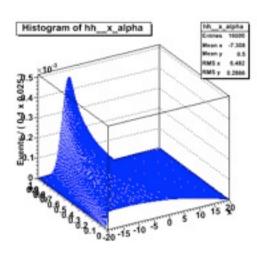
Tabulate effect of individual variations of sources of systematic uncertainty

- typically one at a time evaluated at nominal and "± 1 σ"
- use some form of interpolation to parametrize  $i^{th}$  variation in terms of **nuisance parameter**  $\alpha_i$





n



$$\mathbf{f}(\mathcal{D}|\boldsymbol{\alpha}) = \operatorname{Pois}(n|\boldsymbol{\alpha}) \prod_{e=1}^{n} f(x_e|\boldsymbol{\alpha})$$

#### Simultaneous multi-channel model



Control Regions: Some channels are not populated by signal processes, but are used to constrain the nuisance parameters

Constraint Terms: Often auxiliary measurements for certain nuisance parameters summarized / idealized as

$$f_p(a_p|\alpha_p)$$
 for  $p \in \mathbb{S}$ 

Simultaneous Multi-Channel Model: Several disjoint regions of the data are modeled simultaneously. Identification of common parameters across many channels requires coordination between groups such that meaning of the parameters are really the same.

$$\mathbf{f}_{\text{tot}}(\mathcal{D}_{\text{sim}}, \mathcal{G}|\boldsymbol{\alpha}) = \prod_{c \in \text{channels}} \left[ \text{Pois}(n_c|\nu_c(\boldsymbol{\alpha})) \prod_{e=1}^{n_c} f_c(x_{ce}|\boldsymbol{\alpha}) \right] \cdot \prod_{p \in \mathbb{S}} f_p(a_p|\alpha_p)$$

where

$$\mathcal{D}_{\text{sim}} = \{\mathcal{D}_1, \dots, \mathcal{D}_{c_{\text{max}}}\}$$
  $\mathcal{G} = \{a_p\} \text{ for } p \in \mathbb{S}$ 

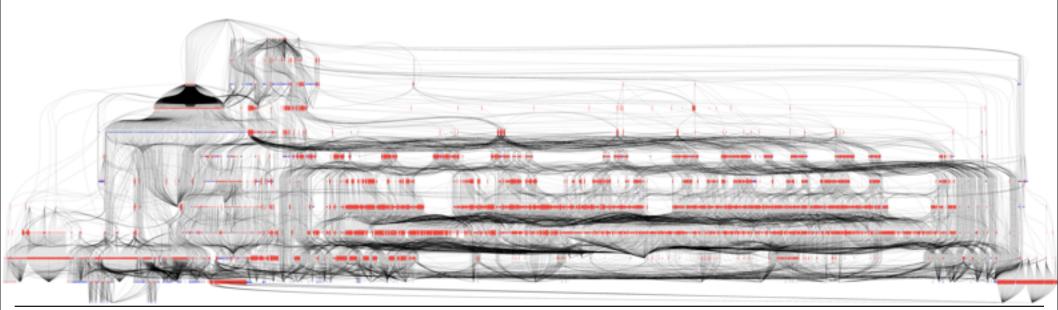
## Visualizing the combined model



**State of the art:** Our most recent combined Higgs search includes 70 disjoint channels and >100 nuisance parameters

 Models for individual channels come from about 12 sub-groups performing dedicated searches for specific Higgs decay modes

$$\mathbf{f}_{\text{tot}}(\mathcal{D}_{\text{sim}}, \mathcal{G} | \boldsymbol{\alpha}) = \prod_{c \in \text{channels}} \left[ \text{Pois}(n_c | \nu_c(\boldsymbol{\alpha})) \prod_{e=1}^{n_c} f_c(x_{ce} | \boldsymbol{\alpha}) \right] \cdot \prod_{p \in \mathbb{S}} f_p(a_p | \alpha_p)$$



## HistFactory XML



## For binned analyses, the HistFactory tool that ships with ROOT solves this problem

- XML files organize the histograms
- conventions define model exactly
- command line tool creates likelihood

$$\mathbf{f}_{\text{tot}}(\mathcal{D}_{\text{sim}}, \mathcal{G}|\boldsymbol{\alpha}) = \prod_{c \in \text{channels}} \left[ \text{Pois}(n_c|\nu_c(\boldsymbol{\alpha})) \prod_{e=1}^{n_c} f_c(x_{ce}|\boldsymbol{\alpha}) \right] \cdot \prod_{p \in \mathbb{S}} f_p(a_p|\alpha_p)$$

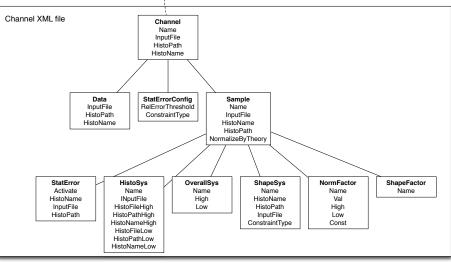
```
Top-level XML file

Combination
OutputFilePrefix

Function
Name
Expression
Dependents

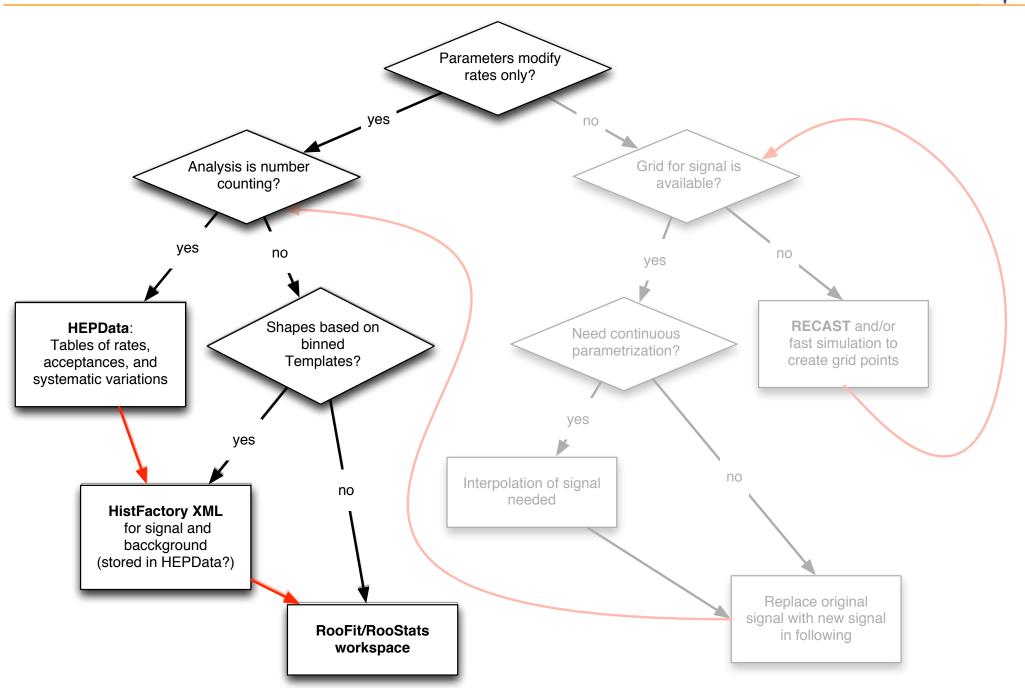
POI

ParamSetting
Val
Const
Type
RelativeUncertainty
```



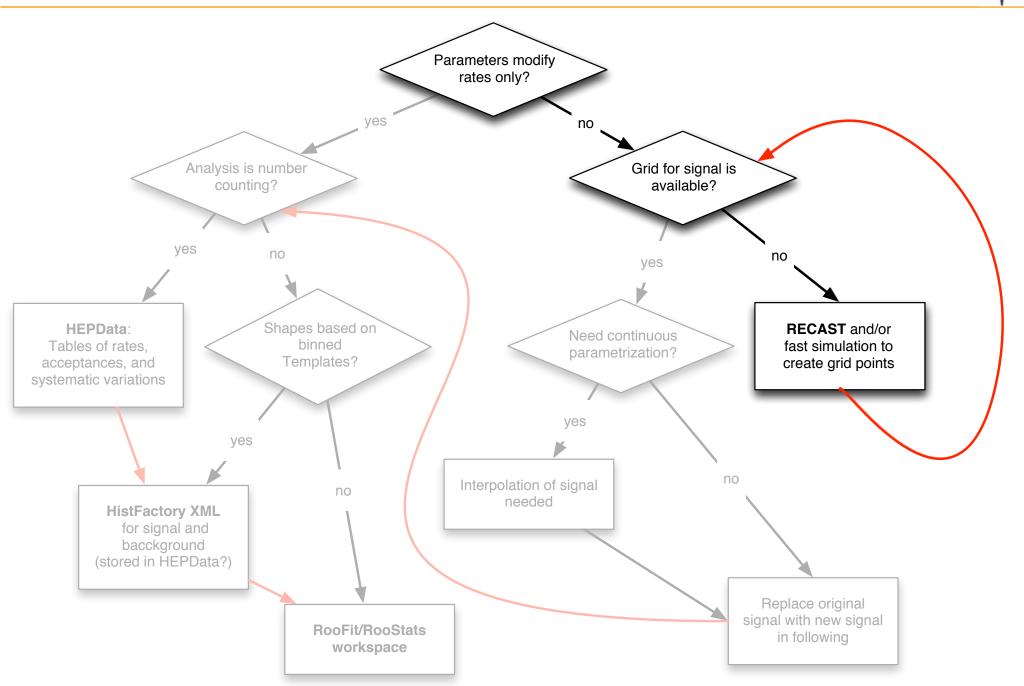
#### A Roadmap





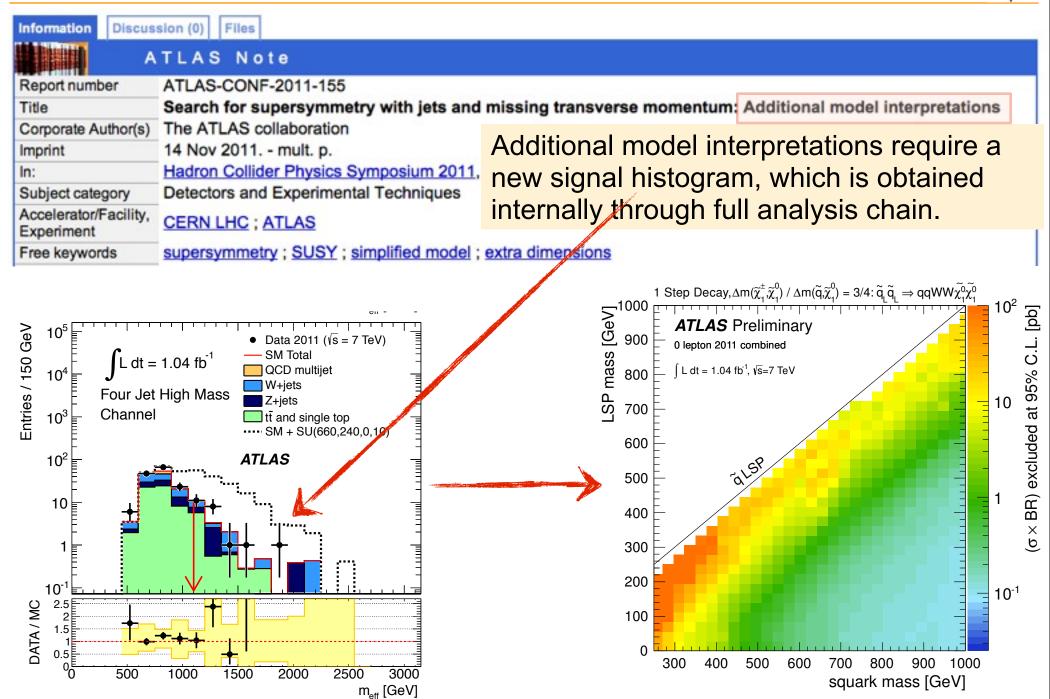
#### A Roadmap





## Analysis re-interpretation: "recasting"

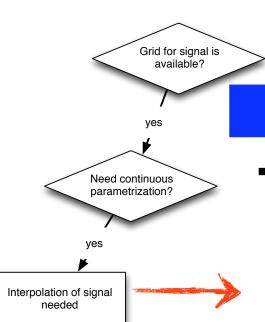




## Interpolating efficiencies in theory parameters

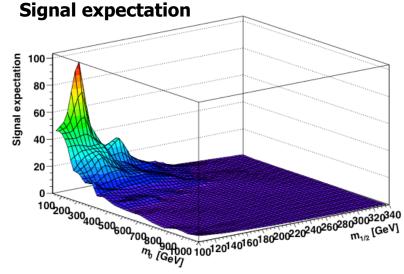


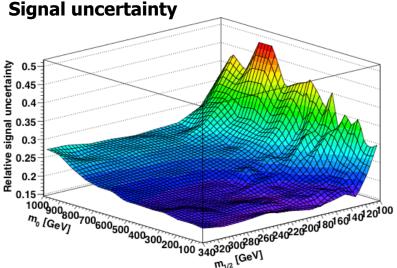
[http://indico.cern.ch/getFile.py/access?contribId=14&resId=0&materiaIId=slides&confId=118137]



## Interpolation examples

- Linear, non-linear, smoothed interpolation?
- Non-trivial with >1 interpolation parameters
- This will make a difference!
- Interpolation in what variable?
  - Signal expectation? Only works if background is constant over the grid.
    - > Selections may change over grid to favor certain decay topologies
  - Likelihood?
- RooFit / RooStats allows for 3-dimensional interpolation
  - Can be extended for N-dim.
  - But: probably don't want simplified models with more than 3 pars.





16

Max Baak (CERN)



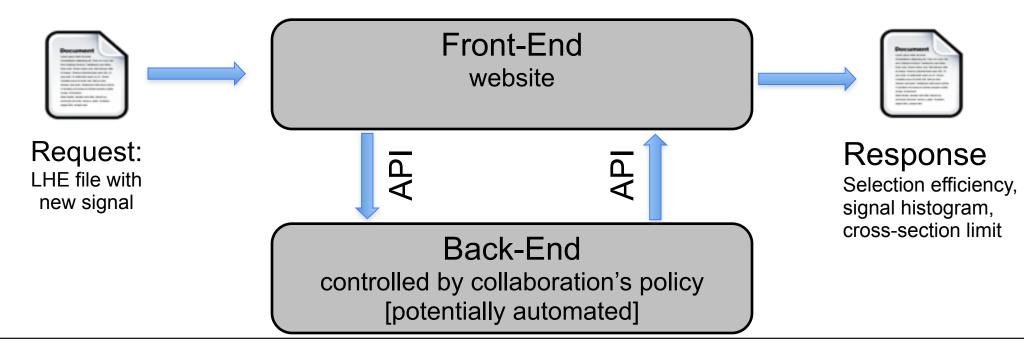


RECAST is a framework for recasting that aims to collect, standardize, and facilitate the processing of recast requests from the community.

- cuts don't change: re-use background estimates and observation from original analysis
- what is needed is to archive the analysis cuts & provide a pipeline for new signal
- data is kept private, still goes through necessary approval process as determined by collaboration, original paper receives citation & recognition (doi's tracked by INSPIRE)

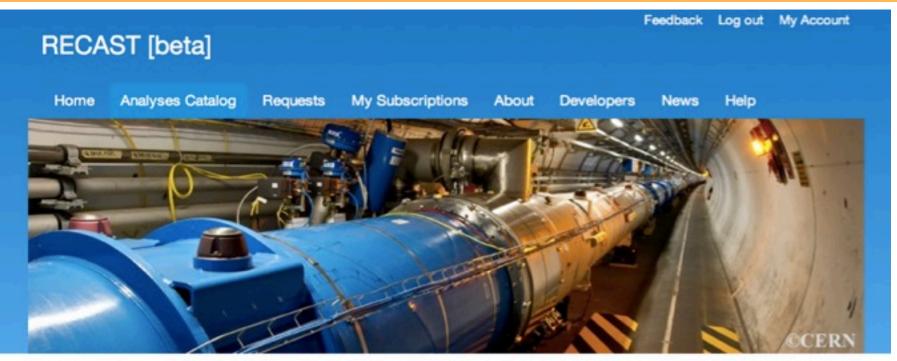
RECAST front-end is a website that collects and organizes the Requests and Responses

- standardizes request & response format, API allows for process to be automated,
- back-end implementation is up to collaboration



## http://recast.perimeterinstitute.ca



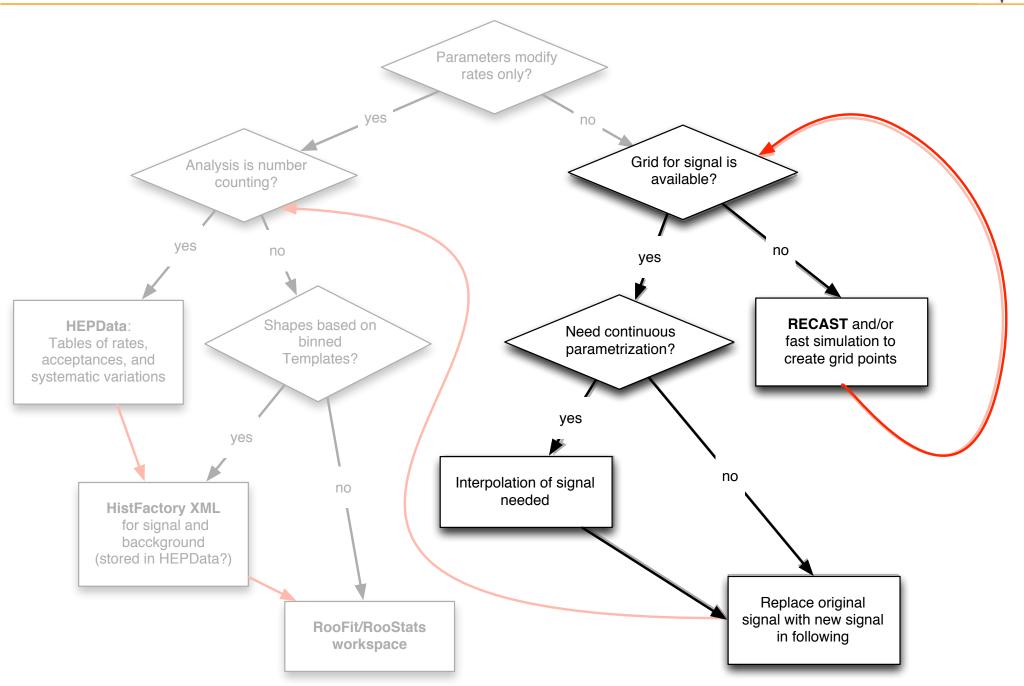


Analysis Catalog New Analysis

Analysis	Collaboration	Subscribers	Requests	Active	Completed	Actions	
Search for Diphoton Events with Large Missing Transverse Momentum in 1 fb^-1 of 7 TeV Proton-Proton Collision Data with the ATLAS Detector	Atlas	1	1	0	1	view   edit   un-subscribe   add request	
Search for New Phenomena in Events with Three or more Charged Leptons	Atlas	0	0	0	0	view   edit   subscribe   add request	
Multileptonic SUSY searches	CMS	2	1	1	0	view   un-subscribe   add request	
Search for Anomalous Production of Multilepton Events and R-Parity-Violating Supersymmetry in √s = 7 TeV	CMS	0	0	0	0	view   subscribe   add request	
Search for a Vector-like Quark with Charge 2/3 in t + Z Events from pp Collisions at sqrt(s) = 7 TeV	CMS	0	0	0	0	view   subscribe   add request	

#### Roadmap

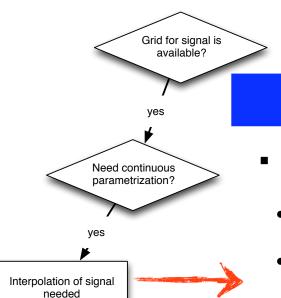




#### Interpolating efficiencies in theory parameters



[http://indico.cern.ch/getFile.py/access?contribId=14&resId=0&materiaIId=slides&confId=118137]



1 Step Decay,  $\Delta m(\widetilde{\chi}_{1}^{\pm}, \widetilde{\chi}_{1}^{0}) / \Delta m(\widetilde{q}, \widetilde{\chi}_{1}^{0}) = 3/4$ :  $\widetilde{q}_{1} \widetilde{q}_{1} \Rightarrow qqWW\widetilde{\chi_{1}^{0}}\widetilde{\chi_{1}^{0}}$ 

ATLAS Preliminary

1000 900

B 700

600

400

300

## Interpolation examples

- Linear, non-linear, smoothed interpolation?
- Non-trivial with >1 interpolation parameters
- This will make a difference!



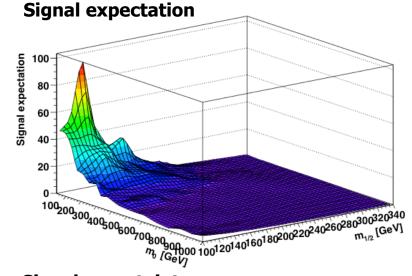
- Signal expectation? Only works if background is constant over the grid.
  - Selections may change over grid to favor certain decay topologies
- Likelihood?

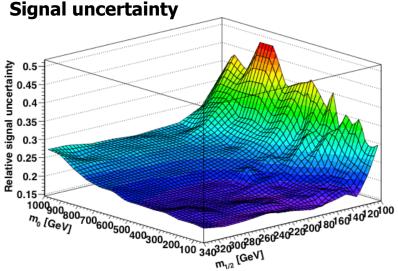
 $(\sigma \times BR)$  excluded at 95% C.L. [pb]

10<sup>-1</sup>

squark mass [GeV]

- RooFit / RooStats allows for 3-dimensional interpolation
  - Can be extended for N-dim.
  - But: probably don't want simplified models with more than 3 pars.





Max Baak (CERN)

Kyle Cranmer (NYU)

500 600

## HistFactory XML



**RECAST** and/or

fast simulation to

create grid points

Grid for signal is

available?

Need continuous

parametrization?

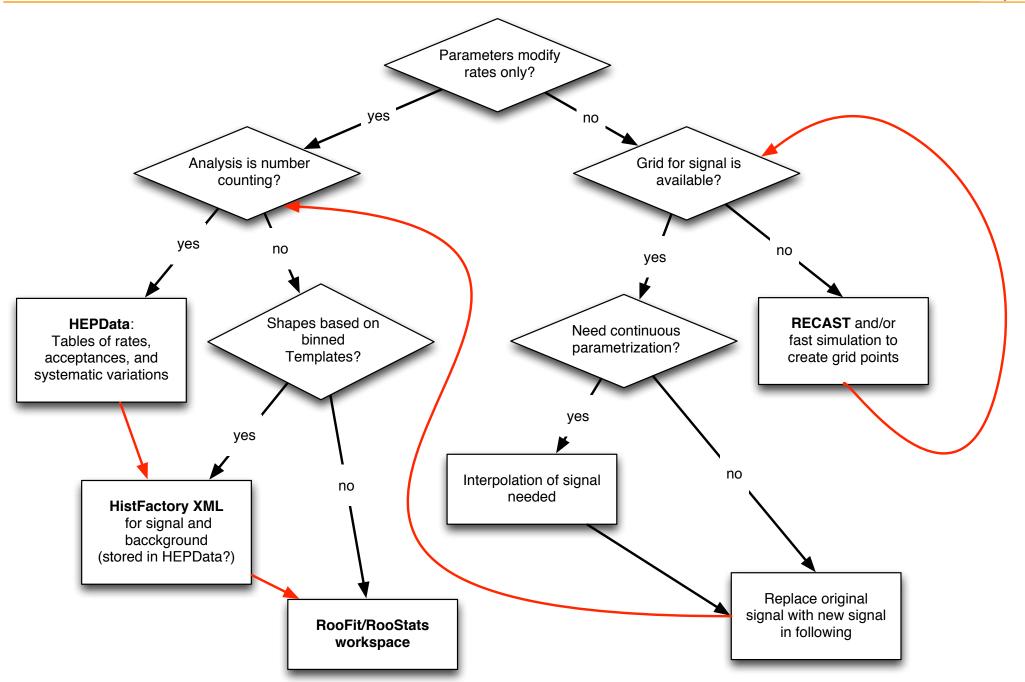
Once one has the histogram for the new signal, a straight forward editing of the XML file will produce a new likelihood with the same background model

- multiple different components for different production modes
- useful for simplified models

```
Interpolation of signal
                                                                                 needed
<!DOCTYPE Channel SYSTEM 'HistFactorySchema.dtd'>
 <Channel Name="A" InputFile="./data/ABCD.root" >
    <Data HistoName="A data" HistoPath="" />
    <!-- This is the signal (eg. mu)-->
                                                                                                             Replace original
    <Sample Name="A_signal" HistoPath="" HistoName="unit_histogram"</pre>
                                                                                                           signal with new signal
                                                                                                              in following
      <!-- now mu is number of events-->
      <NormFactor Name="mu" Val="1" Low="0" High="200" />
      <OverallSys Name="syst1" High="1.01" Low="0.99" />
    </Sample>
    <!-- This bkg is estimated from MC (eg. mu_A^K) -->
    <Sample Name="A_backgroundMC" HistoPath="" NormalizeByTheory="True" HistoName="unit_histogram" >
      <NormFactor Name="mu_K_A" Val="100" Low="0" High="200" />
    </Sample>
    <!-- Background 2 is completely Data-Driven -->
    <Sample Name="A_backgroundDD" HistoPath="" NormalizeByTheory="False" HistoName="unit_histogram" >
      <NormFactor Name="mu_D_U" Val="100" Low="24500" High="26000" />
      <NormFactor Name="etaB" Val="1" Low="0." High="0.02" Const="False" />
      <NormFactor Name="etaC" Val="1" Low="0." High="0.3" Const="False" />
      <!-- NormFactor and ShapeFactor same for a 1-bin histogram. But we can name NormFactor-->
    </Sample>
 </Channel>
```

#### Roadmap





## Comments on Rivet & HiggsBounds



Rivet: Some analyses are being incorporated into Rivet.

- generally background subtracted and unfolded to particle-level
- primarily used for MC tunings

In that sense RECAST is complementary

- the detector simulation performs folding
  - as is done by current "additional model interpretations" documents
- primarily aimed at searches

One could imagine some interaction between the projects

**HiggsBounds:** HiggsBounds does aim to reinterpret existing constraints in the context of different Higgs sectors. Doing the best with what's available

- but not "arbitrary" Higgs sectors! It can only constrain model that has topologies that have explicitly searched for by experiments
- it is based on the topology with the strongest expected limit.
  - once there are several decay modes, this approach quickly looses power

to combine different searches need likelihoods.

#### Interaction with INSPIRE & HEPData



**INSPIRE**: Advanced discussions regarding the interaction of RECAST and INSPIRE.

- New responses get DOI number from CERN, are aggregated with original collaboration publication. New responses are citable objects, and increment citation of original paper
- New requests (from theorists) get their own DOI number, so theorist can put out paper pointing to their request independently of a collaboration response

**HEPData**: Signal histograms from the new model could go into HEPData.

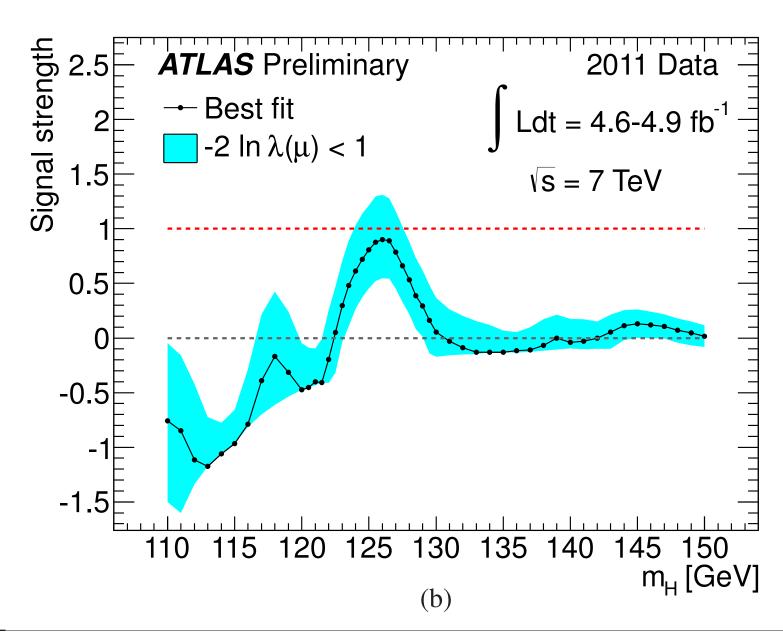


## Now a word on the Higgs





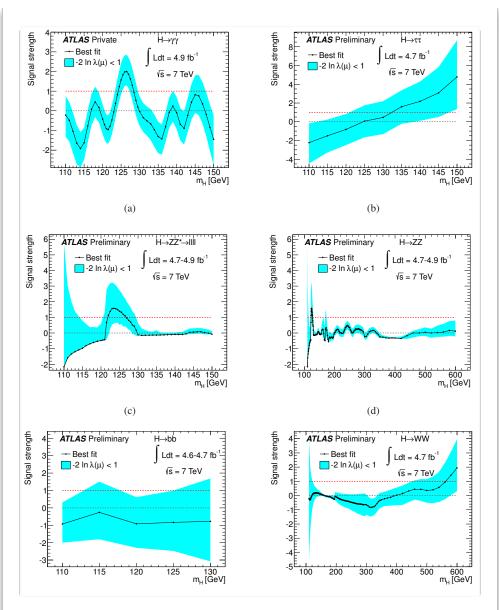
#### This is a global scaling of $\sigma$ BR for all production and decay modes.



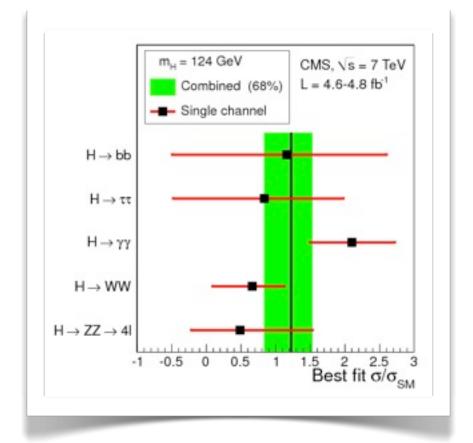
## Individual µ plots



**Recommendation 5:** For Higgs searches, provide all relevant information on a channel-by-channel basis.



This is **not** what we need for the coupling measurements b/c the production modes are assumed to take their SM ratios



## Reinterpreting the results

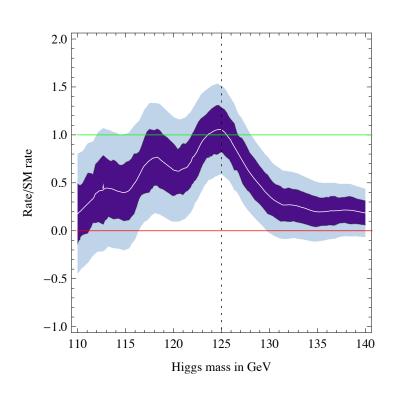


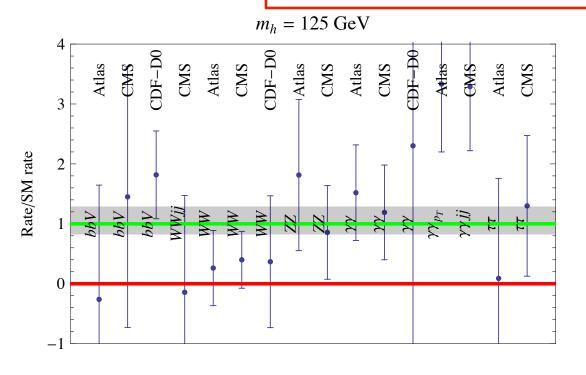
Clearly, if we don't release the necessary information, people will

do the best they can with what we provide.

#### CMS PLB 710 (2012)

For a Higgs boson having a mass,  $m_{\rm H}$ , of 120 GeV the overall acceptance times selection efficiency of the dijet tag for Higgs boson events is 15% (0.5%) for those produced by VBF (gluon–gluon fusion). This corresponds to about 2.01 (0.76) expected events. Events passing this tag are excluded from the four classes defined by  $R_9$  and pseudorapidity, but enter the fifth class. About 3% of Higgs boson signal events are expected to be removed from the four classes defined by diphoton properties. In the mass range  $100 < m_{\gamma\gamma} < 180$  GeV the fractions of diphoton events in the selected data, which pass the dijet VBF tag and enter the fifth class, and which would otherwise have entered one of the four classes defined in Table 2, are 0.8%, 0.5%, 0.3% and 0.4%, respectively.





P. P. Giardino, K. Kannike, M., A. Strumia. arXiv:1203.4254

## Difficulties interpreting our results



Searches often optimized for a given production and decay, but several production and decay modes populate those regions of phase space

- confused by the fact the selections are often labeled "VBF" etc.
- Note: older coupling studies were based on analyses with much more severe "VBF" cuts and gluon fusion contributions were smaller

Most results do not document the relative contributions from various production and decay processes to the total signal rate

• ie. ATLAS H→γγ does not give breakdown of ggF and VBF in the 9 subchannels. Why not?

Even if we did, the distributions are different, so we would really need to give detailed description of the shapes

- "The experiments have problems giving out information that in principle can't be used properly" -Yuri Gershtein (approximate)
- Note: many older studies based idealized analyses, shapes were not an issue

Likely that the coupling measurements will initially be done by collaborations

 thus important that we have open discussion with theorists about how this is done

## Moving beyond a single µ



In practical terms, we need a parameter for each branching ratio and a parameter for each production cross-section ("experimental parametrization").

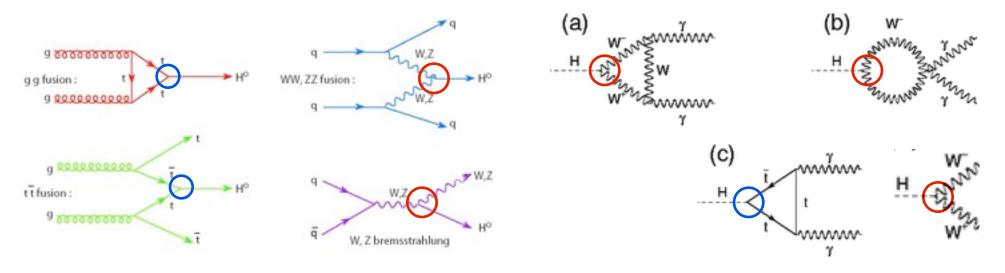
- We need signal contributions for different production mode separately
- · Call them μ<sub>i and</sub> μ<sub>j</sub> where i is production index and j is decay index
- take into account cross-contamination (ie. H→WW→lvlv in H→ZZ →llvv)
- · subtleties around theoretical uncertainties in these more general models

Only consider SM-like interactions at first

much more work needed if kinematic distributions change

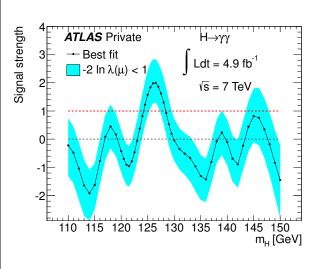
However, the production and decay really are not independent

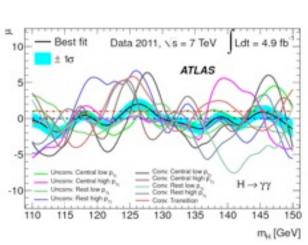
prepare to re-parametrize in terms of couplings

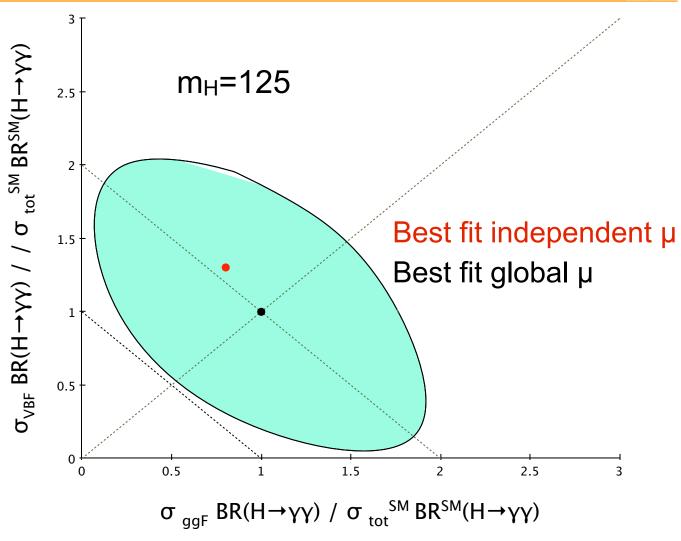


## μ<sub>i</sub> contours for individual channels









Above drawn with equal efficiencies, different efficiencies will lead to a tilted contour.

Need significant differences in shape or relative efficiency across sub-channels to break degeneracy among production modes

If we introduce additional  $\sigma_X$  for each production mode profile will fill plane

## Narrow width approximation



#### The basic starting point for the various parametrizations:

$$\sigma(H) \times \mathrm{BR}(H \to xx) = \frac{\sigma(H)^{\mathrm{SM}}}{\Gamma_p^{\mathrm{SM}}} \cdot \frac{\Gamma_p \Gamma_x}{\Gamma}$$

#### No useful direct constraint on total width at LHC

• allow for invisible? allow for unseen / buried / etc.?

#### Various strategies:

- not a higher SU(2) representation:  $\Gamma_V \leq \Gamma_V^{
  m SM}$ 
  - together with  $\Gamma_V^2/\Gamma = \text{meas} \ \Rightarrow \ \Gamma_{\text{vis}} \leq \Gamma \leq \Gamma_{V,SM}^2/\text{meas}$
- SFitter:  $\Gamma_{\text{tot}} = \sum_{\text{obs}} \Gamma_i(g_{iiH}) + \text{generation universality}$
- "Invisible Higgs Hypothesis"  $\Gamma = \Gamma_{vis} + \Gamma_{inv}$

**....** 

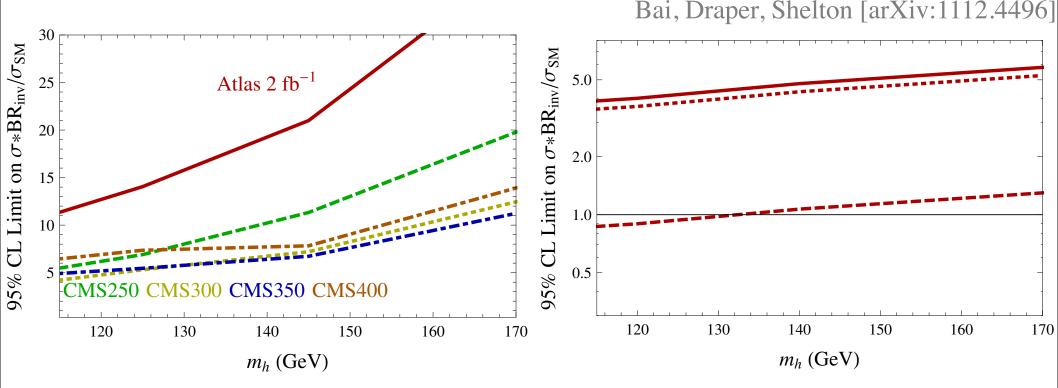
#### Or give up on total width and measure ratios

## Recasting for H→ invisible



# Bai, Draper, Shelton [arXiv:1112.4496] reinterpreted searches for monojets and H→ZZ→IIvv to constrain H→ invisible

Request ~	Analysis	Model	Status
1205.0033	Search for the standard model Higgs boson in the H→ZZ→2l2v channel in pp collisions at s√ = 7 TeV	Invisible Higgs	Active
1205.0032	Search for a Standard Model Higgs in the H- >ZZ->llvv decay channel with 4.7 fb-1 with the ATLAS detector	Invisible Higgs	Active



H→ZZ→IIvv to constrain pp→ ZH

Monojet to constrain pp→ H

#### **Conclusions**



We have the technical ability to publish likelihood functions digitally (RooFit/RooStats)

 We should make fundamental distinction between parameters that scale only rates and those that change acceptance, efficiencies, etc.

HEPData might store signal & background histograms

- need meta-information to organize this info (including systmatics)
  - HistFactory XML is a concrete solution for binned histograms

In order to extend analyses to different signal with different efficiencies and acceptances, need to run simulation.

- Fast simulation and/or parametrization for fine scans
- RECAST for validated reinterpretation via the experiments

Moving beyond SM Higgs searches towards Higgs coupling measurements is very important and also delicate

- critical to take into account different production modes in each of the search channels. Current results usually don't provide this information
- if the experiments are going to do final coupling fits, then we need good interaction with theorists

We are making progress, the Higgs is likely to change the discussion

## Eierlegende Wollmilchsau





## Acceptance

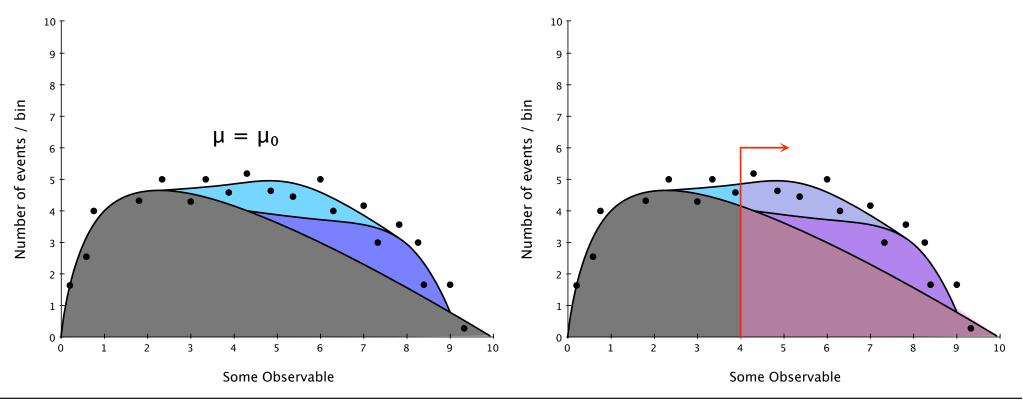


As we move around the model's parameter space the distributions change, thus changing the signal efficiency and acceptance.

This is harder to parametrize than branching ratios for different topologies

Remember that even at this fixed point in the model's parameter space, the efficiency and acceptance can change as you vary the nuisance parameters associated with systematic effects.

at first, maybe we can neglect this effect and it's an adequate approximation



#### Acceptance

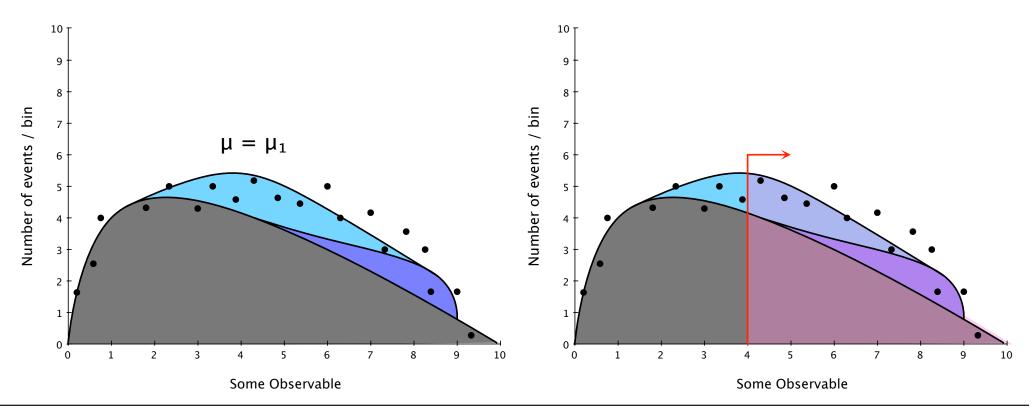


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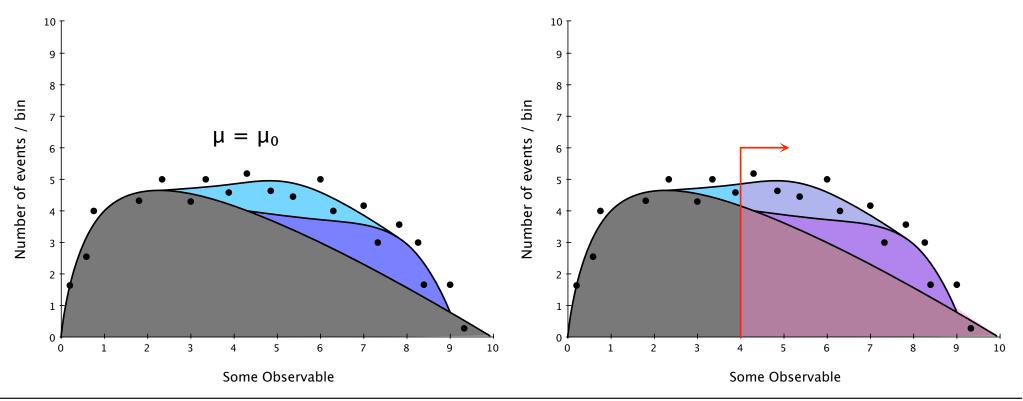


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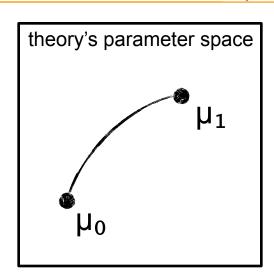


## Interpolating

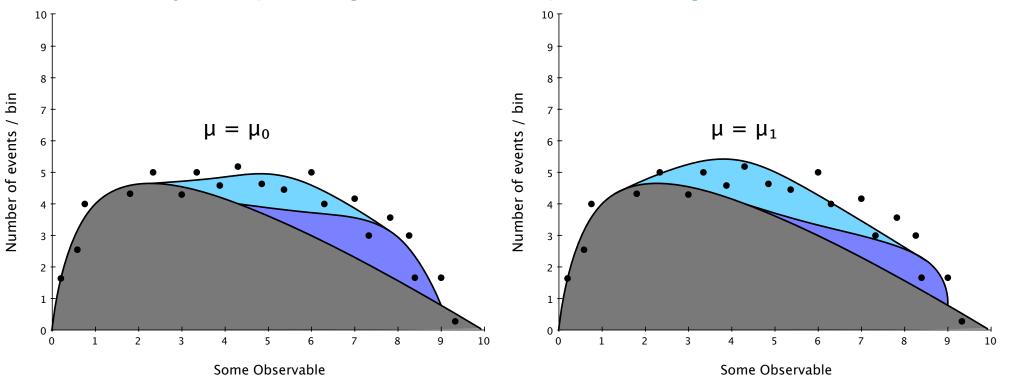


Most statistical techniques require ability to evaluate likelihood at arbitrary points in the parameter space ⇒

- Either need to have evaluated model at sufficiently many discrete parameter points
- Or have a way of interpolating expected signal distribution (including efficiency & acceptance)



Often by interpolating between template histograms

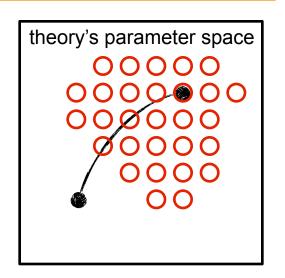


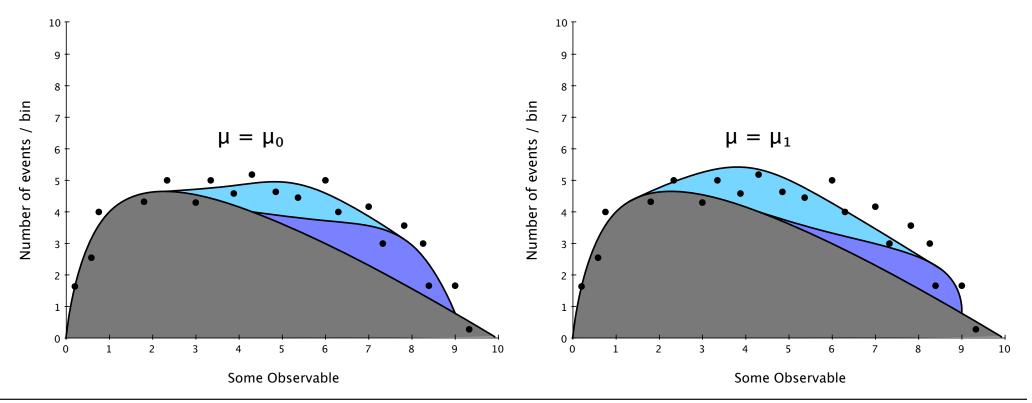
## **Extrapolating**



Initially the experiments may scan some initial set of model points.

- These define a domain of validity for the model
- How does one go to model points outside this set?
  - if the experiments had a service to provide signal templates for new model points, then one can interpolate between these new anchor points.



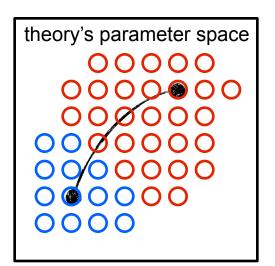


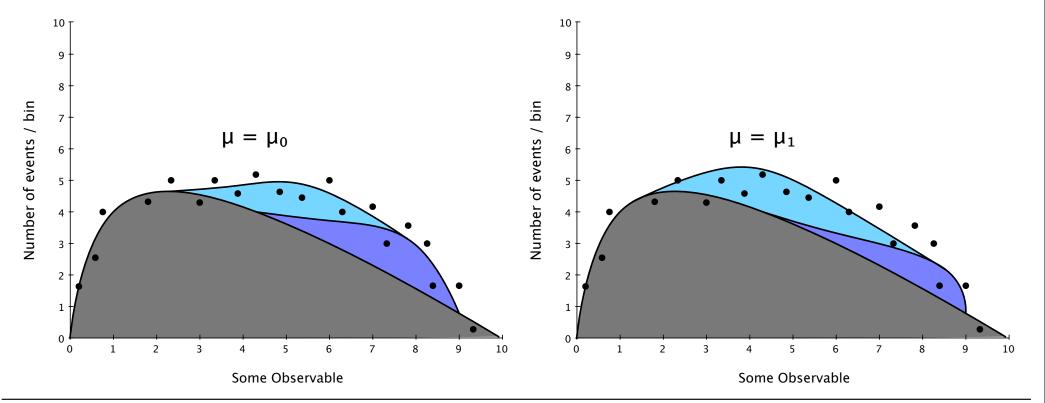
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## First interface with SuperBayes



Repeated same analysis as Bridges, KC, Trotta et al (1011.4306) with RooStats likelihood

see consistent results!

