

**Big bang or freeze ?**

A vast field of galaxies, including spirals, ellipticals, and irregular shapes, scattered across a dark cosmic background. The galaxies are in various colors, including yellow, blue, and purple, and vary in size and orientation. Some are bright and clear, while others are faint and distant.

# *NATURE* | NEWS

Cosmologist claims Universe may not be expanding  
**Particles' changing masses could explain why  
distant galaxies appear to be rushing away.**

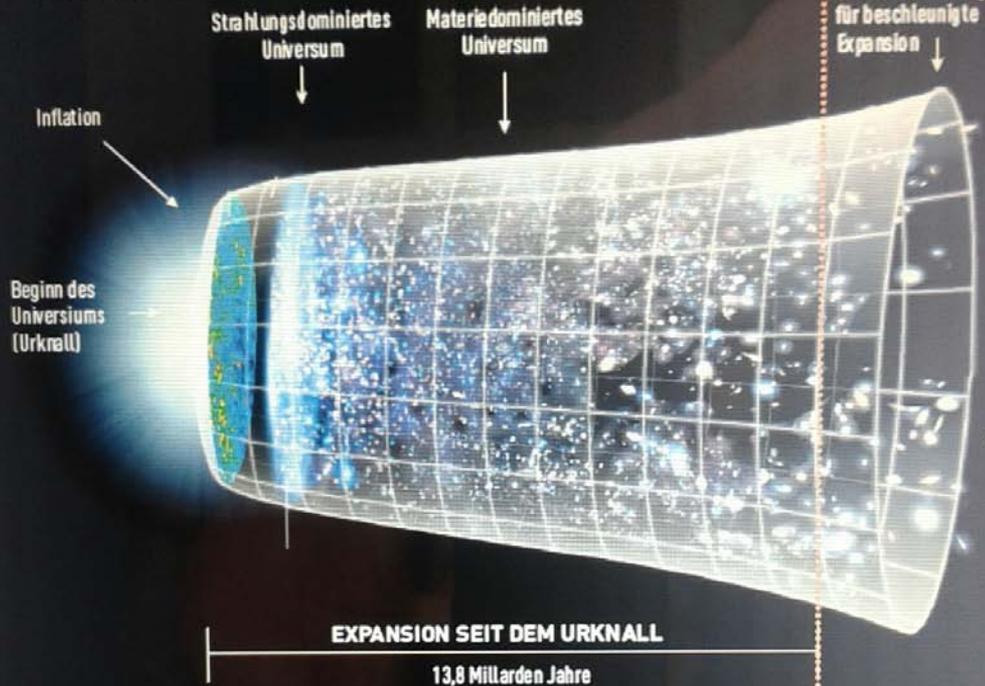
**Jon Cartwright**      16 July 2013



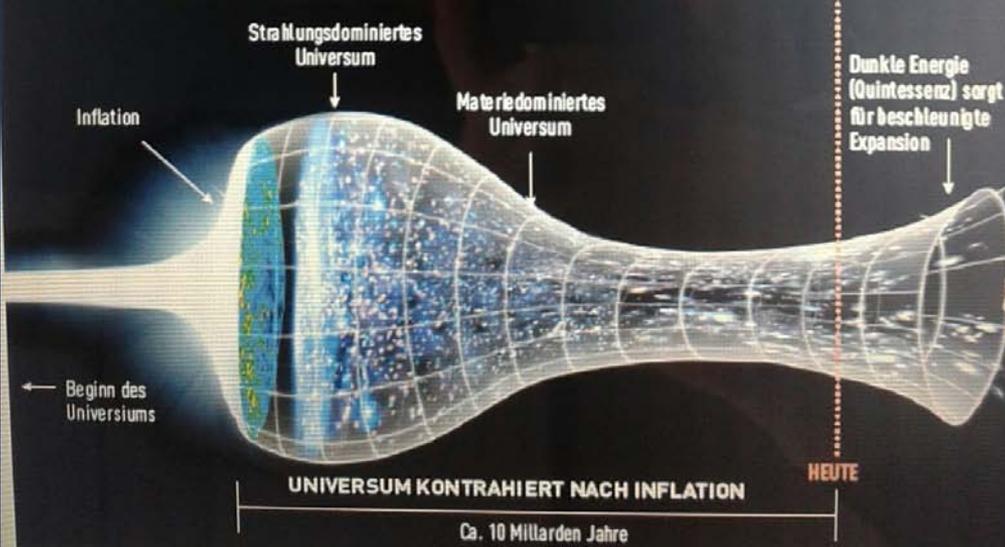
German physicist stops  
Universe

25.07.2013

## Klassisches Bild der Kosmologie



## Model von Wetterich



Sonntagszeitung  
Zürich  
Laukenmann

**The Universe is shrinking**

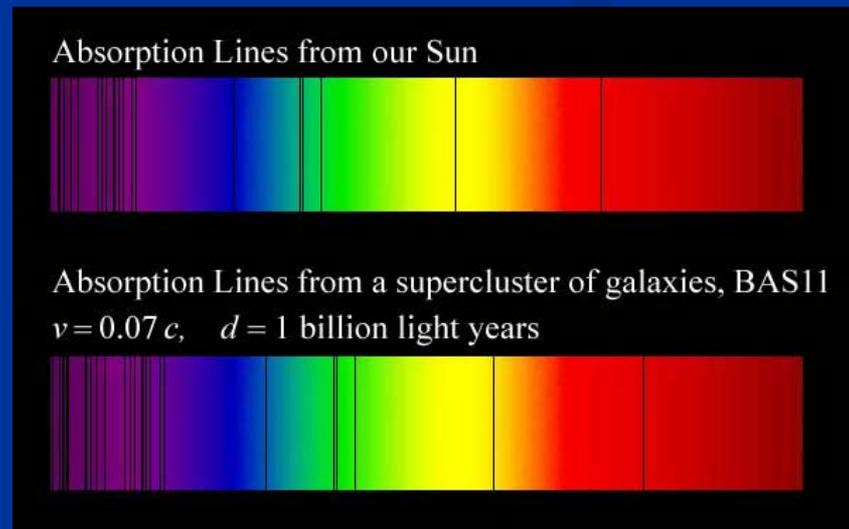
**The Universe is shrinking ...**

**while Planck mass and particle  
masses are increasing**

# Redshift

instead of redshift due to expansion :

smaller frequencies have been emitted in the past, because electron mass was smaller !



# What is increasing ?

Ratio of distance between galaxies  
over size of atoms !

atom size constant : expanding geometry

alternative : shrinking size of atoms

general idea not new : Hoyle, Narlikar,...

# Different pictures of cosmology

- same physical content can be described by different pictures
- related by field – redefinitions ,  
e.g. Weyl scaling , conformal scaling of metric
- which picture is usefull ?

# Cosmological scalar field ( cosmon )

- scalar field is crucial ingredient
- particle masses proportional to scalar field – similar to Higgs field
- particle masses increase because value of scalar field increases
- scalar field plays important role in cosmology
- cosmon : pseudo Goldstone boson of spontaneously broken scale symmetry

# Cosmon inflation

Unified picture of inflation and  
dynamical dark energy

Cosmon and inflaton are the same  
scalar field

# Quintessence

Dynamical dark energy ,  
generated by scalar field (cosmon )

C.Wetterich,Nucl.Phys.B302(1988)668, 24.9.87

P.J.E.Peebles,B.Ratra,ApJ.Lett.325(1988)L17, 20.10.87

## Prediction :

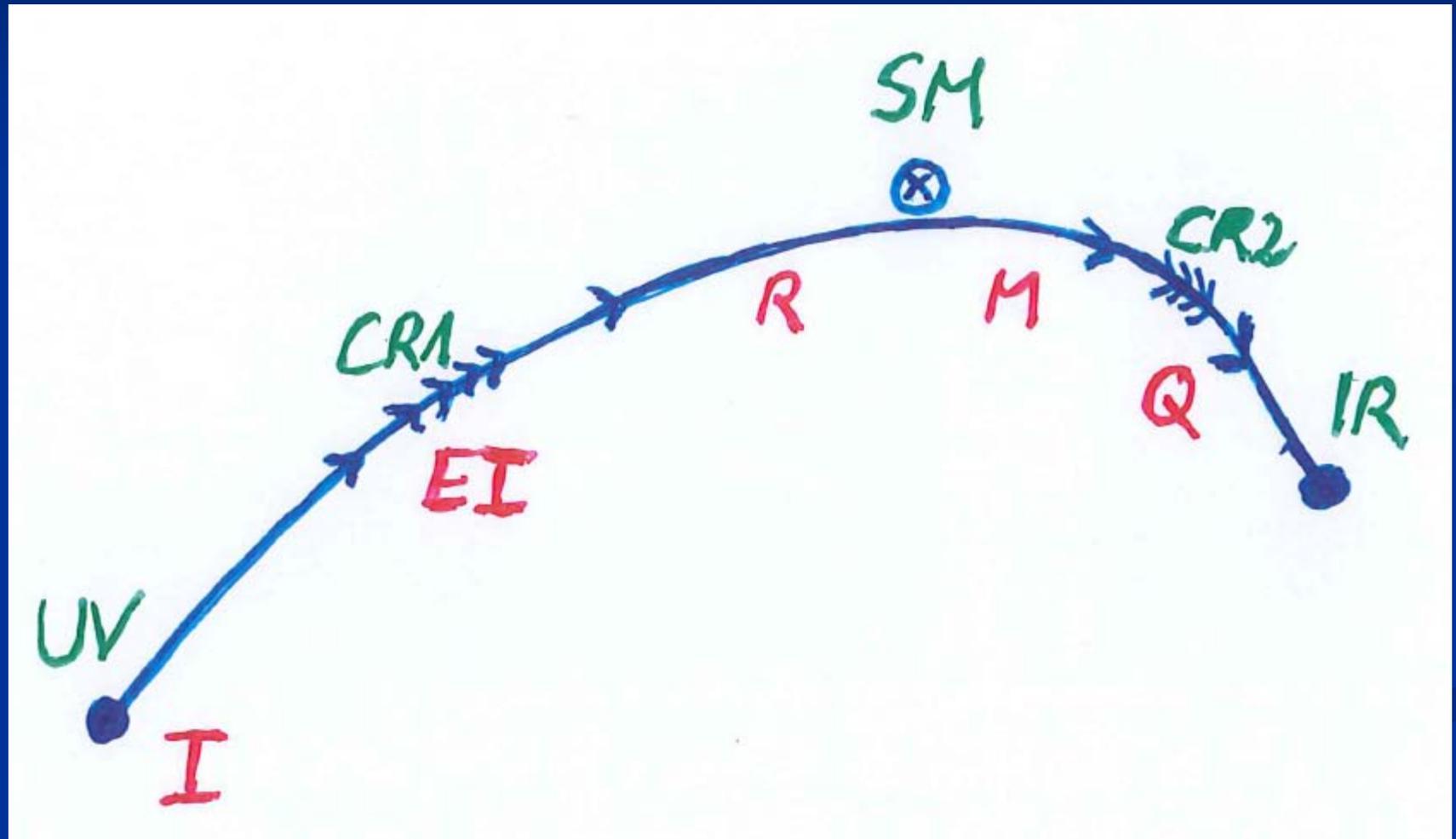
homogeneous dark energy  
influences recent cosmology

- of same order as dark matter -

Original models do not fit the present observations  
.... modifications  
( different growth of neutrino mass )

scalar field may be  
important feature of  
quantum gravity

# Crossover in quantum gravity



# Approximate scale symmetry near fixed points

- UV : approximate scale invariance of primordial fluctuation spectrum from inflation
- IR : almost massless pseudo-Goldstone boson (cosmon) responsible for dynamical Dark Energy

# Variable Gravity

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

scale invariant for  $\mu = 0$  and  $B$  const.

quantum effects : flow equation for kineticial

$$\mu \frac{\partial B}{\partial \mu} = \frac{\kappa \sigma B^2}{\sigma + \kappa B}$$

# Variable Gravity

- Scalar field coupled to gravity
- Effective Planck mass depends on scalar field
- Simple quadratic scalar potential involves intrinsic mass  $\mu$
- Nucleon and electron mass proportional to dynamical Planck mass
- Neutrino mass has different dependence on scalar field

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2}\chi^2 R + \mu^2 \chi^2 + \frac{1}{2}(B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

# No tiny dimensionless parameters ( except gauge hierarchy )

- one mass scale  $\mu = 2 \cdot 10^{-33} \text{ eV}$
- one time scale  $\mu^{-1} = 10^{10} \text{ yr}$
- Planck mass does not appear
- Planck mass grows large dynamically

# Infrared fixed point

■  $\mu \rightarrow 0$

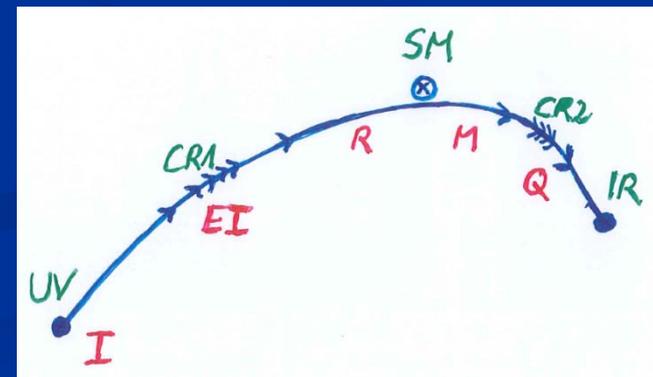
■  $B \rightarrow 0$

$$\mu \partial_\mu B = \kappa B^2 \quad \text{for} \quad B \rightarrow 0$$

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \mu^2 \chi^2 + \frac{1}{2} (B(\chi/\mu) - 6) \partial^\mu \chi \partial_\mu \chi \right\}$$

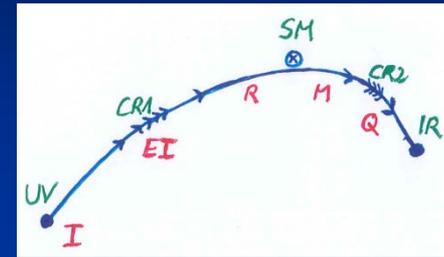
■ no intrinsic mass scale

■ scale symmetry



# Ultraviolet fixed point

■  $\mu \rightarrow \infty$



■ kinetic diverges

$$B = b \left( \frac{\mu}{\chi} \right)^\sigma = \left( \frac{m}{\chi} \right)^\sigma$$

■ scale symmetry with anomalous dimension  $\sigma$

$$g_{\mu\nu} \rightarrow \alpha^2 g_{\mu\nu}, \quad \chi \rightarrow \alpha^{-\frac{2}{2-\sigma}} \chi$$

# Renormalized field at UV fixed point

$$\chi_R = b^{\frac{1}{2}} \left(1 - \frac{\sigma}{2}\right)^{-1} \mu^{\frac{\sigma}{2}} \chi^{1 - \frac{\sigma}{2}}$$

$$1 < \sigma < 2$$

$$\Gamma_{UV} = \int_x \sqrt{g} \left\{ \frac{1}{2} \partial^\mu \chi_R \partial_\mu \chi_R - \frac{1}{2} C R^2 + D R^{\mu\nu} R_{\mu\nu} \right\}$$

no mass  
scale

$$\Delta\Gamma_{UV} = \int_x \sqrt{g} E \left( \mu^2 - \frac{R}{2} \right) \mu^{-\frac{2\sigma}{2-\sigma}} \chi_R^{\frac{4}{2-\sigma}},$$

deviation from  
fixed point  
vanishes for

$$E = b^{-\frac{2}{2-\sigma}} \left(1 - \frac{\sigma}{2}\right)^{\frac{4}{2-\sigma}}$$

$$\mu \rightarrow \infty$$

# Asymptotic safety

if UV fixed point exists :

*quantum gravity is  
non-perturbatively renormalizable !*

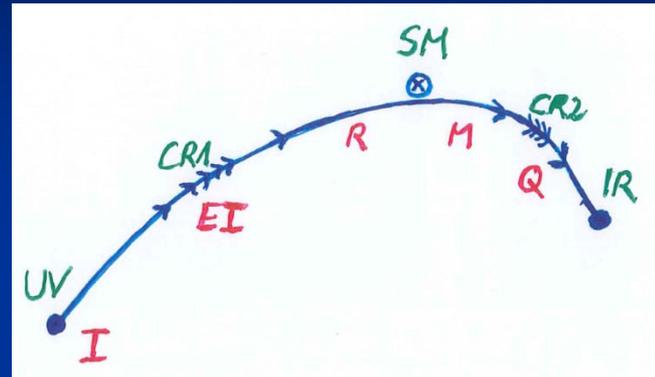
S. Weinberg , M. Reuter

# Quantum scale symmetry

- quantum fluctuations violate scale symmetry
- running dimensionless couplings
- at fixed points , scale symmetry is exact !

# Crossover between two fixed points

$$\mu \frac{\partial B}{\partial \mu} = \frac{\kappa \sigma B^2}{\sigma + \kappa B}$$



$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

$m$  : scale of crossover

can be exponentially larger than intrinsic scale  $\mu$

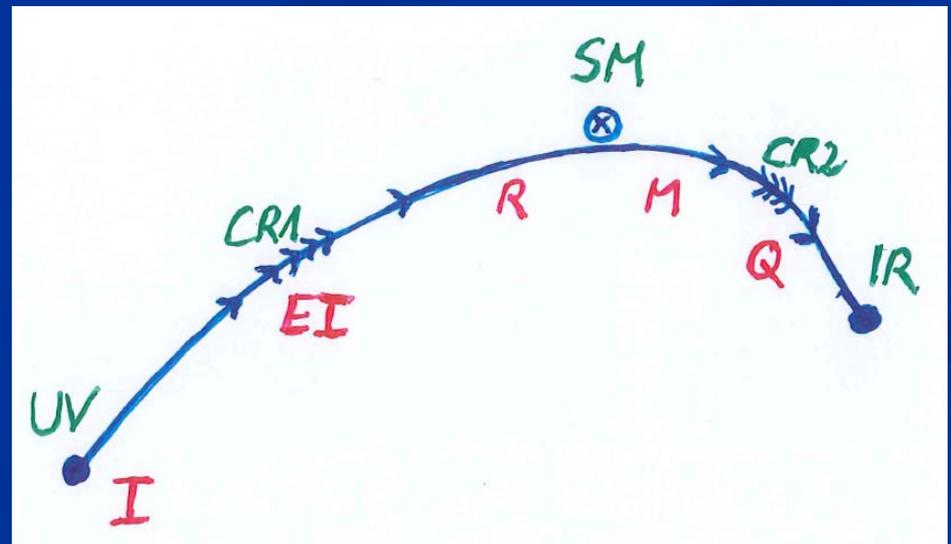
# Origin of mass

- UV fixed point : scale symmetry unbroken  
all particles are massless
- IR fixed point : scale symmetry spontaneously broken,  
massive particles , massless dilaton
- crossover : explicit mass scale  $\mu$  or  $m$  important
- SM fixed point : approximate scale symmetry spontaneously broken, massive particles , almost massless cosmon, tiny cosmon potential

# Cosmological solution : crossover from UV to IR fixed point

- Dimensionless functions as  $B$  depend only on ratio  $\mu/\chi$ .
- IR:  $\mu \rightarrow 0$  ,  $\chi \rightarrow \infty$
- UV:  $\mu \rightarrow \infty$  ,  $\chi \rightarrow 0$

**Cosmology makes  
crossover between  
fixed points by  
variation of  $\chi$ .**



# Simplicity

simple description of **all** cosmological epochs

natural incorporation of Dark Energy :

- inflation
- Early Dark Energy
- present Dark Energy dominated epoch

# Model is compatible with present observations

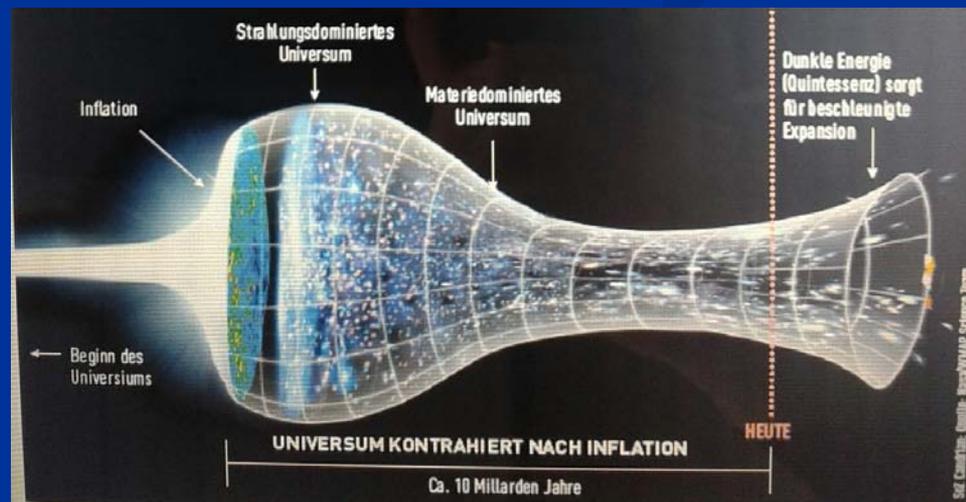
Together with variation of neutrino mass over electron mass during second stage of crossover :  
model is compatible with all present observations

$$\Gamma = \int_x \sqrt{g} \left\{ -\frac{1}{2}\chi^2 R + \mu^2\chi^2 + \frac{1}{2}(B(\chi/\mu) - 6)\partial^\mu\chi\partial_\mu\chi \right\}$$

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

# Expansion

- Inflation : Universe expands
- Radiation : Universe shrinks
- Matter : Universe shrinks
- Dark Energy : Universe expands



# Hot plasma ?

- Temperature in radiation dominated Universe :  
 $T \sim \chi^{1/2}$  **smaller** than today
- Ratio temperature / particle mass :  
 $T / m_p \sim \chi^{-1/2}$  **larger** than today
- $T/m_p$  counts ! This ratio decreases with time.
- Nucleosynthesis , CMB emission as in standard cosmology !

# Infinite past : slow inflation

$\sigma = 2$  : field equations

$$\ddot{\chi} + \left( 3H + \frac{1}{2} \frac{\dot{\chi}}{\chi} \right) \dot{\chi} = \frac{2\mu^2 \chi^2}{m}$$

$$H = \sqrt{\frac{\mu^2}{3} + \frac{m\dot{\chi}^2}{6\chi^3}} - \frac{\dot{\chi}}{\chi}$$

solution

$$H = \frac{\mu}{\sqrt{3}}, \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

# Eternal Universe

- solution valid back to the infinite past in physical time

# Slow Universe

$$H = \frac{\mu}{\sqrt{3}}, \quad \chi = \frac{3^{\frac{1}{4}} m}{2\sqrt{\mu}} (t_c - t)^{-\frac{1}{2}}$$

$$\mu = 2 \cdot 10^{-33} \text{ eV}$$

Expansion or shrinking always slow ,  
characteristic time scale of the order of the age of the  
Universe :  $t_{\text{ch}} \sim \mu^{-1} \sim 10 \text{ billion years !}$

Hubble parameter of the order of **present** Hubble  
parameter for all times , including inflation and big bang !  
Slow increase of particle masses !

# Spectrum of primordial density fluctuations

tensor  
amplitude

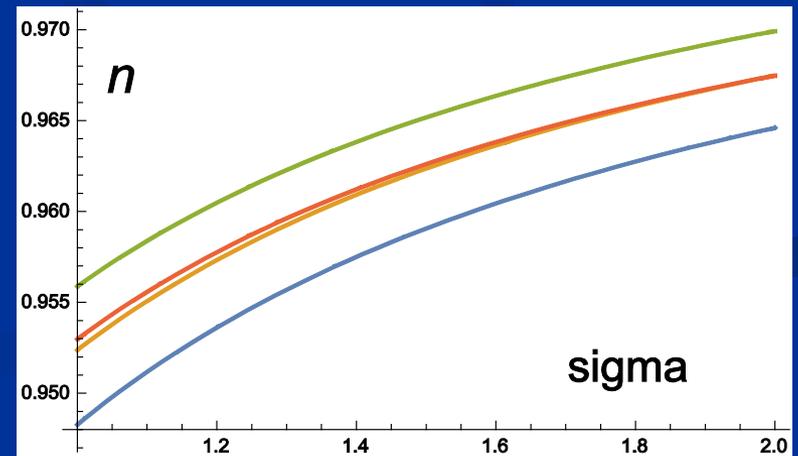
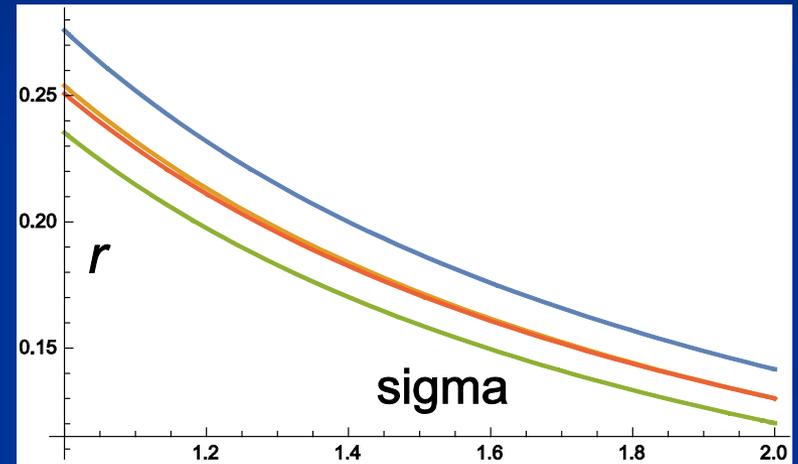
$$r = \frac{32}{B(N)}$$

rather large !

spectral  
index

$$1 - n = \frac{r}{8} \left( 1 + \frac{1}{2} \sigma(N) \right)$$

$$\sigma = - \frac{\partial \ln B}{\partial \ln \chi} \Big|_{B=2\sigma N+6}$$



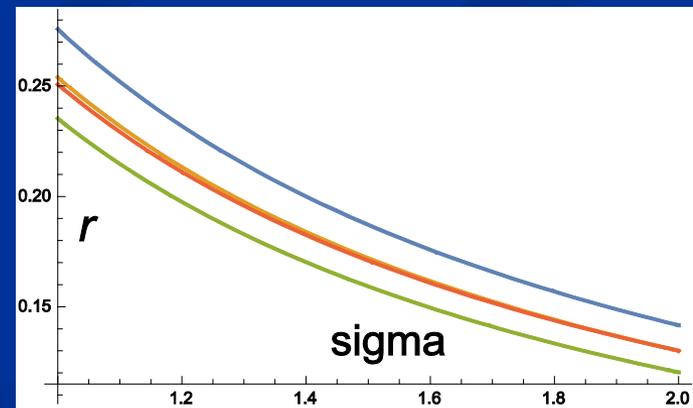
# Anomalous dimension determines spectrum of primordial fluctuations

$$r = \frac{0.26}{\sigma}$$

$$n = 1 - \frac{0.065}{\sigma} \cdot \left( 1 + \frac{\sigma - 2}{4} \right)$$

$$\sigma = 2$$

$$r = 0.13, \quad n = 0.967$$



# Amplitude of density fluctuations

small because of logarithmic running  
near UV fixed point !

$$\mathcal{A} = \frac{(N + 3)^3}{4} e^{-2c_t}$$

$$c_t = \ln \left( \frac{m}{\mu} \right) = 14.1.$$

$$\frac{m}{\mu} = \frac{(N + 3)^{\frac{3}{2}}}{2\sqrt{\mathcal{A}}} = 1.32 \cdot 10^6 \left( \frac{N}{60} \right)^{\frac{3}{2}}$$

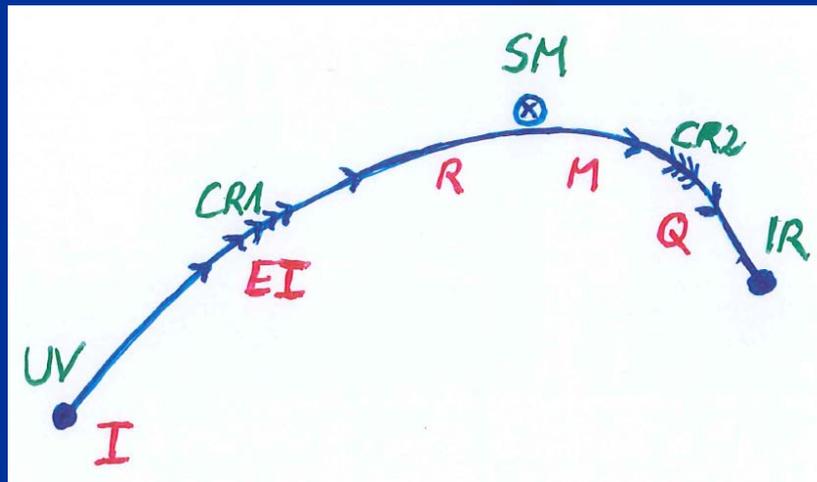
N : number of e – foldings at horizon crossing

# First step of crossover ends inflation

- induced by crossover in B

$$B^{-1} - \frac{\kappa}{\sigma} \ln B = \kappa \left[ \ln \left( \frac{\chi}{\mu} \right) - c_t \right] = \kappa \ln \left( \frac{\chi}{m} \right)$$

- after crossover B changes only very slowly



# Scaling solutions near SM fixed point

( approximation for constant  $B$  )

$$H = b\mu , \quad \chi = \chi_0 \exp(c\mu t)$$

Different scaling solutions for  
radiation domination and  
matter domination

# Radiation domination

$$c = \frac{2}{\sqrt{K+6}}$$

$$b = -\frac{c}{2}$$

**Universe  
shrinks !**

$$T_{00} = \rho = \bar{\rho} \mu^2 \chi^2$$

$$\bar{\rho}_r = -3 \frac{K+5}{K+6}$$

**K = B - 6**

solution exists for  $B < 1$  or  $K < -5$

$$S = \int_x \sqrt{g} \left\{ -\frac{1}{2} \chi^2 R + \frac{1}{2} K(\chi) \partial^\mu \chi \partial_\mu \chi + V(\chi) \right\}$$

$$H = b\mu, \quad \chi = \chi_0 \exp(c\mu t)$$

# Varying particle masses near SM fixed point

- All particle masses are proportional to  $\chi$ .  
( scale symmetry )
- Ratios of particle masses remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.

# cosmon coupling to matter

$$K(\ddot{\chi} + 3H\dot{\chi}) + \frac{1}{2} \frac{\partial K}{\partial \chi} \dot{\chi}^2 = -\frac{\partial V}{\partial \chi} + \frac{1}{2} \frac{\partial F}{\partial \chi} R + q_{\chi}$$

$$q_{\chi} = -(\rho - 3p)/\chi$$

$$F = \chi^2$$

# Matter domination

$$c = \sqrt{\frac{2}{K+6}},$$

$$b = -\frac{1}{3} \sqrt{\frac{2}{K+6}} = -\frac{1}{3}c,$$

**Universe shrinks !**

$$T_{00} = \rho = \bar{\rho} \mu^2 \chi^2,$$

solution exists for

$$B < 4/3, \quad K < -14/3$$

$$\bar{\rho}_m = -\frac{2(3K+14)}{3(K+6)}$$

$$K = B - 6$$

# Early Dark Energy

Energy density in radiation increases ,  
proportional to cosmon potential

$$T_{00} = \rho = \bar{\rho} \mu^2 \chi^2$$

$$V(\chi) = \mu^2 \chi^2$$

fraction in early dark energy

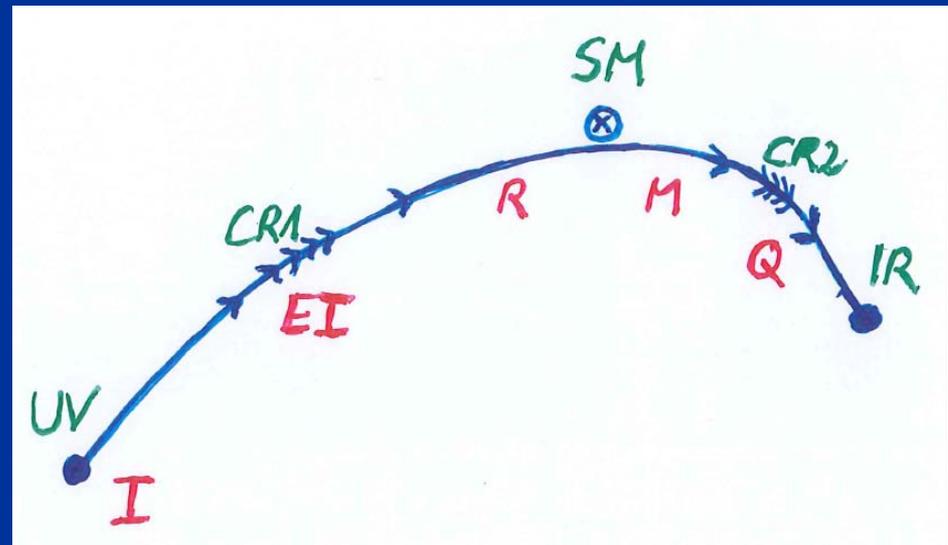
$$\Omega_h = \frac{\rho_h}{\rho_r + \rho_h} = \frac{nB(\chi)}{4}$$

or m

observation requires **B < 0.02** ( at CMB emission )

# Second crossover

- from SM to IR
- in sector of SM-singlets
- affects neutrino masses first



# Varying particle masses at onset of second crossover

- All particle masses **except neutrinos** are proportional to  $\chi$ .
- Ratios of particle masses remain constant.
- Compatibility with observational bounds on time dependence of particle mass ratios.
- Neutrino masses show stronger increase with  $\chi$ , such that **ratio neutrino mass over electron mass grows**.

# Dark Energy domination

neutrino masses scale  
differently from electron mass

$$\left. \frac{\partial \ln m_\nu}{\partial \ln \chi} \right|_{\text{today}} = 2\tilde{\gamma} + 1$$



$$m_\nu = \bar{c}_\nu \chi^{2\tilde{\gamma}+1}$$

$$\chi q_\chi = -(2\tilde{\gamma} + 1)(\rho_\nu - 3p_\nu)$$

new scaling solution. not yet reached.  
at present : transition period

$$\frac{\rho_\nu}{\chi^2} = \bar{\rho}_\nu \mu^2$$

$$b = \frac{1}{3}(2\tilde{\gamma} - 1)c$$

# connection between dark energy and neutrino properties

$$[\rho_h(t_0)]^{\frac{1}{4}} = 1.27 \left( \frac{\gamma m_\nu(t_0)}{eV} \right)^{\frac{1}{4}} 10^{-3} eV$$

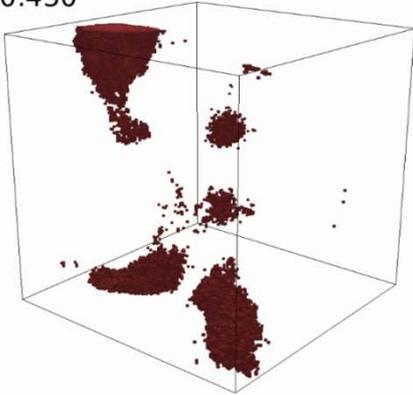
present dark energy density given by neutrino mass

present equation  
of state given by  
neutrino mass !

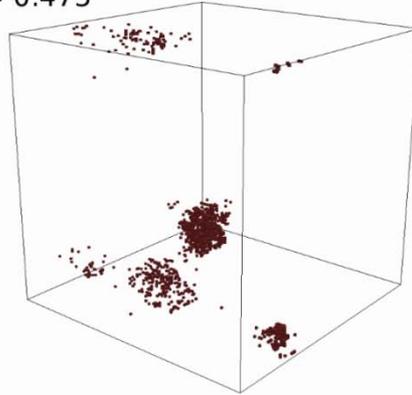
$$w_0 \approx -1 + \frac{m_\nu(t_0)}{12eV}$$

# Oscillating neutrino lumps

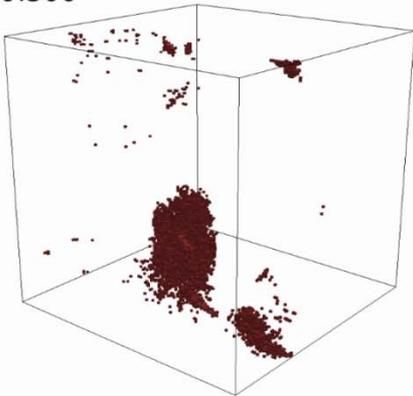
$a = 0.450$



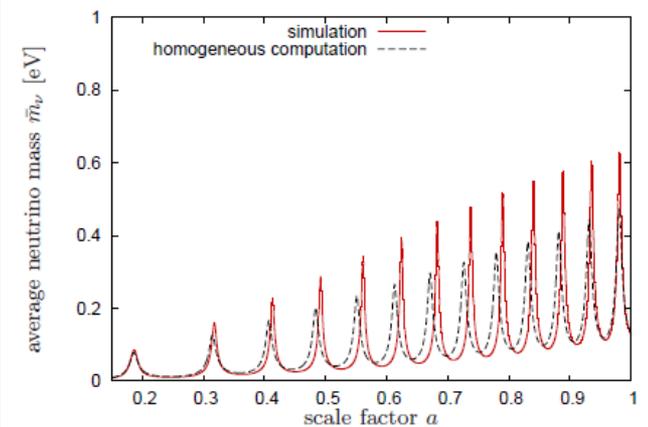
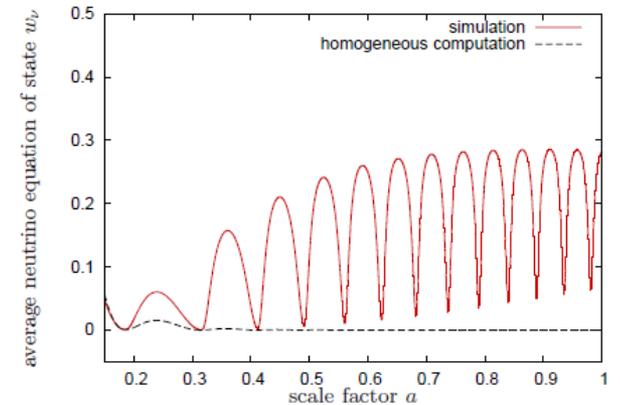
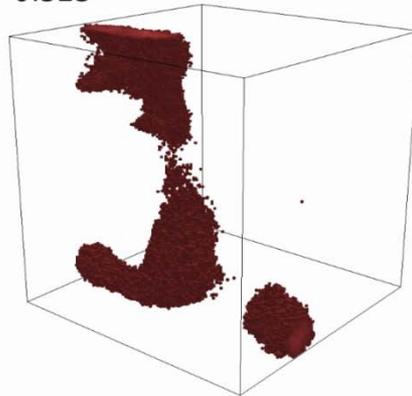
$a = 0.475$



$a = 0.500$



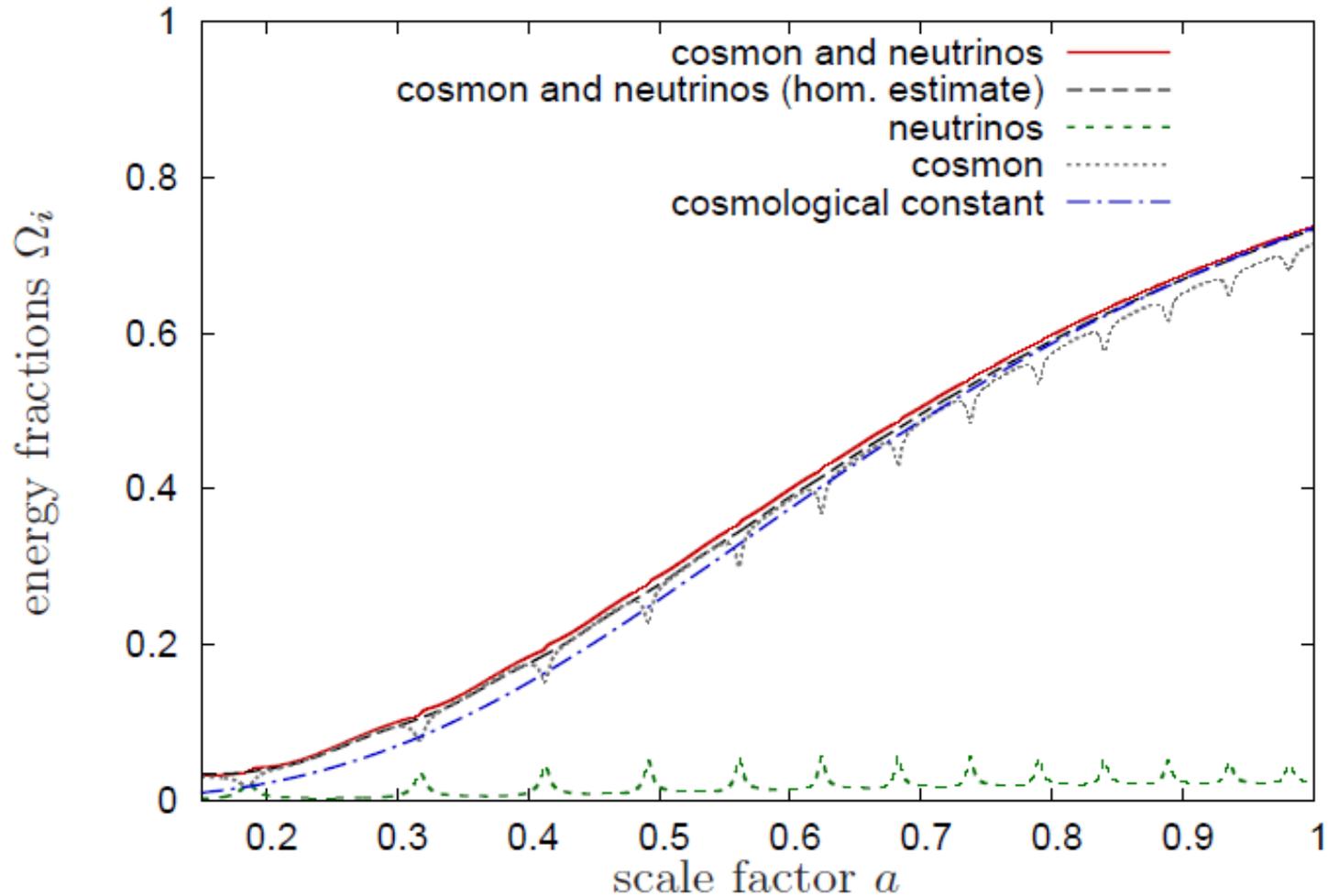
$a = 0.525$



Y. Ayaita, M. Weber, ...

Ayaita, Baldi, Fuehrer,  
Puchwein, ...

# Evolution of dark energy similar to $\Lambda$ CDM



# Compatibility with observations

- Realistic inflation model:

$$n = 0.976, r = 0.13$$

- Almost same prediction for radiation, matter, and Dark Energy domination as  $\Lambda$ CDM
- Presence of small fraction of Early Dark Energy
- Large neutrino lumps

# Einstein frame

$$g'_{\mu\nu} = \frac{\chi^2}{M^2} g_{\mu\nu} , \quad \varphi = \frac{2M}{\alpha} \ln \left( \frac{\chi}{\mu} \right)$$

$$\Gamma = \int_x \sqrt{g'} \left\{ -\frac{1}{2} M^2 R' + V'(\varphi) + \frac{1}{2} k^2(\varphi) \partial^\mu \varphi \partial_\mu \varphi \right\}$$

$$V'(\varphi) = M^4 \exp \left( -\frac{\alpha \varphi}{M} \right)$$

$$k^2 = \frac{\alpha^2 B}{4}$$

# Einstein frame

- Weyl scaling maps variable gravity model to Universe with fixed masses and standard expansion history.
- Standard gravity coupled to scalar field.
- Only neutrino masses are growing.

# conclusions

- crossover in quantum gravity is reflected in crossover in cosmology
- quantum gravity becomes testable by cosmology
- quantum gravity plays a role not only for primordial cosmology
- crossover scenario explains different cosmological epochs
- simple model is compatible with present observations
- no more parameters than  $\Lambda$ CDM : tests possible

# conclusions (2)

- Variable gravity cosmologies can give a simple and realistic description of Universe
- Compatible with tests of equivalence principle and bounds on variation of fundamental couplings if nucleon and electron masses are proportional to variable Planck mass
- Different cosmological dependence of neutrino mass can explain why Universe makes a transition to Dark Energy domination **now**
- **characteristic signal : neutrino lumps**



end

# Scaling of particle masses

mass of electron or nucleon is proportional to variable Planck mass  $\chi$  !

effective potential for Higgs doublet  $h$

$$\tilde{V}_h = \frac{1}{2} \lambda_h (\tilde{h}^\dagger \tilde{h} - \epsilon_h \chi^2)^2$$