

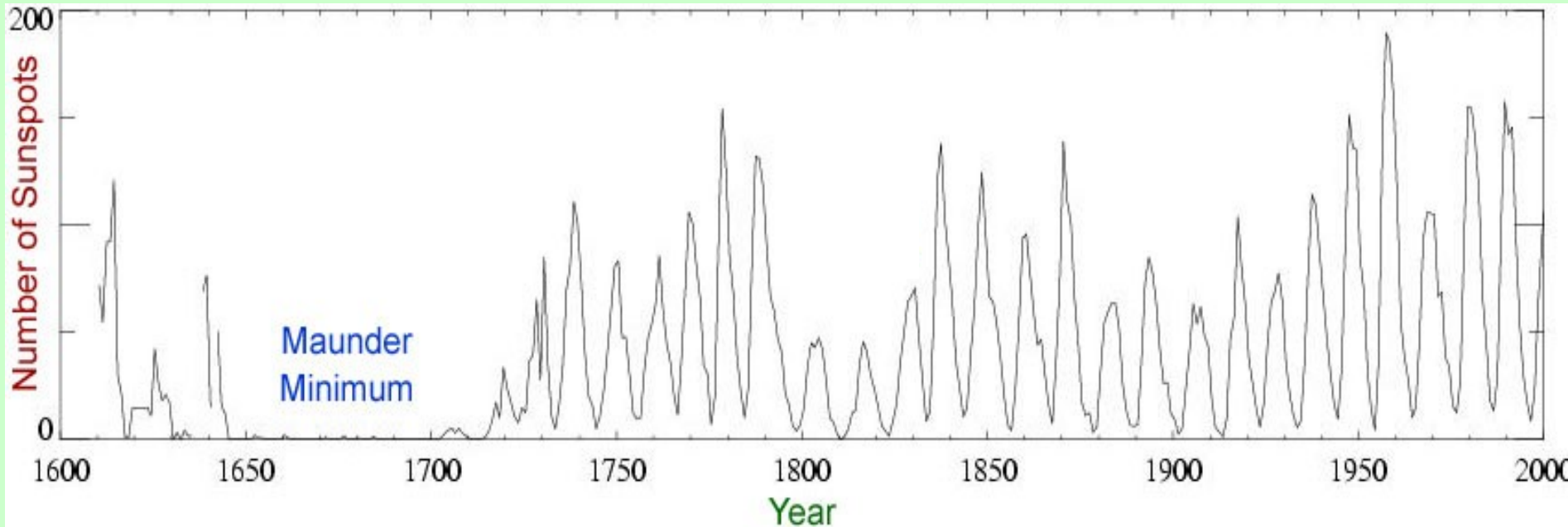


# Grand Minima of Sunspots and Dynamo Models

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Petri J. Kapyla & Maarit J. Kapyla

## Maunder minimum



➤ **Maunder minimum period = 1645 to 1715** (Eddy, 1976; Foukal, 1990; Wilson, 1994)

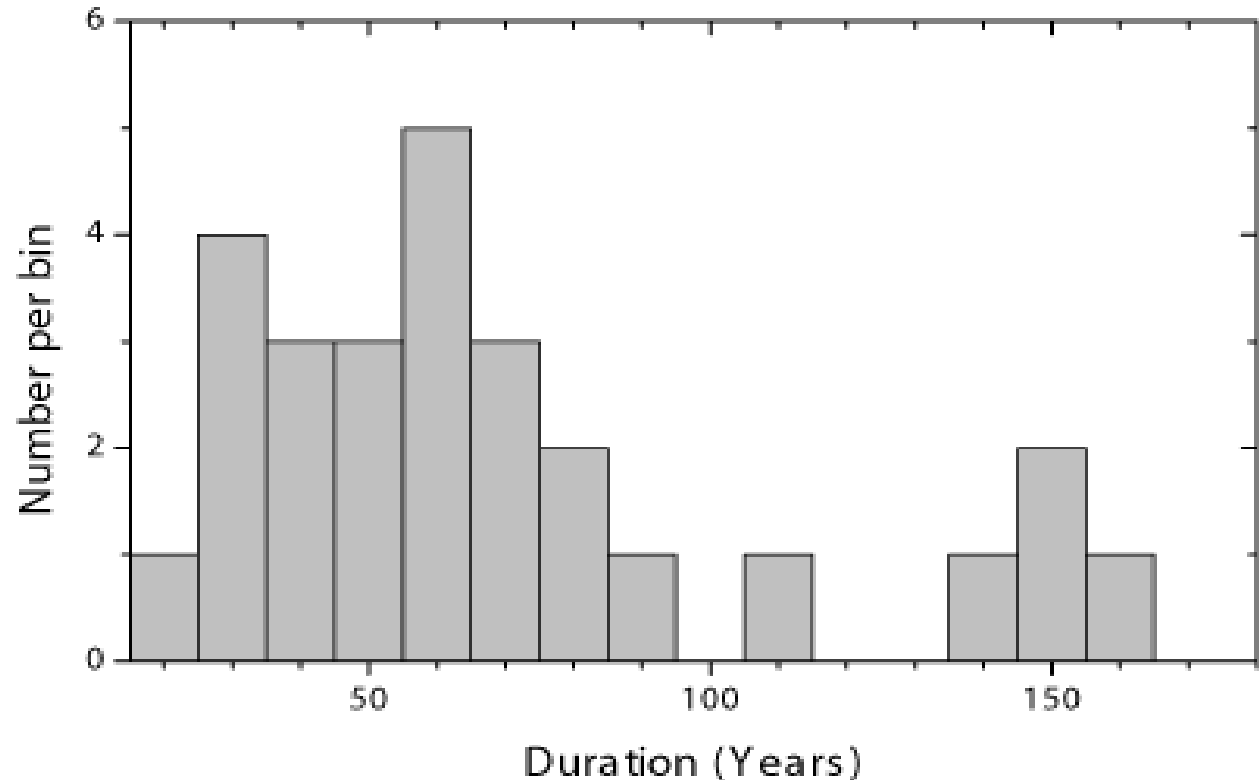
**It is a real phenomenon!** (Sokoloff & Nesme-Ribes 1994; Hoyt & Schatten 1996; .....

# Solar activity in past

## Results from $C^{14}$ data in old tree ring:

❖ **27 grand minima in last 11,000 years**

(Usoskin et al. 2007)



# Theoretical models of grand minima

The story started as early as in 1980s.

All the studies are done using mean-field dynamo models because the global simulations were not even successful to produce 11-year solar cycle (Gilman 1983; Glatzmaier 1985)!

Two broad approaches of grand minima:

=> **Amplitude modulation**

=> **Stochastic noise**

# Amplitude modulations in nonlinear dynamo models

- **Nonlinearity due to back-reaction of  $B$  on  $v$**
- **Lambda quenching can produce grand mimima**(Kitchatinov et al. 1994; Kuker et al. 1999)

→ **Not expected in Sun!**

- **$\alpha$ -quenching:**

$$\alpha = \frac{\alpha_0}{1 + |\overline{B}|^2}$$

→ **stabilizing effect!**

(Long history – Stix 1972; Ivanova & Ruzmaikin 1977; Yoshimura 1978; Schmitt & Schussler 1989).

Coupling between various modes with close frequencies  
(Krause & Meinel 1988; Brandenburg et al. 1989a,b; Sokoloff & Nesme-Ribes 1994; Beer et al. 1998; Brooke et al. 1998)

- Weiss, Cattaneo & Jones (1984) found chaos in some highly truncated models with suppression of differential rotation

## Stochastic noise

Since turbulence is the driver of dynamo action in stars, grand minima through the resulting noise can be possible!

$$\frac{\partial \bar{\mathbf{B}}}{\partial t} = \nabla \times (\bar{\mathbf{V}} \times \bar{\mathbf{B}}) + \nabla \times \varepsilon + \lambda \nabla^2 \bar{\mathbf{B}}$$

Where  $\varepsilon = \overline{\mathbf{v}' \times \mathbf{B}'}$

After approximation:  $\varepsilon = \alpha \bar{\mathbf{B}} - \beta \nabla \times \bar{\mathbf{B}}$

### Fluctuations in $\alpha$ is indeed expected!

(Hoyng 1988; Choudhuri 1992; Moss et al. 1992; Hoyng 1993; Ossendrijver et al. 1996; Moss et al. 2008; Brandenburg et al. 2008)

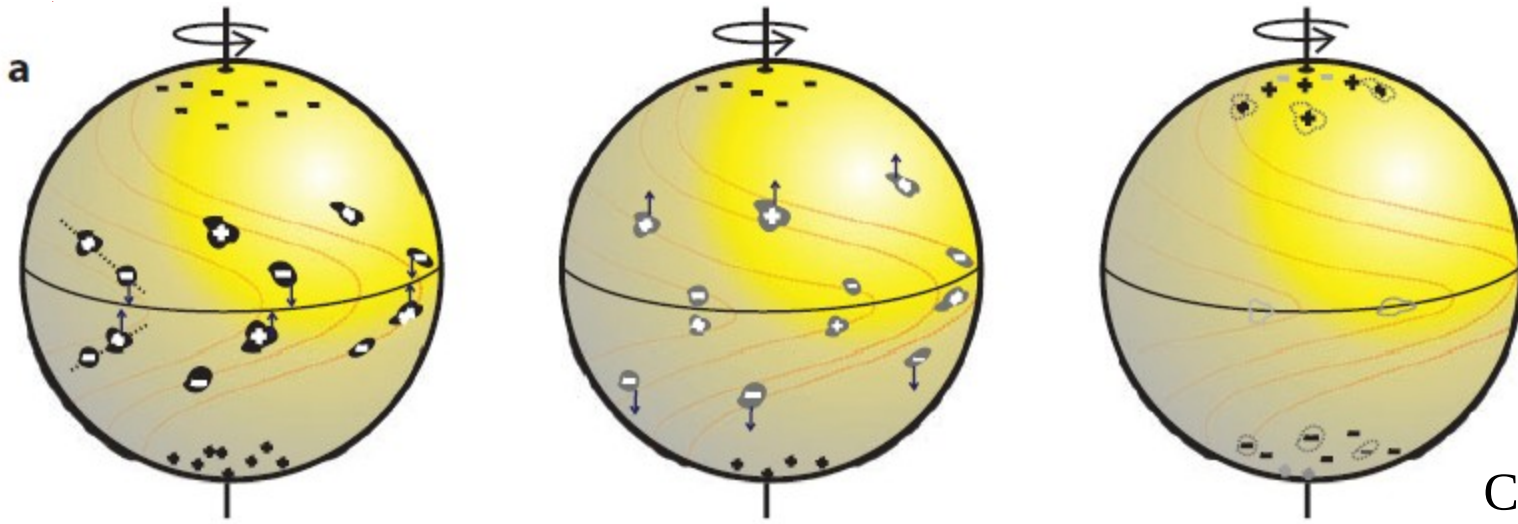
-- fluctuations in dynamo parameters are naturally invoked to explain the origin of grand minima.

Turbulence also introduces “magnetic noise” that affects the mean electromotive force directly (Brandenburg & Spiegel 2008).

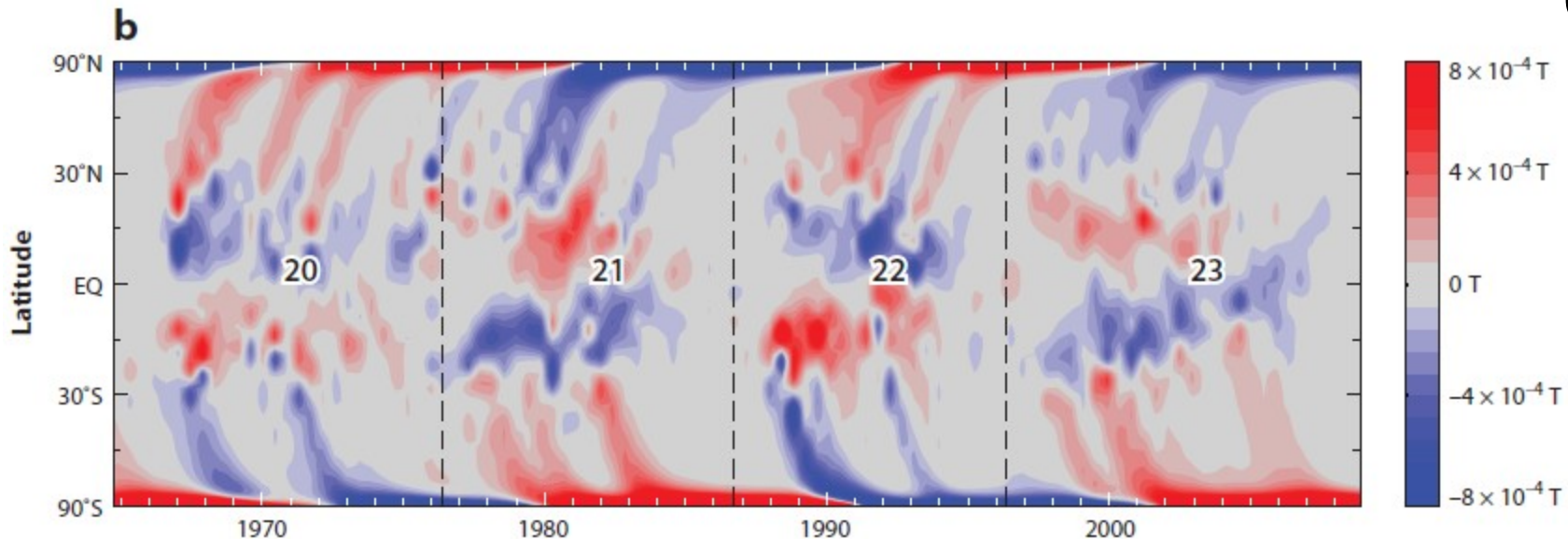
# Fluctuations in flux transport dynamo model:

## Poloidal field generation:–Babcock–Leighton alpha effect:

(Babcock 1961; Leighton 1969; Dasi-Espuig et al. 2010; Munoz-Jaramill



From  
Charbonneau  
(2014)



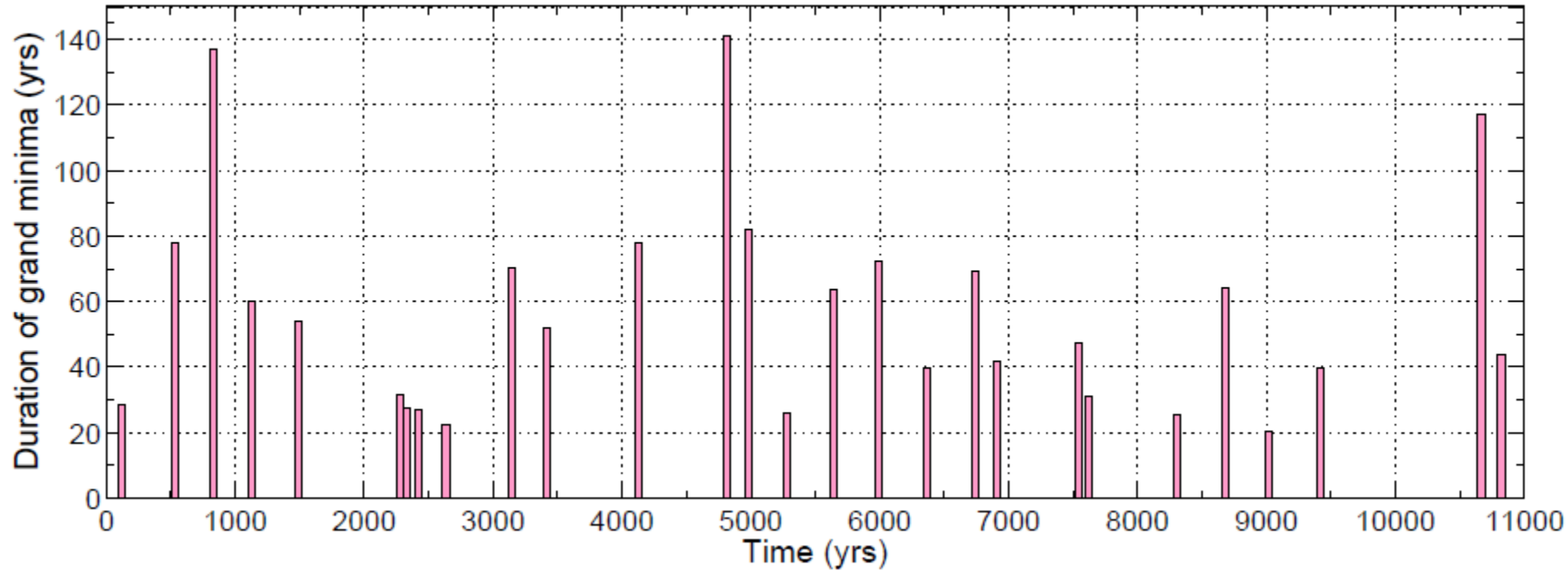
# Possible mechanisms for producing grand minima under flux transport dynamo model

Fluctuations in Babcock-Leighton process may make the poloidal field weak (Charbonneau et al. 2004; Choudhuri & Karak 2009, 2012; Passos et al. 2014)

Fluctuations in meridional circulation may make it very weak (Karak 2010; Karak & Choudhuri 2013)



# Results of simulation of grand minima (adding stochastic fluctuations in Babcock-Leighton $\alpha$ and meridional circulation)



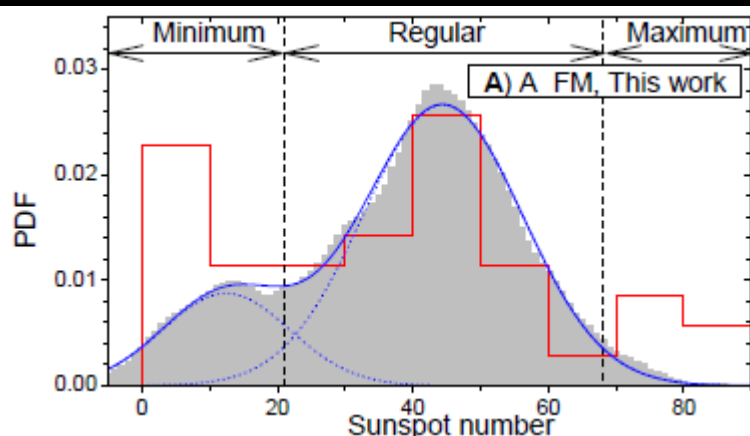
We get 20–30 grand minima in 11,000 years

Observational value = 27

LETTER TO THE EDITOR

## Evidence for distinct modes of solar activity<sup>★</sup>

I. G. Usoskin<sup>1</sup>, G. Hulot<sup>2</sup>, Y. Gallet<sup>2</sup>, R. Roth<sup>3</sup>, A. Licht<sup>2</sup>, F. Joos<sup>3</sup>, G. A. Kovaltsov<sup>4</sup>, E. Thébault<sup>2</sup>, and A. Khokhlov<sup>2,5</sup>



**Results.** The distribution of solar activity is clearly bi-modal, implying the existence of distinct modes of activity. The main regular activity mode corresponds to moderate activity. The existence of a separate Grand minimum mode with reduced solar activity, which cannot be explained by random fluctuations of the regular mode, is confirmed at a high confidence level.

**Conclusions.** The Sun is shown to operate in distinct modes – a main general mode, a Grand minimum mode corresponding to an inactive Sun, and a possible Grand maximum mode corresponding to an unusually active

# Grand minima in 3D MHD simulations???

Periodic box,  
imposed  
large-scale  
shear,

turbulence is  
generated  
artificially  
by helically  
forced flow.

$$\frac{DU}{Dt} = -SU_x \hat{y} - c_s^2 \nabla \ln \rho + \rho^{-1} [\mathbf{J} \times \mathbf{B} + \nabla \cdot (2\rho\nu \mathbf{S})] + \mathbf{f}, \quad (2)$$

$$\frac{D \ln \rho}{Dt} = -\nabla \cdot \mathbf{U}, \quad (3)$$

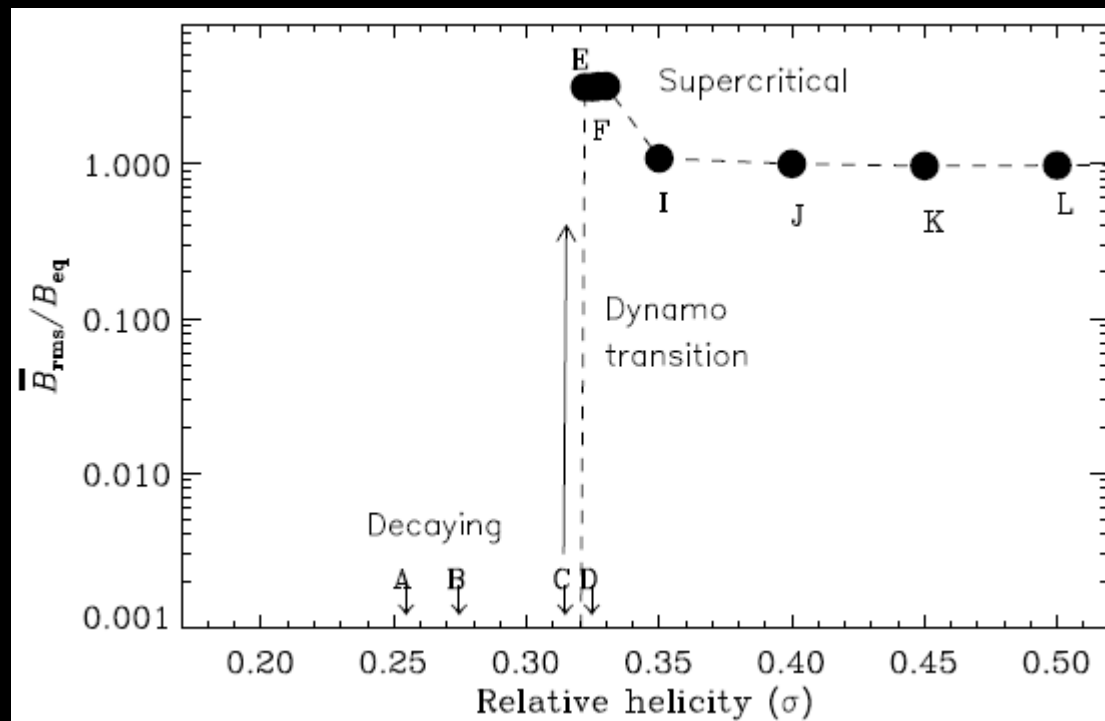
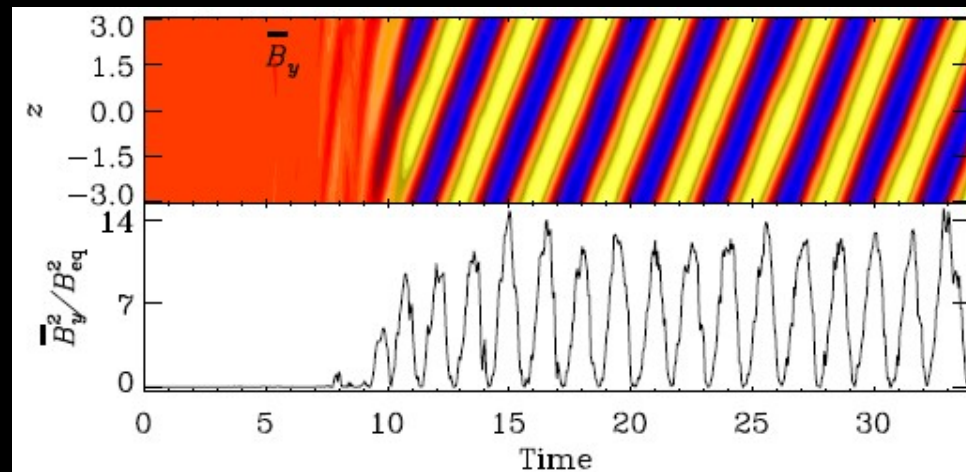
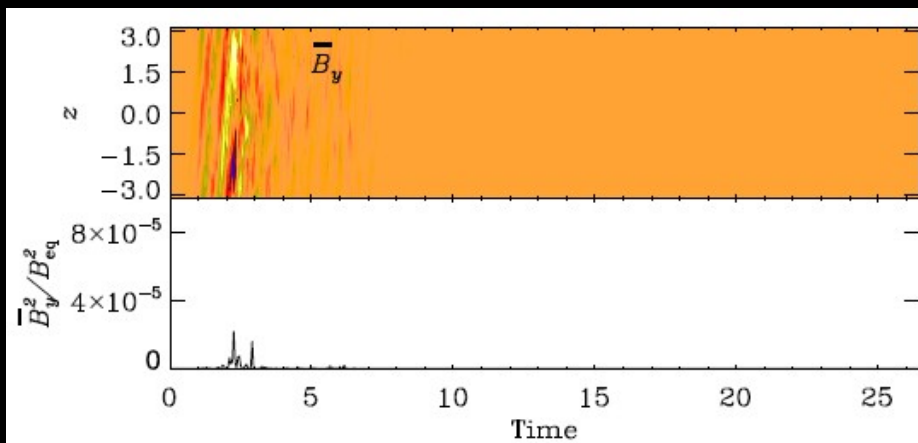
$$\frac{\partial \mathbf{A}}{\partial t} + \overline{\mathbf{U}}^{(S)} \cdot \nabla \mathbf{A} = -S A_y \hat{x} + \mathbf{U} \times \mathbf{B} + \eta \nabla^2 \mathbf{A}. \quad (4)$$

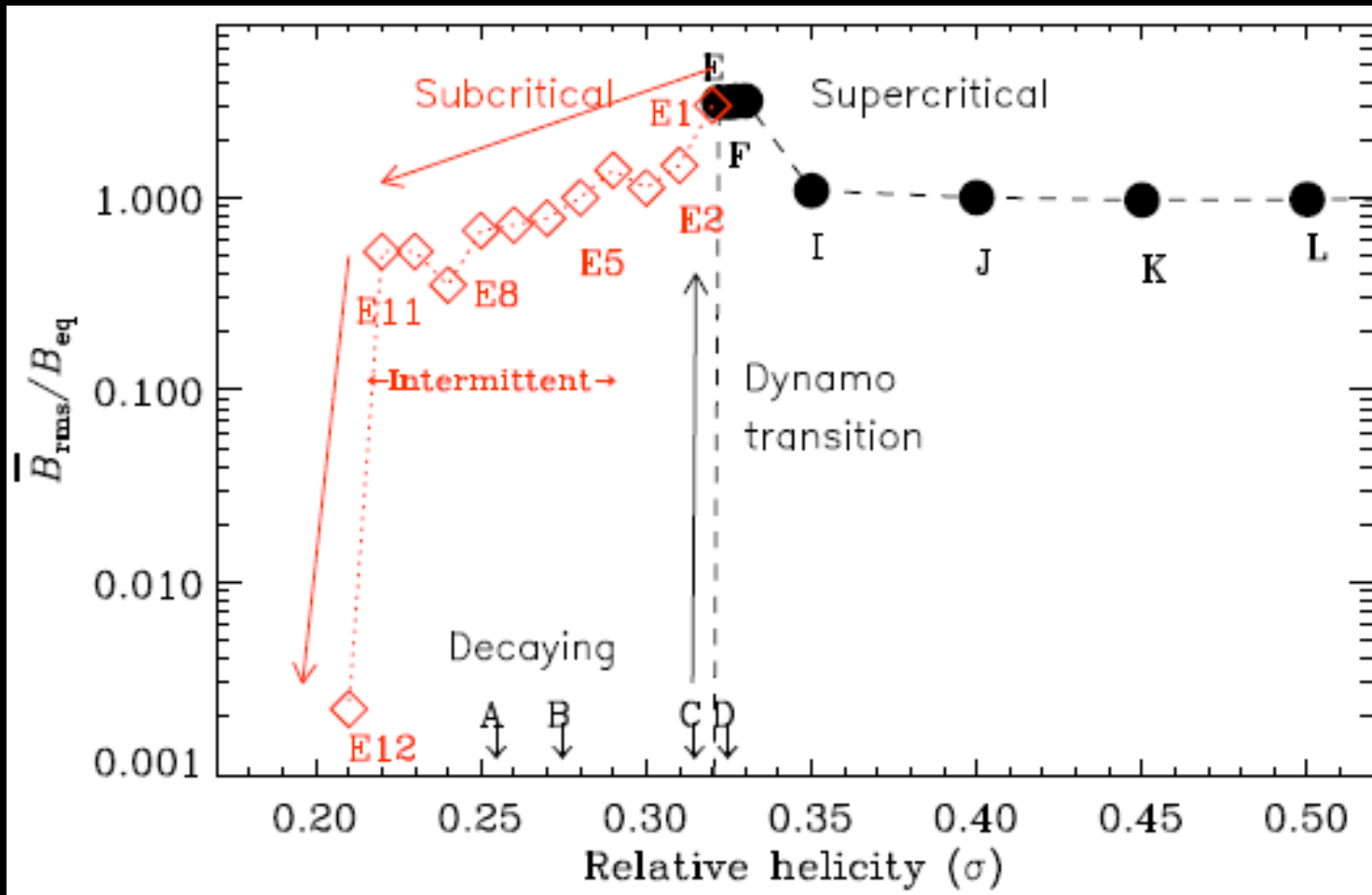
$$\mathbf{f}(\mathbf{x}, t) = \text{Re}\{N \mathbf{f}_{\mathbf{k}(t)} \exp[i\mathbf{k}(t) \cdot \mathbf{x} + i\phi(t)]\}$$

$$\mathbf{f}_{\mathbf{k}} = \mathbf{R} \cdot \mathbf{f}_{\mathbf{k}}^{(\text{nohel})} \quad \text{with} \quad R_{ij} = \frac{\delta_{ij} - i\sigma \epsilon_{ijk} \hat{k}_k}{\sqrt{1 + \sigma^2}}$$

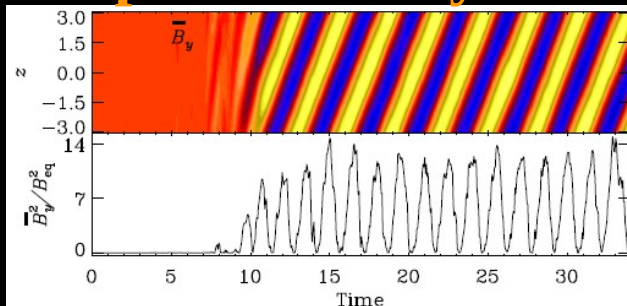
Here  $D/Dt = \partial/\partial t + (\mathbf{U} + \overline{\mathbf{U}}^{(S)}) \cdot \nabla$  is the advective time derivative,  $\overline{\mathbf{U}}^{(S)} = (0, Sx, 0)$  with  $S = \text{const}$  is the

# Results





## Supercritical dynamo



Karak, Kitchatinov & Brandenburg (2015)

**Turbulent transport coefficients are quenched due to magnetic field --**

From quasi-linear approximation (Rudiger & Kitchatinov 1993; Kitchatinov et al. 1994)

**Also seen in simulations: Karak et al. (2014b)**

$$\eta_T = \eta \phi_\eta(B), \quad \alpha_T = \alpha \phi_\alpha(B)$$

$$\phi_\alpha(B) = \frac{15}{32B^4} \left[ 1 - \frac{4B^2}{3(1+B^2)^2} - \frac{1-B^2}{B} \operatorname{arctg}(B) \right]$$

$$\phi_\eta(B) = \frac{3}{8B^2} \left[ 1 + \frac{4+8B^2}{(1+B^2)^2} + \frac{B^2-5}{B} \operatorname{arctan}(B) \right]$$

$$D = \frac{\alpha_T \Omega R^3}{\eta_T^2}$$

# Effective dynamo number versus magnetic field

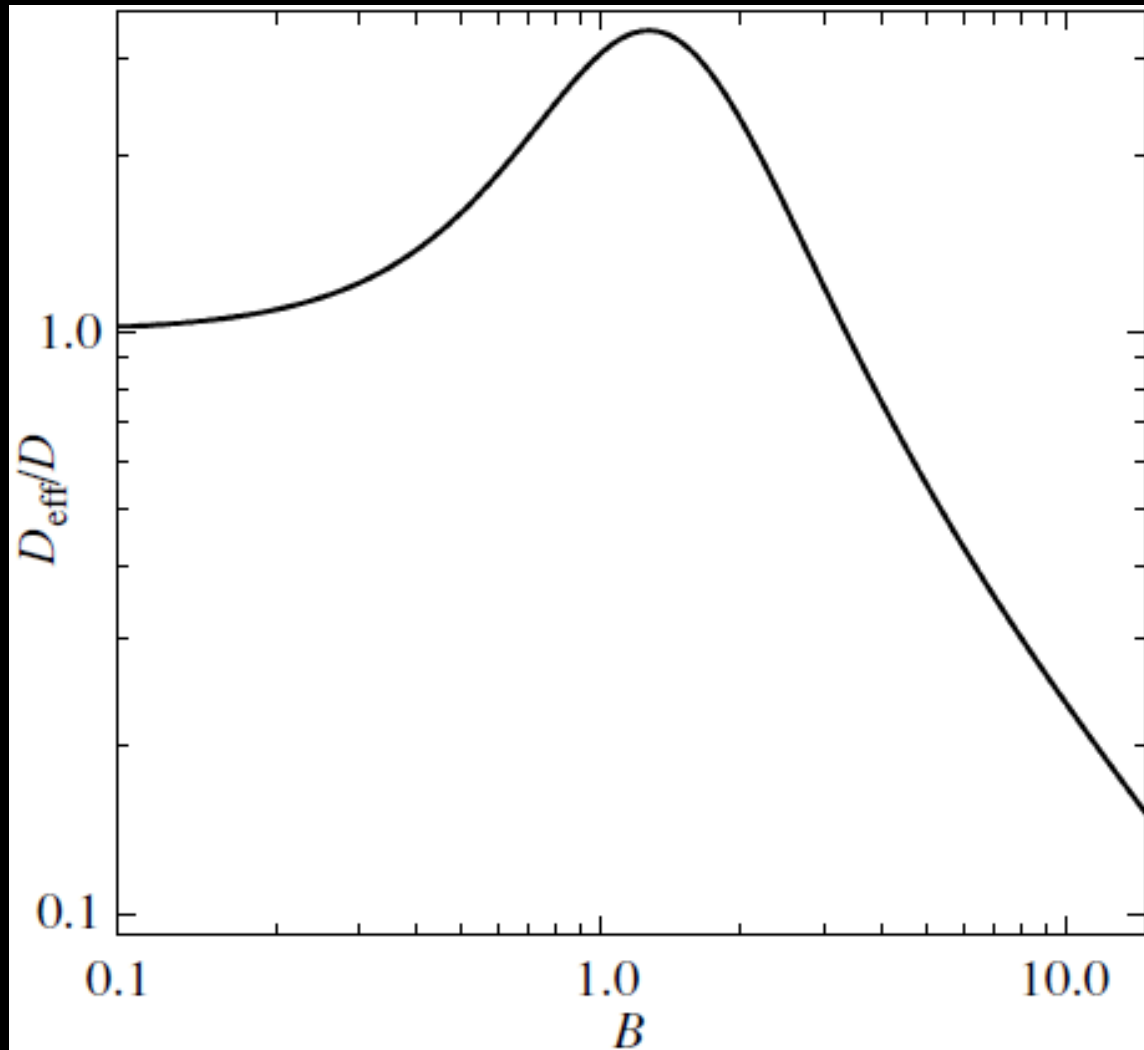


Fig. 1.  $D_{\text{eff}}/D = \phi_{\alpha}(B)/\phi_{\eta}^2(B)$  versus magnetic field. In the region of weak fields,  $D_{\text{eff}}$  increases with  $B$ .

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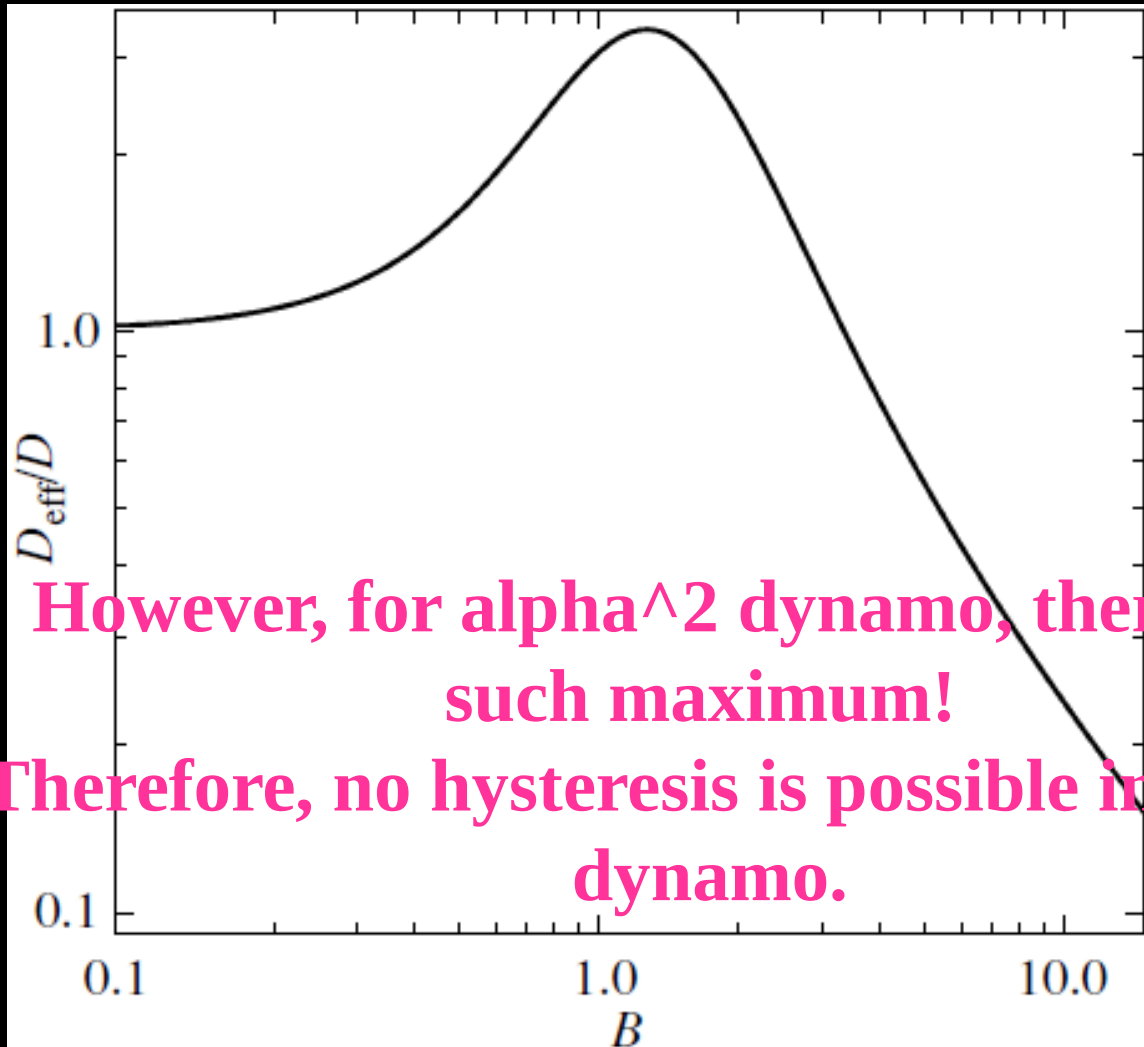


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# Dynamo hysteresis observed in mean-field model with quenching in turbulent transport coefficients

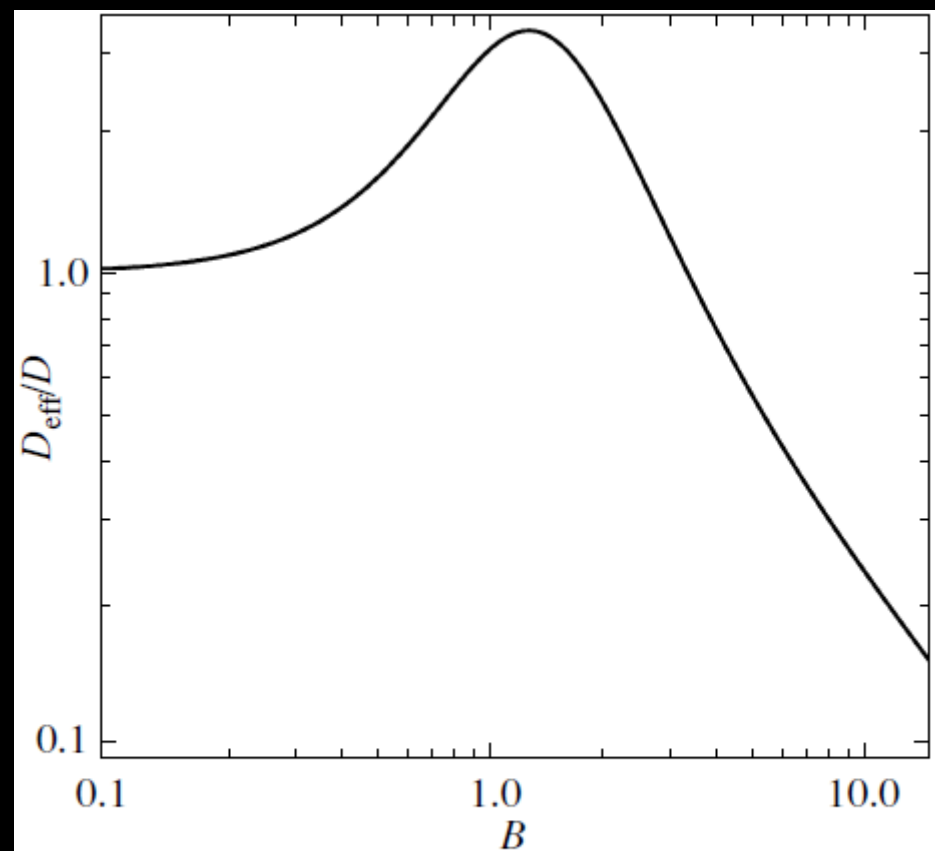
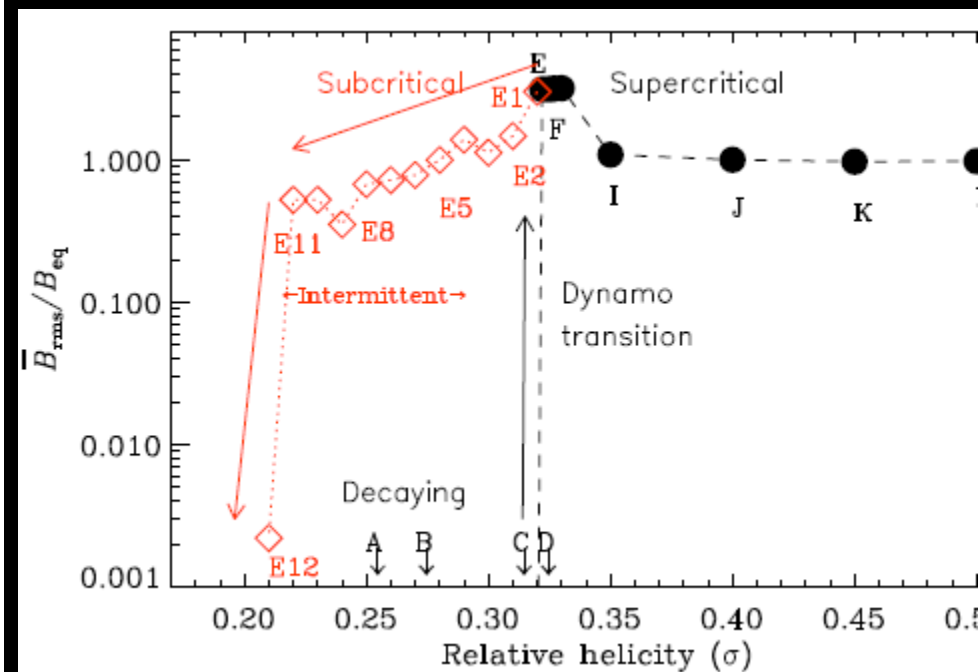
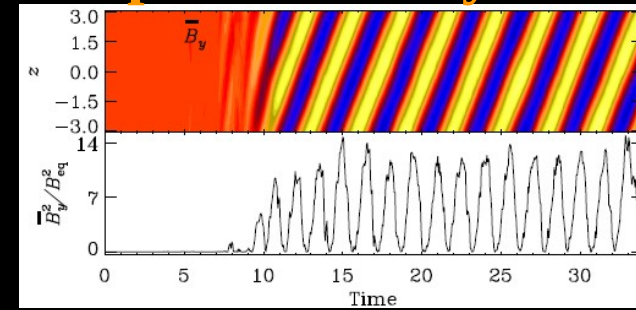


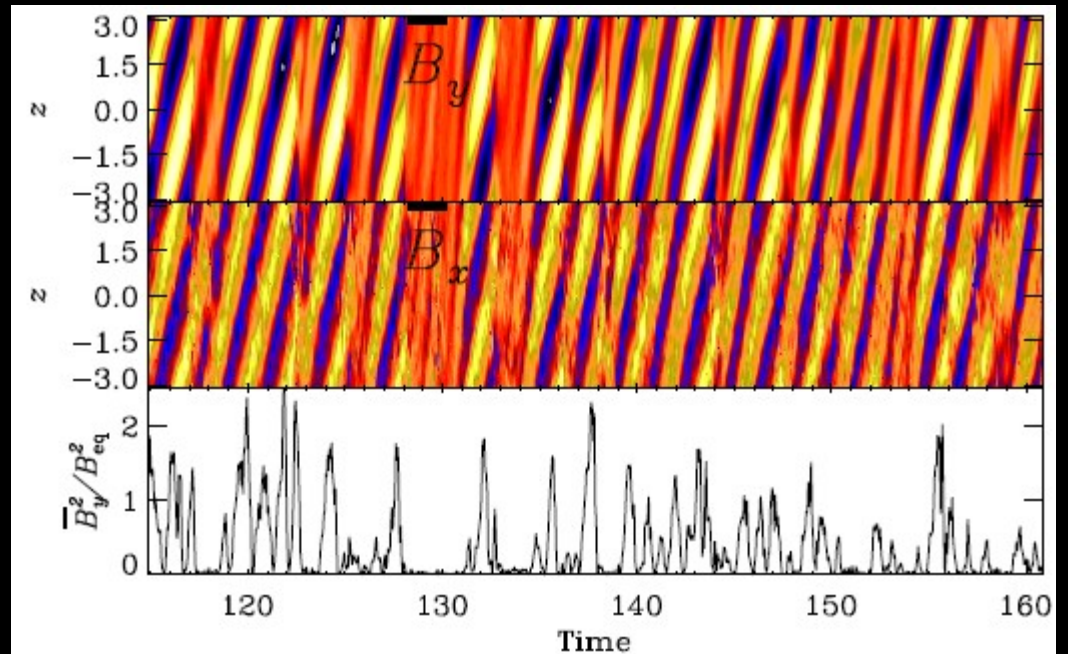
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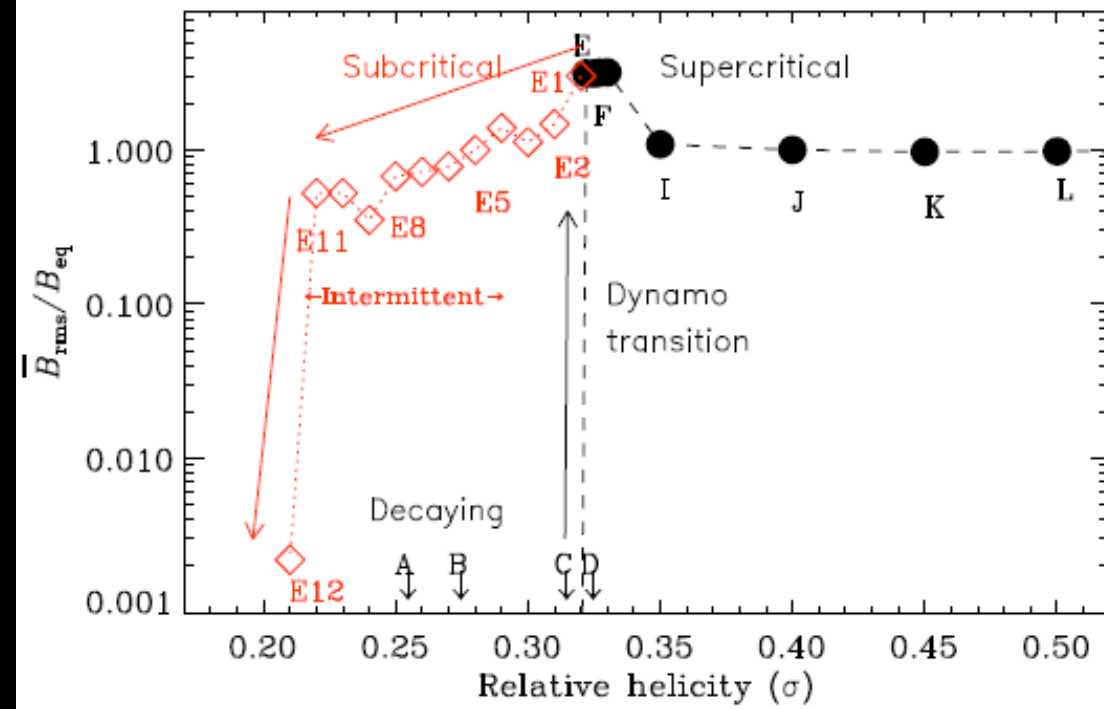
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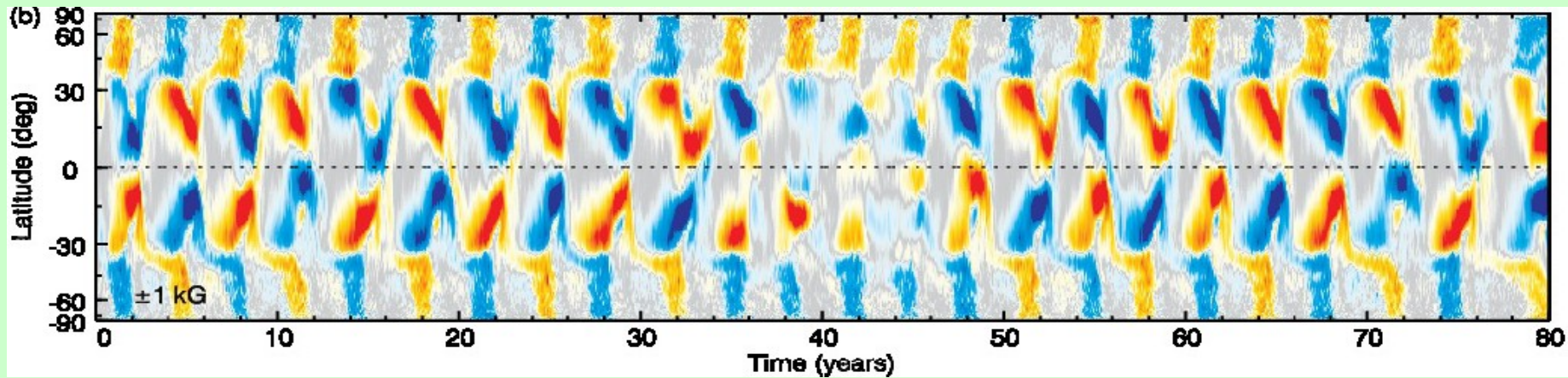
# Intermittent



Karak, Kitchatinov &  
Brandenburg (2015)



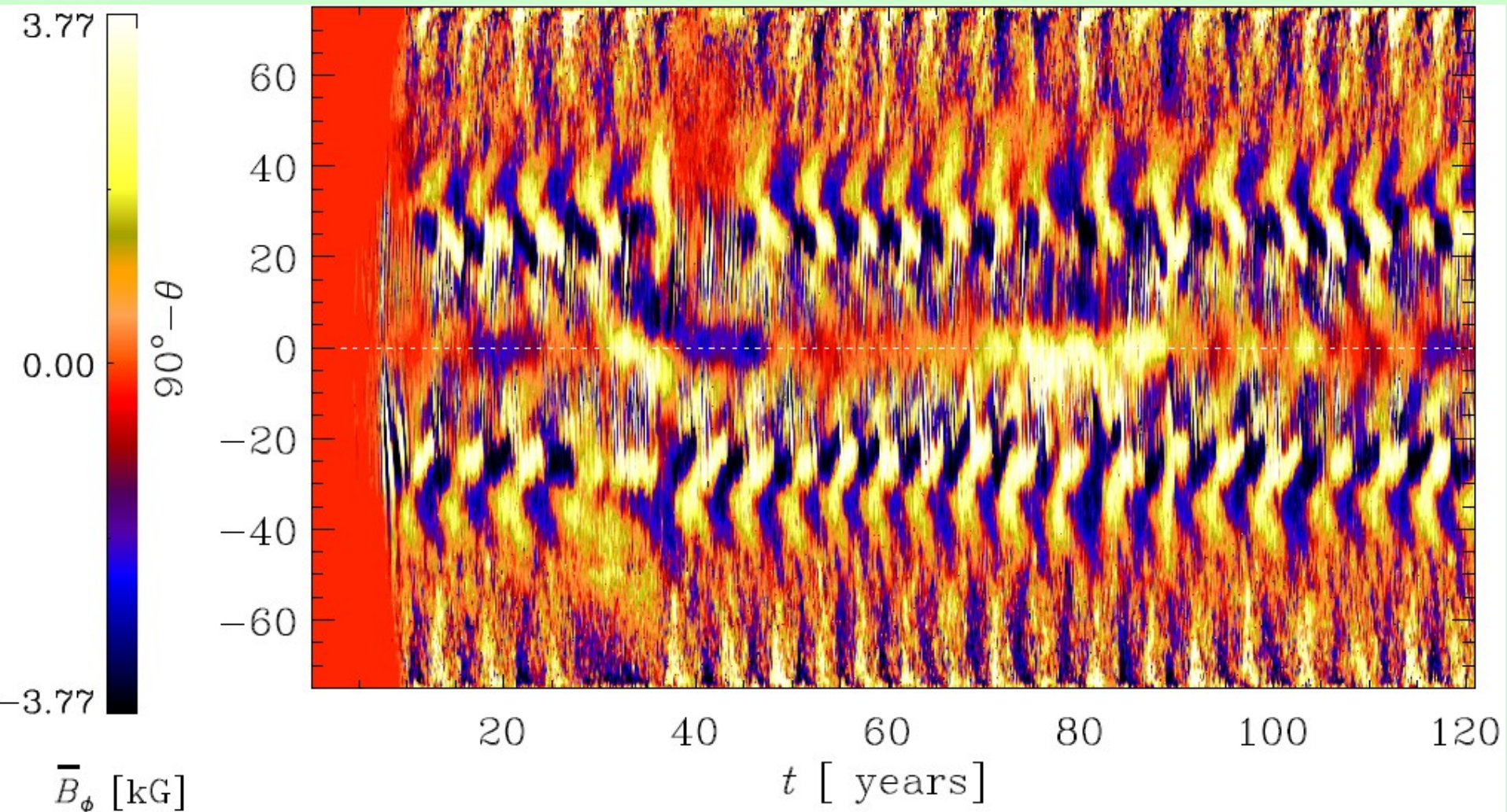
**People started seeing “grand minima-like” events in more realistic spherical global convection simulation!**



Augustson et al. (2014)



# “Grand minima-like” events in more realistic spherical global convection simulation



Kapyla et al. (in preparation)

# Conclusion

**1. We have found the evidence of dynamo hysteresis in turbulent simulations.**

**2. We have shown the intermittent magnetic cycles (which somewhat resembles the grand minima observed in Sun) in 3D simulations.**

**Intermittent magnetic cycle are only observed near the critical dynamo number only.**

**3. Two distinct modes of solar activity found in simulations are relevant to recently found in observations by Usoskin et al. (2014).**

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**Thank you**