

Electroweak Baryogenesis

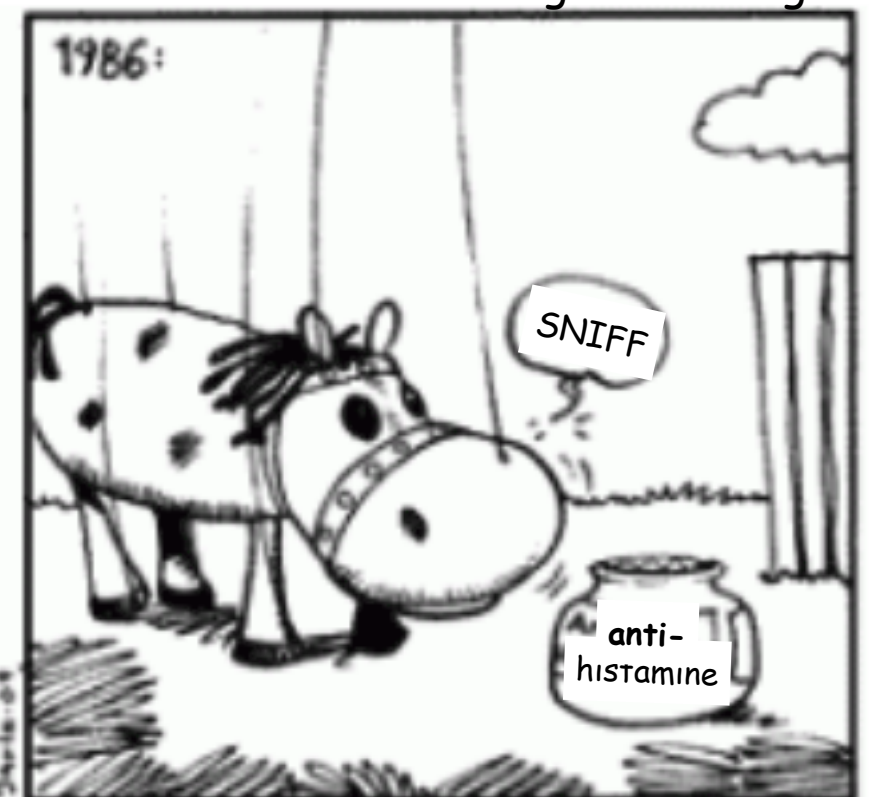


Kimmo Kainulainen
University of Jyväskylä,
Finland

**2015 The Spacetime
Odyssey Continues**

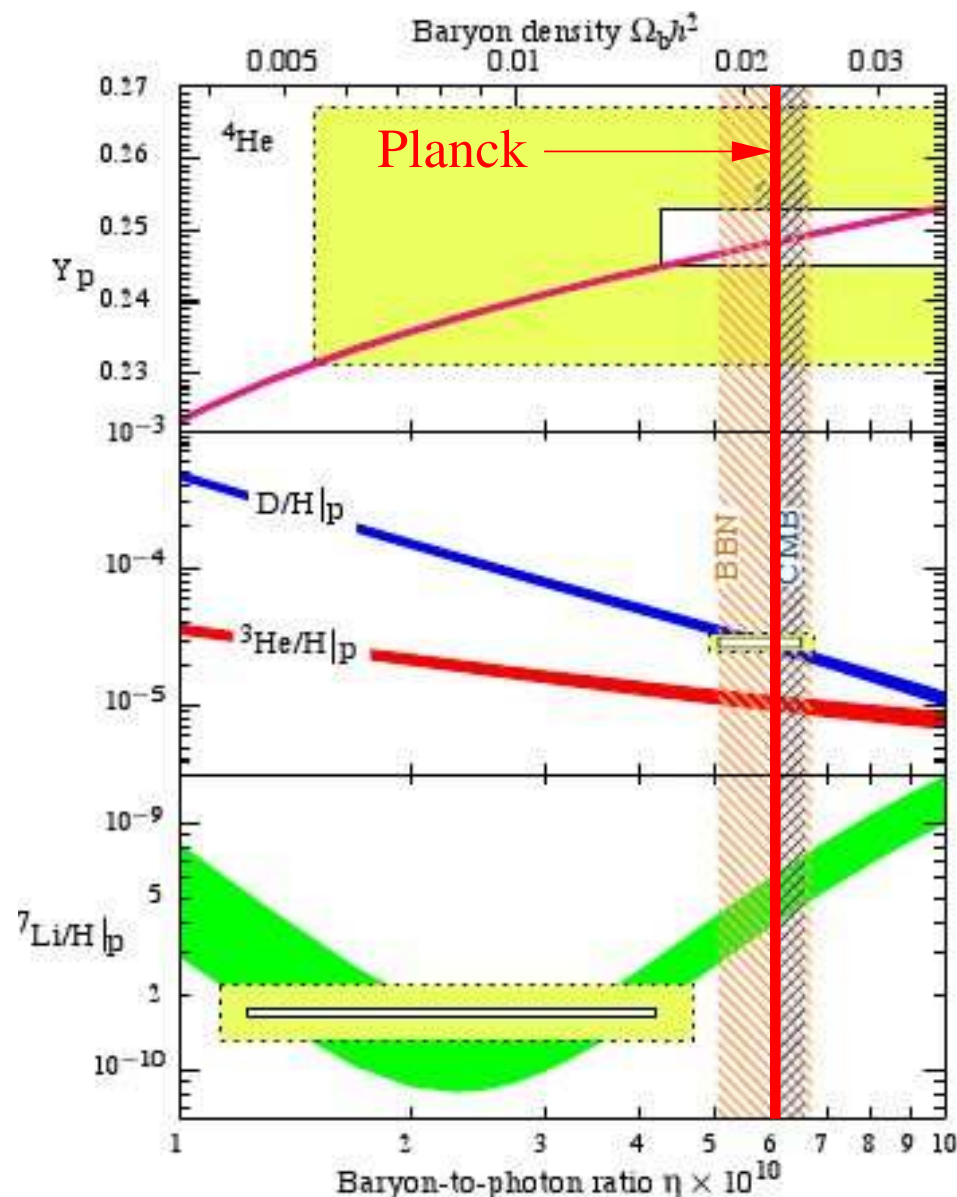
NORDITA, 6.5.2015

Favourite TV-horse gone missing...



Translated from Finnish, a comic strip by Pertti Jarla

Baryon asymmetry



$$\Omega_b h^2 = 0.02225 \pm 0.00016$$

P.Ade et al, ArXiv:1502.01589
(Planck 2015 Cosmological Parameters)

Because of **Inflation**,
this **cannot be initial condition**.

Tensors:

$$T_{\text{BAU}} < 1.7 \times 10^{16} \left(\frac{r}{0.2} \right)^{1/4} \text{ GeV}$$

This leaves a fair amount of room to play:

$$100 \text{ GeV} < T_{\text{BAU}} < 10^{16} \text{ GeV}$$

Baryon asymmetry / mechanisms

Sakharov




- Electroweak baryogenesis
 - MSM, MSSM, NMSSM, 2HDM, SSM,...
- Leptogenesis
 - non-resonant
 - resonant
- Warm, Cold, WIMPy, Dark, ...
Affleck-Dine mechanism,
from GUT, neutrino oscillations,
higher dimension operators,
inflation, preheating,

$T_{\text{EWBG}} \approx 100\text{GeV}$: works at the **lowest possible energy**: By far most **TESTABLE!**

EWBG in a nutshell

$$H \sim 10^{-14} T_{100}^2 \text{ GeV} \quad \begin{matrix} \text{1st} \\ \text{order} \end{matrix} \rightarrow$$

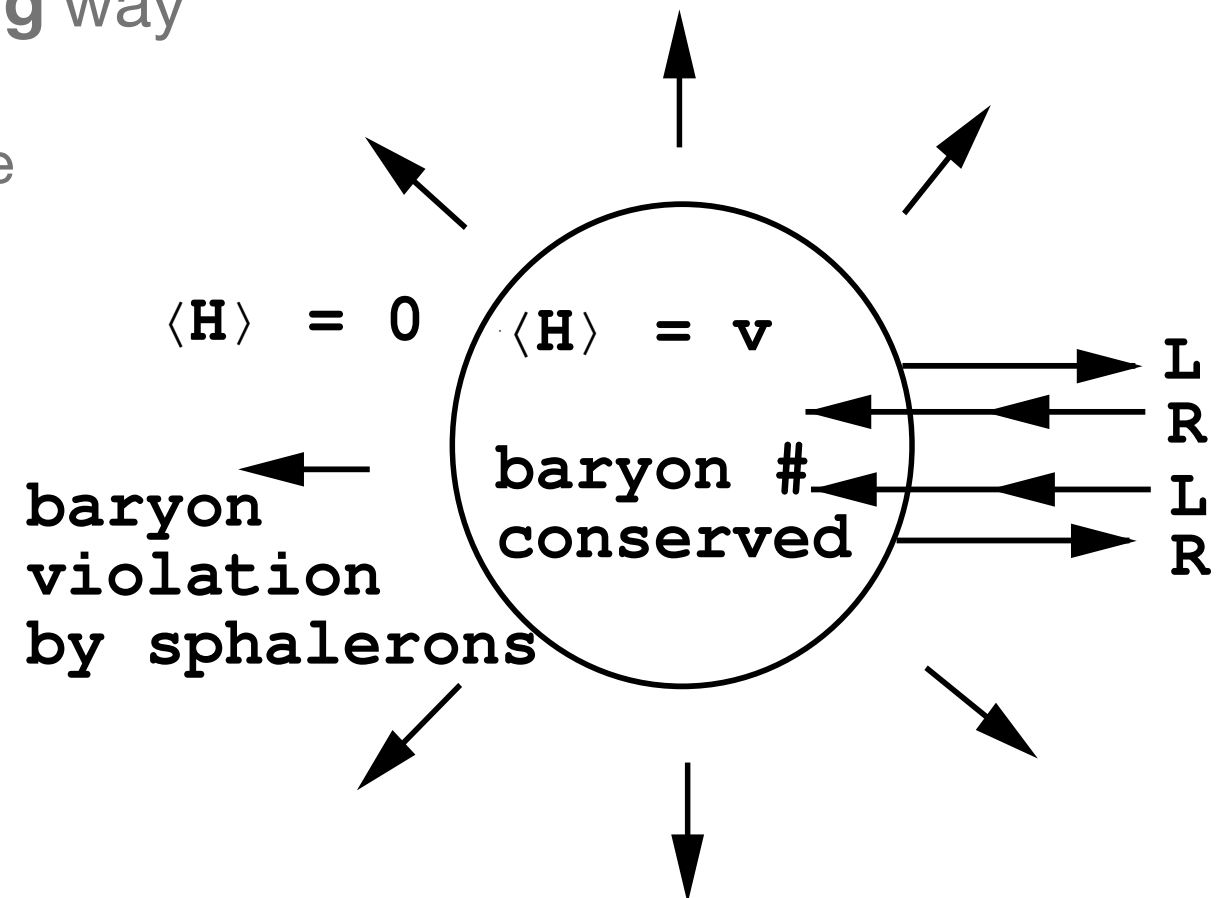
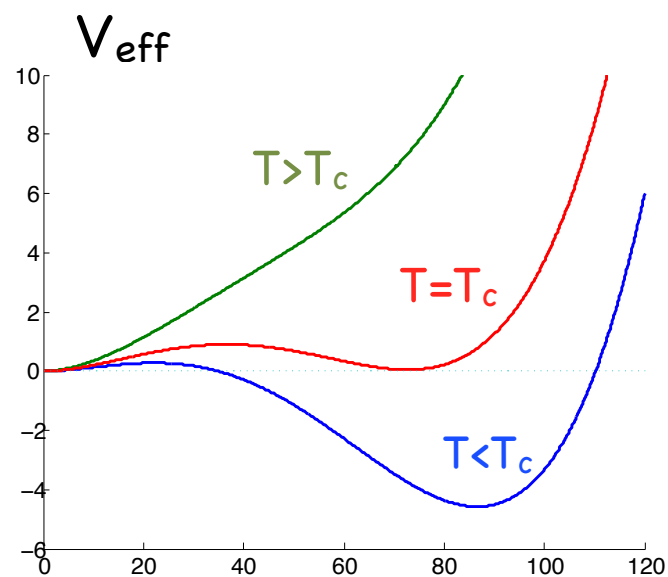
$$\Gamma \sim 10^{-5} T_{100} \text{ GeV} \quad \text{PT}$$


1st order PT at $T_c \sim 100 \text{ GeV}$.

bubbles of **true vacuum**, $\langle H \rangle \neq 0$, form and start expanding into the **false** symmetric **vacuum**.

Particles interact with wall in **CP violating** way

Baryon asymmetry forms inside the bubble



EWBG, A SLIGHTLY BIGGER NUTSHELL

To keep BA

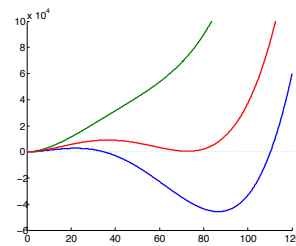
Sphaleron rate in the broken phase ... must be small

Kuzmin, Rubakov & Shaposhnikov, Arnold & McLerran, ... Moore; Rummukainen et al;

- From V_{eff} compute

$$\left(\frac{v(T_c)}{T_c} \right)_{\text{Landau}} > 1$$

H.H.Patel, M.J.Ramsey-Musolf, C.Wainwright, S.Profumo
JHEP 07 (2011) 029; PRD84 (2011) 023521; PRD86 (2012) 083537.
M.Garny and T.Konstandin, JHEP1207 (2012) 189,

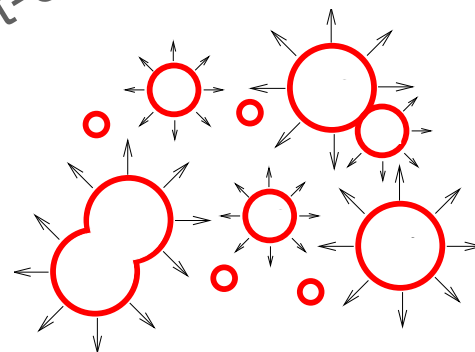


- Dim. reduction to a 3D-Higgs-gauge theory simulated in Lattice

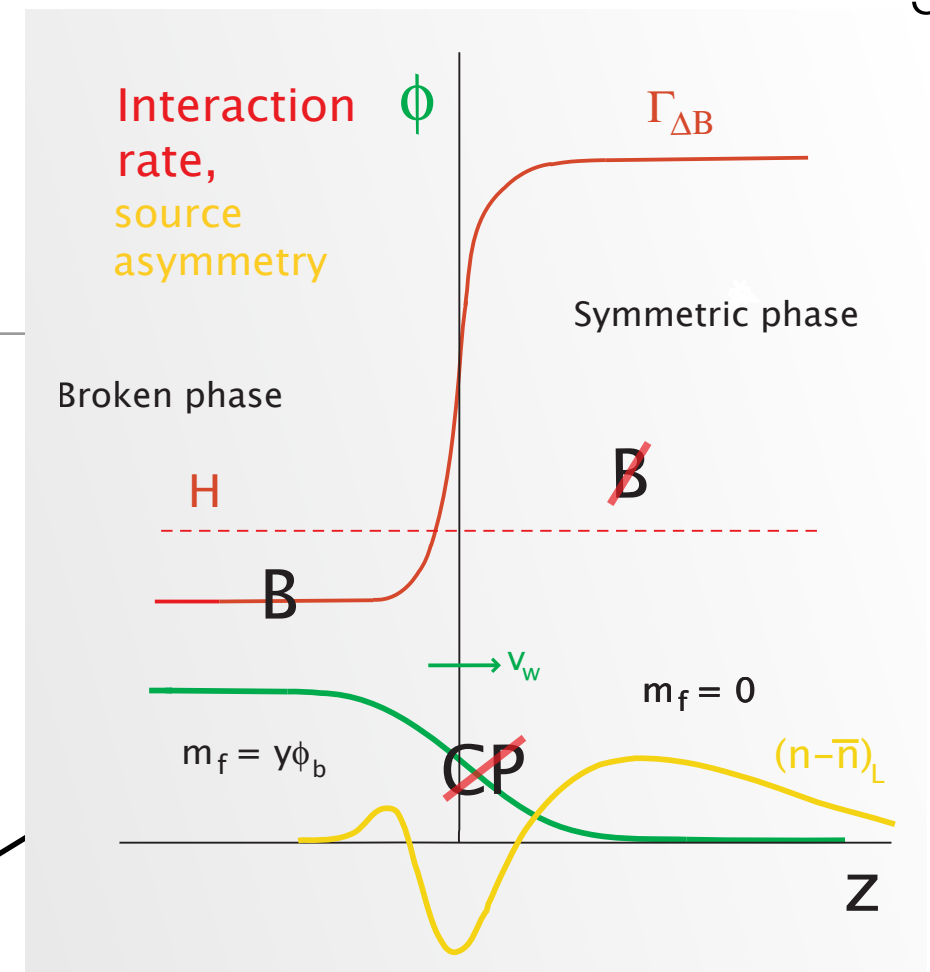
K.Kajantie, M.Laine, K.Rummukainen and M.E.Shaposhnikov,
NPB458 (1996) 90; NPB466 (1996) 189;
PRL77, 2887 (1996)....

2-loop V_{eff} in LG ~OK

M.Laine, G.Nardini and
K.Rummukainen,
JCAP 1301 (2013) 011...



Equilibrium / Nonperturbative / Gauge issues
Mostly out-of-equilibrium / quantum



CP-violating **source** in **transport eqs.**

- Thin wall: **quantum** (cQPA) Herranen, KK, Rahkila,...
 - Thick wall SC: **SC force** Joyce, Prokopec, Turok, Cline, KK, Schmidt, Weinstock, Konstandin, ...
- "vev-insertion"**
Riotto, Carena, Quiros, Wagner, ...

(CP-even) dynamics of the expanding wall

Parametrized by v_w and $\phi(z)$

Kajantie et al,
Prokopec & Moore, John & Smith
Espinosa, Konstandin,
No & Servant (2010),...

Sphaleron rate in the symmetric phase

Ambjorn et al, ... Moore; Rummukainen et al, ...

To make BA

Short history of the EWBG

My most **sincere apologies** for the many, **many** people who did not get mentioned here despite their work of great importance !

B-violation in SM

't Hooft -76
Klinkhamer, Manton -84

1985

Kuzmin, Rubakov, **Shaposhnikov**,
fast B at high T in SM

1987

Arnold, McLerran,...

Affleck-Langer, broken phase

$$\Gamma \sim Ae^{-E/T}$$

1990

Ambjørn, Krasniz, Shaposh...
first **Lattice** results (symm.ph)

$$\Gamma \sim \# \alpha^4 T$$

-

200n

Rummukainen, Laine,
Moore, Bödeker,...

ChS-# diffusion in Lattice,
HTL, Langevin eqs,...

$$\Gamma \sim \# \alpha^5 T$$

Rummukainen, Moore,...

updates

Ramsey-Musolf,
Garny Konstandin,

gauge dep.

Rlotto,...

B-dependence,...

2014

Rummukainen, d'Onofrio,
Tranberg: definite results **SM-Lattice**

Transition strength

197n

Weinberg,Jackiw,Kiritsis,Linde,Niemi,Semenoff,...

FTFT, $V_{\text{eff}}(\phi, T)$

1992

Carrington: **$V_{\text{eff}}(\phi, T)_{\text{SM}}$**

1993 -

Arnold, O.Espinosa, Buchmuller

Fodor, ... **EWPT industry using V_{eff}**

TOP

Kajantie, Rummukainen,
Laine, Shaposhnikov:

DR+Lattice => SM dead

1996

LSS in MSSM,

Carena, Quiros, Wagner, J.R.Espinosa, ... (V_{eff})

Cline, KK, Rummukainen, Laine, Losada...

DR+Lattice

2000

2000-

MSSM / phenomenology

Carena, Quiros, Wagner, Nardini,...

Rummukainen, Laine, ...

constraints on **LSS getting worse...**

2011

J.R.Espinosa, Gripaios, Konstandin, Riva:

strong 2-step trans. in SM+S

2012

HIGGS

Renewed interest on

NMSSM, 2HDM's, SM+S,
portals,...

Baryon creation, QKE's

1990

Cohen, Kaplan, Nelson
spontaneous BG, ...

1993-4

Farrar, Shaposhnikov,

Gavela, Hernandez, Orloff, Pene,...

Quantum Reflection

1994

M.Joyce, T.Prokopec, N.Turok,

Cline, KK, MJ, TP, Schmidt, Konstandin...

Semiclassical force BG

WKB / CTP $S_{\text{CP}}(z)$

-2002

1996

Riotto, Carena, Quiros, Wagner,...

"vev-insertion method",
also from **CTP**

... Profumo, Ramsey-Musolf, Tulin,...

-200n

2003-

CTP mostly used to
develop **QKE's** for
(resonant)

Leptogenesis

Pilaftisis et al,

Buchmuller et al, Garny et al,

Garbrecht et al, Herranen et al,

(Morrissey, Ramsey-Musolf, ...

Prokopec, Konstandin, ...

Flavour mixing ...)

~2010-

~2009-

cQPA combines **SCBG**

and **QR**, using **CTP**

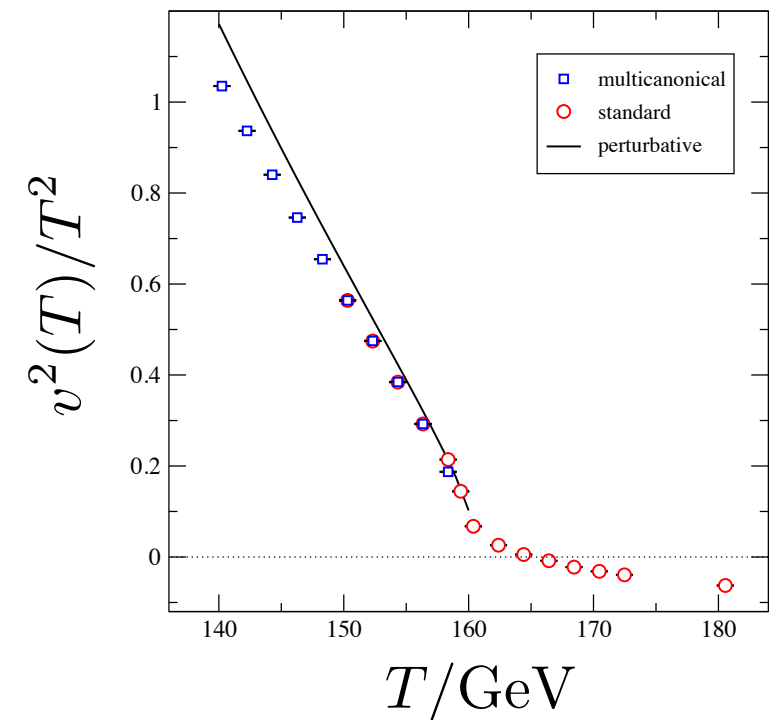
Herranen, KK, Rahkila

EWPT and B-violation in the SM; latest results

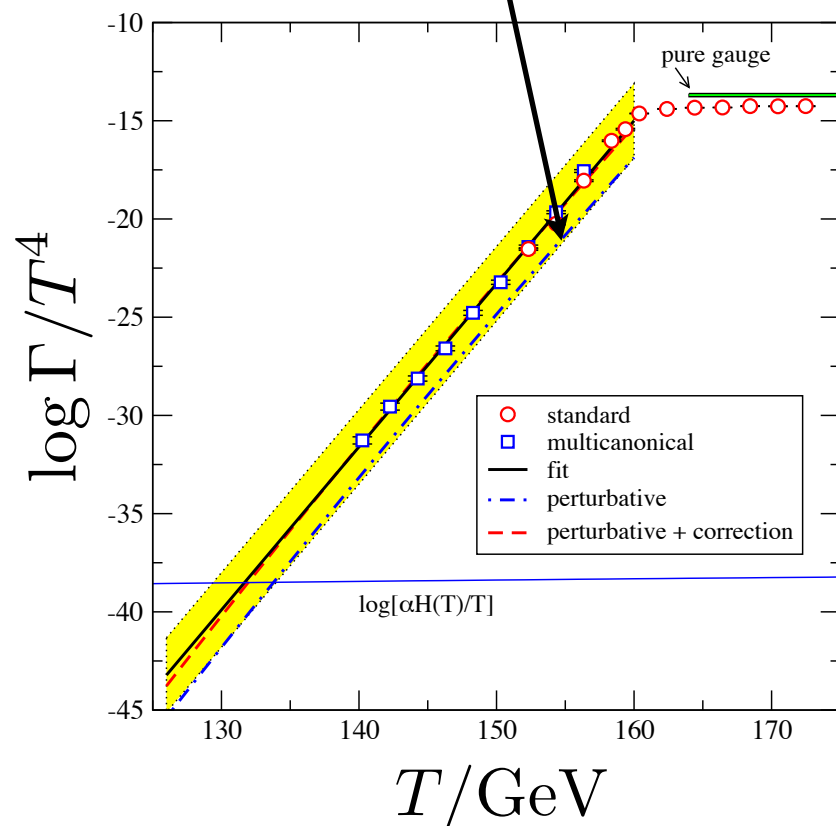
PT in SM, is a *cross-over* with

$$T_c \approx 160 \text{ GeV}$$

K.Rummukainen, M.d'Onofrio and A.Tranberg, PRL113.141602



Perturbative result Y.Burnier, M.Laine & M.Shaposhnikov,
JCAP 0602 (2006) 007



Sphaleron rate in SM

$$\Gamma_{\text{Symm.}}/T^4 = (8.0 \pm 1.3) \times 10^{-7} \approx (18 \pm 3)\alpha_W^5.$$

$$\log \frac{\Gamma_{\text{Broken}}}{T^4} = (0.83 \pm 0.01) \frac{T}{\text{GeV}} - (147.7 \pm 1.9).$$

Sphalerons drop out of eq. in broken phase when

$$\Gamma(T_*)/T_*^3 = \alpha H(T_*)$$

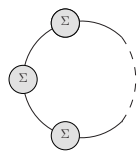
eg:

$$T_* = (131.7 \pm 2.3) \text{ GeV}$$

Models with a strong PT / Loop corrections / MSSM

Most effort has been put to **increase the effective cubic coupling by loop corrections**

Need new **light** ($m_i < T$) **bosonic** fields strongly coupled to Higgs



$$\delta V_{\text{eff}} = - \sum_i \frac{T m_i^3(\phi, T)}{12\pi} + \dots$$

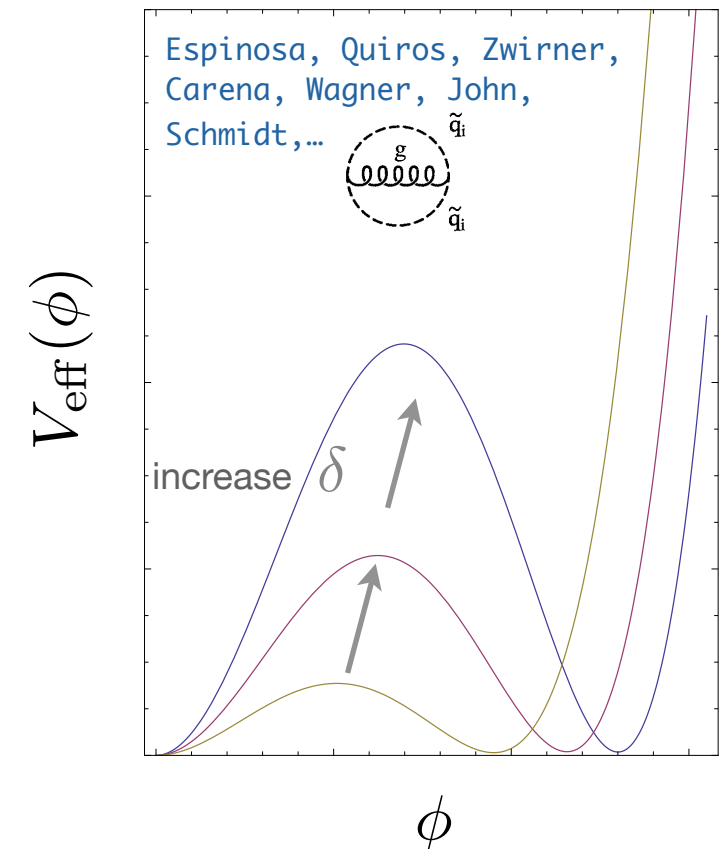
=> **Light Stop Scenario** in the MSSM

[Carena, Quiros, Wagner (1996), ...]

However, also higgs mass mostly from

$$m_h^2 \sim y_t^2 \log \frac{m_{t_R}^2 m_{t_L}^2}{m_t^4}$$

Tension: light t_R => **very** heavy t_L
eg. a very large SUSY breaking m_0



ALSO, to keep $m_{\text{stop}}(T)$ small need

Heavy gluino: $m_g > 500$ GeV

Small or negative m_R => $m_{\text{stop}} < \approx m_{\text{top}}$

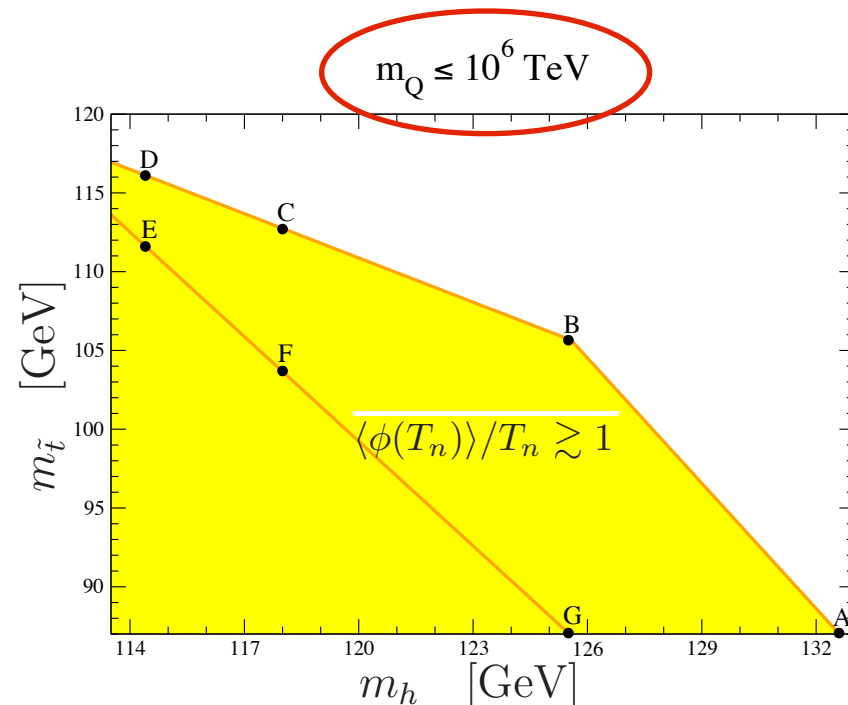
and danger of colour-breaking

etc (EDM's) ... ==> **Effective LSS / MSSM theory with only the light stop and a light neutralino.**

MSSM-EWBG: *alive (?) but perhaps not so well*

RGE-improved low energy eff. th.
Allow *metastability* against color breaking...

$$m_h \leq 127 \text{ GeV}, \quad m_{\tilde{t}_R} \leq 120 \text{ GeV}$$



Carena, Nardini, Quiros & Wagner, 2009

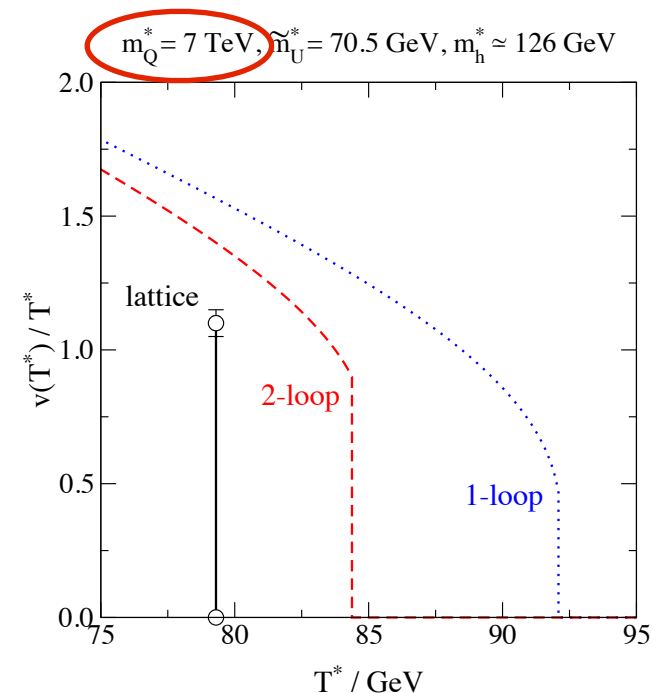
LHC: Stop mass bounds generically $m > \text{few} \times 100 \text{ GeV}$
Stop-enhanced $H \rightarrow gg$ -fusion

One can get around these if there is
a light neutralino (bino) ($m < 60 \text{ GeV}$)

M.Carena, G.Nardini, M.Quiros & C.Wagner, 2013

Lattice + DR: 3D-theory contains also light squarks

$$m_h \approx 126 \text{ GeV} \quad m_{\tilde{t}_r} < 155 \text{ GeV}$$



Laine, Nardini and Rummukainen. 2013

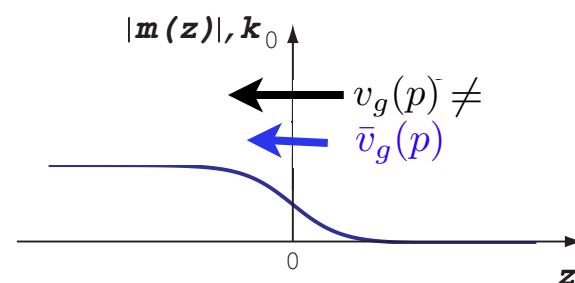
$$\left(\frac{v}{T_c} \right)_{\text{latt}} = 1.117(5) \quad \left(\frac{v}{T_c} \right)_{\text{Landau}} = 0.9$$

GOOD NEWS TO BRING HOME WITH:
Transition typically much stronger than
the (1-) loop calculations of V_{eff} indicate.

BAU generation, QKE's / SC force - QM reflection

Thick wall: SC force

$$\ell_w = 10 - 30 T^{-1}$$



$$(\partial_t + \mathbf{v}_g \cdot \partial_{\mathbf{x}} + \mathbf{F} \cdot \partial_{\mathbf{p}}) f_i = C[f_i, f_j, \dots].$$

$$v_g = \frac{p_0}{\omega} \left(1 + s_{CP} \frac{s|m|^2 \theta'}{2p_0^2 \omega} \right)$$

complex phase of m

$$F = -\frac{|m||m'|}{\omega} + s_{CP} \frac{s(|m|^2 \theta')'}{2\omega^2}.$$

 -force

M.Joyce, T.Prokopec, N.Turok, PRD53 2958 (1996); PRL75 1695 (1995); PRD53 2930 (1996).

J.M.Cline, M.Joyce and KK PLB417 (1998) 79; JHEP 0007 (2000) 018

J.M.Cline and K.Kainulainen, PRL85 (2000) 5519.

KK, T.Prokopec, M.G.Schmidt and S.Weinstock, JHEP 0106, 031 (2001);

PRD66 (2002) 043502. T.Prokopec, M.G.Schmidt and S.Weinstock,

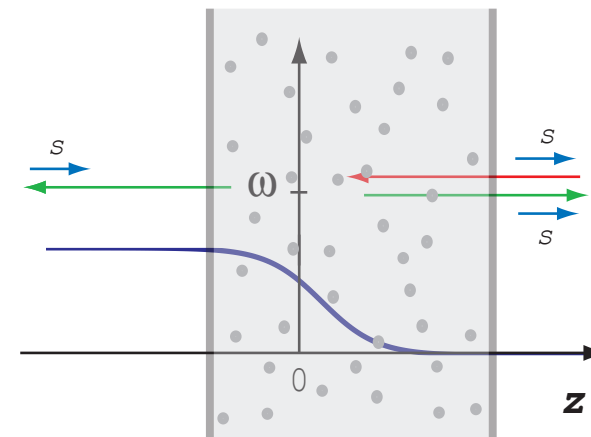
Ann.Phys.314 208 (2004), Ann.Phys.314, 267 (2004).

T.Konstandin, T.Prokopec and M.G.Schmidt, NPB716 (2005) 373; NPB738 (2006) 1

V.Cirigliano, C.Lee, M.J.Ramsey-Musolf and S.Tulin, PRD81 (2010) 103503.

Thin wall: quantum reflection

$$\ell_w = \text{few } T^{-1}$$



Collisionless case:

$$(i \not{\partial}_u - m^\dagger P_L - m P_R) \psi(u) = 0.$$

Complex mass (matrix) =>



Sufficient CP-violation in the MSM CKM-matrix?

G.R.Farrar and M.E.Shaposhnikov, PRL70, 2833 (1993); PRD (199...

No, because of decoherence due to collisions

M.B.Gavela, P.Hernandez, J.Orloff and O.Pene, MPLA 9, 795 (1994)

Gavela, P. Hernandez, J. Orloff, O. Pene and C. Quimbay, NPB 430,

382 (1994) P.Huet and E.Sather, PRD51, 379 (1995).

But methods too rudimentary, need CTP/KB

QKE's, more advanced methods

Inclusion of quantum reflections into QKE's needs more sophisticated methods

A suitable method (**cQPA**) actually exists:

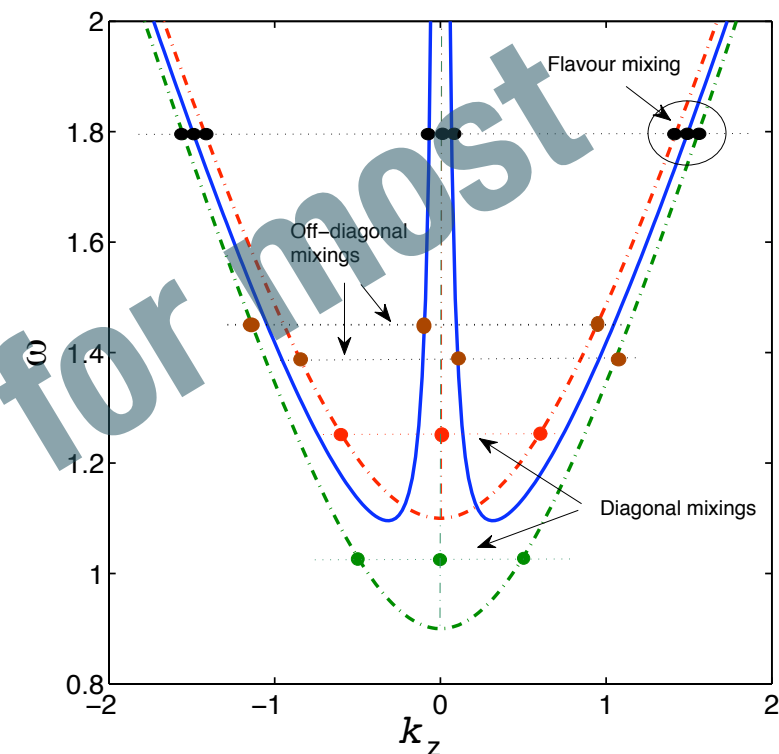
In planar symmetric problem, the **information about reflection coherence condenses to a set of new shell functions**

=> Extended Boltzmann type eqs. with coherence

Tested already in **homogeneous problems**

M.Herranen, KK & P.M Rahkila,
JHEP 0809 (2008) 032; JHEP 0905 (2009) 119;
JHEP 1012 (2010) 072; JHEP 1202 (2012) 065
C.Fiedler, M.Herranen, KK & P.M Rahkila,
JHEP 1202 (2012) 080.

M.Herranen, KK, P.M.Rahkila NPB810 (2009) 389



$$\partial_t \bar{\mathcal{S}}_{ij}^< = -i[H_{\text{eff}}, \bar{\mathcal{S}}^<]_{ij} + \gamma^0 \langle c_{ij} + c_{ij}^\dagger \rangle \gamma^0$$

$$\bar{\mathcal{S}}_{ij}^< = \sum_{h\pm} P_h P_{i\pm} \gamma^0 \left(P_{j\pm} f_{ijh\pm}^m + P_{j\mp} f_{ijh\pm}^c \right)$$

Works also for **leptogenesis** M.Herranen, KK, P.M.Rahkila

Application to EWBG (toy model) ongoing:

M.Herranen, KK, P.M.Rahkila, H.Jukkala

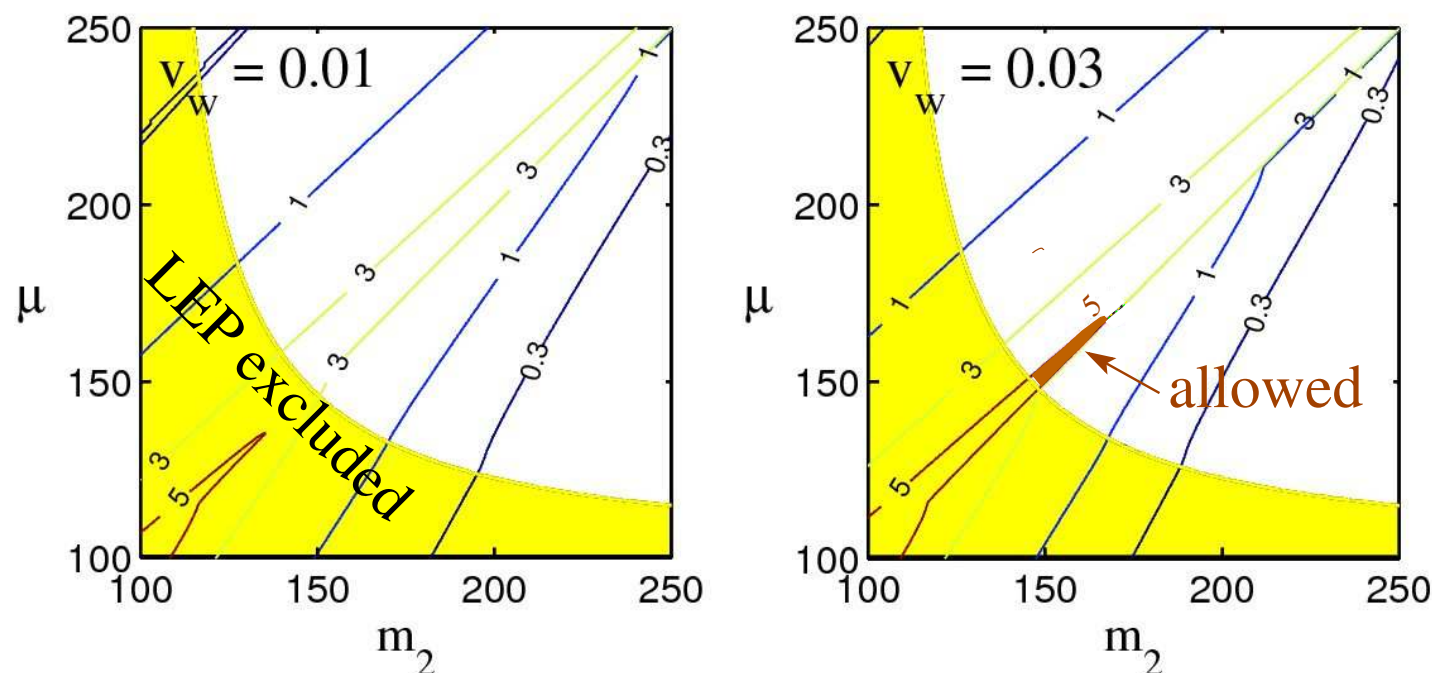
DREAM: A “CAMB” package for the EWBG analysis

BAU generation, MSSM / Thick wall - SC

Chargino transport

$$\mathcal{M}_{\chi^\pm} = \begin{pmatrix} M_2 & gh_2 \\ gh_1 & \mu \end{pmatrix}$$

Enhancement when $m_2 \sim \mu$



Adiabatic, flavour diagonal limit

J.M.Cline, M.Joyce and KK,
JHEP 0007 (2000) 018.

Similar results were found by

T.Konstandin, T.Prokopec, M.G.Schmidt,
and M.Seco, NPB738 (2006) 1.

which also used SC/CTP approach
and **included flavour mixing effects**

However, there are differences in the literature:

paper	method	η/η_{obs}
[41] (2000)	mass insertion formalism; no Higgs resummation	~ 35
[42] (2002)	mass insertion formalism; including Higgs resummation	~ 10
[43] (2004)	mass insertion formalism; no Higgs resummation; more realistic diffusion network	~ 140
[24] (2005)	Kadanoff-Baym formalism; flavor oscillations; assumes the adiabatic regime	~ 3.5

T.Konstandin, arXiv:1302.6713 [hep-ph]

Stop transport (weak source [CJK])

J.Kozaczuk, S.Profumo, M.Ramsey-Musolf and CL.
Wainwright, PRD86 (2012) 096001

Neutralino transport (bino-driven) !!

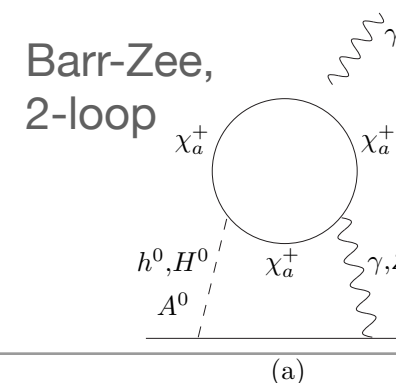
Y.Li, S.Profumo, and M.Ramsey-Musolf,
PLB673 (2009) 95-100.

MSSM / eEDM

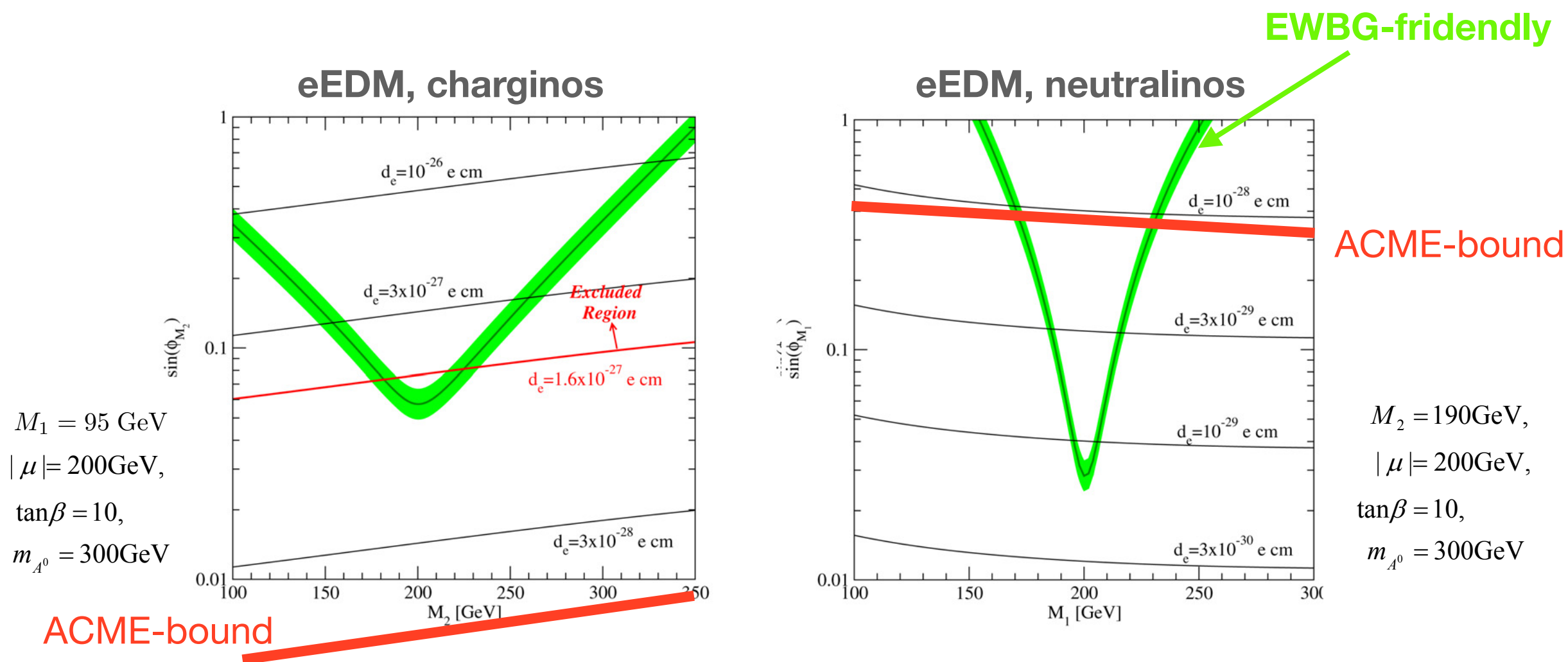
Same phases that give BAU generate EDM's
(more generally supersymmetric CP problem)

2013 ACME-bound on eEDM: $d_e < 8.9 \times 10^{-29}$

ACME collaboration, Science 343 (2014) 6168, 269-272



Bino driven EWBG (optimistic calculation) [Li, Profumo, Ramsey-Musolf, PLB673 \(2009\)](#)



- chargino transport mechanism **excluded**
- light bino ($< 60 \text{ GeV}$) appears *not ok*

Loopholes on loopholes? Finetuned cancellations

- between, CP-even and CP-odd higgses [Bian, Liu, Shu, 2014](#)
- between, one and two-loop contributions [Li, Wagner, 2015](#)

EWBG in the MSSM ?

Is this not just fighting to keep a sinking ship afloat?



Leszek Roszkowski:
“SUSY cannot be disproved,
only abandoned”

2HDM's



Many new CP-violating phases:

$$\begin{aligned}
 V = & \frac{\lambda}{4} \left(H^{\dagger i} H_i - \frac{v^2}{2} \right)^2 + m_1^2 (S^{\dagger i} S_i) + (m_2^2 H^{\dagger i} S_i + \text{h.c.}), \\
 & + \lambda_1 (H^{\dagger i} H_i) (S^{\dagger j} S_j), + \lambda_2 (H^{\dagger i} H_j) (S^{\dagger j} S_i) + \left[\lambda_3 H^{\dagger i} H^{\dagger j} S_i S_j + \text{h.c.} \right], \\
 & + \left[\lambda_4 H^{\dagger i} S^{\dagger j} S_i S_j + \lambda_5 S^{\dagger i} H^{\dagger j} H_i H_j + \text{h.c.} \right] + \lambda_6 (S^{\dagger i} S_i)^2, \\
 & + y_t \bar{t}_L (H^{0*} \delta_{ti} + (\eta_U \delta_{ti} + \eta'_U V_{tb}^* V_{bi})) S^{0*}) q_R^i
 \end{aligned}$$

MFV for new Yukawa's to avoid **FCNC**

G.C.Branco, W.Grimus & L.Lavoura, PLB380 (1996) 119

MCMC of the PM-space finds **both strong EWPT and BAU**, but points are **rare: $<1/10^4$** .

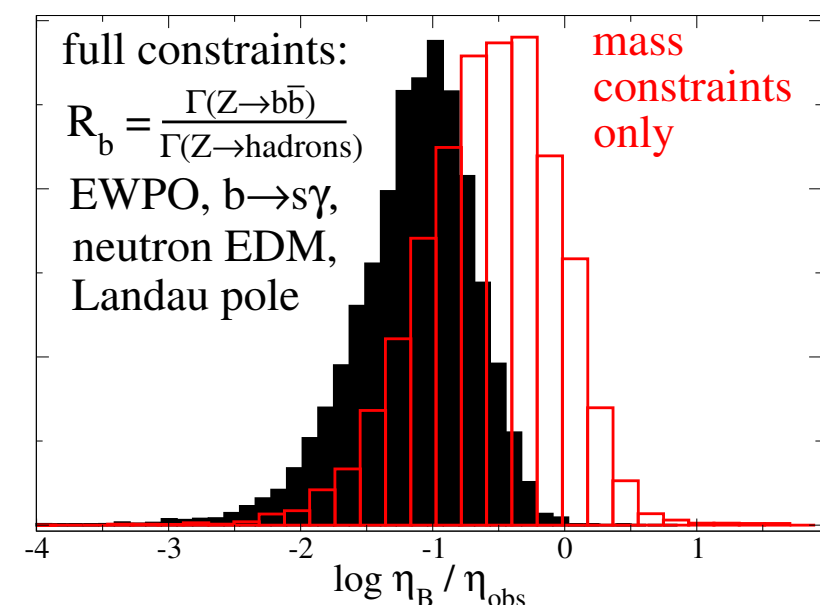
J.Cline, KK, M.Trott, JHEP 1111 (2011) 089

A more detailed scan of different types of 2HDM with similar results was carried out in:

G.C.Dorsch, S.J.Huber & J.M.No, JHEP 1310 (2013) 029.

Post-ACME analysis 2HDM + *vector like fermions* OK: Chao and Ramsey-Musolf: JHEP 1410 (2014) 180

Loophole with cancellations between, CP-even and CP-odd higgses works here as well. Bian, Liu, Shu, 2014



SSM a strong PT at “tree level” !

Get easily models satisfying $v/T > 1$ -limit with large enough a lambda.

eEDM and nEDM are not a problem.

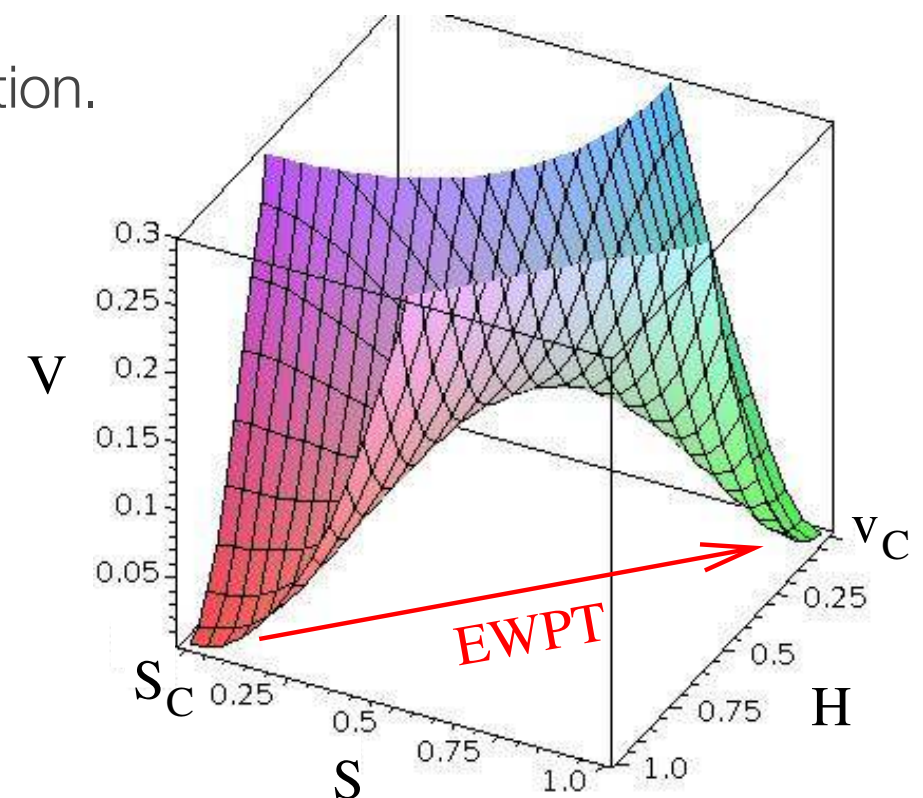
Take simply

$$V = V_{\text{MSM}} + \frac{1}{2}\mu_S^2 S^2 + \frac{1}{2}\lambda_{sh} S^2 |H|^2 + \frac{1}{4}\lambda_s S^4 \quad (\mu_S^2 < 0)$$

If λ_{hs} is large enough, there is a barrier between $\mathbf{H} = \mathbf{0}$ and $\mathbf{S} = \mathbf{0}$ vacua at $\mathbf{T} = \mathbf{0}$.

Transition may proceed in two steps, and model can give **a potential barrier at tree-level at $T_c \rightarrow$ strong phase transition.**

J.R.Espinosa, T.Konstandin, F.Riva, NPB854 (2012) 592



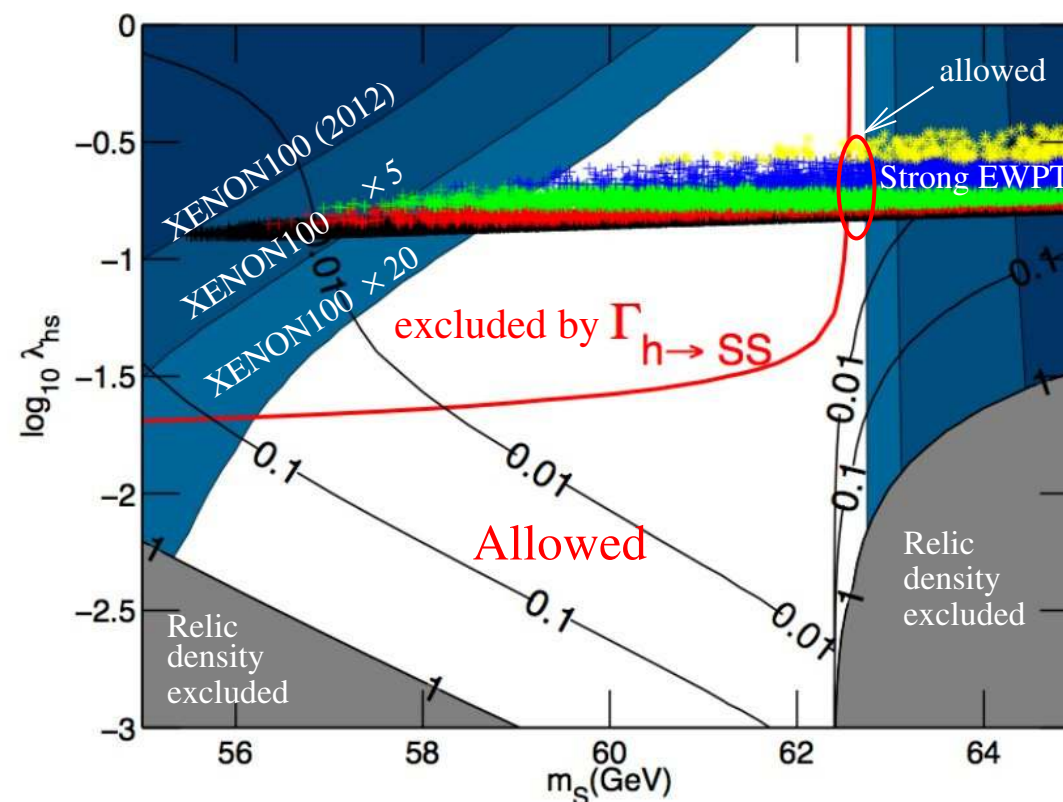
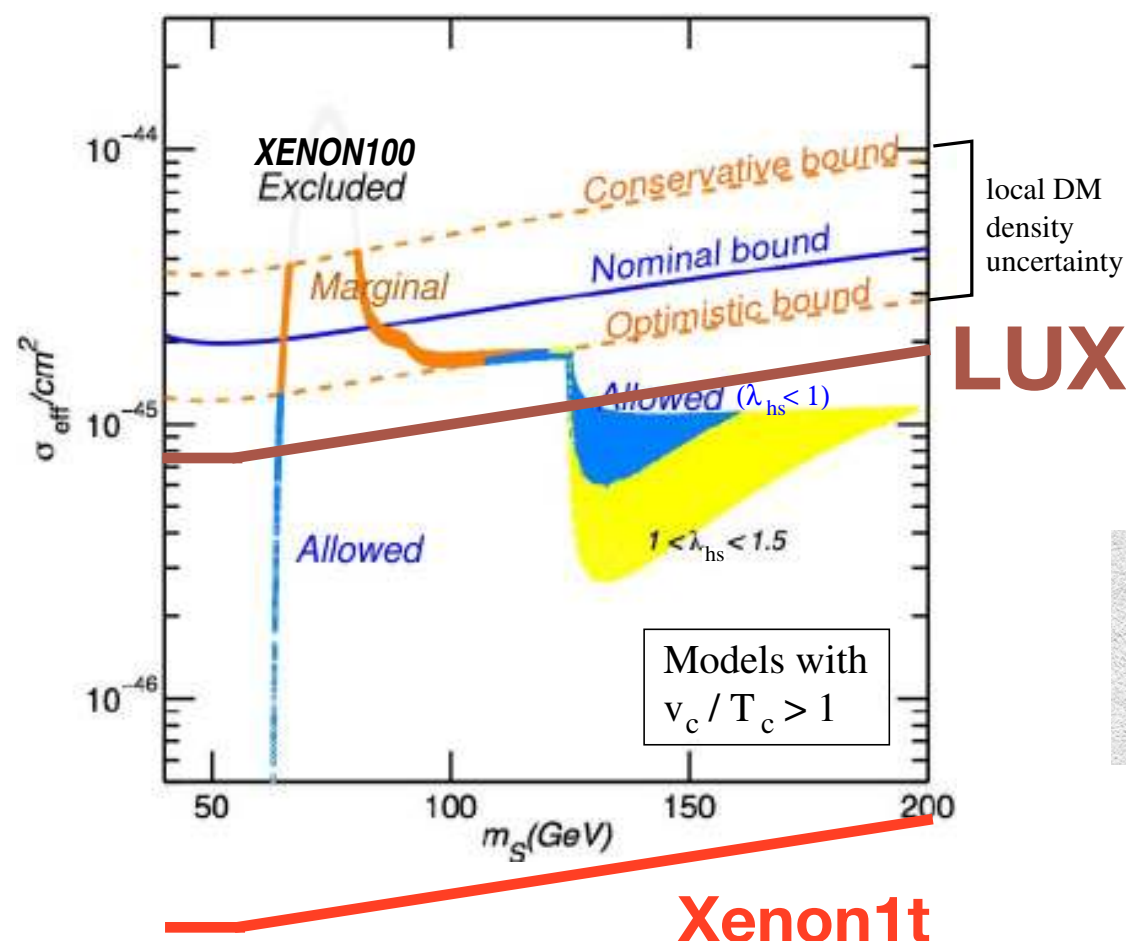
Finite-T effects only lift the degeneracy of vacua. Strength of transition determined by tree-level V.

SM+S with Z_2 , BAU and DM

Strong PT: need a large λ_{sh} , yet

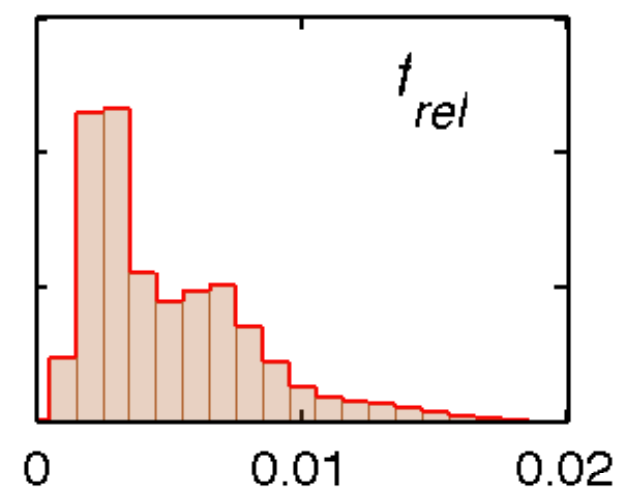
$$\Omega_{DM} \sim 1/v\sigma \sim 1/\lambda_{sh}^2$$

=> small Ω_{DM} . Subleading DM



Cline, KK, Scott, Weniger, PRD 2013

BAU acceptable $v/T > 1$ models



J.M. Cline, KK, JCAP 1301 (2013)

Even subleading
DM, BAU-capable
models detectable

ETC: (IDM, NMSSM,...) TCDM

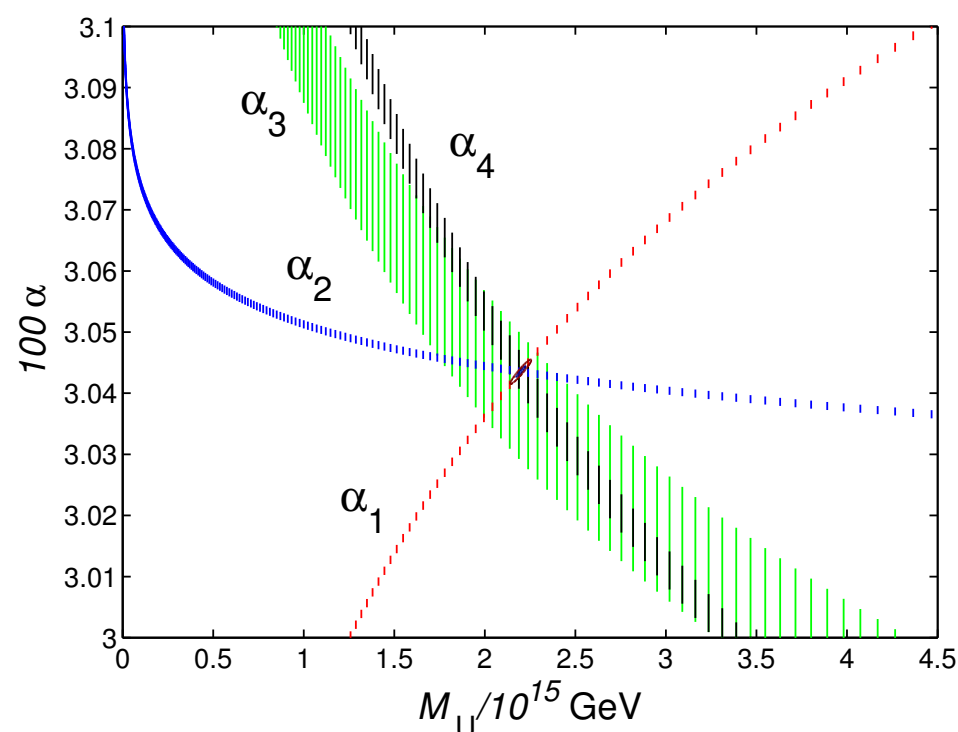
A model for **Dark Matter**, plausible **Naturalness** and a hint for a complete **Gauge Unification**

KK, Kimmo Tuominen
and Jussi Virkajärvi

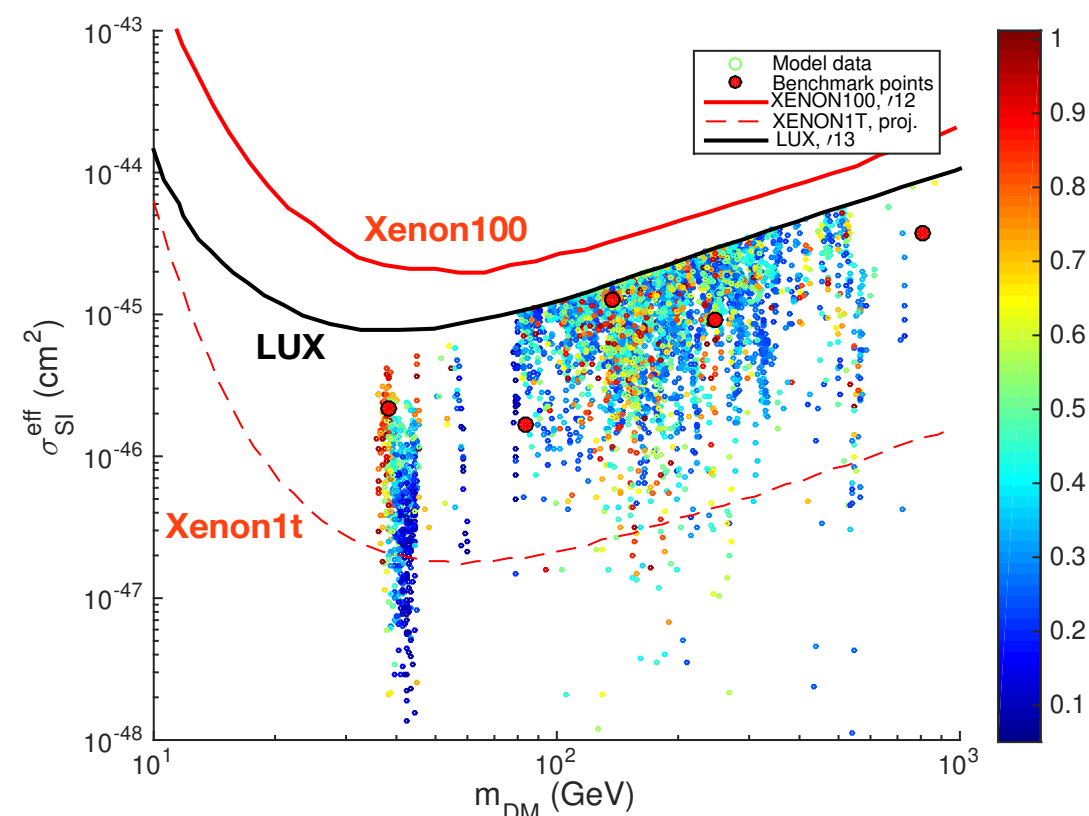
	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$SU(N_{TC})$	Z_2
L_L	1	2	-1/2	1	-1
E_R^c	1	1	1	1	-1
ω	1	adj.	0	1	-1
β	1	1	0	1	-1
\tilde{g}	adj.	1	0	1	-1
Q_L	1	2	1/6	3	1
U_R^c	1	1	-2/3	3	1
D_R^c	1	1	1/3	3	1
η_1	1	1	0	3	-1
η_2	1	1	0	3	-1
\tilde{G}	1	1	0	adj.	-1

3 neutral Majorana fields
+ 2 charged Dirac fields

Particle
spectrum
and the
unification
consistency
coupled to
existence
of a TeV
TC-scale.



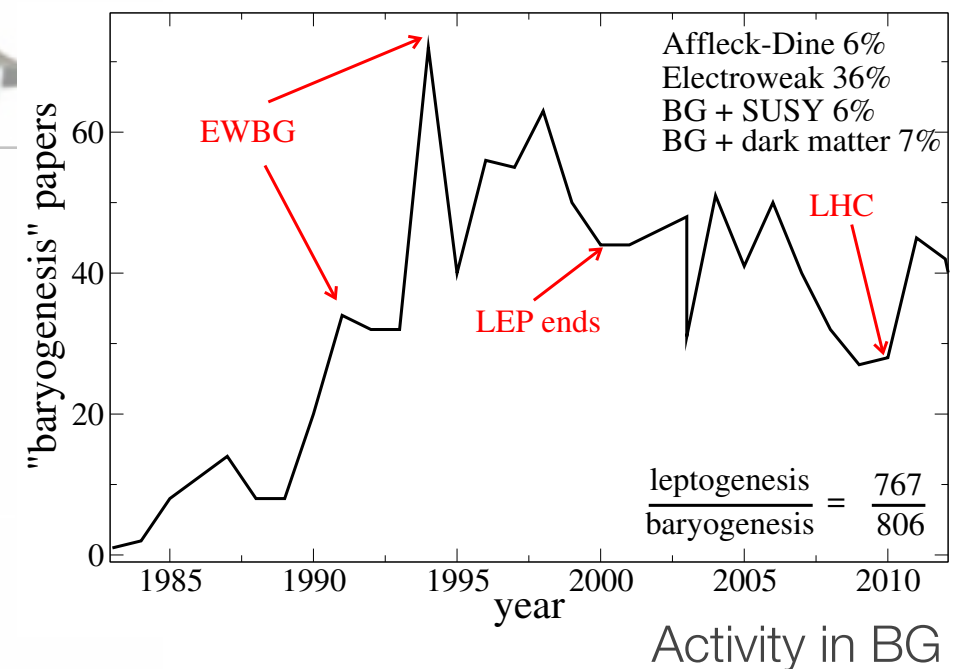
KK, Tuominen,
Virkajärvi,
arXiv:1504.07197



All pieces for EWBG are
qualitatively in place.
(CP in DM-sector)
Calculation not done yet.

“Conclusions”

EWBG continues to be interesting albeit ever more constrained by LHC and other lab data



Current action is in phenomenological model building

MSSM EWBG appears to be **all but dead** / **NMSSM** should be OK, btw

2HDM + extensions possible, though **restricted**

SSM:

strong (2-stage) transition **at tree level**

Singlet effect is likely a part of a more complete working EWBG model.

QKE's not fully understood (work in progress) Interesting but not pressing issue.