Dark Matter Theory

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Dark matter theory

- Fifty shades of dark
- The forbidden fruit
- Confusion of the mind
- That which does not kill us makes us stronger

Fifty shades of dark

Evidence for cold dark matter





vacuum $p=-\rho$

Planck (2015) TT,TE,EE+lowP+lensing+ext $1 \text{ pJ} = 10^{-12} \text{ J}$ $\rho_{\text{crit}} = 1.68829 \ h^2 \text{ pJ/m}^3$

Evidence for nonbaryonic cold dark matter



Matter fluctuations uncoupled to the plasma can gravitationally grow into galaxies in the given 13 Gyr Dark matter is non-baryonic More than 80% of all matter does not couple to the primordial plasma! SDSS



Evidence for *nonbaryonic* **cold dark matter** GALACTIC DARK MATTER



The observed microlensing events are not due to stellar remnants

Fields, Freese, Graff 1998 Graff, Freese, Walker, Pinsonneult 1999



Evidence for *nonbaryonic* **cold dark matter** *GALACTIC DARK MATTER*



The observed microlensing events are not due to stellar remnants

Fields, Freese, Graff 1998 Graff, Freese, Walker, Pinsonneult 1999



I HATE MACHOS

Katherine Freese at COSMO 99, Trieste

Is dark matter an elementary particle?



No known particle can be nonbaryonic cold dark matter!

Physicists have many ideas





Particle dark matter

 neutrinos (hot) • sterile neutrinos, gravitinos (warm) thermal relics • lightest supersymmetric particle (cold) • lightest Kaluza-Klein particle (cold) Bose-Einstein condensates, axions, axion clusters non-thermal relics • solitons (Q-balls, B-balls, ...) supermassive wimpzillas Mass range Interaction strength range 10⁻²² eV (10⁻⁵⁶g) B.E.C.s Only gravitational: wimpzillas $10^{-8} M_{\odot}$ (10^{+25} g) axion clusters Strongly interacting: B-balls

Particle dark matter

Hot dark matter

- relativistic at kinetic decoupling (start of free streaming)
- big structures form first, then fragment

light neutrinos

Cold dark matter

- non-relativistic at kinetic decoupling
- small structures form first, then merge

neutralinos, axions, WIMPZILLAs, solitons

Warm dark matter

- semi-relativistic at kinetic decoupling
- smallest structures are erased

sterile neutrinos, gravitinos

Particle dark matter

Thermal relics

in thermal equilibrium in the early universe

neutrinos, neutralinos, other WIMPs,

Non-thermal relics

not in thermal equilibrium in the early universe

axions, WIMPZILLAs, solitons,



Axions as dark matter

Hot

Produced thermally in early universe

Important for $m_a > 0.1 eV$ ($f_a < 10^8$), mostly excluded by astrophysics

Cold

Produced by coherent field oscillations around mimimum of $V(\theta)$ (Vacuum realignment)

Produced by decay of topological defects (Axionic string decays) Still a very complicated and uncertain calculation! e.g. Harimatsu et al 2012



Visinelli, Gondolo 2009 + updates

Neutrinos

Heavy active neutrinos

PHYSICAL REVIEW LETTERS

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NUMBER 4

Cosmological Lower Bound on Heavy-Neutrino Masses

Benjamin W. Lee^(a) Fermi National Accelerator Laboratory,^(b) Batavia, Illinois 60510

and

Steven Weinberg^(c) Stanford University, Physics Department, Stanford, California 94305 (Received 13 May 1977)

The present cosmic mass density of possible stable neutral heavy leptons is calculated in a standard cosmological model. In order for this density not to exceed the upper limit of 2×10^{-29} g/cm³, the lepton mass would have to be *greater* than a lower bound of the order of 2 GeV.

2 GeV/ c^2 for $\Omega_c = 1$

Now 4 GeV/ c^2 for Ω_c =0.25

Cosmic density of massive neutrinos



Sterile neutrino dark matter

Standard model + right-handed neutrinos

Active and sterile neutrinos oscillate into each other.

Sterile neutrinos can be warm dark matter (mass > 0.3 keV)

Dodelson, Widrow 1994; Shi, Fuller 1999; Laine, Shaposhnikov 2008



vMSM Laine, Shaposhnikov 2008 **Supersymmetric particles**

Supersymmetric dark matter

Neutralinos (the most fashionable/studied WIMP)

Goldberg 1983; Ellis, Hagelin, Nanopoulos, Olive, Srednicki 1984; etc.

Sneutrinos (also WIMPs)

Falk, Olive, Srednicki 1994; Asaka, Ishiwata, Moroi 2006; McDonald 2007; Lee, Matchev, Nasri 2007; Deppisch, Pilaftsis 2008; Cerdeno, Munoz, Seto 2009; Cerdeno, Seto 2009; etc.

Gravitinos (SuperWIMPs)

Feng, Rajaraman, Takayama 2003; Ellis, Olive, Santoso, Spanos 2004; Feng, Su, Takayama, 2004; etc.

Axinos (SuperWIMPs)

Tamvakis, Wyler 1982; Nilles, Raby 1982; Goto, Yamaguchi 1992; Covi, Kim, Kim, Roszkowski 2001; Covi, Roszkowski, Ruiz de Austri, Small 2004; etc.

Neutralino dark matter: impact of LHC

• The CMSSM is in dire straights

Constrained Minimal Superssymetric Standard Model

"a Higgs mass of ~125 GeV excludes the least fine-tuned CMSSM points; remaining viable models may be difficult to probe with dark matter searches" Sandick 1210.5214

• But there are many supersymmetric models



Neutralino dark matter: impact of LHC

Cahill-Rowell et al 1305.6921

"the only pMSSM models remaining [with neutralino being 100% of CDM] are those with bino coannihilation" pMSSM (phenomenological MSSM) $\mu, m_A, \tan \beta, A_b, A_t, A_{\tau}, M_1, M_2, M_3,$ $m_{Q_1}, m_{Q_3}, m_{u_1}, m_{d_1}, m_{u_3}, m_{d_3},$ $m_{L_1}, m_{L_3}, m_{e_1}, m_{e_3}$ (19 parameters)



The forbidden fruit

Searches for particle dark matter







Indirect









Dark matter creation with particle accelerators

Searching for the conversion protons \rightarrow energy \rightarrow dark matter





The ATLAS detector

Particle production at the Large Hadron Collider

The principle

Dark matter particles transform into ordinary particles, which are then detected or inferred

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The principle

Dark matter particles transform into ordinary particles, which are then detected or inferred

Gunn, Lee, Lerche, Schramm, Steigman 1978; Stecker 1978







HEAT BESS

AMS

GAPS

PAMELA

The principle

Dark matter particles transform into ordinary particles, which are then detected or inferred

The first stars to form in the universe may have been powered by dark matter instead of nuclear fusion.



They were dark-matter powered stars or for short Park Stars

- Explain chemical elements in old halo stars
- Explain origin of supermassive black holes in early quasars

Spolyar, Freese, Gondolo 2007-2008

The principle of direct detection

Dark matter particles that arrive on Earth scatter off nuclei in a detector

Goodman, Witten 1985



Dark matter particle

Low-background underground detector

Expected event rate is small

Expected WIMP spectrum



~l event/kg/year (nuclear recoils)

Expected event rate is small

Expected WIMP spectrum

Measured banana spectrum





~I event/kg/year (nuclear recoils) ~100 events/kg/second (electron recoils)

Expected event rate is small



~I event/kg/year (nuclear recoils) ~100 events/kg/second (electron recoils)
Confusion of the mind

Evidence for cold dark matter particles?

GeV γ -rays



Hooper et al 2009-14

3.5 keV X-ray line



Bulbul et al 2014

135 GeV γ -ray line



Weniger 2012

Annual modulation

Positron excess



Adriani et al 2009; Ackerman et al 2011; Aguilar et al 2013



Gamma-rays from dark matter?

1 GeV gamma-ray excess?

Goodenough, Hooper 2009; Hooper, Goodenough; Boyarsky, Malyshev, Ruchayskiy; Hooper, Linden 2011; Abazajian, Kaplinghat 2012; Gordon, Macias 2013; Abazajian, Canac, Horiuchi, Kaplinghat; Daylan et al 2014

> Fermi-LAT all-sky map

Fit diffuse + Fermi-bubble, find residual



I start - D J ins



Gamma-rays from dark matter (2015)

Self-annihilation into $b\overline{b}$

(similar for $\tau^+\tau^-$)



Gamma-rays from dark matter (2015)

Self-annihilation into $b\overline{b}$

(similar for $\tau^+\tau^-$)



Positrons from dark matter?

Excess in cosmic ray positrons

High energy cosmic ray positrons are more than expected



Adriani et al. [PAMELA ,2008

Ackernmann et al [Fermi-LAT] 2011



10

Accardo et al [AMS-02] 2014

10²

103

Energy [GeV]

Excess in cosmic ray positrons

Positron excess as "smoking gun" for dark matter



Excess in cosmic ray positrons

Dark matter? Pulsars? Secondaries from extra primaries?





Blasi 2009

Dynamical dark matter

Dienes, Thomas 2011, 2012 Dienes, Kumar, Thomas 2012, 2013

A vast ensemble of fields decaying one into another Example: Kaluza-Klein tower of axions in extra-dimensions





Phenomenology obtained through scaling laws

 $m_n = m_0 + n^{\delta} \Delta m,$ $\rho_n \sim m_n^{\alpha}, \, \tau_n \sim m_n^{-\gamma}$

Direct detection of dark matter?

Annual modulation in direct detection

• DAMA observes more nuclei are "hit" in Summer, fewer in Winter



 This is exactly what is expected of dark matter WIMPs

Drukier, Freese, Spergel 1986



DAMA modulation

Model Independent Annual Modulation Result

DAMA/Nal + DAMA/LIBRA-phase1 Total exposure: 487526 kg×day = 1.33 ton×yr





No systematics or side reaction able to account for the measured modulation amplitude and to satisfy all the peculiarities of the signature Comparison between single hit residual rate (red points) and multiple hit residual rate (green points); Clear modulation in the single hit events; No modulation in the residual rate of the multiple hit events A=-(0.0005±0.0004) cpd/kg/keV



The data favor the presence of a modulated behaviour with all the proper features for DM particles in the galactic halo at about 9.20 C.L.

Belli, IDM2014

DAMA modulation

Model Independent Annual Modulation Result

DAMA/Nal + DAMA/LIBRA-phase1 Total exposure: 487526 kg×day = 1.33 ton×yr



No systematics or side processes able to quantitatively account for the measured modulation amplitude and to simultaneously satisfy the many peculiarities of the signature are available.

DAMA modulation

Model Independent Annual Modulation Result



- Nc
- Nc
- Nc
 ev
- R(t)
- here
- Sm (cpd/kg/keV)

"Public? What does it mean?"

Pierluigi Belli at IDM2014

peculiarities of the signature are available.

Direct dark matter searches (2015)



Billard et al 2013, Snowmass 2013, LUX 2013, SuperCDMS 2014

Evidence for light dark matter particles?



No significant modulation Same target material Ahmed et al (CDMS) 1203.1309



Not so many events

Akerib et al (LUX) 2013

That which does not kill us makes us stronger

All particle physics models

Write down and analyze all possible WIMP interactions with ordinary matter

Effective operators

if mediator mass >> exchanged energy



Four-particle effective operator

There are many possible operators. Interference is important although often neglected. Long(ish) distance interactions are not included.

Name	Operator	Coefficient
D1	$ar\chi\chiar q q$	m_q/M_*^3
D2	$ar{\chi}\gamma^5\chiar{q}q$	im_q/M_*^3
D3	$ar{\chi}\chiar{q}\gamma^5 q$	im_q/M_*^3
D4	$ar{\chi}\gamma^5\chiar{q}\gamma^5q$	m_q/M_*^3
D5	$\bar{\chi}\gamma^{\mu}\chi\bar{q}\gamma_{\mu}q$	$1/M_{*}^{2}$
D6	$\bar{\chi}\gamma^{\mu}\gamma^{5}\chi\bar{q}\gamma_{\mu}q$	$1/M_{*}^{2}$
D7	$\bar{\chi}\gamma^{\mu}\chi\bar{q}\gamma_{\mu}\gamma^{5}q$	$1/M_{*}^{2}$
D8	$\bar{\chi}\gamma^{\mu}\gamma^{5}\chi\bar{q}\gamma_{\mu}\gamma^{5}q$	$1/M_{*}^{2}$
D9	$\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\mu\nu}q$	$1/M_{*}^{2}$
D10	$\bar{\chi}\sigma_{\mu\nu}\gamma^5\chi\bar{q}\sigma_{lphaeta}q$	i/M_*^2
D11	$\bar{\chi}\chi G_{\mu\nu}G^{\mu\nu}$	$\alpha_s/4M_*^3$
D12	$\bar{\chi}\gamma^5\chi G_{\mu\nu}G^{\mu\nu}$	$i\alpha_s/4M_*^3$
D13	$\bar{\chi}\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$i\alpha_s/4M_*^3$
D14	$\bar{\chi}\gamma^5\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$\alpha_s/4M_*^3$

Name	Operator	Coefficient	
C1	$\chi^\dagger\chiar q q$	m_q/M_*^2	
C2	$\chi^\dagger \chi ar q \gamma^5 q$	im_q/M_*^2	
C3	$\chi^\dagger \partial_\mu \chi \bar{q} \gamma^\mu q$	$1/M_{*}^{2}$	
C4	$\chi^{\dagger}\partial_{\mu}\chi\bar{q}\gamma^{\mu}\gamma^{5}q$	$1/M_{*}^{2}$	
C5	$\chi^{\dagger}\chi G_{\mu\nu}G^{\mu\nu}$	$\alpha_s/4M_*^2$	
C6	$\chi^{\dagger}\chi G_{\mu\nu}\tilde{G}^{\mu\nu}$	$i\alpha_s/4M_*^2$	
R1	$\chi^2 ar q q$	$m_q/2M_*^2$	
R2	$\chi^2 ar q \gamma^5 q$	$im_q/2M_*^2$	
R3	$\chi^2 G_{\mu\nu} G^{\mu\nu}$	$\alpha_s/8M_*^2$	
R4	$\chi^2 G_{\mu\nu} \tilde{G}^{\mu\nu}$	$i\alpha_s/8M_*^2$	

Table of effective operators relevant for the collider/direct detection connection *Goodman, Ibe, Rajaraman, Shepherd, Tait, Yu 2010*

LHC limits on WIMP-quark and WIMP-gluon interactions are competitive with direct searches

Beltran et al, Agrawal et al., Goodman et al., Bai et al., 2010; Goodman et al., Rajaraman et al. Fox et al., 2011; Cheung et al., Fitzptrick et al., March-Russel et al., Fox et al., 2012......



These bounds do not apply to SUSY, etc.

Complete theories contain sums of operators (interference) and not-so-heavy mediators (Higgs)

Fox, Harnik, Primulando, Yu 2012

All short-distance operators classified

Fitzpatrick et al 2012

 $\mathbf{1}, \quad \vec{S}_{\chi} \cdot \vec{S}_N, \quad v^2, \quad i(\vec{S}_{\chi} \times \vec{q}) \cdot \vec{v}, \quad i\vec{v} \cdot (\vec{S}_N \times \vec{q}), \quad (\vec{S}_{\chi} \cdot \vec{q}) (\vec{S}_N \cdot \vec{q}) \quad i\vec{S}_N \cdot \vec{q}, \quad i\vec{S}_{\chi} \cdot \vec{q}, \\ \vec{v}^{\perp} \cdot \vec{S}_{\chi}, \quad \vec{v}^{\perp} \cdot \vec{S}_N, \quad i\vec{S}_{\chi} \cdot (\vec{S}_N \times \vec{q}). \quad (i\vec{S}_N \cdot \vec{q})(\vec{v}^{\perp} \cdot \vec{S}_{\chi}), \quad (i\vec{S}_{\chi} \cdot \vec{q})(\vec{v}^{\perp} \cdot \vec{S}_N).$

All nuclear form factors classified

Response $\times \left[\frac{4\pi}{2J_i+1}\right]^{-1}$	Leading Multipole	Long-wavelength Limit	Response Type
$\sum_{J=0,2,\dots}^{\infty} \langle J_i M_{JM} J_i\rangle ^2$	$M_{00}(q\vec{x}_i)$	$rac{1}{\sqrt{4\pi}}1(i)$	M_{JM} : Charge
$\sum_{J=1,3,\dots}^{\infty} \langle J_i \Sigma_{JM}'' J_i \rangle ^2$	$\Sigma_{1M}^{\prime\prime}(q\vec{x}_i)$	$rac{1}{2\sqrt{3\pi}}\sigma_{1M}(i)$	L_{JM}^5 : Axial Longitudinal
$\sum_{J=1,3,\dots}^{\infty} \langle J_i \Sigma'_{JM} J_i \rangle ^2$	$\Sigma'_{1M}(q\vec{x}_i)$	$\frac{1}{\sqrt{6\pi}}\sigma_{1M}(i)$	$T_{JM}^{\rm el5}$: Axial Transverse Electric
$\sum_{J=1,3,\dots}^{\infty} \langle J_i \frac{q}{m_N} \Delta_{JM} J_i\rangle ^2$	$\frac{q}{m_N}\Delta_{1M}(q\vec{x}_i)$	$-rac{q}{2m_N\sqrt{6\pi}}\ell_{1M}(i)$	T_{JM}^{mag} : Transverse Magnetic
$\sum_{J=0,2,\dots}^{\infty} \langle J_i \frac{q}{m_N} \Phi_{JM}'' J_i\rangle ^2$	$\frac{q}{m_N}\Phi_{00}''(q\vec{x}_i)$	$-rac{q}{3m_N\sqrt{4\pi}}ec{\sigma}(i)\cdotec{\ell}(i)$	L_{JM} : Longitudinal
$\sum_{J=2,4,\dots}^{\infty} \langle J_i \frac{q}{m_N} \tilde{\Phi}'_{JM} J_i\rangle ^2$	$\frac{\frac{q}{m_N}\Phi_{2M}''(q\vec{x}_i)}{\frac{q}{m_N}\tilde{\Phi}_{2M}'(q\vec{x}_i)}$	$\begin{vmatrix} -\frac{q}{m_N\sqrt{30\pi}} [x_i \otimes (\vec{\sigma}(i) \times \frac{1}{i}\vec{\nabla})_1]_{2M} \\ -\frac{q}{m_N\sqrt{20\pi}} [x_i \otimes (\vec{\sigma}(i) \times \frac{1}{i}\vec{\nabla})_1]_{2M} \end{vmatrix}$	$T_{JM}^{\rm el}$: Transverse Electric

nuclear oscillator model *Fitzpatrick et al 2012*

Experimental limits on single operators...

Schneck et al (SuperCDMS) 2015



Combined analysis of short-distance operators

Catena, Gondolo 2014



Combined analysis of short-distance operators

Catena, Gondolo 2014



All astrophysics models

Do not assume any particular WIMP density or velocity distribution

DM-nucleus elastic scattering



Nuclear recoil

Detector response model

$$\begin{pmatrix} event \\ rate \end{pmatrix} = \begin{pmatrix} detector \\ response \end{pmatrix} \times \begin{pmatrix} particle \\ physics \end{pmatrix} \times (astrophysics)$$

Is a nuclear recoil detectable?

Counting efficiency, energy resolution, scintillation response, etc.

$$\begin{pmatrix} \text{detector} \\ \text{response} \end{pmatrix} = \mathcal{G}(E, E_R)$$

Probability of detecting an event with energy (or number of photoelectrons) E, given an event occurred with recoil energy E_R .

Particle physics model



What force couples dark matter to nuclei?

Coupling to nucleon number density, nucleon spin density, ...



Astrophysics model

$$\begin{pmatrix} event \\ rate \end{pmatrix} = \begin{pmatrix} detector \\ response \end{pmatrix} \times \begin{pmatrix} particle \\ physics \end{pmatrix} \times (astrophysics)$$

How much dark matter comes to Earth?

$$\begin{array}{l} \text{Local halo density}\\ (\text{astrophysics}) = \eta(v_{\min}, t) \equiv \rho_{\chi} \int_{v > v_{\min}} \frac{f(\mathbf{v}, t)}{v} \, \mathrm{d}^{3}v\\ \end{array}$$

$$\begin{array}{l} \text{Minimum WIMP speed to impart recoil energy } E_{R}\\ v_{\min} = (ME_{R}/\mu + \delta)/\sqrt{2ME_{R}} \end{array}$$

Astrophysics model: velocity distribution

Standard Halo Model

truncated
Maxwellian
$$f(\mathbf{v}) = \begin{cases} \frac{1}{N_{\rm esc}\pi^{3/2}\bar{v}_0^3} e^{-|\mathbf{v}+\mathbf{v}_{\rm obs}|/\bar{v}_0^2} & |\mathbf{v}| < v_{\rm esc} \\ 0 & \text{otherwise} \end{cases}$$



The spherical cow of direct WIMP searches

Astrophysics model: velocity distribution

We know very little about the dark matter velocity distribution near the Sun





Odenkirchen et al 2002 (SDSS) Streams of stars have been observed in the galactic halo SDSS, 2MASS, SEGUE,.....

Cosmological N-Body simulations including baryons are challenging but underway

Astrophysics model: velocity distribution





Agnese et al (SuperCDMS) 2014

Astrophysics-independent approach



Fox, Liu, Wiener 2011; Gondolo, Gelmini 2012; Del Nobile, Gelmini, Gondolo, Huh 2013-14
Astrophysics-independent approach

Gondolo Gelmini 2012

• The measured rate is a "weighted average" of the astrophysical factor.



• Every experiment is sensitive to a "window in velocity space."



Spin-independent isoscalar interactions

$$\sigma_{\chi A} = A^2 \sigma_{\chi p} \mu_{\chi A}^2 / \mu_{\chi p}^2$$



Astrophysics-independent approach

Halo modifications alone cannot save the SI signal regions from the Xe and Ge bounds

CDMS-Si event rate is similar to yearly modulated rates

Still depends on particle model

Del Nobile, Gelmini, Gondolo, Huh 2014

In the next episodes

In the next episodes..... Revenge



In the next episodes..... Precision cosmic rays

AMS (Alpha Magnetic Spectrometer)

AMS-02 can measure isotopic ratios to ~1% precision up to Fe and ~100 GeV/nucleon, and much better at lower energies.





ຸອ*xt episodes.....* WIM ແ



University of Hawaii 1. Jacque, S. Bons, S. Veisser*

MIT H. Che, C. Dezenne, P. Fisher^a, S. Henderson, W. Koch, J. Lopez, H. 70mita

Royal Holloway (UK) 6. Drain, R. Eggleson, P. Gianpa, J. Murze*

al direct detection e direction of nuclear recoil

&D efforts

- DRIFT
- Dark Matter TPC
- NEWAGE
- MIMAC
- D3
- Emulsion Dark Matter Search
- Columnar recombination



DMTPC

Only ~10 events needed to confirm extraterrestrial signal

In the next episodes..... WIMP astronomy



Synopsis

- Fifty shades of dark
 - There is evidence for nonbaryonic cold dark matter.
 - There are many candidates for nonbaryonic dark matter particles.
- The forbidden fruit
 - WIMP interaction rates in direct searches are very small.
 - No bananas in the lab.
- Confusion of the mind
 - Some experiments claim dark matter detection while others exclude it.
- That which does not kill us makes us stronger
 - Move to consider all possible WIMP-SM currents.
 - Do not assume any specific dark halo model.