Integrating traffic, geographic and economic aspects in Internet modeling

Petter Holme Josh F. Karlin Stephanie Forrest

University of New Mexico

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http://www.cs.unm.edu/~holme/



Peter Holme

Josh F. Karlin

Stephanie Forrest

Autonomous Systems

Internet is divided into different subnetworks—Autonomous Systems (AS)

- An IP network (or collection of IP networks) with the same routing policy.
- Typically one AS corresponds to one administrative unit.



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- Border Gateway Protocol determines how packets are routed between ASes
- Each server keeps a list of paths it can route a packets through.
- Policy (economical agreements) determines the order of paths.
- → a hierarchy where packets are routed up (to provider), sideways (to peer), and downwards (to customer).
- A BGP server has a quite incomplete picture of the whole AS-graph.

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Degree distribution

Broad degree-distribution (possibly power-law, or log-normal).



Models

• Typically focus on network topology.

- . . . possibly with a geometry.
- . . . or traffic.
- No geografically explicit ASes.



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Barabási–Albert model



probability of attachment: $\propto k_i$

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attach *i* to vertex *j* minimizing: $|\mathbf{r}_i - \mathbf{r}_j| + \alpha d(j, 0)$



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FKP model



attach *i* to vertex *j* minimizing: $|\mathbf{r}_i - \mathbf{r}_j| + \alpha d(j, 0)$

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Radial structure

Plot quantities as function of the average distance to the rest of the AS graph.

P. Holme, J. Karlin and S. Forrest, Proc. R. Soc. A **463**, 1231–1246 (2007).



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Radial structure



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Radial structure



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Radial structure



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Radial structure



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has spatially explicit ASes



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flowing between them



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Make a mechanistic model that:



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Make a mechanistic model that:



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Overall structure

The model begins with one agent located at the pixel with the highest population density. The model then iterates over the following steps:

- Network growth. The number of agents is increased. The agents are expanded geometrically, and their capacities are adjusted.
- Onetwork traffic. Messages are created, migrated toward their targets, and delivered. This process is repeated N_{traffic} times before the next network-growth step.



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Network Growth



geography represented as sq. grid



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geography represented as sq. grid each pixel has a pop. density



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Network Growth



geography represented as sq. grid each pixel has a pop. density the ASes are modeled as:

a set of locations (coordinates)



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Network Growth



geography represented as sq. grid each pixel has a pop. density the ASes are modeled as:

a set of locations (coordinates) set of links (to AS at same pixel)



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Network Growth



geography represented as sq. grid each pixel has a pop. density the ASes are modeled as:

> a set of locations (coordinates) set of links (to AS at same pixel) budget



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geography represented as sq. grid each pixel has a pop. density the ASes are modeled as:

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geography represented as sq. grid each pixel has a pop. density the ASes are modeled as: a set of locations (coordinates)

set of links (to AS at same pixel) budget queue capacity



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Network Growth



geography represented as sq. grid each pixel has a pop. density the ASes are modeled as:

> a set of locations (coordinates) set of links (to AS at same pixel) budget queue

> > capacity

costs for: increasing capacity connecting to other, adding loc.



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geography represented as sq. grid each pixel has a pop. density the ASes are modeled as:

> a set of locations (coordinates) set of links (to AS at same pixel) budget queue capacity

costs for: increasing capacity connecting to other, adding loc. income prop. to traffic

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Network Growth



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1. (while nwk too dense,) add ASes



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- 1. (while nwk too dense,) add ASes
- 2. increase capacity as much as needed



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- 3. link addition



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connect unconnected pairs at random



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connect unconnected pairs at random (if both ASes can afford a connection)



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4. spatial extension



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ASes spend their budget on new loc



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- 2. increase capacity as much as needed
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connect unconnected pairs at random

(if both ASes can afford a connection)

4. spatial extension

ASes spend their budget on new loc choose affordable pixel w highest pop



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Traffic dynamics





Peter Holme

Josh F. Karlin

Stephanie Forrest

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Josh F. Karlin

Stephanie Forrest

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Traffic dynamics



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Time evolution



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Degree distribution



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Degree distribution



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Traffic vs centrality



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Geography



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Geography



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Mechanistic growth model of AS-level Internet

- Degree distribution matches
- Periphery not as complex as reality
- Traffic fluctuations affect low- and medium-sized ASes
- Spatial distribution not completely crazy



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