



# Interplay between orbital degrees of freedom and spin fluctuations in the nematic phase of iron-based superconductors

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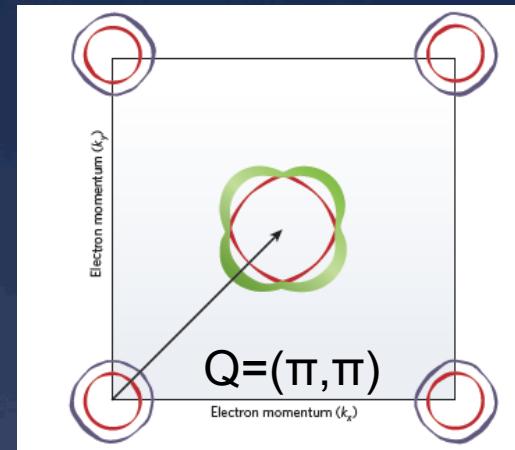
# Collaborations

- \* Theory:
  - \* Emmanuele Cappelluti (Rome)
  - \* Laura Fanfarillo (SISSA Trieste)
  - \* Belen Valenzula (CSIC Madrid)
  
- \* Experiments:
  - \* Veronique Brouet (CNRS Orsay Paris)

# What is new in pnictides?

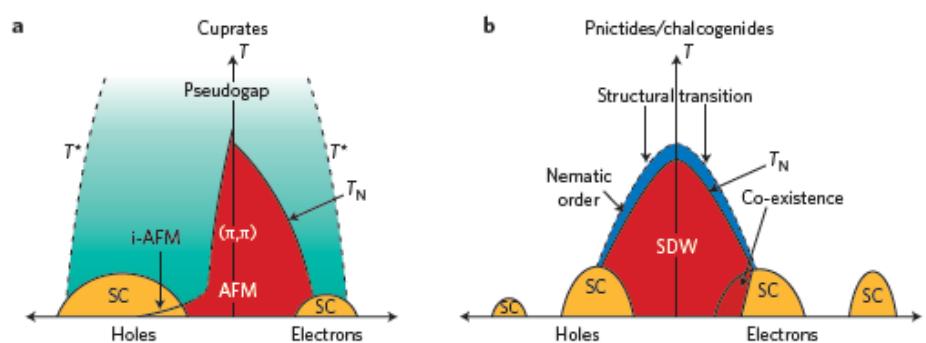
- \* Multiband systems

*(already seen in MgB<sub>2</sub>, graphene, etc.)*



- \* Proximity/coexistence with an AF phase, possible relevance of spin-fluctuations mediated interactions

*(already seen in heavy fermions, cuprates, etc.)*



# What is new in pnictides?

- \* Multiband systems

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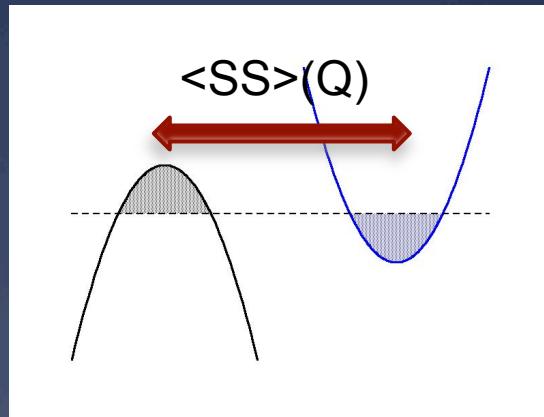
Coexistence of  
hole and electron  
bands

- \* Proximity/coexistence with an AF phase, possible relevance of spin-fluctuations mediated interactions

*(already seen in heavy fermions, cuprates, etc.)*



Interband  
interaction



More  
(interacting  
electron-hole bands)  
is different!

# Fermi-surface shrinking

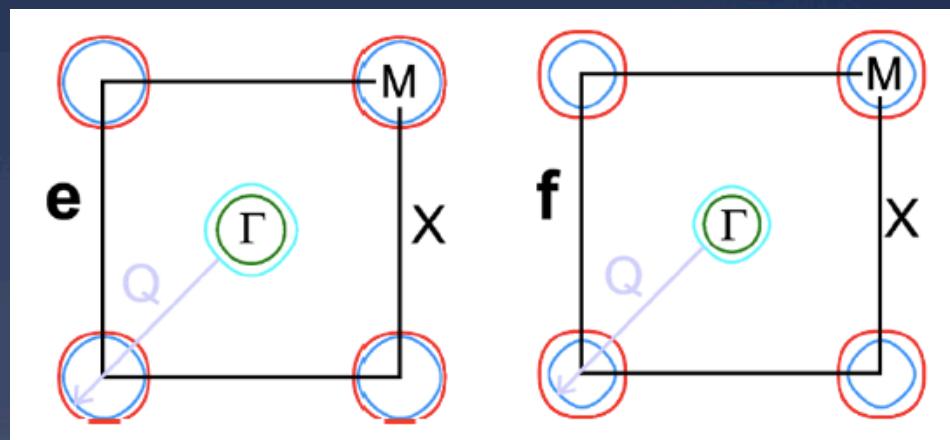
- \* De Haas Van Alphen experiments measure the Fermi surface areas for various bands

- \* Shrinking of all the FS with respect to DFT

- \* Total number of particles is still conserved

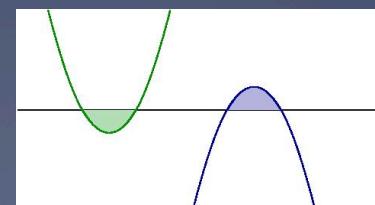
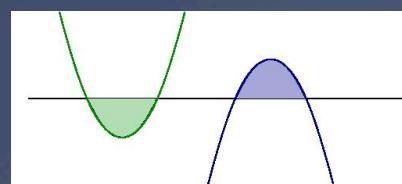
A. Coldea et al., Phys. Rev. Lett. 101, 216402 (2008)

unshifted LDA      shifted LDA



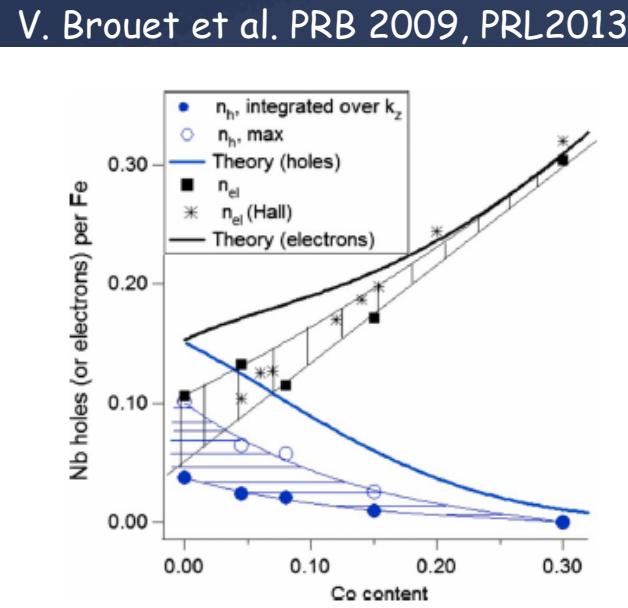
$$n = n_e + (2 - n_h)$$

$n_e - n_h$  is conserved, not  $n_e + n_h$

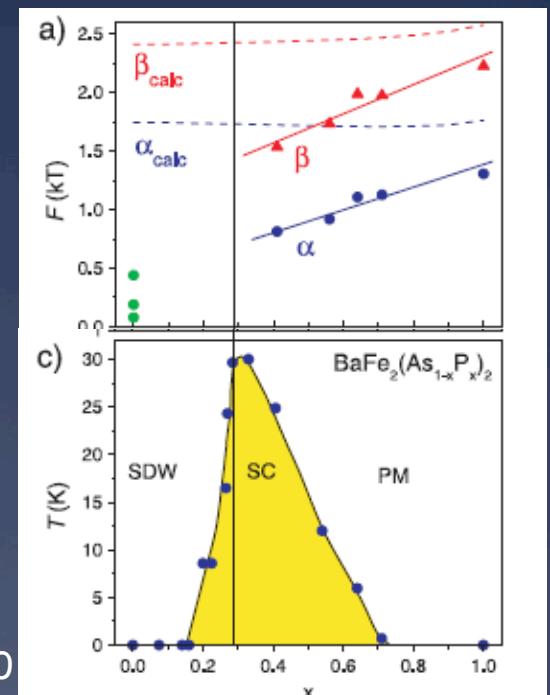


# Fermi-surface shrinking

- \* Both dHvA and ARPES show a **systematic** shrinking of the Fermi surface that can hardly be understood as a **systematic** inaccuracy of DFT



H. Shishido et al. PRL 2010

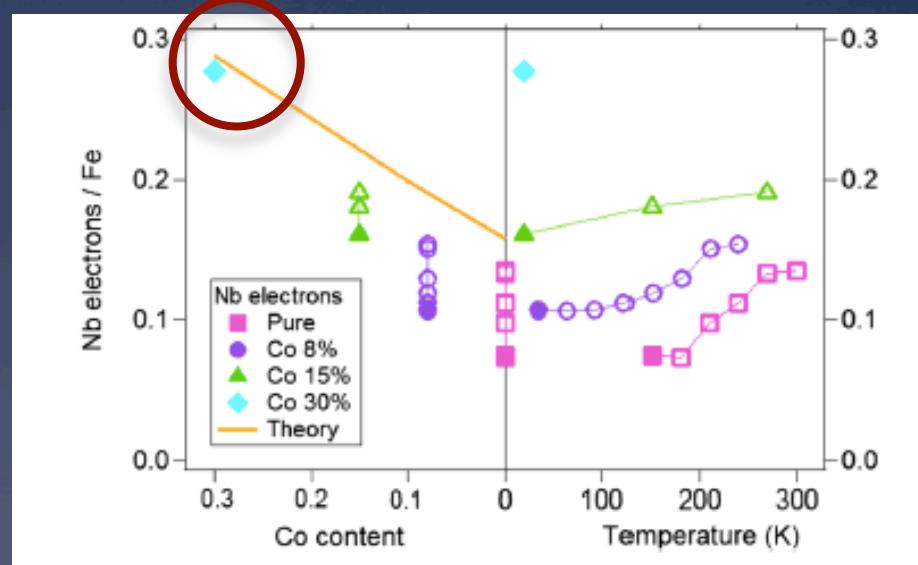
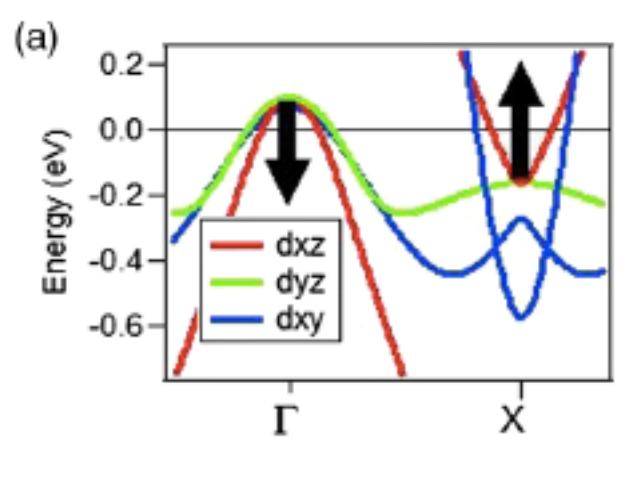


# Fermi-surface shrinking

- \* The effect is stronger at lower doping and lower temperatures. In e-doped 122 it disappears when hole pockets are completely filled

Ba(Fe<sub>1-x</sub>Co<sub>x</sub>)<sub>2</sub>As<sub>2</sub>

V. Brouet et al., PRL 110, 167002 2013

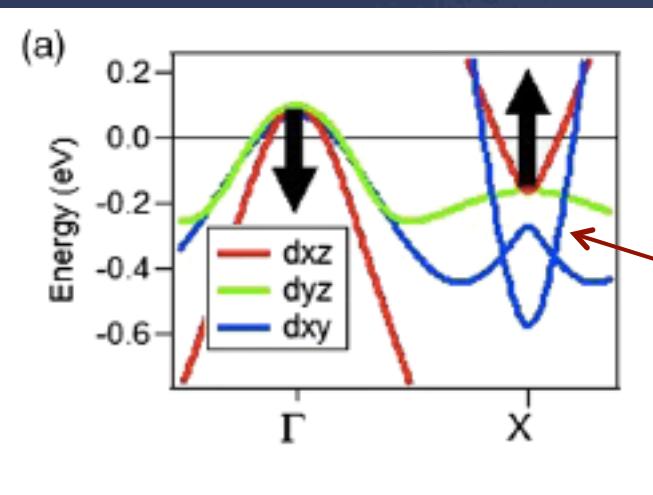


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V. Brouet et al., PRL 110, 167002 2013



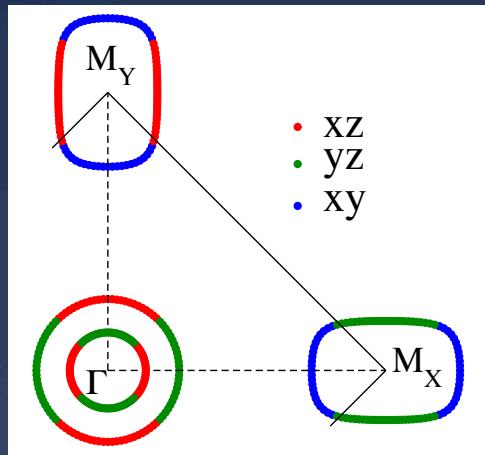
However, not all *orbital* components are affected in the same way

xy band is NOT shifted

# Orbital effects on the FS shrinking

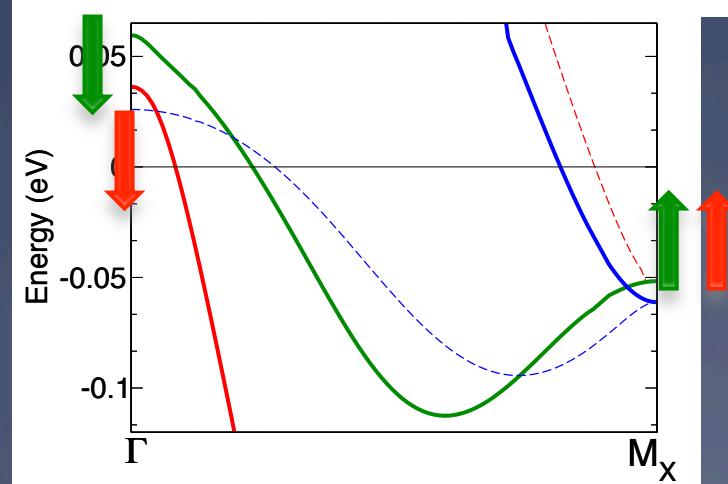
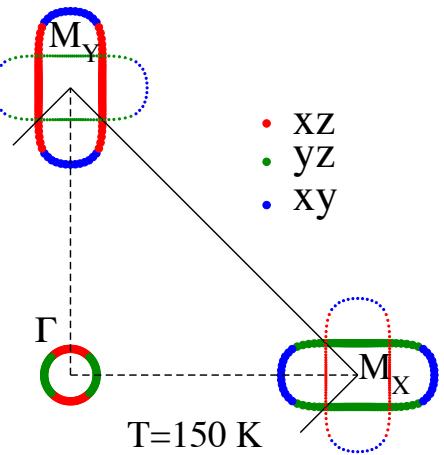
\* Already evident in 122, best seen in FeSe

LDA



Only xz,yz shifted,  
leading to more  
elliptical electron pockets

Experiments



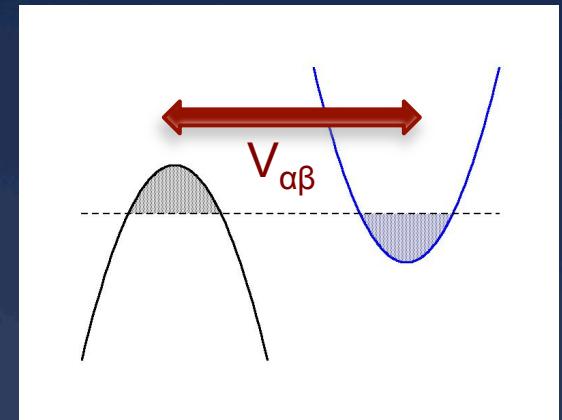
L. Fanfarillo, L.B. et al. arXiv:1605.02482

The FS shrinking is a  
common feature of all  
iron-based  
superconductors

Let us try to understand it first  
within the "band" language  
No orbital degrees of freedom for the moment

# Eliashberg approach

- \* hole+electron (parabolic) bands
- \* Multiband interaction mediated by a bosonic mode with characteristic energy  $\omega_0$  and coupling  $\lambda=VN$



$$\Sigma_\alpha(i\omega_n) = -T \sum_{m,\beta} V_{\alpha,\beta} D(\omega_n - \omega_m) G_\beta(i\omega_m)$$

$$D(\omega_l) = \int d\Omega \frac{2\Omega B(\Omega)}{(\Omega^2 + \omega_l^2)} \quad B(\Omega) = \frac{1}{\pi} \frac{\Omega \omega_0}{\omega_0^2 + \Omega^2}$$

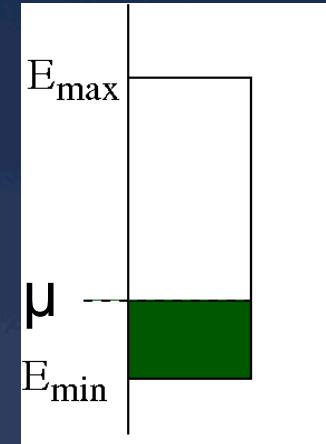
- \* Imaginary part of the self-energy: broadening of the energy levels
- \* Real part of the self-energy: mass renormalization and band shift (FS shrinking)

# (1) The standard Eliashberg theory for the one-band case

- \* Infinite bandwidth: mass renormalization  $\lambda=NV$

$$\Sigma'(\omega) = -\lambda\omega, \quad \lambda = NV$$

$$G^{-1}(\omega, k) = \omega(1 + \lambda) - \varepsilon_k + \mu$$



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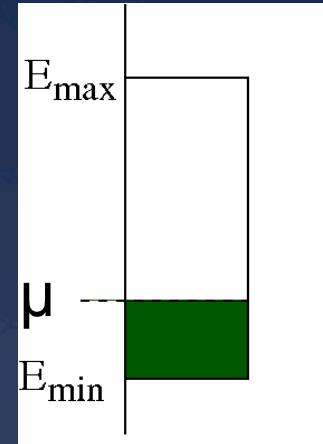
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- \* Finite bandwidth:  $\omega=0$  self-energy is finite

$$\Sigma'(\omega) = \chi - \lambda\omega \quad G^{-1}(\omega, k) = \omega(1 + \lambda) - \varepsilon_k + \mu - \chi = \omega(1 + \lambda) - \varepsilon_k + \tilde{\mu}$$

$$\chi \approx -\omega_0 \frac{VN}{2} \ln \left| \frac{E_{\max} - \mu}{E_{\min} - \mu} \right|$$

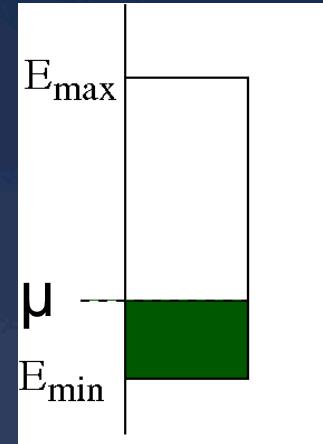


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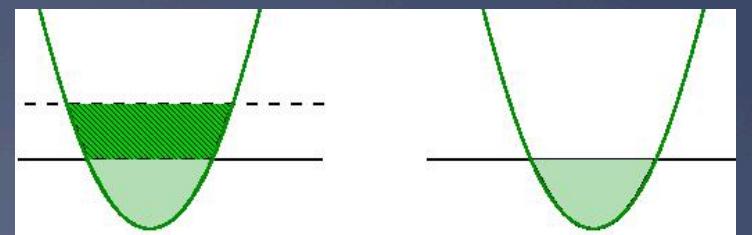


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- \* However, this effect is immaterial because it is re-adsorbed in a chemical-potential shift, to guarantee particle-number conservation



## (2) Multiband case

- \* In a multiband system particle-number conservation follows from a balance between **electron** and **hole** bands, so energy shifts are visible

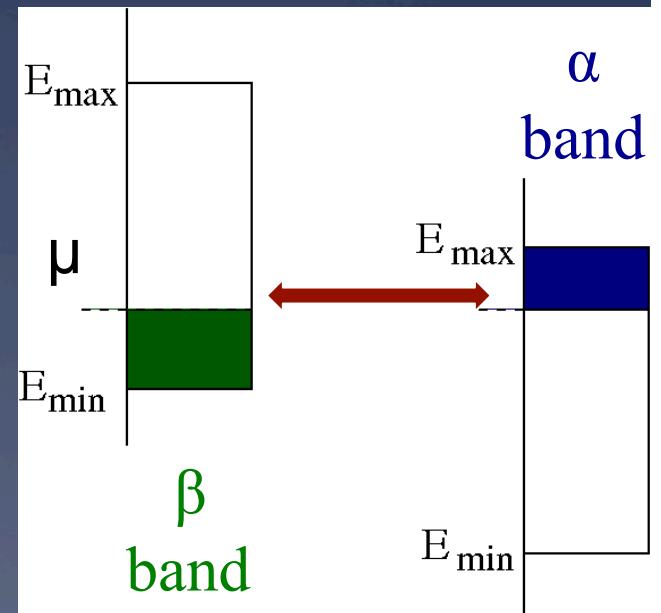
$$\chi_\alpha \approx -\omega_0 \sum_{\beta} \frac{V_{\alpha,\beta} N_{\beta}}{2} \ln \left| \frac{E_{\max,\beta} - \mu}{E_{\min,\beta} - \mu} \right|.$$

e band:  $E_{\max} - \mu > \mu - E_{\min} \rightarrow \chi < 0$   
 h band:  $E_{\max} - \mu < \mu - E_{\min} \rightarrow \chi > 0$

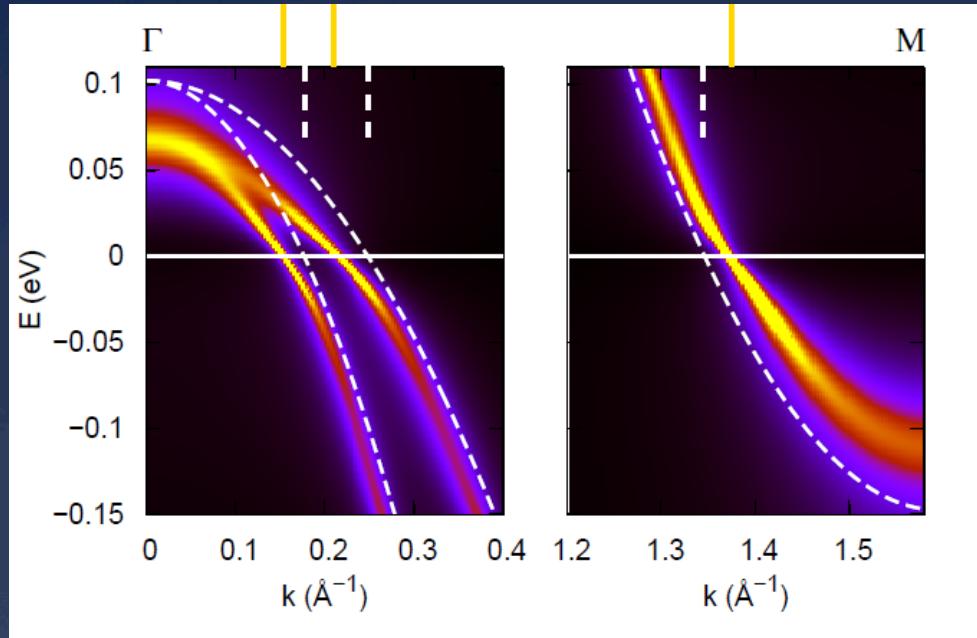
$$k_F^2 = 4\pi N [E_{\max} + \chi(0)] \quad \text{Hole band}$$

Intraband interactions:  
 $\chi > 0$ , **expansion** of the FS

Interband interactions:  
 $\chi < 0$ , **shrinking** of the FS



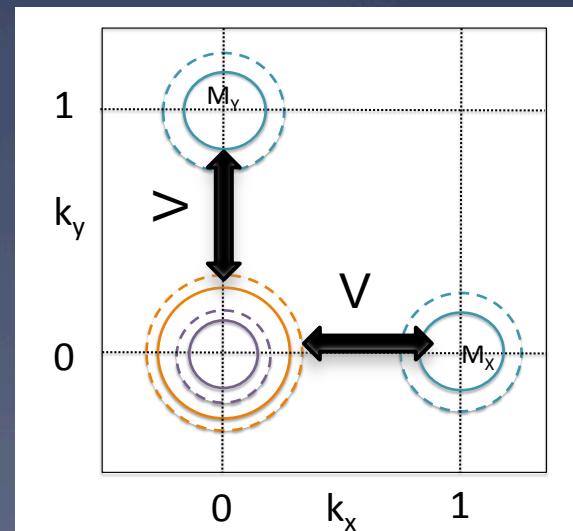
# Fermi-surface shrinking = interband interactions



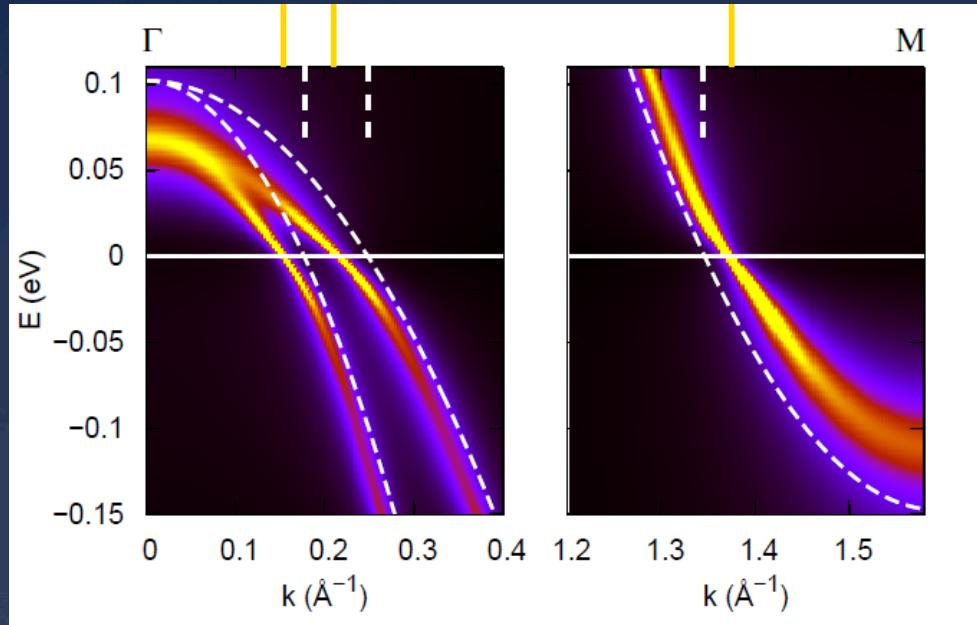
- \* Parabolic bands, no orbital character, including an overall high-energy renormalization
- \* Only interband coupling
- \* Uniform shrinking of all the bands

L.Ortenzi, E.Cappelluti, L.B., L.Pietronero,  
Phys Rev Lett 103, 046404 (2009)

$$\Sigma_h(i\omega_n) = -TV \sum_m D(\omega_n - \omega_m) G_e(i\omega_m)$$



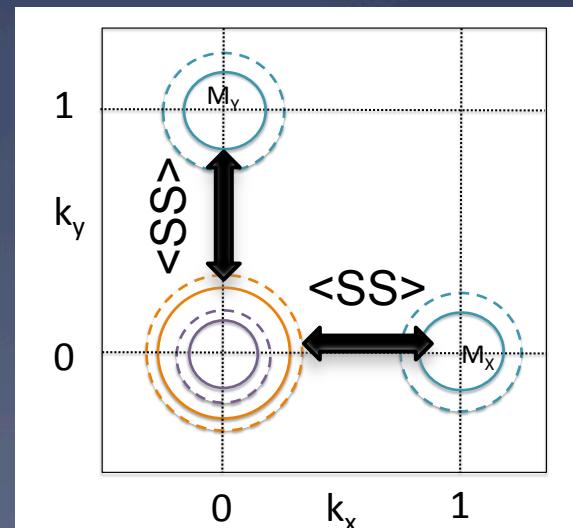
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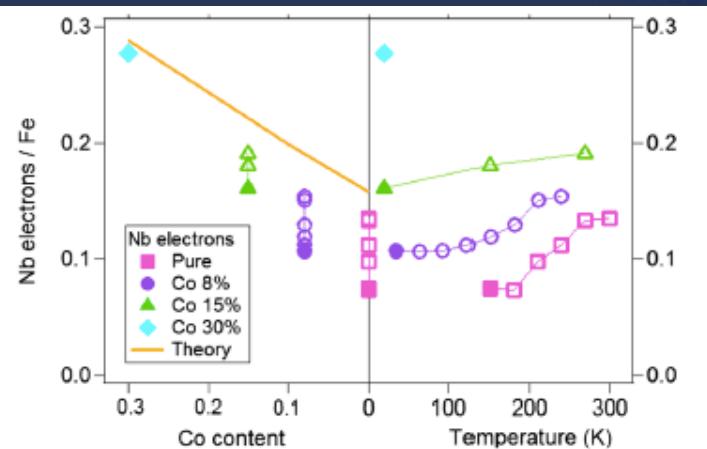
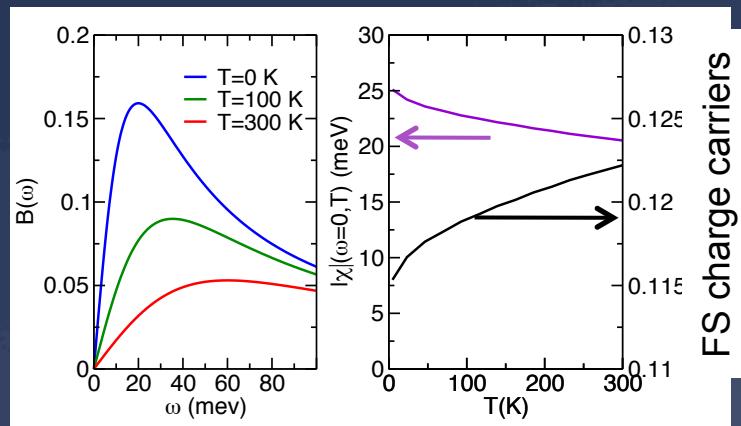
The most-likely candidate for  
interband interactions  
are spin fluctuations



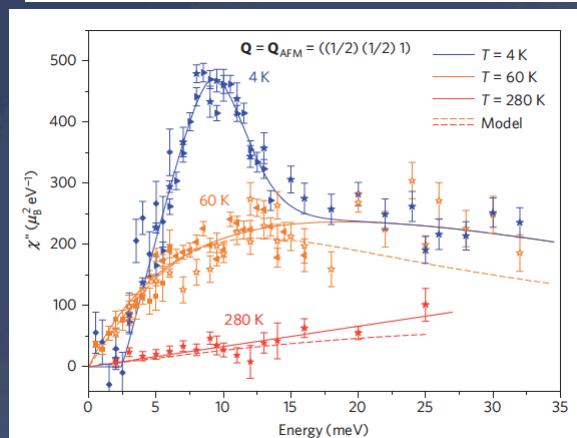
# Temperature dependence

- \* By using the T dependence of the spin spectrum measured by neutrons we can reproduce the T-dependent FS shrinking

L.B. and E. Cappelletti, PRB 83, 104516 (2011)



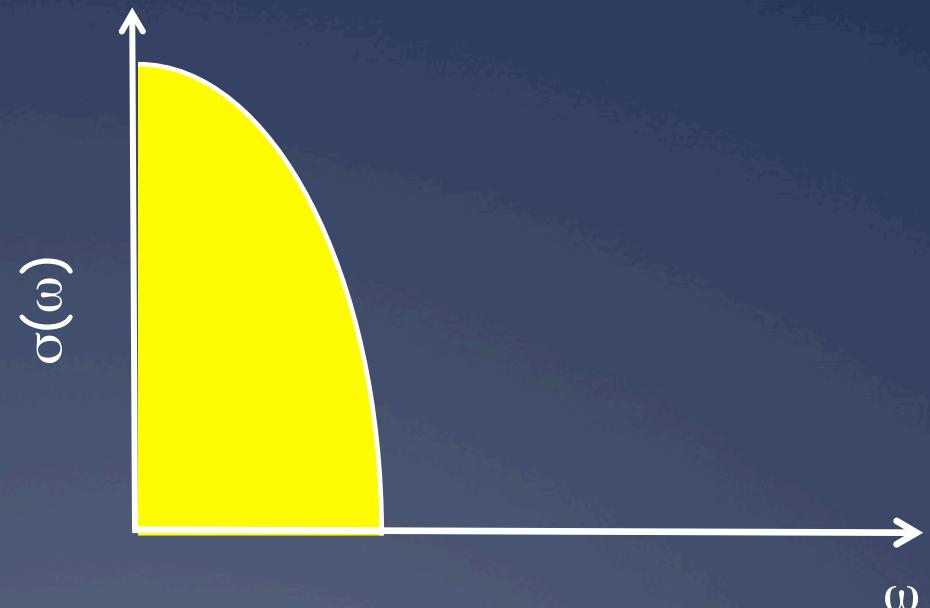
V. Brouet et al., PRL 110, 167002 2013



The FS shrinking is stronger at low T  
This has also profound implications for the optical sum rule

# Optical sum rule

$$W = \int_0^\infty d\omega \text{Re}\sigma_{xx}(\omega) = \frac{\pi e^2 n}{m}$$

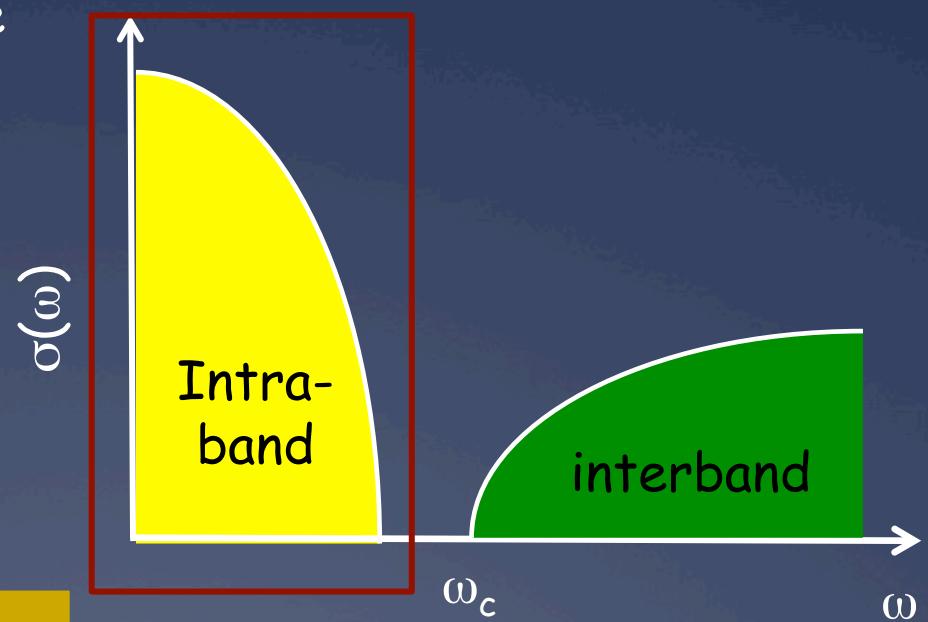


# Optical sum rule

$$W = \int_0^{\omega_c} d\omega \text{Re}\sigma_{xx}(\omega) = \frac{\pi e^2}{2N} \sum_{\mathbf{k},\sigma} \frac{\partial^2 \epsilon_{\mathbf{k}}}{\partial k_x^2} n_{\mathbf{k},\sigma}$$

- \*  $W(T)$  decreases as  $T^2/D$  in the normal state (Sommerfeld) ( $D$ =bandwidth)

$$W(T)=W(0)-BT^2$$



**Interacting** systems: correlations affect the T dependence

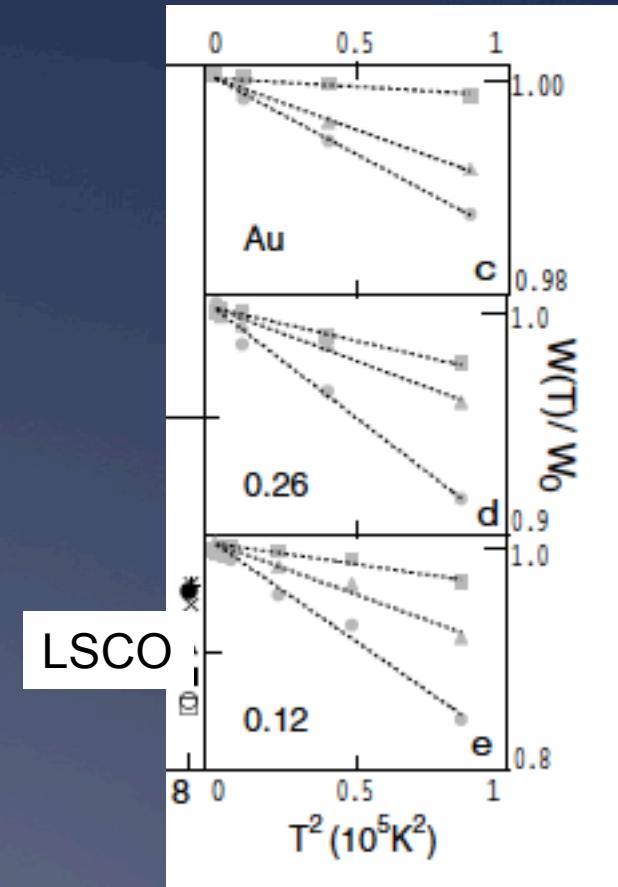
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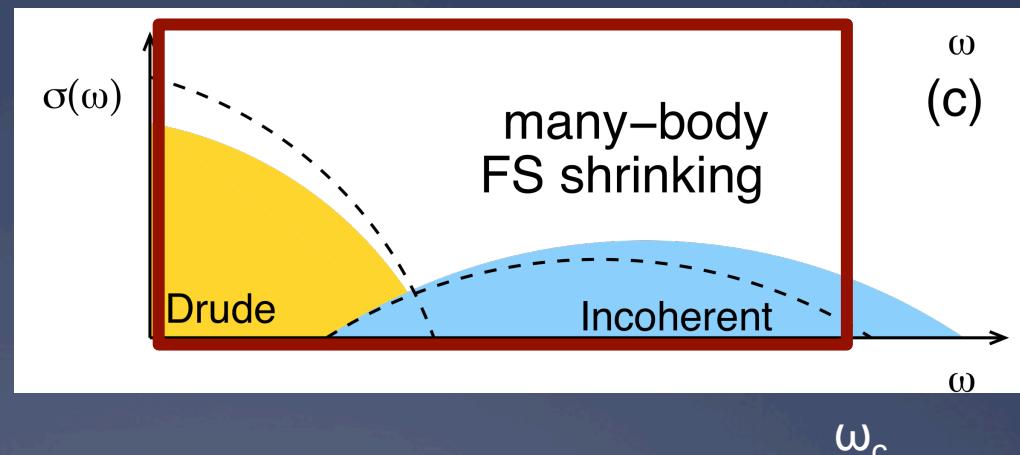
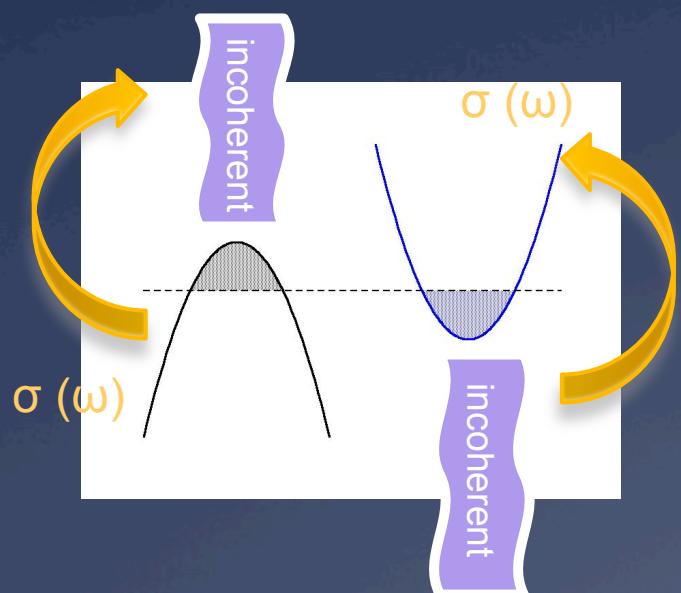
**Interacting** systems: correlations affect the T dependence



# FS shrinking and optical sum rule

The interband interaction leads to a finite DOS in the otherwise unoccupied part of the spectrum

The incoherent spectral weight is transferred up to energies much larger than the typical threshold  $\omega_c$  for interband transitions

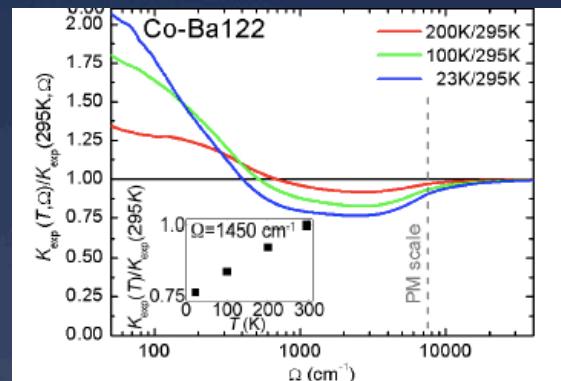
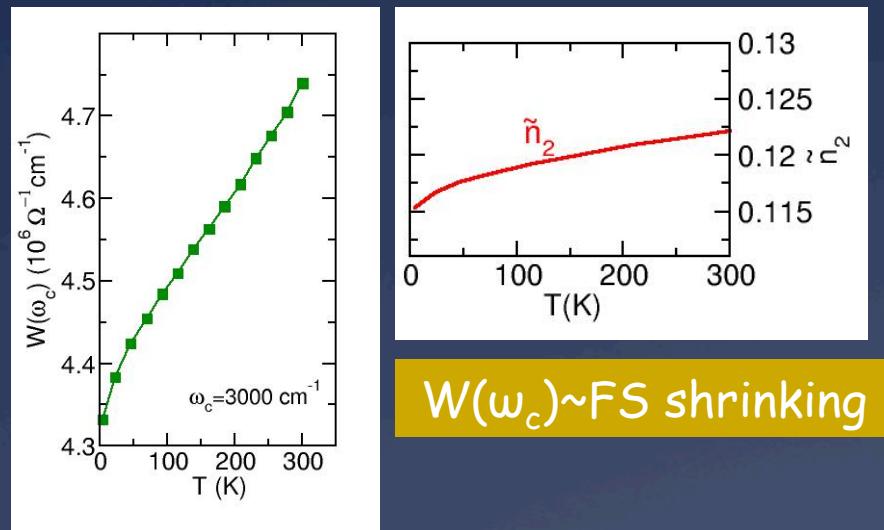


The optical spectral weight up to  $\omega_c$ ,  $W(\omega_c)$  scale  
with the T dependent FS area

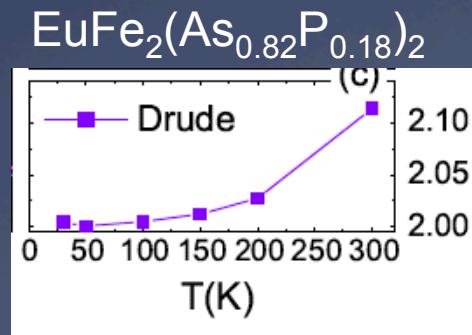
# FS shrinking and optical sum rule

Anomalous *increase* of the the optical sum rule with T

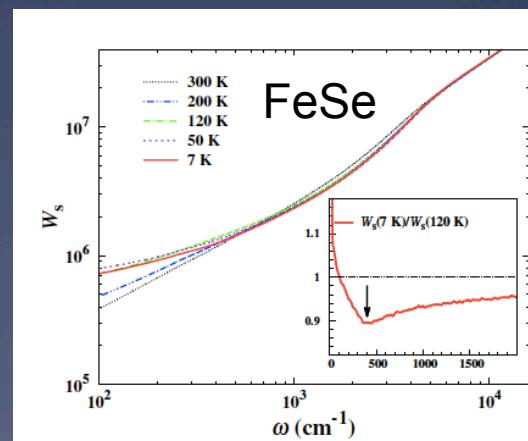
L.B. and E. Cappelletti, PRB 83, 104516 (2011)



A.A.Schafgans et al. PRL 108, 147002



D. Wu et al. PRB 83, 100503 (11)

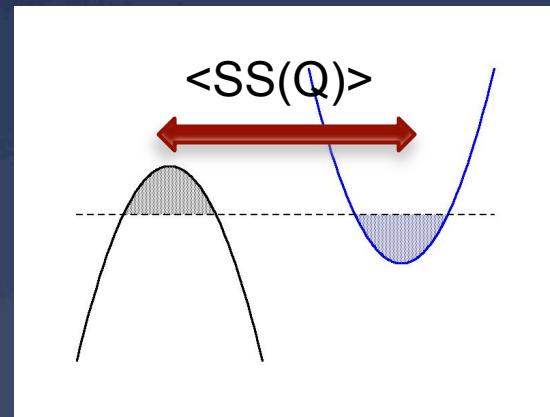


H. Wang, arXiv:1606.02198

# Take-home message I

- \* FS shrinking in iron-based systems is a non-trivial effect due to the multiband character and to the interband interactions

Strong particle-hole asymmetry (almost full/empty bands)



Hole&Electron  
pockets connected  
by interband  
interactions

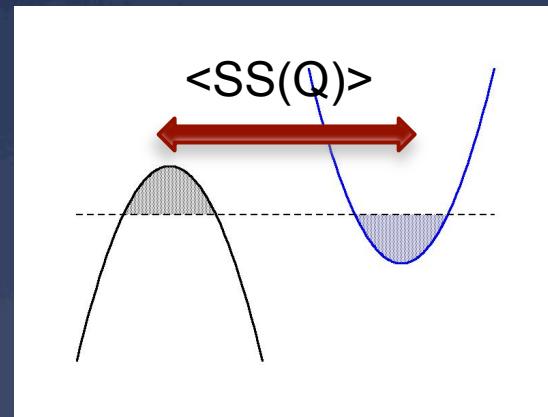
Interband=spin fluctuations



Doping/T dependence FS shrinking= strength of spin fluctuations

We still miss the orbital degrees of freedom  
Let us go back from the band basis to the  
orbital basis

Strong particle-hole  
asymmetry (almost  
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Hole&Electron  
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Interband=spin fluctuations



Doping/T dependence FS shrinking= strength of spin fluctuations

# Low-energy orbital model

- \* Approximate description of the bands with three orbital components  $xz, yz$  and  $xy$

$$\hat{H}_0^l = h_0^l \tau_0 + \vec{h}^l \cdot \vec{\tau}^l = \begin{pmatrix} h_0^l(\mathbf{k}) + h_3^l(\mathbf{k}) & h_1^l(\mathbf{k}) - ih_2^l(\mathbf{k}) \\ h_1^l(\mathbf{k}) + ih_2^l(\mathbf{k}) & h_0^l(\mathbf{k}) - h_3^l(\mathbf{k}) \end{pmatrix}$$

- \* Only  $yz, xz$  at  $\Gamma$ , only  $yz/xz, xy$  at  $X/Y$

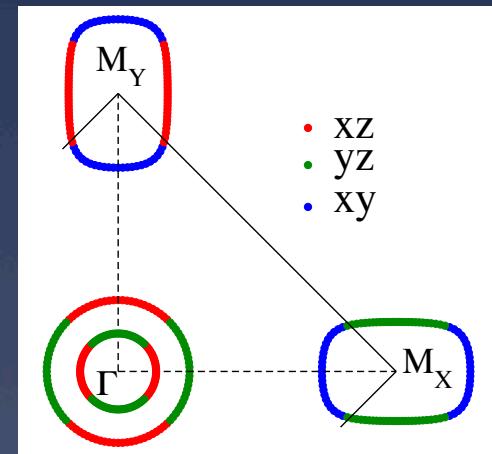
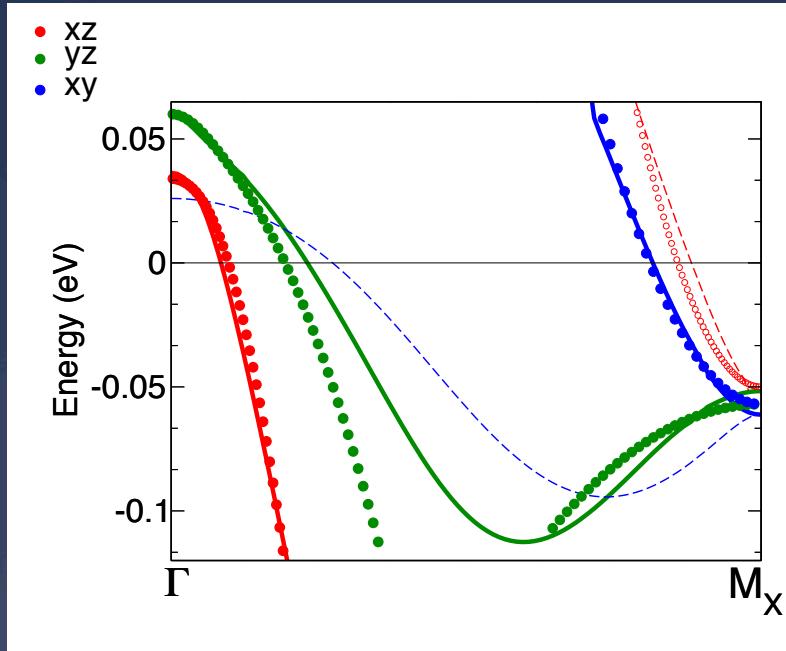
$$\hat{H}_0^\Gamma = \begin{pmatrix} \varepsilon_\Gamma - a_\Gamma k^2 + b_\Gamma(k_x^2 - k_y^2) & -2b_\Gamma k_x k_y \\ -2b_\Gamma k_x k_y & \varepsilon_\Gamma - a_\Gamma k^2 - b_\Gamma(k_x^2 - k_y^2) \end{pmatrix} \quad \Psi^\Gamma = (c^{yz}, c^{xz})$$

$$E^{\Gamma,\pm} = \varepsilon_\Gamma - (a_\Gamma \pm b_\Gamma)k^2$$

See V. Cvektovic and O. Vafek, PRB 88, 134510 (2013)

# Low-energy orbital model

- \* Approximate description of the bands with three orbital components  $xz, yz$  and  $xy$



- \* Mass renormalization and SOC fitted to the experiments

# Low-energy orbital model

- \* Approximate description of the bands with three orbital components
- \* Self-energy effect must be computed in the orbital basis

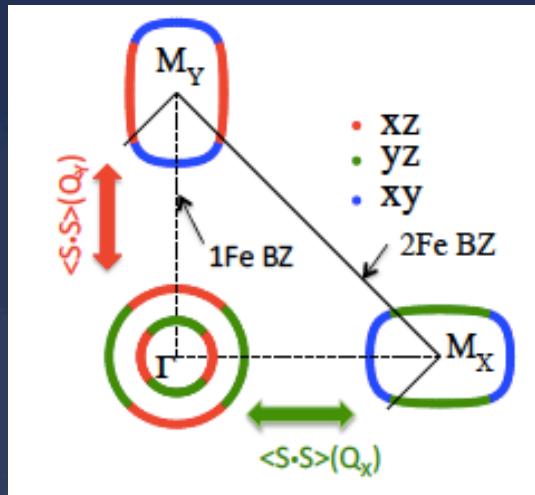
$$\hat{G}^{-1} = \hat{G}_0^{-1} - \hat{\Sigma}$$

- \* Also the microscopic spin-spin interaction carries information on the orbital degrees of freedom

$$H_{int} = -1/2 \sum_{\mathbf{q}'} U_{\eta\eta'} \mathbf{S}_{\mathbf{q}}^{\eta} \cdot \mathbf{S}_{-\mathbf{q}'}^{\eta'}, \quad \mathbf{S}_{\mathbf{q}}^{\eta} = \sum_{\mathbf{k}ss'} (c_{\mathbf{k}s}^{\eta\dagger} \sigma_{ss'} c_{\mathbf{k}+\mathbf{q}s'}^{\eta})$$

# Orbital character and spin fluctuations

- \* The SF along X or Y select different orbitals

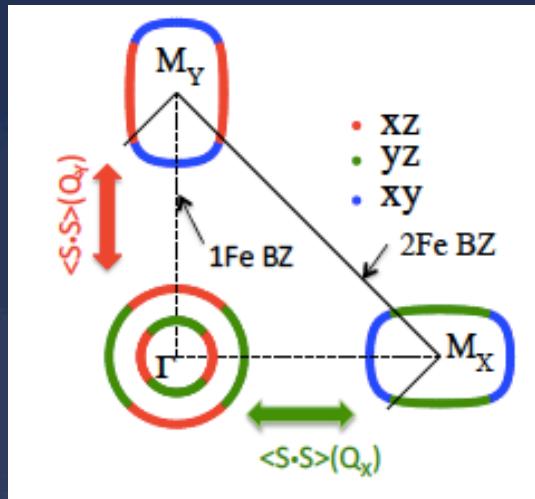


$$\begin{aligned}\langle \mathbf{S} \cdot \mathbf{S} \rangle(Q_X) &\Rightarrow \langle \mathbf{S}_{Q_X}^{yz} \cdot \mathbf{S}_{Q_X}^{yz} \rangle \\ \langle \mathbf{S} \cdot \mathbf{S} \rangle(Q_Y) &\Rightarrow \langle \mathbf{S}_{Q_Y}^{xz} \cdot \mathbf{S}_{Q_Y}^{xz} \rangle\end{aligned}$$

See L. Fanfarillo, A. Cortijo and B. Valenzuela,  
PRB 91, 214515 (15)

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See L. Fanfarillo, A. Cortijo and B. Valenzuela,  
PRB 91, 214515 (15)

## Orbital-selective FS shrinking

- \* The self-energy corrections probe SF in different directions, while the sign is still dictated by the particle-hole asymmetry of the band+interband interaction

$$\hat{\Sigma}^\Gamma = \begin{pmatrix} \Sigma_{yz}^\Gamma & 0 \\ 0 & \Sigma_{xz}^\Gamma \end{pmatrix}$$

$$\hat{\Sigma}^X = \begin{pmatrix} \Sigma_{yz}^X & 0 \\ 0 & 0 \end{pmatrix}$$

$$\hat{\Sigma}^Y = \begin{pmatrix} \Sigma_{xz}^Y & 0 \\ 0 & 0 \end{pmatrix}$$

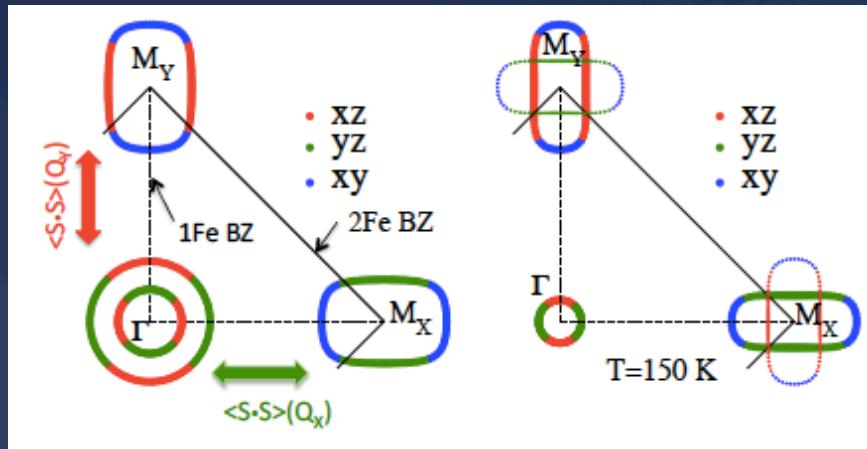
$$\Psi^\Gamma = \begin{pmatrix} c_{yz} \\ c_{xz} \end{pmatrix}$$

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$$\Psi^Y = \begin{pmatrix} c_{xz} \\ c_{xy} \end{pmatrix}$$

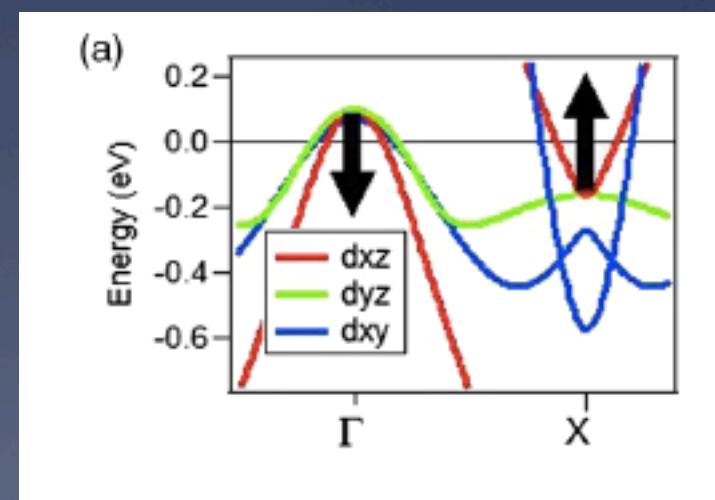
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- \* No effect on the  $xy$  orbital at  $X/Y$ , enhanced ellipticity



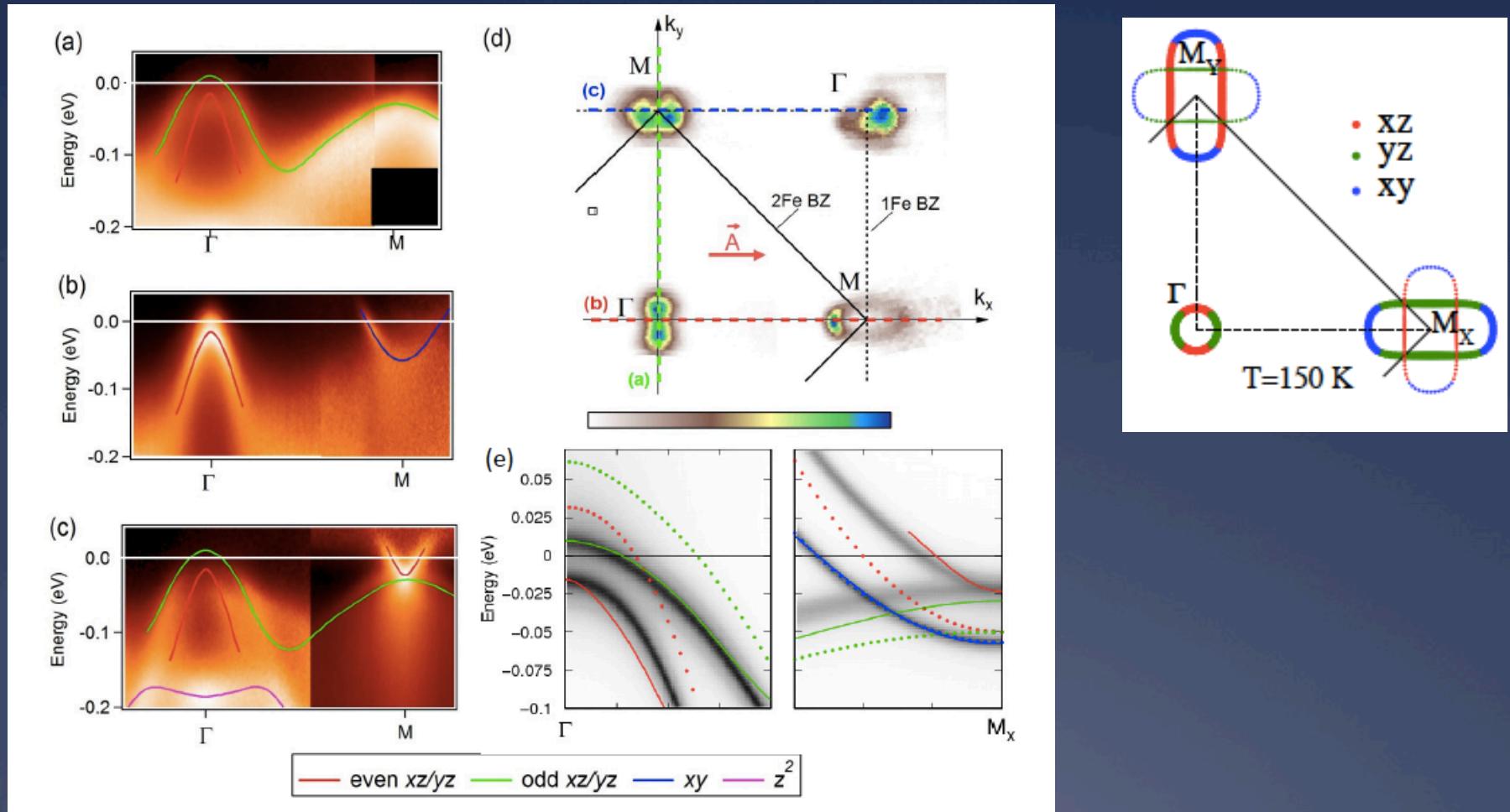
Ba(Fe<sub>1-x</sub>Cox)₂As₂  
V. Brouet et al., PRL 110, 167002 2013

N.B.: in the usual paramagnetic states SF along X or Y are equal



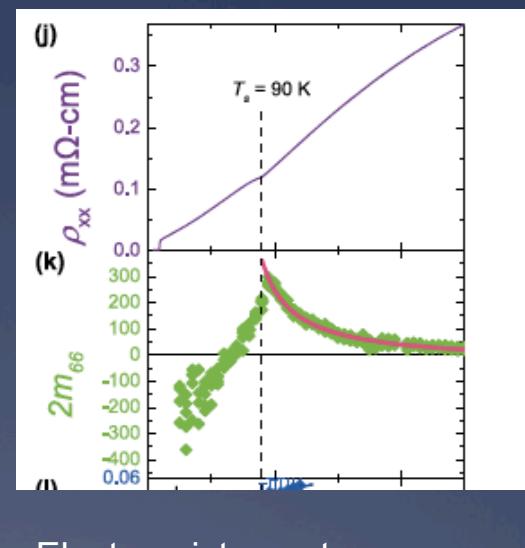
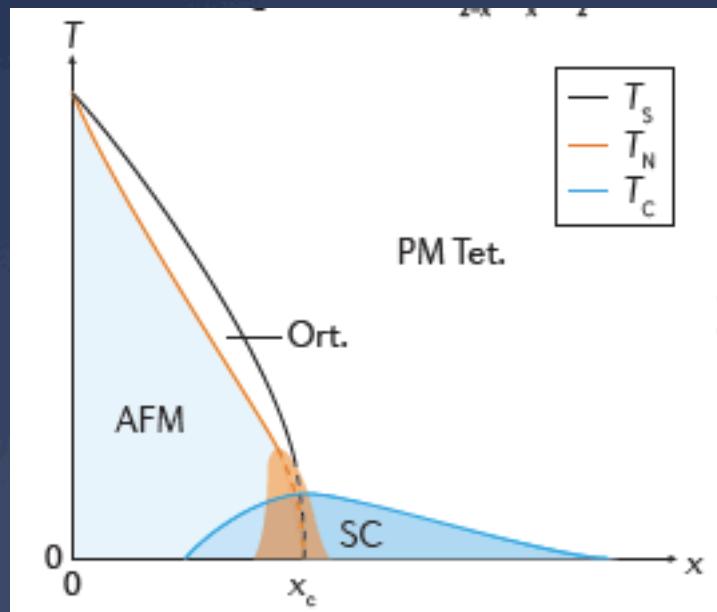
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\* No effect on the  $xy$  orbital at  $X/Y$ , enhanced ellipticity



# Nematicity

- \* Orthorhombic transition at  $T_s$ : electronic-properties anisotropy much larger than what expected from simple structural change

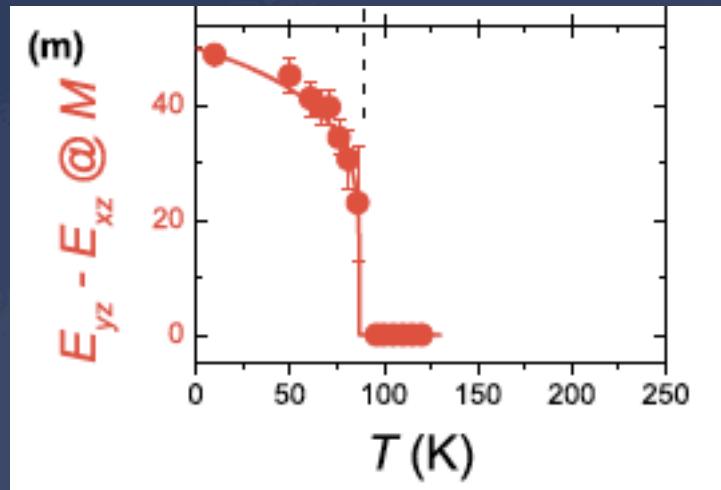


Elastoresistance tensor

# Nematicity

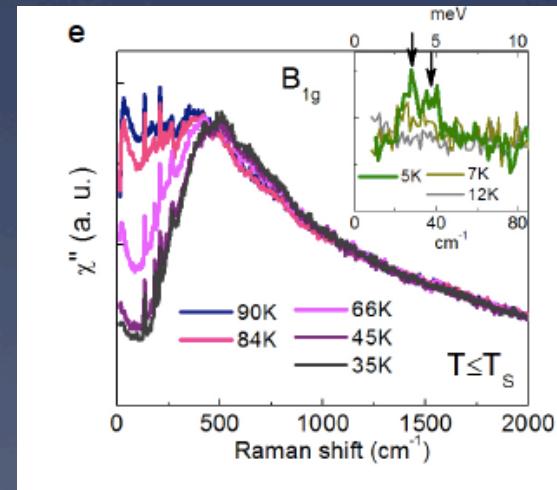
- \* Orthorhombic transition at  $T_s$ : electronic-properties anisotropy much larger than what expected from simple structural change
- \* "Hard": electronic structure (ARPES), orbital order
- \* "Soft": two-particle probes (Raman), spin fluctuations

Splitting of the xz/yz orbitals



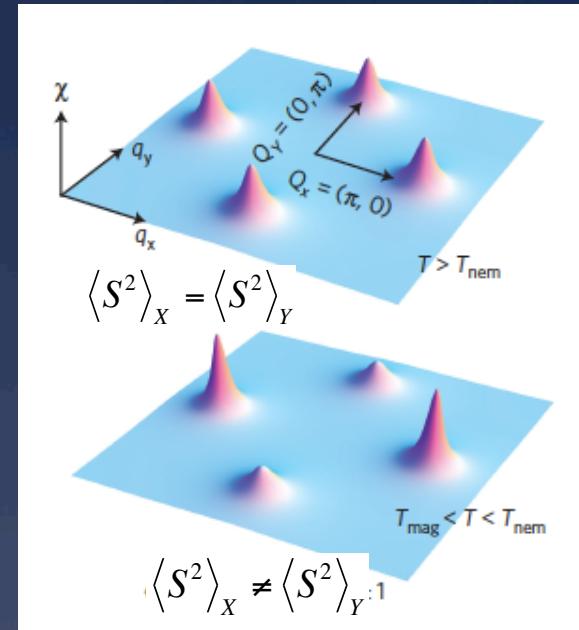
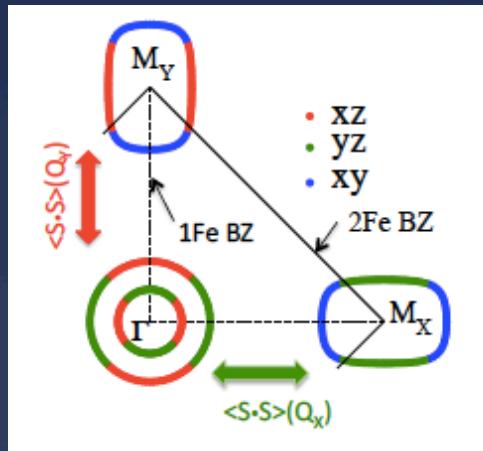
Watson et al. PRB 91, 155106 (15)

Enhanced B1g Raman response



P. Massat et al. arXiv:1603.01492

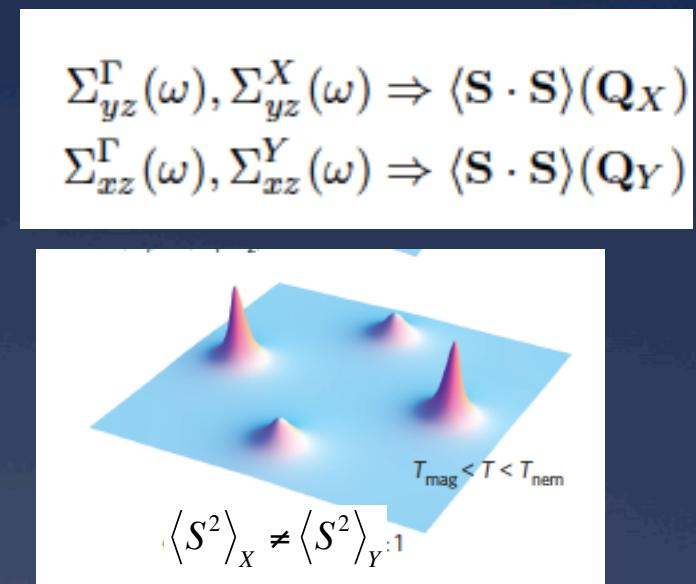
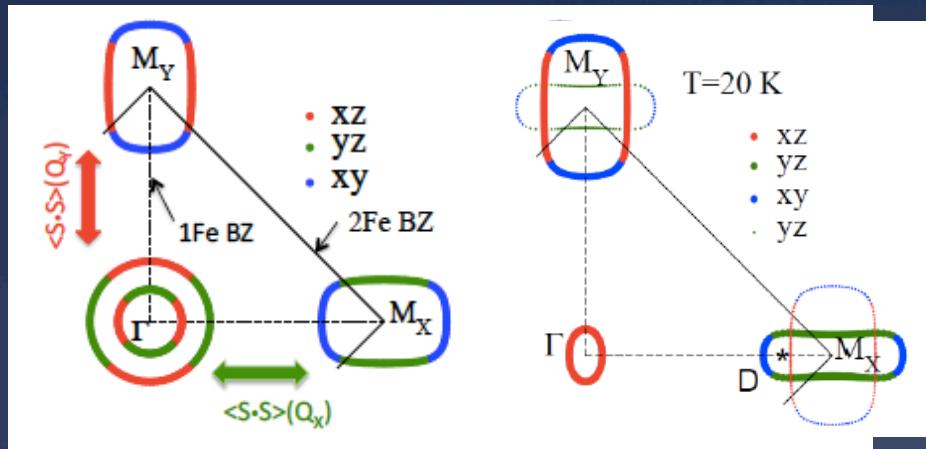
# Nematicity



What happens when SF along X and Y become inequivalent?  
"Soft" nematic transition

Fernandes et al. Nat. Phys'14

# Nematicity



Inequivalent SF  $\rightarrow$  inequivalent orbital self-energy  $\rightarrow$  orbital ordering with different signs at  $\Gamma$  and X/Y

$$\hat{\Sigma}^{\Gamma} = \begin{pmatrix} \Sigma_{yz}^{\Gamma} & 0 \\ 0 & \Sigma_{xz}^{\Gamma} \end{pmatrix} \quad \hat{\Sigma}^X = \begin{pmatrix} \Sigma_{yz}^X & 0 \\ 0 & 0 \end{pmatrix} \quad \hat{\Sigma}^Y = \begin{pmatrix} \Sigma_{xz}^Y & 0 \\ 0 & 0 \end{pmatrix}$$

Curved arrow pointing from the self-energy equations to the Hamiltonian.

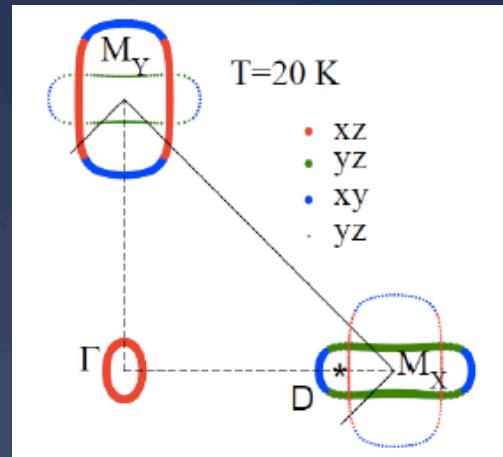
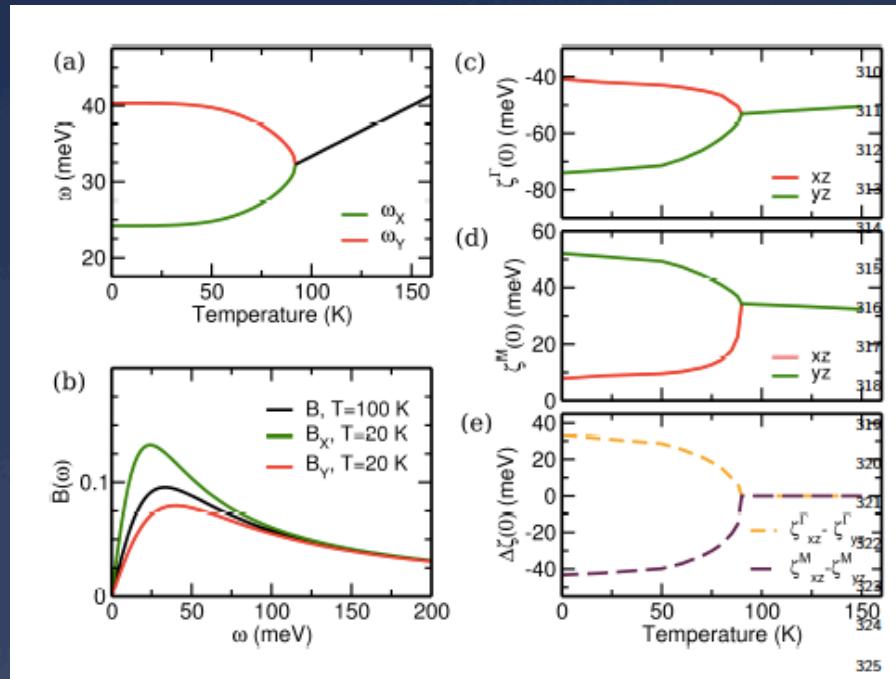
$$H_O = \Delta_b(T) \sum_k (\cos k_x - \cos k_y) [n_{xz}(k) + n_{yz}(k)] + \Delta_s(T) \sum_k [n_{xz}(k) - n_{yz}(k)] +$$

S. Mukherjee et al  
PRL 115, 026402 (15);  
PRB 92, 224515 (15)

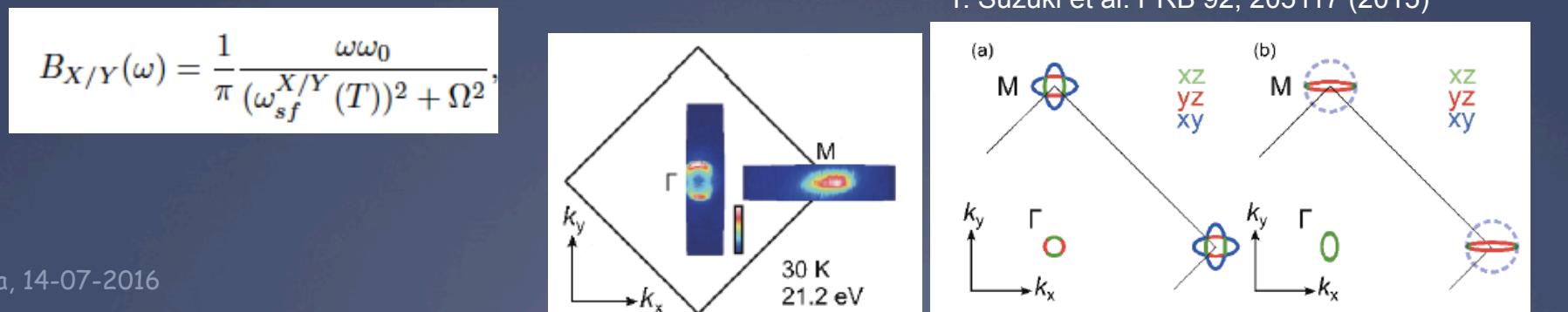
# Nematic FS shrinking

- \* T-dependent inequivalent spin fluctuations

L. Fanfarillo, L.B. et al. arXiv:1605.02482



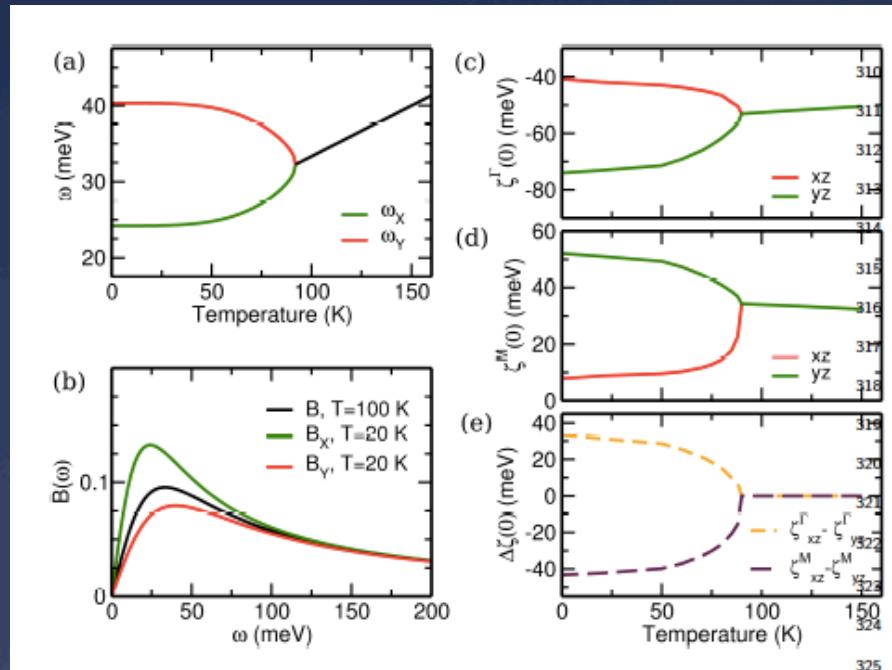
Y. Suzuki et al. PRB 92, 205117 (2015)



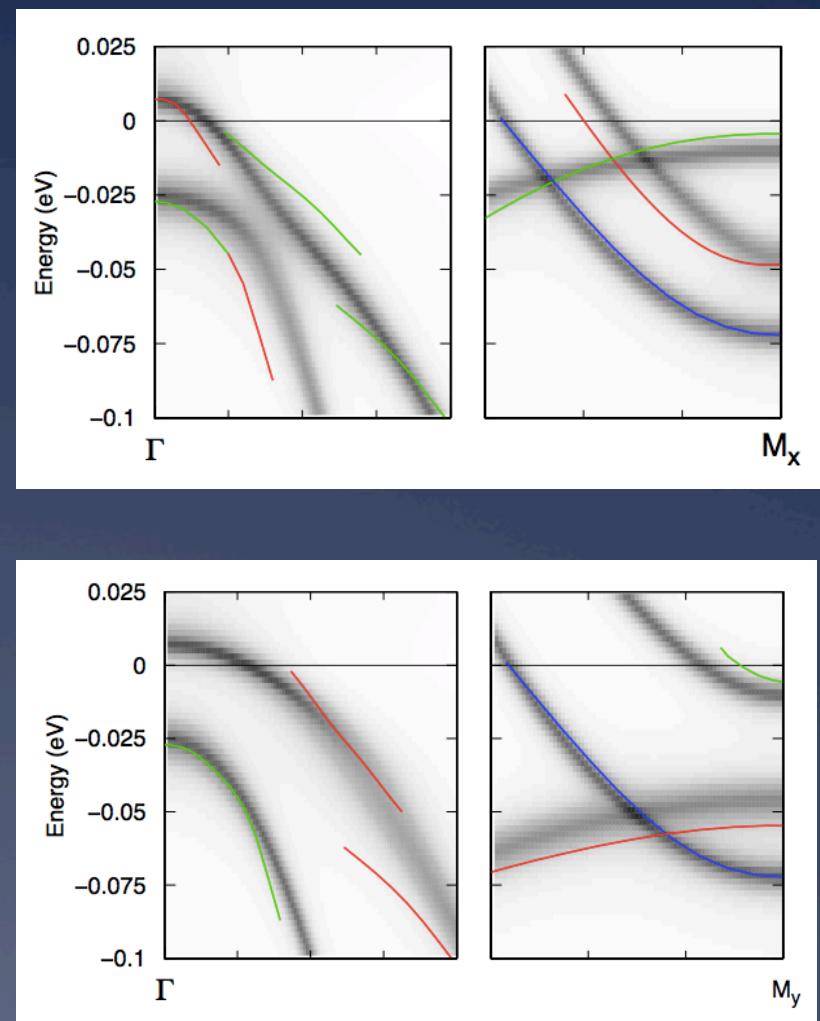
# Nematic FS shrinking

- \* T-dependent inequivalent spin fluctuations

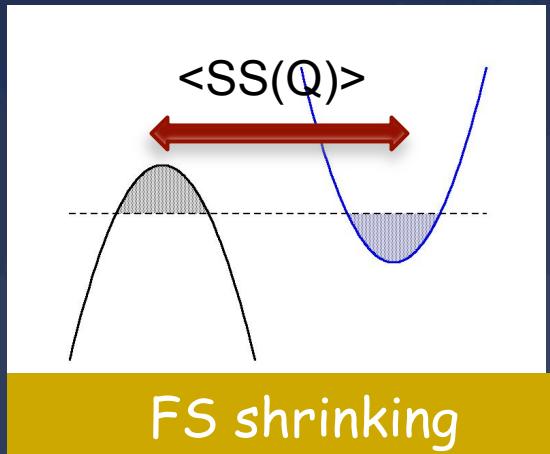
L. Fanfarillo, L.B. et al. arXiv:1605.02482



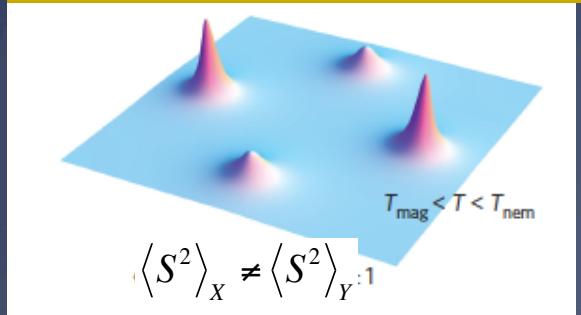
$$B_{X/Y}(\omega) = \frac{1}{\pi} \frac{\omega \omega_0}{(\omega_{sf}^{X/Y}(T))^2 + \Omega^2},$$



# Take-home message (II)



"soft" nematic mechanism



+ Orbital content =

Orbital-selective FS shrinking

+ Orbital-selective FS shrinking =

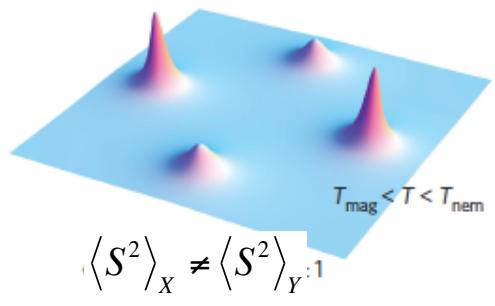
"hard" electronic nematicity

# Take-home message (II)



Orbital order in the nematic phase is the “hard” side of the “soft” spin-fluctuation mechanism

“soft” nematic mechanism



Orbital-selective FS shrinking



“hard” electronic nematicity

More  
(interacting  
electron-hole bands)  
is different!

- Band shrinking and orbital ordering
- Optical sum rule
- Anomalous multiband Hall effect  
*L. Fanfarillo et al. PRL 109, 096402 (2012)*
- Collective superconducting modes, Leggett mode and its signature in Raman  
*M. Marciani et al. PRB 88, 214508 (2013)*  
*T. Cea and L.B. arXiv:1606.04874*

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