Emergence of Homochirality in Chemical Systems



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Year 2008



KEIO 150 Design the Future

History

1858

Keio History & World Timeline



1861 The Civil War breaks out in the United States.

1863 Fukuzawa's school switches its focus to English studies.

 Fukuzawa's school moves to a new location and is renamed after the <u>Keio Era</u>. Three years later, the Keio school moves to Mita, the current site of Keio University's main campus.

1868 The Meiji Restoration begins in Japan.

1869 The Suez Canal opens, shortening the sea route between Europe and Asia.

1874 Keio Yochisha Elementary School is established.

Keio University establishes a college with 1890 Departments of Law, Literature (presently Faculty of Letters), and Economics.

Keio becomes a comprehensive educational 1898 institution with college, secondary and elementary schools.

The Fujiwara Institute of Technology is donated 1944 to Keio University, and becomes the Faculty of Engineering.

Biorhythms

Temporary Periodic Patterns



Cell cycle Circadian rhythm Pulsation

Spatially Periodic Patterns



Surface of Animal Body

Once you know the concept of Temporary and Spatially Periodic Patterns can_ Dissipative Structure be realized by Artificial Chemical Reaction !!

QuickTimey Ç² YUV420 ERA[EIEbEN eLiEEvEçEOEaEA Ç¹³⁸DZÇAEsENE EEǾa©ÇEÇZǽÇ...ÇOiKovÇ-Ç AB

Bray Reaction: W. C. Bray, J. Am. Chem. Soc., 1921, 43, 1262.
Belouzov-Zhabotisky Reaction: B. P. Belouzov, 1958.
Brusselator: I. Prigogine, R. Lefever, J. Phys. Chem., 1958, 48, 1965.



Modeling: A. M. Turing, *Philos. Trans. Roy. Soc. London*, **1952**, *B 237*, 37.

Experimental realization: V. Castets, E. Dulos, J. Boissonade, P. De Kepper, *Phys. Rev. Lett.*, **1990**, *64*, 2953.

Self-Organizationin Nonequilibrium System : Dissipative Structure

Proposed by Ilya Prigogine: Nobel Laureate in Chemistry in 1977



Irreversible Dissipative Processes



Self-Organized State (Dissipative Structure)

- Reaction
- Diffusion
- Heat Conduction

• Oscillation

- Oscillation
- Pattern Formation
- Chiral Symmetry Breaking

Lower Chemical Potential Matter

 $d_{i}S$

Chemical Oscillation



Brusselator (1968)

Spatial Pattern Formation

Turing Model (1942)



$$\frac{\partial X}{\partial t} = -7X^2 - 50XY + 57 + D_X \frac{\partial^2 X}{\partial t^2}$$
$$\frac{\partial Y}{\partial t} = 7X^2 + 50XY - 2Y - 55 + D_Y \frac{\partial^2 Y}{\partial t^2}$$

Turing Pattern Fomation by CIMA Reaction (1990)



FIG. 1. Sustained chemical pattern in the gel strip reactor. (a) Sketch of the reactor: The gel strip is tightly squeezed between two flat plates 1 mm apart. Reactants are fed through the well-mixed reservoirs A and B. (b) Contrast-enhanced image: Dark regions correspond to reduced states colored in blue; clear zones correspond to oxidized states. (c) Enlarged image of the region of pattern (dimensions in mm). Experimental conditions: The gel is prepared by dissolving in 100 ml of water: 17.1 g acrylamide, 0.10 g N,N'-methylene-bisacrylamide, 0.70 g ammonium persulfate, 1.0 g triethanolamine, and 2.8 g thiodène (iodine color indicator from PROLABO). A thin uniformly flat layer of the solution is left to polymerize at 0°C for 1 h. The resulting sheet of polymer is then thoroughly washed and set to swell in water for 24 h before the reactor strip is cut off. After swelling of the gel, the concentration of the color indicator (taken as amylose) is $\sim 10^{-4}$ mole/l and does not significantly decay during the experiments. Boundary feed compositions: in A, [NaClO₂] δ = 2.6×10⁻² mole/l, [K1] δ = 3.0×10⁻³ mole/l, [NaOH] δ = 10⁻² mole/l, [NaOH] δ = 10⁻² mole/l, [NaOH] δ = 3×10⁻³ mole/l; in B, [CH₂(COOH)₂] δ = 9×10⁻³ mole/l, [K1] δ = 3.0×10⁻³ mole/l, [H₂SO₄] δ = 10⁻² mole/l, [NaOH] δ = 3×10⁻³ mole/l; [Na₂SO₄] δ = 3×10⁻³ mole/l. Temperature: 7°C.

Linear Stability Analysis for Two Variables System

Rate equation (Time derivative of concentration)

$$\frac{dX}{dt} = f(X,Y)$$
$$\frac{dY}{dt} = g(X,Y)$$

Steady state solution

$$f(X,Y) = 0, g(X,Y) = 0 \longrightarrow X_{SS}, Y_{SS}$$

Perturbation by Fluctuation

$$X = X_{SS} + \delta X$$
$$Y = Y_{SS} + \delta Y$$

Linear Stability Analysis for Two Variables System

First order term of Taylor series

$$\frac{d\delta X}{dt} = \left(\frac{\partial f}{\partial X}\right)_{SS} \delta X + \left(\frac{\partial f}{\partial Y}\right)_{SS} \delta Y$$
$$\frac{d\delta Y}{dt} = \left(\frac{\partial g}{\partial X}\right)_{SS} \delta X + \left(\frac{\partial g}{\partial Y}\right)_{SS} \delta Y$$

Fluctuation

 $\delta X = c_1 \exp(\lambda t), \ \delta Y = c_2 \exp(\lambda t)$

Jacobian matrix

$$\mathbf{J} = \begin{vmatrix} \frac{\partial f}{\partial X} & \frac{\partial f}{\partial Y} \\ \frac{\partial g}{\partial X} & \frac{\partial g}{\partial Y} \end{vmatrix} \qquad \mathbf{C} = \begin{vmatrix} c_1 \\ c_2 \end{vmatrix} \qquad (\mathbf{J} - \lambda \mathbf{I})\mathbf{C}$$

- 1

Linear Stability Analysis for Two Variables System

Characteristic equation

 $\lambda^2 - \lambda tr(\mathbf{J}) + \det(\mathbf{J}) = 0$



Oscillating Mouse & Traveling Wave Mouse

"Traveling stripes on the skin of a mutant mouse" N. Suzuki, M. Hirata, S. Kondo, *P. Natl. Acad. Sci. USA*, **100**, 9680-9685 (2003)



Fig. 3. Pattern change of a homozygous *Foxn1tw* mouse during the 30-day cycle. (*a*) Days 30-60. (*b*) Days 90-120. (*c*) Days 210-240 after birth. Pictures are taken at 5-day intervals with a Nikon digital camera. The pattern change shown here is typical for a homozygous *Foxn1tw* mouse.

Chiral Aymmetry



α -Helix of Protein and Double Helix of DNA





Frank's Model

$$\frac{dL}{dt} = k_1A + k_2AL - k_3LD$$

$$\frac{dD}{dt} = k_1A + k_2AD - k_3LD$$

$$A \longrightarrow L \qquad A \longrightarrow D$$

$$A \longrightarrow D$$

$$A \longrightarrow L \qquad A \longrightarrow D$$

$$A \longrightarrow D$$

$$A \longrightarrow D$$

$$A \longrightarrow D$$

$$A \longrightarrow D$$

$$J = \begin{bmatrix} Ak_2 - k_3D & -k_3L \\ -k_3D & Ak_2 - k_3L \end{bmatrix} \qquad \qquad \lambda_1 = Ak_2 > 0$$
$$\lambda_2 = -\sqrt{(Ak_2)^2 + 4Ak_1k_3}$$

D. K. Kondepudi, G. W. Nelson, Nature, 1985, 314, 438-441.

Chiral Symmetry Breaking Transition by Kondepudi & Nelson's Model



D. K. Kondepudi, G. W. Nelson, *Nature*, **1985**, *314*, 438-441.

Frank's Model



F. C. Frank, Biophys. Acta, 1953, 11, 459-463.

Convection Pattern Formation on Earth



Chiral Symmetry Breaking Transition

$$S T$$

$$S + T \stackrel{k_{1f}}{\underset{k_{1r}}{\underset{k_{2f}}{\underset{k_{2r}}}{\underset{k_{2r}}{k_{2r}}{\underset{k$$

D. K. Kondepudi, G. W. Nelson, Nature, 1985, 314, 438-441.

Chiral Autocatalysis in Crystallization of 1, 1'-Binaphthyl

1, 1'-Binaphthyl m.p.: Racemic crystal: 145°C; Chial crystal: 158°C





D. K. Kondepudi, K. Asakura, et al., J. Am. Chem. Soc., 1999, 121, 1448-1451.

Crystal Growth of of 1, 1'-Binaphthyl



K. Asakura, D. K. Kondepudi, et al., Chirality, 2002, 14, 85-89.

Crystal Growth Front as an Open System



K. Asakura, D. K. Kondepudi, et al., Chirality, 2004, 16, 131-136.

Chiral Symmetry Breaking Transition in Crystallization of 1, 1'-Binaphthyl



K. Asakura, D. K. Kondepudi, et al., J. Phys. Chem. B, 2005, 109, 1586-1592.

Crystallization Front Model

Liquid phase: L Growth layer: G_S , G_R Interface of crystal to liquid: I_S , I_R Crystal bulk phase: C_S , C_R



$$L + I_{S} \xrightarrow{k_{01}} G_{S} + C_{S}$$

$$L + I_{R} \xrightarrow{k_{01}} G_{R} + C_{R}$$

$$L + I_{S} \xrightarrow{k_{02}} G_{R} + C_{S}$$

$$L + I_{R} \xrightarrow{k_{02}} G_{S} + C_{R}$$

$$L + I_{S} + G_{S} \xrightarrow{k_{11}} 2 G_{S} + C_{S}$$

$$L + I_{R} + G_{R} \xrightarrow{k_{11}} 2 G_{R} + C_{R}$$

$$L + I_{S} + G_{R} \xrightarrow{k_{12}} G_{S} + G_{R} + C_{S}$$

$$L + I_{S} + G_{R} \xrightarrow{k_{12}} 2 G_{R} + C_{S}$$

$$L + I_{S} + G_{R} \xrightarrow{k_{12}} 2 G_{S} + C_{R}$$

$$L + I_{R} + G_{S} \xrightarrow{k_{12}} 2 G_{S} + C_{R}$$

$$L + I_{R} + G_{S} \xrightarrow{k_{12}} 2 G_{S} + C_{R}$$

$$L + I_{R} + G_{S} \xrightarrow{k_{13}} G_{S} + G_{R} + C_{R}$$

$$L + I_{S} + G_{R} \xrightarrow{k_{13}} G_{S} + G_{R} + C_{R}$$

$$L + I_{R} + G_{R} \xrightarrow{k_{13}} G_{S} + G_{R} + C_{R}$$

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$$L + I_{R} + G_{R} \xrightarrow{k_{13}} G_{S} + G_{R} + C_{R}$$

$$L + I_{R} + G_{R} \xrightarrow{k_{13}} G_{S} + G_{R} + C_{R}$$

Kinetic Equations and Their Simplification

$$\frac{dG_s}{dt} = k_{01}I_s + k_{02}I_R + k_{11}I_SG_s + k_{12}(I_SG_R + I_RG_S) + k_{13}I_RG_R - k_{20}G_S$$

$$\frac{dG_R}{dt} = k_{01}I_R + k_{02}I_S + k_{11}I_RG_R + k_{12}(I_SG_R + I_RG_S) + k_{13}I_SG_S - k_{20}G_R$$

$$\frac{dI_s}{dt} = -k_{01}I_S - k_{02}I_S - k_{11}I_SG_S - 2k_{12}I_SG_R - k_{13}I_SG_S + k_{20}G_S$$

$$\frac{dI_R}{dt} = -k_{01}I_R - k_{02}I_R - k_{11}I_RG_R - 2k_{12}I_RG_S - k_{13}I_RG_R + k_{20}G_R$$

$$k_{02} \cong 0, k_{13} \cong 0$$

$$\frac{dG_s}{dt} = k_{01}I_S + k_{11}I_SG_S + k_{12}(I_SG_R + I_RG_S) - k_{20}G_S$$

$$\frac{dG_R}{dt} = k_{01}I_R + k_{11}I_RG_R + k_{12}(I_SG_R + I_RG_S) - k_{20}G_R$$

$$\frac{dI_s}{dt} = -k_{01}I_S - k_{11}I_SG_S + 2k_{12}I_SG_R + k_{20}G_S$$

$$\frac{dI_s}{dt} = -k_{01}I_R - k_{11}I_SG_S + 2k_{12}I_SG_R + k_{20}G_S$$

Steady State Solution of Kinetic Model

Symmetric steady state

$$G_{S} = G_{R} = \frac{-2k_{01} + k_{11} + 2k_{12} - 2k_{20} + \sqrt{(2k_{01} - k_{11} - 2k_{12} + 2k_{20})^{2} + 4(2k_{11} + 4k_{12})k_{01}}}{2(2k_{11} + 4k_{12})}$$

$$I_{S} = I_{R} = \frac{2k_{01} + k_{11} + 2k_{12} + 2k_{20} - \sqrt{(2k_{01} - k_{11} - 2k_{12} + 2k_{20})^{2} + 4(2k_{11} + 4k_{12})k_{01}}}{2(2k_{11} + 4k_{12})}$$

Asymmetric steady state

$$\begin{bmatrix} G_{s} = \frac{-k_{01} + k_{11} - k_{20} + \sqrt{\left(k_{01} - k_{11} + k_{20}\right)^{2} + 4k_{01}k_{11}}}{2k_{11}} \\ I_{s} = \frac{k_{01} + k_{11} + k_{20} - \sqrt{\left(k_{01} - k_{11} + k_{20}\right)^{2} + 4k_{01}k_{11}}}{2k_{11}} \\ G_{R} = I_{R} = 0 \end{bmatrix} \begin{bmatrix} G_{s} = I_{s} = 0 \\ G_{R} = I_{s} = 0 \\ G_{R} = \frac{-k_{01} + k_{11} - k_{20} + \sqrt{\left(k_{01} - k_{11} + k_{20}\right)^{2} + 4k_{01}k_{11}}}{2k_{11}} \\ I_{R} = \frac{k_{01} + k_{11} + k_{20} - \sqrt{\left(k_{01} - k_{11} + k_{20}\right)^{2} + 4k_{01}k_{11}}}{2k_{11}} \\ I_{R} = \frac{k_{01} + k_{11} + k_{20} - \sqrt{\left(k_{01} - k_{11} + k_{20}\right)^{2} + 4k_{01}k_{11}}}{2k_{11}} \end{bmatrix}$$

Back to Complex Kinetic Model

$$\frac{dG_{S}}{dt} = k_{01}I_{S} + k_{11}I_{S}G_{S} + k_{12}(I_{S}G_{R} + I_{R}G_{S}) - k_{20}G_{S}$$

$$\frac{dG_{R}}{dt} = k_{01}I_{R} + k_{11}I_{R}G_{R} + k_{12}(I_{S}G_{R} + I_{R}G_{S}) - k_{20}G_{R}$$

$$\frac{dI_{S}}{dt} = -k_{01}I_{S} - k_{11}I_{S}G_{S} + 2k_{12}I_{S}G_{R} + k_{20}G_{S}$$

$$\frac{dI_{R}}{dt} = -k_{01}I_{R} - k_{11}I_{R}G_{R} + 2k_{12}I_{R}G_{S} + k_{20}G_{R}$$

$$k_{02} \neq 0, k_{13} \neq 0$$

$$\frac{dG_s}{dt} = k_{01}I_s + k_{02}I_R + k_{11}I_sG_s + k_{12}(I_sG_R + I_RG_s) + k_{13}I_RG_R - k_{20}G_s$$

$$\frac{dG_R}{dt} = k_{01}I_R + k_{02}I_s + k_{11}I_RG_R + k_{12}(I_sG_R + I_RG_s) + k_{13}I_sG_s - k_{20}G_R$$

$$\frac{dI_s}{dt} = -k_{01}I_s - k_{02}I_s - k_{11}I_sG_s - 2k_{12}I_sG_R - k_{13}I_sG_s + k_{20}G_s$$

$$\frac{dI_R}{dt} = -k_{01}I_R - k_{02}I_R - k_{11}I_RG_R - 2k_{12}I_RG_s - k_{13}I_RG_R + k_{20}G_R$$

XRD Analysis of Crystal Phase of 1, 1'-Binaphthyl 1, 1'-XRD





K. Asakura, D. K. Kondepudi, et al., Chirality, 2004, 16, 131-136.

Linear Stability Analysis

Jacobian Matrix



$$= \begin{bmatrix} k_{11}I_{s} + k_{12}I_{R} - k_{20} & k_{12}I_{s} & k_{01} + k_{11}G_{s} + k_{12}G_{R} & k_{12}G_{s} \\ k_{12}I_{R} & k_{11}I_{R} + k_{12}I_{s} - k_{20} & k_{12}G_{R} & k_{01} + k_{11}G_{R} + k_{12}G_{s} \\ -k_{11}I_{s} + k_{20} & -2k_{12}I_{s} & -k_{01} - k_{11}G_{s} - 2k_{12}G_{R} & 0 \\ -2k_{12}I_{R} & -k_{11}I_{R} + k_{20} & 0 & -k_{01} - k_{11}G_{R} - 2k_{12}G_{s} \end{bmatrix}$$

Linear Stability Analysis

Eigenvalues for Asymmetric Solution

$$\lambda_1 = 0, \ \lambda_2 = -\sqrt{\left(k_{01} - k_{11} + k_{20}\right)^2 + 4k_{01}k_{11}}$$

 $k_{01} = 0.001, \ k_{12} = 0.002, \ k_{20} = 0.002, \ 0.005, \ 0.01$



Linear Stability Analysis

Eigenvalues for Symmetric Solution

 $k_{01} = 0.001, \ k_{12} = 0.002, \ k_{20} = 0.002, \ 0.005, \ 0.01$



Bifurcation Diagram



K. Asakura, R. Plasson, D. K. Kondepudi, *Chaos*, **2006**, *16*, 037116.

R. Plasson, D. K. Kondepudi, K. Asakura, *J. Phys. Chem. B*, **2006**, *110*, 8481-8487.

K. Asakura, D. K. Kondepudi, *et al.*, *J. Phys. Chem. B*, **2005**, *109*, 1586-1592.

Chiral Symmetry Breaking Transition

$$S T$$

$$S + T \stackrel{k_{1f}}{\underset{k_{1r}}{\underset{k_{2f}}{\underset{k_{2r}}}{k$$

D. K. Kondepudi, G. W. Nelson, Nature, 1985, 314, 438-441.

Chirally Autocatalytic Reaction



FIG. 2 Proposed reaction scheme of asymmetric autocatalysis of (S)-1.



FIG 1. Asymmetric autocatalysis of chiral pyrimidyl alkanol (1). Runs A1–3 correspond to Table 1. The enantiomeric excess of (S)-1 increases from 5 to 89% e.e. without the use of additional chiral auxiliaries. During the reactions (runs A1–3), the (S)-1 increases by a factor of 94 times, while (R)-1 increases by a factor of only eight times.

K. Soai, T. Shibata, H. Morioka, K. Choji, Nature, 1995, 378, 767-768.

Soai Reaction



Figure 1. Process for replicative asymmetric amplification.

D. A. Singleton, L. K. Vo, J. Am. Chem. Soc, **2002**, 124, 10010-10011.

-		-	-		
trial*	% ee ^ø	trial ^a	% ee ^s	trial®	% ee ^ø
10	16 S*	17 ^{g,i,u}	65 S ^m	33 ^{e, s,u}	21 <i>S</i> ¹
2°,t	11 S ^k , 78 S ^l	18 ^{g,i,u}	70 S ^m	34 ^{e, s, u}	81 R ⁱ
30,d	18 S ^k	19 ^{g,i,r,u}	85 S ⁱ	35 ^{0,h,u}	29 S ⁱ
40,d	16 S ^k	208,i,r,u	86 S ^I	36 ^{c,h,u}	29 S ^I
5°.«.j	32 S ¹	21 ^{g,h,i}	48 S ⁱ	37 ^{g,i,h,r,µ}	18 S ^I , 54 S ^m
6°fj	22 S ¹	228,h,i	52 S ^I	388.1,4	11 S ¹ , 42 S ⁿ
7°fh.j	30 R ^m	23 ^{g,h,i,u}	48 S ⁱ	39 ^{g,i,u}	5 S ^k , 48 S ⁱ
80,e,h,j,t,u	80 <i>S</i> ⁿ	24 ^{g,i,u}	37 S ⁱ	40 ^{g,i,u,v}	3 S ^k , 43 S ^l
9°.e.j.t.u	75 S ⁿ	25 ^{g,h,i}	32 S ^I	41 ^{e,i,u}	18 Sª, 48 S°
10 ^{e,h,u}	26 R ^I	26 ^s	21 R ¹	42 ^{e,i,u}	8 S ^m , 32 S ⁿ
11 ^{<i>i</i>,<i>u</i>}	54 S ¹	270,5	67 S ^m	43e,i,h,u	4 SP, 18 S9
12°,h,u	22 R ^I	28 ^{e,j,s,u}	25 R ^I	44 ^{e,i,u}	22 SP, 45 SI
130,4	23 R ^I	29с.ј.з.и	32 S ^I	45 ^{e,i,u}	5 Sª, 21 Sº
14 ^{e,h}	48 R ^m	30 ^{e,j,s,u}	26 R ^I	46 ^{e,i,u}	4 Sª, 24 S⁰
15 ^{e,i}	21 Sª, 70 S°	31 <i>e.j.s.u</i>	18 <i>S</i> ⁱ	47 ^{e,h,i,u}	8 Sª, 26 S°
16 ^{e,i}	13 <i>S</i> ¹	32 ^{e,s,t}	34 R ⁱ	48 ^{e,i,u}	13 Sª, 21 Sº

Table 1. Results from Trials of Replicative Asymmetric Amplification without Discrete Optically Active Additives

^{*a*} The trials employed the procedure of Figure 1, transferring 10% of the product solution at each generation unless otherwise noted. ^{*b*} Determined by NMR using Eu(hfc)₃. ^{*c*} Toluene solvent, reagent grade or purified as noted. ^{*d*} Solvent distilled from P₂O₅. ^{*c*} Solvent distilled from Na/benzophenone. ^{*f*} Solvent treated with H₂SO₄ followed by distillation. ^{*b*} Solvent purified by repeated crystallization. ^{*h*} New batch of solvent, relative to previous otherwise identical trials. ^{*i*} Benzene solvent, reagent grade or purified as noted. ^{*j*} Reaction in Teflon flask. ^{*k*} After second generation. ^{*i*} After third generation. ^{*m*} After fourth generation. ^{*n*} After fifth generation. ^{*o*} After sixth generation. ^{*p*} After seventh generation. ^{*q*} After eighth generation. ^{*r*} Transferring 2.5% of the product solution at each generation. ^{*s*} Ethyl ether solvent, reagent grade or purified as noted. ^{*i*} Reaction used a Teflon septum. ^{*w*} The pairs of trials 8/9, 12/13, 17/18, 19/20, 23/24, 28/29, 30/31, 33/34, 35/36, 37/38, 39/40, 41/42, 43/44, 45/46, and 47/48 were carried out side-by-side using identical reagents. ^{*w*} Absence of light.

Large Variation in ee and Rate of Reaction Observed in Soai Reaction



I. D. Gridnev, Chem. Lett., 2006, 35, 148-153.

Crazy Clock

I. R. Epstein, N ature, 1995, 374, 321-327.

I. Nagypal, I. R. Epstein, J. Chem. Phys., 1988, 89, 6925-6928.

 $4S_2O_3^{2-} + CIO_2^{-} + 2H_2O = 2S_4O_6^{3-} + 4OH^- + CI^ S_2O_3^{2-} + 2CIO_3^{-} + H_2O = 2SO_4^{2-} + 2CI^- + 2H^+$



Figure 5. Cumulative probability distribution of reaction times at several stirring rates in a 4.00-cm³ reaction mixture at 20.0 °C. Symbols: •, 500 rpm; ©, 620 rpm; △, 760 rpm.



Figure 8. Representative pH traces of the reaction at 20.0 °C (see text). Successive ourves are shifted by 0.07 pH units for better viewing, since in the absence of a shift, the initial portions of the curves coincide.