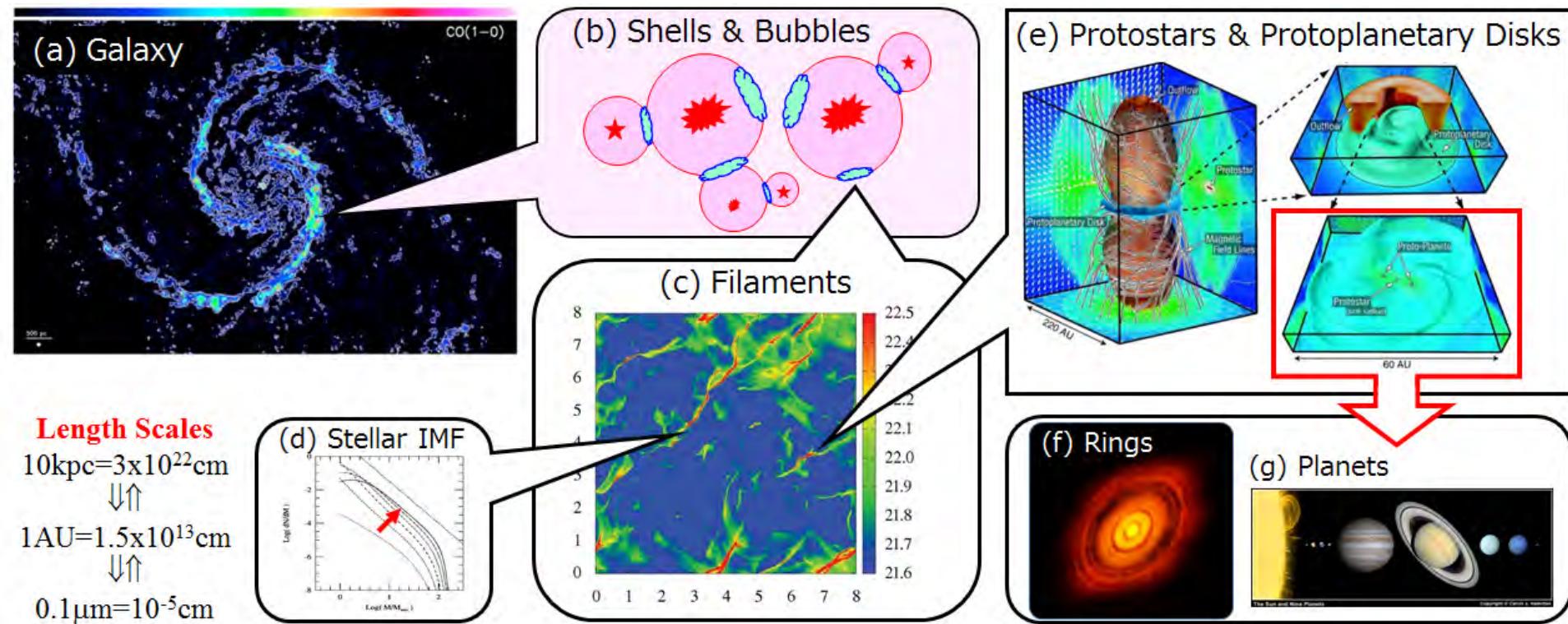


Phase Transition Dynamics of ISM: The Formation of Molecular Clouds and Galactic Star Formation

Shu-ichiro Inutsuka (Nagoya University)



Outline

- Formation of Molecular Clouds
 - Phase Transition Dynamics
 - Thermal Instability, Sustained Turbulence
 - Effect of Magnetic Field
- Self-Gravitational Dynamics of Filaments
 - Mass Function of Dense Cores → IMF
- Galactic Picture of Cloud/Star Formation
 - Destruction of Molecular Clouds
 - SF Efficiency & Schmidt-Kennicutt Law
 - Mass Function of Molecular Clouds
- Summary

Dynamical Timescales of ISM

Dynamical Three Phase Medium

- e.g., McKee & Ostriker 1977
 - SN Explosion Rate in Galaxy... $1/(100\text{yr})$
 - Expansion Time... 1Myr
 - Expansion Radius... 100pc
- $(10^{-2}\text{ yr}^{-1}) \times (10^6\text{ yr}) \times (100\text{pc})^3 = 10^{10} \text{ pc}^3 \sim V_{\text{Gal.Disk}}$
- $(10\text{kpc})^2 \times 100\text{pc}$

Dynamical Timescale of ISM $\sim 1\text{Myr}$

\ll Timescale of Galactic Density Wave $\sim 100\text{Myr}$

Expanding HII regions can be more important!

Basic Equations for ISM Dynamics

- Eq. of Continuity

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x}(\rho v) = 0$$

- EoM

$$\frac{\partial}{\partial t}(\rho v) + \frac{\partial}{\partial x}(P + \rho v^2 + \Pi) = 0$$

- Eq. of Energy

- Radiative Heating & Cooling: Γ, Λ

- H, C⁺, O, Fe⁺, Si⁺, H₂, CO

- Chemical Reaction

- HII, HI, H₂, CII, CO

- Thermal Conduction

- conduction coefficient: κ

$$\begin{aligned}\frac{\partial E}{\partial t} + \frac{\partial}{\partial x} \left((E + P)v - \kappa \frac{\partial T}{\partial x} \right) \\ = \rho \Gamma - \rho^2 \Lambda\end{aligned}$$

Self-Gravity Negligible for Low Density Gas

for $M < M_{\text{Jeans}}$

Observed “Turbulence” in ISM

Observation of Molecular Clouds

line-width $\delta v > C_S$

Universal Supersonic Velocity Dispersion

even in the clouds without star formation activity

→ should not be due to star formation activity

Numerical Simulation of (Isothermal) MHD

Turbulence \Rightarrow Rapid Shock Dissipation or Cascade

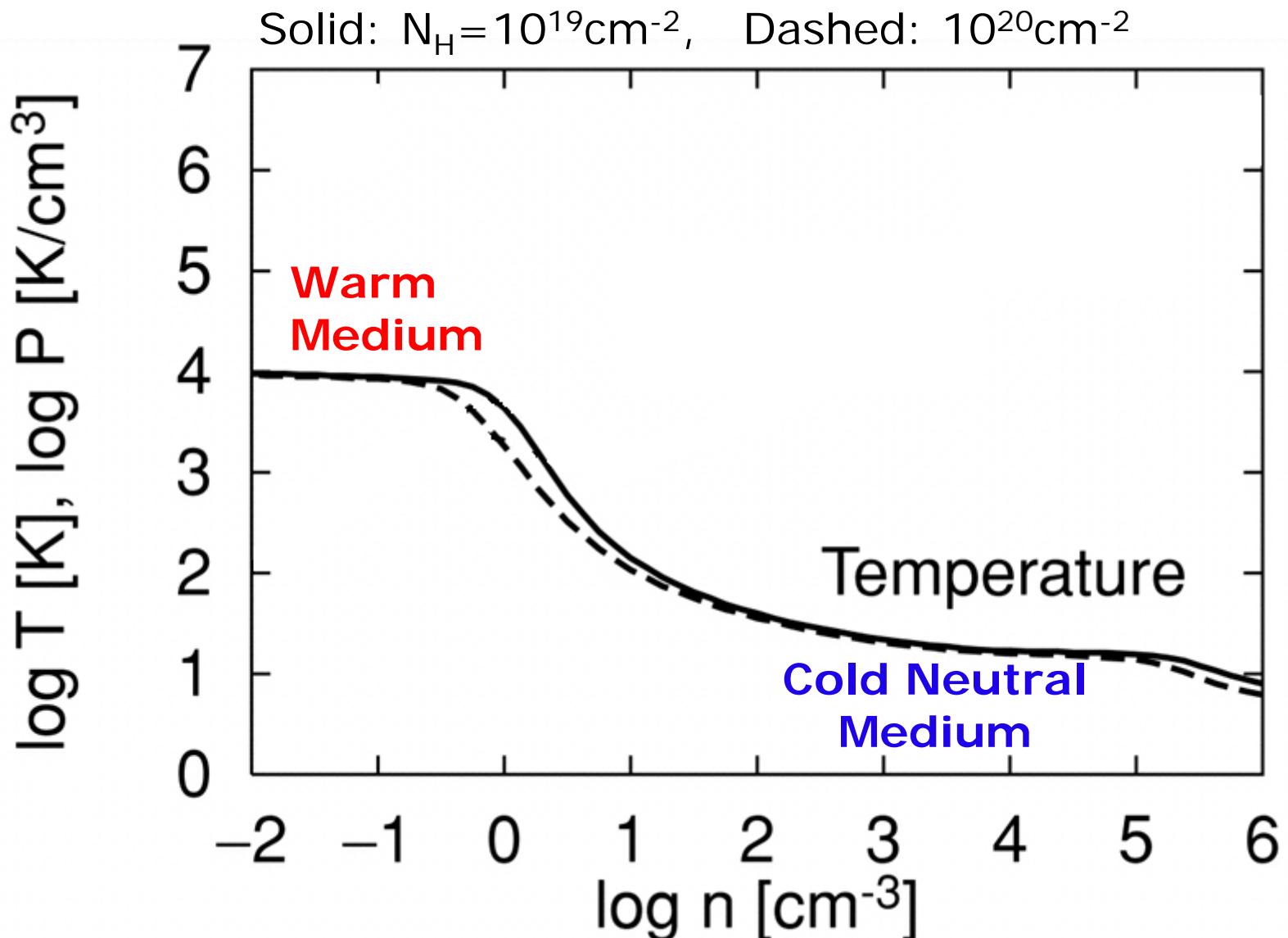
– Dissipation time « Lifetime of Molecular Clouds

- Gammie & Ostriker 1996, Mac Low 1997, Ostriker et al. 1999, Stone et al. 1999, etc...

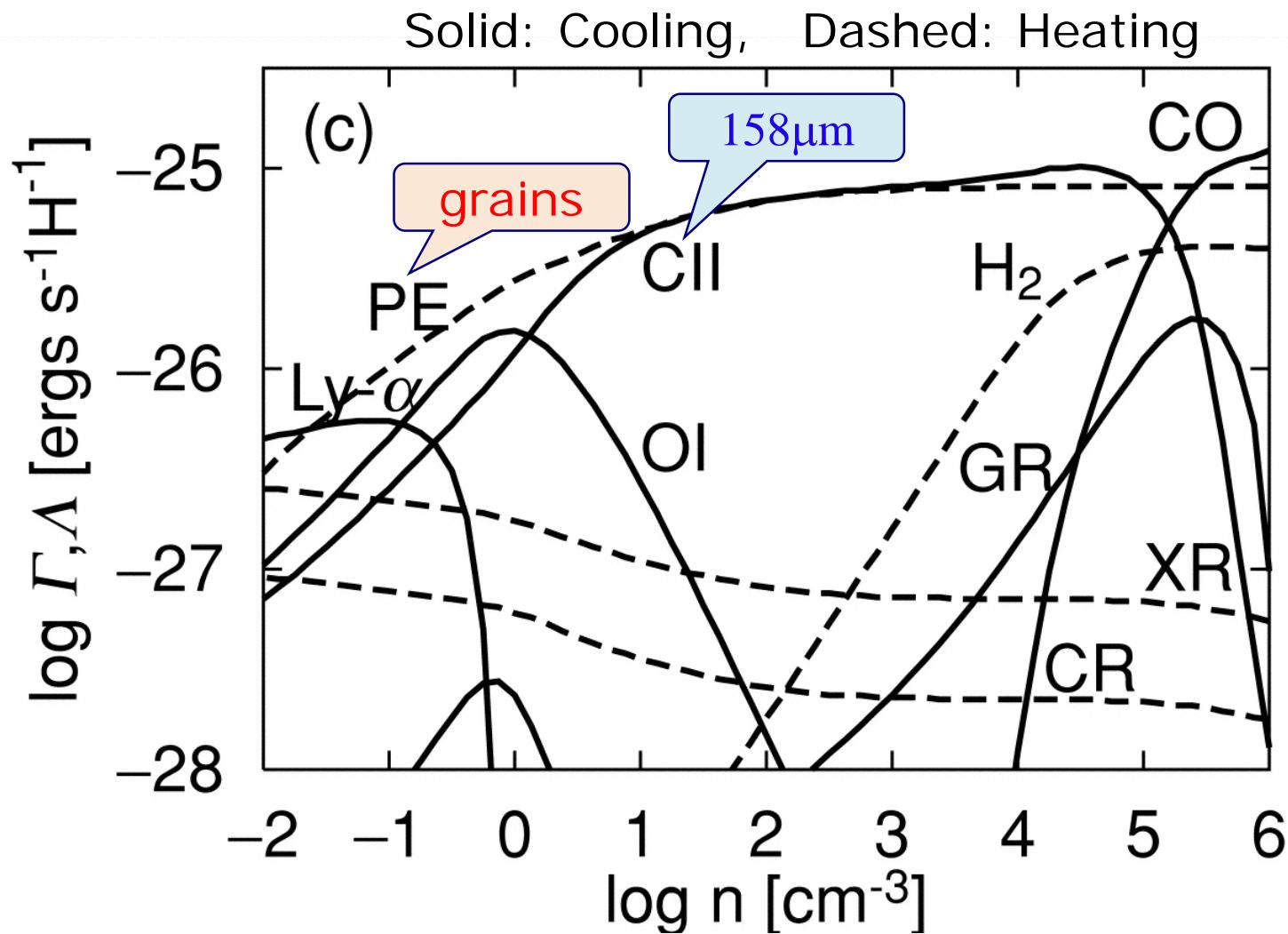
Studies on Origin of Supersonic Motions

- Koyama & Inutsuka, ApJL **564**, L97 , 2002
- Krtsuk & Norman 2002a, ApJ **569**, L127; 2002b ApJ **580**, L51
- Audit & Hennebelle 2005, A&A **433**, 1
- Heitsch, et al. 2005, ApJ **633**, L113, Vazquez-Semadeni et al. 2006, etc...

Radiative Equilibrium for a given density

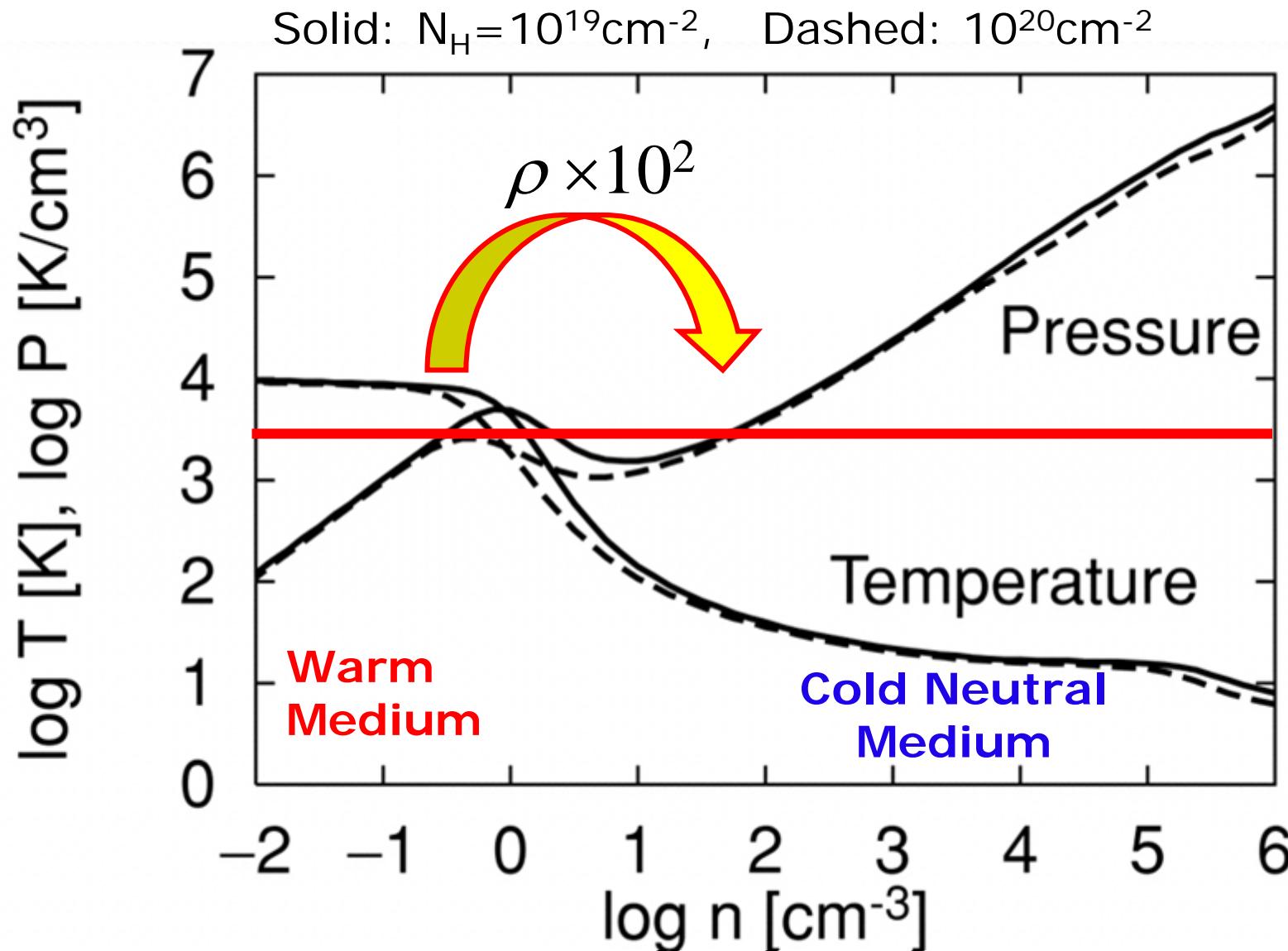


Radiative Cooling & Heating



Koyama & Si (2000) ApJ 532, 980, (adding CO to Wolfire et al. 1995)

Radiative Equilibrium for a given density



e.g., Wolfire et al. 1995, Koyama & SI 2000

Dispersion Relation of Thermal Instability

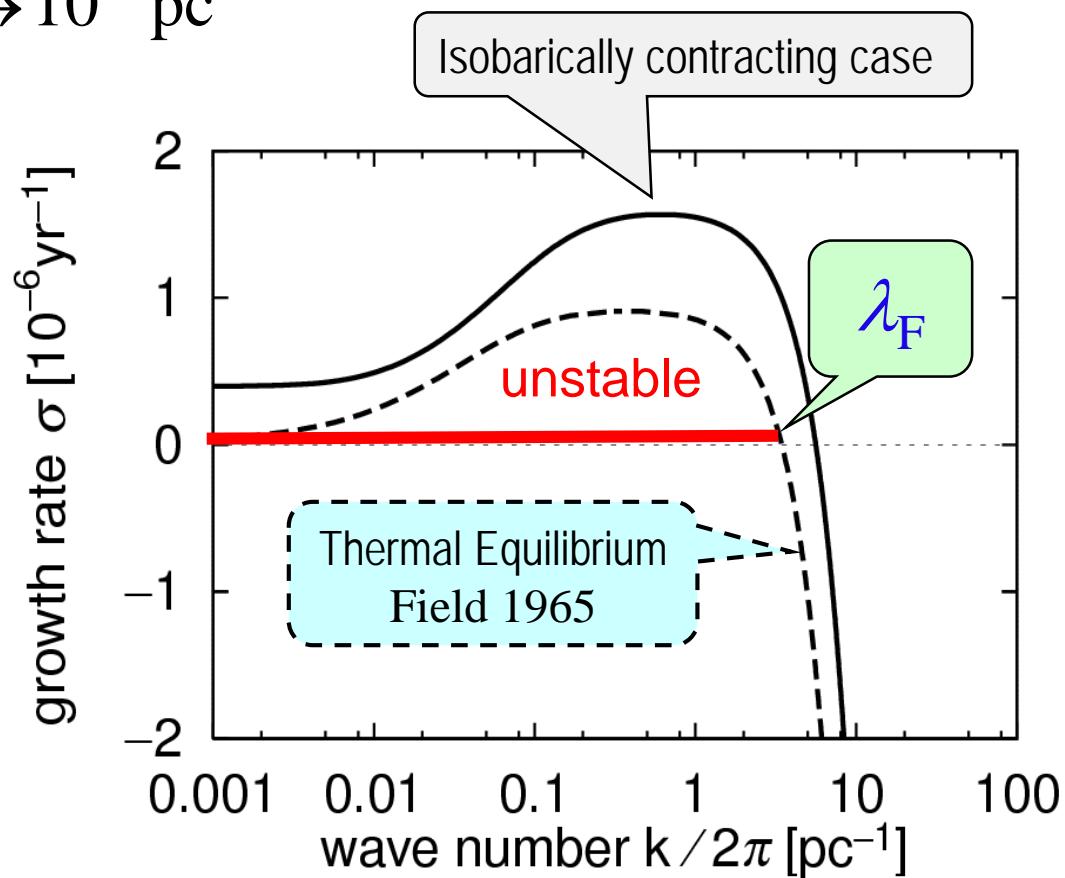
“Field length” : $\lambda_F \equiv \sqrt{\frac{\kappa T}{\rho^2 \Lambda}} \rightarrow 10^{-2} \text{ pc}$

Thermal Instability

for $\lambda > \lambda_F$

If $\kappa = 0$, then $\lambda_{\text{crit}} = 0$

In two-phase medium,
the width of transition layer
= λ_F .



Koyama & Inutsuka (2004) ApJ, 602, L25

Warning to Numerical Simulation

THE ASTROPHYSICAL JOURNAL, 602:L25–L28, 2004 February 10
© 2004. The American Astronomical Society. All rights reserved. Printed in U.S.A.

THE FIELD CONDITION: A NEW CONSTRAINT ON SPATIAL RESOLUTION IN SIMULATIONS OF THE NONLINEAR DEVELOPMENT OF THERMAL INSTABILITY

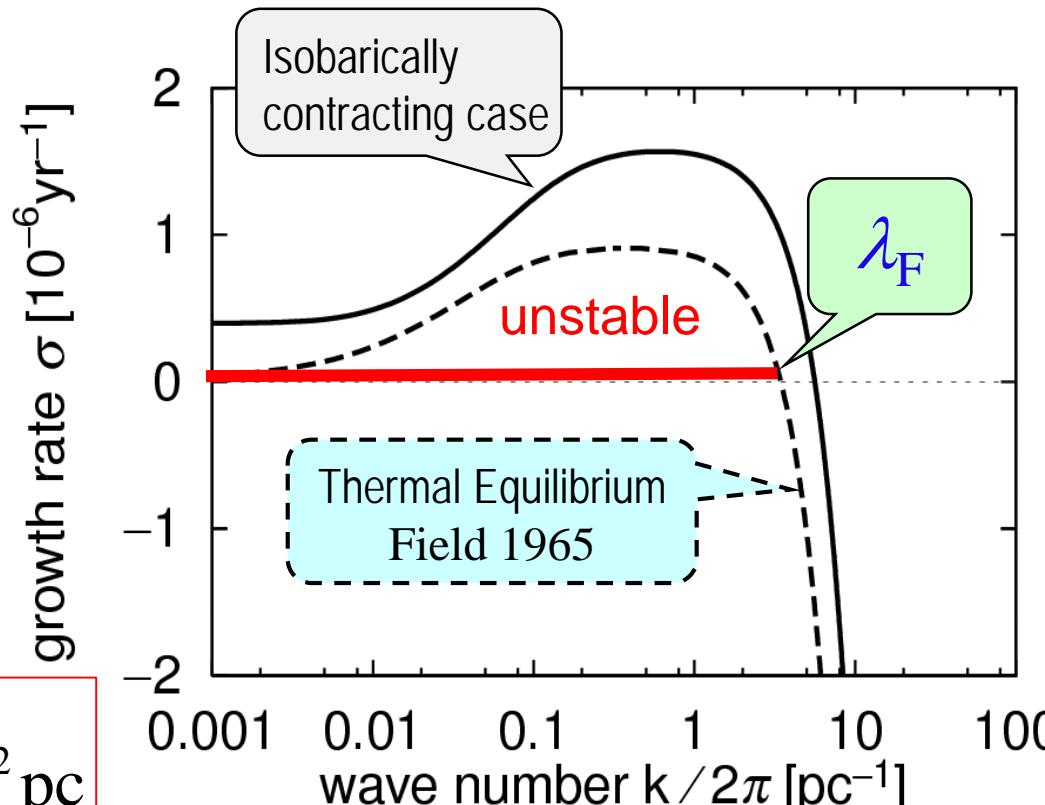
HIROSHI KOYAMA^{1,2} AND SHU-ICHIRO INUTSUKA³

Received 2003 February 6; accepted 2004 January 2; published 2004 January 30

Requirement for
Spatial Resolution
“Field Condition”

We should resolve the
structure of
transition layer: λ_F

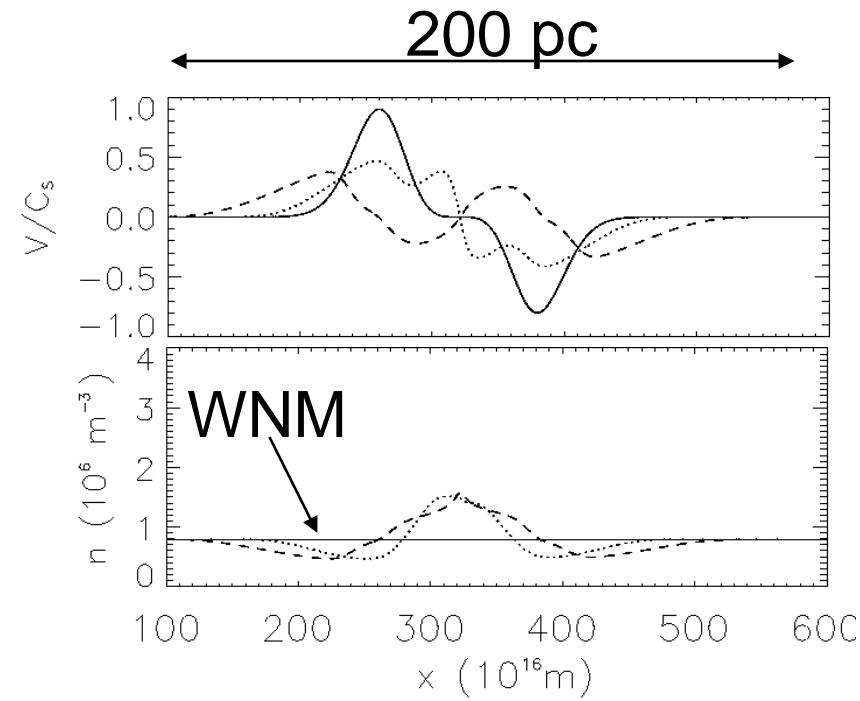
$$\text{Field length: } \lambda_F \equiv \sqrt{\frac{KT}{\rho^2 \Lambda}} \approx 10^{-2} \text{ pc}$$



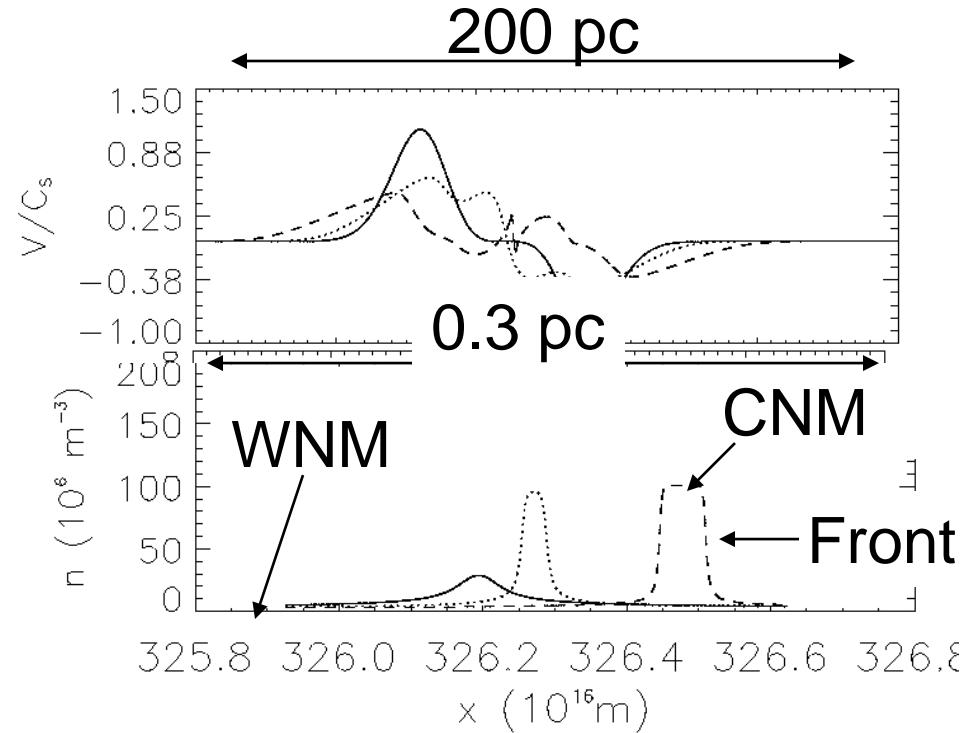
Dynamical Triggering of Thermal Instability

Hennebelle & Pérault 1999; Koyama & Inutsuka 2000

A converging flow which does not trigger thermal transition:



A **slightly** stronger converging flow does trigger thermal transition:



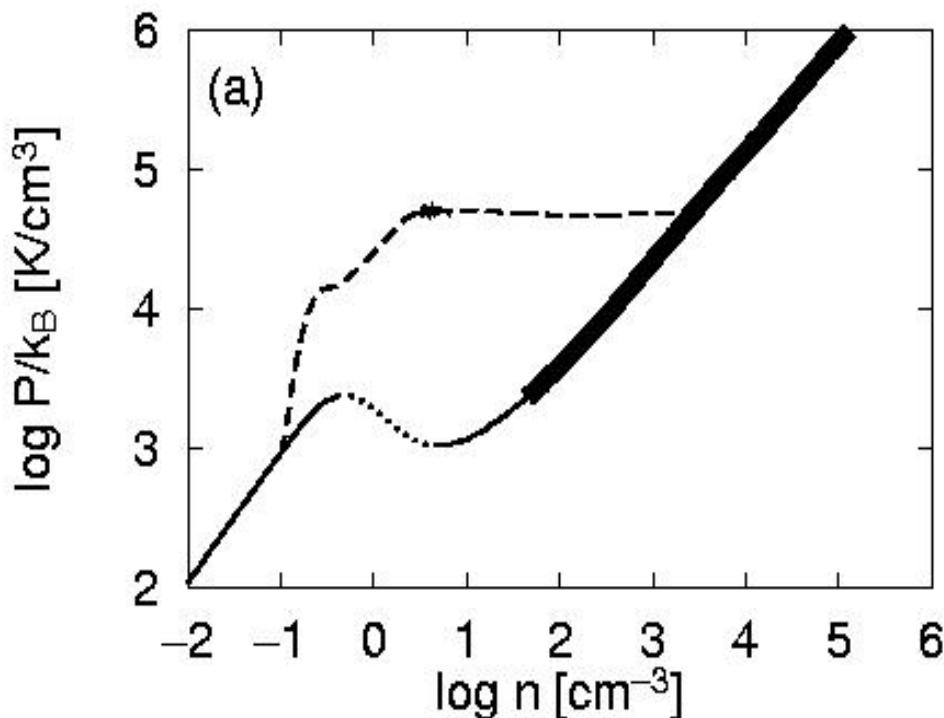
Hennebelle & Pérault 1999

→ WNM is linearly stable but non-linearly unstable.

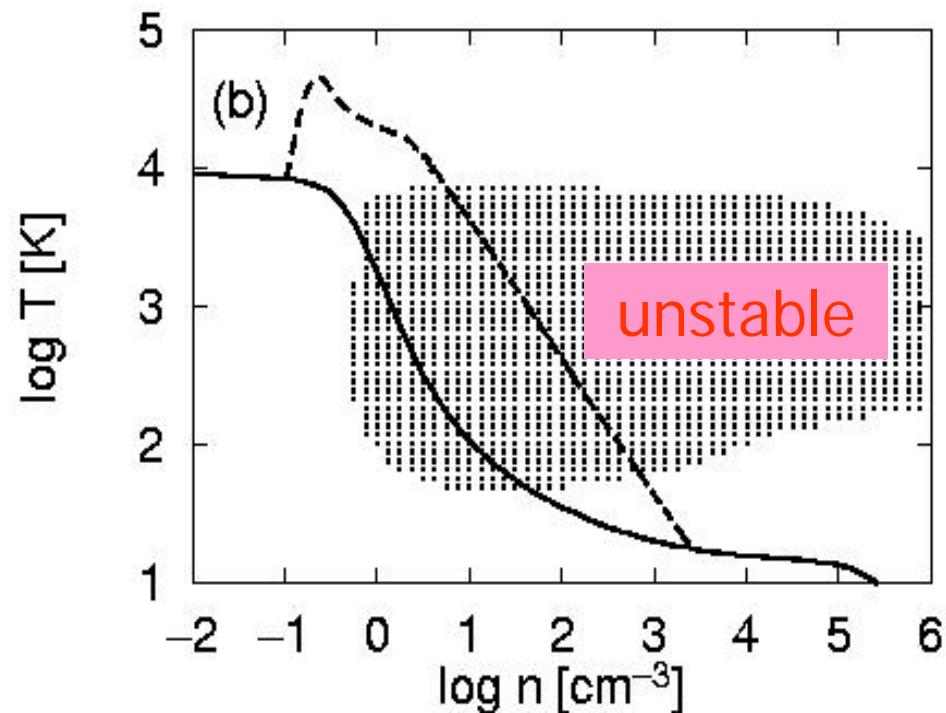
1D Shock Propagation into WNM

Realistic Cooling/Heating + Chemistry (H_2 , CO)

Density-Pressure Diagram



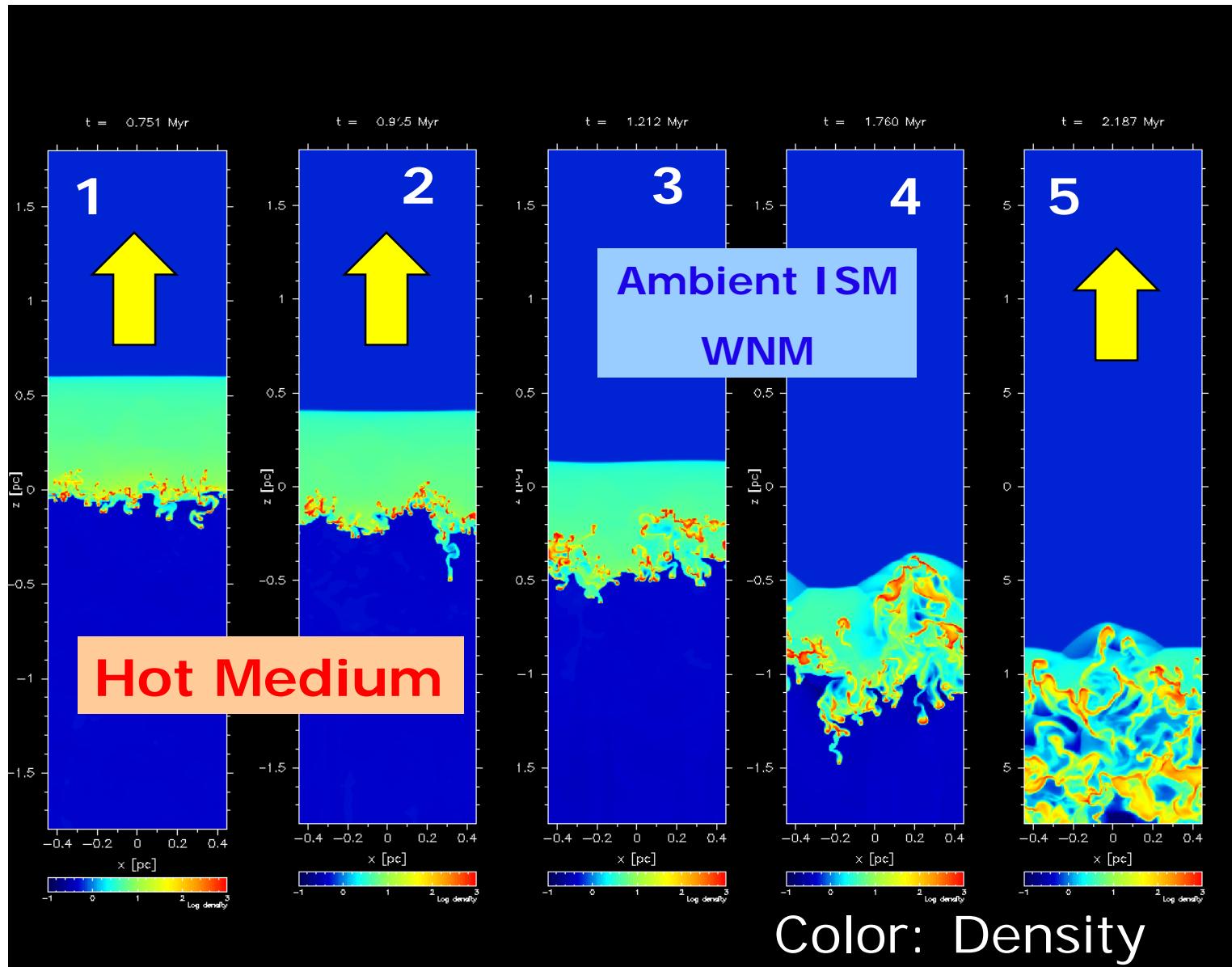
Density-Temperature Diagram



Koyama & Inutsuka 2000, ApJ 532, 980

See also Hennebelle & Pérault 1999

Shock Propagation into WNM



Koyama & Inutsuka (2002) ApJ 564, L97

Summary of TI-Driven Turbulence

- 2D/3D Calculation of Propagation of Shock Wave into WNM via Thermal Instability

→ fragmentation of cold layer into cold clumps with long-sustained supersonic velocity dispersion (\sim km/s)

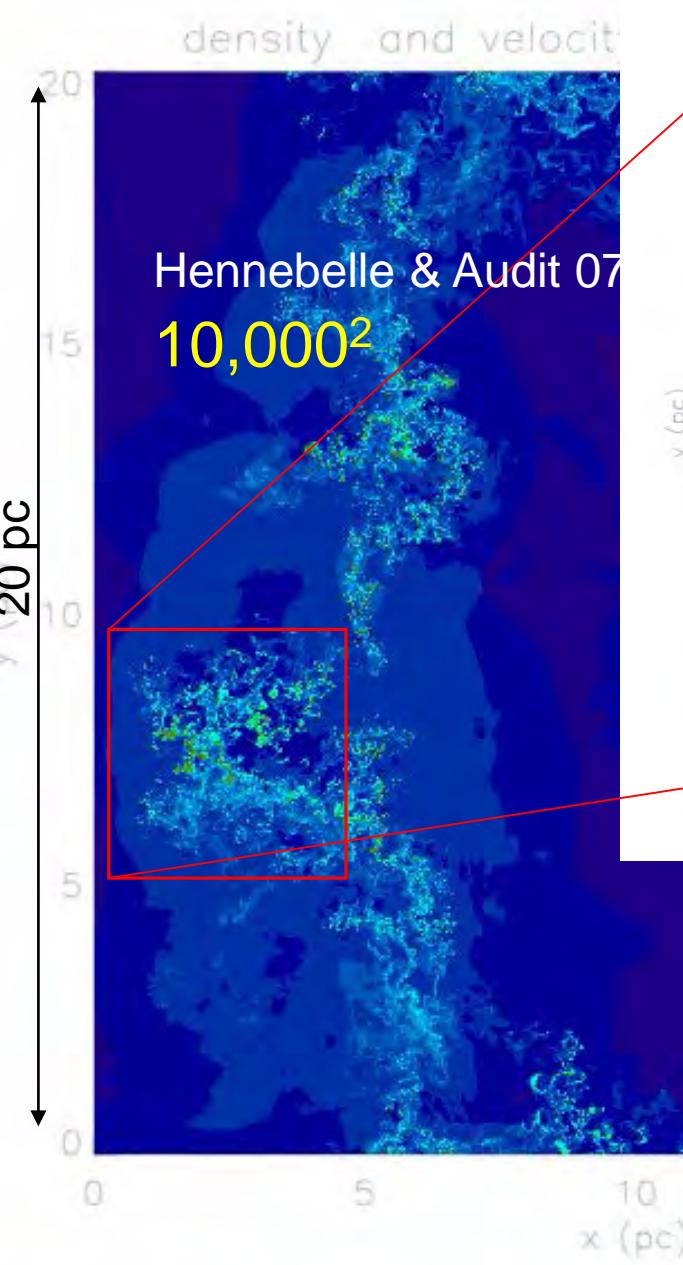
1D: Shock $\Rightarrow E_{\text{th}} \Rightarrow E_{\text{rad}}$

2D&3D: Shock $\Rightarrow E_{\text{th}} \Rightarrow E_{\text{rad}} + E_{\text{kin}}$

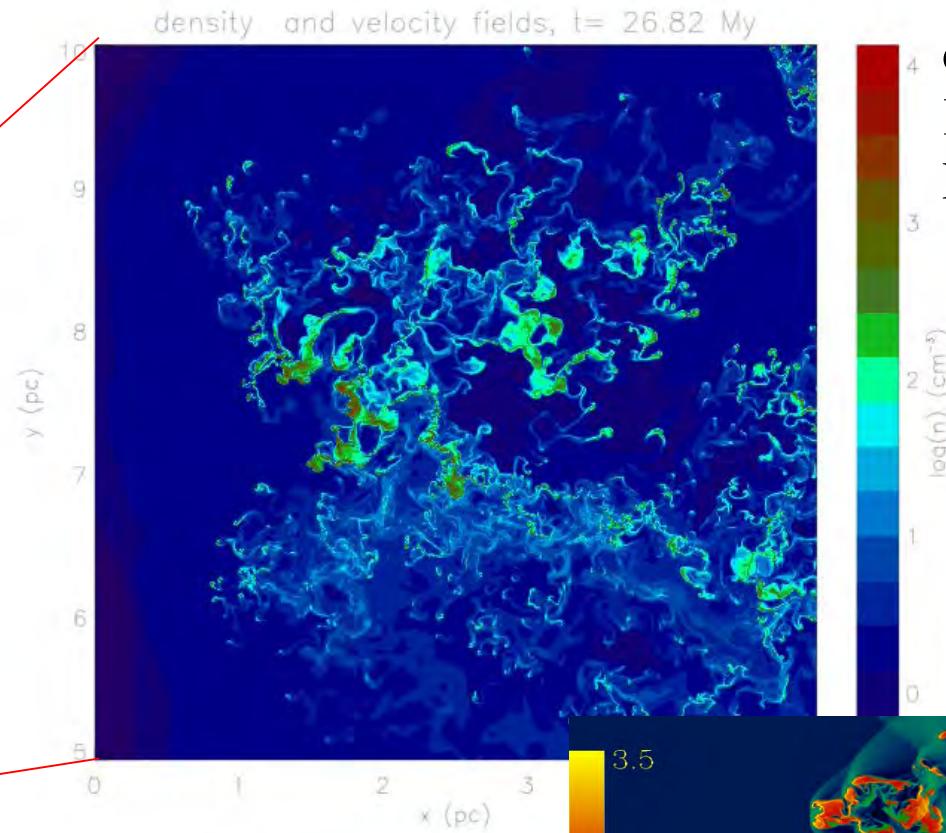
$$\delta v \sim \text{a few km/s} < C_{S,\text{WNM}} = 10 \text{ km/s}$$

← 10^4 K due to Ly α line: Universality!

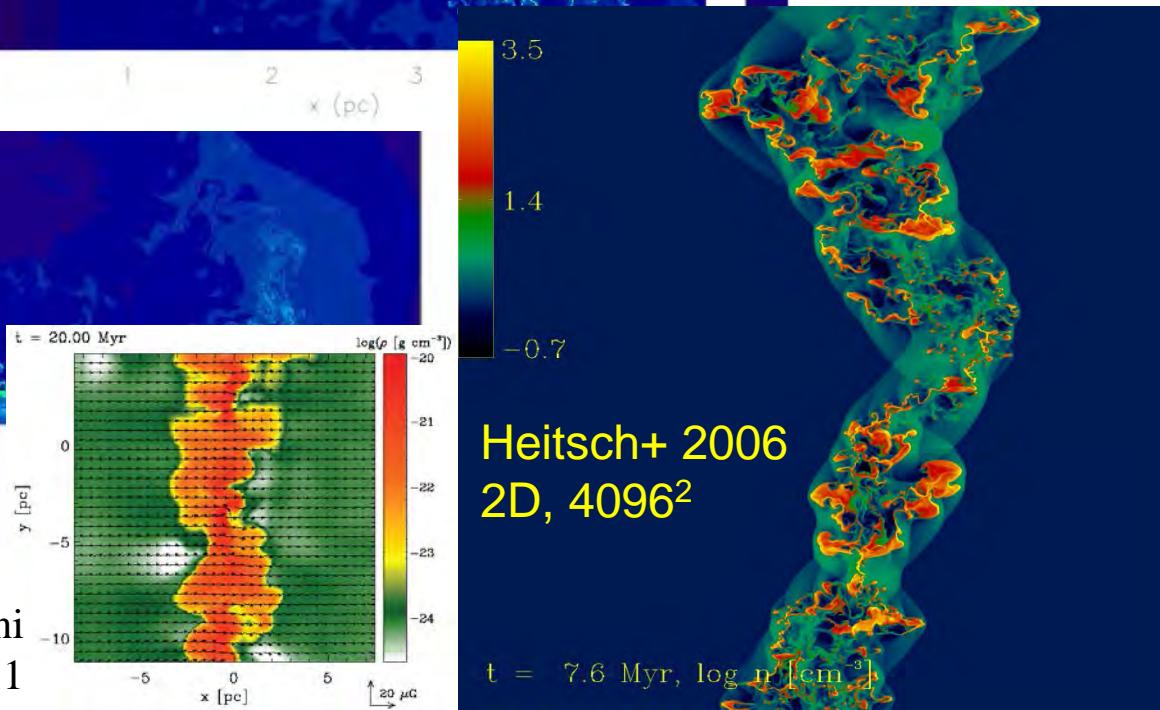
$$T_{\text{CNM}} \sim 10^2 \text{ K} \leftarrow \text{C}^+ 158 \mu\text{m} (\sim 10^2 \text{ K})$$



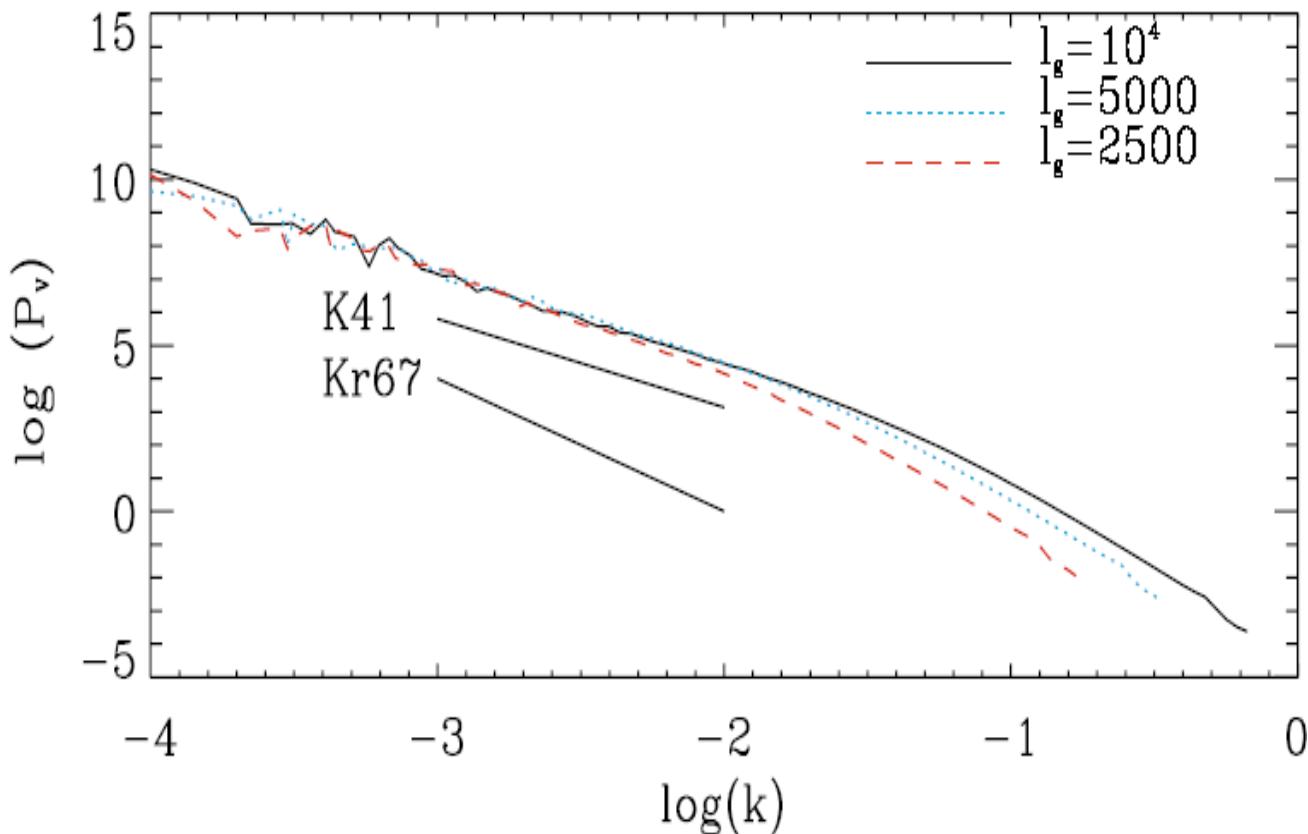
Vazquez-Semadeni
et al. 2011



Heitsch+ 2006
2D, 4096²



Property of “Turbulence”... Subsonic

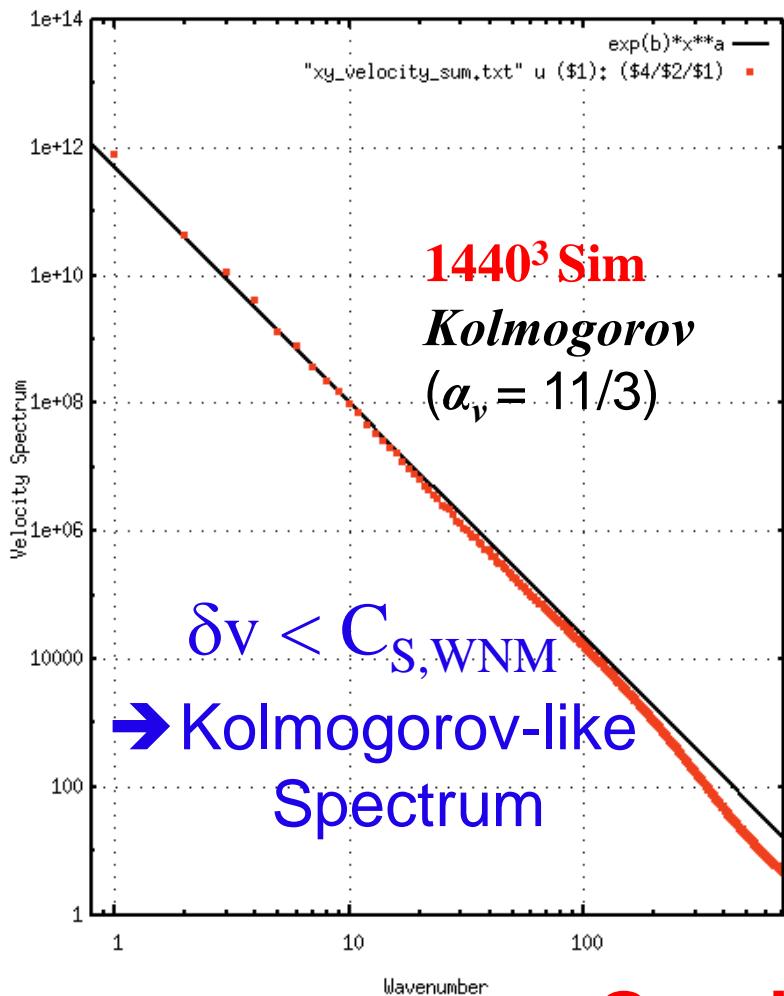


$\delta v < C_{S,WNM} \rightarrow$ Kolmogorov Spectrum

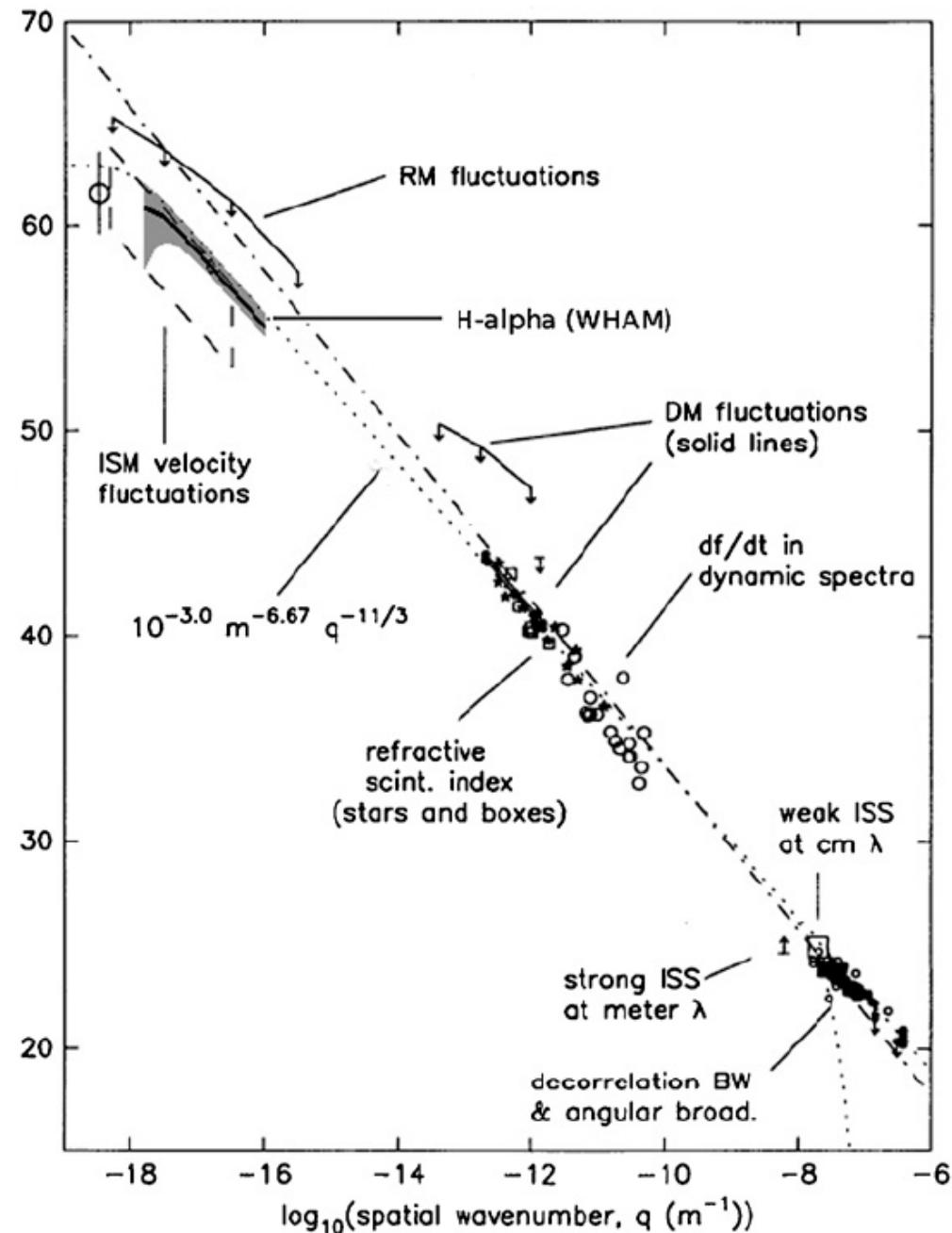
2D: Hennebelle & Audit 2007; see also Gazol & Kim 2010

Property of 3D "Turbulence"

Muranushi, Inoue & SI (unpublished)



Good Agreement!



Chepurnov & Lazarian 2010
Armstrong et al. 1995

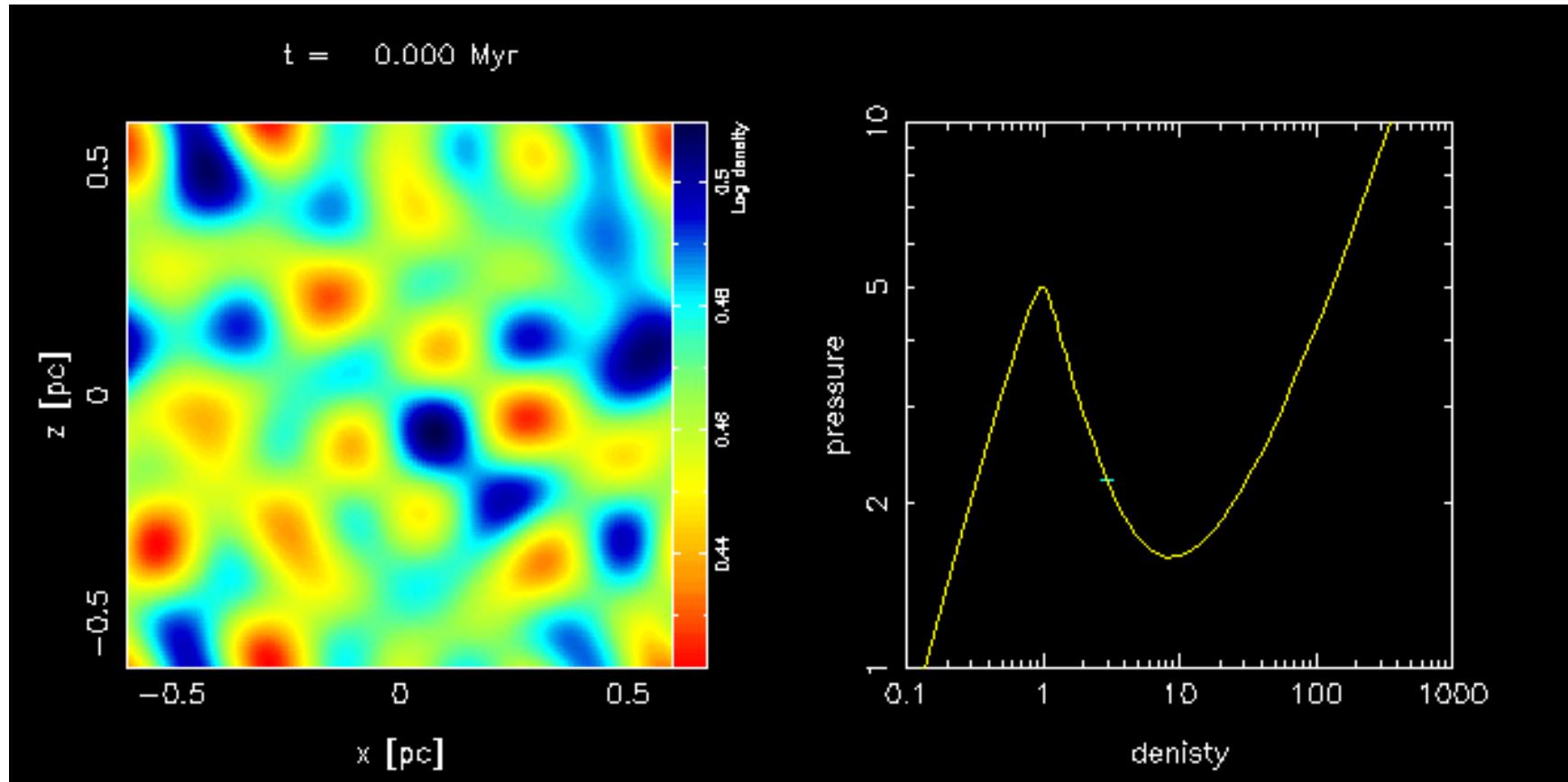
Two Aspects in Multi-Phase Dynamics

2: Phase Transition Dynamics without Shock Waves

Does turbulence decay without external mechanical driving such as due to shock waves?

The Answer is NO!

Sustained “Turbulence” in Periodic Box

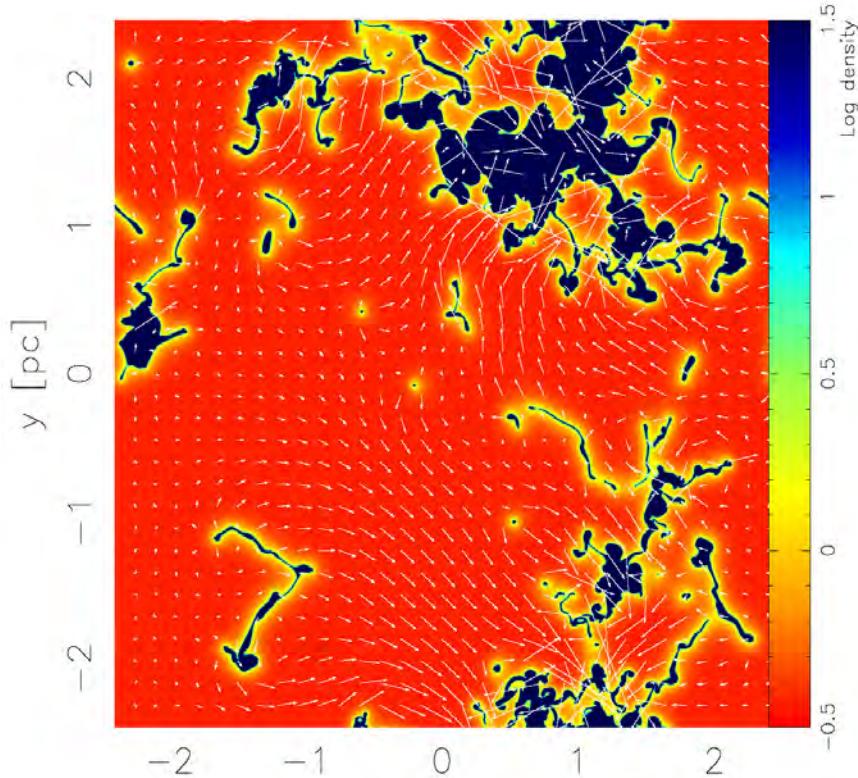


Periodic Box Evolution without Shock Driving

With Cooling/Heating and Thermal Conduction
Without Physical Viscosity ($Prandtl \# = 0$)

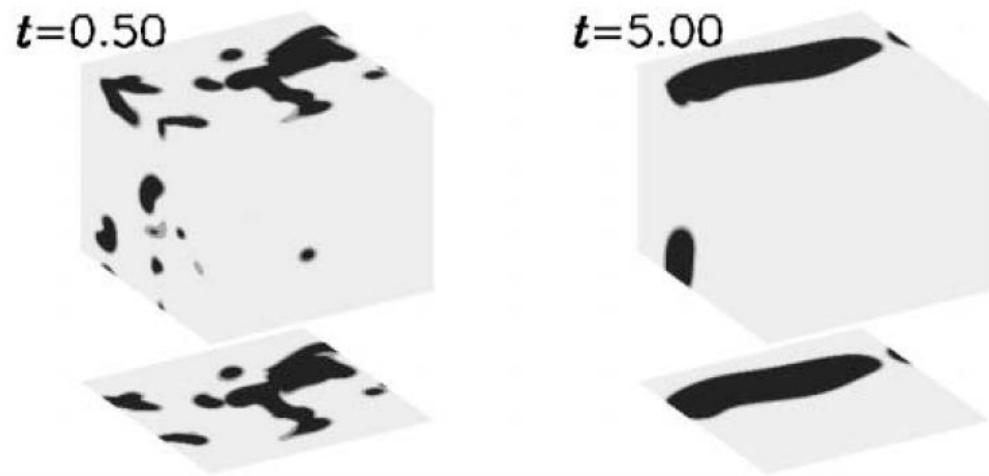
Non-Linear Development of TI without External Forcing

Sustained Turbulence for realistic conduction κ



Koyama & Inutsuka 2006;
Iwasaki & Inutsuka 2014 ApJ 784,115

Decaying Turbulence for $\kappa \propto n$



Brandenburg et al. 2007

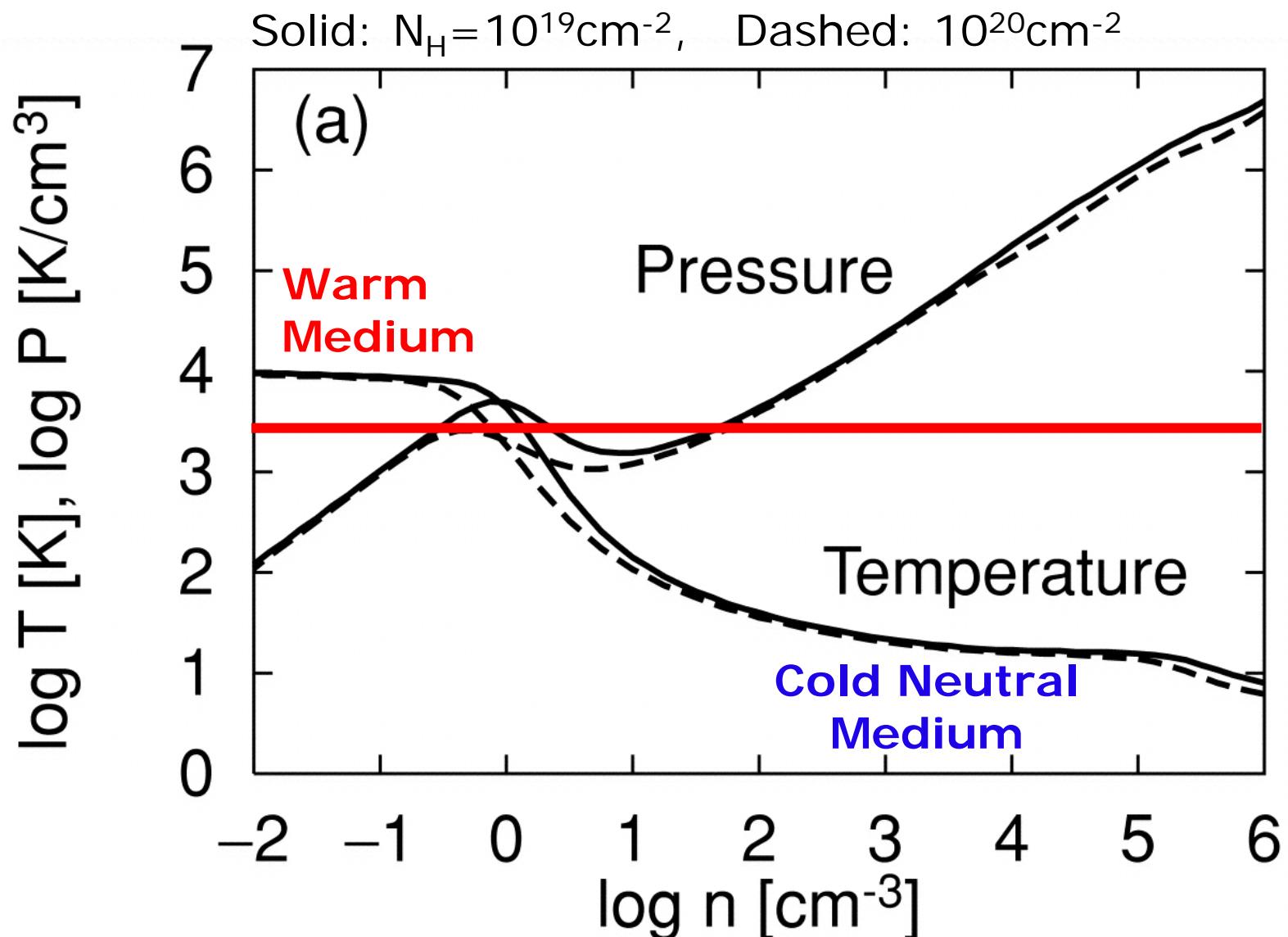
In reality, $\kappa = \text{const.}$

$$\kappa \propto n v l \propto \underline{n} v / (\underline{n} \sigma)$$

Further Analysis on Phase Transition Dynamics

1. Evaporation & Condensation
2. New Instability of Transition Layer
3. Effect of Magnetic Field

Radiative Equilibrium for a given density



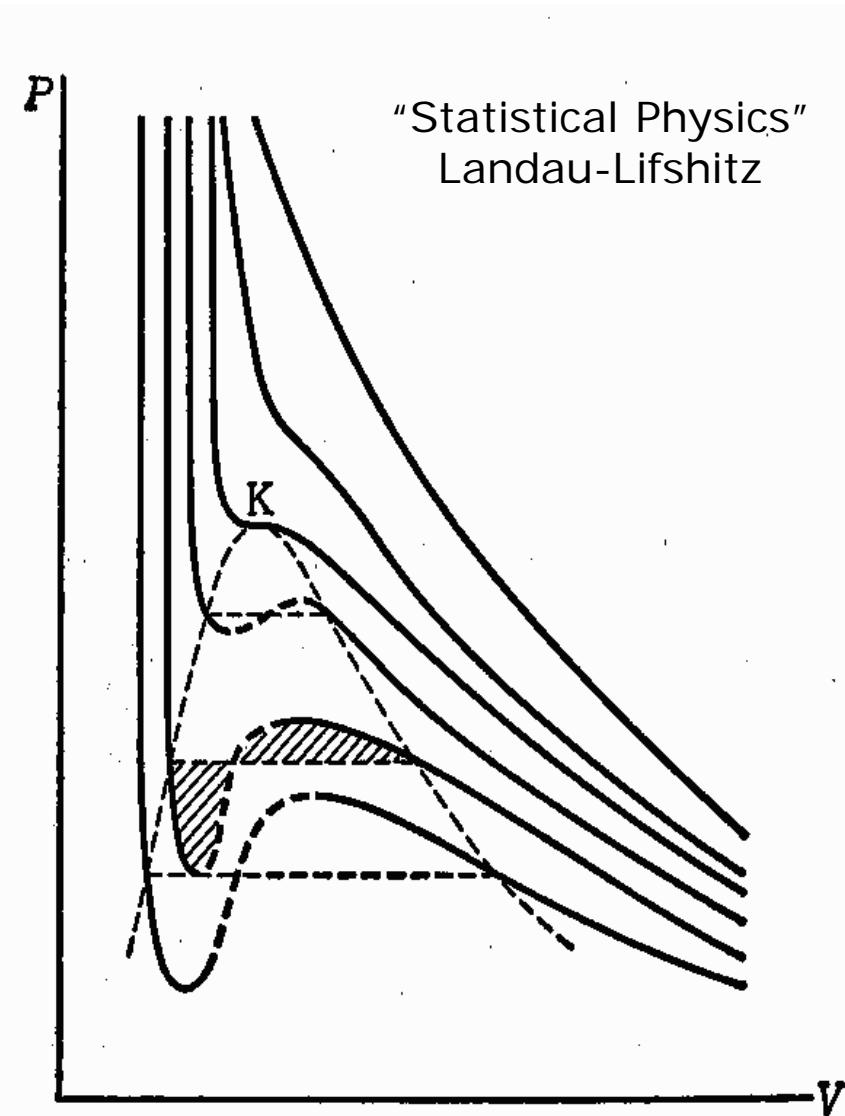
Textbook Example of Phase Equilibrium

EoS of van der Waals Gas

$$P = \frac{NT}{V - nb} - \frac{N^2 a}{V^2}$$

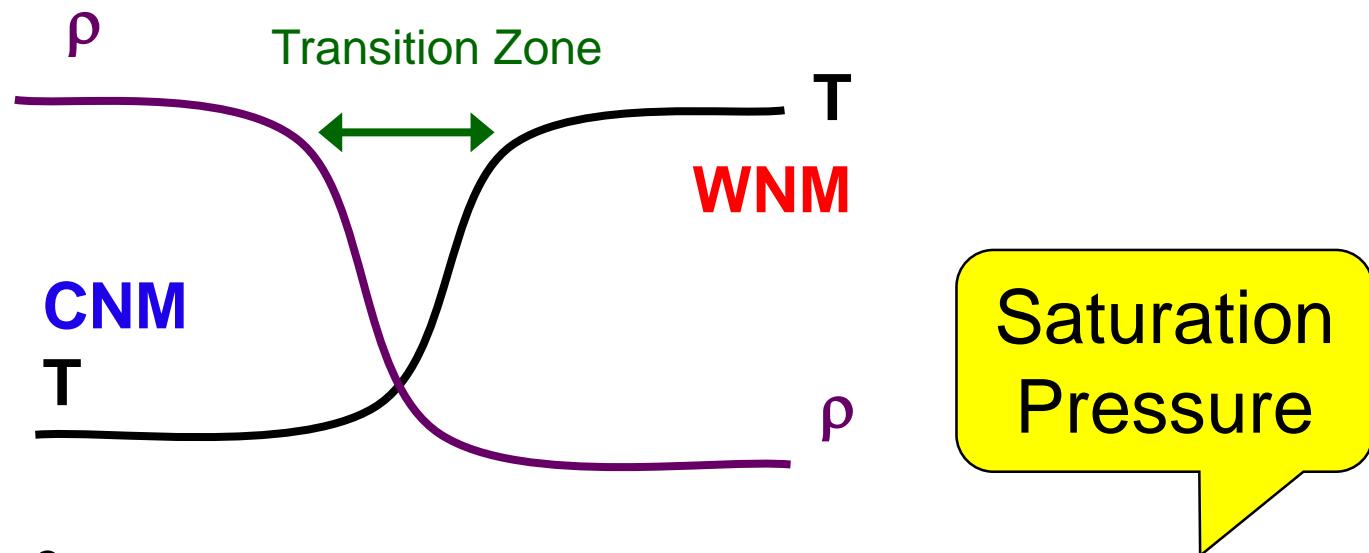
$$\begin{aligned}\mu_1 = \mu_2 &\Leftrightarrow 0 = \int_1^2 d\mu \\ &= \int_1^2 V(P, T = \text{const}) dP\end{aligned}$$

Equal Areas of shaded regions
(Maxwell's rule)



Exact Equilibrium of 2-Phases

1D Case

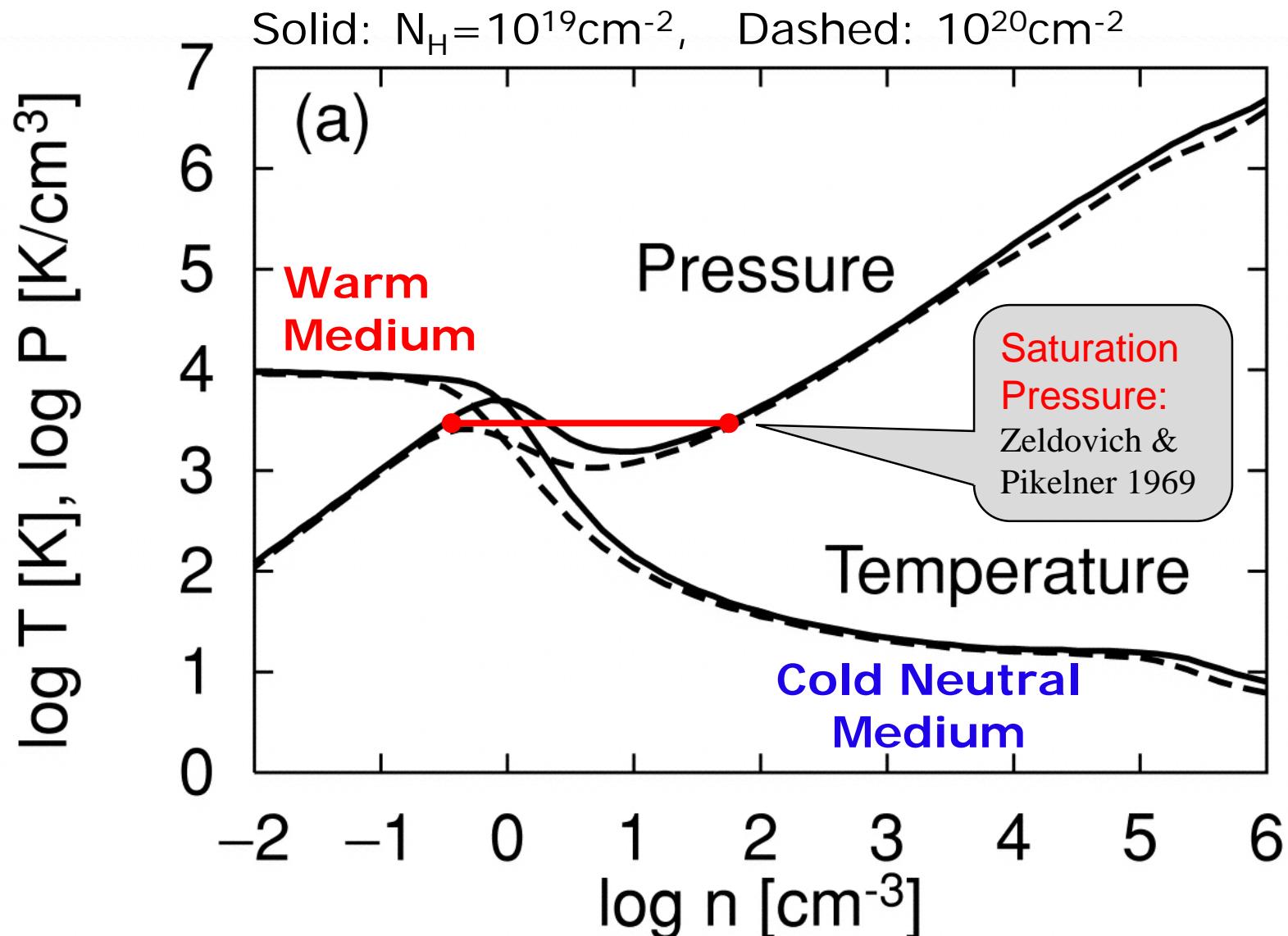


$$\int (\rho \Gamma - \rho^2 \Lambda) dV = 0 \Rightarrow \text{only at } P = P_{\text{sat}}$$

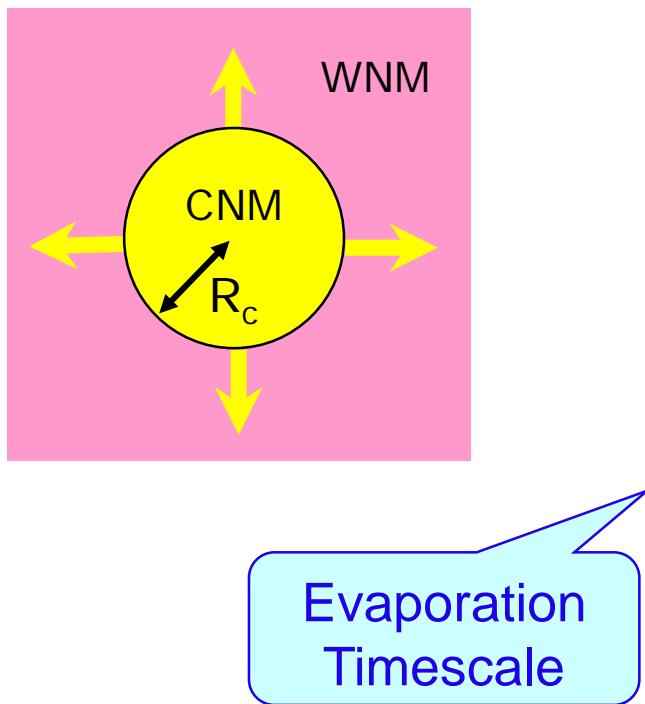
- 1D Plane-Parallel Case: Zeldovich & Pikelner 1969
- 2D Cylindrical Symmetry: Graham & Langer 1973
- 3D Spherical Symmetry: Nagashima, SI, Koyama 2005

No Unique $P_{\text{sat}} \rightarrow$ 2-Phase with various P

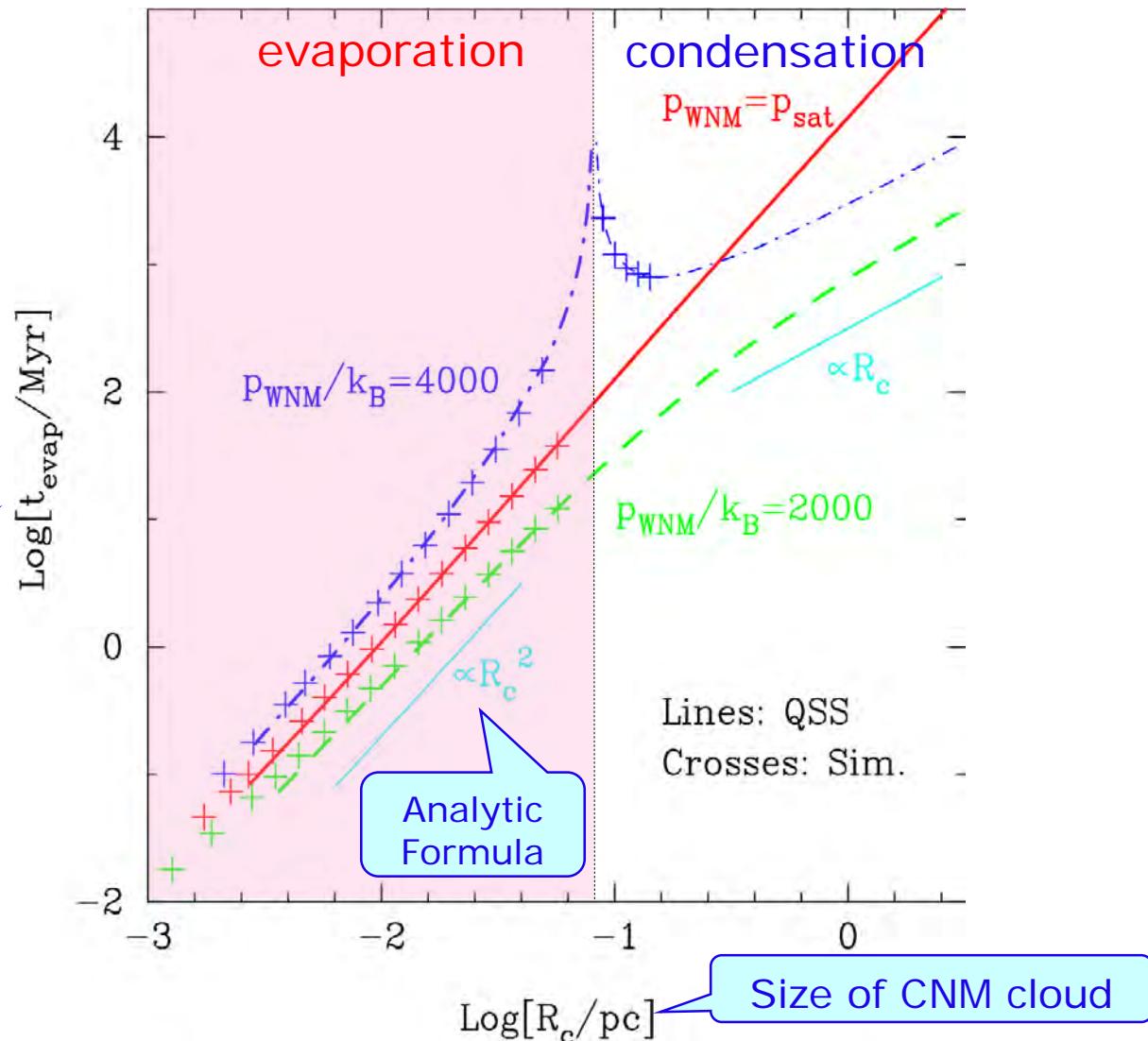
Saturation Pressure in 1D Geometry



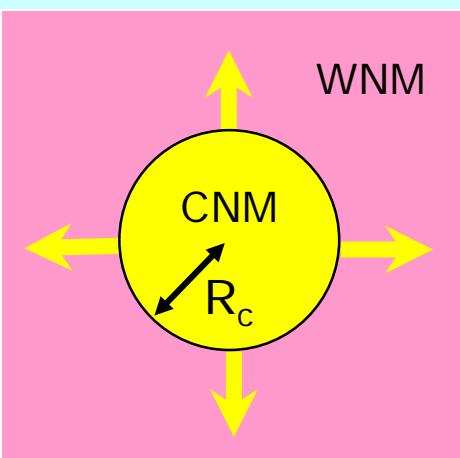
Evaporation of Spherical CNM in WNM



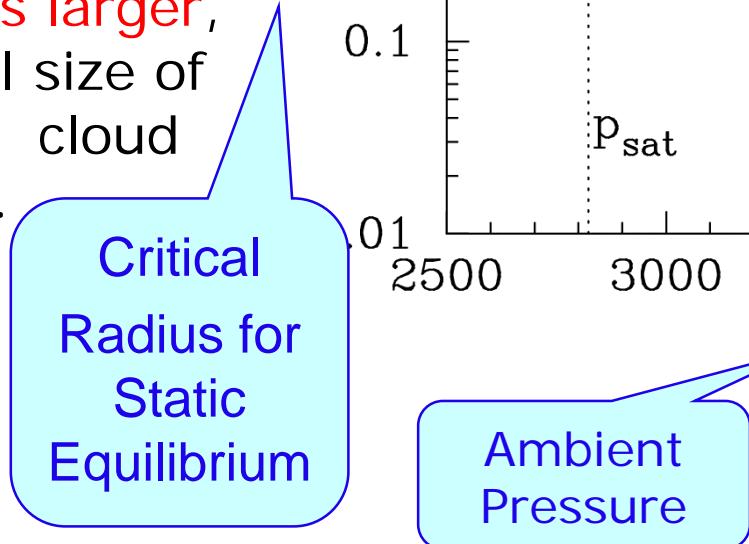
Smaller CNM
cloud evaporates:
 $R \sim 0.01\text{pc}$ clouds
evaporate in $\sim\text{Myr}$



Evaporation of Spherical CNM in WNM



If the ambient pressure is larger, the critical size of the stable cloud is smaller.

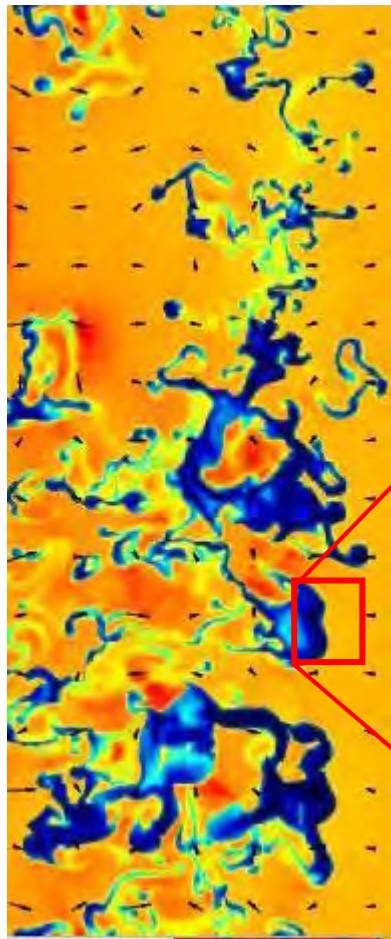


Nagashima, SI, & Koyama 2006,
ApJL 652, L41

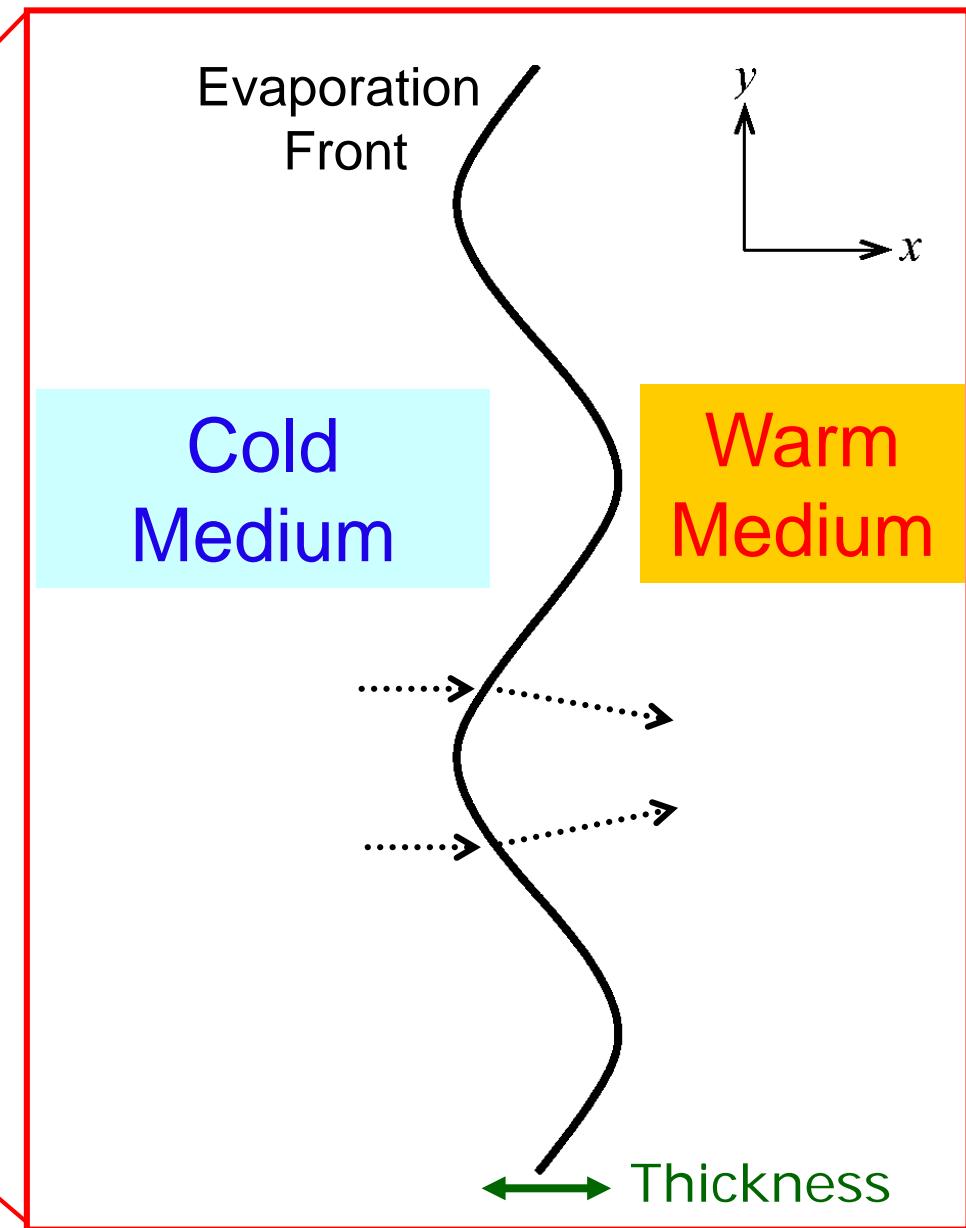
Further Analysis on Phase Transition Dynamics

1. Evaporation & Condensation
2. New Instability of Transition Layer
3. Effect of Magnetic Field

2) Instability of Phase Transition Layer



important in maintaining
the “turbulence”



Instability of Phase Transition Layer

Similar Mechanisms...

1) Darrieus-Landau (DL) Instability

Flame-Front Instability

Important in SNe Ia

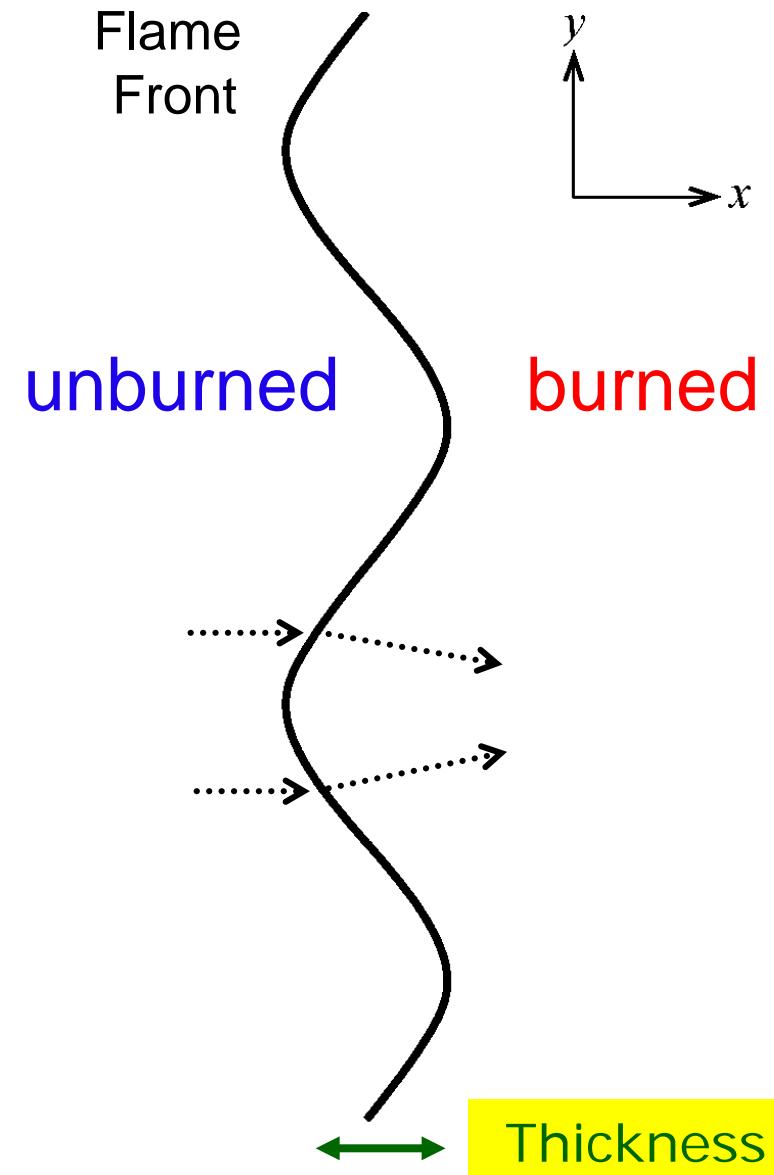
Effect of Magnetic Field

See Dursi (2004)

2) Corrugation Instability in MHD Slow Shock

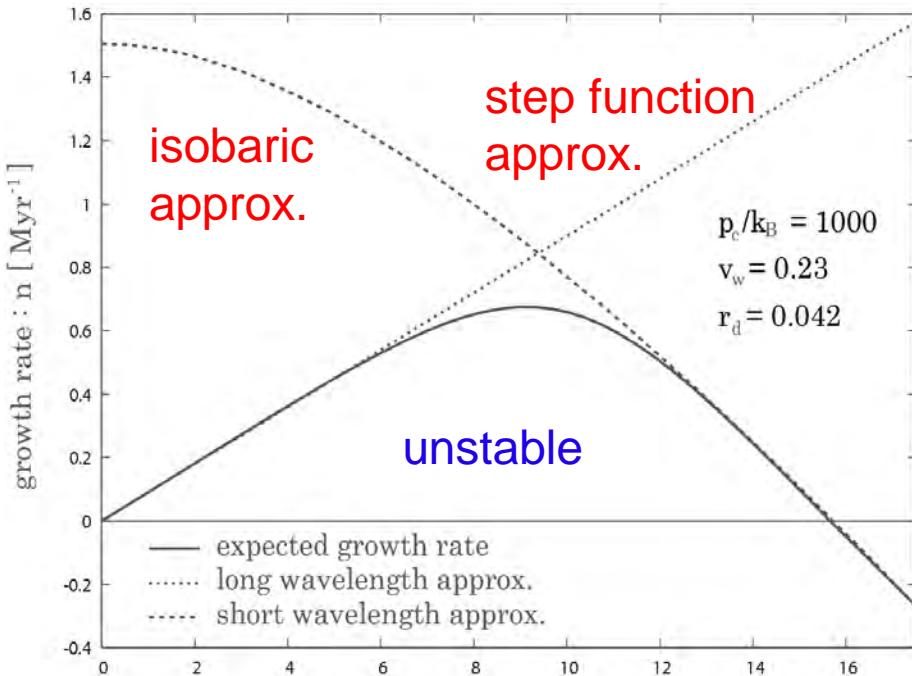
– Edelman 1990

– Stone & Edelman 1995



Linear Analysis of New Instability

Growth Rate (Myr^{-1})

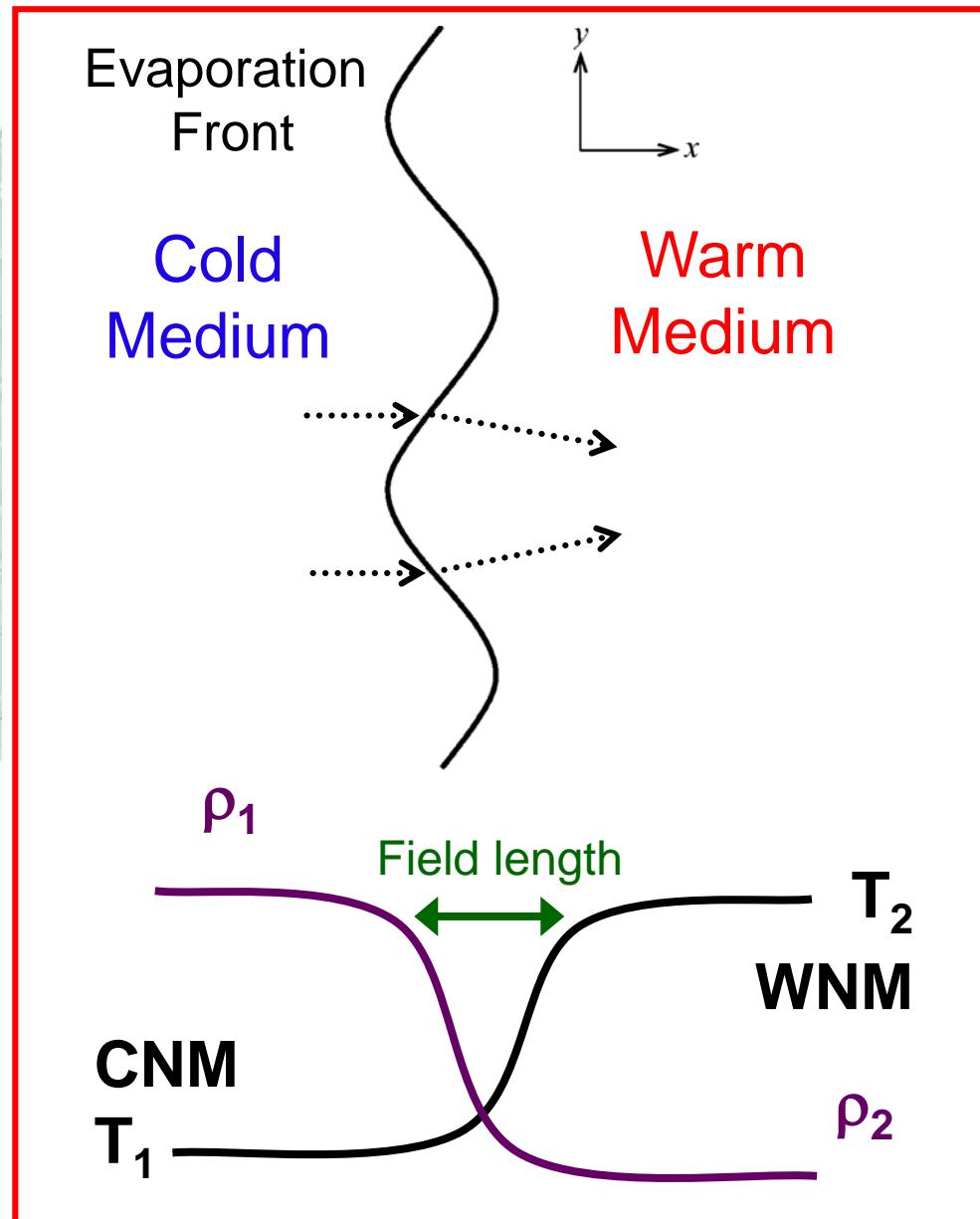


wavenumber $k_y/2\pi$ [pc⁻¹]

Inoue, SI, & Koyama 2006, ApJ **652**, 1131

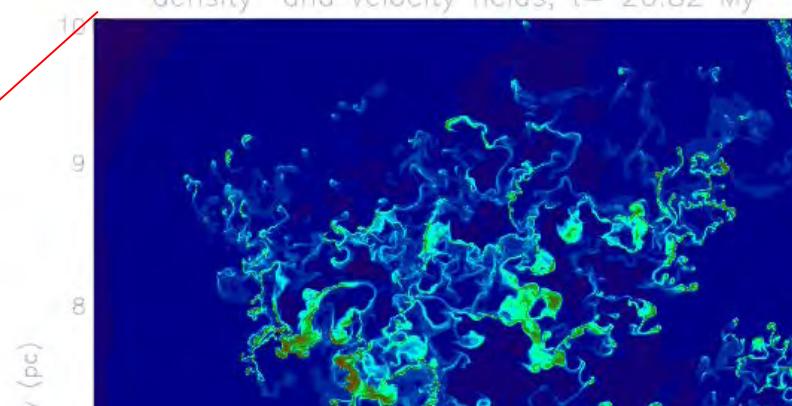
Effect of B :

Stone & Zweibel 2009, ApJ 696, 233



density and velocity

density and velocity fields, $t = 26.82$ My

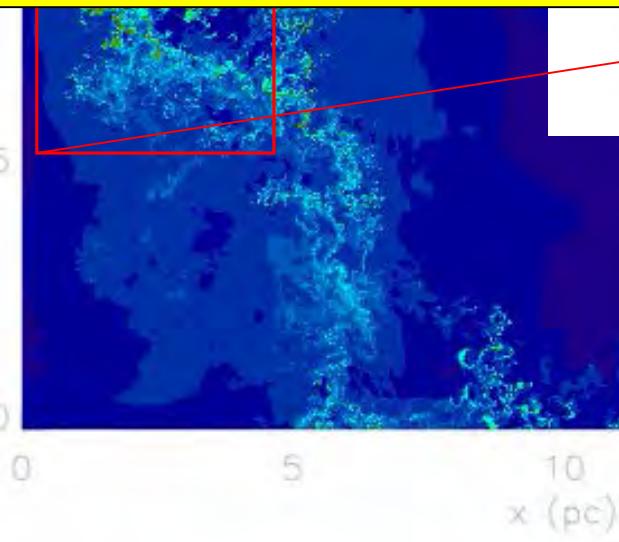


Magnetic Field?

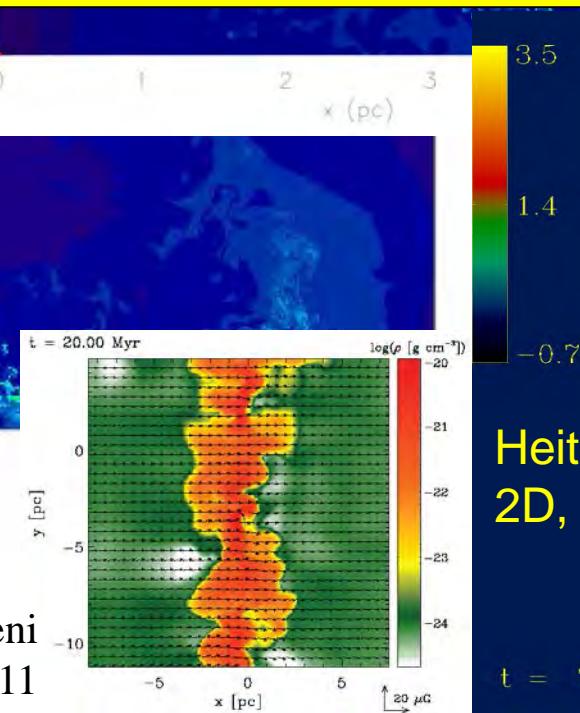
20 pc

y

x

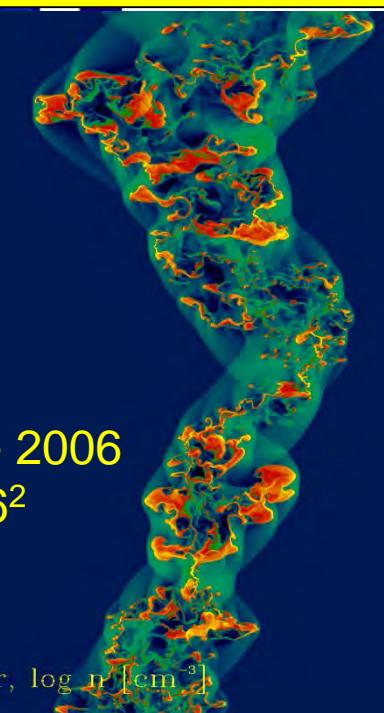


Vazquez-Semadeni
et al. 2011



Heitsch+ 2006
2D, 4096 2

$t = 7.6$ Myr, $\log n$ [cm^{-3}]



Cloud Formation in Magnetized Medium

Can compression of **magnetized**
WNM create **molecular clouds?**

Ref. Inoue & SI (2008) ApJ **687**, 303

Ambipolar
diffusion included

Inoue & SI (2009) ApJ **704**, 161

Inoue & SI (2012) ApJ **759**, 35

SI, Inoue, Iwasaki, Hosokawa 2015 A&A **580**, A49

Two-Fluid Resistive MHD + Cooling/Heating +
Thermal Conduction + Chemistry (H_2 , CO,...)

Colliding WNM with $B_0 = 3 \mu\text{G}$

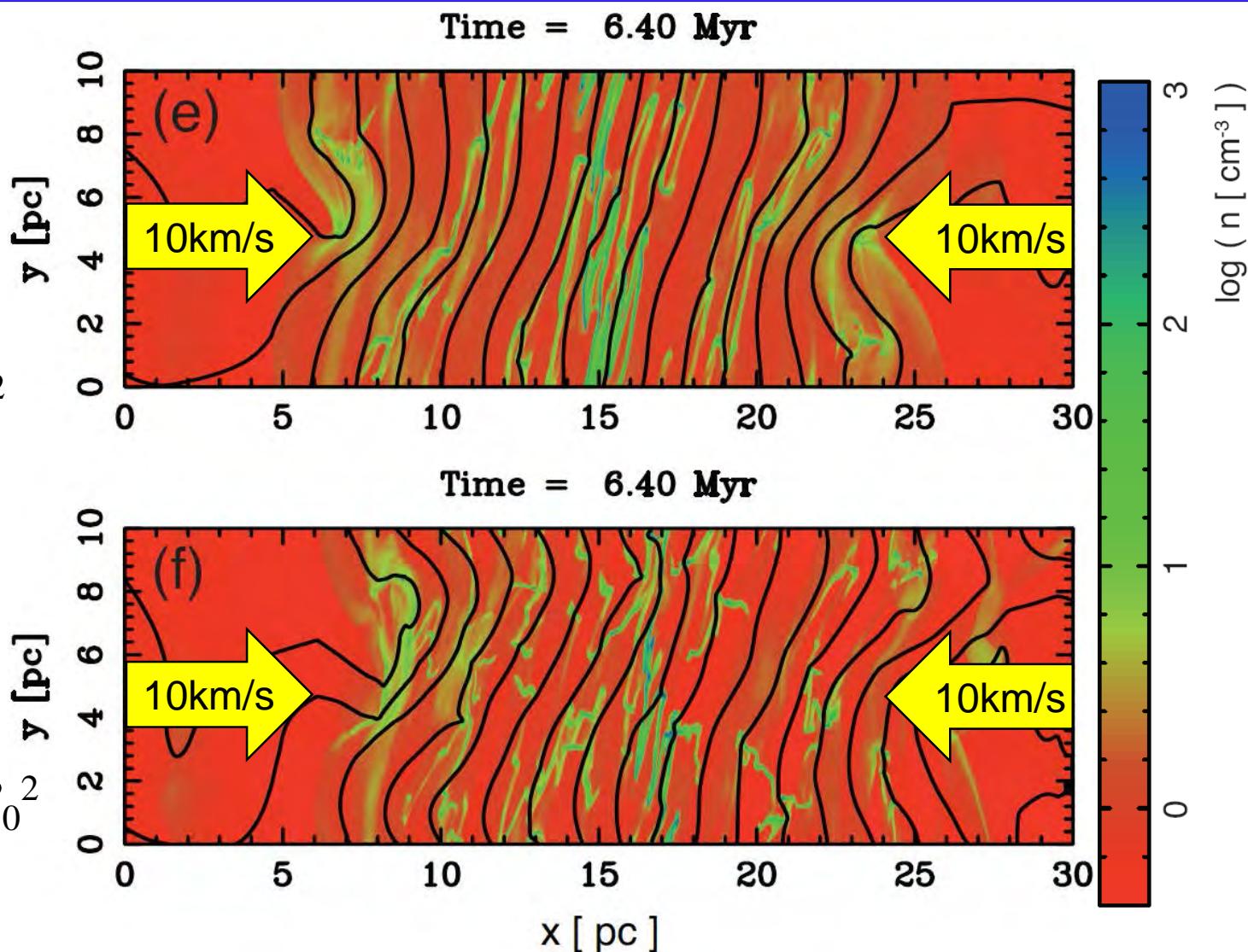
$v = 10 \text{ km/s}$

(a) 15deg

$$\langle \delta B^2 \rangle_{\text{init}} = B_0^2$$

(a) 40 deg

$$\langle \delta B^2 \rangle_{\text{init}} = 4B_0^2$$



2-Fluid MHD Simulation (AD included)

Inoue & Si (2008) ApJ 687, 303

Compression of Magnetized WNM

Can direct compression of magnetized WNM
create molecular clouds? → Not at once!

Inoue & SI (2008) ApJ **687**, 303

Inoue & SI (2009) ApJ **704**, 161

Essentially same result by

Heitsch+2009; Körtgen & Banerjee 2015;
Valdivia+2016

We need multiple episodes of compression.

→ Timescale of Molecular Cloud Formation ~ **a few 10^7 yr**

Next Question: What happens for further compressions?

Compression of CNM (HI) \rightarrow H₂

Compression along

Magnetic Field

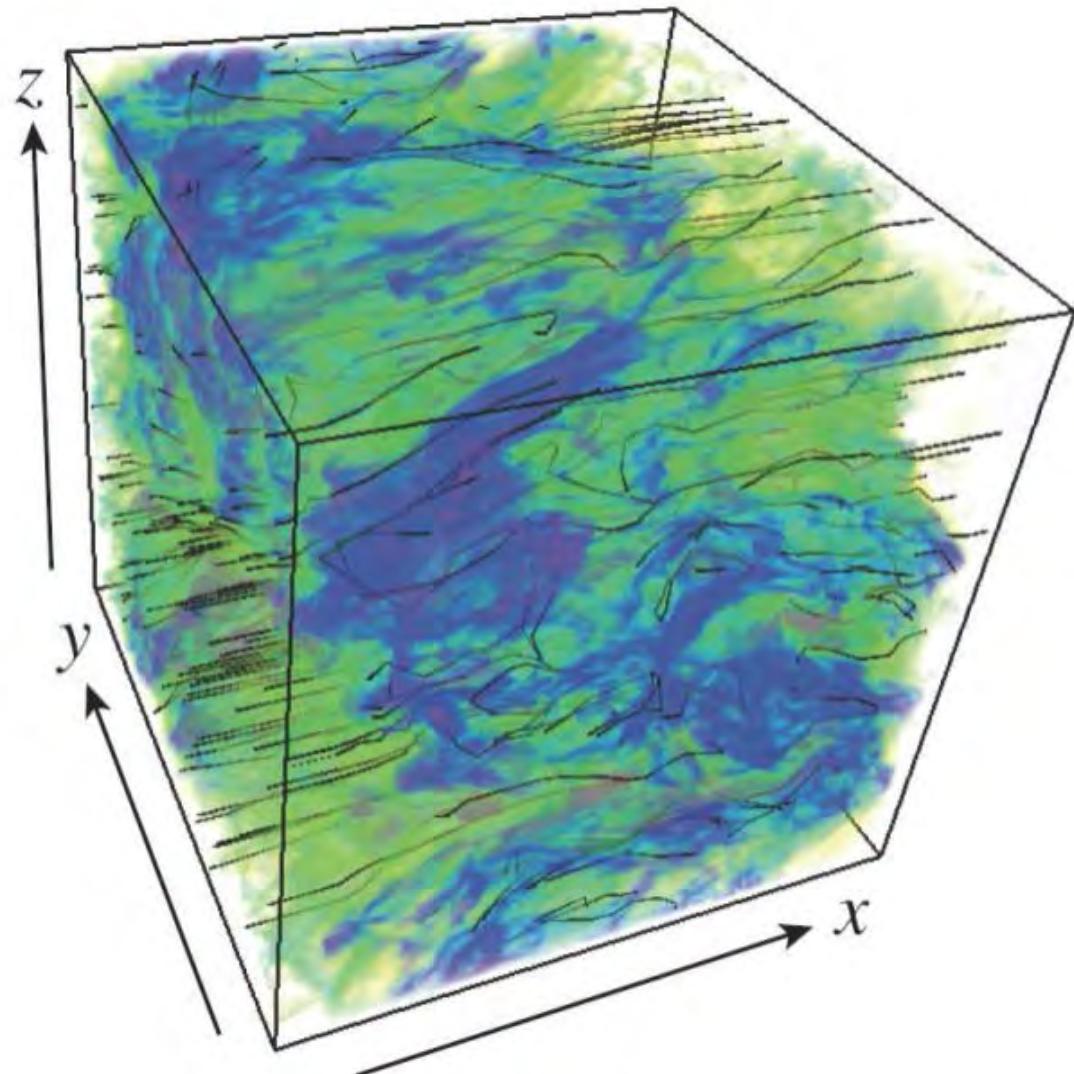
lines, + H₂, CO



Formation of
Magnetized
Molecular Clouds

Transformation of HI to H₂

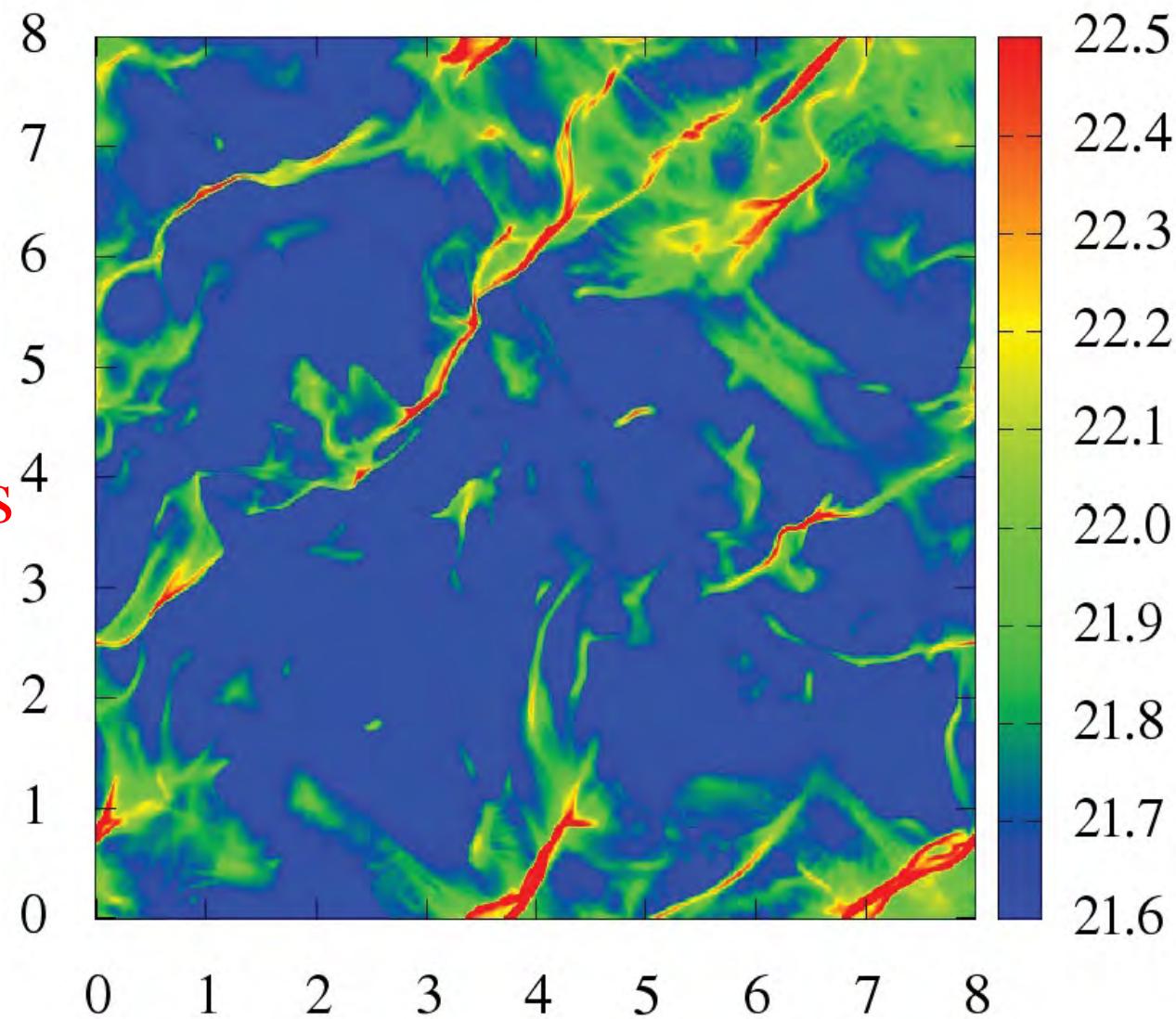
Inoue & SI (2012) 759, 35



Further Compress. of Mole. Clouds

Further
Compression of
Molecular Cloud

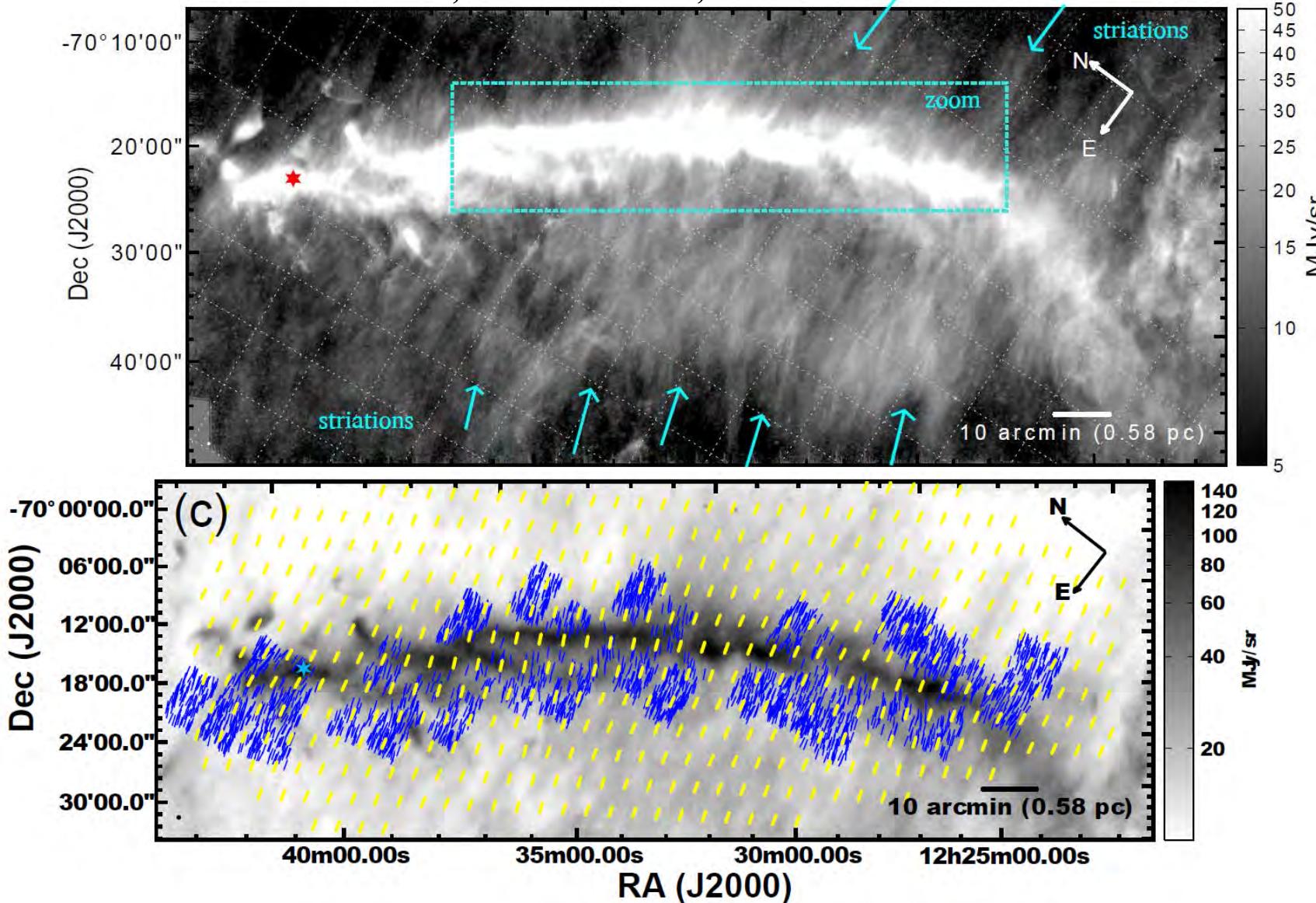
→ Magnetized
Massive Filaments
& Striations



Self-Gravity Included, *SI, Inoue, Iwasaki, & Hosokawa 2015*

Observed Molecular Clouds

Cox, Arzoumanian, André+ 2016



See also Soler+, Fissel+

Yellow and Blue Lines: Magnetic Field Lines

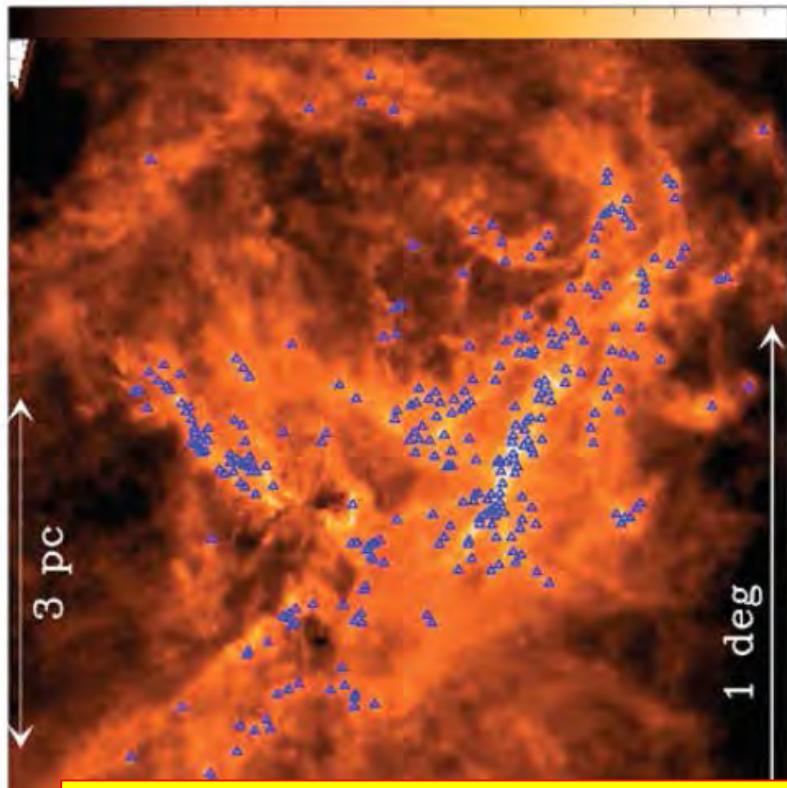
Highlight of Herschel Result (André+2010)

Prestellar cores are preferentially found within the densest filaments

△ : Prestellar cores - 90% found at $N_{H_2} > 7 \times 10^{21} \text{ cm}^{-2} \Leftrightarrow A_v(\text{back}) > 8$

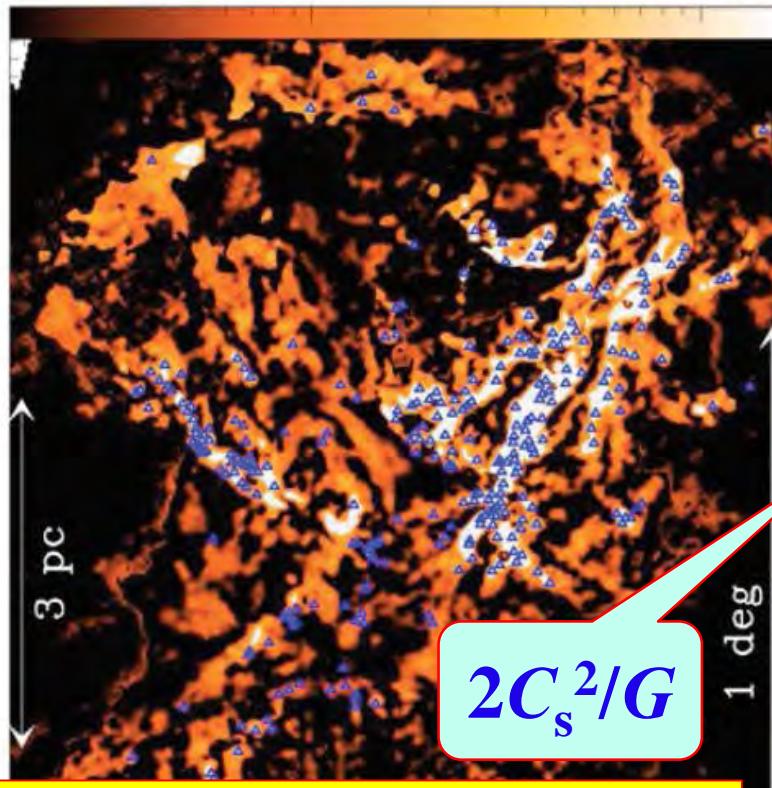
Aquila N_{H_2} map (cm^{-2})

10^{22} 10^{23}



Aquila curvelet N_{H_2} map (cm^{-2})

10^{21} 10^{22}



Unstable 1 $M_{\text{line}}/M_{\text{line,crit}}$ Stable

Self-Gravity Essential in Filaments

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- Formation of Molecular Clouds
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Mass Function of Cores in a Filament

Inutsuka 2001, ApJ **559**, L149

Line-Mass Fluctuation of Filaments

Initial Power Spectrum

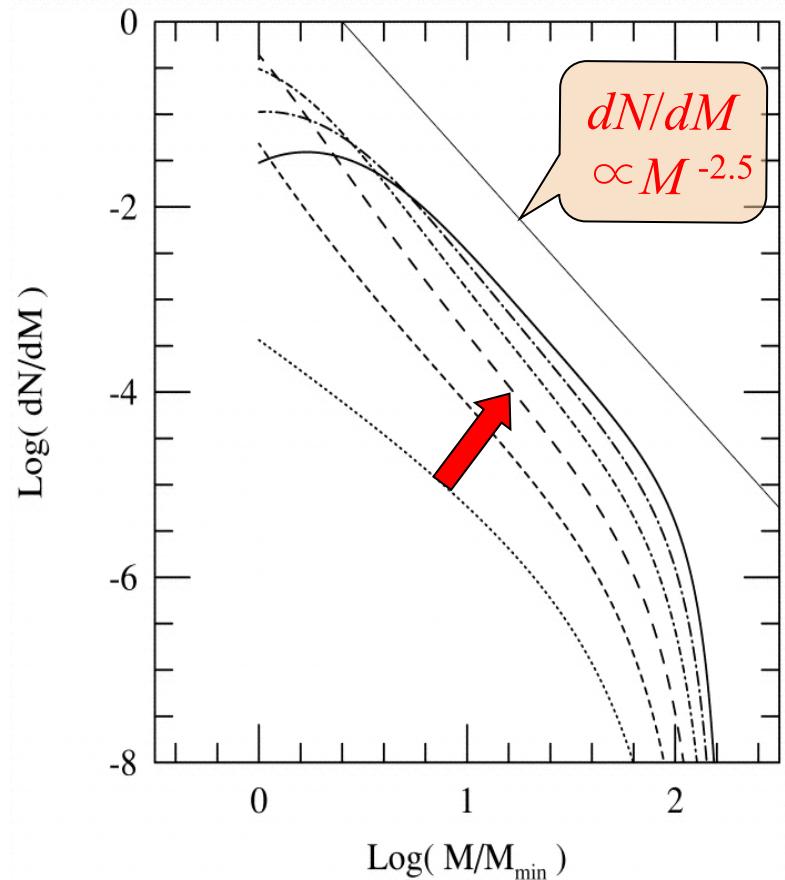
$$P(k) \propto k^{-1.5}$$

Mass Function

$$dN/dM \propto M^{-2.5}$$

Observation of Both Perturbation Spectrum and Mass Function

→ Clear and Direct Test!

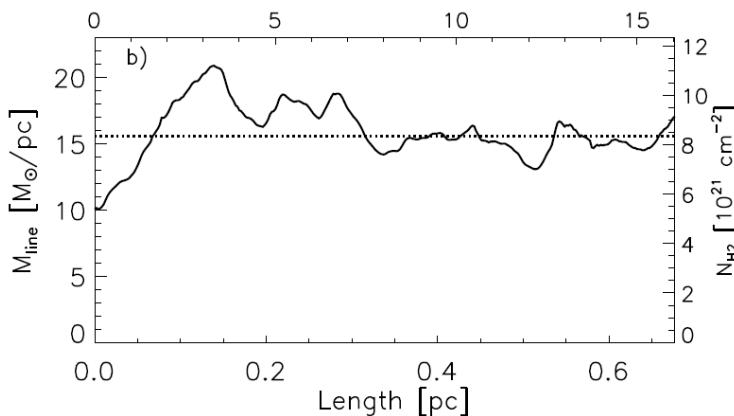
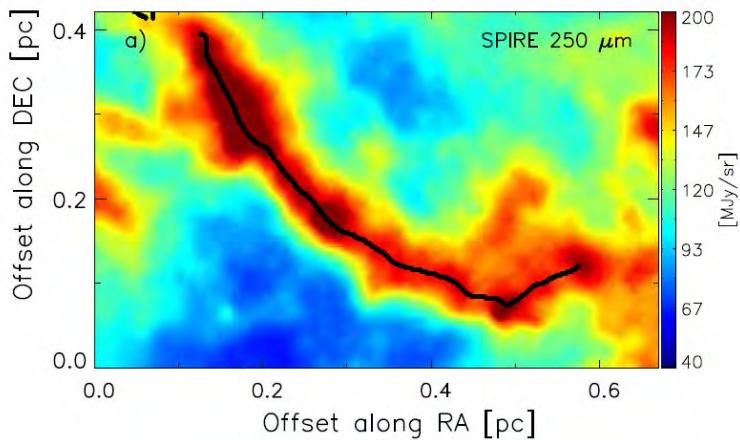


$$P(k) \propto k^{-1.5}$$

$t/t_{ff} = 0$ (dotted), 2, 4, 6, 8, 10 (solid)

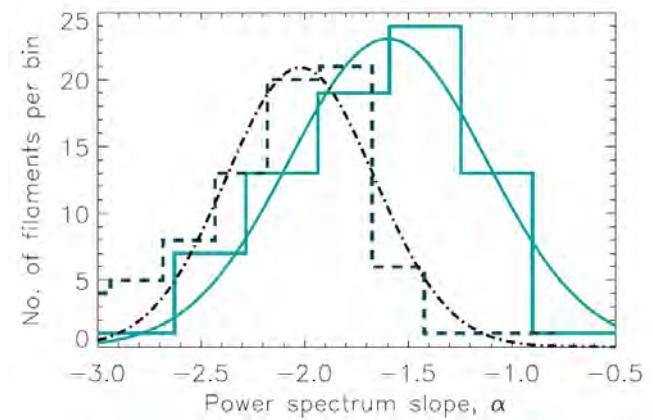
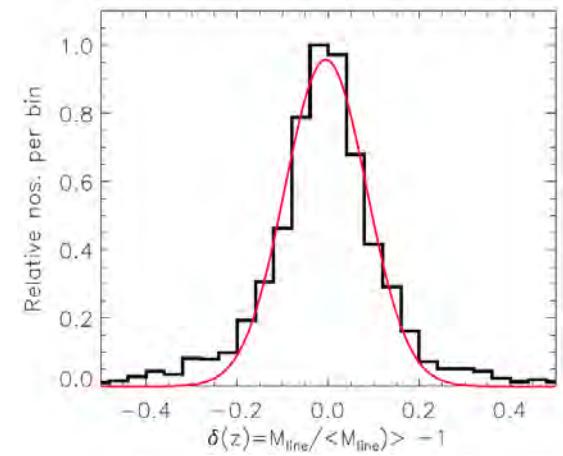
“A possible link between the power spectrum of interstellar filaments and the origin of the prestellar core mass function”

Roy, André, Arzoumanian *et al.* (2015) A&A **584**, A111



$\delta \dots$
Gaussian

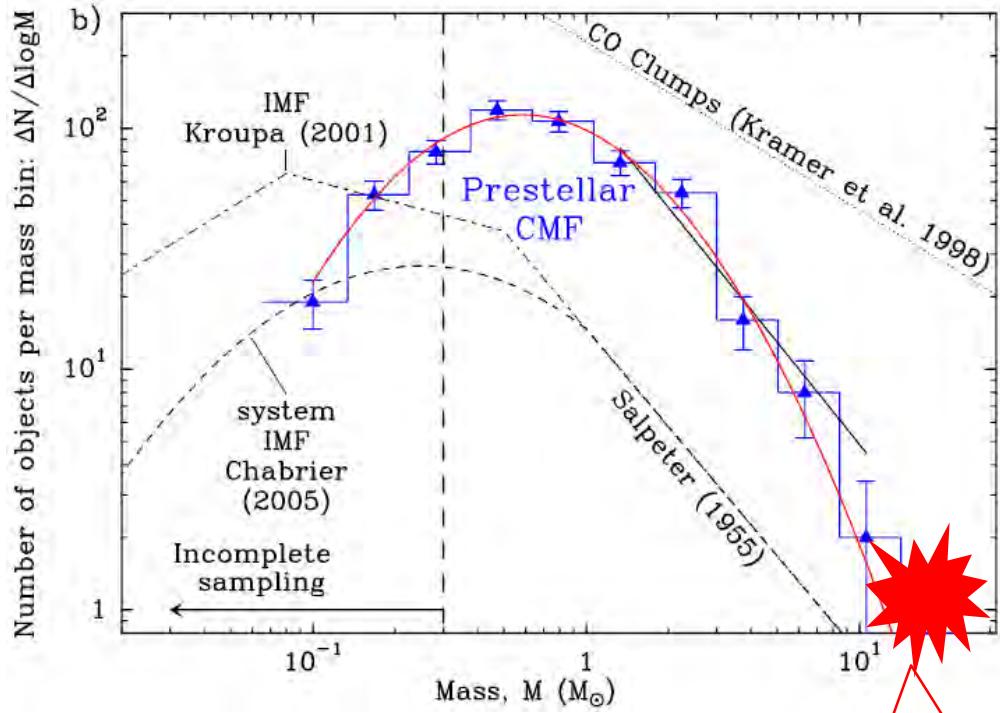
$$P(k) \propto k^n$$
$$n = -1.6 \pm 0.3$$



Supporting Inutsuka 2001

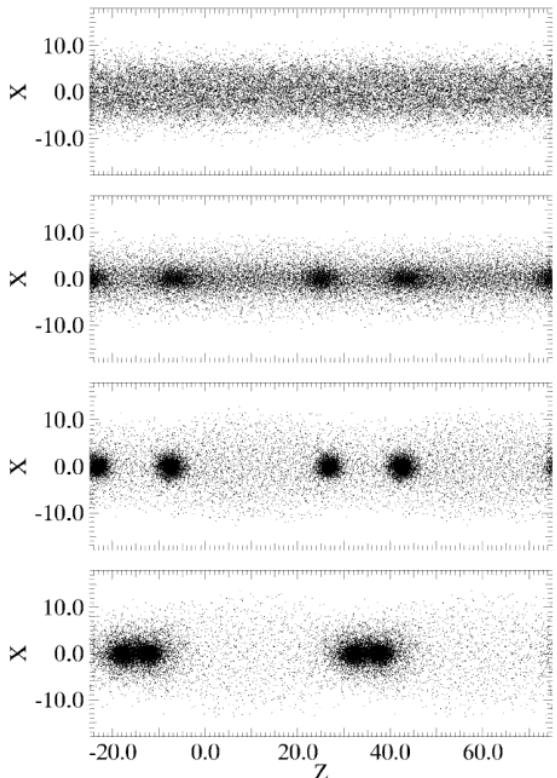
Applicability of Filament Paradigm for Massive Stars?

Aquila CMF from Herschel



André+2010; Könyves+2010

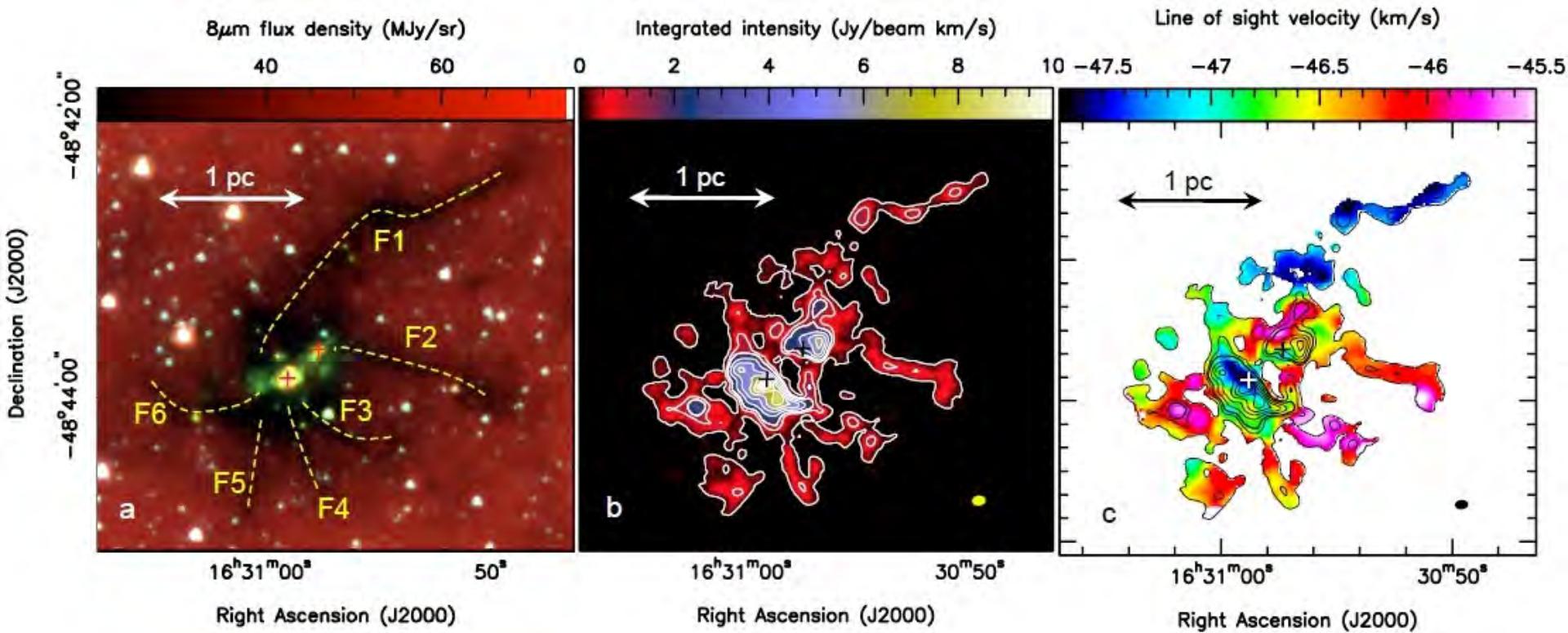
Massive stars can be
formed in filaments?



SI & Miyama 1997

Larger Wavelength
→ Massive Core

Massive Stars through Filaments



(Peretto+2013)

- Uniform but Different Velocity in Each Filament
 - Infall through Filament $\sim 10^{-3} M_{\odot}/\text{yr}$
- Nicely Understood in Filament Paradigm

Toward Global Picture of Cloud Formation

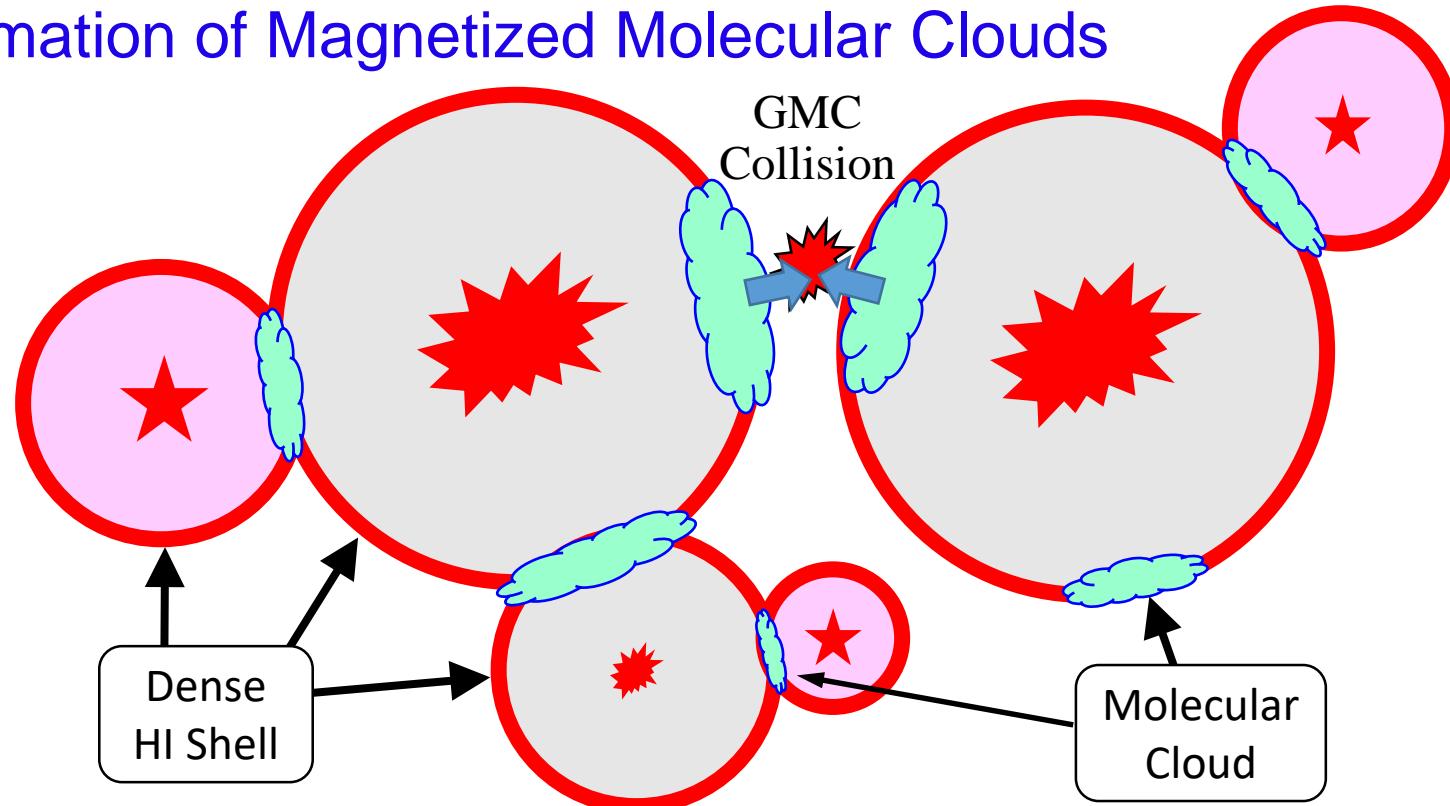
$$t_{\text{form}} = \text{a few} \times 10^7 \text{yr}$$

$$N_{\text{H}} \sim 10^{21} \text{cm}^{-2} = 1 \text{cm}^{-3} \times 300 \text{pc}$$

$$300 \text{pc} \sim 10 \text{km/s} \times 30 \text{Myr}$$

Network of Expanding Shells

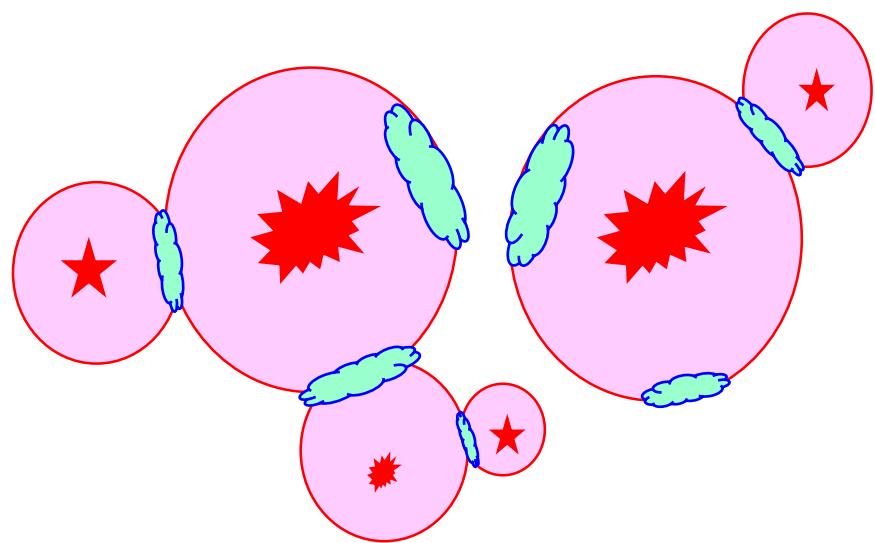
Multiple Episodes of Compression →
Formation of Magnetized Molecular Clouds



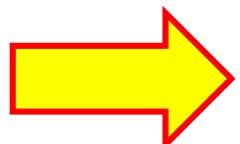
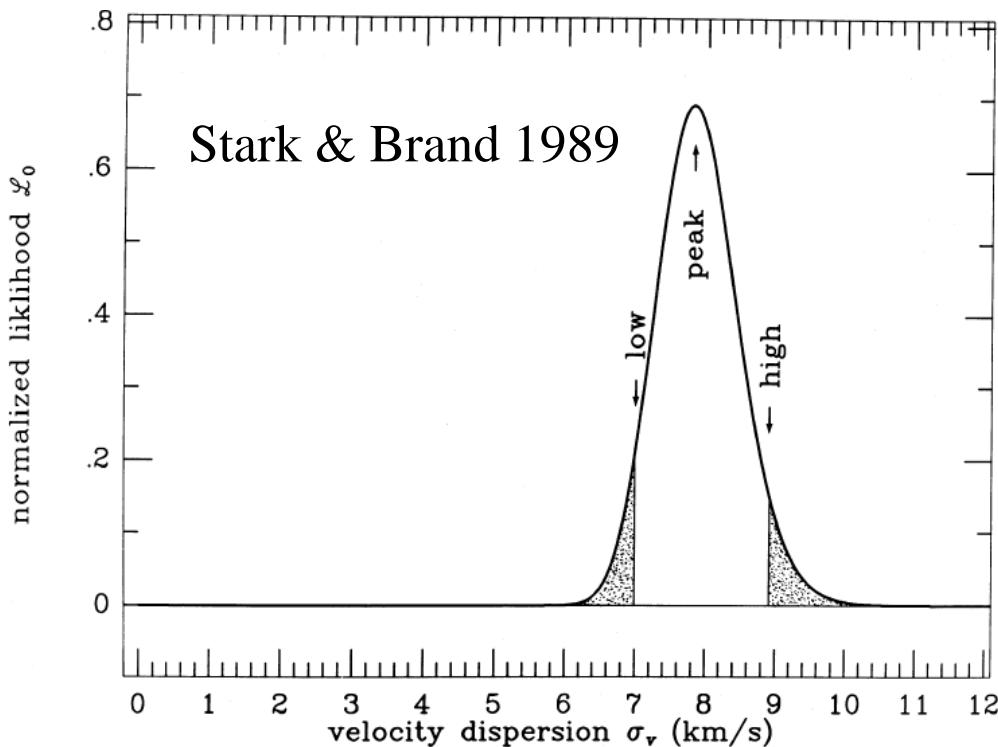
Long (>10Myr) Exposure Picture!
Each bubble disappears quickly (<Myr).

Velocity Dispersion of Clouds

Multiple Episodes of
Compression →
Formation of Magnetized
Molecular Clouds



Shell Expansion
Velocities $\sim 10^1$ km/s



Cloud-to-Cloud
Velocity Dispersion

Outline

- Formation of Molecular Clouds
 - Phase Transition Dynamics
 - Thermal Instability, Sustained Turbulence
 - Effect of Magnetic Field
- Self-Gravitational Dynamics of Filaments
 - Mass Function of Dense Cores → IMF
- Galactic Picture of Cloud/Star Formation
 - Destruction of Molecular Clouds
 - SF Efficiency & Schmidt-Kennicutt Law
 - Mass Function of Molecular Clouds
- Summary

Filament Paradigm Completely Successful?!



Other Modes of Star Formation?

Cloud Collision (*Fukui, Tan, Tasker, Dobbs,...*)
Collect & Collapse (*Elmegreen-Lada, Whitworth,
Palouš, Deharveng, Zavagno,...*)

Formation of Molecular Clouds

Can direct compression of magnetized WNM
create molecular clouds? → Not at once.

We need multiple episodes of compression.

Inoue & SI (2008) ApJ **687**, 303; Inoue & SI (2009) ApJ **704**, 161

Inoue & SI (2012) ApJ **759**, 35 Transformation of HI to H₂

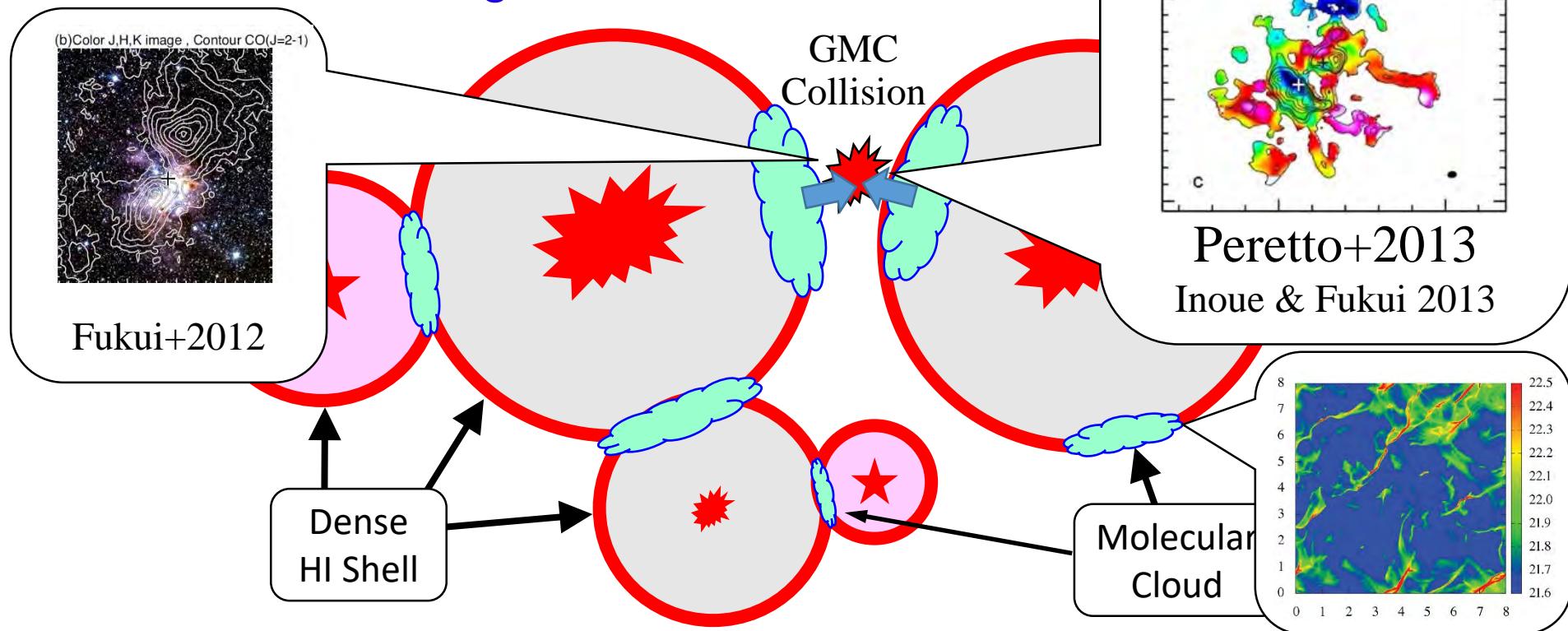
$$t_{\text{form}} = \text{a few } 10^7 \text{ yr}$$

Further Compression of Molecular Clouds

→ Magnetized Massive Filaments & Striations
= “Herschel Filaments”

Network of Expanding Shells

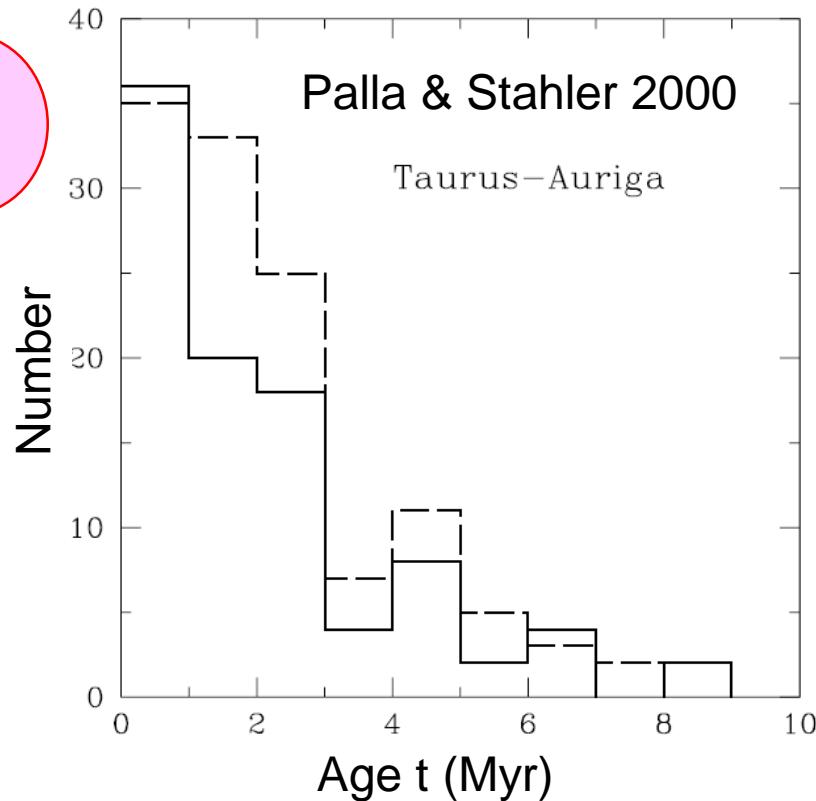
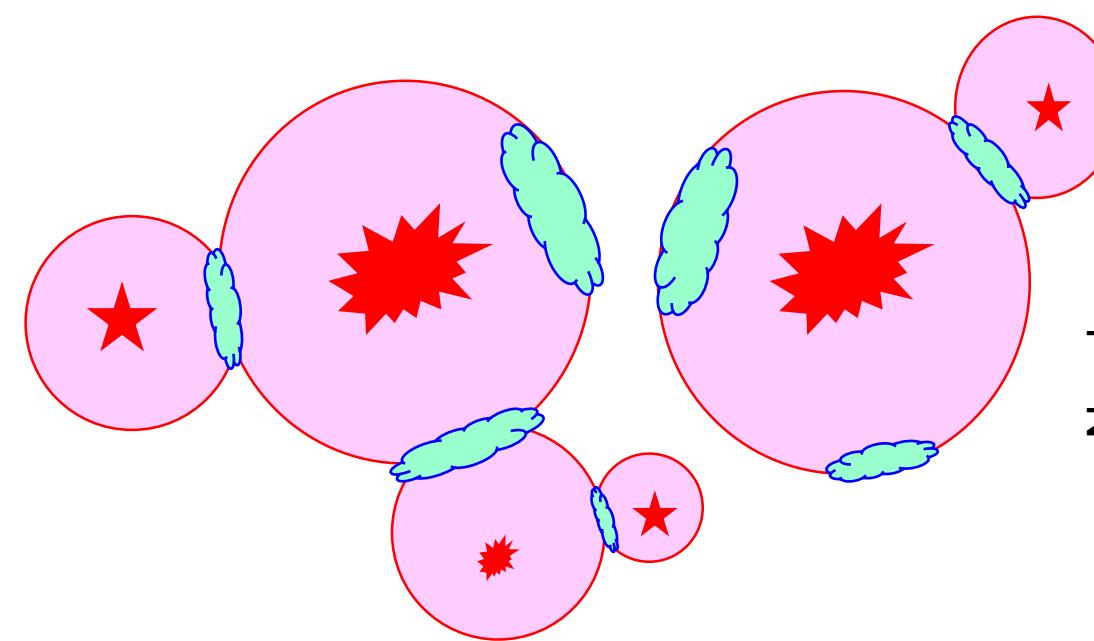
Multiple Episodes of Compression →
Formation of Magnetized Molecular Clouds



Each Bubble Visible Only for Short Time (~1Myr)!

δv of Clouds ~ Cloud-Cloud Col. Velocity ~ **10km/s**

Natural Acceleration of Star Formation



Molecular Cloud Growth
→ Collisions of Clouds
→ Accelerated SF

Also in *Lupus*, *Chamaeleon*,
 ρ *Ophiuchi*, *Upper Scorpius*,
IC 348, and *NGC 2264*

c.f., Vazquez-Semadeni+2007

Destruction of Molecular Clouds

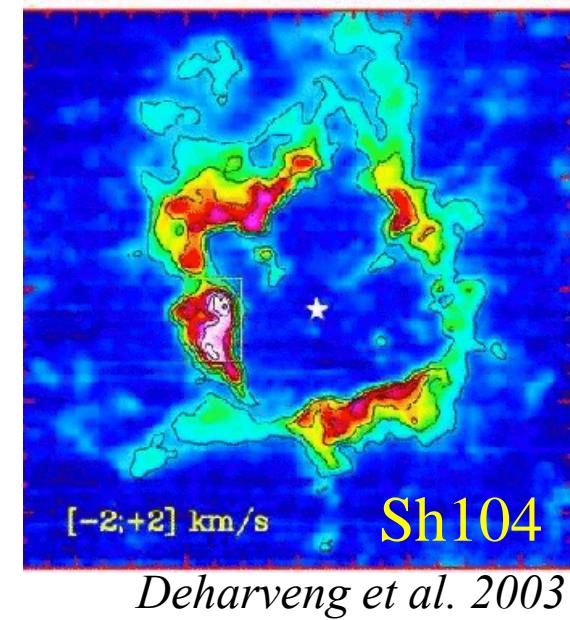
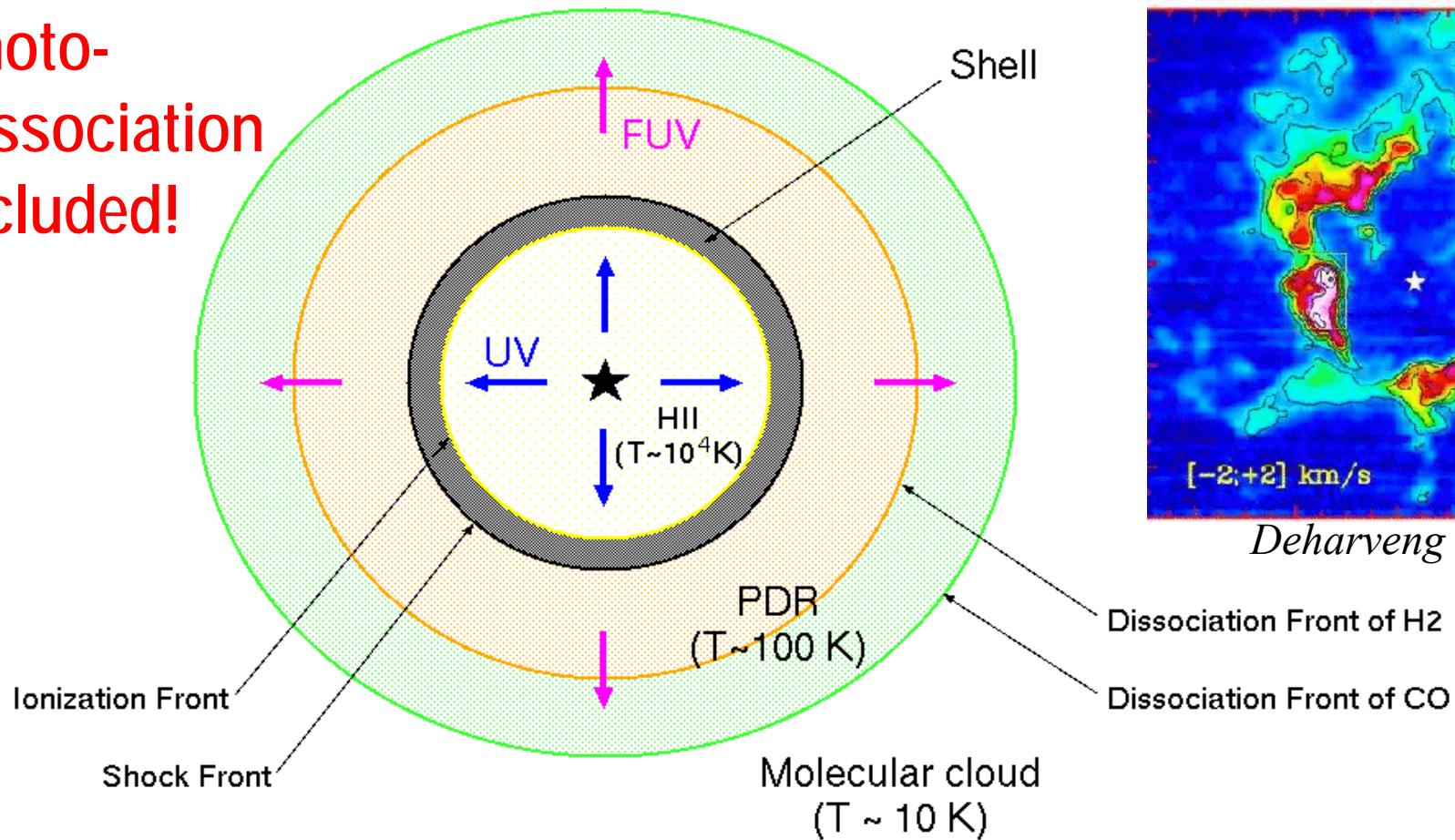
How to Stop Star Formation?

Radiative Feedback

See also *Kuiper+*, *Walch+*, *Hennebelle+*

Expanding HII Region in Magnetized Molecular Cloud

Photo-
Dissociation
Included!



Deharveng et al. 2003

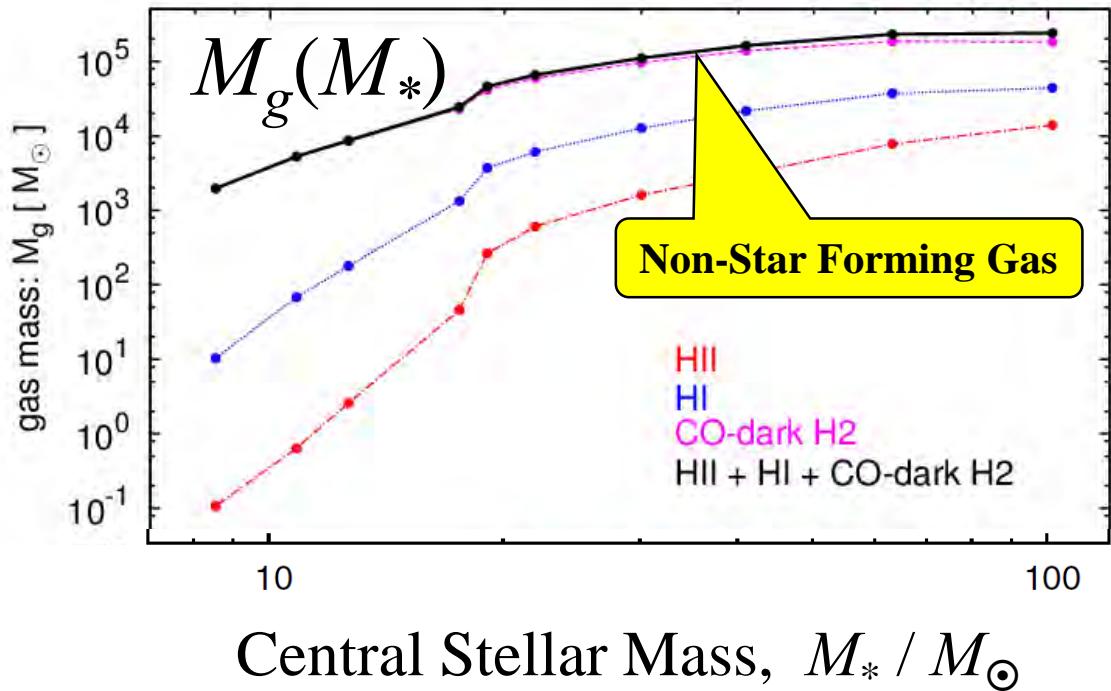
Radiation Magnetohydrodynamics Calculation
UV/FUV + H₂ + CO Chemistry (Hosokawa & Si 2005, 2006ab, 2007)

Disruption of Magnetized Molecular Clouds

Feedback due to **UV/FUV**
in a **Magnetized** Cloud
by MHD version of
Hosokawa & SI (2005,2006ab)



$30M_{\odot}$ star destroys
 $10^5 M_{\odot}$ H₂ gas
in 4Myrs!



Star Formation Efficiency, KS-Law

$10^5 M_\odot$ H₂ destroyed by $M_* > 30 M_\odot$ in 4Myrs!

If $M_{\text{total}} \sim 10^3 M_\odot$ stars

→ ~1 Massive ($> 30 M_\odot$) Star for Standard IMF

$$\rightarrow \varepsilon_{SF} = \frac{10^3 M_\odot}{10^5 M_\odot} = 0.01$$

Zuckerman & Evans 1974
Star Formation Time
~10Myr

Cloud Disruption Time: $T_d = 4 \text{ Myr} + T_*$

Gas Depletion time: $\tau_{\text{depl}} = \frac{T_d}{\varepsilon_{SF}} \sim 1.4 \text{ Gyr}$

No Dependence on Cloud Mass! (e.g., Bigiel+2011)

Galactic Population of Molecular Clouds

???

Mass Function of Molecular Clouds

$$dn = N_{\text{cl}}(M_{\text{cl}})dM_{\text{cl}}$$

$$\frac{\partial N_{\text{cl}}}{\partial t} + \frac{\partial}{\partial M_{\text{cl}}} \left(N_{\text{cl}} \frac{dM_{\text{cl}}}{dt} \right) = - \frac{N_{\text{cl}}}{T_{\text{depl}}}$$

Self-Growth

$$\frac{M_{\text{cl}}}{T_{\text{form}}}$$

$T_{\text{depl}} = \text{const.}$
“KS Law”

In steady state

$$\rightarrow N_{\text{cl}}(M_{\text{cl}}) = \frac{N_0}{M_0} \left(\frac{M_{\text{cl}}}{M_0} \right)^{-\alpha}, \quad \alpha = 1 + \frac{T_{\text{form}}}{T_{\text{dis}}}$$

$$T_{\text{dis}} \sim 14 \text{ Myr} \quad \& \quad T_{\text{form}} \sim 10 \text{ Myr} \rightarrow \alpha = 1.7$$

Effect of Cloud-Cloud Collision on Mass Function of Molecular Clouds

Formulation of Coagulation Equation

$$\frac{\partial n_{\text{cl}}}{\partial t} + \frac{\partial}{\partial M} \left(n_{\text{cl}} \frac{dM}{dt} \right) = - \frac{n_{\text{cl}}}{T_d}$$

$T_d = \text{const. "KS Law"}$

$$\frac{M_{\text{cl}}}{T_f}$$

$$+ \frac{1}{2} \int_0^\infty \int_0^\infty K(m_1, m_2) n_{\text{cl},1} n_{\text{cl},2} \delta(m - m_1 - m_2) dm_1 dm_2 \\ - \int_0^\infty K(m, m_2) n_{\text{cl}} n_{\text{cl},2} dm_2 .$$

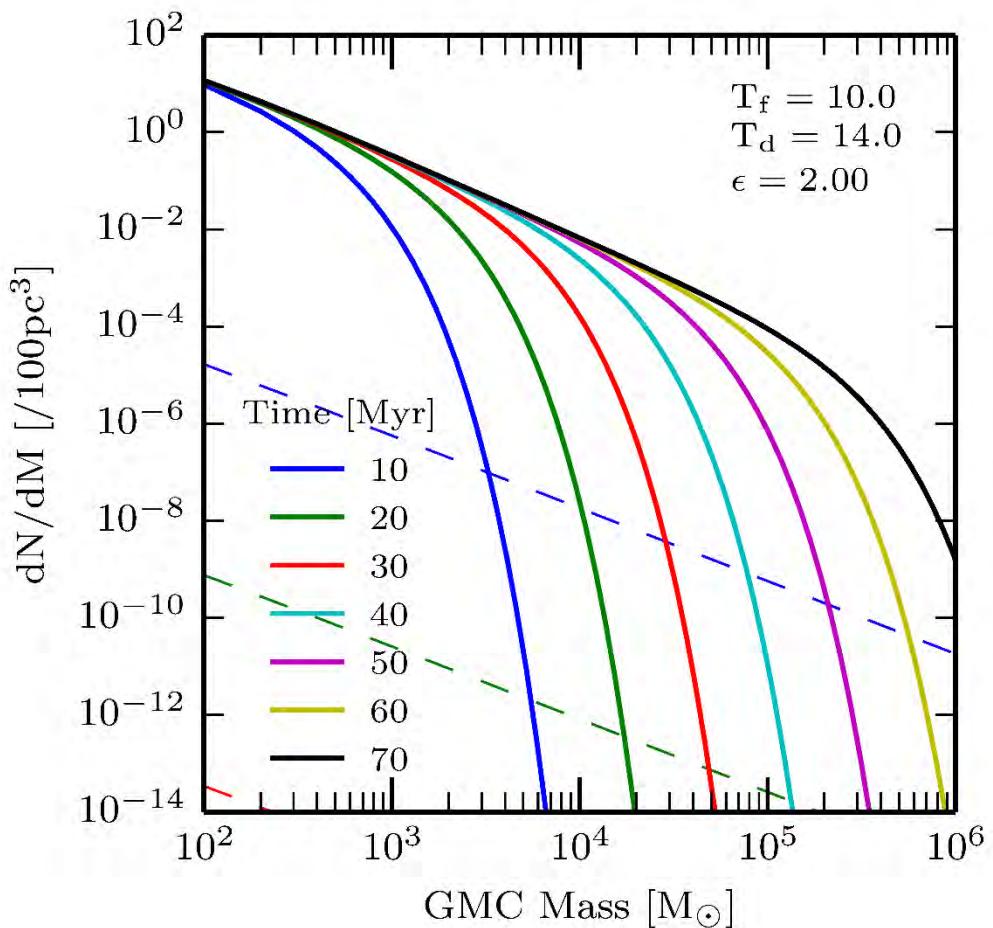
Effect of Cloud-
Cloud Collision

Resultant Mass Functions

Case without Cloud-Cloud Collision

**self-growth &
self-dispersal
only**

Assumption:
 $\delta v_{\text{cloud-cloud}} = 10 \text{ km/s}$



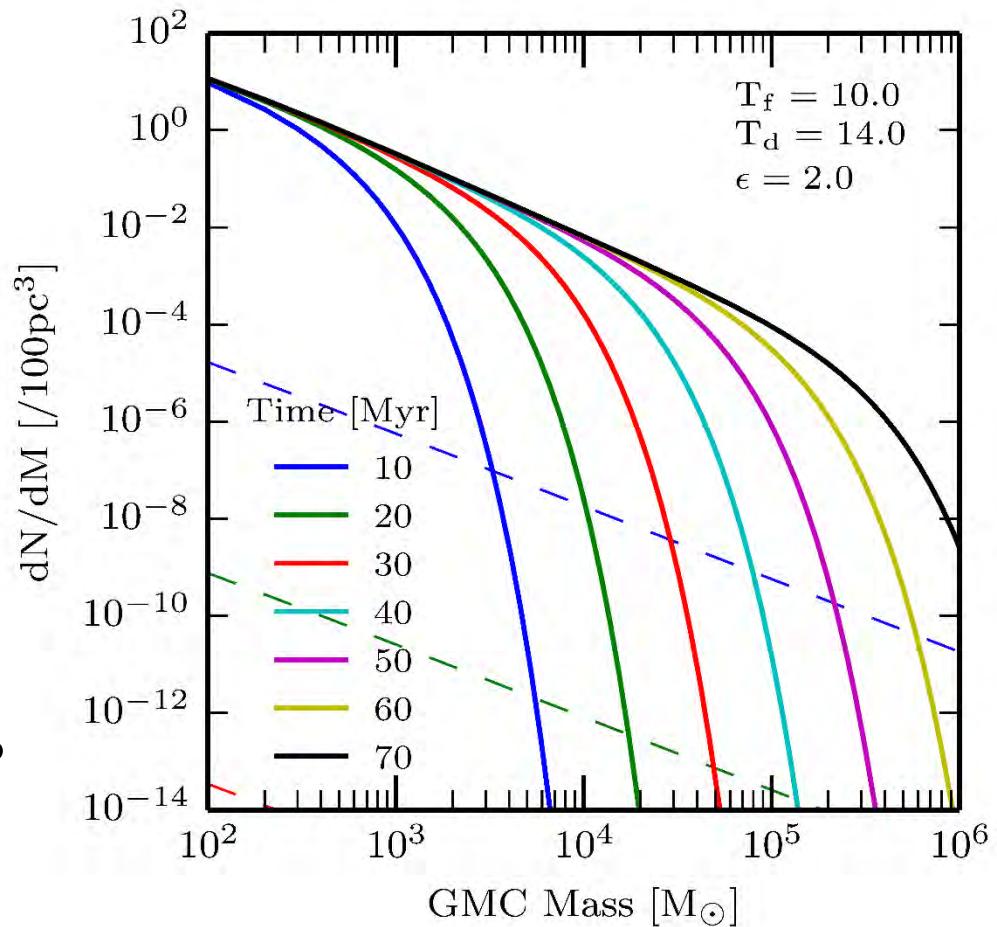
Resultant Mass Functions

Case with Cloud-Cloud Collision

+ self-growth
& self-dispersal

Assumption:

$$\delta v_{\text{cloud-cloud}} = 10 \text{ km/s}$$



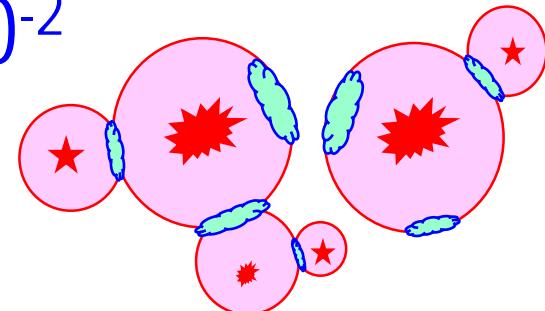
CCC does not alter GMC mass function significantly!

Summary

- Fragmentation of Filaments → Core Mass Function
- Bubble-Dominated Formation of Molecular Clouds

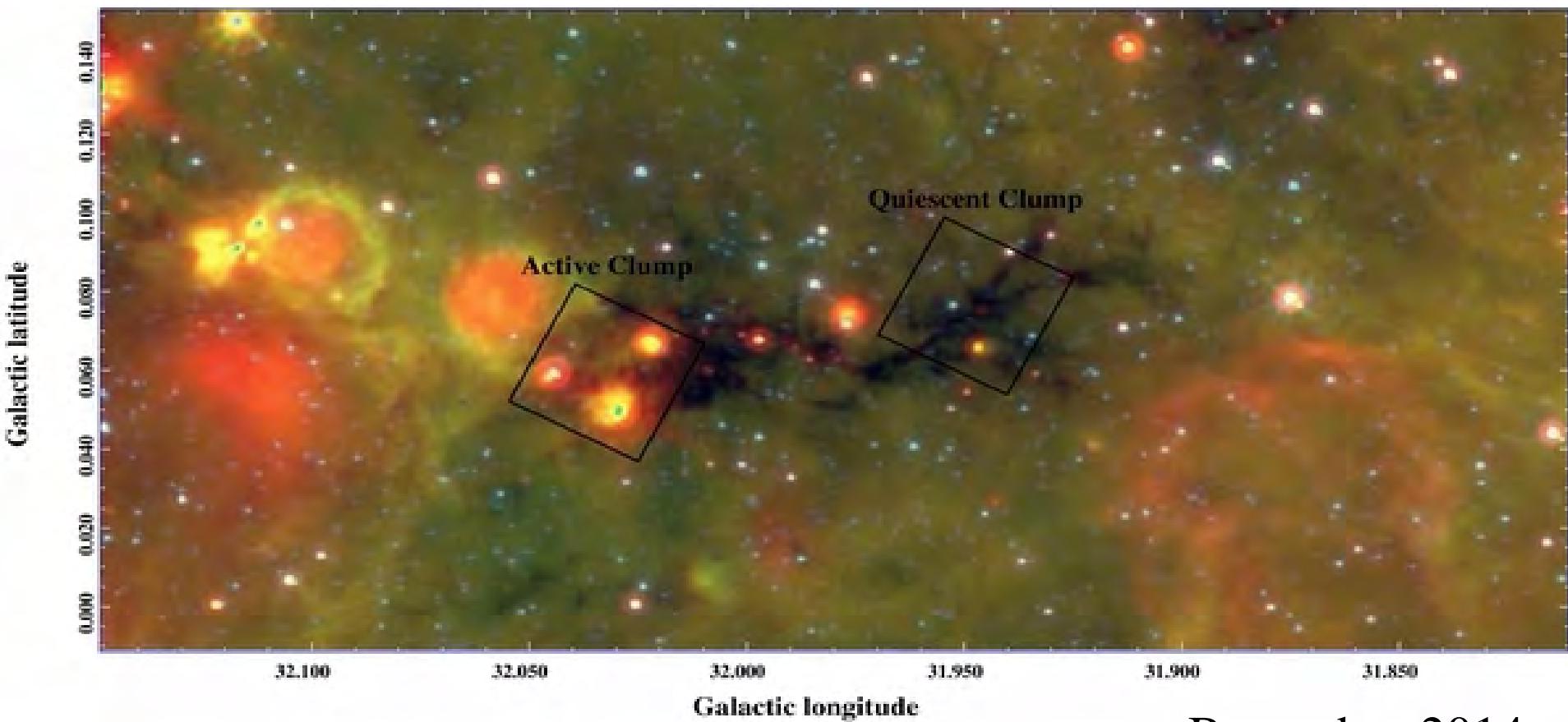
→ Unified Picture of Star Formation

- $\delta v_{\text{cloud-cloud}} \sim 10^1 \text{ km/s}$
- Star Formation Efficiency: $\epsilon_{\text{SF}} \sim 10^{-2}$
- Schmidt-Kennicutt Law
- Accelerated Star Formation
- Slope of Cloud Mass Func = $1 + T_{\text{form}}/T_{\text{dis}} \sim 1.7$



SI, Inoue, Iwasaki, & Hosokawa 2015, A&A 580, A49
Kobayashi, SI, Kobayashi, & Hasegawa 2017, ApJ 836, 175

Massive Star Formation in Ridge

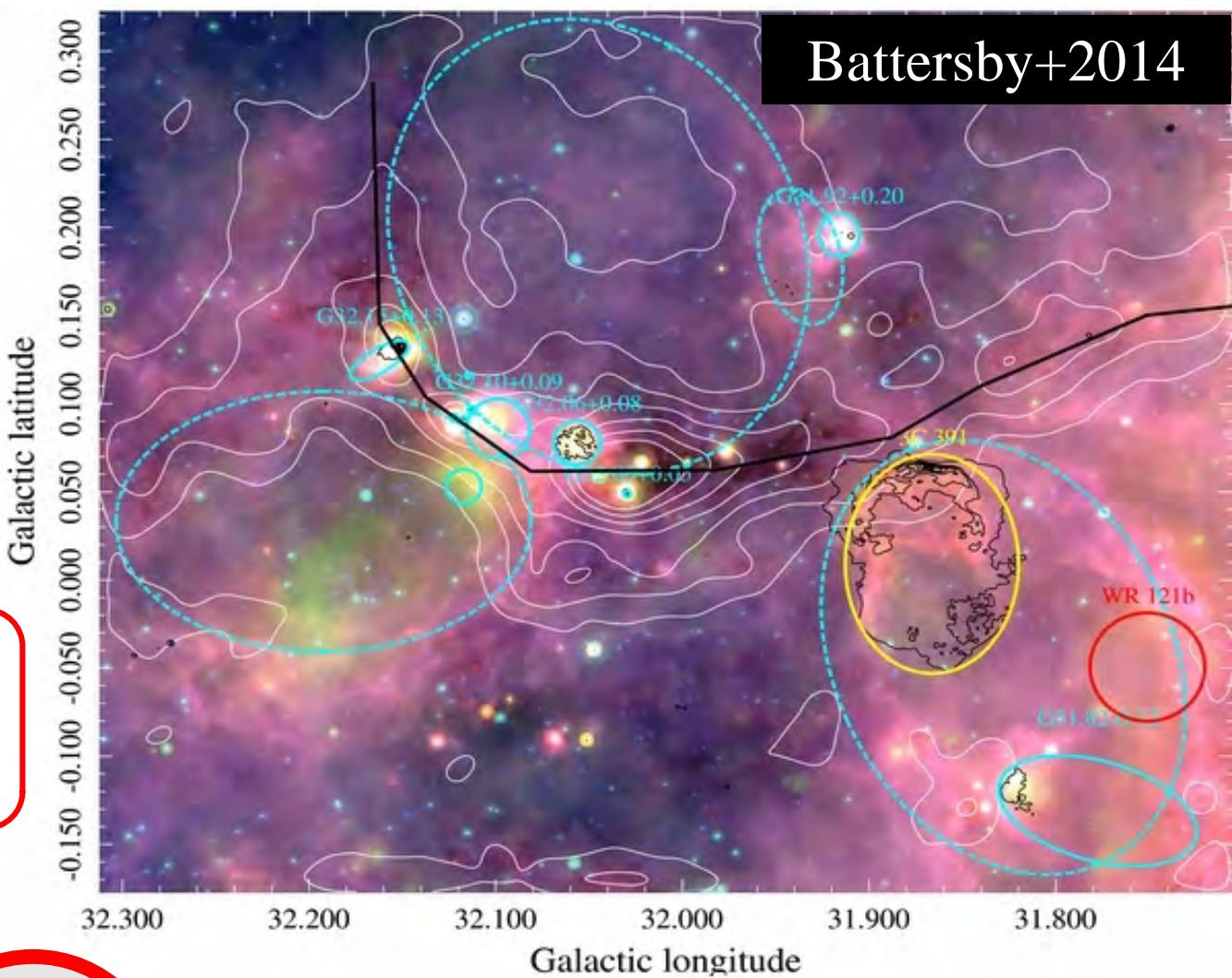
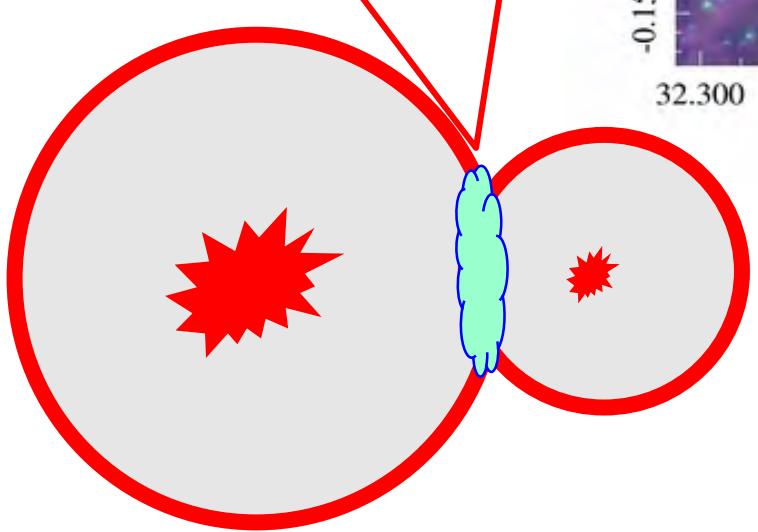


Battersby+2014

Extensive Herschel Studies on Massive Star Formation in “Ridges”

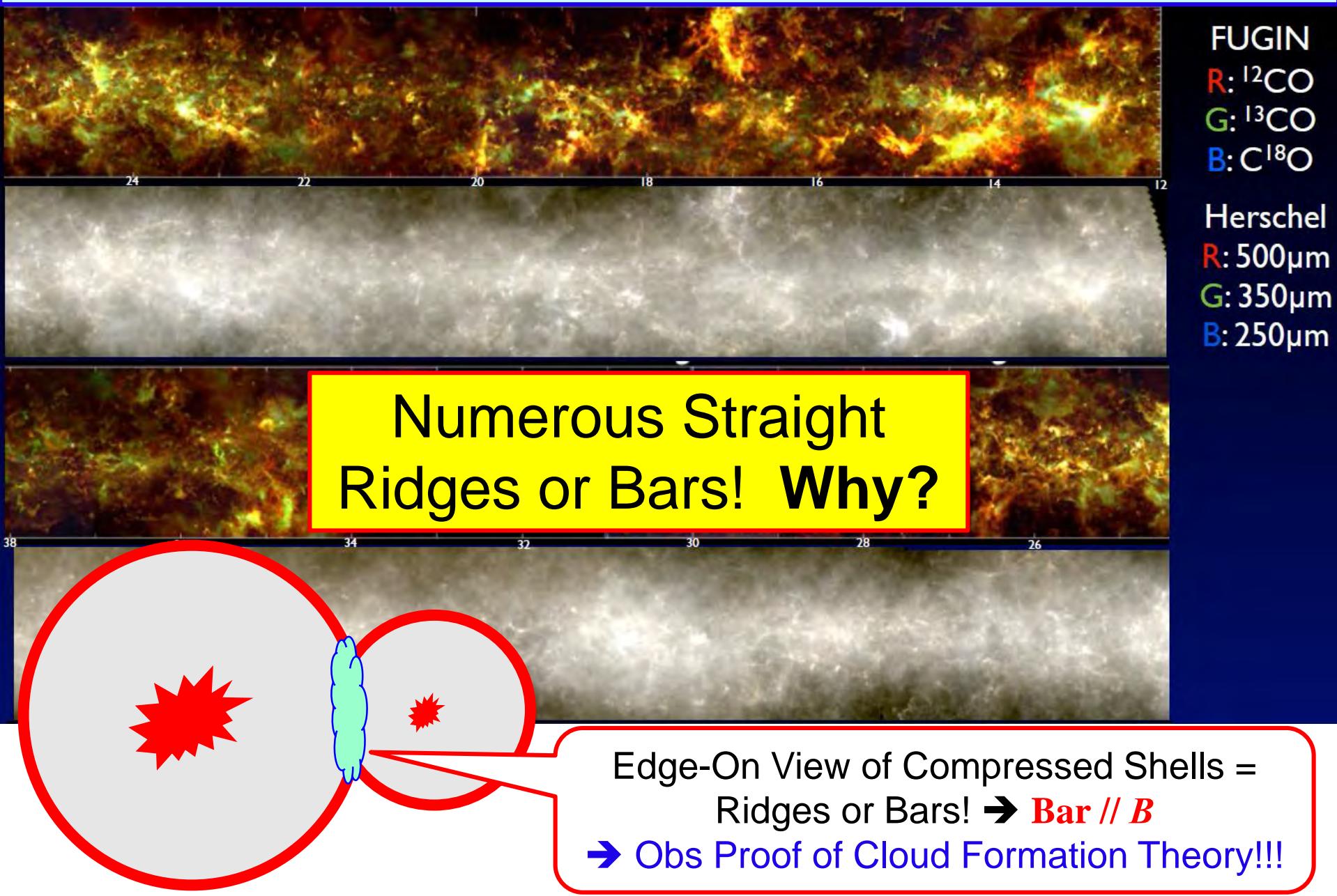
Ridge or Edge-On Shell?

Edge-On View of
Compressed Shell
→ Ridge or Bar!



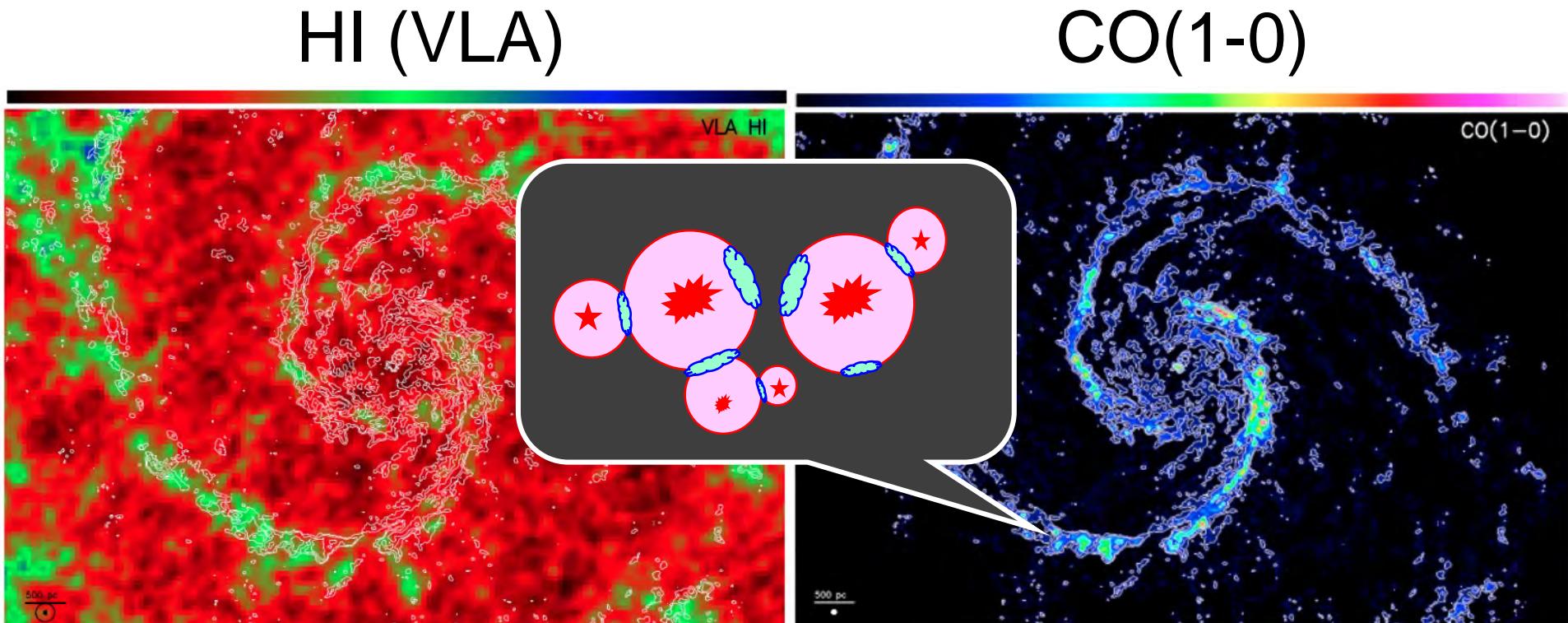
Bubbles (cyan dashed circles)
HII regions (cyan solid circles)
SNR 3C 391 (yellow oval)
Wolf-Rayet star WR 121b (red oval)

Advent of Large Surveys such as FUGIN



Galactic Scale View

HI Clouds vs Molecular Clouds



M51 in PAWS Schinnerer+ (2013)

Slope of Cloud Mass Function

Steady State Mass Function of Molecular Clouds

$$\rightarrow N_{\text{cl}}(M_{\text{cl}}) = \frac{N_0}{M_0} \left(\frac{M_{\text{cl}}}{M_0} \right)^{-\alpha}, \quad \alpha = 1 + \frac{T_{\text{form}}}{T_{\text{dis}}}$$

Typically, $T_{\text{dis}} \sim T_{\text{form}} + 4 \text{Myr} \rightarrow \alpha = 1.7$

In low density region (Inter-Arm Region)

Larger $T_{\text{form}} > T_{\text{dis}} \rightarrow$ Larger α

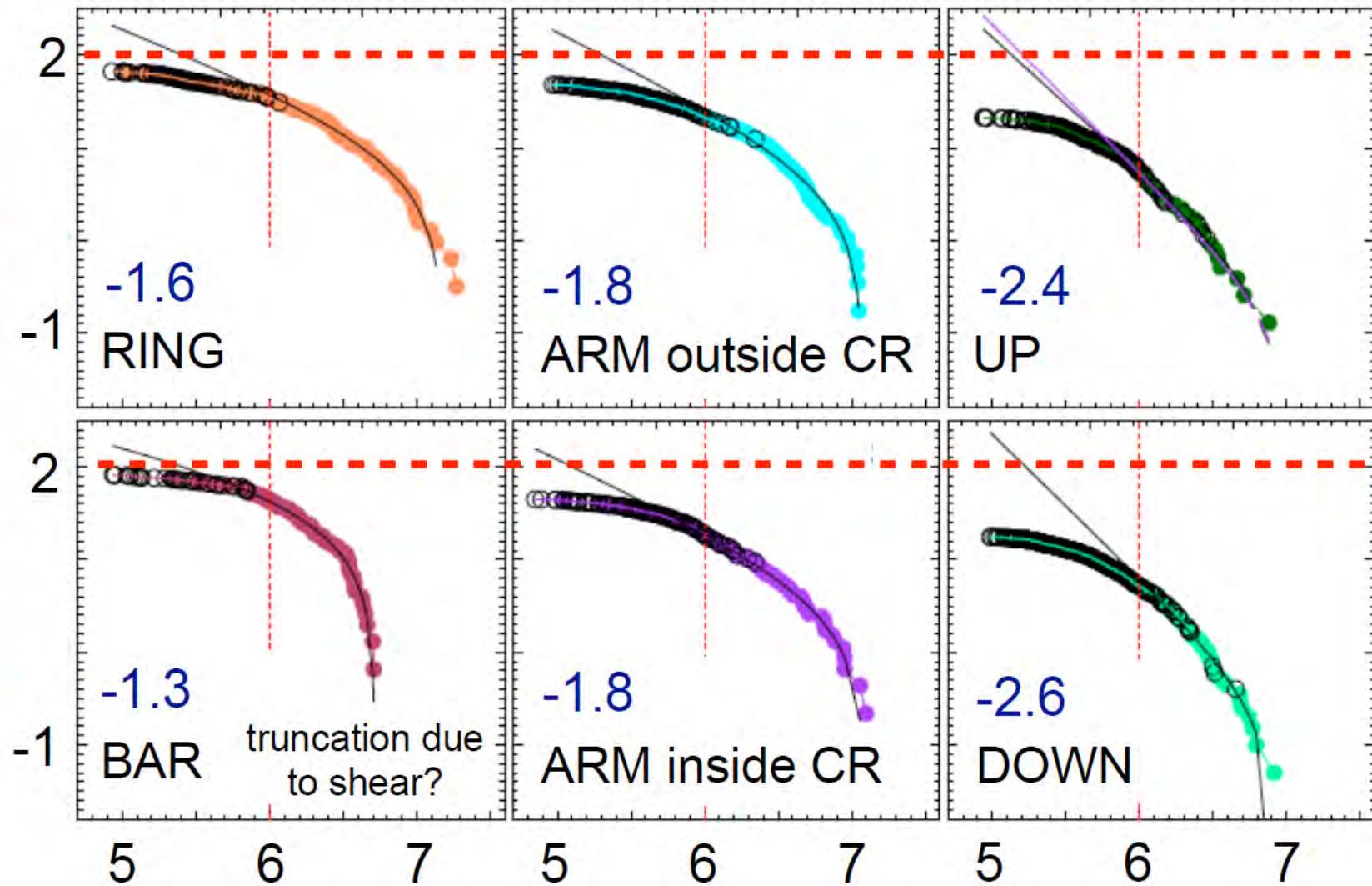
In high density region (Arm Region)

Smaller $T_{\text{form}} \rightarrow$ Smaller α

\rightarrow GMCs in M51 (Colombo+2014)

Variation of GMC Mass Function in M51

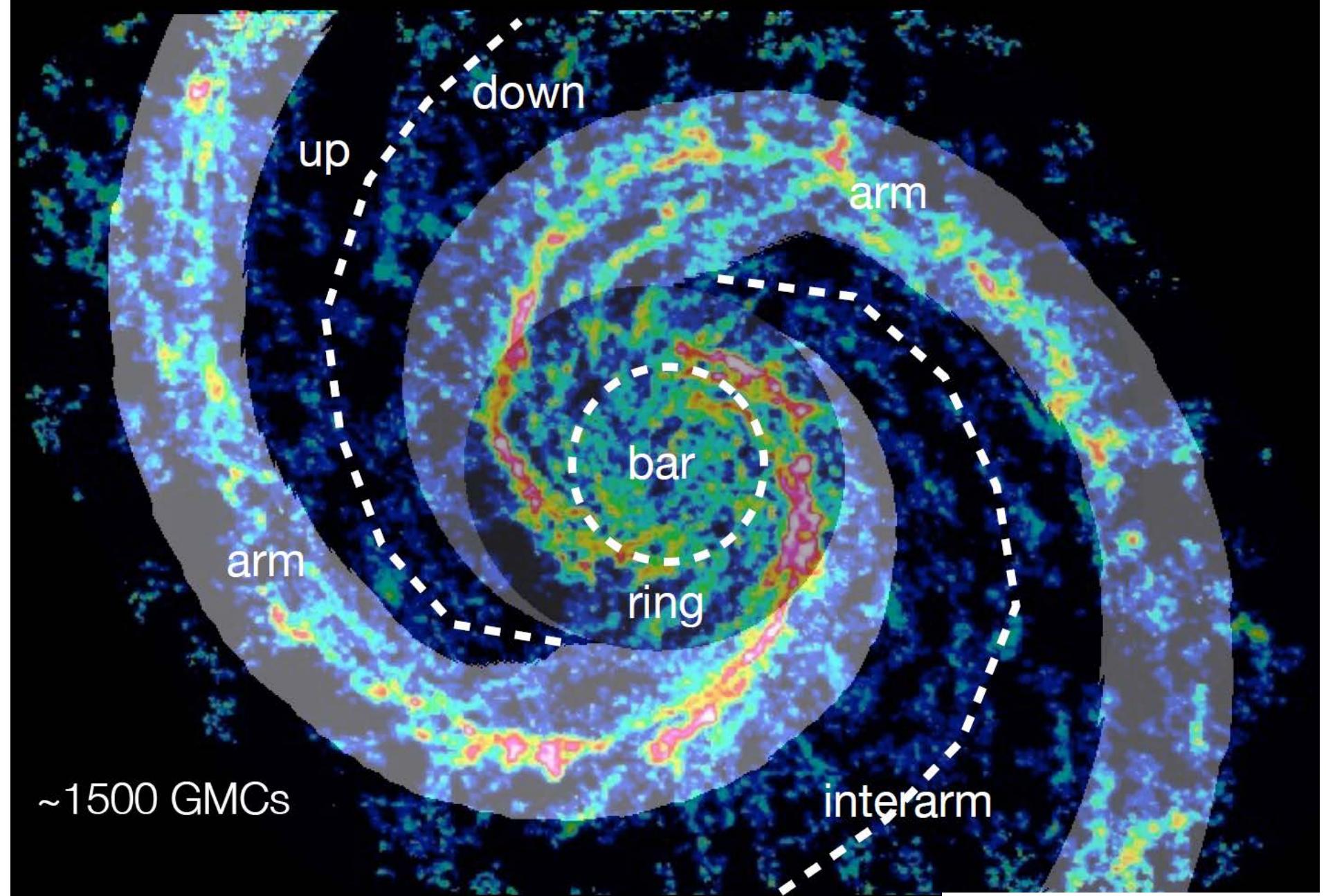
log($N(M > M) / [kpc^2]$)



log(Mass/M_⊙)

Colombo+2014

Colombo et al (2014)



©Annie Hughes, MPIA

Mass Function of Molecular Clouds

$$dn = N_{\text{cl}}(M_{\text{cl}})dM_{\text{cl}}$$

$$\frac{\partial N_{\text{cl}}}{\partial t} + \frac{\partial}{\partial M_{\text{cl}}} \left(N_{\text{cl}} \frac{dM_{\text{cl}}}{dt} \right) = - \frac{N_{\text{cl}}}{\tau_{\text{dis}}}$$

→ CO-Dark Gas

In steady state, mass of CO-dark gas can be huge!

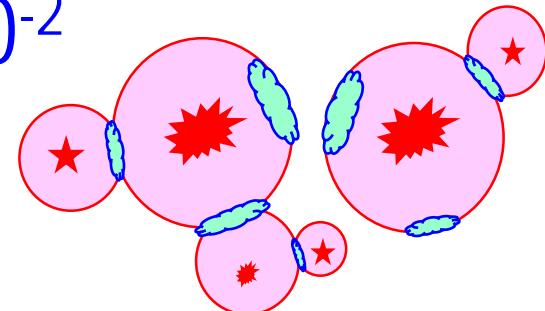
→ Formation of Molecular Clouds should recycle CO-Dark Gas!

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- Bubble-Dominated Formation of Molecular Clouds

→ Unified Picture of Star Formation

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SI, Inoue, Iwasaki, & Hosokawa 2015, A&A 580, A49
Kobayashi, SI, Kobayashi, & Hasegawa 2017, ApJ 836, 175

Future Work

- Galactic Disk Scale Simulations with GMC Model as a Sub-Grid Physics: Spatial Resolution $\sim 100\text{pc}$
- Galactic Center
- Model of Spur

*SI, Inoue, Iwasaki, & Hosokawa 2015, A&A **580**, A49
Kobayashi, SI, Kobayashi, & Hasegawa 2017, ApJ **836**, 175*