# CMB component separation intution and GreenPol

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Rules of thumb:

1.0 at  $f_{skv} \sim 0.1$  $A_{f_{0}} < 1\mu K$ P<sub>synch</sub> @ 30 GHz P<sub>dust</sub> @ 353 GHz 0.8  $P_{dust}$ Cumulative distribution 0.6 Synchrotron 3 10 μK<sub>RJ</sub> @ 353 GHz 0.4 Psynch 0.2 **Noise floor** 10 µK<sub>RJ</sub> @ 30 GHz 0.0  $10^{-1}$  $10^{0}$  $10^{1}$  $10^{2}$  $10^{3}$ Polarization amplitude  $[\mu K]$ 







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NB! Only intended to provide a rough order-of-magnitude estimate! Precise values depend of course sensitively on sky location and angular scales

What is the ideal frequency coverage for a typical CMB + synchrotron + thermal dust model space?

 $\mathbf{h} \mathbf{u}^d$ 

• Assume following typical model for a single pixel on the sky:

$$s_{\nu} = A_{cmb} + A_s g(\nu) \left(\frac{\nu}{\nu_0^s}\right)_s^{\beta} + A_d g(\nu) \left(\frac{\nu}{\nu_0^d}\right)_s^{\beta_d + 1} \frac{e^{\frac{h\nu_0}{kT_d}} - 1}{e^{\frac{h\nu_0}{kT_d}} - 1}$$

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  - T<sub>d</sub>: Effective thermal dust temperature



• Given a set of observed frequencies with associated instrumental noise RMS's, the posterior distribution for this model reads

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  - Note: This is essentially a special case of the Planck 2015 analysis, reducing *Commander* to a single pixel, and including only CMB, synchrotron and thermal dust in the model

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• In addition, since most experiments are limited by focal plane area, and the size of a diffraction limited detector scales inverse proportionally to its wavelength, the effective noise (including focal plane penalty) scales as

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- (Lots of other effects as well, of course, but we only care about order-of-magnitude estimates here)
- Distribute channels according to total signal-to-noise in the following cases

# The atmosphere



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# Case 1: Low foreground, high-latitude sky



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 However, extending to lower frequencies carries a very low cost in sensitivity, even when accounting for focal plane area. Critical point: S ~ ν-3, while N ~ ν-3/2.













1) As foregrounds become brighter, the optimal solution moves to lower frequencies.









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# Case 3: Galactic plane







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- 2) But if foregrounds are non-negligible, *extend the frequency range as much* as possible until the model breaks down, *even when accounting for focal plane area!*

 $N_{\rm band} = 9$ 

 $A_{fg}$  = 10  $\mu$ K







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2) If at all possible, one should strive to include frequencies below 30 GHz in order to measure synchrotron properly (as opposed to gambling on being lucky)

### Case 4: Ground-based, intermediate latitudes



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1) Best 5-band ground-based solution is 10-350 GHz (maximum leverage)

2) Two nearly equally sensitive solutions exist for 10-90 GHz and 45-350 GHz.



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In order to go deep (r < 0.01), we need to measure *both low and and high* frequencies to high precision!

## «GreenPol» -- low frequencies from Greenland

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 $\mu K_{RJ}$  @ 353 GHz
#### «GreenPol» -- low frequencies from Greenland



μK<sub>RJ</sub> @ 353 GHz

#### «GreenPol» -- low frequencies from Greenland



• NSF-OPP











# 72° N supports unique cross-linking



# Sensitivity per focalplane

Frequency [GHz]	FWHM [Arcmin]	Bandwidth [GHz]	NET [µK*√sec]	Pixels/Telescop e	Aggregate NET [µK*√sec]
10	80	4	316	7	120
15	53	4	316	13	88
20	40	4	443	19	102
30	27	6	361	25	72
45*	18	6	200	40	16

- 10-30 GHz receivers assume currently available HEMT amplifiers cooled to 20K
- 45 GHz receiver assumes an achievable bolometric detector array.

The above assumptions are for one telescope each frequency. We expect a real experiment will incorporate more than one telescope per frequency.

### Commander simulations



Fuskeland et al. 2017, in prepration

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- From now on, the name of the game is component separation, not noise reduction
- In this landscape, *frequency leverage* is the key factor
- Low-frequency observations should be an integral part of any ambitious next-generation project, both for sensitivity and robustness