Nuclear Reaction Networks

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The physics of macronova Stockholm, June 12 - 20, 2018









Lecture 3: Applications to the r process

Operation of the r process

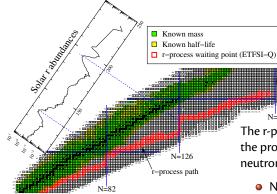
2 The r process in mergers

R-process sites

- Any r-process site should be able to produce both the "seed" nuclei where neutrons are captured and the neutrons that drive the r-process. The main parameter describing the feasibility of a site to produce r-process nuclei is the neutron-to-seed ratio: $n_n/n_{\rm seed}$.
- If the seed nuclei have mass number $A_{\rm seed}$ and we have $n_n/n_{\rm seed}$ neutrons per seed, the final mass number of the nuclei produced will be $A=A_{\rm seed}+n_n/n_{\rm seed}$.
- For example, taking $A_{\rm seed}=90$ we need $n_n/n_{\rm seed}=100$ if we want to produce the 3rd r-process peak ($A\sim195$) and $n_n/n_{\rm seed}=150$ to produce U and Th.

Making Gold in Nature: r-process nucleosynthesis

Astrophysical environment must provide a large amount of free neutrons. Depends on the neutron richness of the ejecta.



The r-process requires the knowledge of the properties of extremely neutron-rich nuclei:

Nuclear masses.

N=184

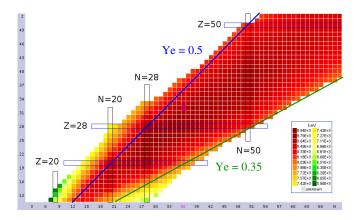
- Beta-decay half-lives.
- Neutron capture rates.
- Fission rates and yields.

R-process sites

In an astrophysical site there are only two possible ways to achieve large neutron-to-seeds:

- Let us consider high temperature neutron-rich matter with high entropy that it is ejected at high velocities. As the material expands α particles will be formed. However, the build up of heavy nuclei by 3-body reactions becomes very unefficient by two reasons: 1) Too many photons per nucleon due to the high entropy, 2) Too litle time to produce heavy nuclei due to the fast expansion. It means that we will have an α -rich freeze out with a few heavy nuclei produced and many neutrons left ($Y_{\alpha} \approx Y_{e}/2$, $Y_{n} \approx 1-2Y_{e}$). The Big Bang is an extreme case of α -rich freeze-out. This is commonly denoted as "high entropy" r-process
- ② Let us consider matter very high density matter with low entropies. Due to the high densities electrons have large fermi energies and will drive the composition very neutron rich. At some point the neutron drip line is reached and nuclei start to "drip" neutrons. This is the situation in the crust of neutron stars where densities are 10^{12-13} g cm⁻³ and $Y_e \leq 0.05$: $Y_n = 1 \langle A \rangle Y_e / \langle Z \rangle$, $Y_h = Y_e / \langle Z \rangle$; $n_s = Y_n / Y_h = \langle A \rangle [\langle Z \rangle / (Y_e \langle A \rangle) 1]$; $n_s \sim 500 2000$. This is commonly denoted as "low entropy" r-process.

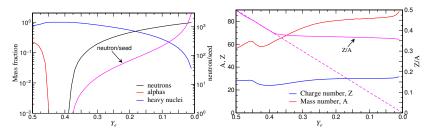
Dependence on Y_e



With reduced Y_e the peak of the nuclear abundance distribution moves from 56 Ni to heavier neutron rich nuclei. For low Y_e becomes energetically favourable to have free neutrons.

Abundances at 3 GK

Adiabatic expansions with s = 15



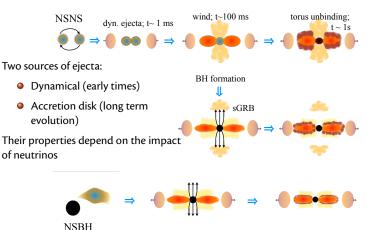
For neutron-rich moderate entropy ejecta ($s \sim 20$) ejecta we have:

$$n_s = A \left(\frac{Z}{A} \frac{1}{Y_e} - 1 \right)$$

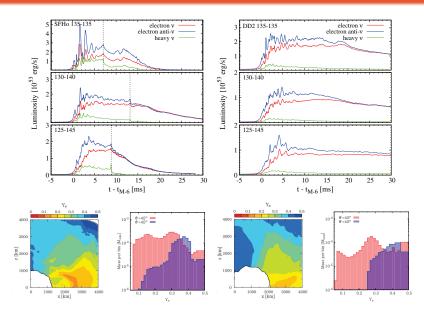
Calculation by Bowen Jiang

Merger channels and ejection mechanism

In mergers we deal with a variety of initial configurations (netron-star neutron-star vs neutron-star black-hole) with additional variations in the mass-ratio.



Impact of neutrinos on NS-NS mergers



Why is Y_e modified?

 Y_e is mainly determined by the competition between

$$v_e + n \rightleftharpoons p + e^-$$

 $\bar{v}_e + p \rightleftharpoons n + e^+$

The evolution of Y_e is given by:

$$\frac{dY_e}{dt} = \lambda_{\nu_e n} Y_n - \lambda_{\bar{\nu}_e p} Y_p = \lambda_{\nu_e n} - (\lambda_{\nu_e n} + \lambda_{\bar{\nu}_e p}) Y_e,$$

using $Y_e = Y_p$ and $Y_n = 1 - Y_n$. If matter is exposed long time enough to neutrino fluxes it will reach an equilibrium given by:

$$Y_e^{\text{eq}} = \frac{\lambda_{\nu_e n}}{\lambda_{\nu_e n} + \lambda_{\bar{\nu}_e p}}.$$

We need to estimate the neutrino absorption rates.

neutrino absorption rates on nucleons

If we assume that the produced electron (positron) is extremelly relativistic ($E_e = p_e c$) the cross section for (anti)neutrino absorption is:

$$\sigma(E_{\nu}) = \sigma_0(E_{\nu} \pm \Delta)^2$$

plus sign for neutrinos and minus sign for antineutrinos,

 $\Delta = m_n c^2 - m_p c^2 = 1.2933$ MeV, and

$$\sigma_0 = \frac{(1+3g_A^2)G_F^2 V_{ud}^2}{\pi \hbar^4 c^4} = 9.33(4) \times 10^{-44} \text{ cm}^2 \text{ MeV}^{-2}$$

For the absorption rate we need to integrate over the neutrino spectrum and multiply by the neutrino flux $(L_{\nu}/(4\pi r^2\langle E_{\nu}\rangle))$ obtaining:

$$\lambda_{\nu_e n} = \frac{L_{\nu_e}}{4\pi r^2} \sigma_0 \left(\varepsilon_{\nu_e} + 2\Delta + \frac{\Delta^2}{\langle E_{\nu_e} \rangle} \right)$$

$$\lambda_{\bar{\nu}_e p} = \frac{L_{\bar{\nu}_e}}{4\pi r^2} \sigma_0 \left(\varepsilon_{\bar{\nu}_e} - 2\Delta + \frac{\Delta^2}{\langle E_{\bar{\nu}_e} \rangle} \right)$$

with
$$\varepsilon_{\nu} = \langle E_{\nu}^2 \rangle / \langle E_{\nu} \rangle$$
.

Equilibrium Y_e

The equilibrium Y_e^{eq} can be expressed as:

$$Y_e^{\text{eq}} = \left[1 + \frac{L_{\bar{\nu}_e}}{L_{\nu_e}} \frac{\varepsilon_{\bar{\nu}_e} - 2\Delta + \Delta^2/\langle E_{\bar{\nu}_e} \rangle}{\varepsilon_{\nu_e} + 2\Delta + \Delta^2/\langle E_{\nu_e} \rangle}\right]^{-1}$$

In order to achieve $Y_e < 0.5$ we need:

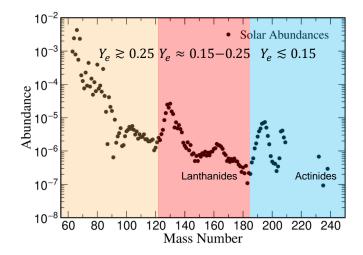
$$Y_e^{\text{eq}} = \frac{\lambda_{\nu_e n}}{\lambda_{\nu_e n} + \lambda_{\bar{\nu}_e p}} < 1/2 \Rightarrow \lambda_{\bar{\nu}_e p} > \lambda_{\nu_e n}$$

This can be translated to a condition on the average energies:

$$\varepsilon_{\bar{\nu}_e} - \varepsilon_{\nu_e} > 4\Delta - \left[\frac{L_{\bar{\nu}_e}}{L_{\nu_e}} - 1\right] \left[\varepsilon_{\bar{\nu}_e} - 2\Delta\right]$$

Dependence nucleosynthesis on Y_e

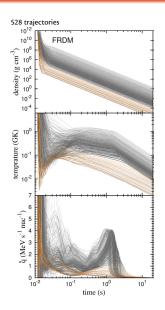
Nucleosynthesis depends on neutron richness of ejecta



The relevant nuclear physics depends on the particular conditions.

Nucleosynthesis low Y_e ejecta

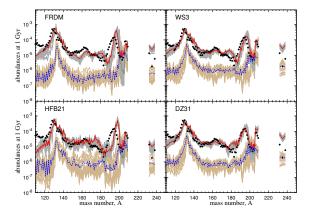
- r-process stars once electron fermi energy drops below $\sim 10~\text{MeV}$ to allow for beta-decays ($\rho \sim 10^{11}~\text{g cm}^{-3}$).
- Important role of nuclear energy production (mainly beta decay).
- Energy production increases temperature to values that allow for an $(n, \gamma) \rightleftharpoons (\gamma, n)$ equilibrium for most of the trajectories.
- Systematic uncertainties due to variations of astrophysical conditions and nuclear input



Mendoza-Temis, Wu, Langanke, GMP, Bauswein, Janka, PRC **92**, 055805 (2015)

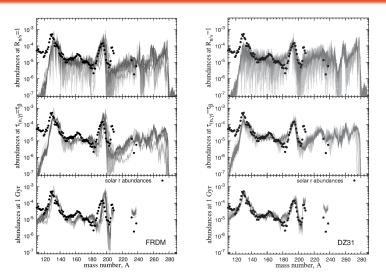
Final abundances different mass models

Mendoza-Temis, Wu, Langanke, GMP, Bauswein, Janka, PRC 92, 055805 (2015)



- Robustness astrophysical conditions, strong sensitivity to nuclear physics
- Second peak ($A \sim 130$) sensitive to fission yields.
- Third peak ($A \sim 195$) sensitive to masses (neutron captures) and beta-decay half-lives.

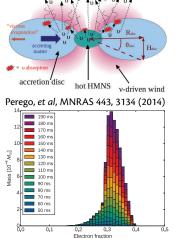
Temporal evolution (selected phases)



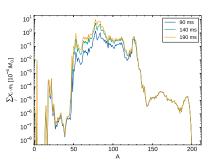
Fission is fundamental to determine the final r-process abundances.

Nucleosynthesis before BH formation

An Hypermassive neutron star produces large neutrino fluxes that drive the composition to moderate neutron rich ejecta.



Martin, et al, ApJ 813, 2 (2015)

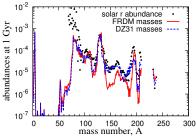


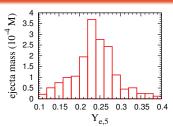
Only nuclei with A < 120 are produced (no lanthanides, blue kilonova).

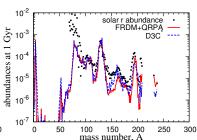
See also Lippuner et al, MNRAS 472, 904 (2017)

Nucleosynthesis after BH formation

- Accretion disk around BH ejects relatively neutron-rich matter [Fernández, Metzger, MNRAS 435, 502 (2013)]
- Produces all r-process nuclides (Lanthanide/Actinide rich ejecta)
 [Wu et al, MNRAS 463, 2323 (2016)]



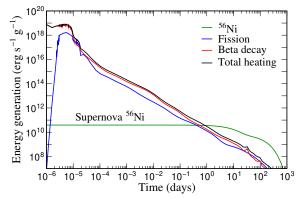




See also Just et al, MNRAS 448, 541 (2015), Siegel and Metzger PRL 119, 231102 (2017)

Energy production from r-process ejecta

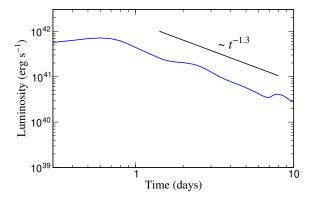
The decay of r process products produces energy following a power law $\varepsilon \sim t^{-1.3}$. Many nuclei decaying at the same time heating up the ejecta



We expect an electromagnetic transient with properties depending on:

- Energy production rate
- Efficiency energy is absorbed by gas (thermalization efficiency)
- Opacity gas (depends on composition, presence of lanthanides/actinides)

Kilonova: Electromagnetic signature of the r process



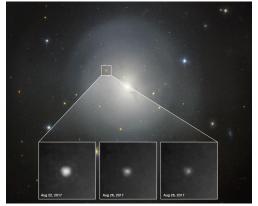
Luminosity equivalent to 1000 novas (kilonova) in timescales of days.

Depends on amount of ejected material, velocity and composition (opacity)

Metzger, GMP, Darbha, Quataert, Arcones et al, MNRAS 406, 2650 (2010)

AT 2017 gfo: electromagnetic signature from r process

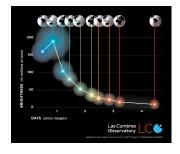
In-situ signature of r process nucleosynthesis

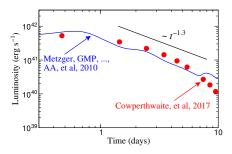


NASA and ESA. N. Tanvir (U. Leicester), A. Levan (U. Warwick), and A. Fruchter and O. Fox (STScI)

- Novel fastly evolving transitent
- Signature of statistical decay of fresly synthesized r process nuclei

AT 2017 gfo: interpretation

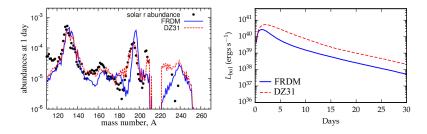




- Time evolution determined by the radioactive decay of r-process nuclei
- Two components:
 - blue dominated by light elements (Z < 50)
 - Red due to presence of Lanthanides (Z = 57-71) and/or Actinides (Z = 89-103)
- Likely source of heavy elements including Gold, Platinum and Uranium

Nuclear physics impact on light curve

Provided sufficiently neutron rich matter is ejected $Y_e \lesssim 0.15$ (merger neutron star black hole) a robust r process takes place

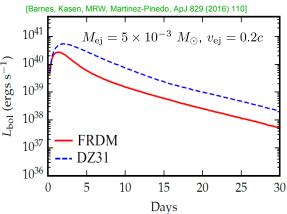


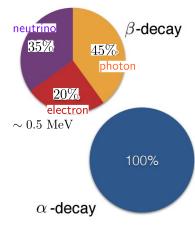
Luminosity is sensitive to abundances of long-lived actinides that release energy by alpha-decay.

Mendoza-Temis, Wu, Langanke, GMP, Bauswein, Janka, PRC **92**, 055805 (2015) Barnes, Kasen, Wu, GMP, ApJ **829**, 110 (2016); Rosswog et al, CQG **34**, 104001 (2017)

Nuclear physics inputs and the kilonova heating rate

– α & β particles thermalize in a similar way while $\gamma\text{-ray}$ thermalization quickly become inefficient





Produces substantially larger energy than beta-decay for similar half-live. Followed by a chain of several alpha decays

Relevant α -decays

Color code		e Hal	Half-life		Decay Mode			QEC	$Q_{\beta+}$	Sn	Sp	Qa		S _{2n}		S _{2p}	Q _{2β} -
Q _{β-n}		В	BE/A		(BE-LDM Fit)/A			t. E ₂₊	E ₃₋	E ₄₊ E	4+/E ₂₊	β2	B(E2) ₄	₂ /B(E2)	20 0	σ(n,γ)	σ(n,F)
z	212Ac	213Ac	214Ac	215Ac	216Ac	217Ac	218Ac	219Ac	220Ac		$ au_{lpha}=$			225Ac	226Ac	227Ac	228Ac
87	211Ra	21 2Ra	21 3Ra	214Ra	215Ra	216Ra	217Ra	218Ra			221Ra 11.4 (223104	224Ra	$ au_{lpha}^{ au_{lpha}}$	= 3.6	days
	210Fr	211Fr	212Fr	213Fr	214Fr	215Fr	216Fr	217Fr	218Fr	21 9F r	220Fr	221	222Ft	223Pr	224Fr	225Fr	226Fr
	209Rn	210Rn	211Rn	212Rn	21 3Rn	214Rn	215Rn	216Rn	217Rn	218Rn	219 P A	220R	221 R n	222Rn			days
85	208At	209At	210At	211At	212At	213At	214At	215At	216At	217	218A1	219At	220A	221 At	222At	223At	224At
	207Po	208Po	209Po	210Po	211Po	212Po	21.3Po	214Po	21595	\$16P	217Po	218	219Po	220Po	221Po	222Po	223Po
83	206Bi	207Bi	208Bi	209Bi	21001	21/Bi	31.2B	213	214Bi	215Bi	21671	217Bi	218Bi	219Bi	220Bi	221Bi	222Bi
	205Рь	206Рь	207РЬ	208	207 - 6	210T	211.Рь	1 2P	21 3Pb	214	215Pb	216Pb	217Pb	218Pb	219Pb	220Рь	
81	204Tl	205Tl	206Tl	207Tl	08TI	209Tl	210Tl	211Tl	21 2Tl	21 3Tl	214Tl	215Tl	216Tl	217Tl			
	123		125		127		129		131		133		135		137		N

Open questions

- Kilonova observations have already been used to constrain the dynamics and morphology of the ejecta.
- So far we have indirect evidence of the r process production. Can we find evidence of the production of particular elements?
- Can we at least constrain the nucleosynthesis relevant properties of the ejecta, e.g. Y_e ?
- What are the astrophysical and nuclear physics conditions relevant for the production of Lanthanides and Actinides?
- ...

Bibliography

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