



# Formation and evolution of primordial black hole binaries

---

VV and H. Veermäe, arXiv: 1908.09752  
M. Raidal, C. Spethmann, VV and H. Veermäe, arXiv: 1812.01930  
M. Raidal, VV and H. Veermäe, arXiv: 1707.01480

by  
Ville Vaskonen

# Outline

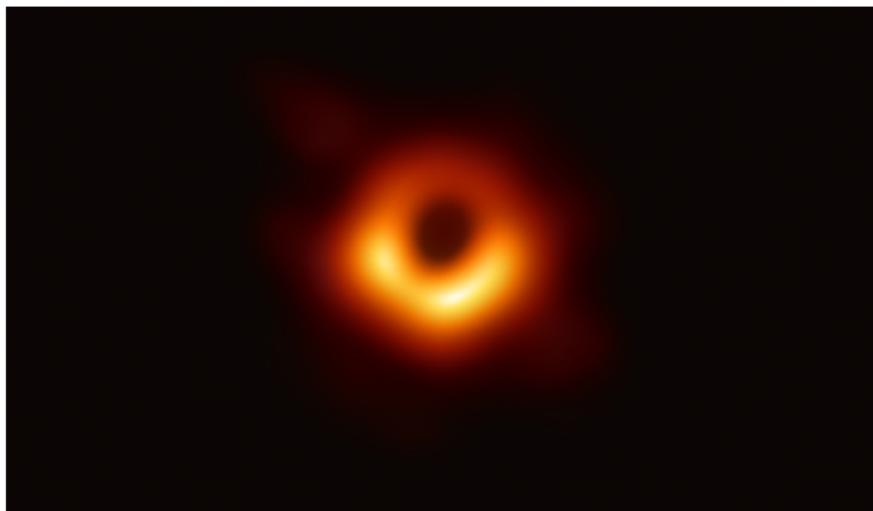
1. Introduction
2. PBH binary formation
3. Numerical simulations
4. Survival of the binaries
5. Constraints from LIGO/Virgo
6. Summary

# 1

## Introduction

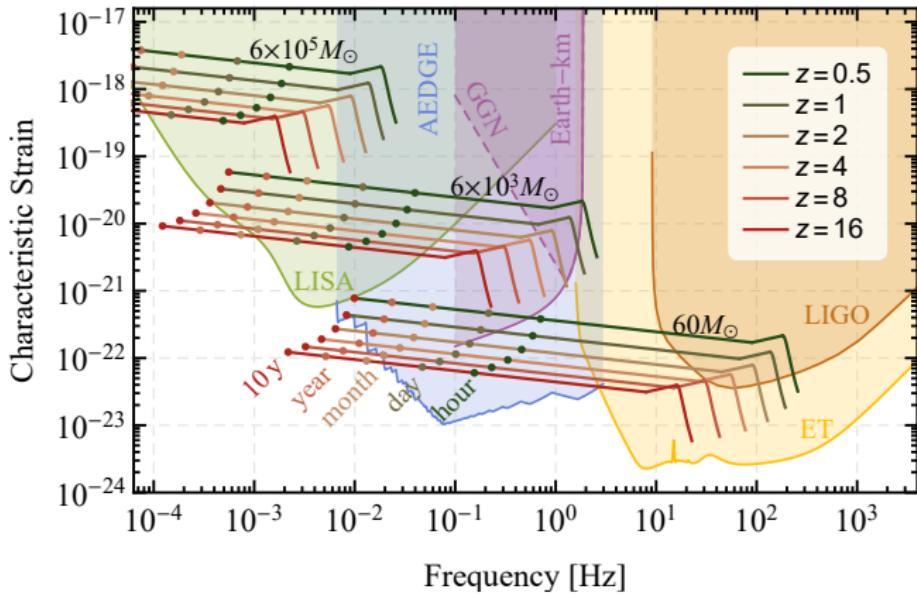
# Motivation

1. dark matter
2. supermassive black holes
3. LIGO-Virgo observations

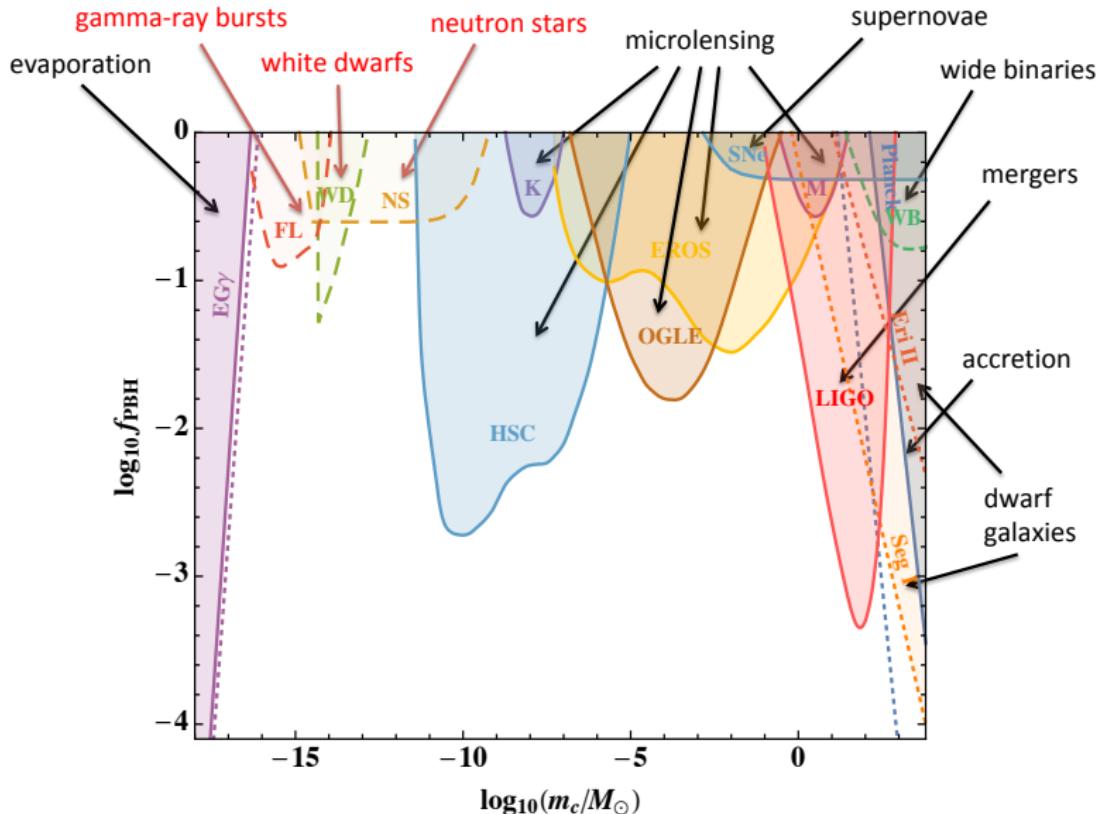


[Astrophys. J. 875 (2019) L1]

# Motivation



# PBH constraints



# Extended PBH mass function

- ▶ Constraints for extended mass functions:

[B. Carr, M. Raidal, T. Tenkanen, VV and H. Veermäe, arXiv: 1705.05567.]

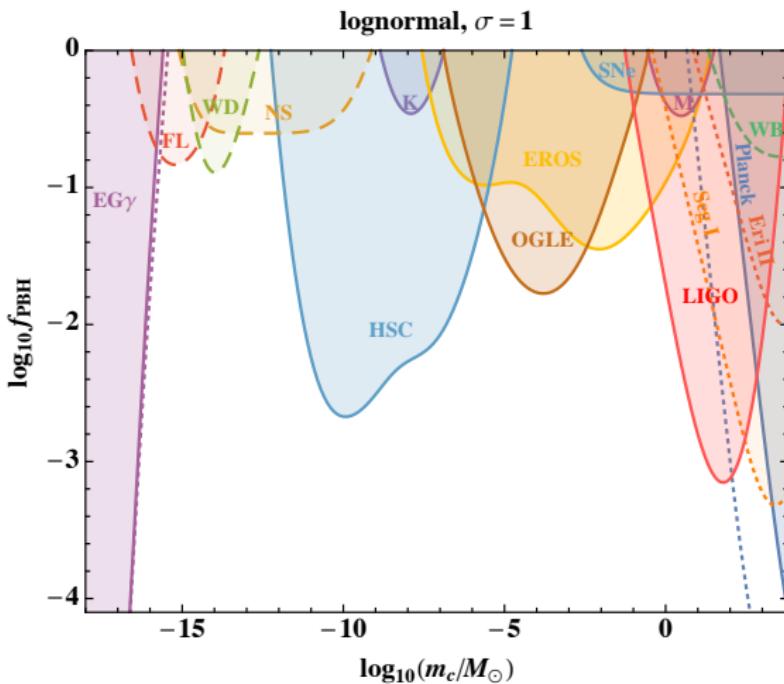
$$f_{\text{PBH}} \leq \left( \int dm \frac{\psi(m)}{f_{\max}(m)} \right)^{-1}.$$

- ▶ Lognormal mass function:

$$\psi(m) = \frac{1}{\sqrt{2\pi}\sigma m} \exp\left(-\frac{\log^2(m/m_c)}{2\sigma^2}\right),$$

$\log m_c$  and  $\sigma^2$  are the mean and variance of the  $\log m$  distribution.

# Constraints for lognormal $\psi$



Wider mass function  $\implies$  smaller maximal PBH abundance.

# PBH Formation

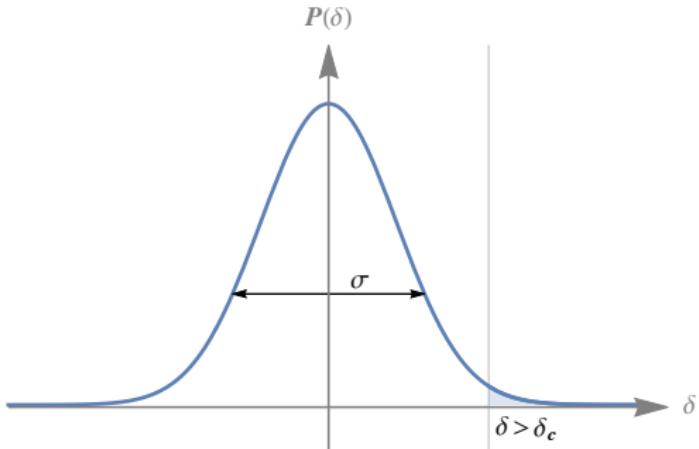
[B. Carr, *Astrophys. J.* 201, 1 (1975).]

- ▶ Large density perturbations collapse into BHs at horizon re-entry,

$$M \sim M_H .$$

- ▶ PBH abundance:

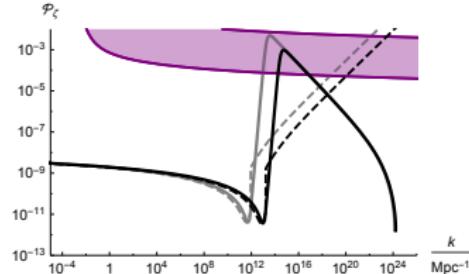
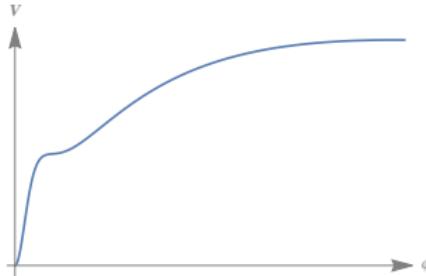
$$\frac{\rho}{\rho_{\text{tot}}} \sim \int_{\delta_c} d\delta P(\delta) .$$



# Examples

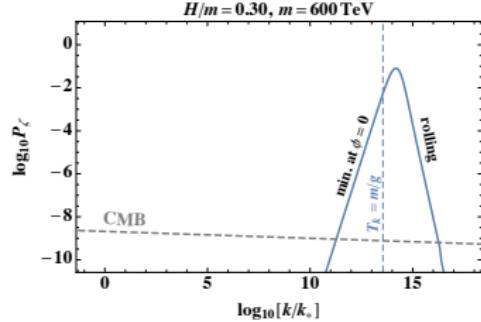
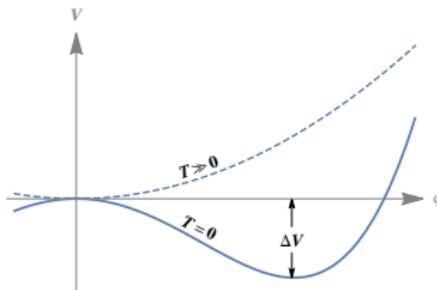
## ► Single field double inflation:

[K. Kannike, L. Marzola, M. Raidal and H. Veermäe, arXiv: 1705.06225]



## ► Thermal inflation:

[K. Dimopoulos, T. Markkanen, A. Racioppi and VV, arXiv: 1903.09598]

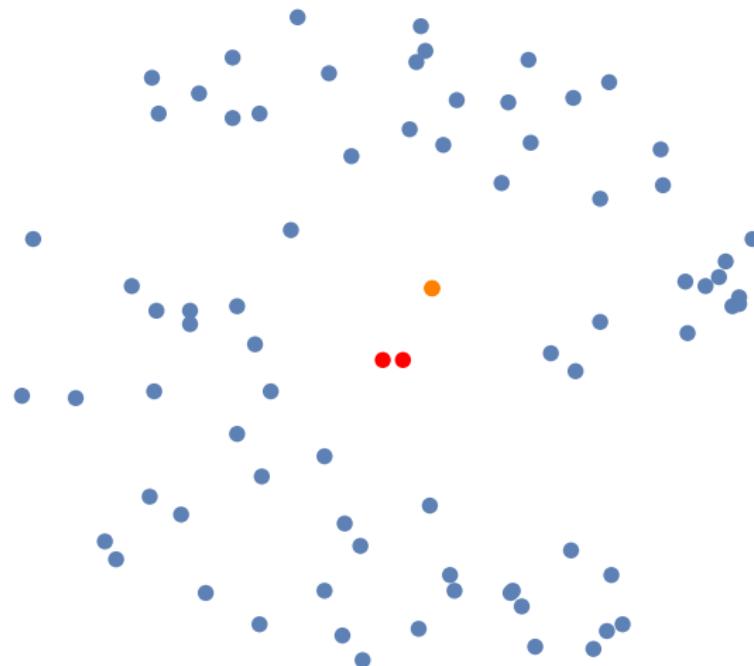


# 2

PBH binary formation

# Initial state

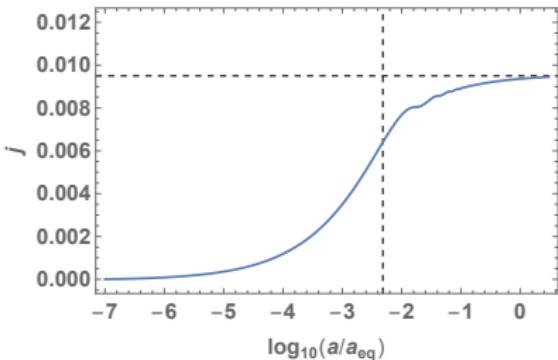
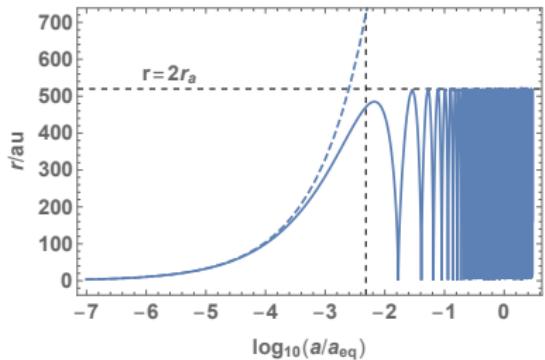
[T. Nakamura, M. Sasaki, T. Tanaka and K. S. Thorne, astro-ph/9708060.]



# Decoupling from expansion

$$\mathbf{F}/\mu = \underbrace{\hat{\mathbf{r}}\ddot{a}/a}_{\text{Hubble flow}} - \underbrace{M\hat{\mathbf{r}}/r^2}_{\text{self-gravity}} + \underbrace{(\hat{\mathbf{r}} \cdot \mathbf{T} \cdot \mathbf{r})\hat{\mathbf{r}}}_{\text{radial tidal forces}} + \underbrace{(\mathbf{r} \times (\mathbf{T} \cdot \mathbf{r})) \times (\hat{\mathbf{r}}/r)}_{\text{tidal torque}},$$

$$\mathbf{T}_{i,j} = \partial_i \partial_j \phi(\mathbf{r}_c)$$



# Coalescence time

- ▶ GW emission  $\implies$

[P. C. Peters, Phys. Rev. 136 B1224 (1964).]

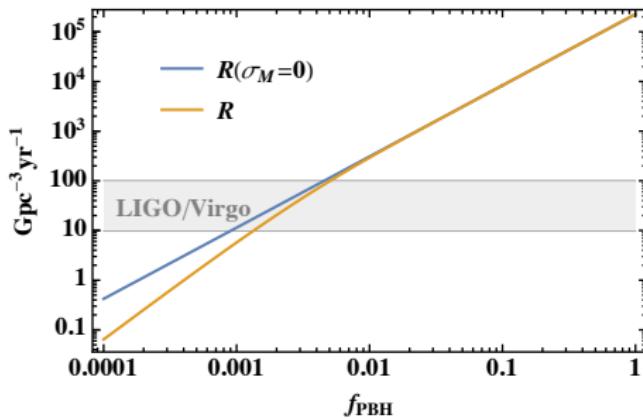
$$\tau = \frac{3}{85} \frac{r_a^4}{\eta M^3} j^7.$$

For example  $m_1 = m_2 = 10M_\odot$ ,  $j = 0.01$  and  $r_a = 260$  au gives  
 $\tau \simeq 10^{10}$  yr  $\simeq$  age of the universe.

- ▶ To get the merger rate we need
  - ▶ the PBH mass function,
  - ▶ the distribution of initial binary separation and
  - ▶ the distribution of tidal torques.

# Merger rate

- ▶ Torques from all PBHs and other matter inhomogeneities:  
[Y. Ali-Haïmoud, E. D. Kovetz and M. Kamionkowski, 1709.06576.]

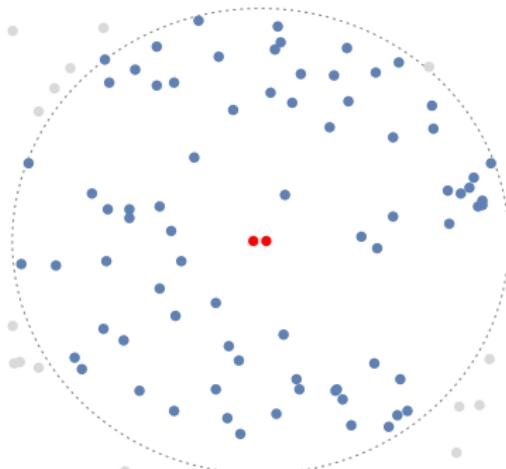


# 3

## Numerical simulations

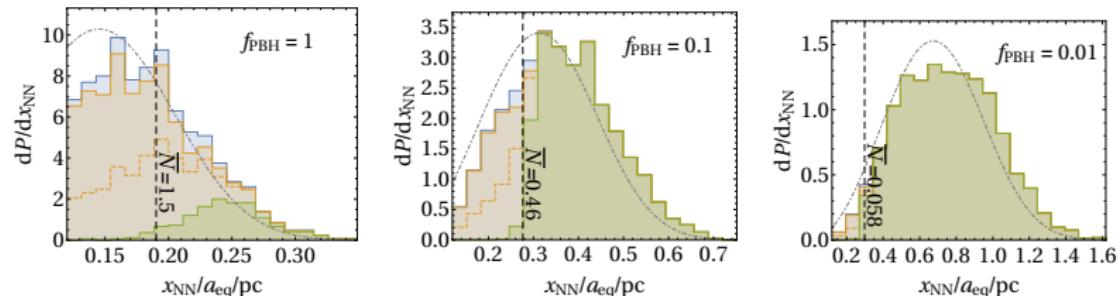
# N-body simulation

- ▶  $N - 2$  randomly distributed PBHs in a sphere.
- ▶ A central PBH pair that will form a binary with lifetime  $\tau = t_0$
- ▶ We simulated  $N = 70$  bodies from  $a_{\text{beg}} = 10^{-3}a_{\text{eq}}$  to  $a_{\text{end}} = 3a_{\text{eq}}$ .
- ▶ The expansion of the universe is accounted by including a Hubble acceleration,  $\ddot{r} = \ddot{a}r/a$ .
- ▶ The gravitational attraction of PBHs outside the sphere is approximated by a uniform mass density.



# Disruption of the binaries

$x_{NN}$  = the initial comoving distance of the PBH nearest to the binary.  
 $z_{\text{end}} \simeq 1000$ :



1. If the initial configuration contains a third PBH close to the PBH pair that is expected to form a binary, it is very likely that it collides with the binary.
2. PBHs will form dense clusters relatively early, and binaries absorbed by these clusters are likely to be disrupted.

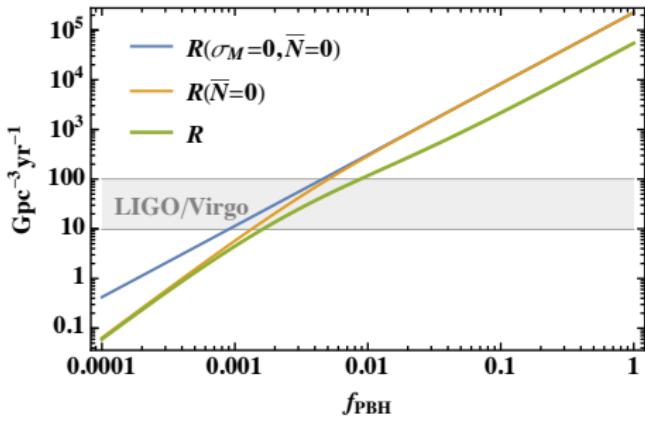
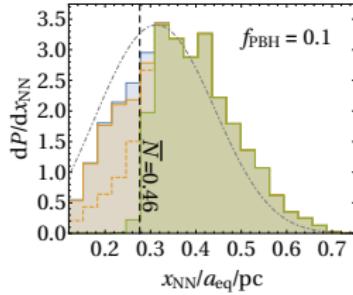
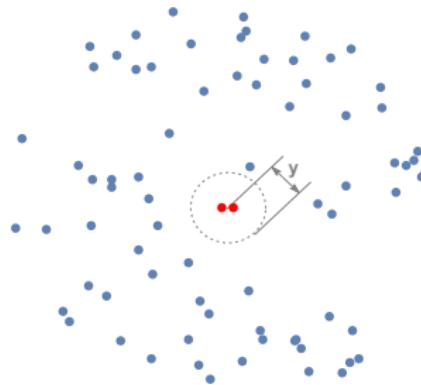
# 4

## Survival of the binaries

# Disruption by the nearest PBH

To avoid disruption by the PBH nearest to the binary, we require that the average number of PBHs inside a sphere of radius  $y$  is

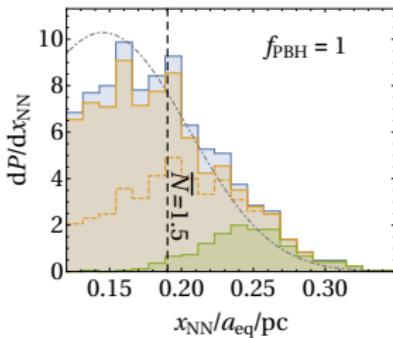
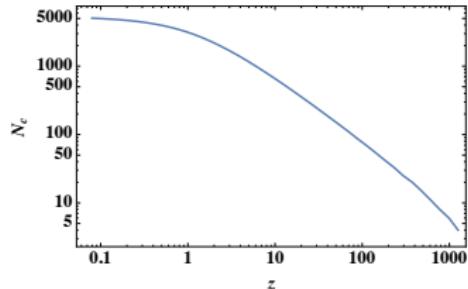
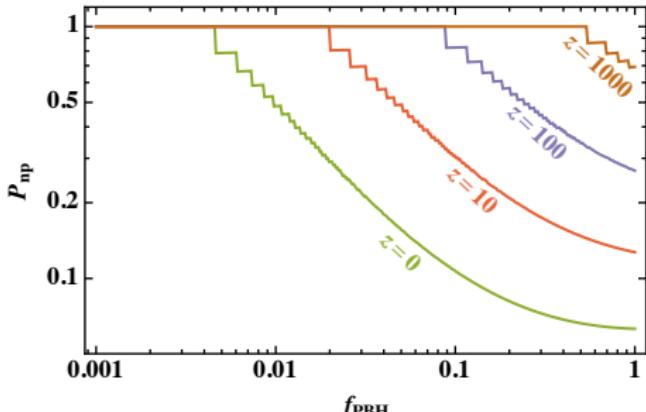
$$\bar{N}(y) \simeq \frac{M}{\langle m \rangle} \frac{f_{\text{PBH}}}{f_{\text{PBH}} + \sigma_M}.$$



# Disruption in a cluster

- ▶ Halos with  $N < N_c(z)$  PBHs have collapsed before redshift  $z$ .
- ▶ All binaries in clusters that collapse are disrupted  $\implies$  survival probability

$$P_{\text{np}}(z) = \sum_{N=N_c(z)}^{\infty} P_N .$$



# Contribution of the perturbed binaries

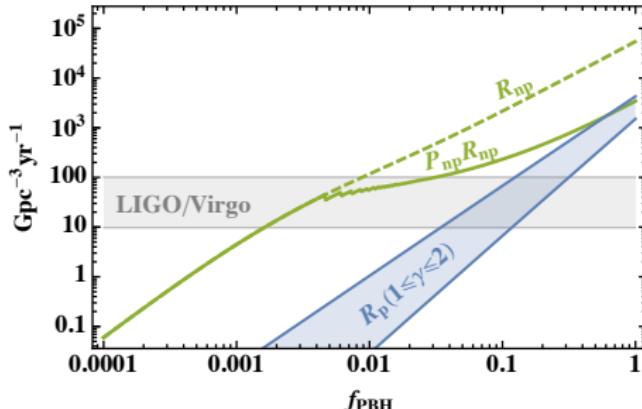
Binary-PBH interactions increases

- ▶ the binding energy  $E$  of the binary by  $\mathcal{O}(1)$  factor,
- ▶ the angular momentum  $j$  of the binary by  $\mathcal{O}(10)$  factor.

$$\tau = \frac{3}{1360} \frac{M}{\eta E^4} j^7.$$

⇒  $\tau$  increases by several orders of magnitude.

⇒ Disrupted binaries that initially had a very short lifetime can contribute to the present merger rate.



# 5

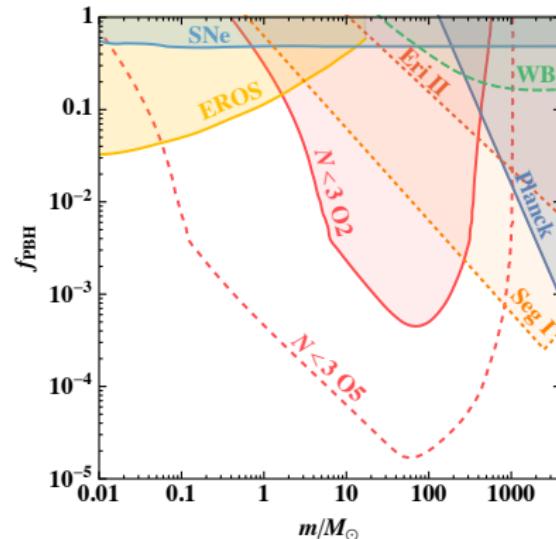
Constraints from LIGO/Virgo observations

# No PBHs

- ▶ Expected number of events:

$$N = \Delta t \int dR(m_1, m_2, z) dV_c(z) \theta(\rho(m_1, m_2, z) - \rho_c).$$

- ▶ Assume Poisson statistics:  $N < 3$ .

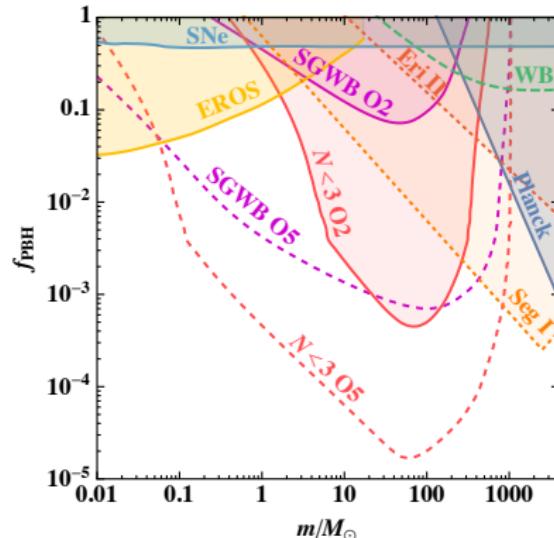


# No SGWB

- ▶ Expected stochastic GW background:

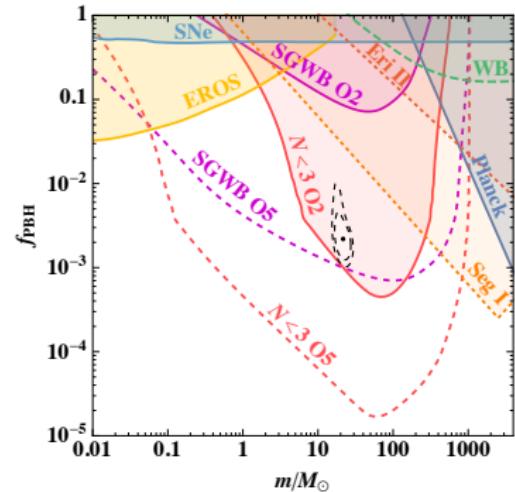
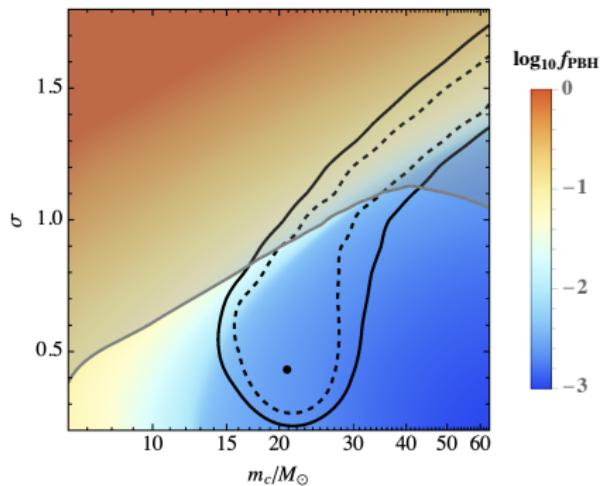
$$\Omega_{\text{GW}}(\nu) = \frac{\nu}{\rho_c} \int \frac{dR(m_1, m_2, z) dz}{(1+z)H(z)} \frac{dE_{\text{GW}}(\nu_r)}{d\nu} \theta(\rho_c - \rho(m_1, m_2, z)),$$

- ▶ Require that SNR<8:



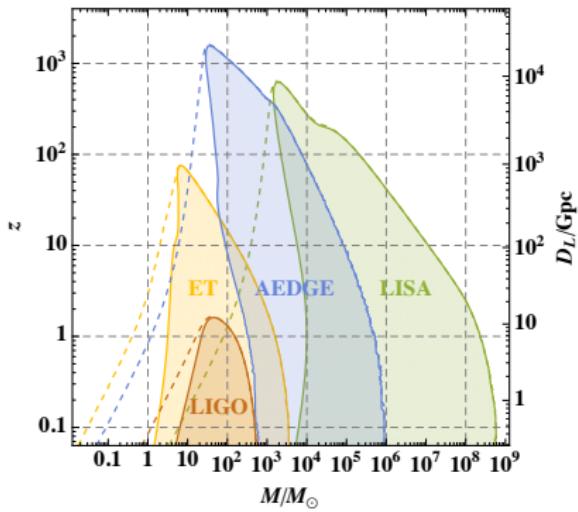
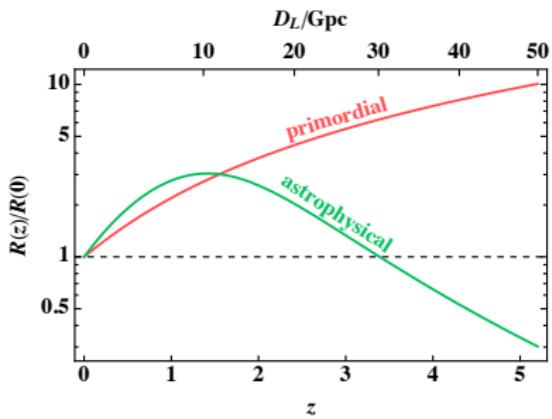
# Fit for lognormal mass function

- ▶  $N_{\text{obs}} = 10$  BH-BH merger events in  $\Delta t \simeq 165$  days.
- ▶ A likelihood fit for the masses and event rate:  
 $m_c \simeq 20M_\odot$ ,  $\sigma \simeq 0.4$ ,  $f_{\text{PBH}} \simeq 0.002$ .



# Separating PBBHs from ABBHs

Different behaviour of the merger rates as a function of  $z$  allows us to separate the primordial and astrophysical origins of the events:



# 6

## Summary

# Summary

- ▶ A population of PBH binaries is formed before matter-radiation equality from large Poisson fluctuations.
- ▶ Many of these binaries are disrupted by a nearby PBH or a small cluster of PBHs.
- ▶ The present merger rate for  $f_{\text{PBH}} \simeq 1$  still is well above the observed one.
- ▶ LIGO/Virgo observations give the strongest constraint on  $f_{\text{PBH}}$  in the mass range  $2 - 120M_{\odot}$ .
- ▶ Future GW experiments can tell the origin of the observed BH binary population.