Gravitational Waves: I. The Stochastic Background and its Anisotropies II. A test for Gravitational Theories





- Stochastic gravitational-wave background (SGWB)
- GWs \rightarrow info about population of compact binaries
- GWs \rightarrow info about beyond Standard Model
- Anisotropies in the SGWB \rightarrow info about large-scale-structure (LSS)
- GWs \rightarrow test general relativity (GR) and modified gravity models
- GWs \rightarrow test quantum gravity (QG) models







BBH events from O1 and O2



O1 and O2 BBHs events

LIGO and Virgo have detected 10 GW signals from binary black hole (BBH) mergers and 1 from a binary neutron star (BNS) merger

Abbott et al, Phys. Rev. Lett. 120, 091101 (2018)





Astrophysical phenomena: supernova explosions or final merging of compact binary objects (NS-NS, BH-BH, BH-NS) can liberate a large amount of energy (up to a few per cent of its total mass) in GWs in a very short time (less than 1 sec, or as small as few milliseconds)



GW bursts

 ${\mathcal T}_g\,$: duration of GW bursts



In Fourier space, a GW burst has a continuum spectrum of frequency over a broad range, up to a maximum frequency $f_{
m max} \sim 1/ au_{
m g}$









Stochastic GW Background (SGWB)



Penzias and Wilson (1965) : Universe is permeated by the CMB electromagnetic radiation





The Universe is permeated also by a SGWB

It emerges from the incoherent superposition of a large number of sources, too weak to be detected separately, and such that the number of sources that contribute to each frequency bin is much larger than one



Produced by a superposition of many weak, independent and unresolved sources of astrophysical or cosmological origin



Supernovae



Neutron stars



Binaries



Inflation







Cosmological phase transitions



LIGO

SGWB from CBCs

GW150914	GW3531012	GW151226	GW170104	GW170608
	÷.,	1		•*
GW176729	GW170609	GW170814	GW170618	GW170823

Abbott et al, Phys. Rev. Lett. 120, 091101 (2018)

Approximately one **binary neutron star merger** every **13 seconds** and one **binary black hole merger** every **223 seconds**

but

most of these events are too faint to be individually detected







SGWB from CBCs



$$\Omega_{\rm gw}(\nu) = \frac{1}{
ho_{\rm c}} \; \frac{d
ho_{\rm gw}(\nu)}{d\ln\nu}$$

Abbott et al, Phys. Rev. Lett. 120, 091101 (2018)

$$\nu_{\rm s} = (1+z)\nu$$

$$\Omega_{\rm GW}(\nu,\theta) = \frac{\nu}{\rho_{\rm c}H_0} \int_0^{z_{\rm max}} dz \frac{R_{\rm m}(z;\theta) \frac{dE_{\rm GW}(\nu_{\rm s};\theta)}{d\nu_{\rm s}}}{(1+z)E(\Omega_{\rm M},\Omega_{\Lambda},z)}$$

$$\Omega_M = 1 - \Omega_{\Lambda} = 0.3065 \qquad E(\Omega_{\rm M},\Omega_{\Lambda},z) = \sqrt{\Omega_{\rm M}(1+z)^3 + \Omega_{\Lambda}}$$

High merging rate and large masses of observed systems implies strong SGWB





input from LIGO/Virgo:

- Iocal rate
- mass distribution

 $p(m_1) \propto m_1^{-lpha_m}$ $p(m_2) = ext{uniform}$ $m_{ ext{min}} \leq m_2 \leq m_1 \leq m_{ ext{max}}$

$$m_{\rm min} = 5M_{\odot}$$

 $m_1 + m_2 \leq 200 M_{\odot}$

Beta distribution for the BH spins

$$p(\chi_i) \propto \chi_i^{\alpha_{\chi}-1} (1-\chi_i)^{\beta_{\chi}-1}$$

 $\begin{array}{c} & & \\ & \alpha_m & \\ & m_{\max} & \\ & \alpha_\chi, \beta_\chi \end{array} \end{array} \Big] infrerred from \\ observed BBHs \\ \end{array}$







The total energy density varies over nearly two orders of magnitude



Jenkins, O'Shaughnessy, Sakellariadou, Wysocki, PRL 122, 111101 (2019)





1dim topological defects formed in the early universe as a result of a PT followed by SSB, characterised by a vacuum manifold with non-contractible closed curves

Kibble (1976)

Generically formed in the context of GUTs



Jeannerot, Rocher, Sakellariadou, PRD68 (2003) 103514

$$G\mu \sim \left(rac{\Lambda_{\rm NP}}{M_{\rm PI}}
ight)^2$$

CS loops (length ℓ) oscillate periodically ($T=\ell/2$) in time emitting GWs (fundamental frequency $~~\omega=4\pi/\ell$)

$$\tau = \frac{\ell}{\gamma_{\rm d}} \qquad \qquad \gamma_{\rm d} \equiv \Gamma G \mu \\ \Gamma \simeq 50$$





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Jeannerot, Rocher, Sakellariadou, PRD68 (2003) 103514



GW in a highly concentrated beam

$$\theta_{\rm b} \approx \left(\frac{4}{\sqrt{3}\nu_{\rm s}l}\right)^{1/3}$$

GW is isotropic



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Cusps: GW amplitude scales as $\omega^{-4/3}$ Kinks: GW amplitude scales as $\omega^{-5/3}$ Kink-kink collision: GW amplitude scales as ω^{-2} $N_{\rm kk} = \frac{N_{\rm k}^2}{4}$

Damour, Vilenkin (2001)





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Jeannerot, Rocher, Sakellariadou, PRD68 (2003) 103514

$$\overline{\Omega}_{gw} = \frac{2(G\mu)^2}{3\pi^2 H_o^2 \nu_o} \int_0^{t_*} \frac{\mathrm{d}t}{t^4} a^5 \int_0^{\gamma_*} \frac{\mathrm{d}\gamma}{\gamma} \overline{\mathcal{F}} \Theta\left(\gamma - \frac{2a}{\nu_o t}\right) \left[N_\mathrm{k}^2 + 4AN_\mathrm{k} \left(\frac{\nu_o \gamma t}{a}\right)^{1/3} + A^2 N_\mathrm{c} \left(\frac{\nu_o \gamma t}{a}\right)^{2/3} \right]$$
$$\gamma \equiv \frac{\ell}{t} \qquad \mathcal{F}(\gamma) \equiv t^4 n(t, \ell)$$

Model 1: old (obsolete model) Model 2: Blanco-Pillado, Olum, Shlaer, PRD (2014) Model 3: Lorenz, Ringeval, Sakellariadou, JCAP1010 (2010) Ringeval, Sakellariadou, Bouchet, JCAP0702 (2007)





1dim topological defects formed in the early universe as a result of a PT followed by SSB, characterised by a vacuum manifold with non-contractible closed curves

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Jeannerot, Rocher, Sakellariadou, PRD68 (2003) 103514





To first approximation, the SGWB is assumed to be isotropic (analogous to CMB)

It would appear as **noise** in a single GW detector

$$s(t) = n(t) + h(t)$$

Signal from Noise GW strain the detector



To detect a SGWB take the correlation between two detector outputs:

$$(s_1(t) \ s_2(t)) = \langle (n_1(t) + h(t)) \ (n_2(t) + h(t)) \rangle$$

= $\langle n_1(t) \ n_2(t) \rangle + \langle n_1(t) \ h(t) \rangle + \langle h(t) \ n_2(t) \rangle + \langle h(t) \ h(t) \rangle$
 $\approx (h(t) \ h(t))$



Correlation methods between two or more interferometric detectors

Root mean square of the
$$h_{rms}^2 = \left\langle \sum_{i,j} h_{ij} h_{ij} \right\rangle = \int_0^\infty d\nu S_h(\nu)$$
 One-strain strain spect

One-sided GW strain power spectral density

$$\sqrt{S_h(
u)} = 2
u^{1/2}|\tilde{h}(
u)|$$

$$\rho_{\rm gw} = \int_0^\infty d\nu S_h(\nu) \frac{\pi c^2 \nu^2}{8G}$$





Stationary, Gaussian, unpolarised, and isotropic stochastic background







$$\Omega_{\rm GW}(\nu) = \Omega_{\rm ref} \left(\frac{\nu}{\nu_{\rm ref}}\right)^{lpha}$$
 $lpha=2/3$

$$\nu_{\rm ref} = 25 {\rm Hz}$$



$$\Omega_{\rm GW} < 4.8 \times 10^{-8}$$
 at 25 Hz

LVC, arXiv:1903.02886

4G0





$$\Omega_{\rm GW}(\nu) = \Omega_{\rm ref} \left(\frac{\nu}{\nu_{\rm ref}}\right)^{\alpha} \quad \alpha=0$$
 $\nu_{\rm ref} = 25 {\rm Hz}$

$$\Omega\!<\!7.9\!\times10^{-9}~{\rm at}~25~{\rm Hz}$$

$$G\mu/c^2 \le 1.1 imes 10^{-6}$$
 For the CS model of Blanco-Pillado, Olum, Shlaer (2014) $G\mu/c^2 \le 1.6 imes 10^{-11}$ Pulsar timing limit Lasky et al (2016)

 $G\mu/c^2 \leq 2.1 \times 10^{-14}$ For the CS model of Lorenz, Ringeval, Sakellariadou, JCAP 1010 (2010) 003 Ringeval, Sakellariadou, Bouchet, JCAP 1712 (2007) 027 $G\mu/c^2 \leq 6.2 \times 10^{-12}$ Pulsar timing limit

LVC, arXiv:1903.02886





To a first approximation, the SGWB is assumed to be isotropic (analogous to the CMB)



The afterglow radiation left over from the Hot Big Bang

- its temperature is extremely uniform all over the sky
- tiny temperature fluctuations (one part 100,000)

$$C_{\ell} = \int \mathrm{d}^2 \hat{\boldsymbol{n}} P_{\ell}(\cos \theta) \left\langle \delta T_{\gamma} \delta T_{\gamma} \right\rangle$$

Similar to the CMB, there are signal searches that attempt to measure an anisotropic SGWB

$$C_{\ell} = \int \mathrm{d}^2 \hat{\boldsymbol{n}} P_{\ell}(\cos \theta) \left\langle \delta \Omega_{\mathsf{gw}} \delta \Omega_{\mathsf{gw}} \right\rangle$$

An anisotropic SGWB was not observed with the aLIGO O1/O2 data; upper limits were set

Abbott et al, arXiv:1903.08844





Gravitational wave sources with an anisotropic spatial distribution lead to a SGWB characterised by preferred directions, and hence anisotropies

Search for anisotropies

for extended sources: spherical harmonic decomposition

$$C_{\ell} = \int d^2 \hat{\boldsymbol{n}} P_{\ell}(\cos \theta) \left\langle \delta \Omega_{\mathsf{gw}} \delta \Omega_{\mathsf{gw}} \right\rangle$$

- for point sources: broadband radiometer analysis $\Omega_{lpha}(\Theta) < (0.19 2.89) imes 10^{-8}
 m sr^{-1}$
- in the direction of interesting objects in the sky (galactic centre, Scorpius X-1, SN 1987A): narrowband radiometer search

$$h_0 < (3.6 - 4.7) \times 10^{-25}$$

An anisotropic stochastic background was not observed with the Advanced LIGO O1/O2 data, but important upper limits were set

Abbott et al, arXiv:1903.08844

 $[1/2 \ [sr^{-1}]$



$$\Omega_{\mathsf{gw}} = \frac{\pi \nu_{\mathsf{o}}^3}{3H_{\mathsf{o}}^2} \int_0^{\eta_*} \mathrm{d}\eta \, a^2 \int \mathrm{d}\zeta \, \bar{n}R(1 + \delta_n + \hat{\boldsymbol{e}}_{\mathsf{o}} \cdot \boldsymbol{v}_{\mathsf{o}}) \int_{S^2} \mathrm{d}^2\sigma_{\mathsf{s}} \, r_{\mathsf{s}}^2 \tilde{h}^2$$

$$\Lambda_* = \frac{4\pi}{\nu_o} \int \mathrm{d}\zeta \int_{\eta_*}^{\eta_o} \mathrm{d}\eta \, a^3 (\eta_o - \eta)^2 f_o \bar{n} H$$

 $\Lambda << 1$: foreground $\Lambda >> 1$: SWGB

Duty cycle: the average number of overlapping signals at experienced by the observer

Jenkins, Sakellariadou, PRD 98, 063509 (2018)





$$\Omega_{gw} = \frac{\pi \nu_o^3}{3H_o^2} \int_0^{\eta_*} \mathrm{d}\eta \, a^2 \int \mathrm{d}\zeta \, \bar{n}R(1 + \delta_n + \hat{\boldsymbol{e}}_o \cdot \boldsymbol{v}_o) \int_{S^2} \mathrm{d}^2\sigma_s \, r_s^2 \tilde{h}^2$$

Anisotropy due to source density contrast $\delta_n \equiv \frac{n-\bar{n}}{\bar{n}}$

Intensity of SGWB:

 $C_{\rm gw}(\theta_{\rm o}, t)$

$$\Omega_{\rm gw}(\nu_{\rm o}, \hat{\boldsymbol{e}}_{\rm o}) \equiv \bar{\Omega}_{\rm gw}(1 + \delta_{\rm gw})$$

 $\delta_{\rm gw} = \delta_{\rm gw}^{\rm (s)} + \mathcal{D}\,\hat{e}_{\rm o}\cdot\hat{v}_{\rm o}$

$$C_{\rm gw}(\theta_{\rm o},\nu_{\rm o}) \equiv \left\langle \delta_{\rm gw}^{\rm (s)}(\nu_{\rm o},\hat{\boldsymbol{e}}_{\rm o})\delta_{\rm gw}^{\rm (s)}(\nu_{\rm o},\hat{\boldsymbol{e}}_{\rm o}')\right\rangle$$

$$\nu_{\rm o}) = \sum_{l=0}^{\infty} \frac{2l+1}{4\pi} C_l(\nu_{\rm o}) P_l(\cos\theta_{\rm o}), \quad \theta_{\rm o} \equiv \cos^{-1}(\hat{e}_{\rm o} \cdot \hat{e}_{\rm o}')$$

Jenkins, Sakellariadou, PRD 98, 063509 (2018)







 $C_1^{1/2} \approx 10^{-10} \ {\rm sr}^{-1}$



Jenkins, Sakellariadou, PRD 98, 063509 (2018)



Anisotropies in the SGWB from cosmic strings



King's London



Magnified $10^{\circ} \times 10^{\circ}$ regions



Angular resolution of about 50 arcseconds



The observer's motion relative to the cosmic rest frame induces a kinematic dipole

Jenkins, Sakellariadou, PRD 98, 063509 (2018)





Consider an FLRW spacetime and neglect cosmological perturbations, keeping only anisotropy due to the source density contrast and the one induced by the peculiar motion of the observer

Star formation rate (SFR) of galaxies \longrightarrow population of CBOs \longrightarrow rate of mergers The formation of massive black holes from stars is inhibited by stellar winds in Metallicity of galaxies high-metallicity environments Masses m_1, m_2 & spin angular momentum S_1 , S_2 of two binaries $\chi_1 \equiv \frac{S_1}{m_1^2}, \qquad \chi_2 \equiv \frac{S_2}{m_2^2}, \qquad \chi_1, \chi_2 \in [-1, +1],$ Mergers: BHBH, NSNS, BHNS $p_{\rm BNS} \propto \delta(\chi_1) \delta(\chi_2),$ $1M_{\odot} \le m_1 \le 2M_{\odot}, \qquad \qquad 1M_{\odot} \le m_2 \le 2M_{\odot},$ $p_{\rm BBH} \propto m_1^{-2.35}/(m_1 - 5M_{\odot}),$ $5M_{\odot} \leq m_2 \leq m_1 \leq 95M_{\odot},$ $m_1 + m_2 < 100 M_{\odot}$ $1M_{\odot} \leq m_2 \leq 2M_{\odot},$ $p_{\rm BHNS} \propto m_1^{-2.35} \delta(\chi_2),$ $5M_{\odot} \leq m_1 \leq 95M_{\odot},$



The fiducial LVC astrophysical model



Jenkins, Regimbau, Sakellariadou, Slezak, PRD 98, 063501 (2018)

analytic estimates:

Use simple analytical functions for the galaxy density \bar{n} and the galaxy-galaxy 2PCF $\langle \delta_n \delta_n \rangle$

$$\langle \delta_n \delta_n \rangle \approx \left(\frac{d}{d_1}\right)^{-\gamma} \delta(z-z'),$$

 $d(z, \hat{e}_{o}, \hat{e}'_{o})$: comoving distance

$$d_1 = (4.29 \pm 0.19)h^{-1}$$
Mpc

$$\gamma = 1.63 \pm 0.04$$

Marulli, et al (2013)

using mock galaxy catalogues *Millenium mock galaxy catalogue*

• N-body simulation of LSS formation through DM clustering

Springel, et al (2005) ; Blaizot, et al (2005) ; Lemson, et al (2006)

• Galaxies added to DM haloes with sophisticated semi-analytic models

De Lucia, Blaizot (2007)

• Light-cone constructed to mimic real galaxy catalog z < 0.78 (cut-off in apparent magnitude)





Jenkins, Regimbau, Sakellariadou, Slezak, PRD 98, 063501 (2018)

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$$d_1 = (4.29 \pm 0.19)h^{-1}$$
Mpc
 $\gamma = 1.63 \pm 0.04$

Marulli, et al (2013)

- using mock galaxy catalogues Millenium mock galaxy catalogue
- o get galaxies from simulation
- o calculate the rate of mergers for each galaxy
- superimpose in order to get a SGWB map







Jenkins, Regimbau, Sakellariadou, Slezak, PRD 98, 063501 (2018)

analytic estimates:

Use simple analytical functions for the galaxy density \bar{n} and the galaxy-galaxy 2PCF $\langle \delta_n \delta_n \rangle$

$$\langle \delta_n \delta_n \rangle \approx \left(\frac{d}{d_1}\right)^{-\gamma} \delta(z-z'),$$

 $d(z, \hat{e}_{o}, \hat{e}'_{o})$: comoving distance

$$d_1 = (4.29 \pm 0.19)h^{-1}$$
Mpc $\gamma = 1.63 \pm 0.04$

Marulli, et al (2013)

• using mock galaxy catalogues *Millenium mock galaxy catalogue* Now we have an explicit expression for Ω_{gw} as a function of sky location

Anisotropies in the Astrophysical Stochastic GW Background (ASGWB)



Most important quantities describing each BBH are the masses and spins of each component BH

Use Bayesian techniques to infer them from GW observations

Truncated power-law BH mass distribution:

Beta distribution for the BH spins:
$$\alpha_m$$
 $p(\chi_i) \propto \chi_i^{\alpha_{\chi}-1} (1-\chi_i)^{\beta_{\chi}-1}$ m_{\max} m_{χ}, β_{χ} infrerred from

Wysocki, Lange, O'Shaughnessy (2018)





Inferring BBH population parameters



Inferring BBH population parameters



 The anisotropies are insensitive to the details of the BBH population; the anisotropy parameter varies by O(1) factor between all the BBH distributions





Jenkins, O'Shaughnessy, Sakellariadou, Wysocki, PRL 122, 111101 (2019)

4G0

Gauge invariant formalism to compute the astrophysical GW spectrum, taking into account all effects intervening between the source and the observer

- events with short emission (merging binaries, SN explosions)
- inspiraling binaries which have not merged during a Hubble time

Bertaca, Ricciardone, Bellomo, Jenkins, Matarese, Raccanelli, Regimbau, Sakellariadou (in progress)







Can we probe LSS with astrophysical SGWB anisotropies?







Finite number of CBC's per observational time *temporal* **shot noise** (scale-invariant bias term)

$$egin{aligned} \mathcal{C}_\ell o \mathcal{C}_\ell + \mathcal{W} & \mathcal{W} \gg \mathcal{C}_\ell & \mathcal{W} & \propto rac{1}{T_{
m obs}} \end{aligned}$$

Finite number of CBCs and very short time within LIGO/Virgo frequency band

angular power spectrum dominated by shot noise



without shot noise

 $\mathcal{W} = 10^{-3} \bar{\Omega}^2$

- finite number of galaxies (*spatial shot noise*) +
- cosmic variance

Jenkins, Sakellariadou, PRD (2019)







Finite number of CBC's per observational time temporal shot noise (scale-invariant bias term)

$$egin{aligned} \mathcal{C}_\ell o \mathcal{C}_\ell + \mathcal{W} & \mathcal{W} \gg \mathcal{C}_\ell & \mathcal{W} & \propto rac{1}{T_{
m obs}} \end{aligned}$$

Finite number of CBCs and very short time within LIGO/Virgo frequency band

angular power spectrum dominated by shot noise

Exploit statistical independence of different shot noise realisations at different times

Cross-correlate different time segments to build a (new) minimum-variance unbiased estimator

$$\hat{C}_{\ell}^{\mathsf{new}} \equiv rac{1}{N_{\mathsf{pairs}}}\sum_{\mu
eq
u}^{N_{\mathsf{pairs}}} rac{1}{2\ell+1}\sum_{m=-\ell}^{+\ell} arOmega_{\ell m}^{\mu} arOmega_{\ell m}^{
u*}$$



$$extsf{/ar}[\hat{C}^{ extsf{new}}_\ell] = rac{2}{2\ell+1}(C_\ell+\mathcal{W})^2$$

Jenkins, Romano, Sakellariadou, arXiv:1907.06642





Can we probe LSS with ASGWB anisotropies?







Deformation of a ring of freely-falling test particles under the influence of GW in z-direction



They correspond to the to the independent electric-type components of the Riemann curvature tensor R_{0i0j}





The three-detector Advanced LIGO-Virgo network is generally unable to distinguish the polarization of transient GW signals, like those from BBHs



- Two LIGO detectors are nearly co-oriented, leaving Advanced LIGO largely sensitive to only a single polarization mode
- Even if the LIGO detectors were more favourably-oriented, a network of at least six detectors is generically required to uniquely determine the polarization content of a GW transient

<u>Problem of disentangling modes</u>: **time-series of 6 polarizations + 2 direction angles** that affect the projection of the modes on the detector --- but only six observables R_{0i0i}







Equal prior probability to noise and signal models, as well as equal prior probability to the seven signal sub-hypotheses

Equal prior probability to the non-GR and GR models and identically weight the six non-GR sub-hypotheses

LIGO

Callister, ..., Sakellariadou, ..., PRX7 (2017) 041058



$$\langle \hat{C}(\nu) \rangle_{\rm TVS} = \beta_{\rm T}(\nu) \Omega_{\rm ref}^{\rm T} \left(\frac{\nu}{\nu_{\rm ref}}\right)^{\alpha_{\rm T}} + \beta_{\rm V}(\nu) \Omega_{\rm ref}^{\rm V} \left(\frac{\nu}{\nu_{\rm ref}}\right)^{\alpha_{\rm V}} + \beta_{\rm S}(\nu) \Omega_{\rm ref}^{\rm S} \left(\frac{\nu}{\nu_{\rm ref}}\right)^{\alpha_{\rm S}}$$
$$\beta_{\rm A}(\nu) \equiv \frac{\gamma_{\rm A}(\nu)}{\gamma_{\rm T}(\nu)} \ , \ \ {\rm A} = \{{\rm T},{\rm V},{\rm S}\}$$



PI curves showing sensitivity of aLIGO to SGWB of T, V, S polarizations

Power-law energy density spectra tangent to the PI curves have SNR=3 after 3 years of observation at design sensibility

Callister, ..., Sakellariadou, ..., PRX7 (2017) 041058

AGO







Mairi Sakellariadou

LIGO

 Given the non-detection of any generic SGWB, we put Upper limits assuming all three modes potentially present, marginalizing over amplitudes and spectral indices for all but one mode

Polarization	Uniform prior	Log-uniform prior
Tensor	8.2×10^{-8}	3.2×10^{-8}
Vector	1.2×10^{-7}	2.9×10^{-8}
Scalar	4.2×10^{-7}	6.1×10^{-8}

Iog Bayes factors consistent with Gaussian noise and GR-polarization modes

Abbott, et al arXiv:1903.02886





Purely phenomenological model

$$E^2 = p^2 c^2 + A_\alpha p^\alpha c^\alpha$$

$$\alpha = 0, 0.5, 1, 1.5, 2.5, 3, 3.5, 4$$

Lorentz-violating dispersion relation

$$A_0 > 0$$
 : massive graviton with $m_g = A_0^{1/2}/c^2$

- $\alpha = 2.5$: multi-fractal spacetime
- $\alpha = 3$: doubly special relativity
- $\alpha = 4$: Horava-Lifshitz and extra dimensional theories

Abbott, et al arXiv:1903.04667







$$E^2 = p^2 c^2 + A_\alpha p^\alpha c^\alpha$$

$$\alpha = 0, 0.5, 1, 1.5, 2.5, 3, 3.5, 4$$

Lorentz-violating dispersion relation

$$v_g/c = (dE/dp)/c = 1 + (\alpha - 1)A_{\alpha}E^{\alpha - 2}/2 + O(A_{\alpha}^2)$$

Scale of modifications to the Newtonian potential associated with this dispersion relation

$$\lambda_A := hc |A_{\alpha}|^{1/(\alpha-2)}$$

Abbott, et al arXiv:1903.04667





$$E^{2} = p^{2}c^{2} + A_{\alpha}p^{\alpha}c^{\alpha}$$
$$\tilde{h}(\nu) = A(\nu)e^{i\Phi(\nu)}$$
$$\tilde{h}(\nu) = A(\nu)e^{i(\Phi(\nu) + \delta\Phi_{\alpha}(\nu))}$$

depends on binary's **luminosity distance**, binary's **detector–frame chirp mass**, binary's **redshift** and a **distance parameter** (where cosmological parameters will also enter)

Abbott, et al arXiv:1903.04667













Damping of the waveform due to gravitational leakage into extra dim

GR:
$$h_{\rm GR} \propto d_L^{-1}$$
 $d_L^{\rm EM} \simeq \frac{z(1+z)}{H_0} \stackrel{z \ll 1}{\simeq} \frac{z}{H_0}$

Deviation depends on the number of dimensions D and would result to a systematic **overestimation of the source** $d_L^{\rm EM}$ **inferred from GW data**

Extra dim models: assume that light and matter propagate in 4 ST dim

$$h \propto \frac{1}{d_L^{\rm GW}} = \frac{1}{d_L^{\rm EM}} \left[1 + \left(\frac{d_L^{\rm EM}}{R_c}\right)^n \right]^{-(D-4)/(2n)}$$

The **strain** measured in a GW interferometer



The **luminosity distance** measured for the optical counterpart of the standard siren



Mairi Sakellariadou

LVC, arXiv:1811.00364



Joint posterior probability for D, d_L^{GW} and d_L^{EM} given the two statistically independent measurements of EM data and GW data

$$p(D|x_{\rm GW}, x_{\rm EM}) = \int p(d_L^{\rm GW}|x_{\rm GW}) p(d_L^{\rm EM}|x_{\rm EM}) \delta(D - D(d_L^{\rm GW}, d_L^{\rm EM}, R_c, n)) \, \mathrm{d}d_L^{\rm GW} \mathrm{d}d_L^{\rm EM}$$

GW170817



90% upper bounds on # of spacetime dim assuming fixed steepness and distance scale 10% lower limits on distance scale assuming fixed transition steepness and # of spacetime dim

Abbott, et al arXiv:1811.00364





Can Quantum Gravity (QG) theories leave a signature in GWs?

 NO: QG corrections will be suppressed by the Planck scale Leading-order perturbative quantum corrections to the Einstein-Hilbert action In FLRW there are only 2 scales for building dimensionless quantities

quantum corrections are of the form $(\ell_{\rm Pl}H)^n$ where $n=2,3,\ldots$

but today are too small: $(\ell_{\rm Pl}H_0)^n \sim 10^{-60n}$ and any late-time QG imprint is Planck-suppressed and undetectable

Nonperturbative effects beyond the simple dimensional argument

If there is a third scale $L \gg \ell_{\rm Pl}$ quantum corrections may become $\sim \ell_{\rm Pl}^a H^b L^c$ with a - b + c = 0 and NOT all these exponents are small

Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1904.00384 Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1907:02489





Long-range nonperturbative mechanism found in most QG candidates: *Dimensional flow* (change of spacetime dimensionality)

$$S = \frac{1}{2\ell_*^{2\Gamma}} \int d\varrho \sqrt{-g^{(0)}} \left[h_{\mu\nu} \mathcal{K} h^{\mu\nu} + O(h_{\mu\nu}^2) + \mathcal{J}^{\mu\nu} h_{\mu\nu} \right]$$

ST distorted by QG effects characterized by ST measure and kinetic term

characteristic scale of geometry

scaling parameter

Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1904.00384 Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1907:02489







Long-range nonperturbative mechanism found in most QG candidates: *Dimensional flow* (change of spacetime dimensionality)

Scaling parameter

$$\Gamma(\ell) := \frac{d_{\mathrm{H}}(\ell)}{2} - \frac{d_{\mathrm{H}}^{k}(\ell)}{d_{\mathrm{S}}(\ell)}$$

	$\Gamma_{\rm UV}$	$\Gamma_{\rm meso}\gtrsim 1$
GFT/SF/LQG	[-3, 0)	yes
Causal dynamical triangulation	-2/3	
κ -Minkowski (other)	[-1/2, 1]	
Stelle gravity	0	
String theory (low-energy limit)	0	
Asymptotic safety	0	
Hořava–Lifshitz gravity	0	
$\kappa\text{-Minkowski}$ bicross-product ∇^2	3/2	yes
$\kappa\text{-Minkowski}$ relative-locality ∇^2	2	yes
Padmanabhan nonlocal model	2	yes

$$d_{
m H}(\ell) := rac{d \ln \mathcal{V}(\ell)}{d \ln \ell}$$

Hausdorff dimension

how volumes scale with their linear size

Hausdorff dim in momentum space

 $d_{\rm H}^k(\ell) := \frac{d\ln\tilde{\mathcal{V}}(k)}{d\ln k} \Big|$



Spectral dimension

governed by type of kinetic term in the action; depends on dispersion relation and on measure in momentum ST

Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1904.00384 Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1907:02489





Tests of QG with GWs: gravitational wave luminosity distance









Constraint the parameters $~\ell_*$, $\gamma~$ by constraining the ratio $~d_L^{ ext{GW}}(z)/d_L^{ ext{EM}}(z)$ as a function of z

<u>Standard sirens</u>: -- NS merger GW170817 (LIGO/Virgo & Fermi) -- simulated z=2 supermassive BH merger within Lisa detectability

Only GFT, SF or LQG could generate a signal detectable with standard sirens

Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1904.00384 Calcagni, Kuroyanagi, Marsat, Sakellariadou, Tamanini, Tasinato, arXiv:1907:02489



Phenomenological proposal

$$\frac{d_L^{\rm gw}(a)}{d_L^{\rm em}(a)} = \Xi_0 + a^n (1 - \Xi_0)$$

$$\Xi_0 = 1$$
 corresponds to GR

Model	$\Xi_0 - 1$	n
HS $f(R)$ gravity	$\frac{1}{2}f_{R0}$	$\frac{3(\tilde{n}+1)\Omega_m}{4-3\Omega_m}$
Designer $f(R)$ gravity	$-0.24\Omega_m^{0.76}B_0$	$3.1\Omega_m^{0.24}$
Jordan–Brans–Dicke	$\frac{1}{2}\delta\phi_0$	$\frac{3(\tilde{n}+1)\Omega_m}{4-3\Omega_m}$
Galileon cosmology	$rac{eta \phi_0}{2 M_{ m Pl}}$	$rac{\dot{\phi}_0}{H_0\phi}$
$\alpha_M = \alpha_{M0} a^{\tilde{n}}$	$rac{lpha_{M0}}{2 ilde{n}}$	${ ilde n}$
$\alpha_M = \alpha_{M0} \frac{\Omega_{\Lambda}(a)}{\Omega_{\Lambda}}$	$-rac{lpha_{M0}}{6\Omega_{\Lambda}}\ln\Omega_{m}$	$-rac{3\Omega_\Lambda}{\ln\Omega_m}$
$\Omega = 1 + \Omega_+ a^{\tilde{n}}$	$\frac{1}{2}\Omega_+$	\tilde{n}
Minimal self-acceleration	$\lambda \left(\ln a_{acc} + \frac{C}{2} \chi_{acc} \right)$	$\frac{C/H_0 - 2}{\ln a_{acc}^2 - C\chi_{acc}}$

Study prospects of observing modified GW propagation using supermassive binaries as standard sirens with LISA:

construct simulated catalogues of LISA massive BH binaries with EM counterparts

 Ξ_0 can be measured to an accuracy between 4.4% and 1.1%

Belgacem,... Sakellariadou, JCAP 1907 (2019) 024





Conclusions

GWs offer a new powerful window into the Universe and the laws governing it

- astrophysical models
- physics beyond the Standard Model
- large scale structure
- dark matter candidates (PBHs, axions, ...)
- GR and modified gravity models
- quantum gravity

King's College London

Mairi Sakellariadou

LIGO Scientific Collaboration