

Gravitational wave detection with atomic clocks

IGOR PIKOVSKI

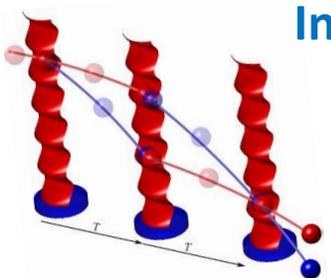
STOCKHOLM UNIVERSITY

Interplay between gravity and low-energy quantum systems

Quantum systems as probes

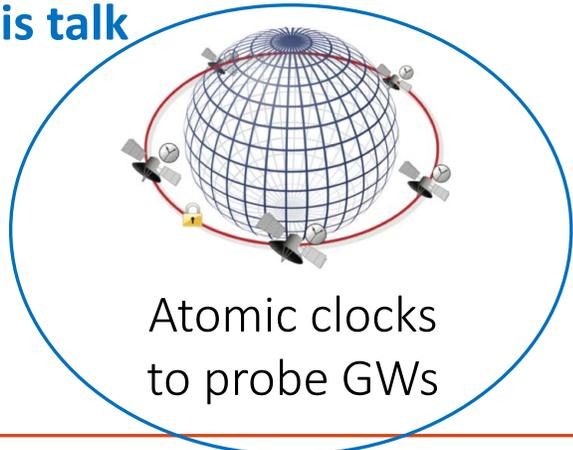
Change in quantum behavior

Expected physics

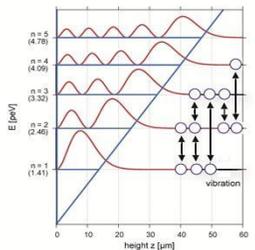


Matter-waves to probe GWs

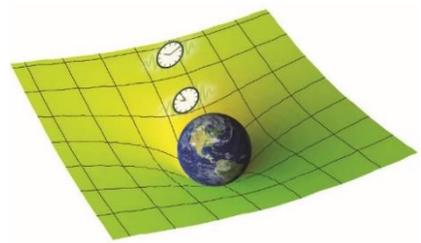
In this talk



Atomic clocks to probe GWs

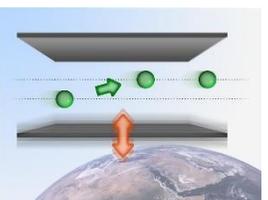


Quantized states of neutrons in gravity

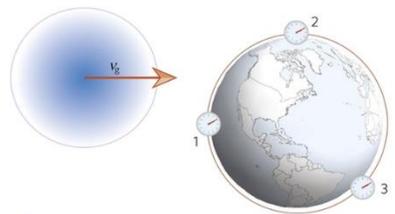


Quantum interference of clocks

Exotic models



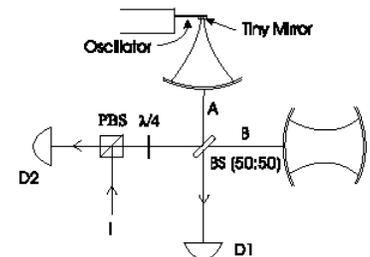
5th force / modified Newton law



Dark matter searches



Commutator deformations



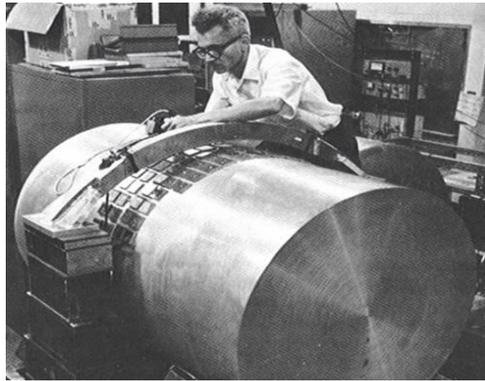
Gravitational wave function collapse

Overview

- Gravitational waves: frequency vs. phase measurements
- History of time keeping
- Atomic clocks
- Optical lattice atomic clock based gravitational wave detector
- Fundamental sensitivity and features
- Outlook

PhD and Postdoc positions open at SU
(quantum optics, quantum info &
interface with gravity, cosmology)
igor.pikovski@fysik.su.se

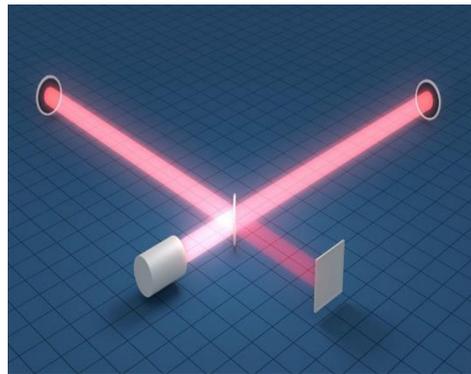
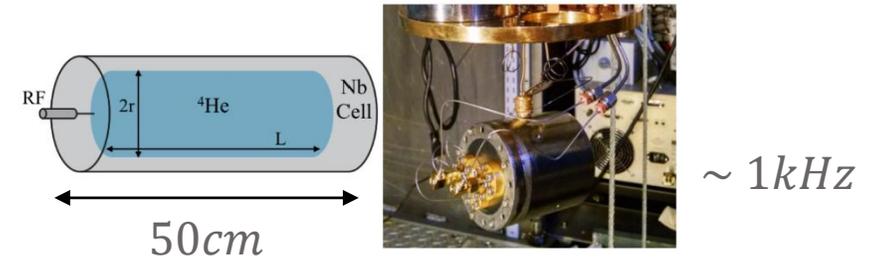
Detecting gravitational waves



A. Resonant bar detectors: stretching of a material

New direction: Superfluid Helium opto-mechanical systems

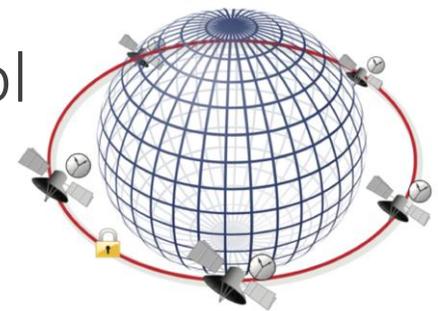
*Singh, De Lorenzo, Pikovski, Schwab.
New J. Phys. 19, 073023 (2017)*



B. Free-space detectors: measuring distance

New direction: Atomic clocks and quantum control

*Kolkowitz, Pikovski, Langellier, Lukin, Walsworth, Ye.
Phys. Rev. D 94, 124043 (2016)*



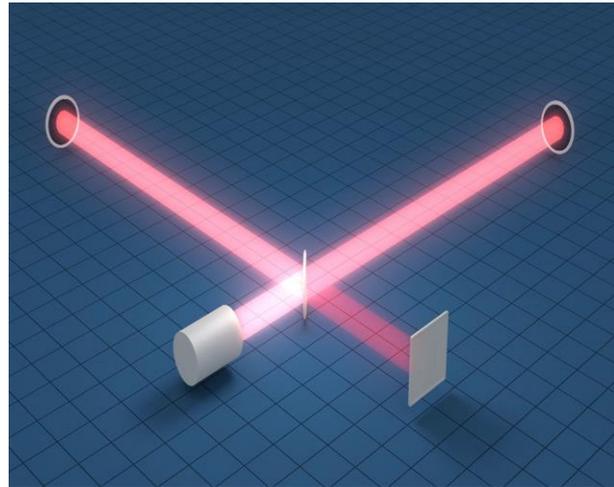
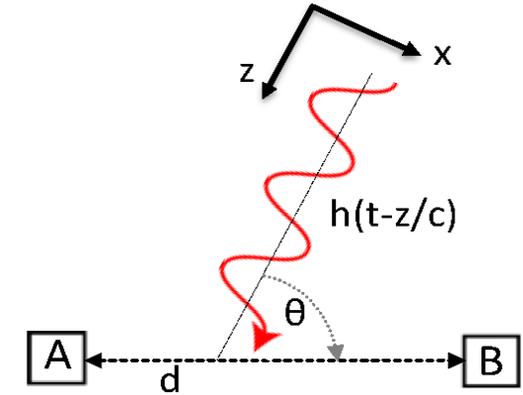
LIGO principle: optical interferometry

$$ds^2 = -c^2 dt^2 + (1 + h(t, z)) dx^2 + (1 - h(t, z)) dy^2 + dz^2$$

Change in relative optical phase due to changes in distance

Distance from A to B in flat space: d

Light travel distance in presence of GW:



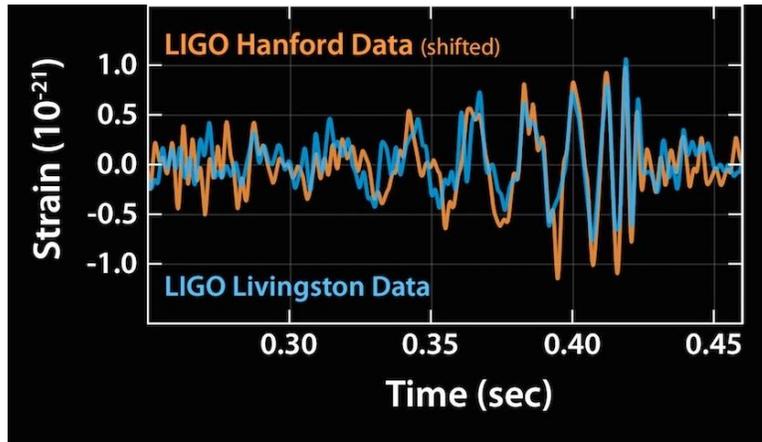
2 arms: cancellation of laser phase noise

$$d + \frac{c}{2} (1 + \cos \theta) \left[H(t) - H \left(t + \frac{d}{c} (1 - \cos \theta) \right) \right] \quad \text{where } dH/dt = h$$

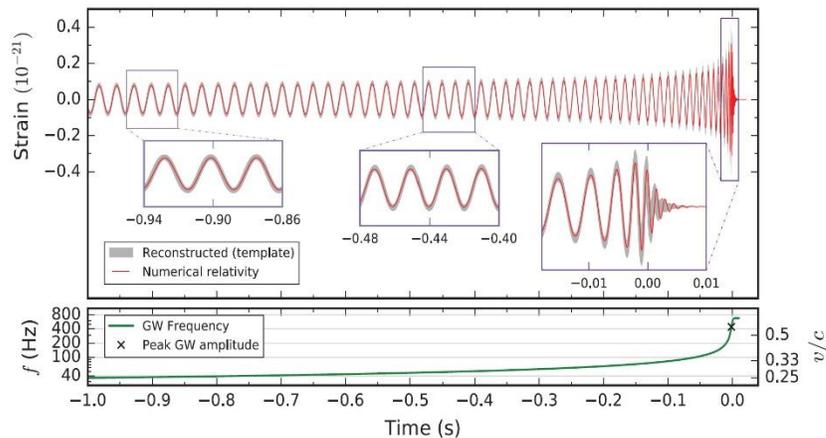
For $d \ll \lambda_{GW}$: $\frac{\Delta d}{d} \approx h(t)$ LIGO signal

Strain measured via changes in optical phase

LIGO detections

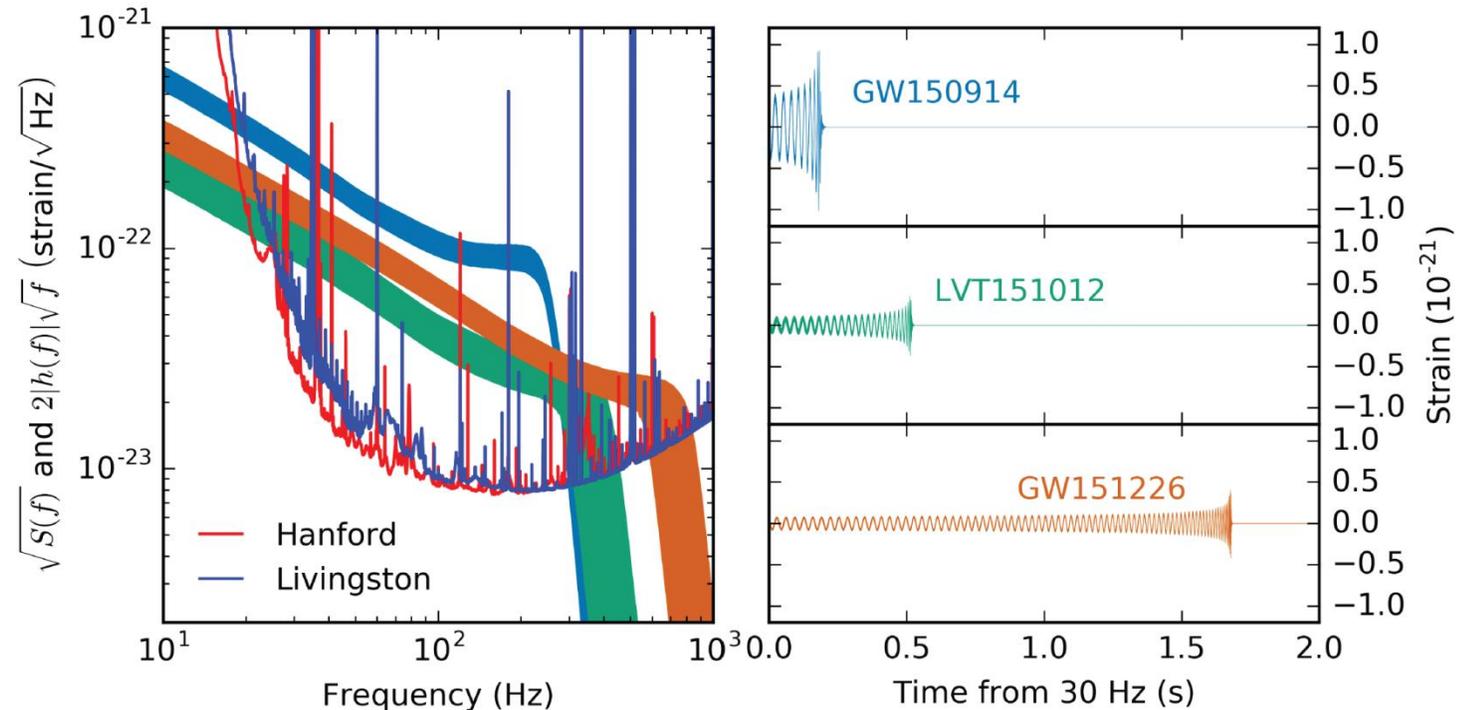


B. Abbott et al. PRL 116, 061102 (2016)



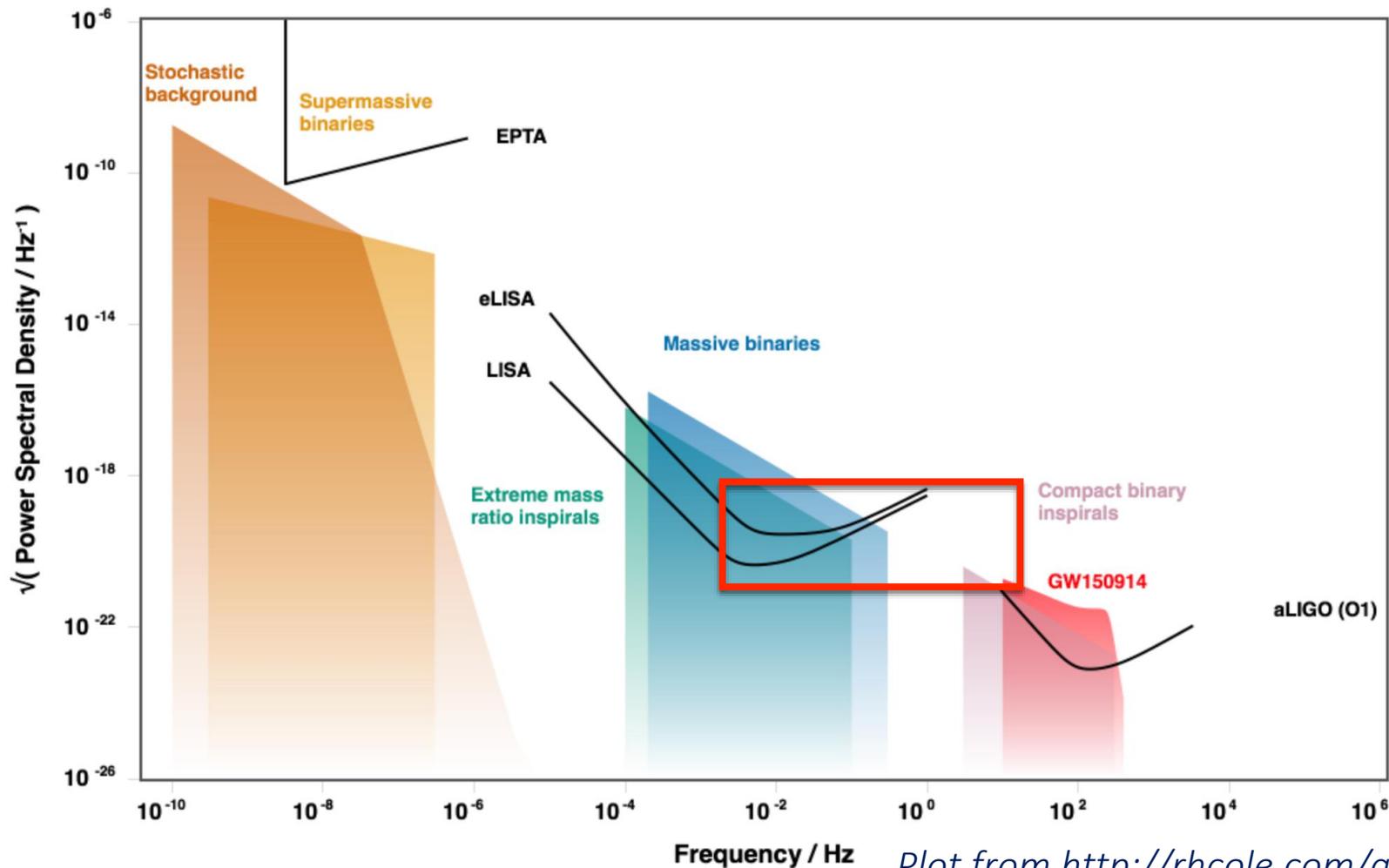
B. Abbott et al. PRL 116, 241103 (2016)

- Limited by photon shot noise at $f \gtrsim 200$ Hz
- On Earth: limited by gravity noise at $f \lesssim 40$ Hz



LIGO collaboration, <https://dcc.ligo.org/P1600088/public/> (2016)

Current and future sensitivity



Plot from <http://rhcole.com/apps/GWplotter>

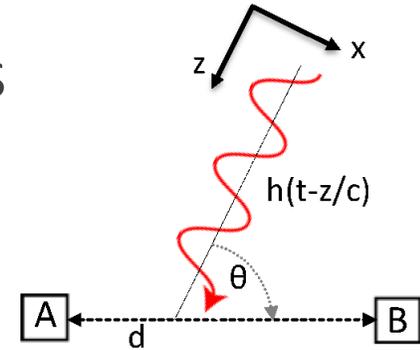
Here: atomic clock based detector in space

- Narrowband with competitive sensitivity
- Tunable in mHz – Hz range using techniques from quantum control
- Can bridge range between LISA and LIGO

Frequency measurements

Frequency measurements: Doppler shifts from gravitational waves

$$s = \frac{\Delta\nu}{\nu} = \frac{1 + \cos \theta}{2} \left(h(t) - h\left(t + \frac{d}{c}(1 - \cos \theta)\right) \right)$$



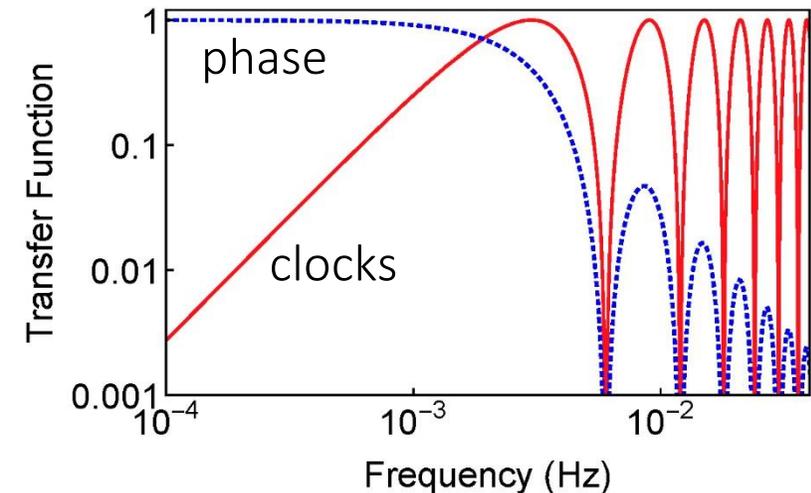
In Fourier space: $\tilde{s}^2(f) = \tilde{h}^2(f)T(f)$ $T(f)$: detector transfer function

Clocks:

- Better signal for $f > c/d$
- Different measurement technique with other advantages

$$T_{phase} = \text{sinc}^2 \left(\pi f \frac{d}{c} \right)$$

$$T_{clocks} = \sin^2 \left(\pi f \frac{d}{c} \right)$$



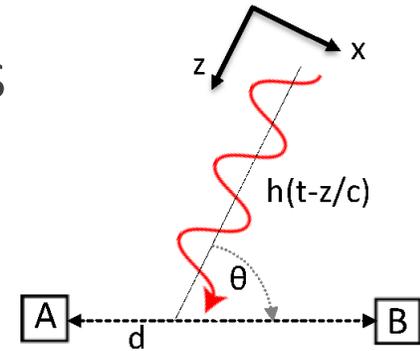
Also used in Pulsar Timing Array

($f < \mu\text{Hz}$) *Hobbs et al. Class. & Quant. Grav. 27, 084013 (2010)*

Frequency measurements

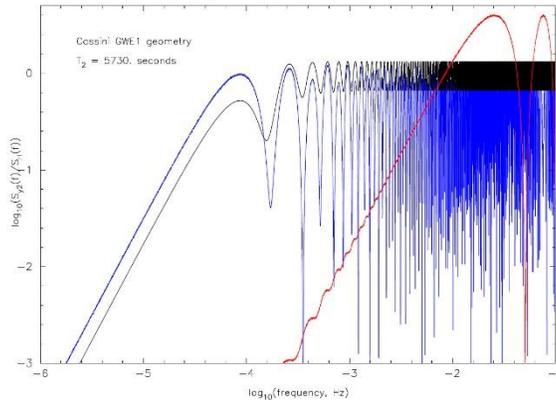
Frequency measurements: Doppler shifts from gravitational waves

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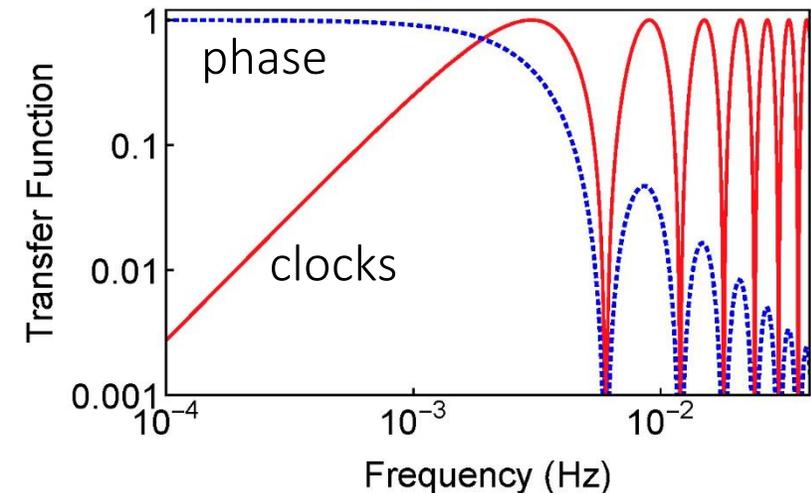
Same principle:
Doppler Tracking



Armstrong, Living Rev. Relativity, 9, (2006)

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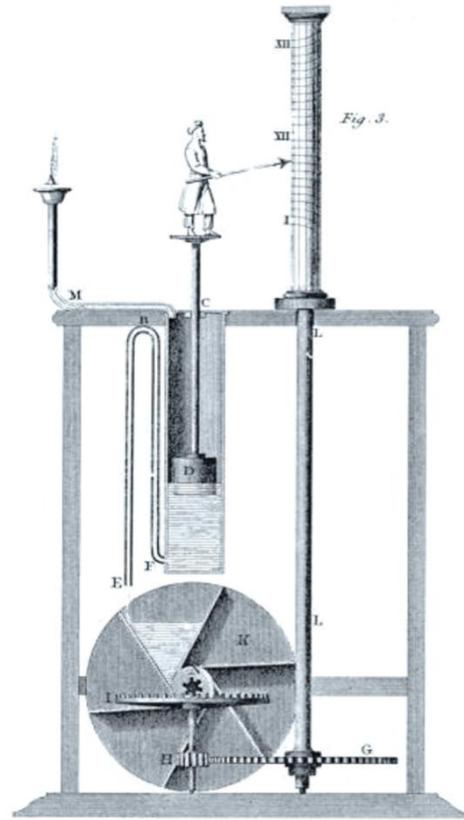
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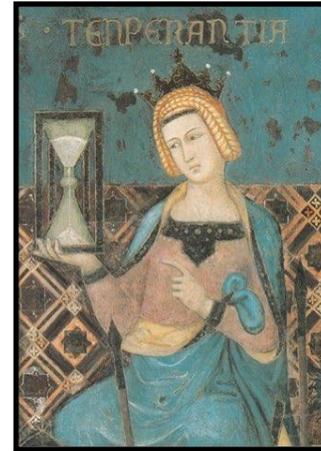
Measurement of time



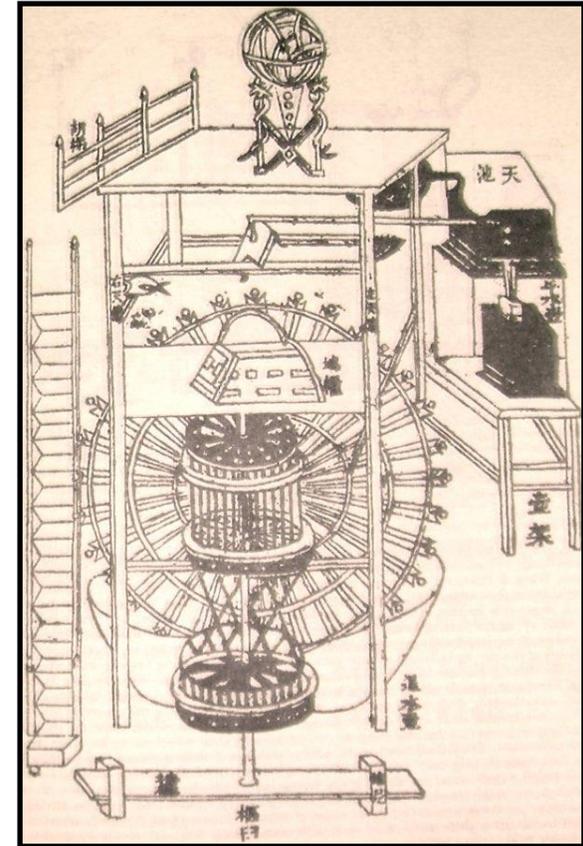
Persian water clock,
300 BC



Ctesibius's clepsydra,
250 BC



Painting of an hourglass,
Lorenzetti, 1338 AD



Su Song's water clock,
1000 AD

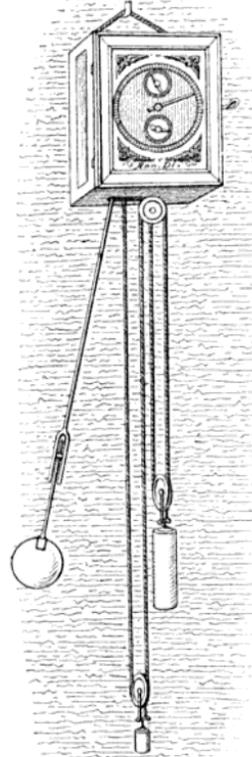
Image credit: [wikipedia.org](https://en.wikipedia.org)

1656: Invention of the pendulum clock

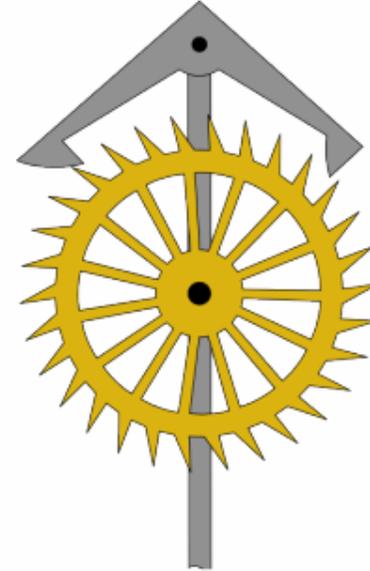


Christiaan Huygens
1629 - 1695

Image credit: [wikipedia.org](https://en.wikipedia.org/wiki/Christiaan_Huygens)



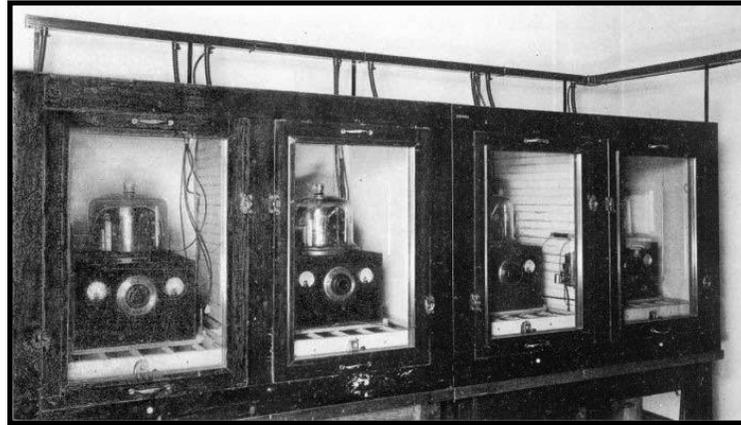
Huygens pendulum clock



Escapement
(counter)

1921: Quartz oscillators invented

Applied voltage results in crystal oscillations, generating electric field



NIST 1929: Accurate to ~ 3 s in 1 year
 $\sigma \sim 1 \times 10^{-7}$



Modern day tuning fork
Accurate to ~ 0.5 s in 1 day
 $\sigma \sim 6 \times 10^{-6}$

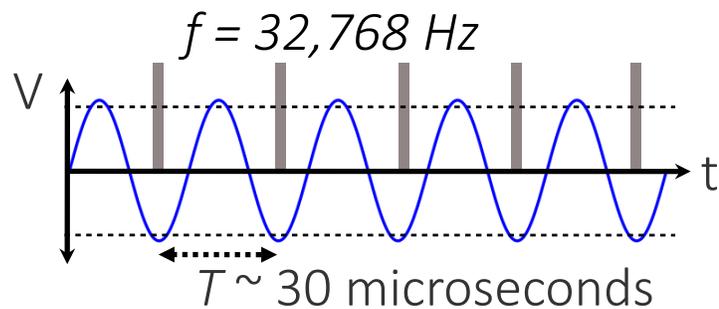
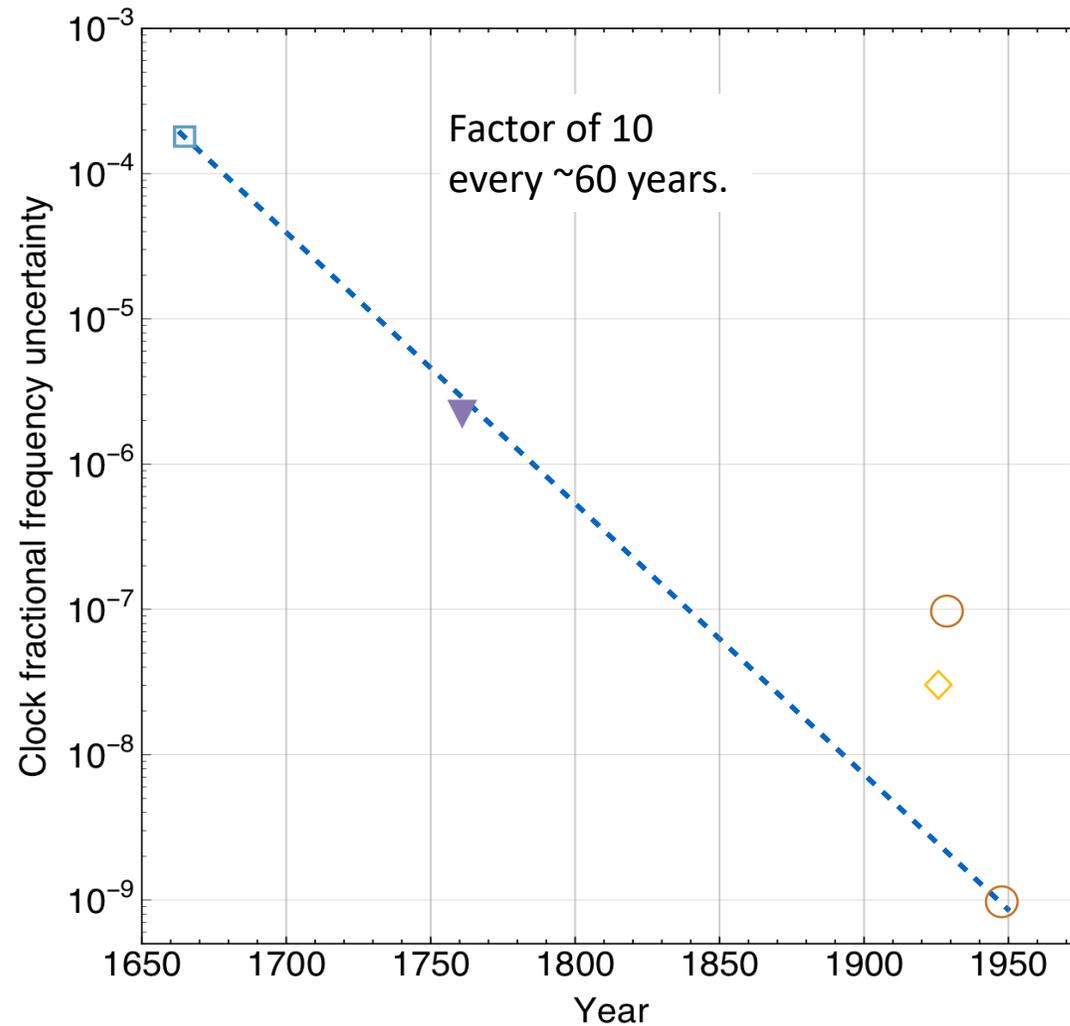


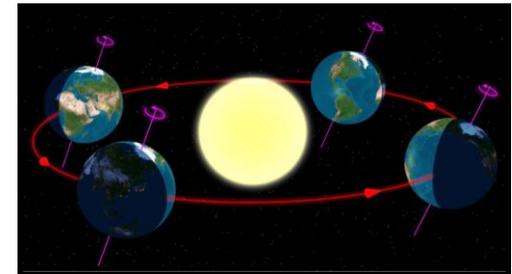
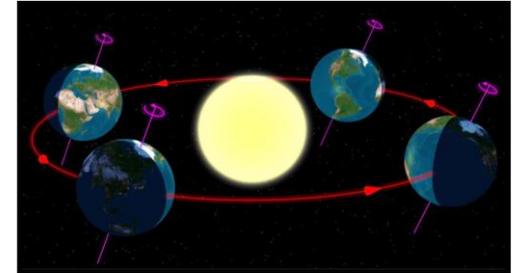
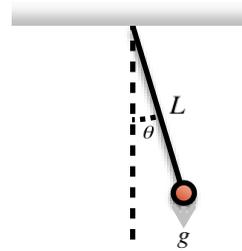
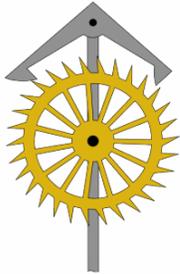
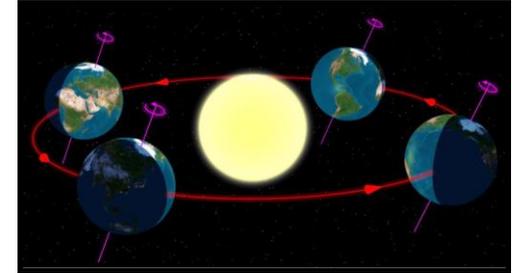
Image credit: [wikipedia.org](https://en.wikipedia.org)

Clock progress, 1656 - 1949

- Huygen pendulum
- ▼ Harrison H4
- ◇ Shortt pendulum
- NBS quartz



Components of a mechanical clock



Counter

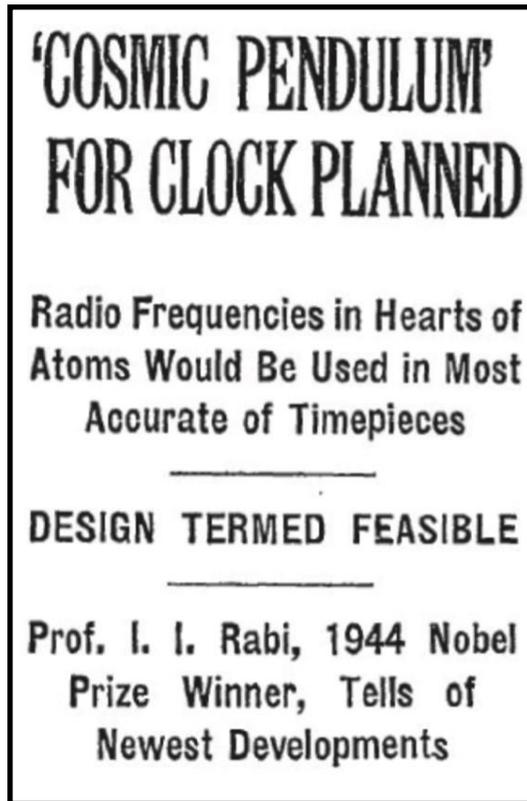
Local oscillator

Frequency reference

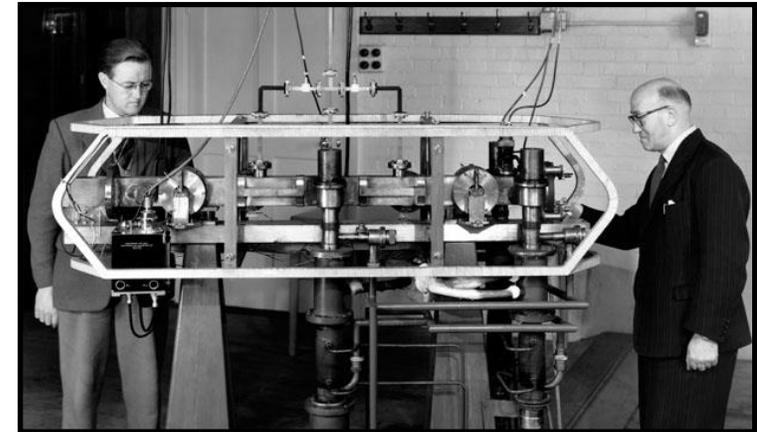
1955: First cesium atomic clock



Isidor Isaac Rabi



NY Times,
Jan 21st, 1945



First cesium beam clock
Jack Parry, Louis Essen

$$\sigma \sim 1 \times 10^{-10}$$

(Accurate to ~ 3 s in 1000 years)

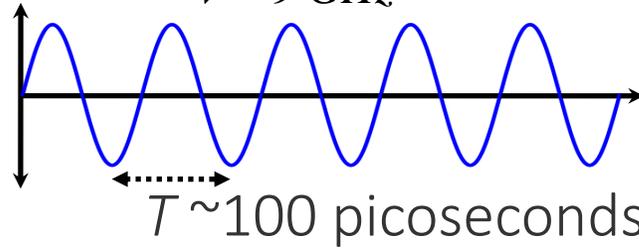
Principles of an atomic clock



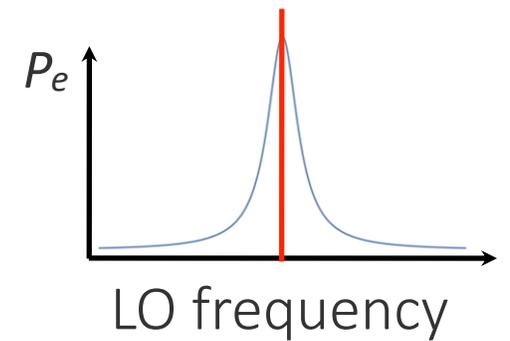
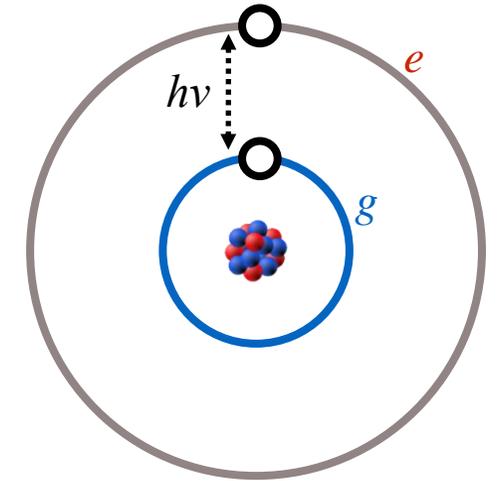
Counter



$\nu = 9 \text{ GHz}$



Local oscillator (LO)



Frequency reference

Atomic clocks

Fundamental limit: fractional frequency instability from projection noise (intrinsic randomness of n 2-level systems):

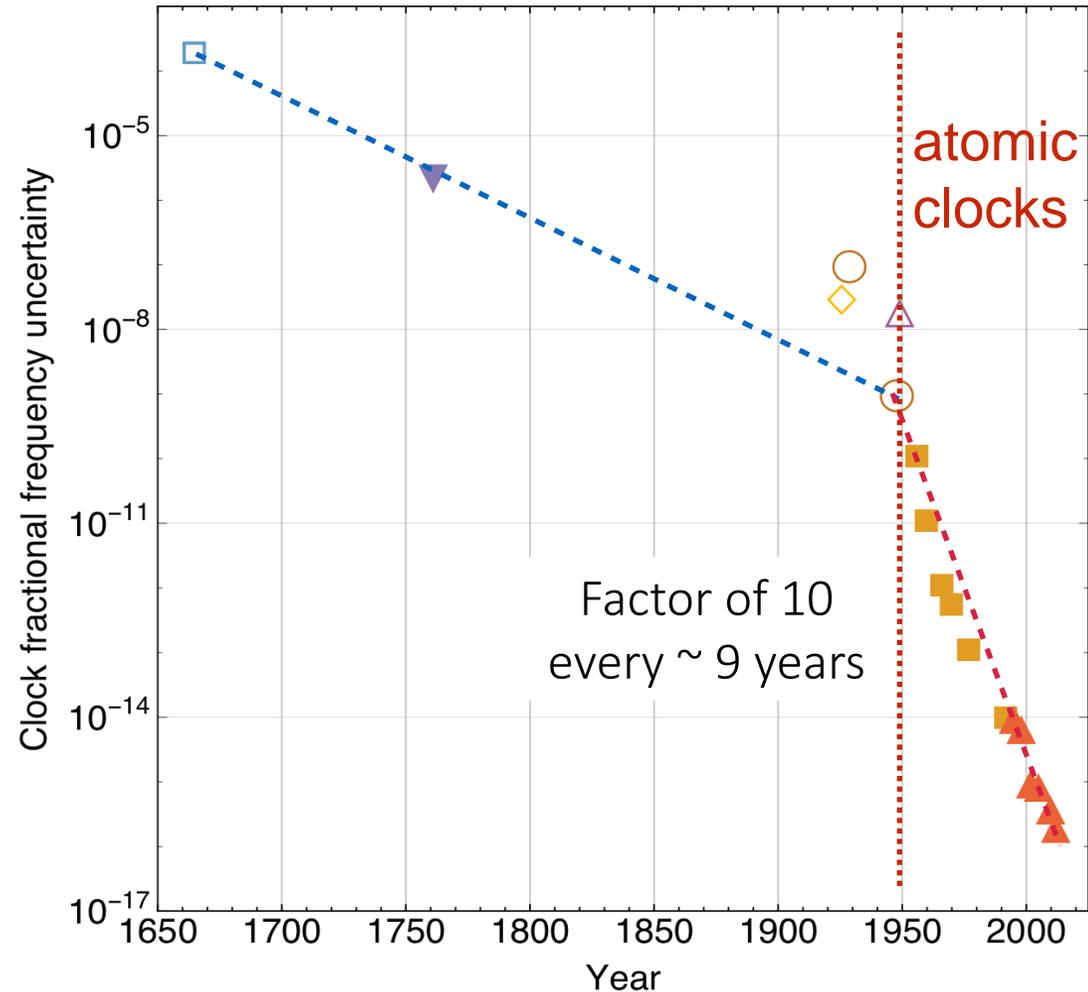
$$\sigma \approx \frac{\Delta\nu}{\nu_o} \times \frac{1}{SNR} = \frac{1}{\nu_o T \sqrt{n_a M}}$$

Best atomic clock will have:

- Narrow transition, and cold atoms
- Many atoms
- Long interrogation times
- Short dead times
- Well isolated atoms to avoid systematics

Clock progress, 1656 - 2016

- Huygen pendulum
- ▼ Harrison H4
- ◇ Shortt pendulum
- NBS quartz
- △ Ammonia maser
- Cs beam
- ▲ Cs fountain



Optical atomic clocks

Fundamental limit: fractional frequency instability from projection noise (intrinsic randomness of n 2-level systems):

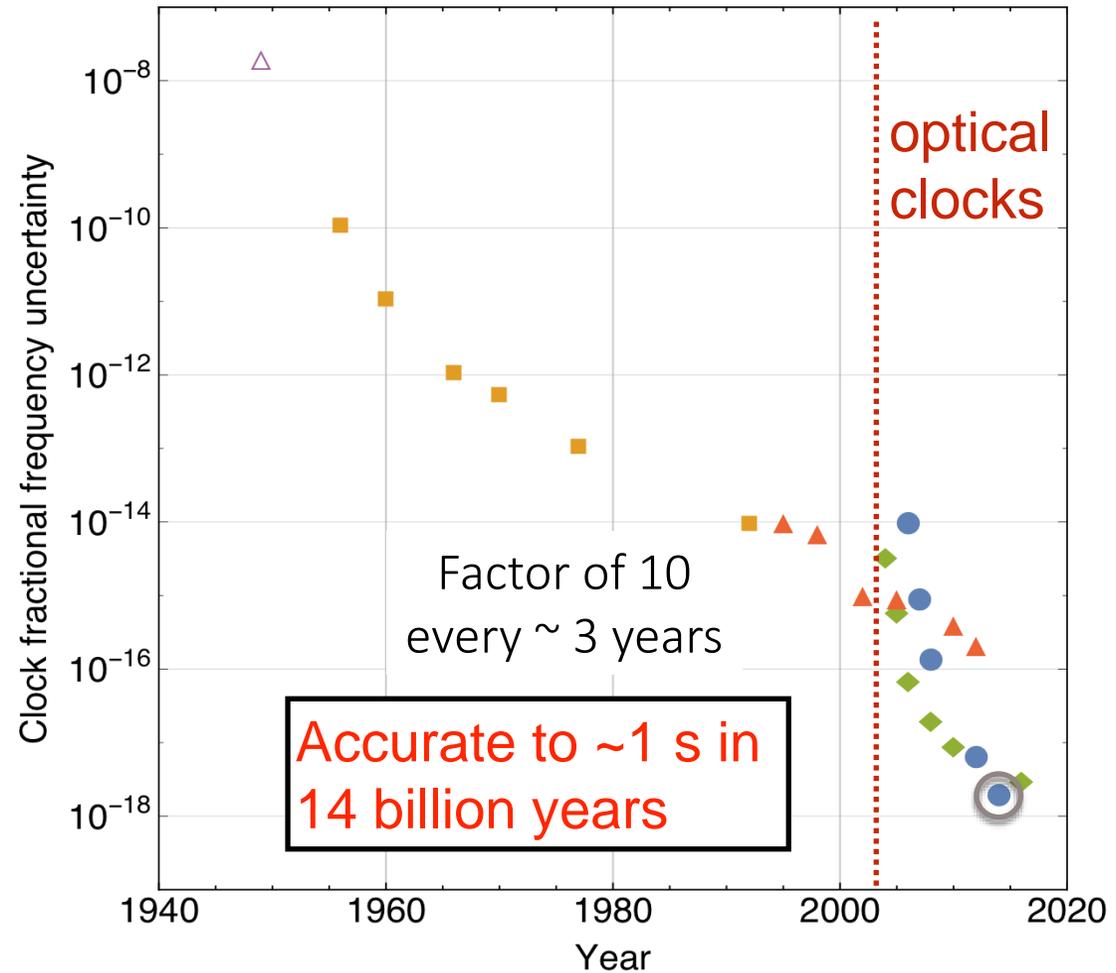
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Best atomic clock will have:

- Narrow transition, and cold atoms
- Many atoms
- Long interrogation times
- Short dead times
- Well isolated atoms to avoid systematics
- **High frequency transition**  Move from $\nu_o = 10^{10}$ Hz to $\nu_o = 10^{15}$ Hz

Atomic clock progress, 1949 - 2016

- △ Ammonia maser
- Cs beam
- ▲ Cs fountain
- ◆ Ion optical clock
- Sr optical lattice clock



Optical lattice atomic clocks in a nutshell

Group of Jun Ye (JILA/CU Boulder)

- Optical frequency

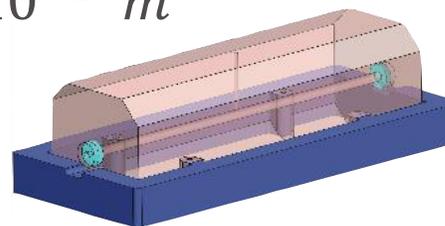
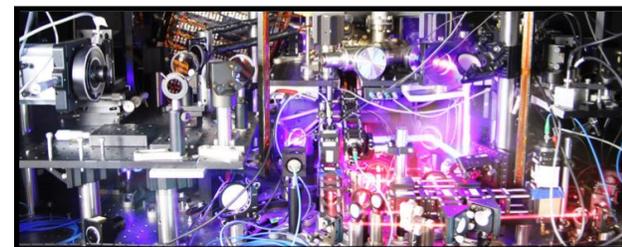
Fractional frequency instability: $\sigma = \frac{\Delta\nu}{\nu} \times \frac{1}{SNR}$

- Ultra-stable laser

Linewidth 26 mHz, $Q \sim 2 \times 10^{16}$, $\Delta L \sim 10^{-16}m$

- Dipole forbidden transitions Sr^{87}

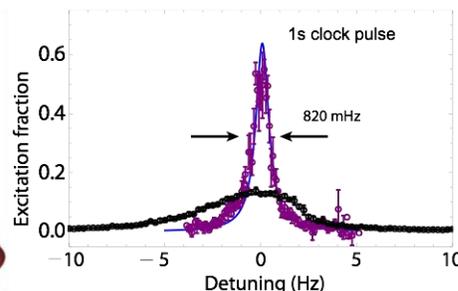
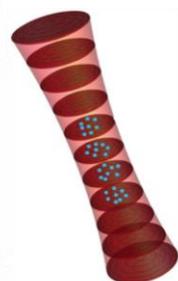
- Strong confinement



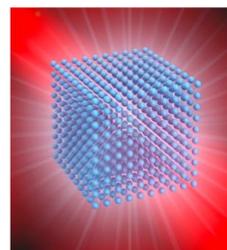
Coherent for ~ 10 earth-moon round trips



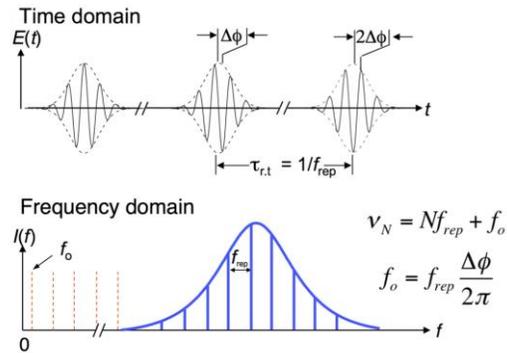
1D:



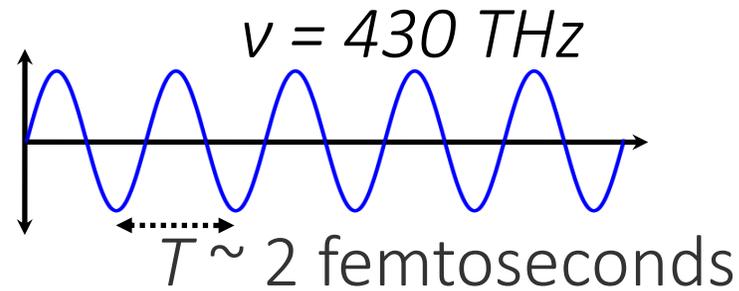
3D:



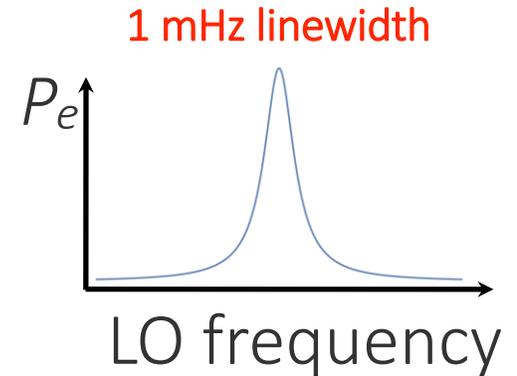
Optical lattice clock



Counter:
Frequency Comb
(ability to count
optical oscillations)



Local oscillator (LO)

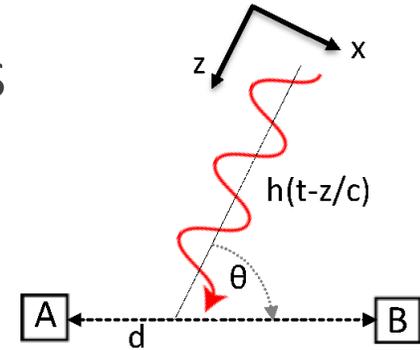


Frequency reference

Back to GWs: Frequency measurements

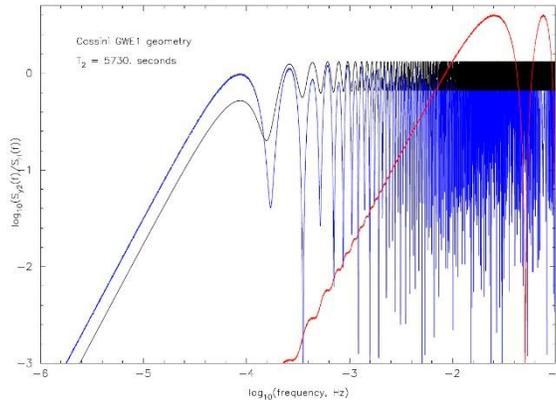
Frequency measurements: Doppler shifts from gravitational waves

$$s = \frac{\Delta\nu}{\nu} = \frac{1 + \cos \theta}{2} \left(h(t) - h\left(t + \frac{d}{c}(1 - \cos \theta)\right) \right)$$



In Fourier space: $\tilde{s}^2(f) = \tilde{h}^2(f)T(f)$ $T(f)$: detector transfer function

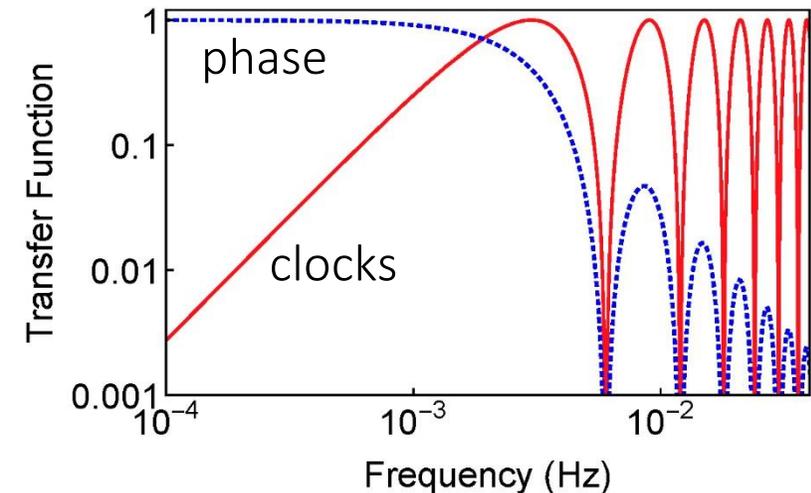
Same principle:
Doppler Tracking



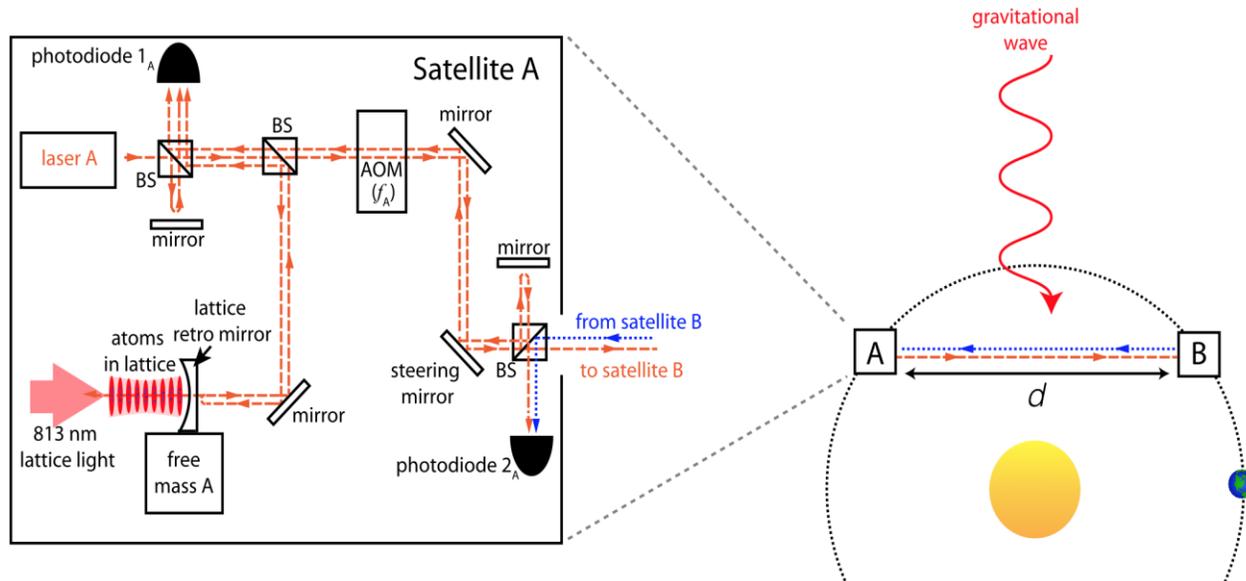
Armstrong, Living Rev. Relativity, 9, (2006)

$$T_{phase} = \text{sinc}^2 \left(\pi f \frac{d}{c} \right)$$

$$T_{clocks} = \sin^2 \left(\pi f \frac{d}{c} \right)$$



Space-based setup using correlated spectroscopy



Two identical drag-free satellites separated from each other by d

On each satellite:

- strontium optical lattice clock
- ultra-stable laser
- free-floating reference mass

Light sent from satellite A to satellite B, where laser B is phase-locked to laser A
 Doppler shift measured by spectroscopic clock comparison. For Ramsey time T :

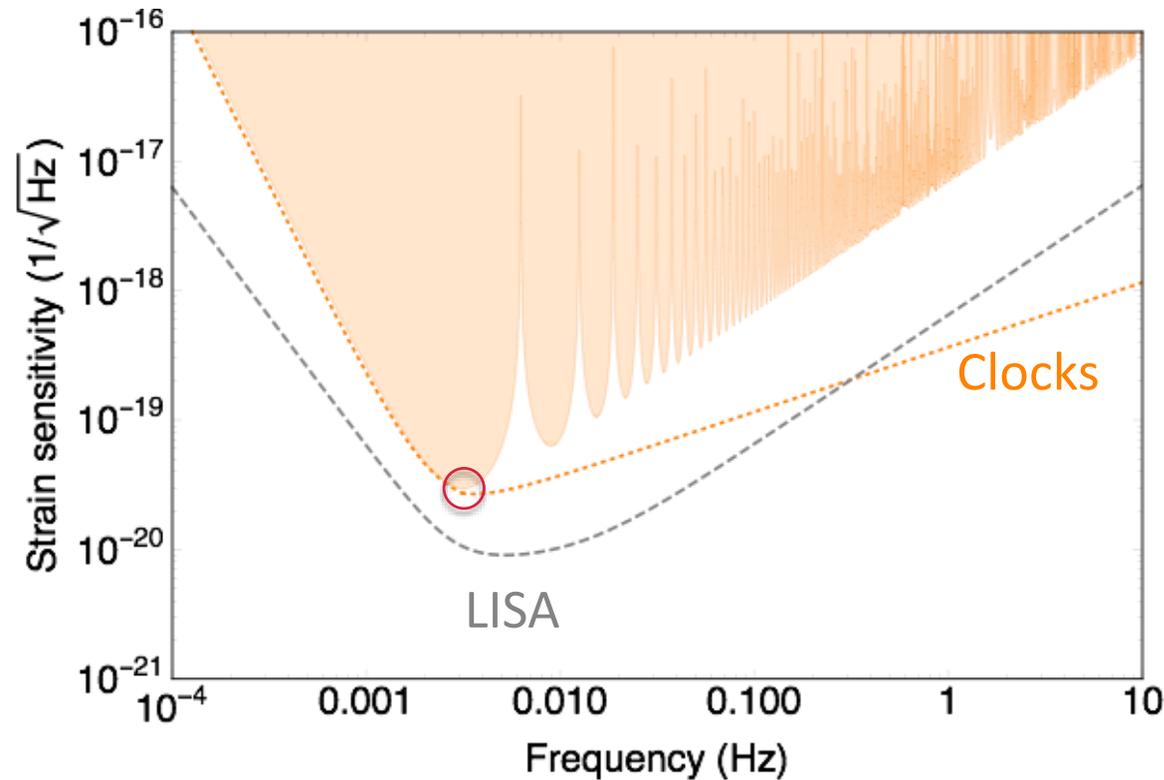
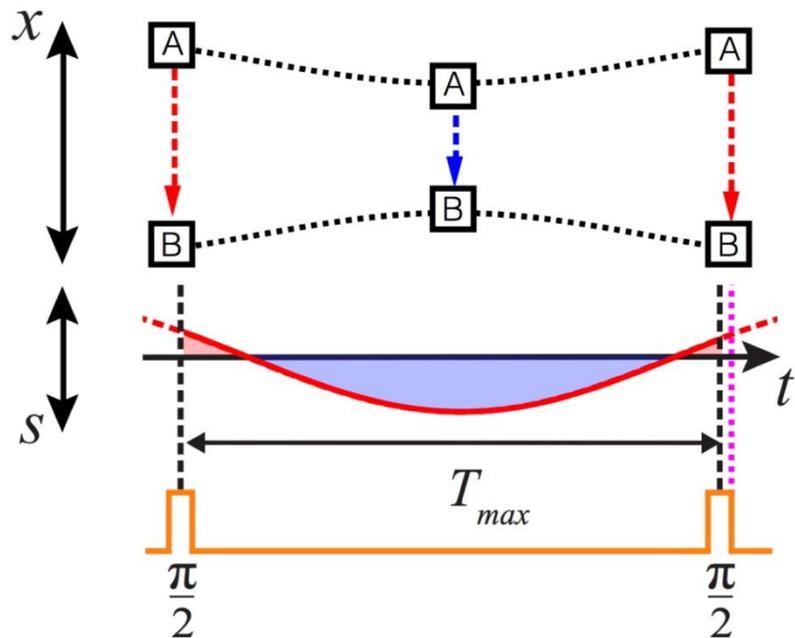
$$s^2 = h^2 \sin^2 \left(\pi f \frac{d}{c} \right) \text{sinc}^2(\pi f T)$$

Sensitivity with Ramsey spectroscopy

Signal: $s_{Ramsey} = \frac{|\Delta\nu|}{\nu} = |h| \left| \sin\left(\pi f \frac{d}{c}\right) \text{sinc}(\pi f T) \right|$

Noise: $\sigma_{min}(\tau) = \frac{1}{\nu} \sqrt{\frac{1}{TN}}$

Long Ramsey sequence:



$N = 7 \times 10^6$
of Sr atoms

$d = 50 \times 10^6$ km
Satellite distance

$T_{max} = 160$ s
Atomic coherence time

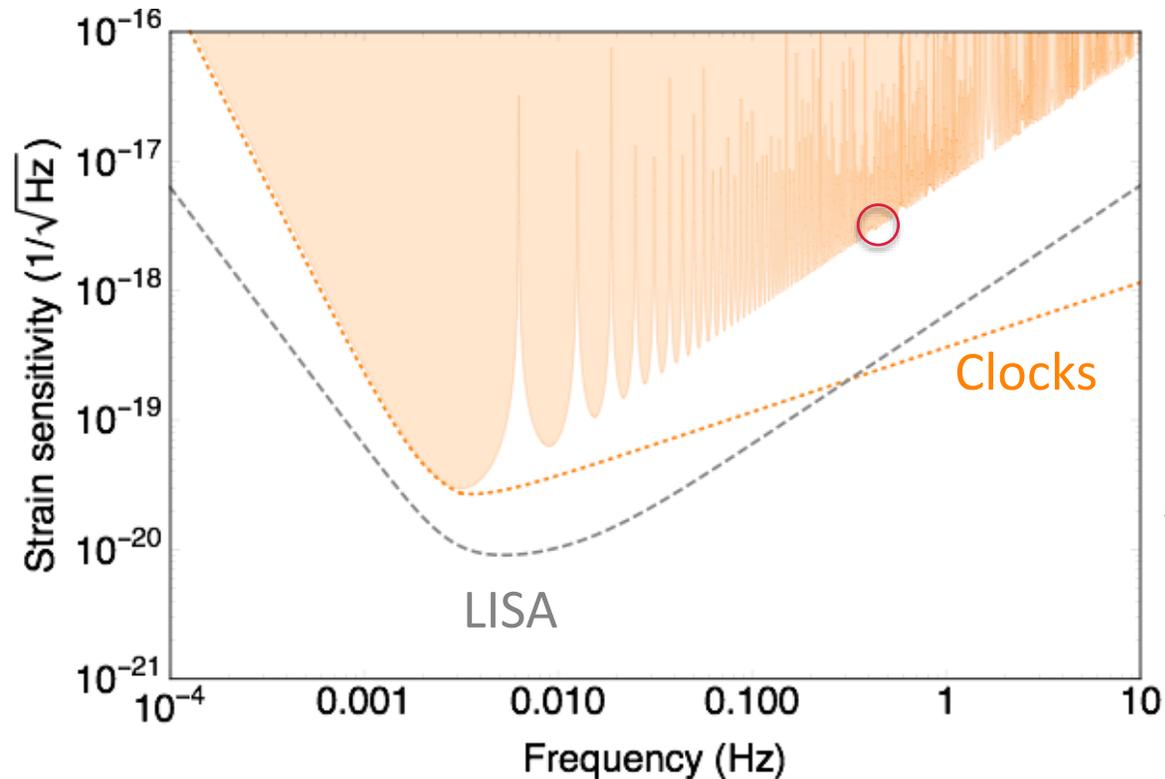
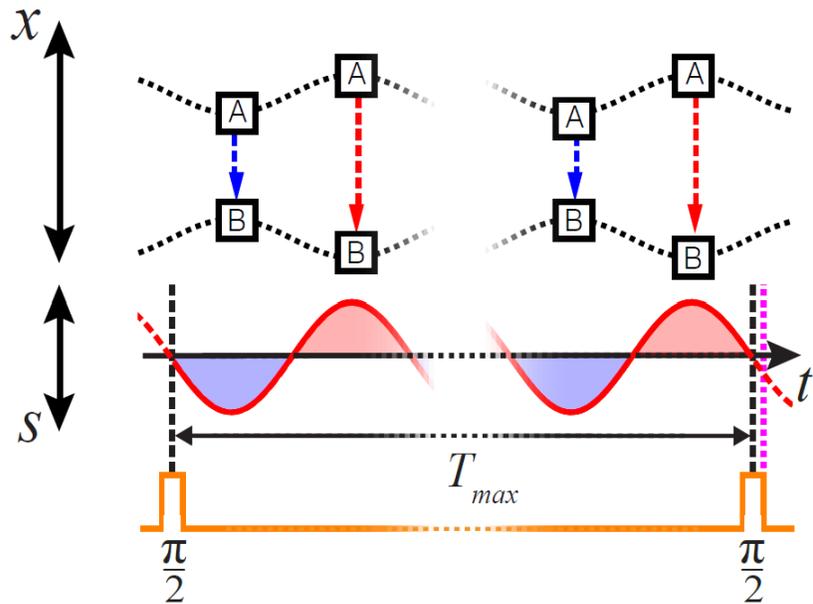
$\sigma_{min} \sim 10^{-20} / \sqrt{\text{Hz}}$
At $f = 1/2T_{max}$

Sensitivity with Ramsey spectroscopy

Signal: $s_{Ramsey} = \frac{|\Delta\nu|}{\nu} = |h| \left| \sin\left(\pi f \frac{d}{c}\right) \text{sinc}(\pi f T) \right|$

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Long Ramsey sequence:



$N = 7 \times 10^6$
of Sr atoms

$d = 50 \times 10^6$ km
Satellite distance

$T_{max} = 160$ s
Atomic coherence time

$$\sigma \sim 10^{-18} / \sqrt{\text{Hz}}$$

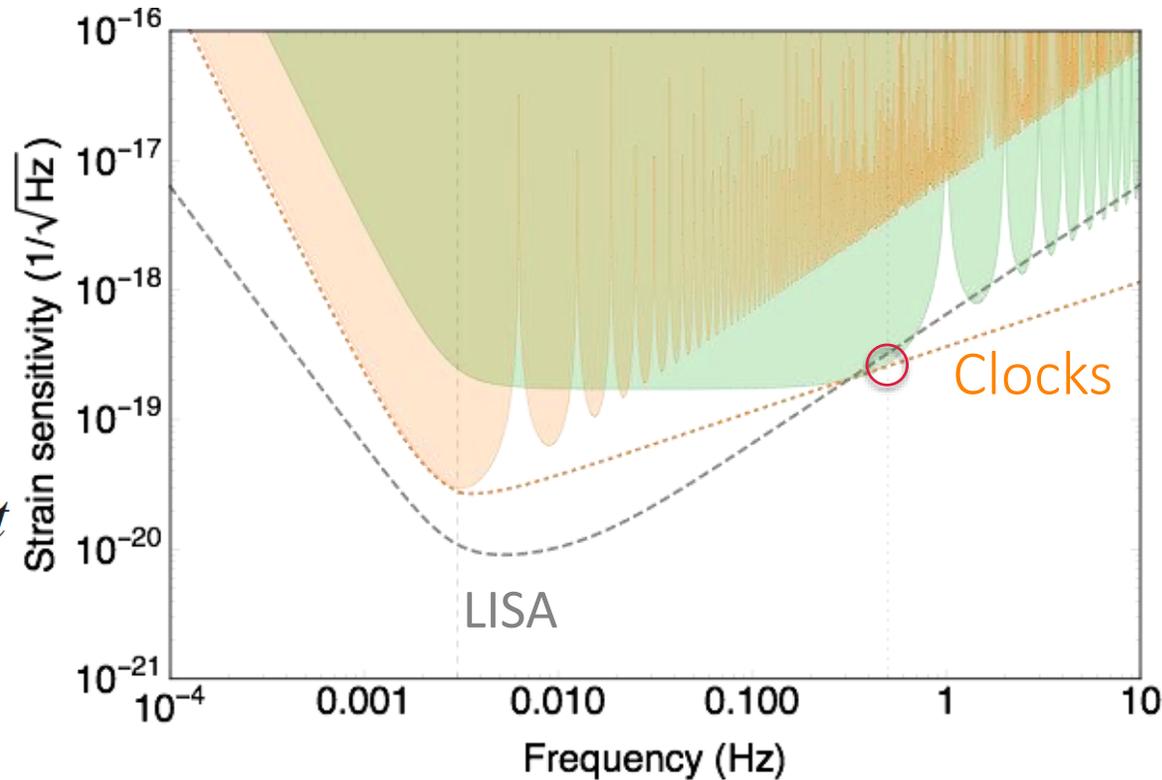
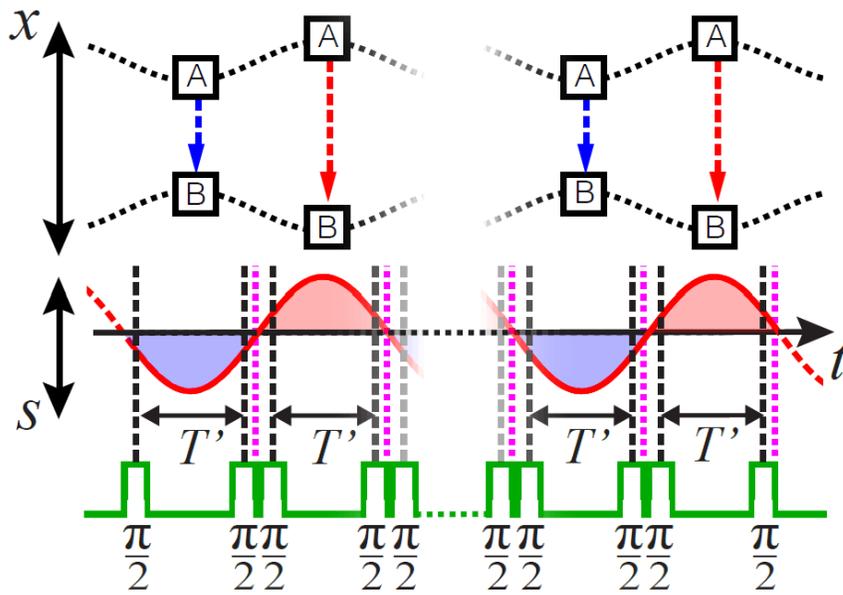
At $f = 160/2T$

Sensitivity with Ramsey spectroscopy

Signal: $s_{Ramsey} = \frac{|\Delta\nu|}{\nu} = |h| \left| \sin\left(\pi f \frac{d}{c}\right) \text{sinc}(\pi f T) \right|$

Noise: $\sigma_{min}(\tau) = \frac{1}{\nu} \sqrt{\frac{1}{TN}}$

Short Ramsey sequence:



$N = 7 \times 10^6$
of Sr atoms

$d = 50 \times 10^6$ km
Satellite distance

$T = 1$ s
Ramsey time

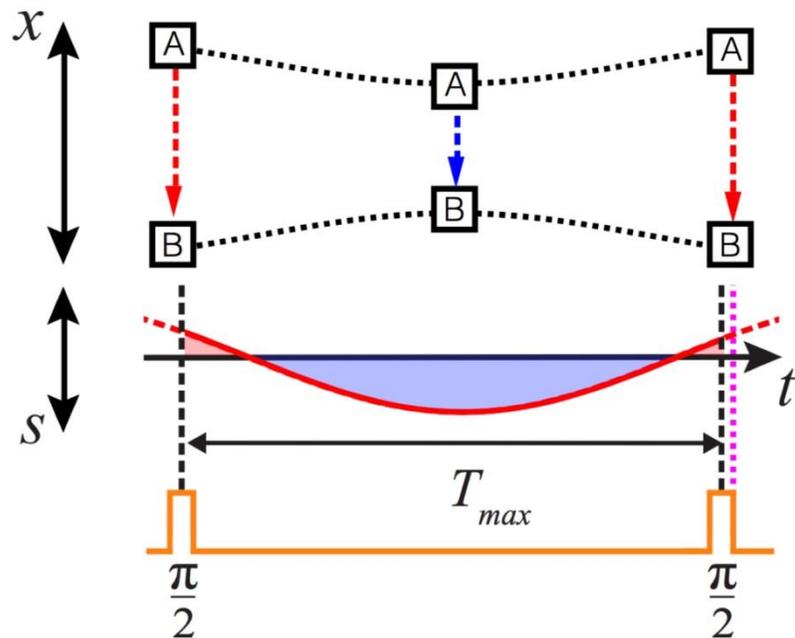
$\sigma \sim 10^{-19} / \sqrt{\text{Hz}}$

At $f = 1/2T$

Frequency tuning: dynamical decoupling

Can change spectroscopic read-out: use dynamical decoupling (DD) to move ideal sensitivity to other f

Long Ramsey

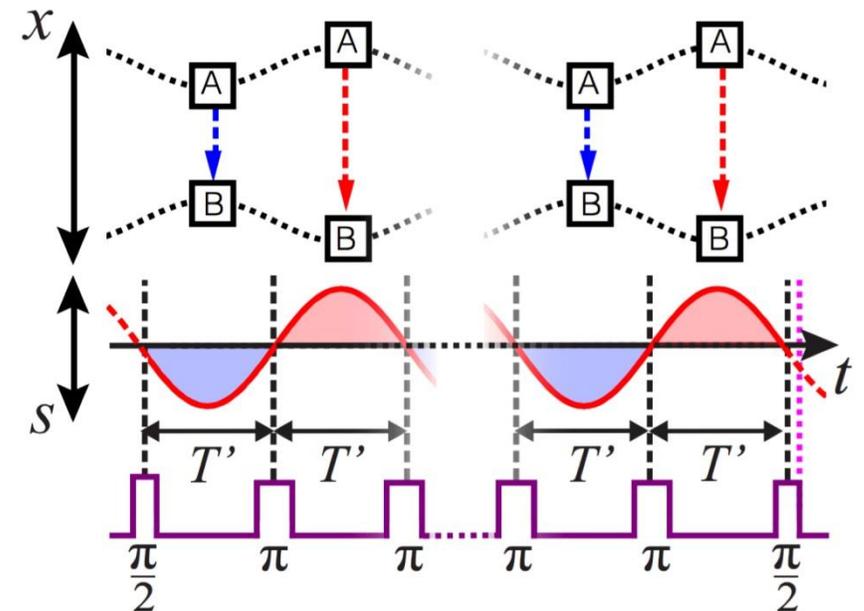


DD: match atomic read-out with high-frequency GW

$$s \rightarrow \bar{s} = \int dt s(t) F(t)$$

DD filter function

Dynamical decoupling

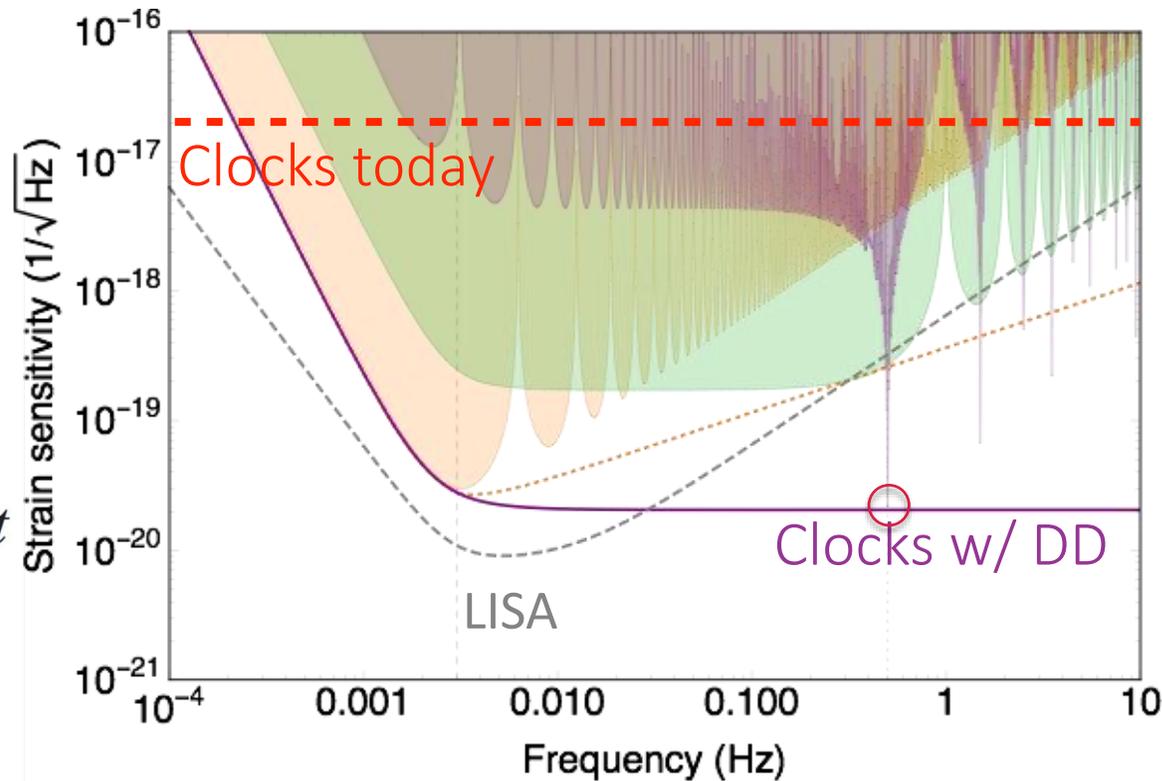
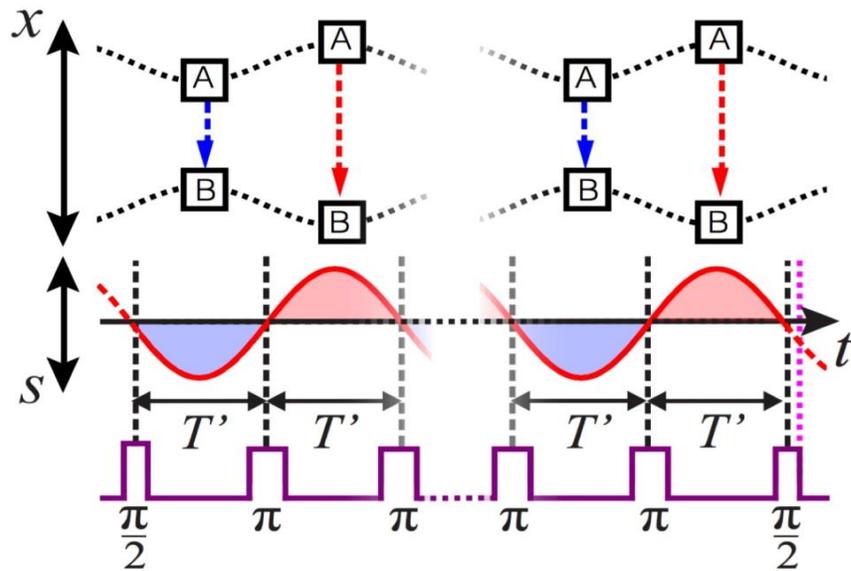


Sensitivity with Dynamical Decoupling technique

Signal: $s_{DD} = \int dt s(t)F(t)$ ← DD filter function matches specific GW frequency

Noise: $\sigma_{min}(\tau) = \frac{1}{\nu} \sqrt{\frac{1}{TN}}$

Dynamical decoupling sequence:



$N = 7 \times 10^6$
of Sr atoms

$d = 50 \times 10^6$ km
Satellite distance

$T = 1$ s
Ramsey time

$\sigma_{min} \sim 10^{-20} / \sqrt{\text{Hz}}$
At $f = 1/2T$

Optical power requirements

Laser noise enters through the phase-lock between satellites A and B. Total noise:

$$\sigma^2 = \frac{1}{(2\pi\nu)^2 T \tau} \left(\frac{1}{N} + \frac{1 - e^{-B\tau}}{2} \frac{T}{\tau} \left(\frac{\Delta_L}{B} + \frac{h\nu}{P} B \right) \right)$$

atom projection noise ←

↓
laser linewidth

↓
shot noise in PLL

T: clock interrogation time

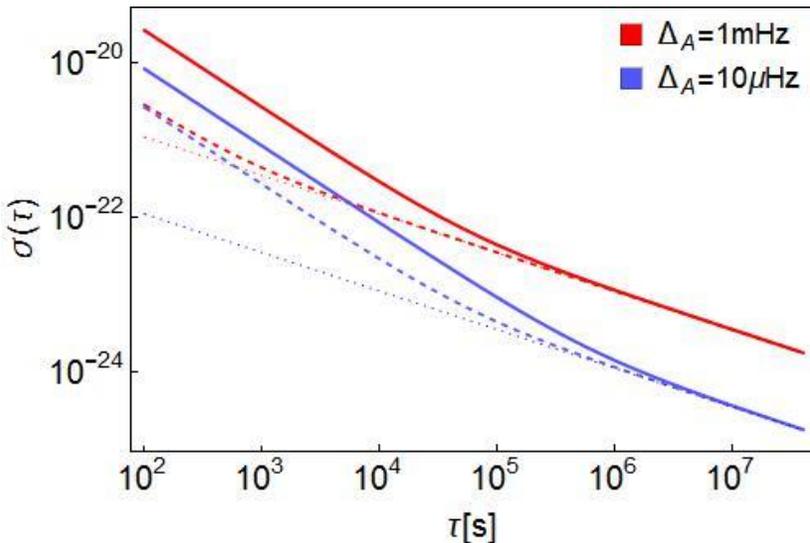
τ: total measurement time

N: # of atoms

B: phase-lock loop bandwidth

Δ_L: Laser linewidth

P: power



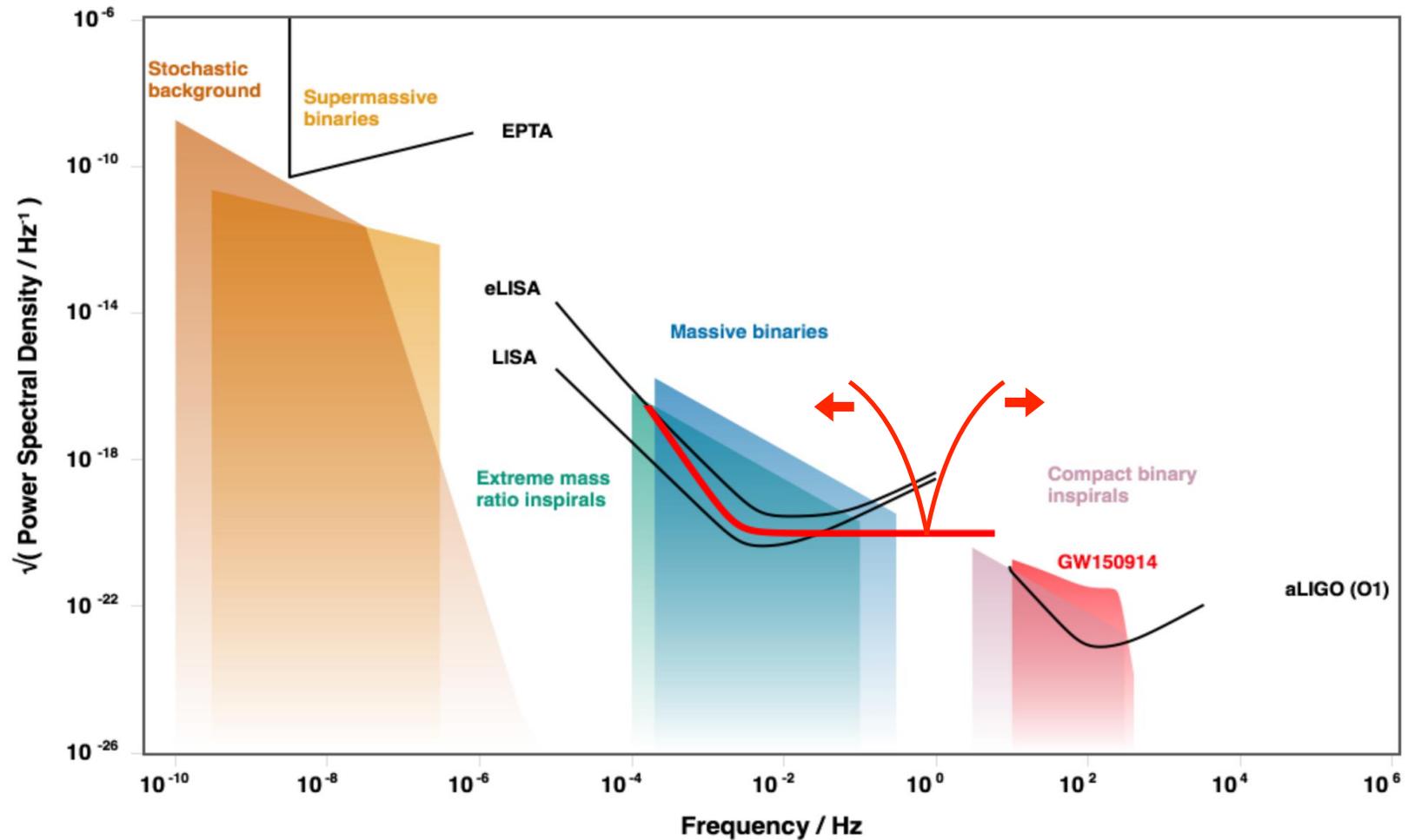
PLL: White frequency noise → white phase noise, averages down faster.

Atom projection noise limited after $\tau \lesssim 1\text{d}$ for $\Delta_L = 1\text{ Hz}$, received laser power $P \sim 10^{-10}\text{ W}$.

Emitted power for $d = 50 \times 10^6\text{ km}$: $P \sim 1.4\text{ W}$.

Sources

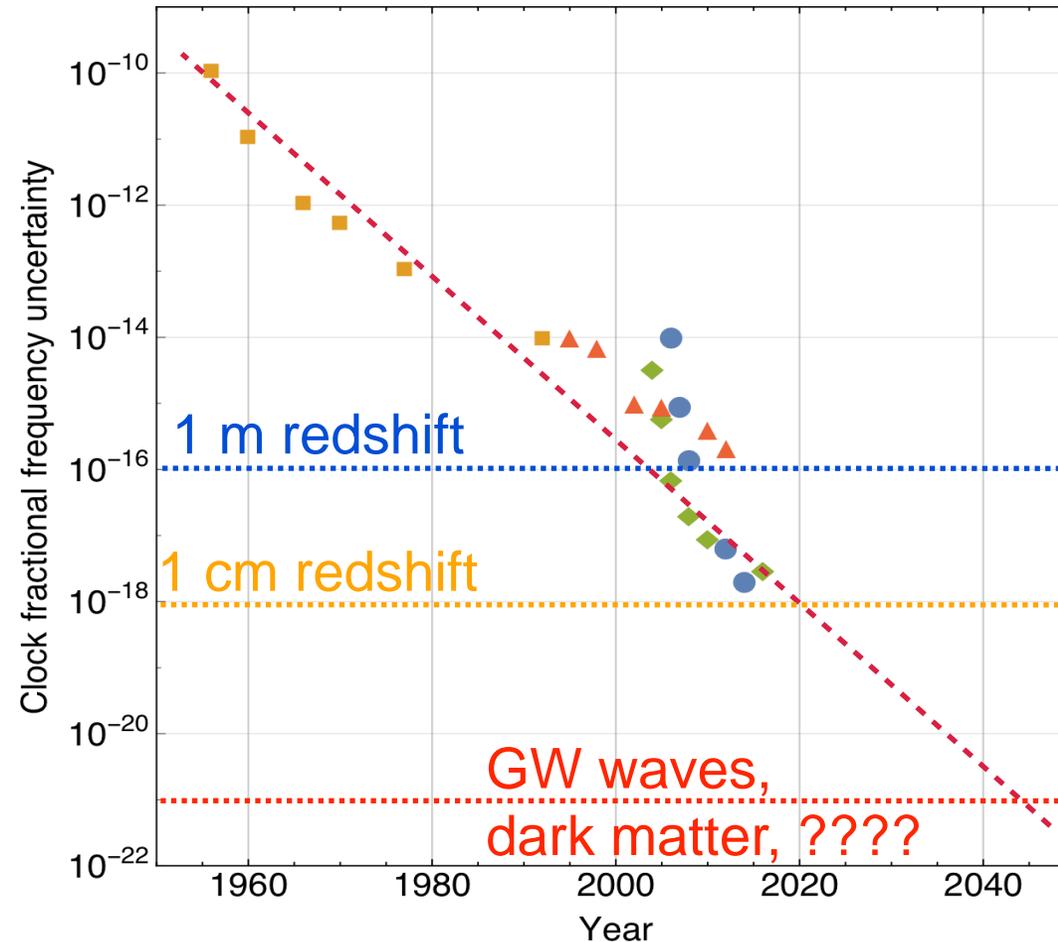
- Can bridge range between LISA and LIGO
- New and potentially strong sources possible in deciHz-range
- Can track inspirals throughout GW chirp



Plot from <http://rhcole.com/apps/Gwplotter/>

Fundamental physics with increased precision

- Cs beam
- ▲ Cs fountain
- ◆ Ion optical clock
- Sr optical lattice clock



Key advantages

- Different systems: utilize quantum control of atoms for frequency tunability
- Different detection method: not shot noise limited, but atom projection noise limited
- Optical power requirements very flexible
- Only 2 satellites required, due to low sensitivity to laser noise
- Can be hybridized with interferometric space missions like LISA, serves as a complementary detector

Potential future improvements

- Entangled atomic states (spin-squeezing, GHZ), can be used to bypass the standard quantum limit for short interrogation times: $\sqrt{N} \rightarrow N$
Bohnet et. al., Nature Photonics 8, 731–736 (2014)
- Entanglement between clocks for further increase the sensitivity of a clock network based detector
Komar et. al., Nature Physics 10, 582 (2014)
- Optimized clock measurement protocols.
Kessler et. al., PRL 112, 190403 (2014)
- Switching to narrower clock transitions using other isotopes or atomic species.
Santra et. al., PRL 94, 173002 (2005)
- Using LMT schemes of atomic fountains for better low-frequency sensitivity
Norcia et. al., PRA 96, 042118 (2017)

Summary

- Optical lattice clocks can be used for GW detection, $h \sim 10^{-20} / \sqrt{\text{Hz}}$
- Effective Doppler shift measurement by correlated clock spectroscopy in space
- Tunability: ideal sensitivity in range 3 mHz – 10 Hz
- Narrow-band detection of continuous sources
- Possible future improvements from atomic technology and quantum control
- Sensitivities comparable to LISA with realistic improvement of ground-based clock technology, can be hybridized with LISA

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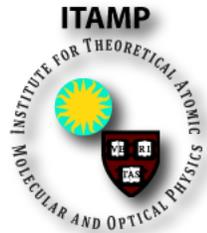
Misha
Lukin



Ron
Walsworth



Jun Ye



& discussions with Avi Loeb, Mark Kasevich, Jason Hogan



S. Kolkowitz, I. Pikovski, N. Langellier, M. D. Lukin, R. L. Walsworth, J. Ye.

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