# The little hierarchy problem at the LHC

Andrea Romanino SISSA/ISAS

 $m{\circ}$  Known fields:  $g_A^\mu$   $W_a^\mu$   $B^\mu$   $Q_i$   $u_i^c$   $d_i^c$   $L_i$   $e_i^c$ 

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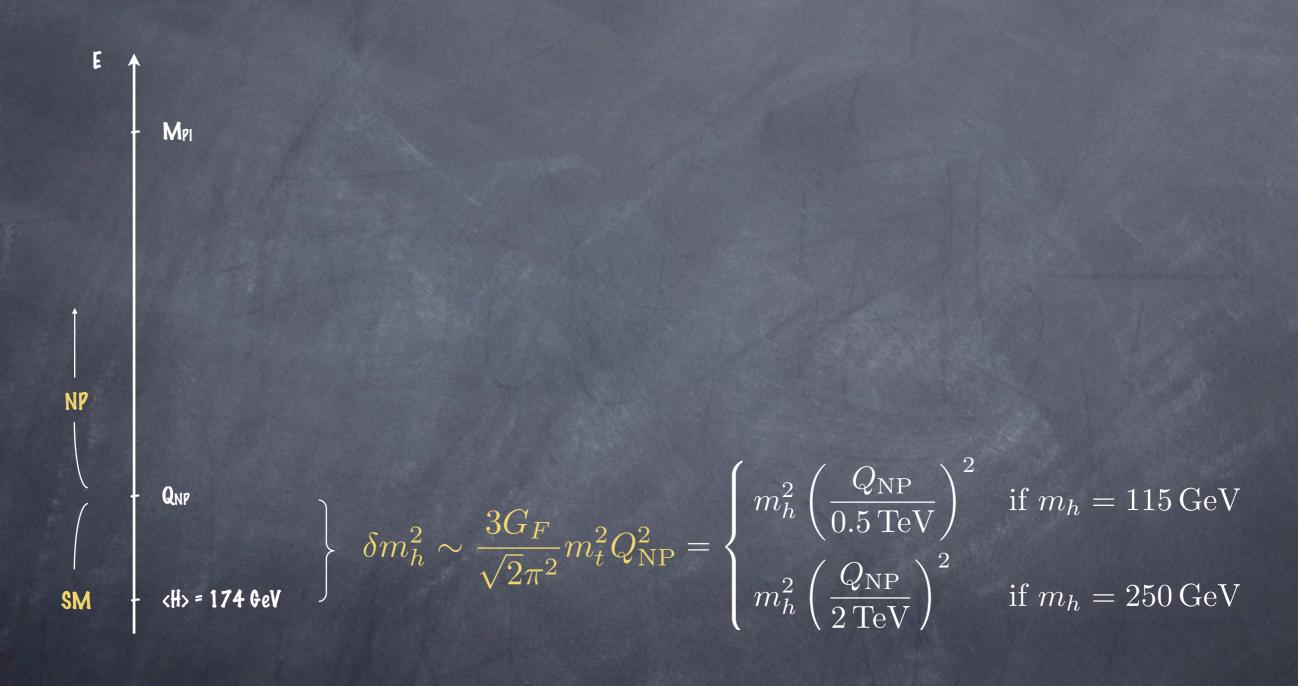
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- Experimental "problems" of the SM:
  - Gravity
  - Dark matter
  - Baryon asymmetry
- Experimental "hints" of physics beyond the SM
  - Neutrino masses
  - Quantum number unification
- Theoretical puzzles of the SM:
  - @ <H> « MPI
  - Family replication
  - Small Yukawa couplings, pattern of masses and mixings
  - Gauge group, no anomaly, charge quantization, quantum numbers
- Theoretical problems of the SM:
  - Naturalness / unitarity problem
  - Cosmological constant problem
  - Strong CP problem

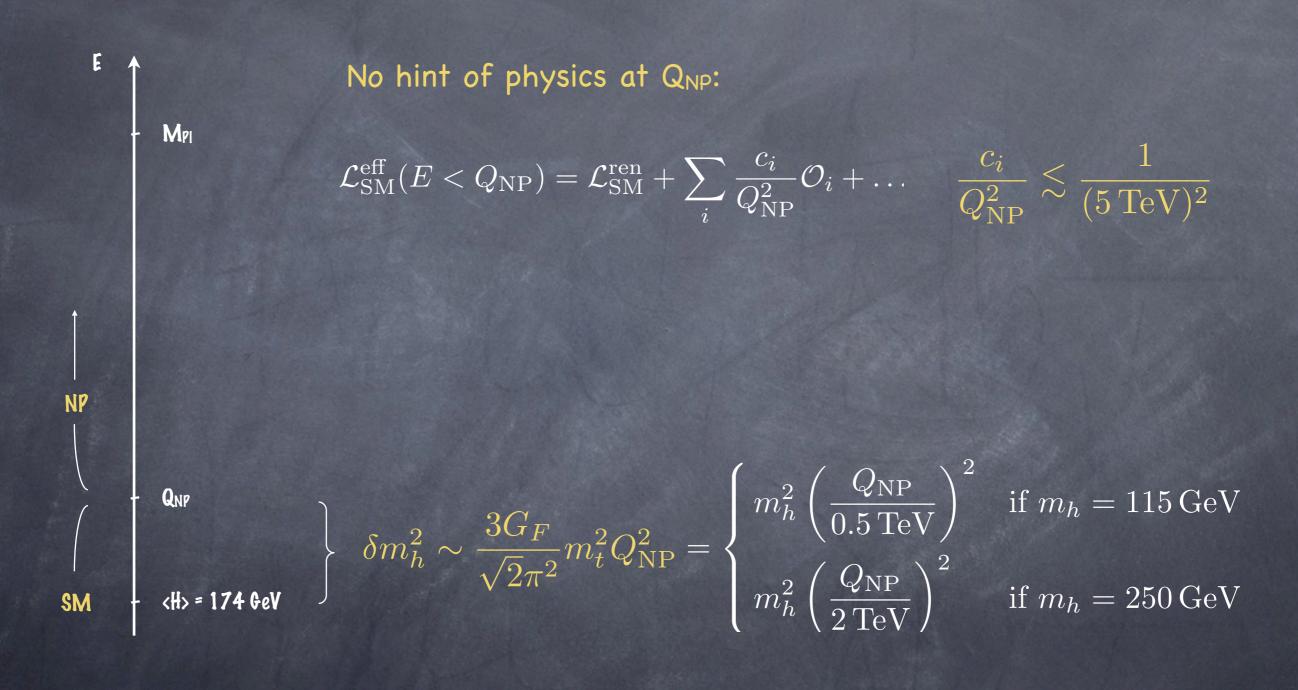
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- Many options; how do they confront the Little Hierarchy problem?

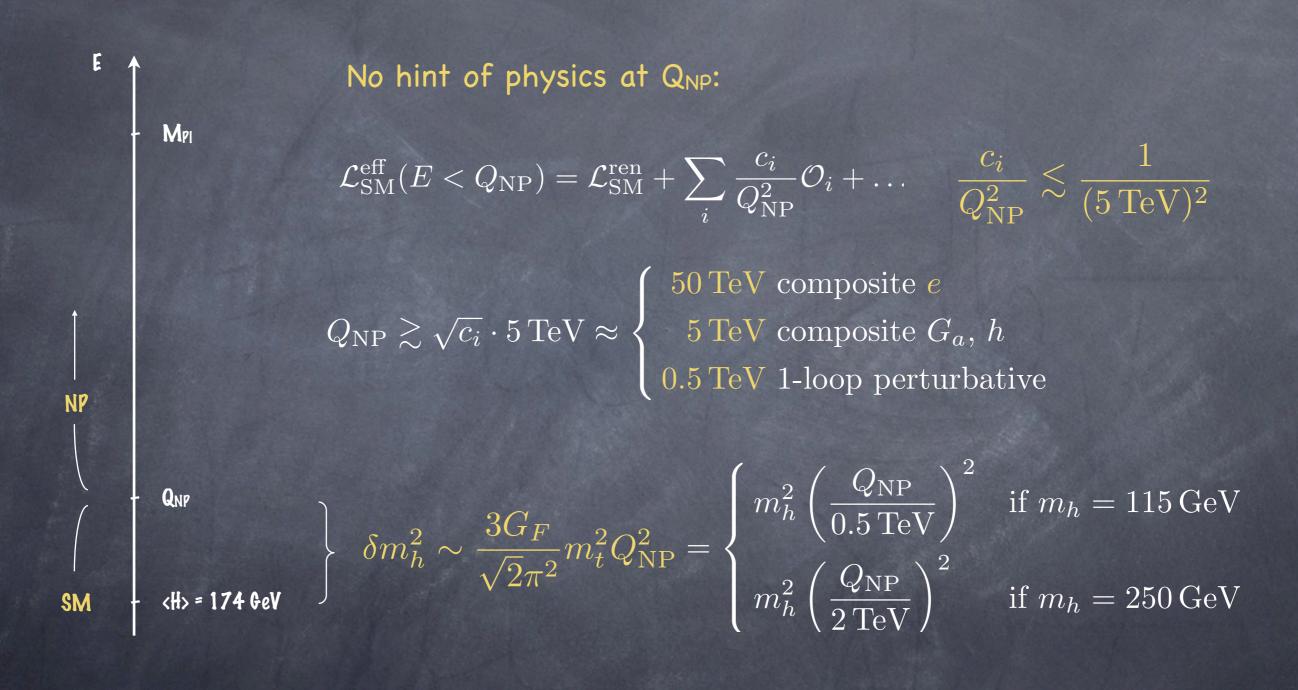
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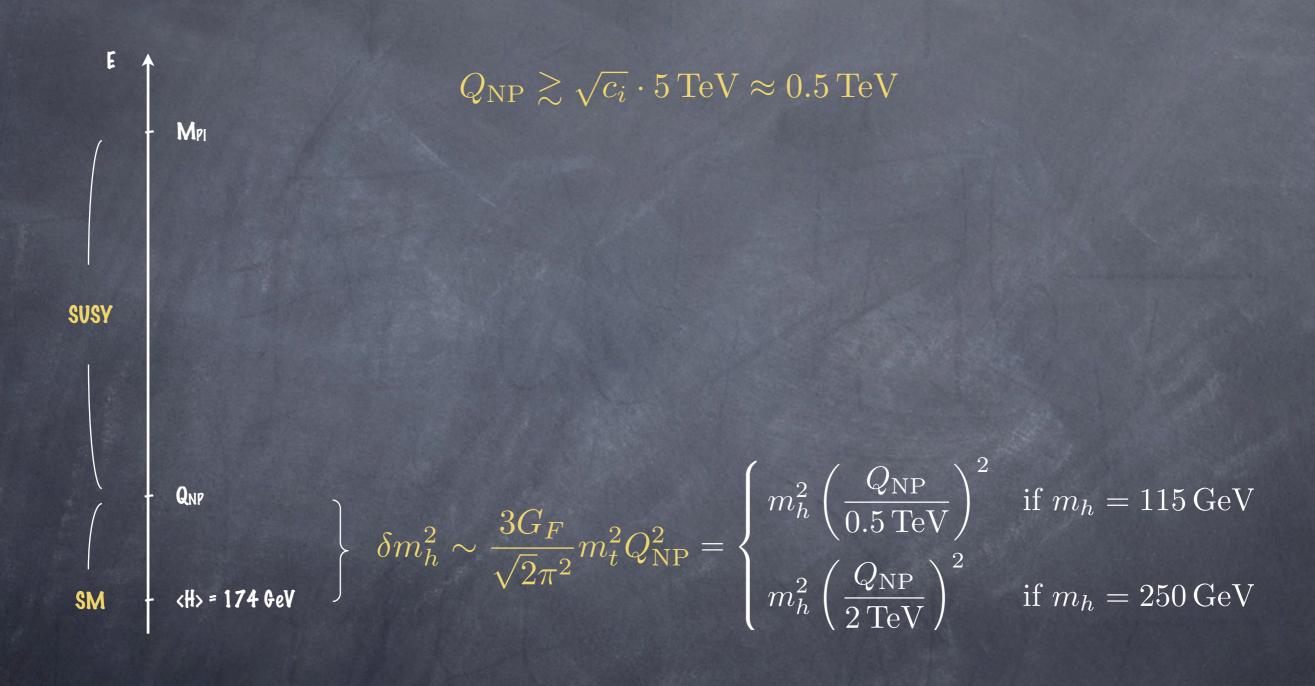
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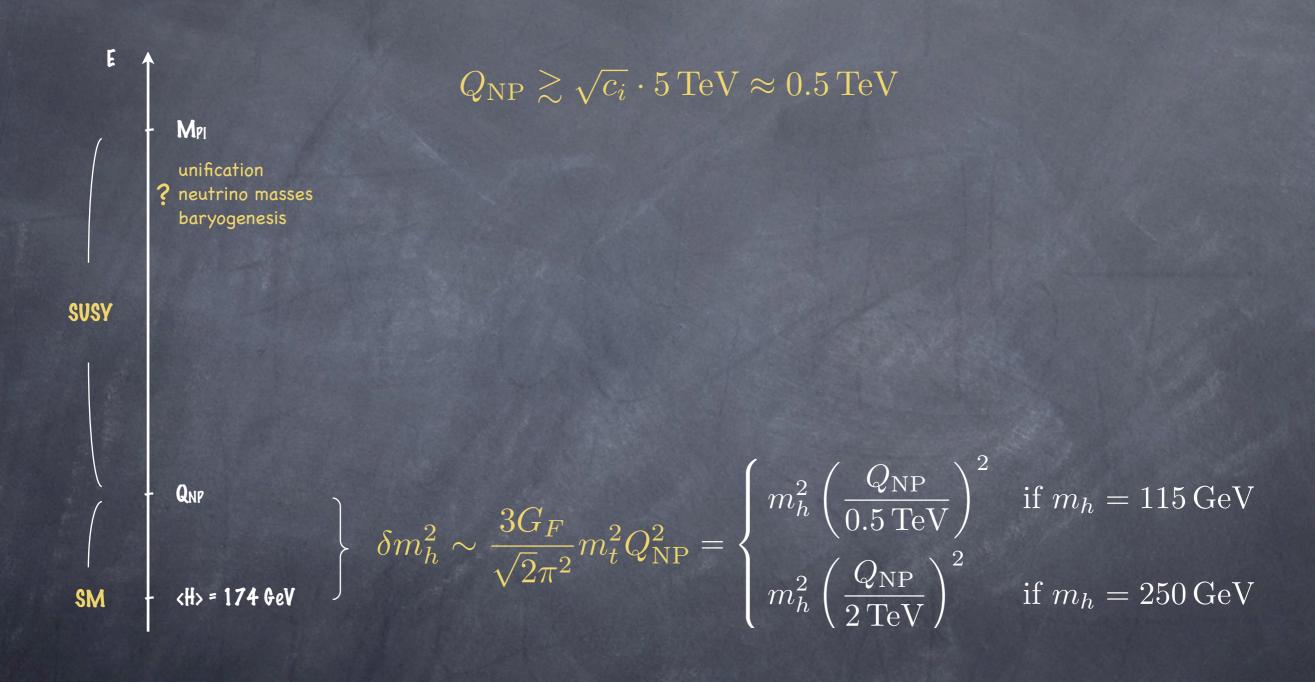
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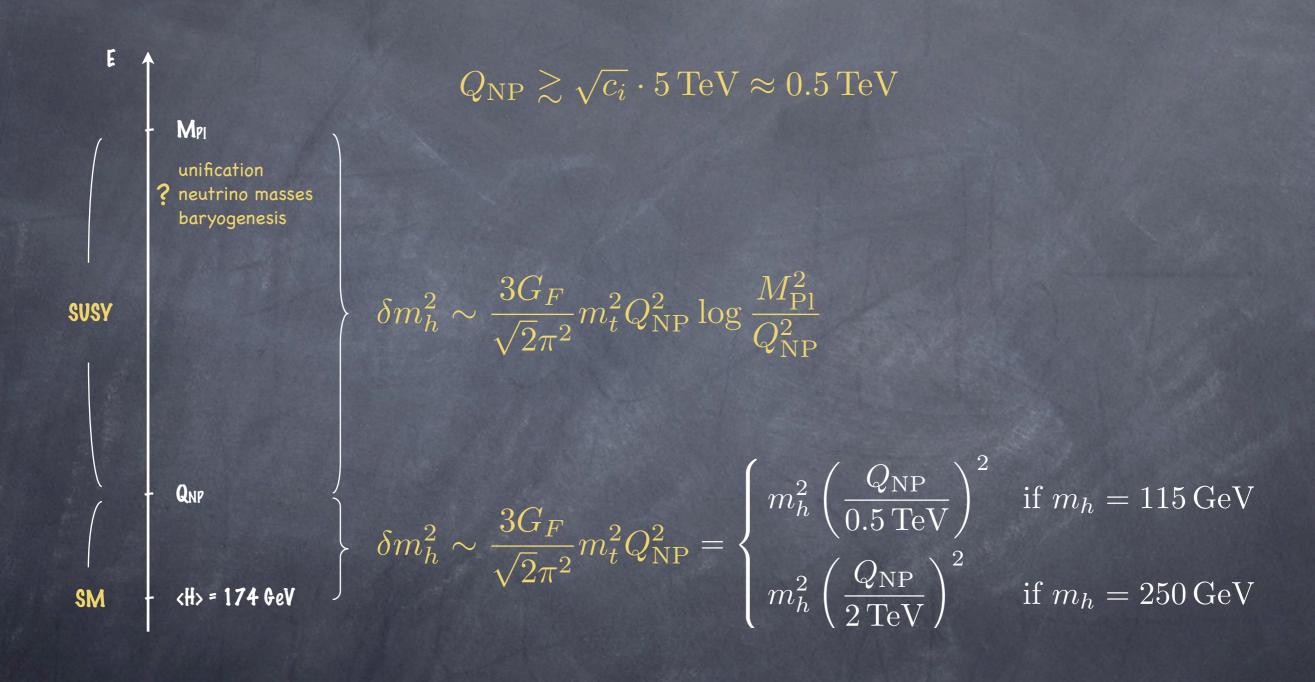
#### MSSM



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# Fine-tuning in the MSSM

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$$\approx -2\left(m_{h_u}^2 (M_0) + |\mu|^2\right) + 2\delta m_{h_u}^2$$

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Indirect bound on stop mass stronger (but direct one is also relevant)

$$(114 \,\text{GeV})^2 < m_h^2 < M_Z^2 \cos^2 2\beta + \frac{3}{4\pi^2} h_t^2 m_t^2 \log \frac{\tilde{m}_t^2}{m_t^2} \Rightarrow \text{FT} \sim 50 \div 100$$

## A comment on scanning procedures

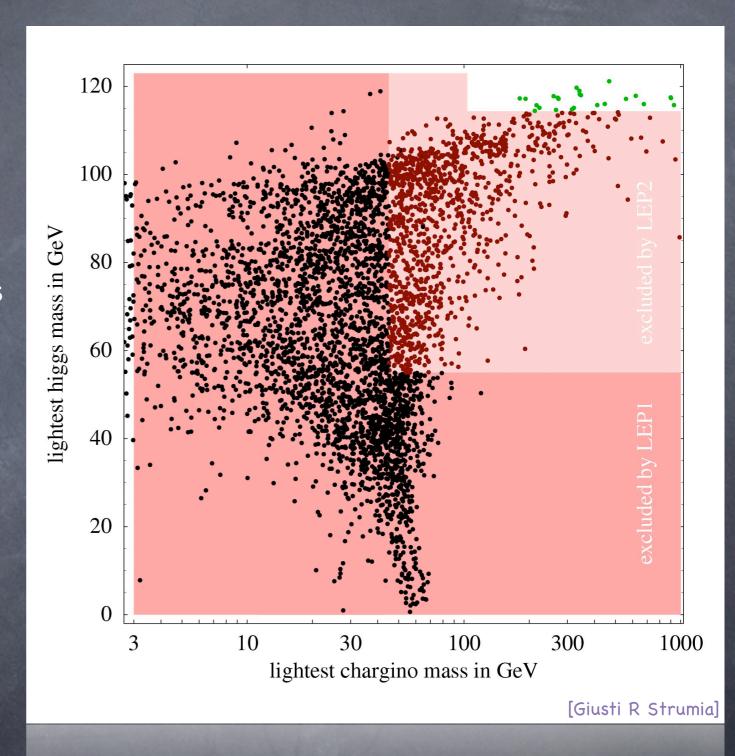
$$M_Z^2 \approx -2\left(m_{h_u}^2(M_0) + |\mu|^2\right) + 2\,\delta m_{h_u}^2$$

The FT problem then may introduce a bias in numerical scans of the MSSM parameter space: the (necessary) cancellation is forced to take place between  $\mu^2$  and all the rest

Example: LSP is rarely an Higgsino (work in progress)

## What is left?

- Quantitative measure of naturalness nicely taking into account and combining all the considerations above
  - Scan the relative sizes of SUSY parameters and the SM parameters in their ranges
  - Set the overall scale of SUSY parameters from <H> = 174 GeV
  - Calculate SUSY spectrum and compare with experiment
- Few O(1%) of points satisfy all experimental constraints



## Beyond MSSM: xMSSM

- Minimal extension: λSH<sub>u</sub>H<sub>d</sub> (symmetries forbid μH<sub>u</sub>H<sub>d</sub>)
  - harmless (unification OK)
  - welcome (μ = λ<S> ≈ susy scale)
- Spectrum: h H → h₁ h₂ h₃, A → a₁ a₂, N₁...N₄ → N₀ N₁...N₄
- Help with FT from  $(114\,{\rm GeV})^2 < m_h^2 < M_Z^2\cos^22\beta + \frac{3}{4\pi^2}h_t^2m_t^2\log\frac{\tilde{m}_t^2}{m_t^2}$ :
  - $\lambda_h = \frac{g^2 + g^{'2}}{4} \cos^2 2\beta + \frac{\lambda^2}{2} \sin^2 2\beta + \text{loops} \quad \text{gain limited by poles}$

 $\lambda(10 \text{ TeV}) < 3 \text{ (EWPTs) best, } \lambda(M_{GUT}) < 3 \text{ (unification) OK}$ 

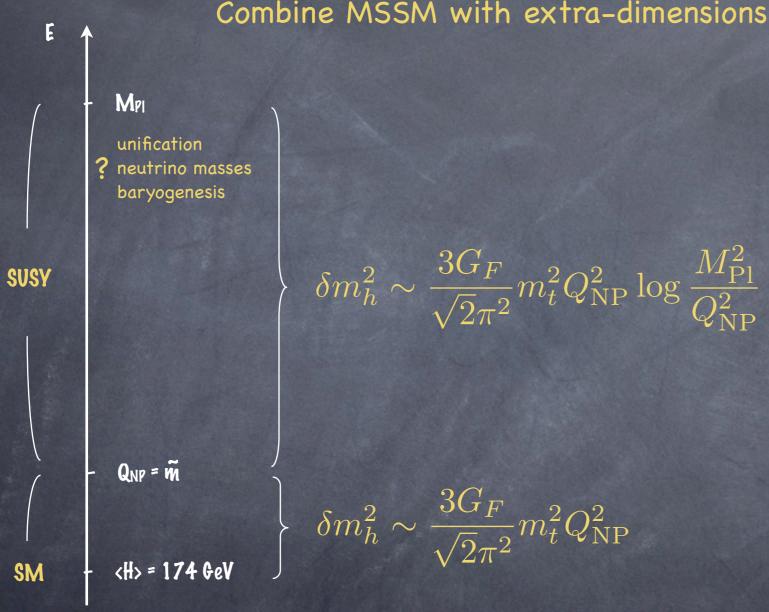
- $m_h^2 < (114\,{
  m GeV})^2$  hidden Higgs: h ightarrow aa ightarrow 4X (ma protected by PQ, R)
- Persistent FT from
  - direct bounds on SUSY partners
  - arranging the invisible decay [Shuster Toro hep-ph/0512189]

Invisible Higgs decays: h → aa → 4X

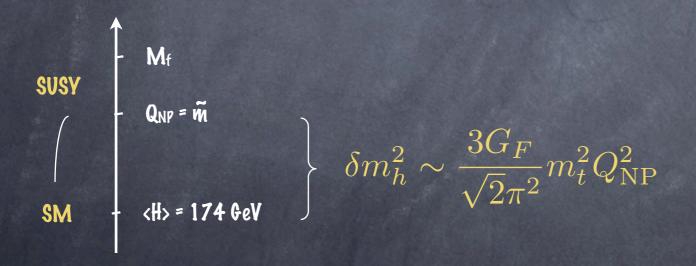
- 3leptons → multileptons from additional steps in chargino/neutralino decays
  - $\odot$  C<sub>1</sub>+N<sub>2</sub> and then

  - ©  $C_1 \rightarrow N_0 + l + v$  (5l overall) or even  $C_1 \rightarrow N_1 + l + v \rightarrow N_0 + 3l + v$  (7l overall)
- Deviation from MSSM coupling relations: VVh = VHA =  $\sin^2(\alpha \beta)$ , VVH = VhA =  $\cos^2(\alpha \beta)$  (optimistic)
- $\odot$  Z' if  $\mu$  is protected by a gauge symmetry

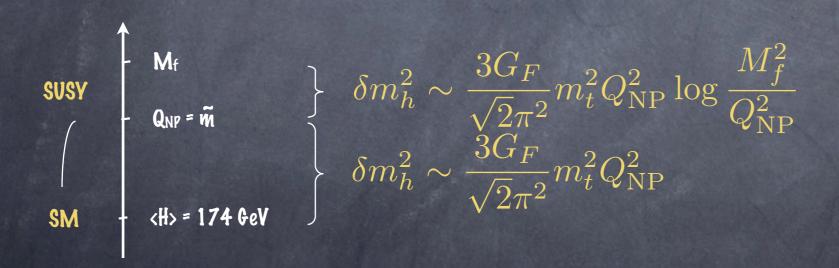
Combine MSSM with extra-dimensions not far from TeV



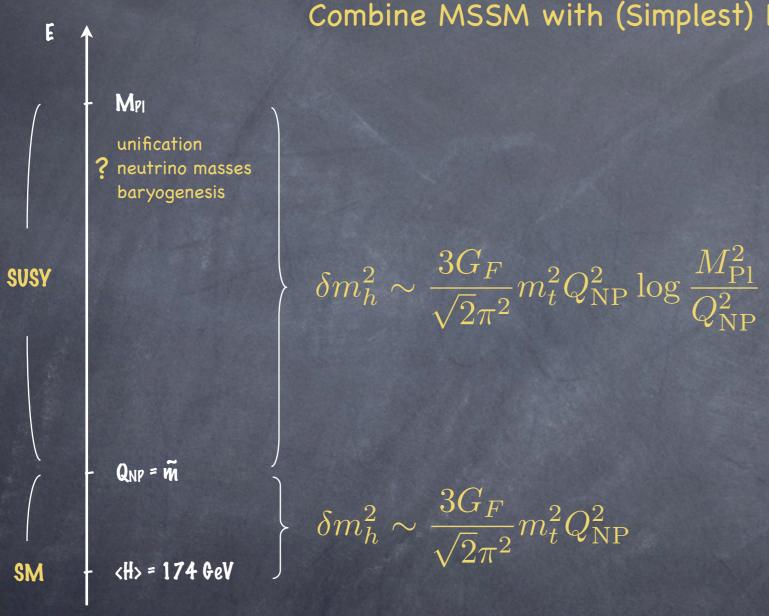
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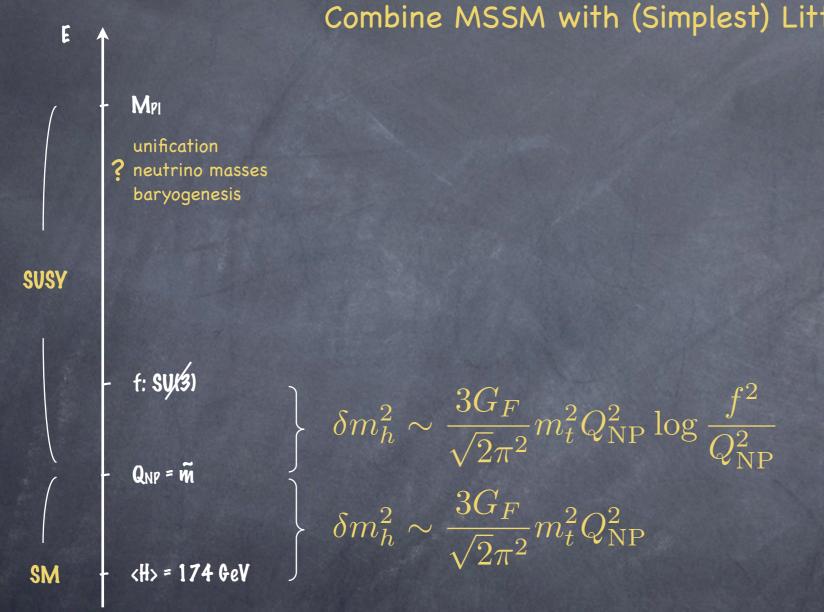
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Combine MSSM with (Simplest) Little Higgs



Combine MSSM with (Simplest) Little Higgs



# SSM with $Q_3 = (t_L b_L) = gaugino$

 $\odot$  G = SU(5) x G'<sub>SM</sub> broken to the diagonal G<sub>SM</sub>

[Cai Cheng Terning, arXiv:0806.0386]

- Extra vector superfields ≈ Q+Q̄, g' W' B'
- $gA_i^{\dagger}T_A^{ij}\lambda_A\psi_j \to \lambda_t H_d^{\dagger}QT^c$

## Higgsless (technicolor & C):  $G_a$  Goldstones of global  $SU(2)_L \times SU(2)_R$  EWPT not calculable or off; recent progress via duality to 5D

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- Protect Higgs mass from Q<sub>NP</sub>: h is also a pseudo-NGB ( $\Leftrightarrow$  shift symmetry H(x)  $\rightarrow$  H(x) + c). Explicit breaking by  $\lambda_t$   $\lambda_H$  g:

$$\delta m_h^2 \sim \frac{3G_F}{\sqrt{2}\pi^2} m_t^2 Q_{\rm NP}^2 = m_h^2 \left(\frac{Q_{\rm NP}}{0.5 \,{\rm TeV}}\right) \text{ for } m_h = 115 \,{\rm GeV}$$

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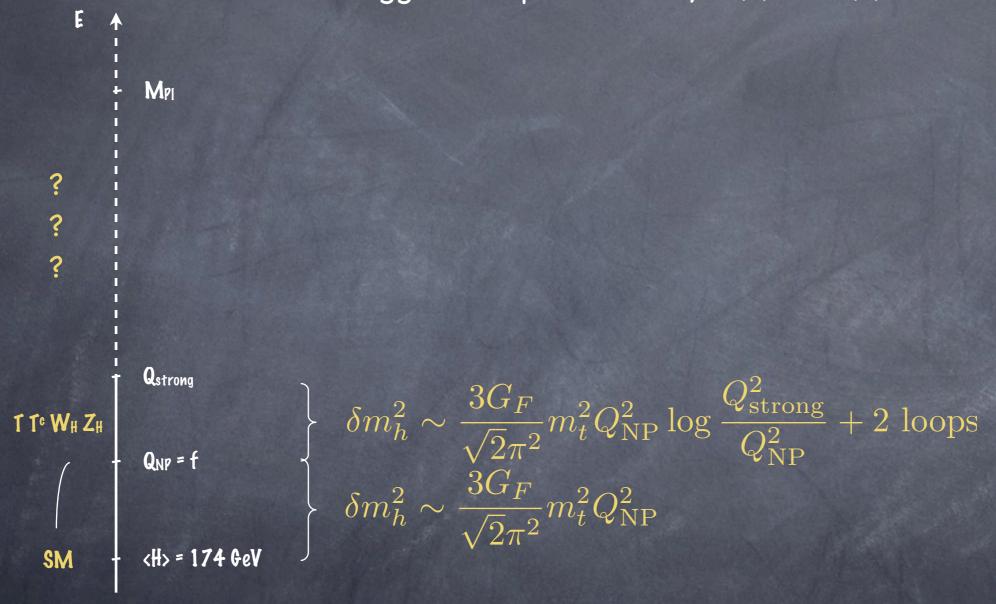
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- More clever explicit breaking ("collective breaking"): Little Higgs
  - $m{\circ}$  no 1-loop  $Q_{\mathrm{NP}}^2$  terms (exact-NGB unless 2+ non-vanishing couplings)
  - the top (gauge, Higgs) loop must be cancelled at a lower scale (= global symmetry breaking scale f « Q<sub>strong</sub>) by same statistics partners

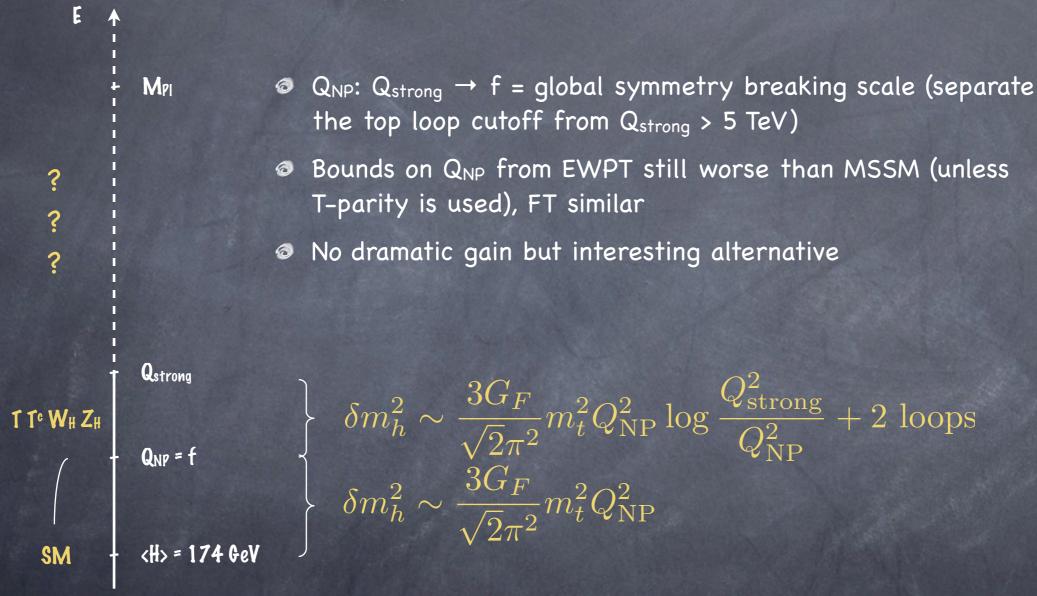
# Little Higgs

Higgs mass protected by  $H(x) \rightarrow H(x) + c$ 



## Little Higgs

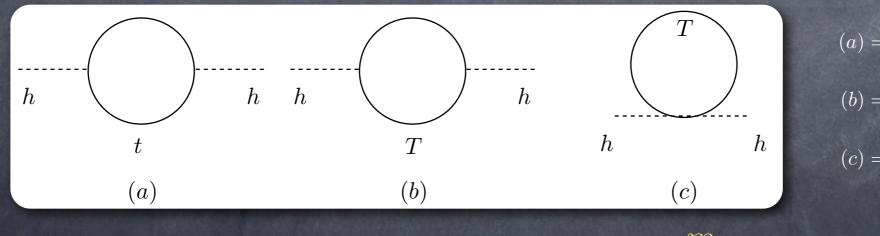
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#### LH @ LHC

- Observe the partners responsible for the divergence cancellation

  - T, T<sup>c</sup>: single production (bWT) dominates (b pdf up to ≈0.2)
  - additional (++) Higgs states
- Observe the divergence cancellation



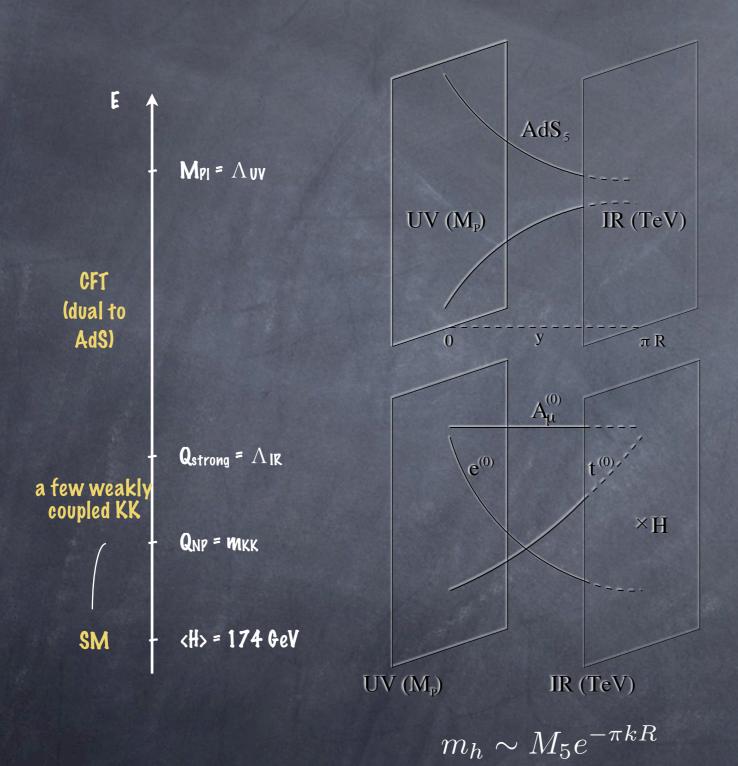
$$(a) = -6\lambda_t^2 \int \frac{d^4k}{(2\pi)^4} \frac{1}{k^2},$$

$$(b) = -6\lambda_T^2 \int \frac{d^4k}{(2\pi)^4} \frac{1}{k^2 - m_T^2},$$

$$(c) = +6\frac{\lambda_T}{f} \int \frac{d^4k}{(2\pi)^4} \frac{m_T}{k^2 - m_T^2}$$

$$-\lambda_t^2 \qquad \qquad -\lambda_T^2 \qquad \qquad +\lambda_T \frac{m_T}{f} \qquad = 0$$

# Warping and composite Higgs



k = curvature

- RS + bulk fermions + H as (A<sub>5</sub>)<sub>0</sub> + deconstruction = Little Higgs + UV completion
- m<sub>H</sub> protection: collective breaking =
   bc breaking of 5D gauge symmetry
- 4D dual: UV brane: elementary IR brane: composite (H, t<sub>R</sub>)
- $Q_{\text{strong}} > 5 \text{ TeV as usual}$   $M_{KK} > \text{TeV}$ , watch  $Z \rightarrow bb$
- Gauge coupling unification in a novel way (but limited calculability)

## @LHC (a first look)

- Keep only first excitation:
  - $\odot$  ISM> =  $\cos \varphi$  | elem> +  $\sin \varphi$  | comp>
  - $|KK\rangle = -\sin\varphi | elem\rangle + \cos\varphi | comp\rangle$
- Production:

  - $\odot$  SM<sub>3</sub> needs to be substantially composite:  $t_R$  (bW fusion) or  $V_{long}$  (DY) (analogous to LH)
- Decay:

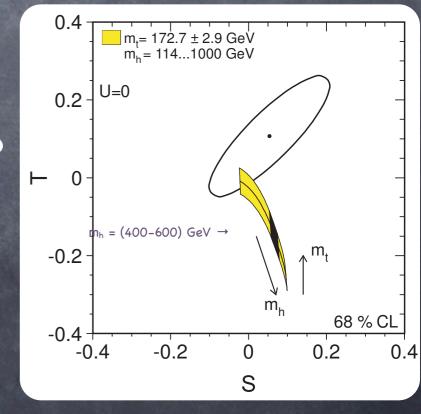
  - $\circ$  also: (gluon)<sub>KK</sub>  $\rightarrow$  t<sub>R</sub>t<sub>R</sub>
  - possibly lepton excitations (if open)

## Back to the residual hierarchy

$$\delta m_h^2 \sim \frac{3G_F}{\sqrt{2}\pi^2} m_t^2 Q_{\rm NP}^2 = \begin{cases} m_h^2 \left(\frac{Q_{\rm NP}}{0.5\,{\rm TeV}}\right)^2 & \text{if } m_h = 115\,{\rm GeV} \\ m_h^2 \left(\frac{Q_{\rm NP}}{2\,{\rm TeV}}\right)^2 & \text{if } m_h = 250\,{\rm GeV} \end{cases}$$

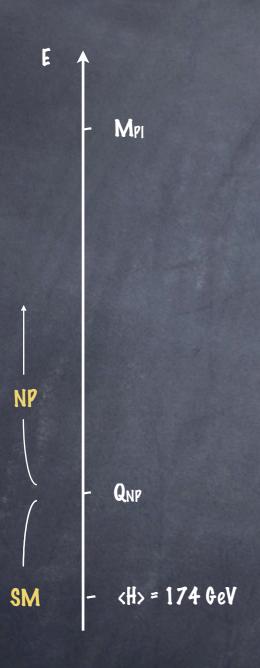
$$Q_{\rm NP} \gtrsim \sqrt{c_i} \cdot 5\,{\rm TeV} \approx \begin{cases} 50\,{\rm TeV} \text{ composite SM fermions} \\ 5\,{\rm TeV} \text{ composite Higgs} \\ 0.5\,{\rm TeV} \text{ 1-loop perturbative} \end{cases}$$

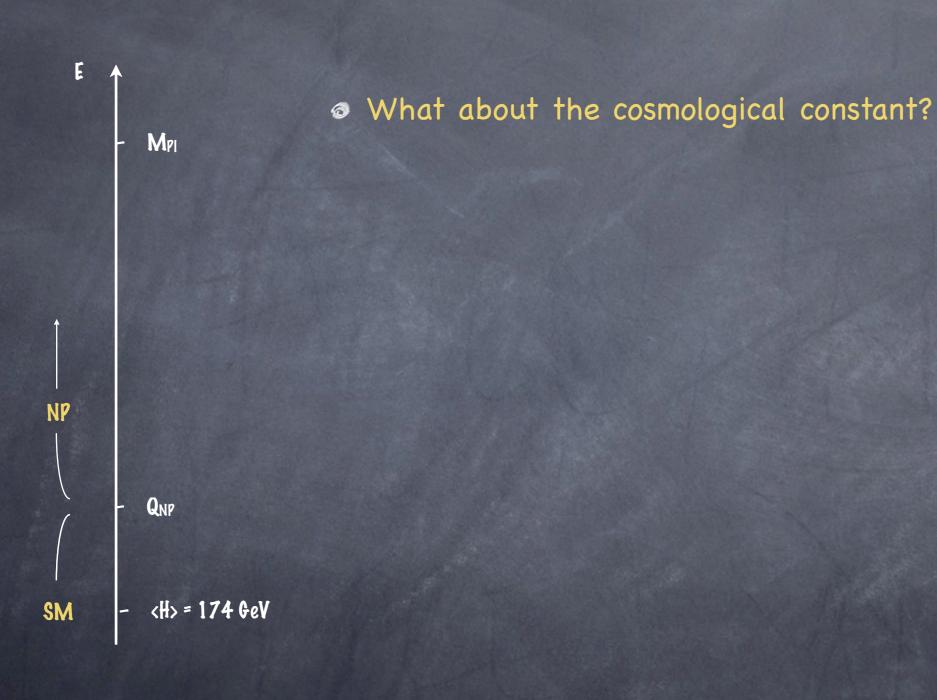
- m<sub>h</sub> = 500 GeV would help; disfavoured by EWPTs only
   within the SM
- Cancel SM heavy Higgs contributions to EWPT with NP (goodness off SM + light H fit accidental but not too much fine-tuned)
- Generic prediction of NP giving  $\Delta T = 0.25\pm0.1$

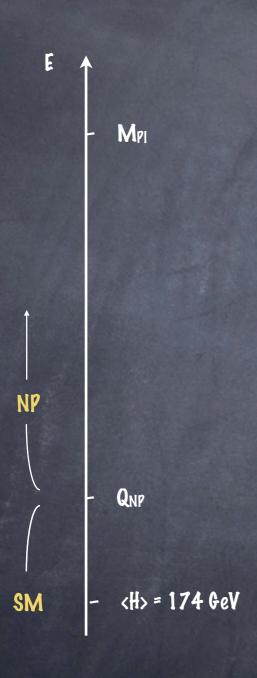


### An inert Higgs

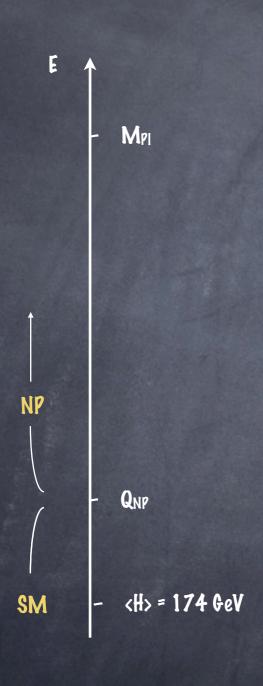
- H<sub>1</sub> (h): usual Higgs (but heavier): EWSB, M<sub>W</sub> M<sub>Z</sub>, m<sub>f</sub>
- ⊕ H₂ (H, A, H±): inert Higgs (60 GeV-1TeV): no vev, no coupling to fermions (H₂→-H₂), gives  $\Delta T = 0.25\pm0.1$
- DM candidate for m<sub>H</sub> ≈ 70 GeV (LEP?)
- @ Pair production: pp  $\rightarrow$  W\*  $\rightarrow$  H+H, H+A or pp  $\rightarrow$  Z\*  $\rightarrow$  H+H-, HA
- Decay into the lightest + gauge bosons (no fermions) → charged leptons in the final states
- UV completion?



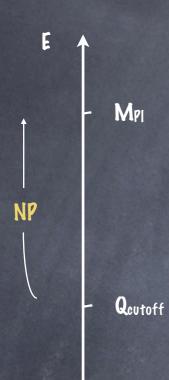




- What about the cosmological constant?
- If the m<sub>h</sub> naturalness criterium is irrelevant, what are the observable consequences?

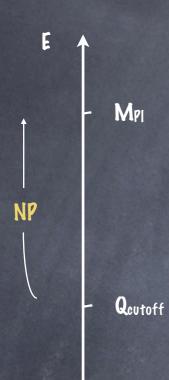


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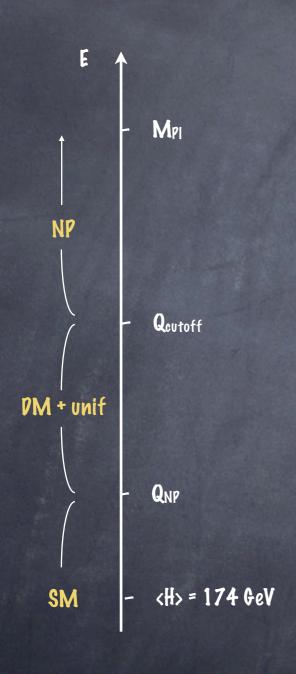
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- Dark matter still motivates NP at the TeV scale

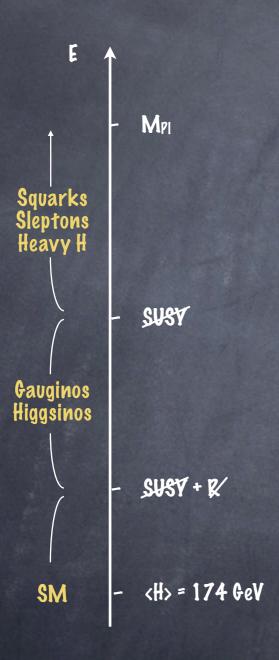


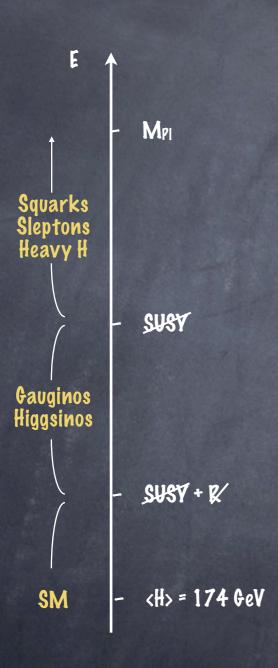
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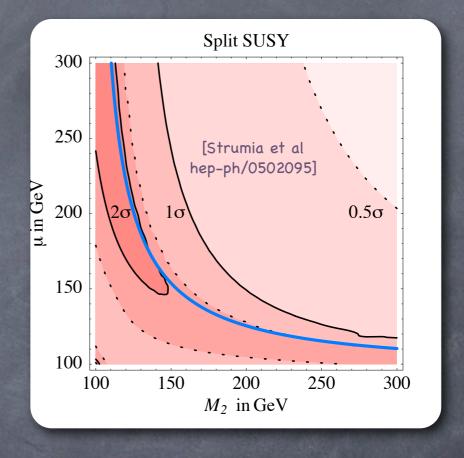


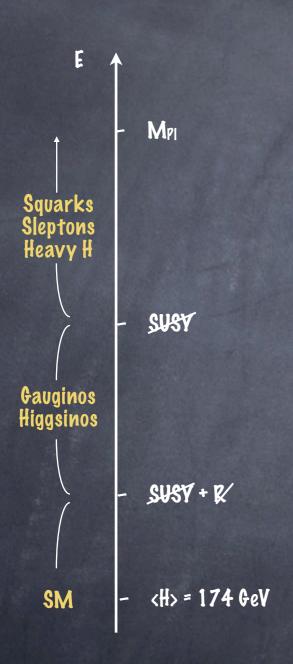
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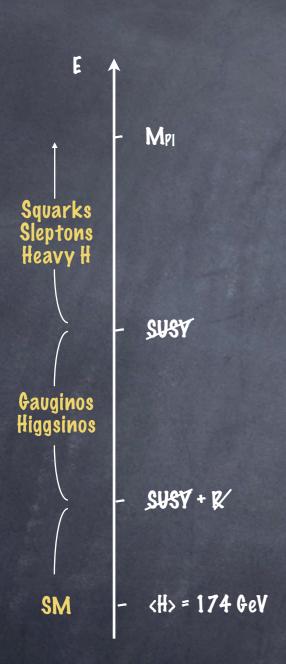


- $\odot$  DM:  $\mu$  < 1.2 TeV (M<sub>1</sub> < M<sub>2</sub>), mostly Bino favourable for LHC
- No bounds from EWPTs

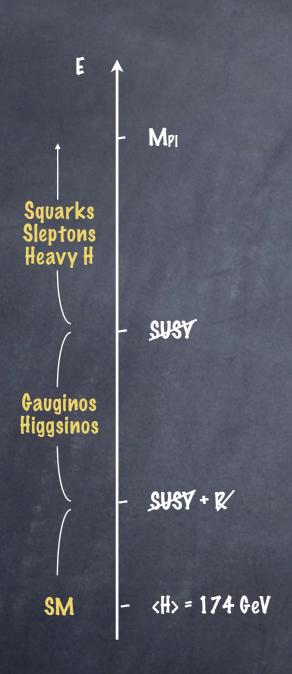




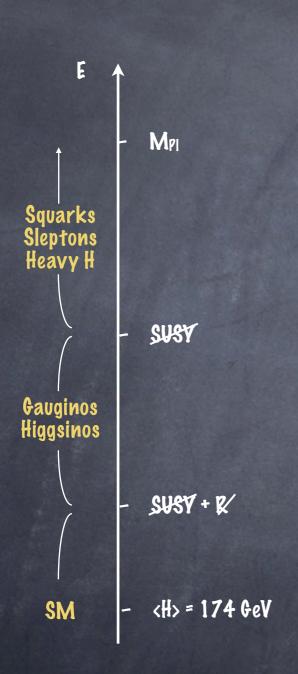
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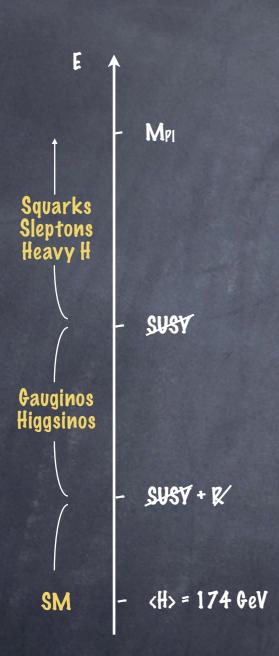


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- Wilder: stopping gluinos (1-2 jets in any direction from denser parts of the detector + m.e.), displaced vertexes (low m), charge flips



### Summary

- Is a % tuning really worth worrying?
- If not, NP could as well be out of reach of the LHC
- Barring independent arguments (e.g. DM)
- Useful and fruitful guideline within models addressing the naturalness issue
- Surprises are not unlikely

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