



NORDITA

MEASURING the HUBBLE CONSTANT with KILONOVAE

Mattia Bulla

with L. Issa, S. Dhawan, M. W. Coughlin and many more

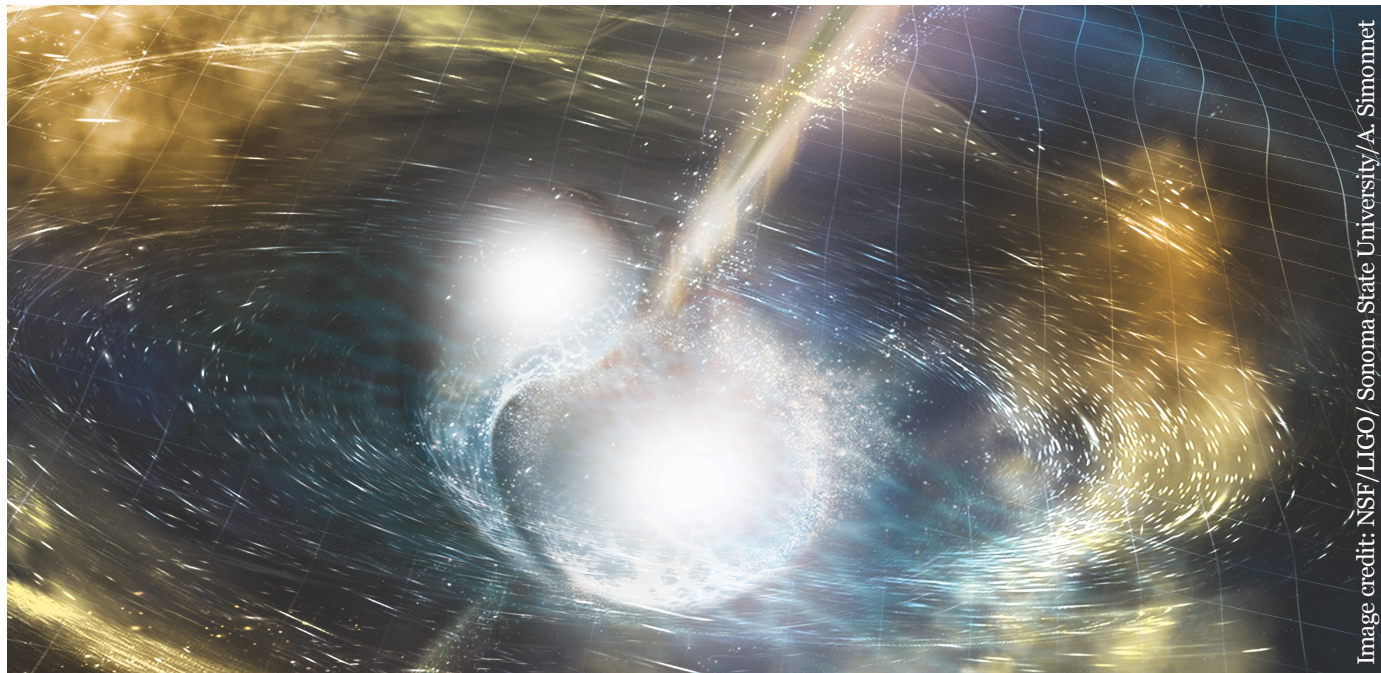
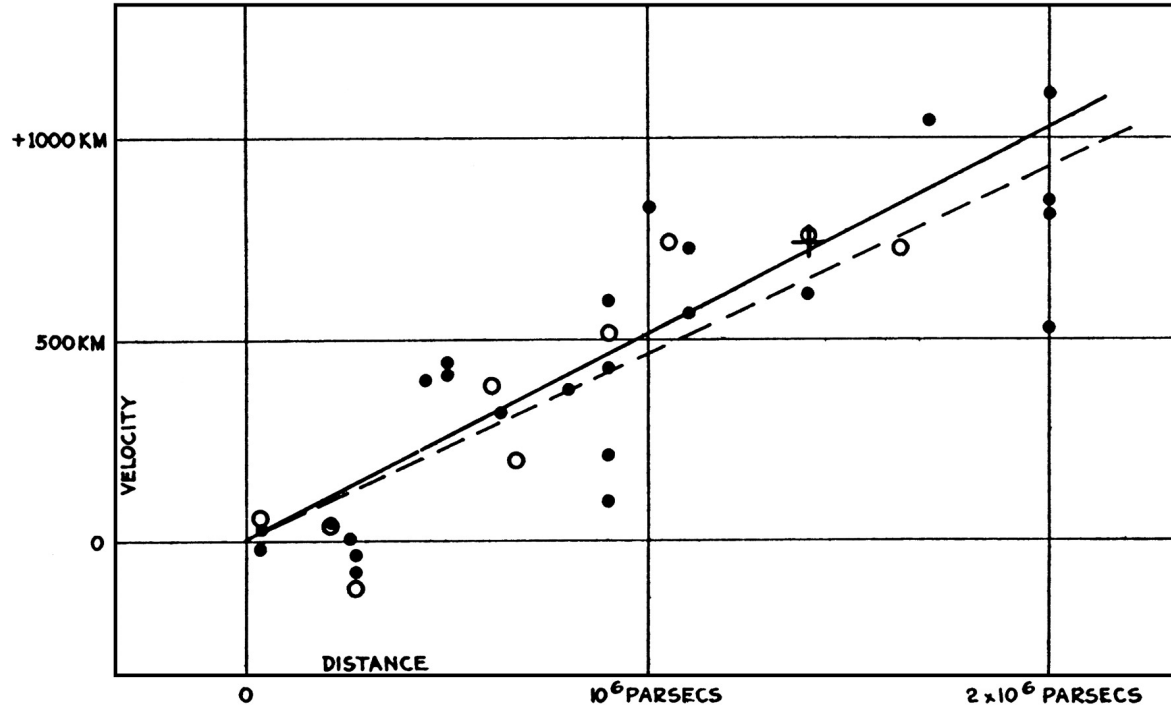


Image credit: NSF/LIGO/ Sonoma State University/ A. Simonnet

The Hubble constant H_0

The expansion rate of our Universe

Hubble 1929



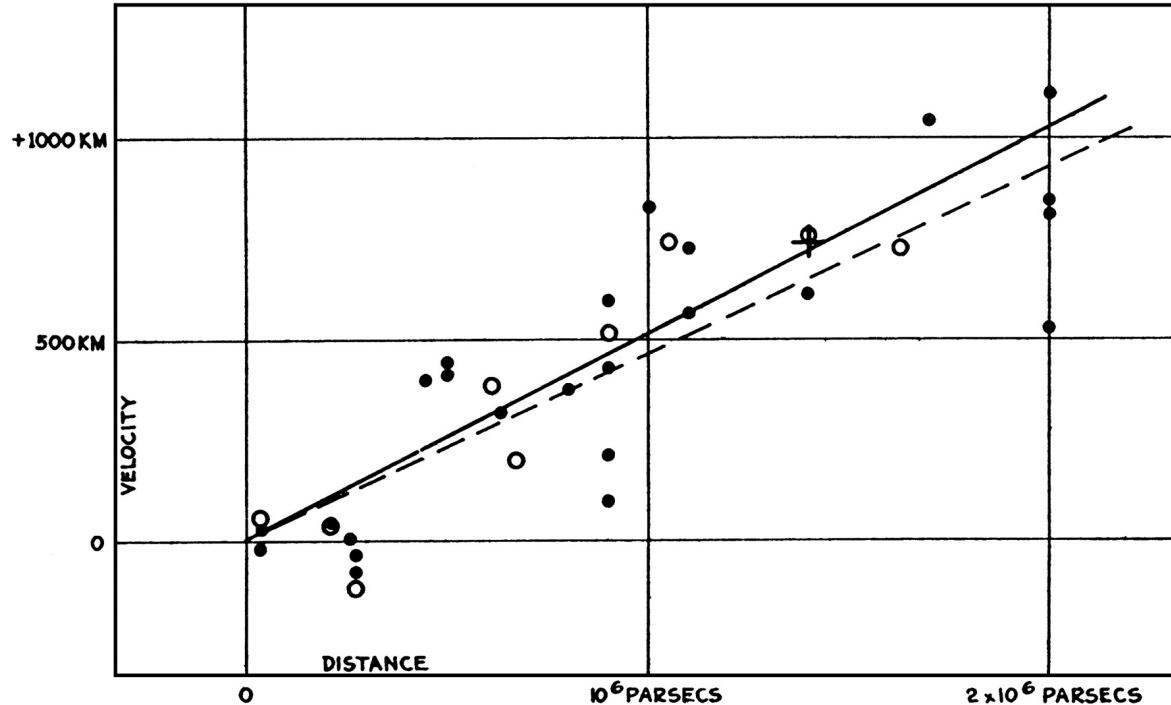
$$H_0 = \frac{\text{Velocity}}{\text{Distance}}$$

$$H_0 \sim 500 \text{ km s}^{-1} / \text{Mpc}$$

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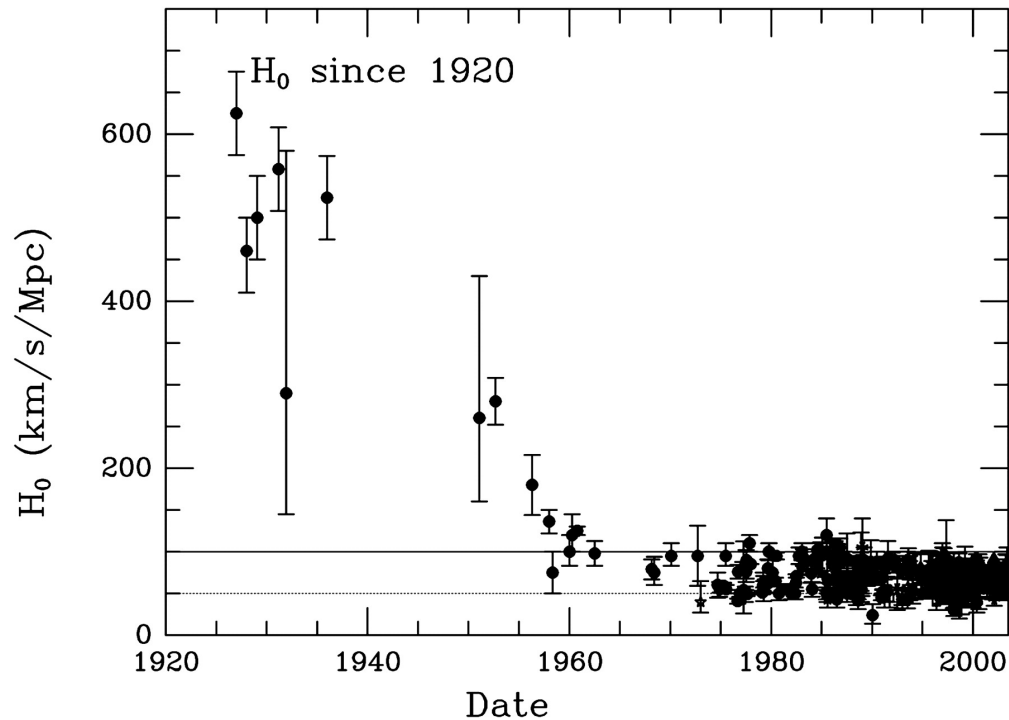
$$\text{Age of the Universe} = \frac{1}{H_0}$$

~ 2 billion years ??

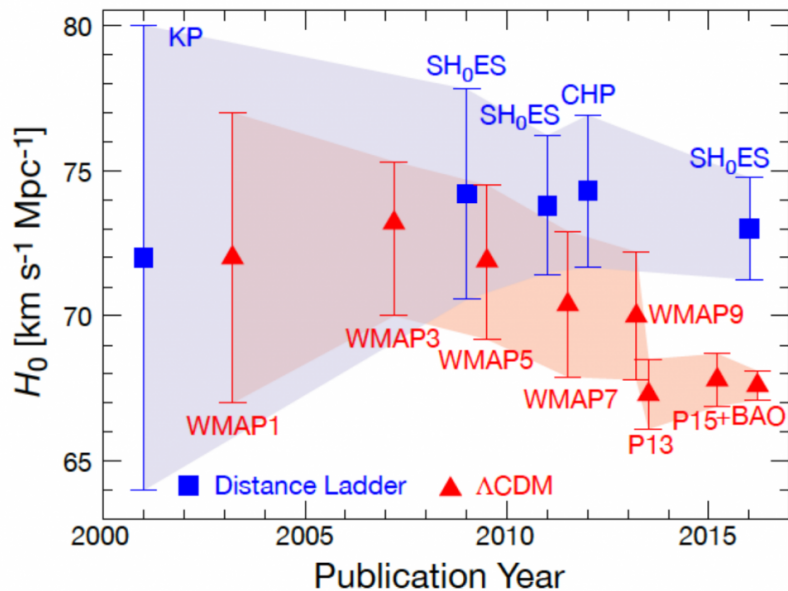
The Hubble constant H_0

The expansion rate of our Universe

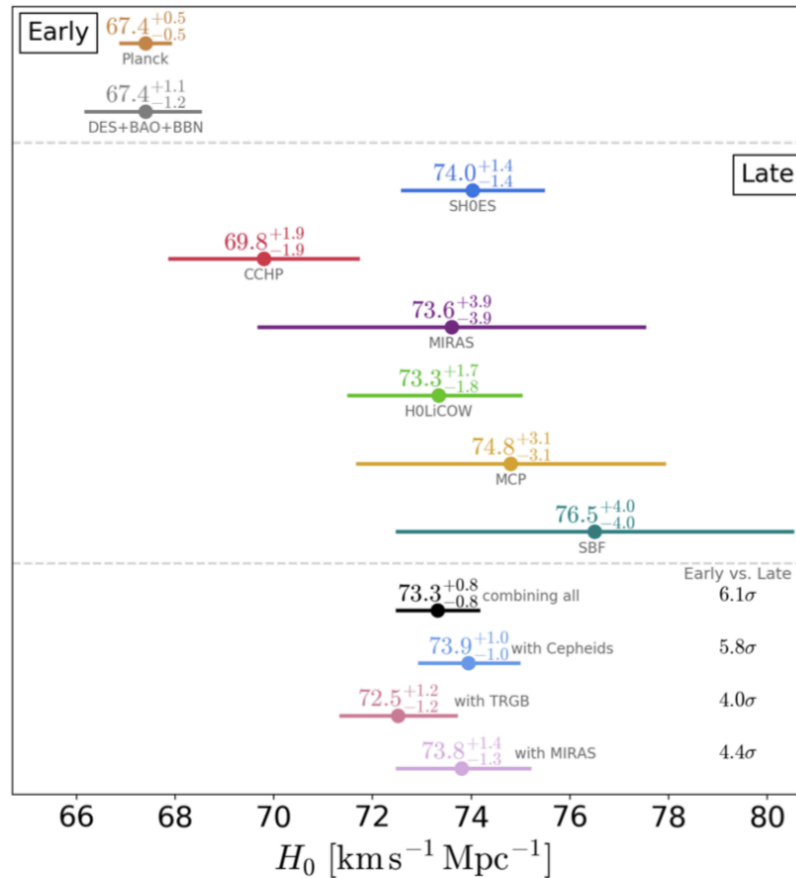
Kirshner 2004



Freedman 2017



The Hubble tension



Gravitational Waves as “Standard Sirens”

Schutz 1986; Holz & Hughes 2005

Determining the Hubble constant from gravitational wave observations

Bernard F. Schutz

Department of Applied Mathematics and Astronomy,
University College Cardiff, PO Box 78, Cardiff CF1 1XL, UK

I report here how gravitational wave observations can be used to determine the Hubble constant, H_0 . The nearly monochromatic gravitational waves emitted by the decaying orbit of an ultra-compact, two-neutron-star binary system just before the stars coalesce are very likely to be detected by the kilometre-sized interferometric gravitational wave antennas now being designed¹⁻⁴. The signal is easily identified and contains enough information to determine the absolute distance to the binary, independently of any assumptions about the masses of the stars. Ten events out to 100 Mpc may suffice to measure the Hubble constant to 3% accuracy.

Identification of the source / host galaxy

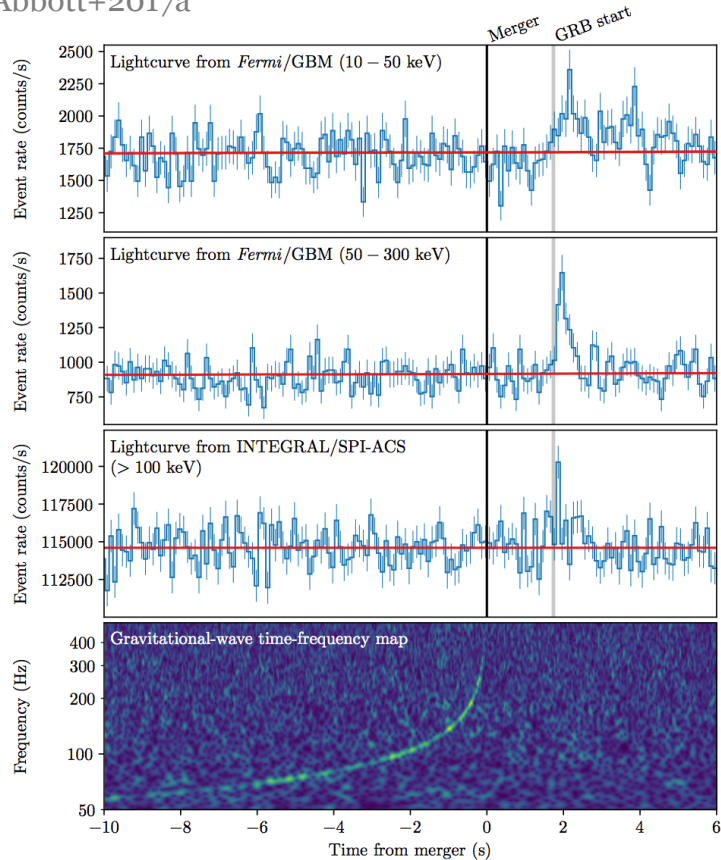
$$H_0 = \frac{\text{Velocity}}{\text{Distance}} = \frac{[\text{speed of light}] \times \text{Redshift}}{\text{Distance}}$$



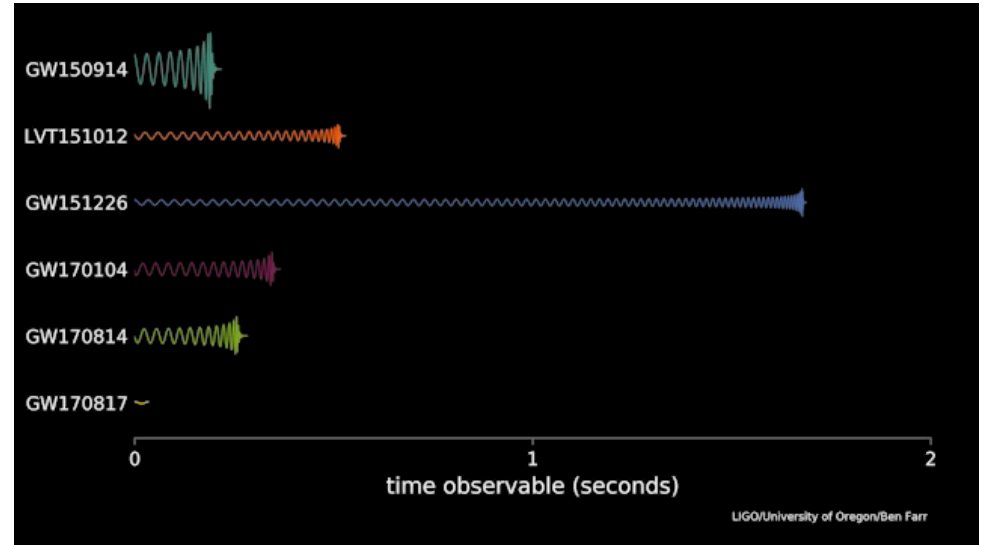
GW 170817 / AT 2017gfo

The first Electromagnetic Counterpart of a Gravitational Wave event

Abbott+2017a



Gravitational-wave signal consistent with the merger of **two neutron stars**

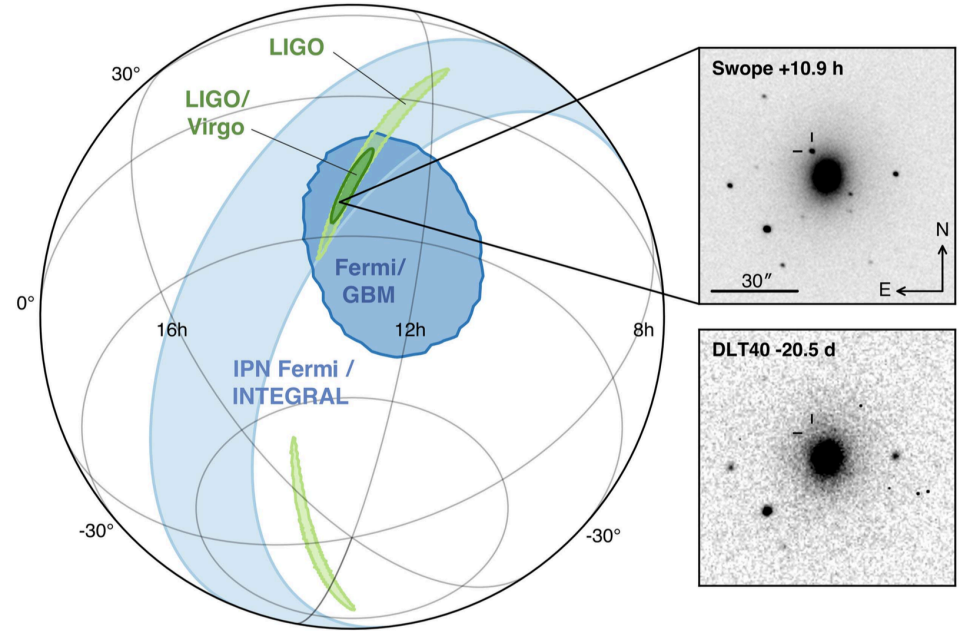
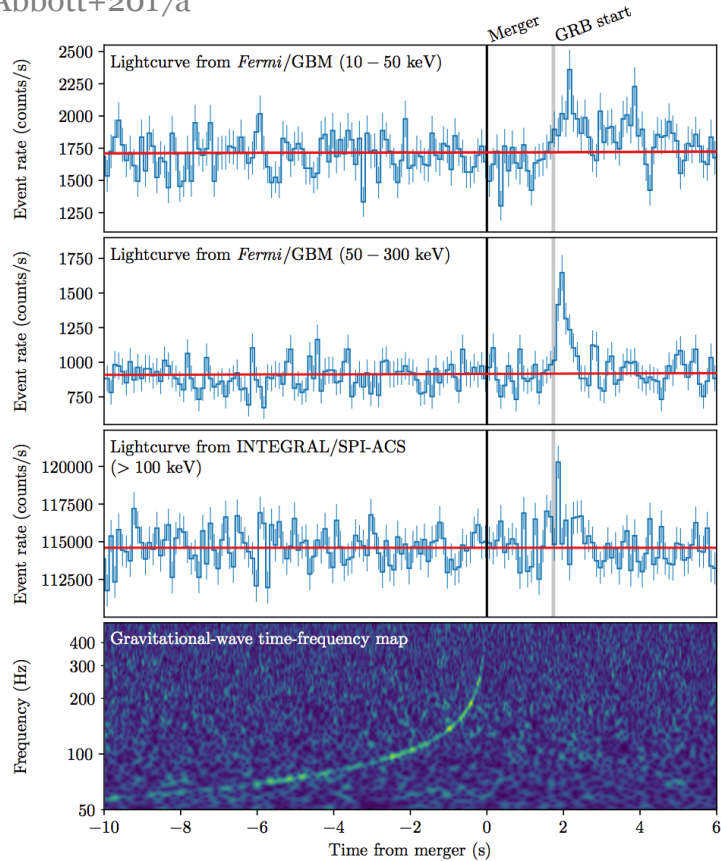


Video credits: ESO

GW 170817 / AT 2017gfo

The first Electromagnetic Counterpart of a Gravitational Wave event

Abbott+2017a



Abbott+2017b

Gravitational Waves as “Standard Sirens”

Schutz 1986; Holz & Hughes 2005

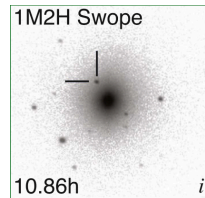
Determining the Hubble constant from gravitational wave observations

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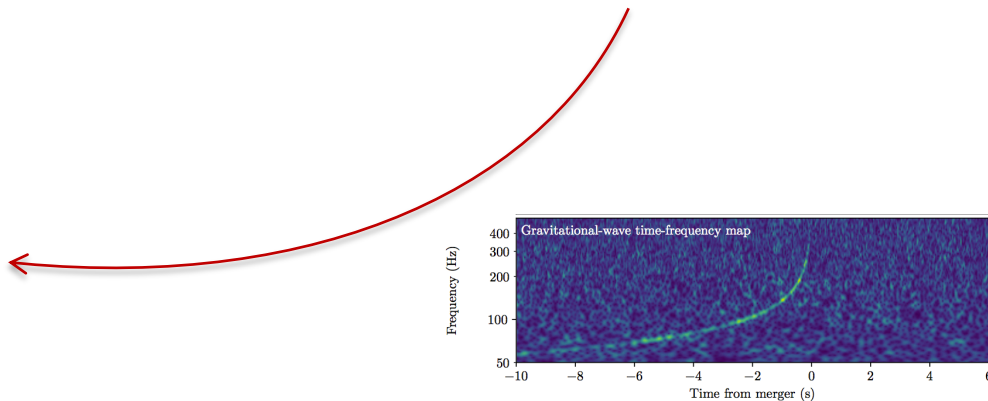
Department of Applied Mathematics and Astronomy,
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Gravitational Waves as “Standard Sirens”

GW170817 / AT2017gfo

Abbott+2017c

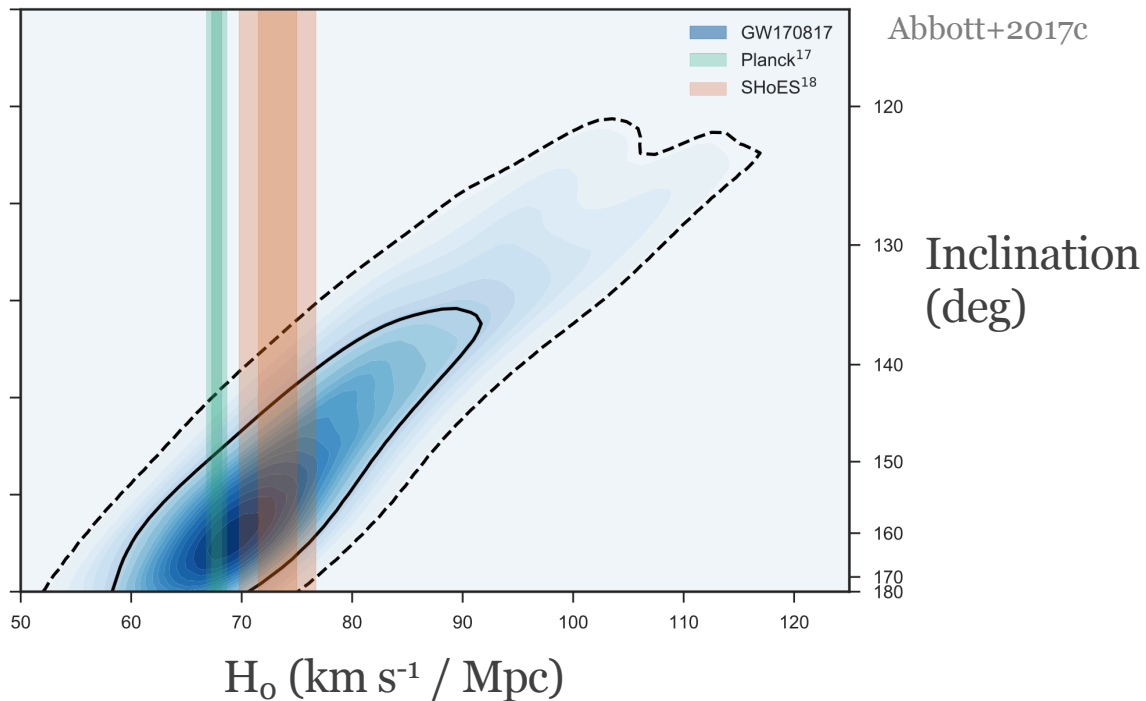
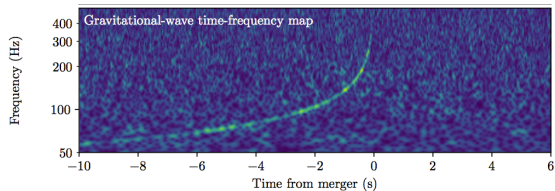
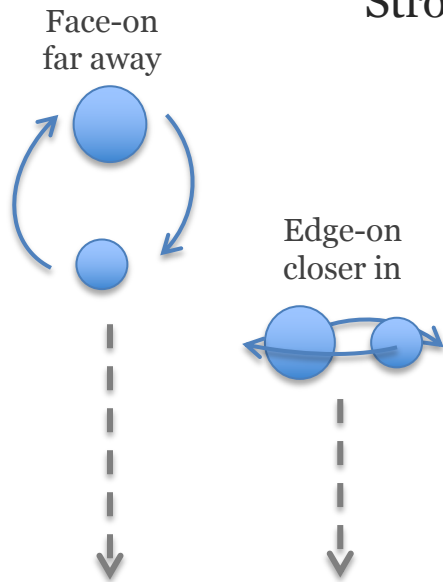
Extended Data Table 1. Summary of constraints on the Hubble constant, binary inclination, and distance

Parameter	68.3% Symm.	68.3% MAP	90% Symm.	90% MAP
$H_0/ (\text{km s}^{-1} \text{Mpc}^{-1})$	$74.0^{+16.0}_{-8.0}$	$70.0^{+12.0}_{-8.0}$	74.0^{+33}_{-12}	70.0^{+28}_{-11}
$H_0/ (\text{km s}^{-1} \text{Mpc}^{-1})$ (flat in z prior)	81^{+27}_{-13}	$71.0^{+23.0}_{-9.0}$	81^{+50}_{-17}	71.0^{+48}_{-11}
$H_0/ (\text{km s}^{-1} \text{Mpc}^{-1})$ ($250 \text{ km s}^{-1} \sigma_{v_r}$)	$74.0^{+16.0}_{-9.0}$	$70.0^{+14.0}_{-9.0}$	74.0^{+33}_{-14}	70.0^{+29}_{-14}
$\cos \iota$ (GW only)	$-0.88^{+0.18}_{-0.09}$	$-0.974^{+0.164}_{-0.026}$	$-0.88^{+0.32}_{-0.11}$	$-0.974^{+0.332}_{-0.026}$
$\cos \iota$ (SHoES)	$-0.901^{+0.065}_{-0.057}$	$-0.912^{+0.061}_{-0.059}$	$-0.901^{+0.106}_{-0.083}$	$-0.912^{+0.095}_{-0.086}$
$\cos \iota$ (Planck)	$-0.948^{+0.052}_{-0.036}$	$-0.982^{+0.060}_{-0.016}$	$-0.948^{+0.091}_{-0.046}$	$-0.982^{+0.104}_{-0.018}$
ι/deg (GW only)	152^{+14}_{-17}	167^{+13}_{-23}	152^{+20}_{-27}	167^{+13}_{-37}
ι/deg (SHoES)	$154.0^{+9.0}_{-8.0}$	$156.0^{+10.0}_{-7.0}$	154.0^{+15}_{-12}	156.0^{+21}_{-11}
ι/deg (Planck)	$161.0^{+8.0}_{-8.0}$	$169.0^{+8.0}_{-12.0}$	161.0^{+12}_{-12}	169.0^{+11}_{-18}
$d/ (\text{Mpc})$	$41.1^{+4.0}_{-7.3}$	$43.8^{+2.9}_{-6.9}$	$41.1^{+5.6}_{-12.6}$	$43.8^{+5.6}_{-13.1}$

Gravitational Waves as “Standard Sirens”

GW170817 / AT2017gfo

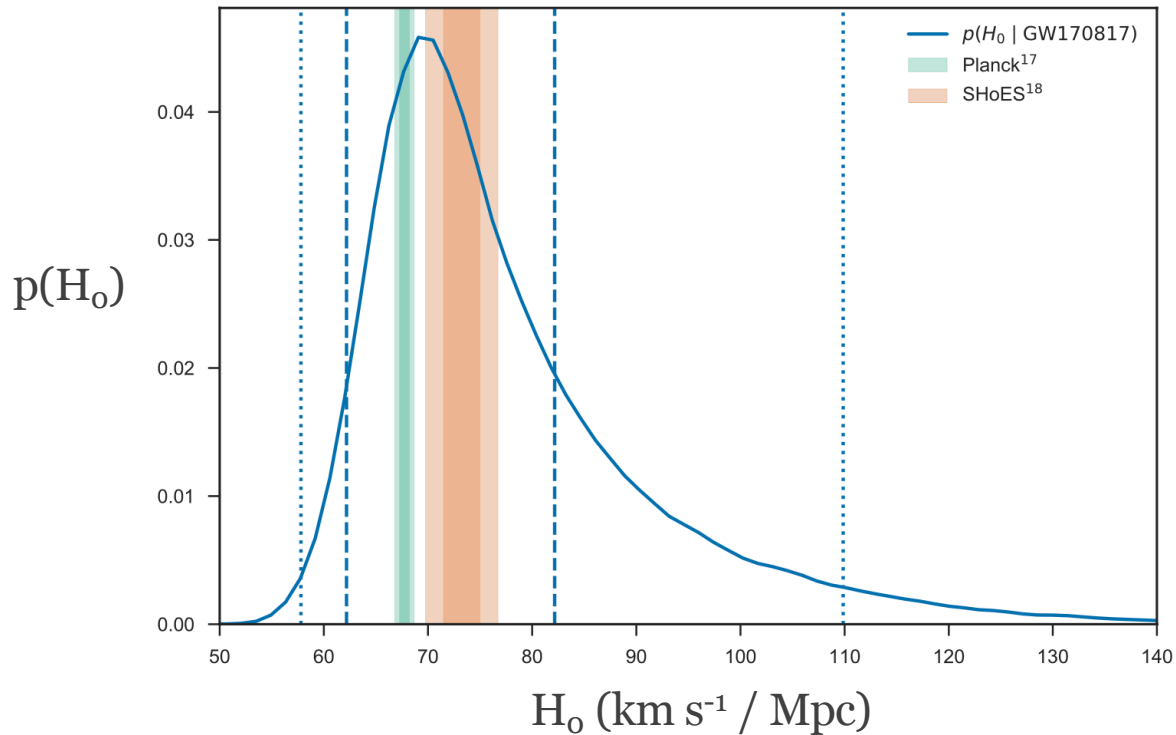
Strong degeneracy between **distance** and **inclination**



Gravitational Waves as “Standard Sirens”

GW170817 / AT2017gfo

Strong degeneracy between **distance** and **inclination**



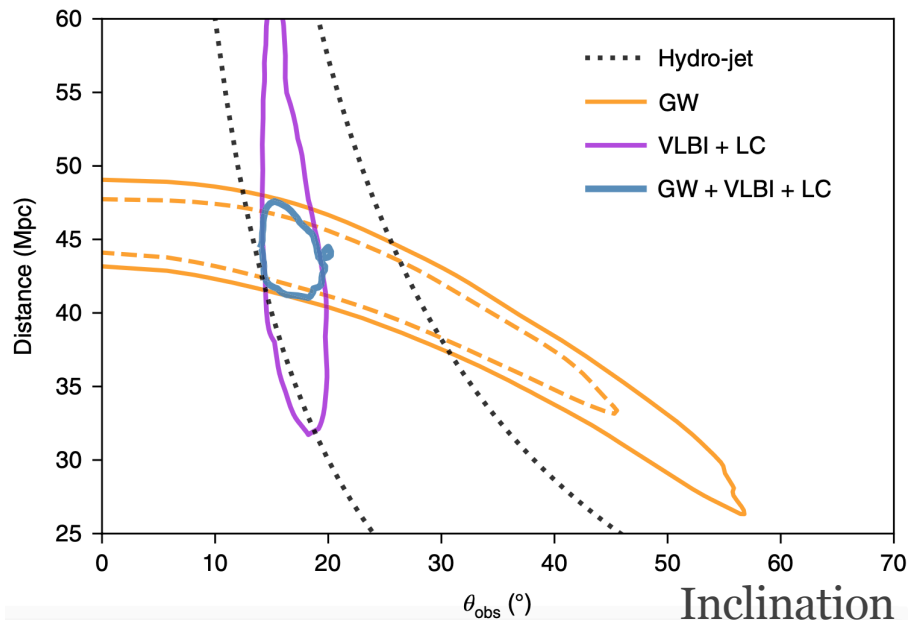
$$H_0 = 74.0^{+16.0}_{-8.0} \text{ km s}^{-1} / \text{Mpc}$$

Gravitational Waves as “Standard Sirens”

GW170817 / AT2017gfo

Strong degeneracy between distance and inclination

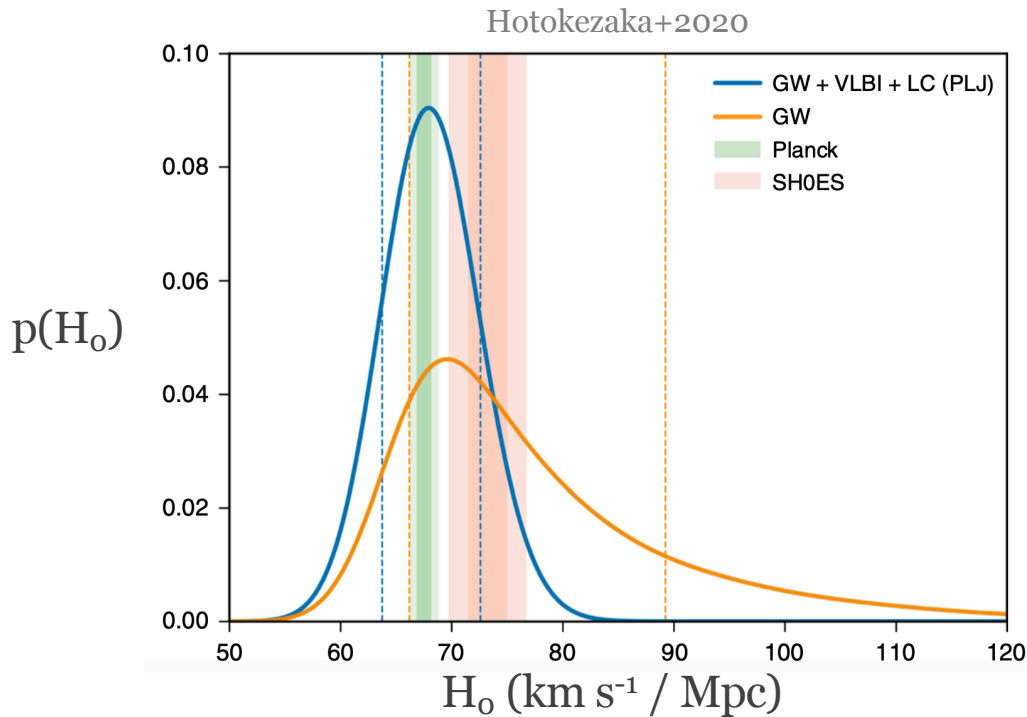
Hotokezaka+2020



Gravitational Waves as “Standard Sirens”

GW170817 / AT2017gfo

Strong degeneracy between distance and inclination



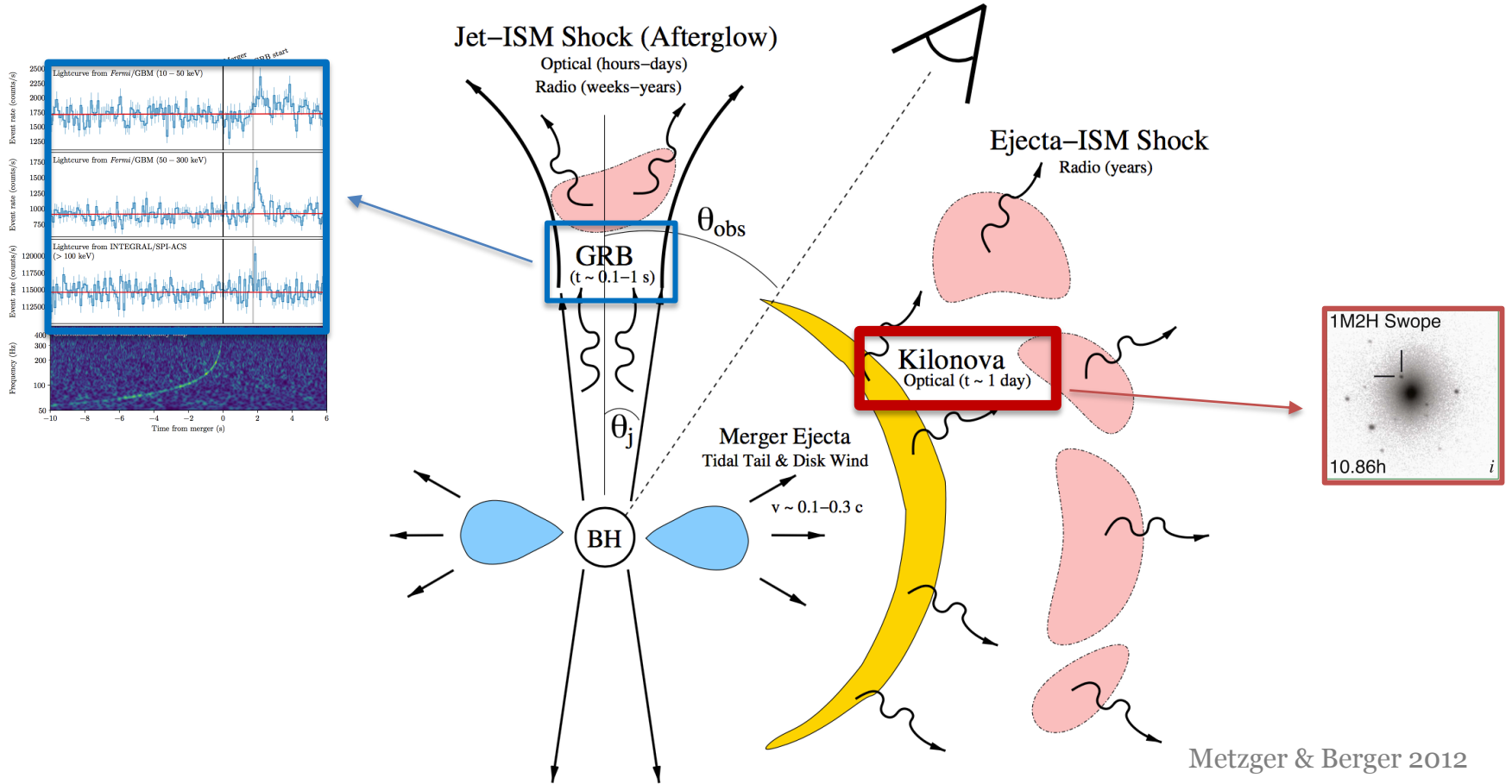
GW only

$$H_0 = 74.0^{+16.0}_{-8.0} \text{ km s}^{-1} / \text{Mpc}$$

GW + radio

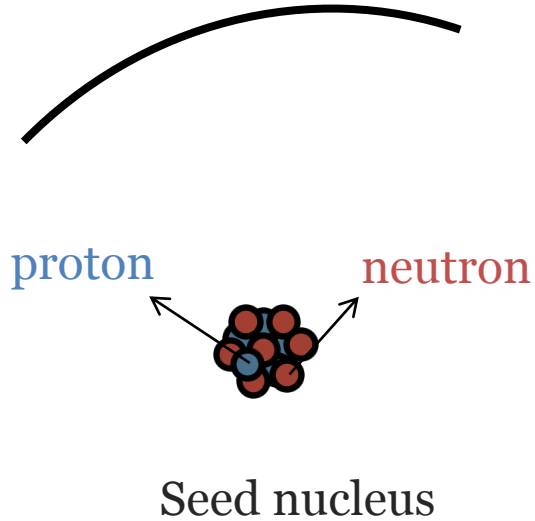
$$H_0 = 70.3^{+5.3}_{-5.0} \text{ km s}^{-1} / \text{Mpc}$$

Kilonova



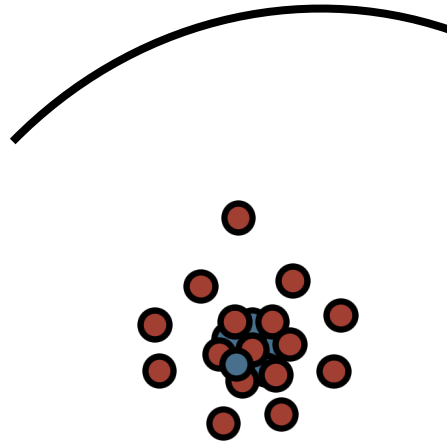
Kilonova

A radioactively-powered emission from NS-NS and NS-BH mergers



Kilonova

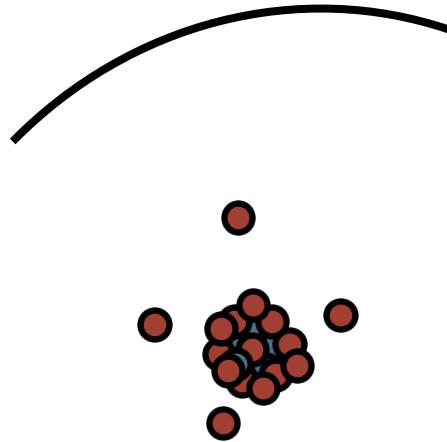
A radioactively-powered emission from NS-NS and NS-BH mergers



High density of free neutrons

Kilonova

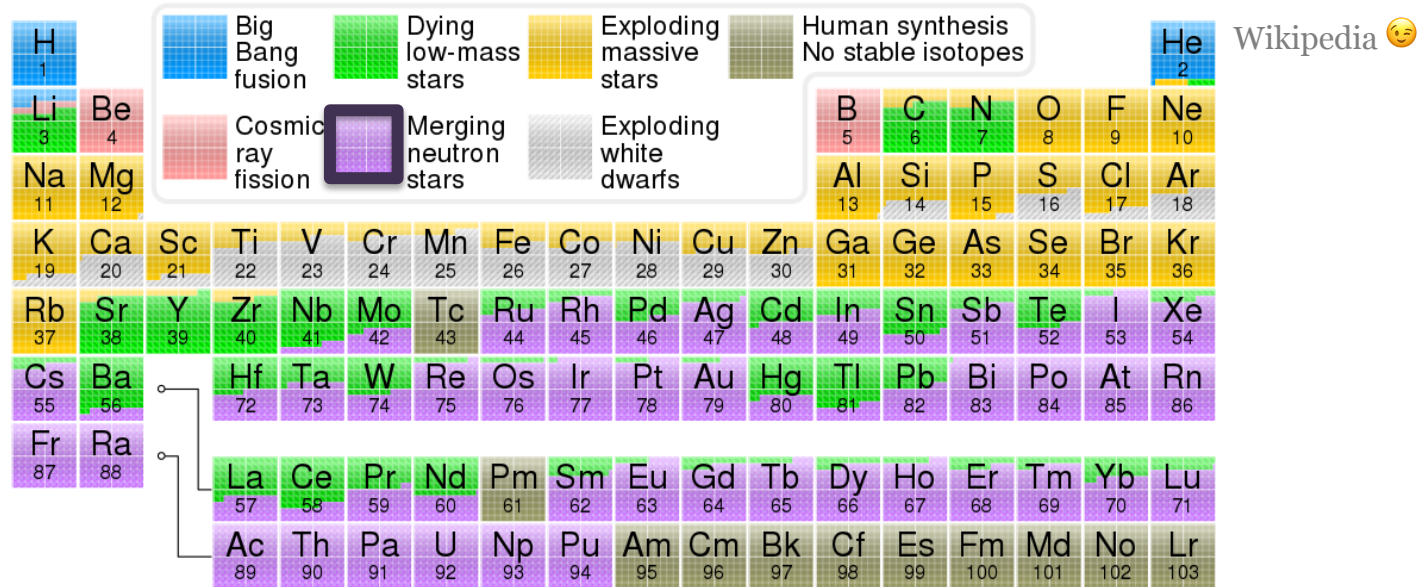
A radioactively-powered emission from NS-NS and NS-BH mergers



Neutron capture via “r-process” (“rapid process”)

Kilonova

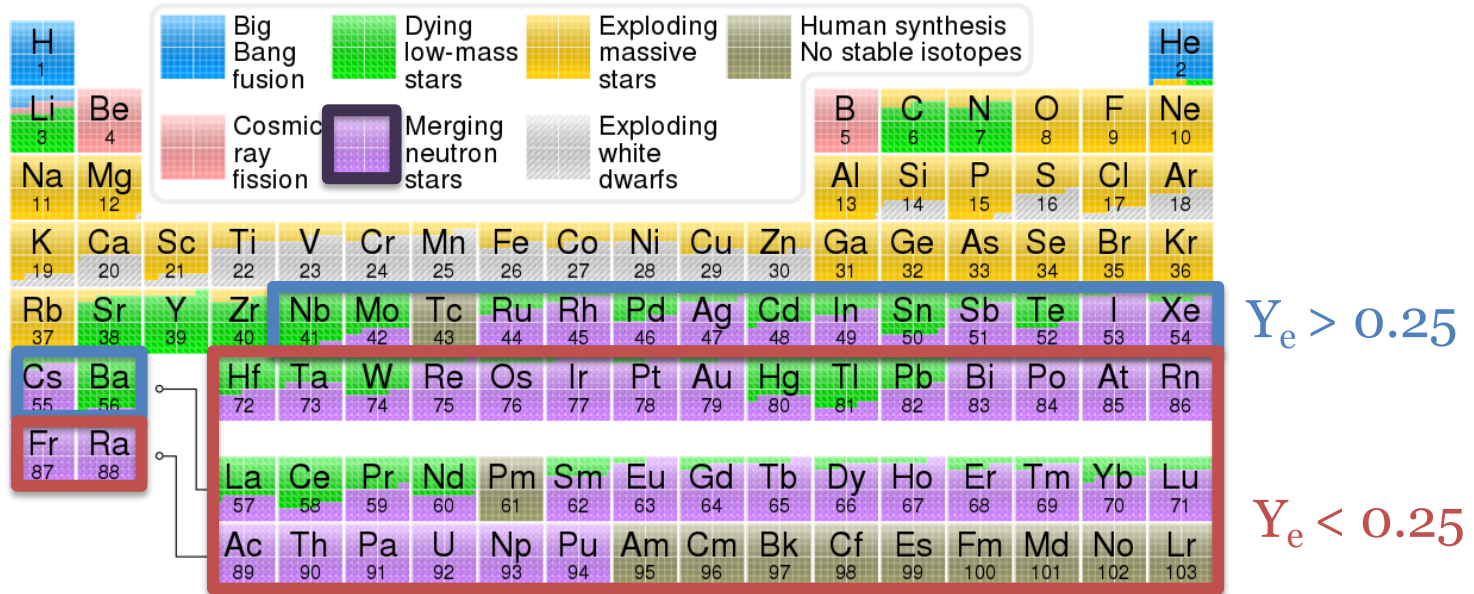
A radioactively-powered emission from NS-NS and NS-BH mergers



r-process responsible for the creation of $\sim 1/2$ of the nuclei heavier than Fe

Kilonova

A radioactively-powered emission from NS-NS and NS-BH mergers

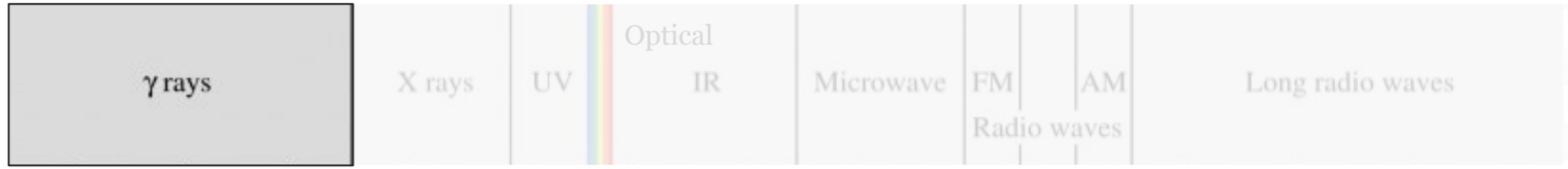


r-process nucleosynthesis controlled by the matter composition

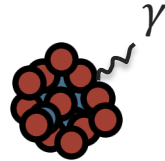
$$\text{Electron fraction } Y_e = \frac{\text{number of protons [./electrons]}}{\text{number of protons+number of neutrons}}$$

Kilonova

A radioactively-powered emission from NS-NS and NS-BH mergers



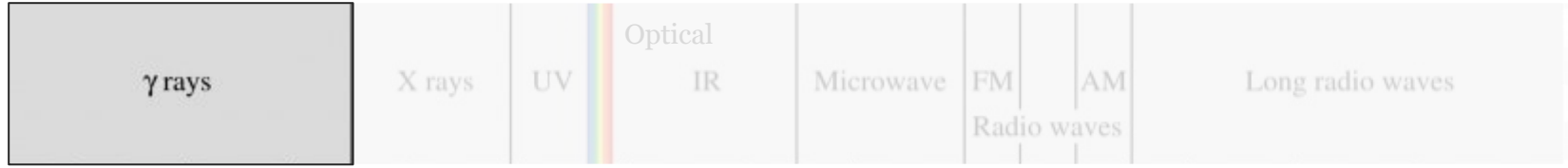
→ Increasing wavelength



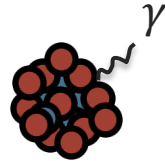
Radioactive elements \rightarrow decay \rightarrow γ photons

Kilonova

A radioactively-powered emission from NS-NS and NS-BH mergers



→ Increasing wavelength



$T \sim 5\,000 - 10\,000\text{ K @ 1 day}$

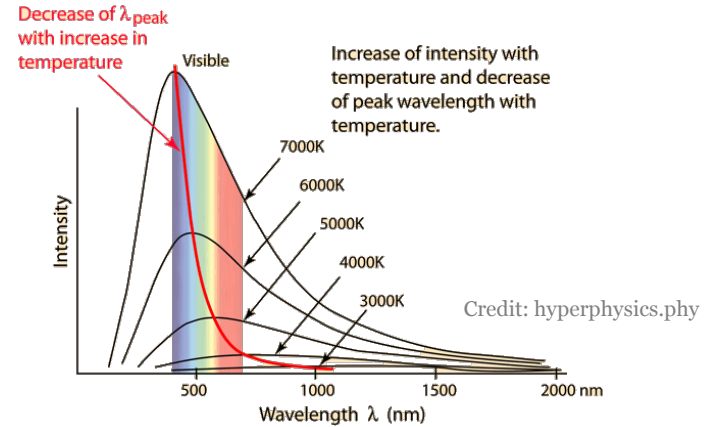
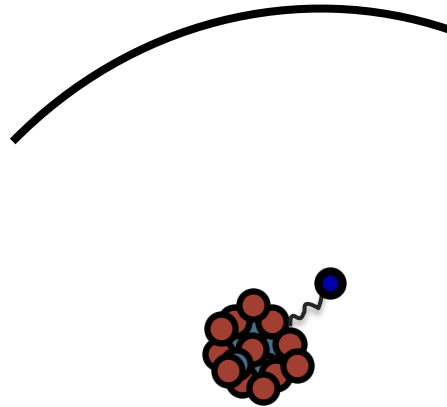
γ photons thermalize -> setting the temperature

Kilonova

A radioactively-powered emission from NS-NS and NS-BH mergers



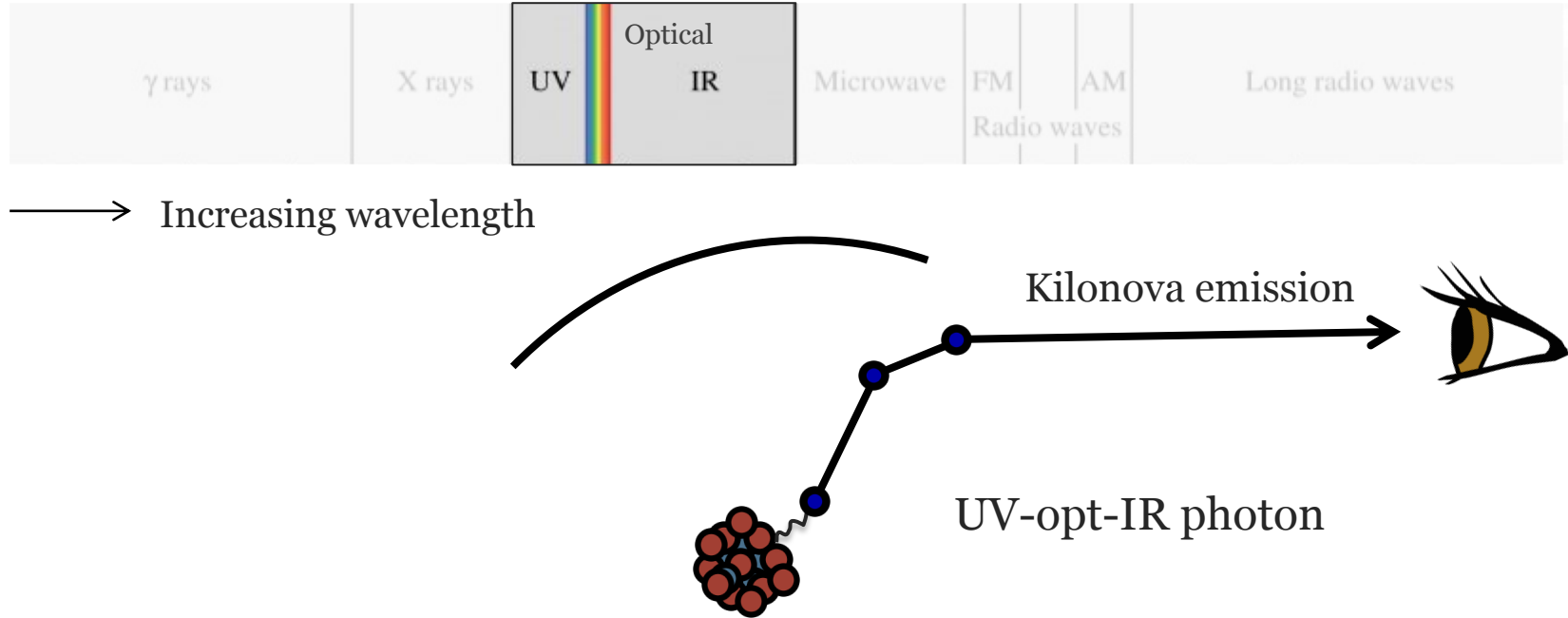
→ Increasing wavelength



γ photons thermalize \rightarrow thermal emission at longer wavelengths (UV-opt-IR)

Kilonova

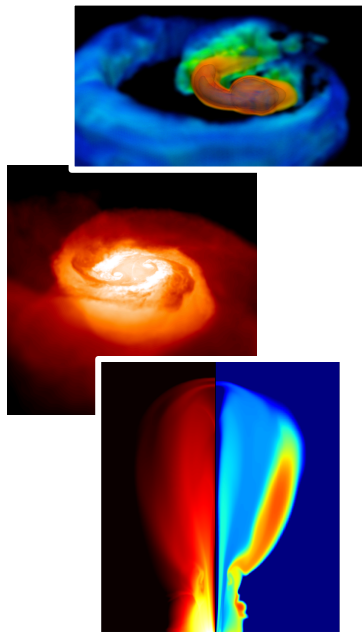
A radioactively-powered emission from NS-NS and NS-BH mergers



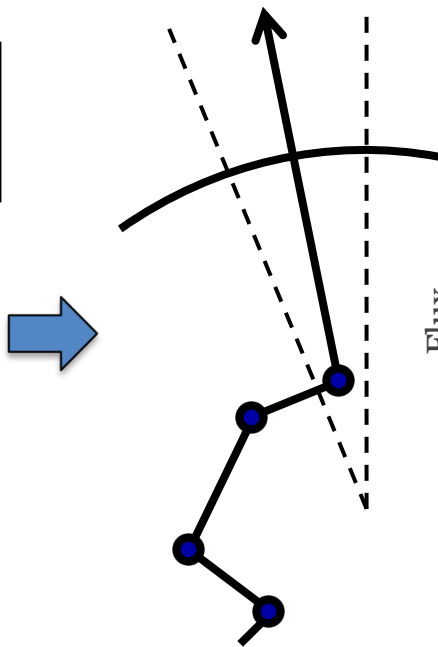
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POSSIS

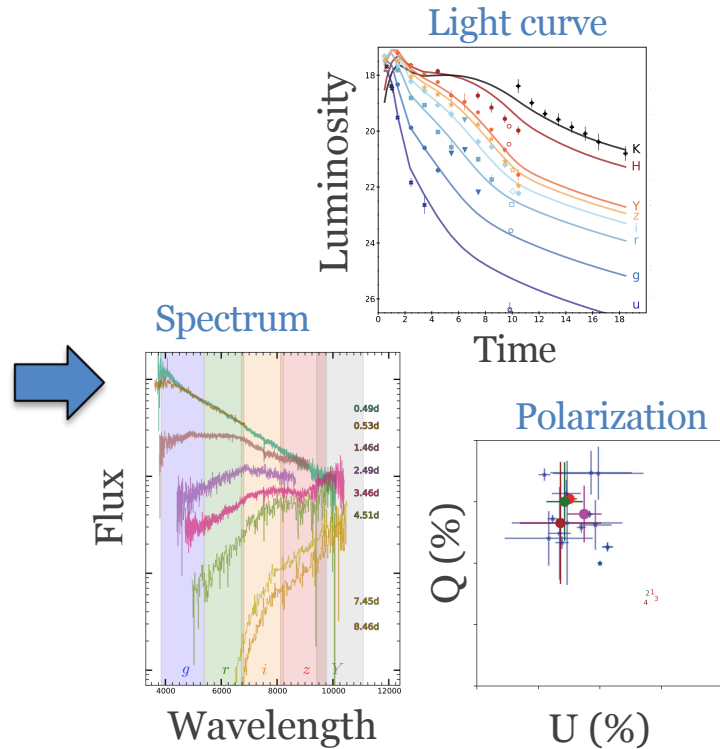
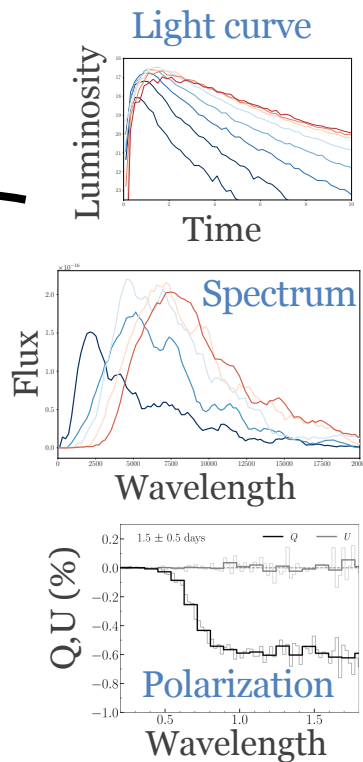
A Monte Carlo radiative transfer code to predict observables for kilonovae



Models



Radiative transfer

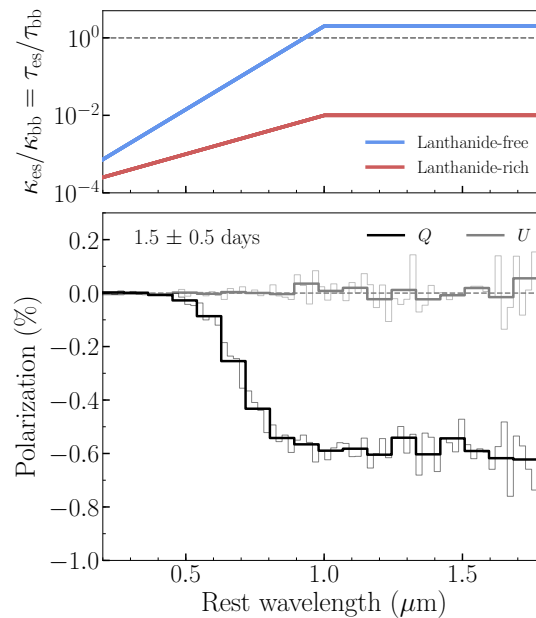
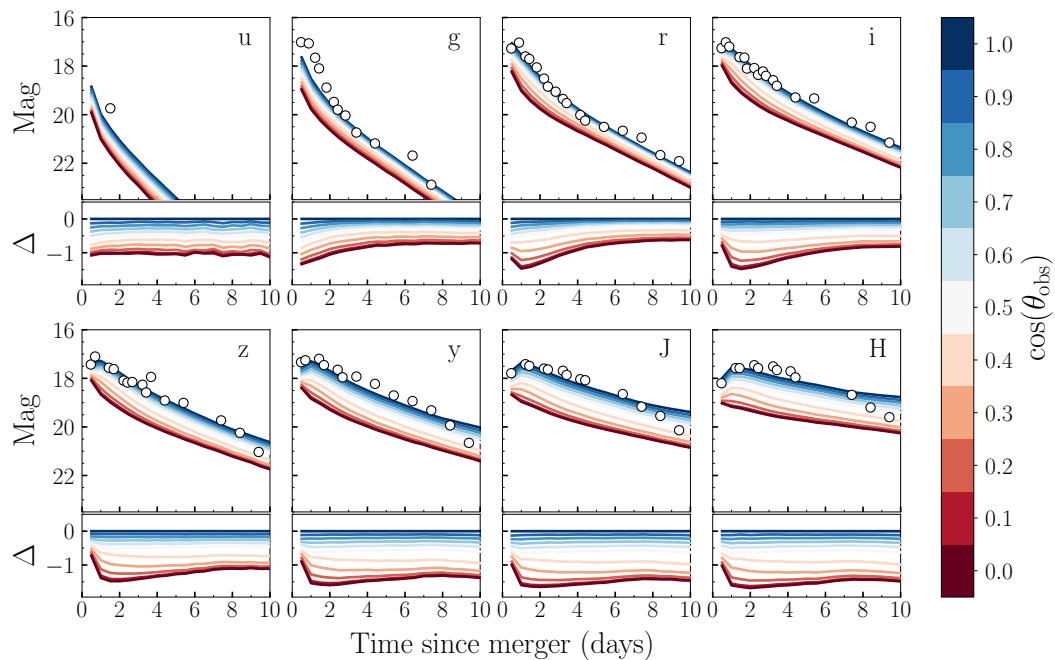


Observations



POSSIS: predicting spectra, light curves, and polarization for multidimensional models of supernovae and kilonovae

M. Bulla  



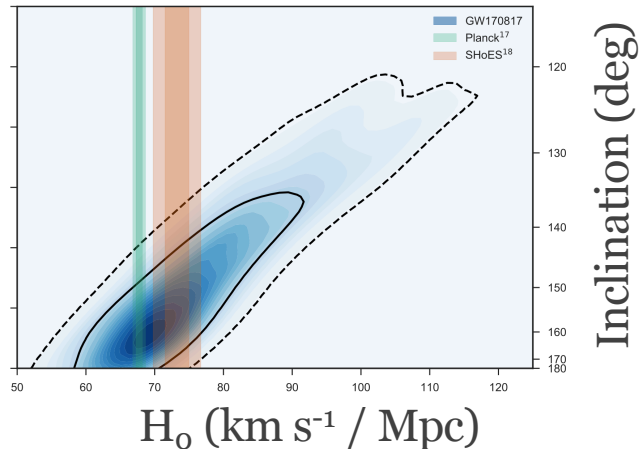
Latest version
of POSSIS
improved with
better physics



H₀ and kilonovae

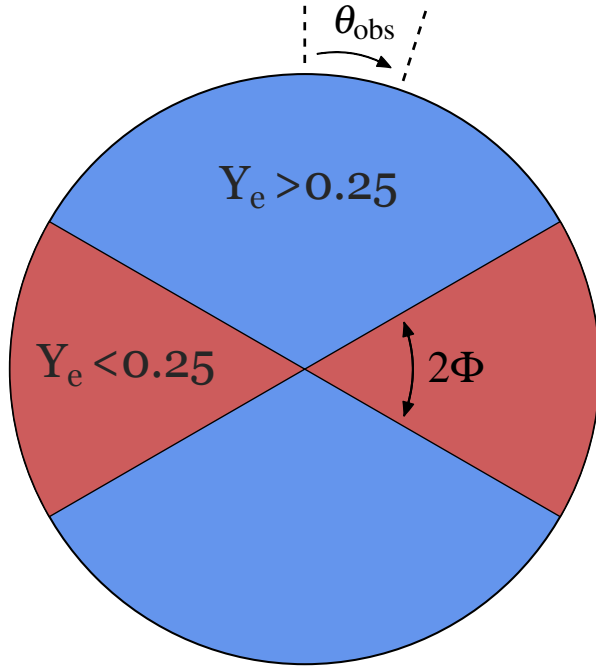
3 approaches to measure/improve on H₀

1. Constrain **inclination** with kilonova **light curves** -> GW + EM (improve standard sirens)
2. Constrain **inclination** with kilonova **polarization** -> GW + EM (improve standard sirens)
3. Constrain **distance** directly from **kilonovae** -> EM



$$H_0 = \frac{[\text{speed of light}] \times \text{Redshift}}{\text{Distance}}$$

1. Constrain inclination with kilonova light curves

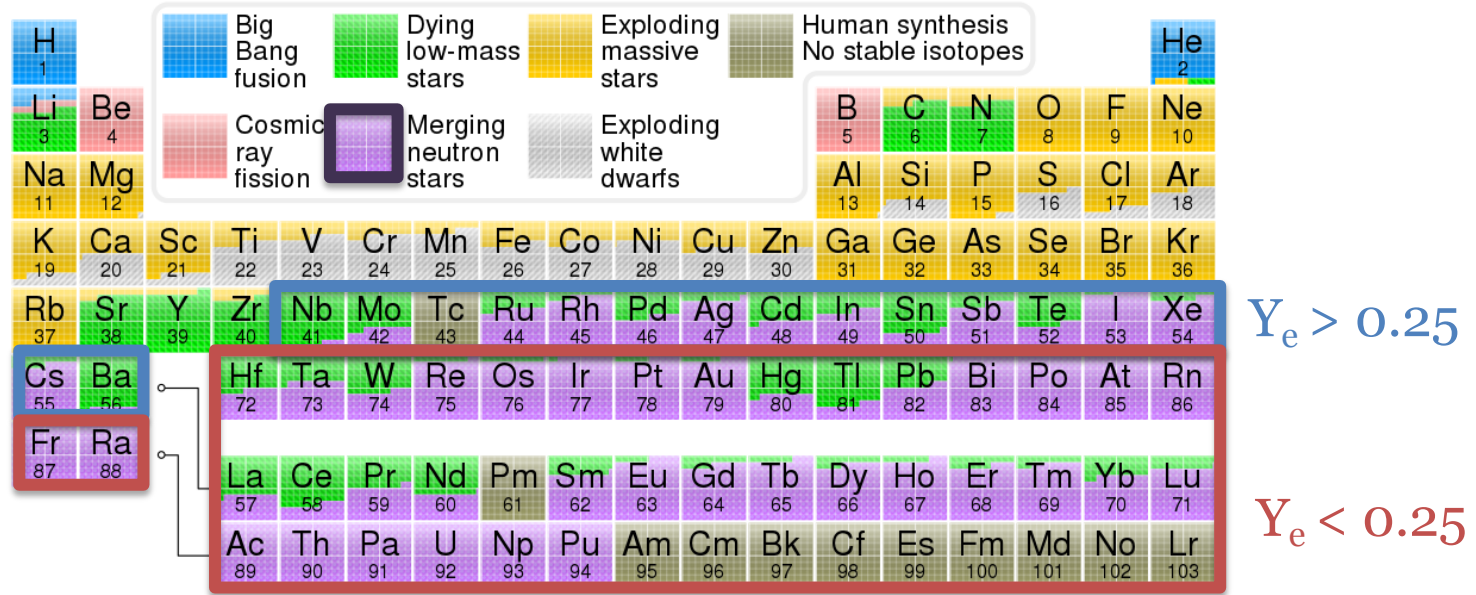


Material ejected **anisotropically**

Asymmetric distribution

(At least) Two components with different **compositions**
and corresponding **opacities**

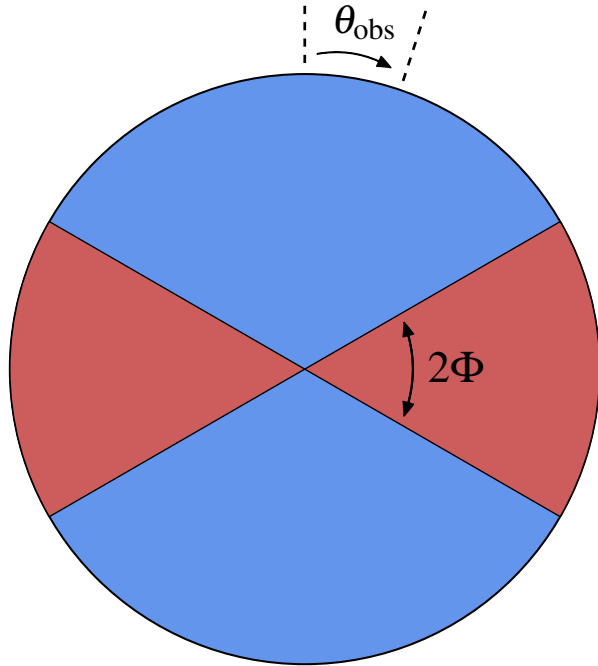
1. Constrain inclination with kilonova light curves



Nucleosynthesis controlled by the matter composition

Electron fraction $Y_e = \frac{\text{number of protons [/electrons]}}{\text{number of protons + number of neutrons}}$

1. Constrain inclination with kilonova light curves



Opacity

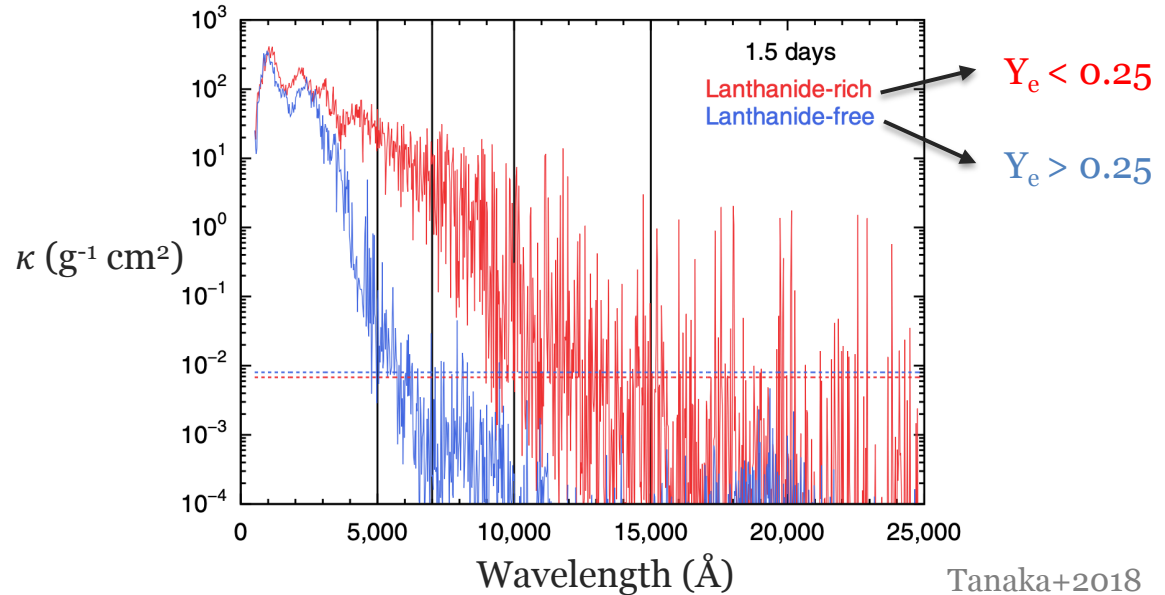
$$\tau = \int \boxed{\kappa} \rho dr$$

$[\text{g}^{-1} \text{cm}^2]$

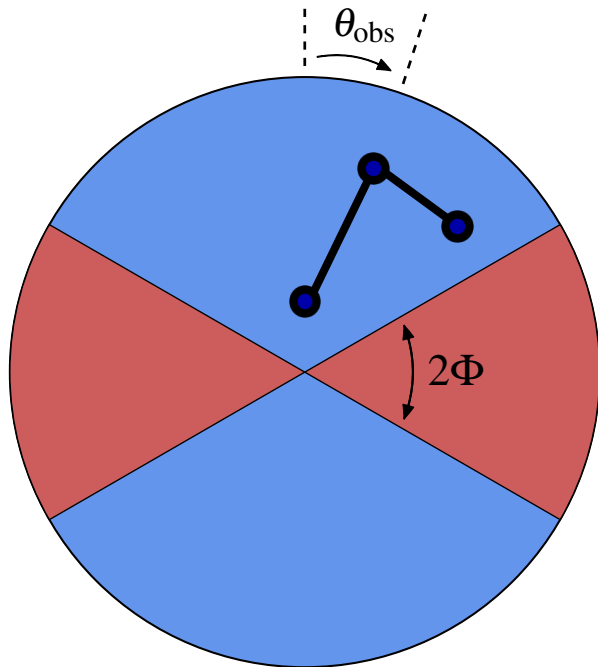
Source of opacities in kilonovae

Electron scattering

Bound-bound (line) absorption



1. Constrain inclination with kilonova light curves



Opacity

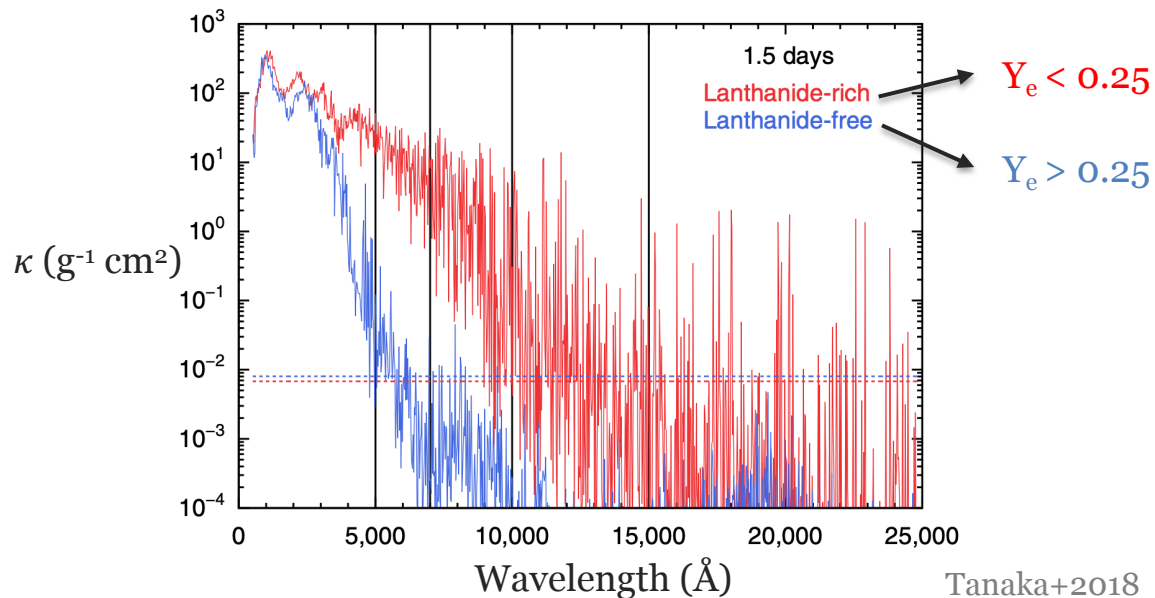
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[g⁻¹ cm²]

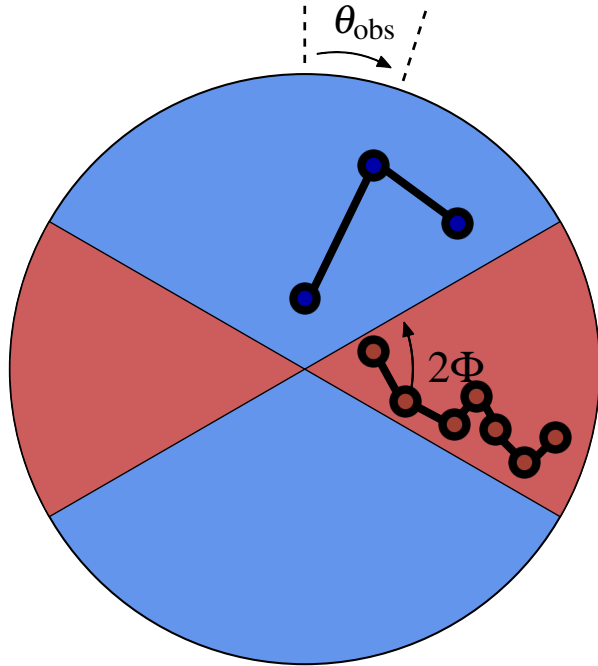
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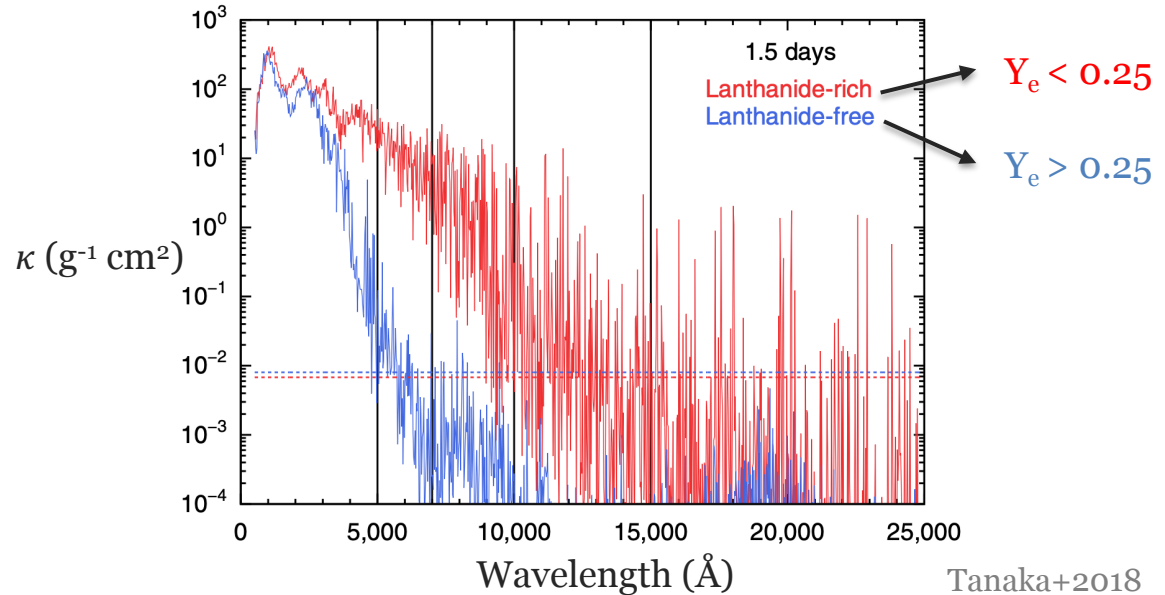
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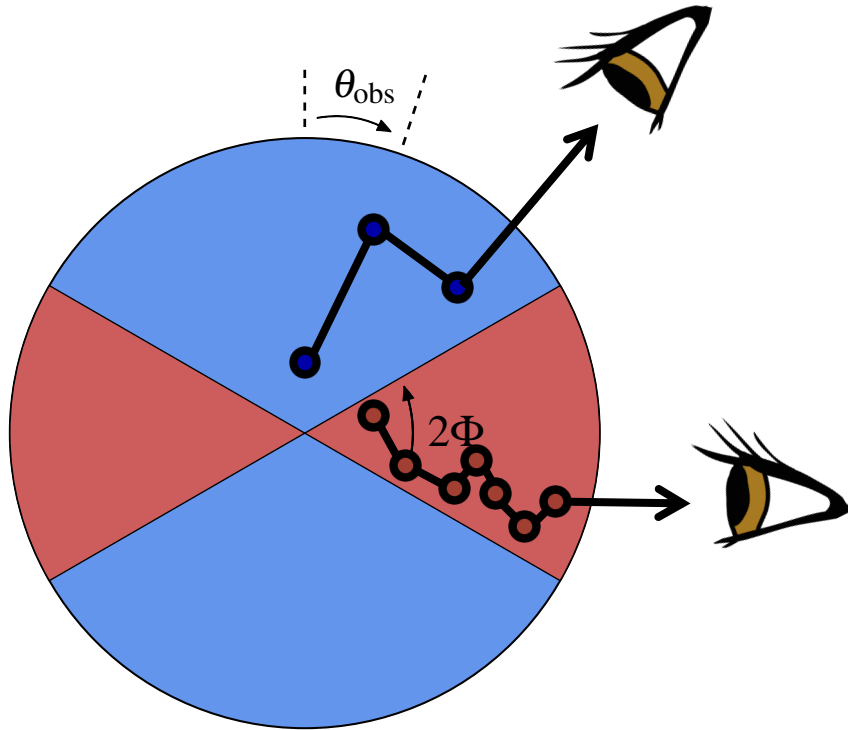
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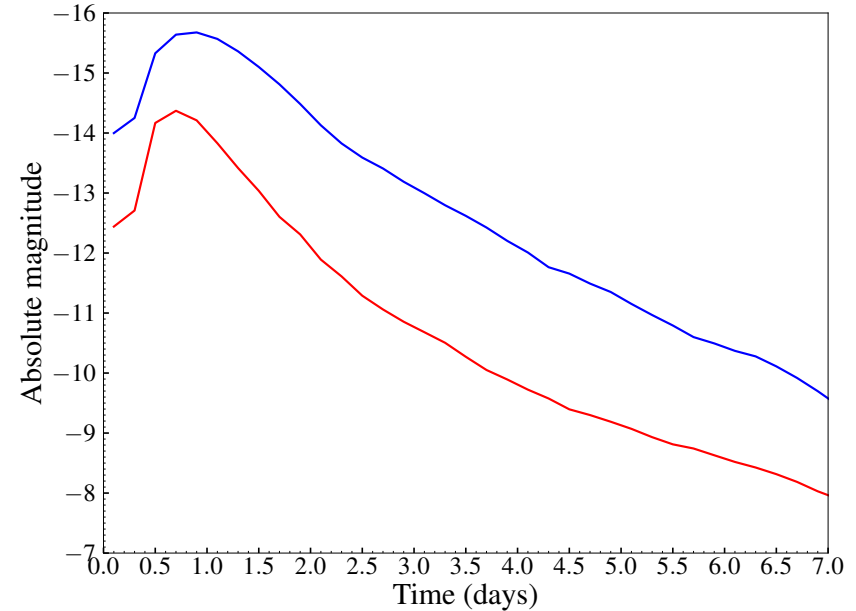
Bound-bound (line) absorption



1. Constrain inclination with kilonova light curves



Viewing-angle dependence in kilonova light curves



1. Constrain inclination with kilonova light curves

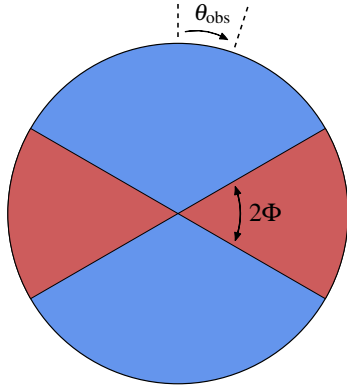
THE ASTROPHYSICAL JOURNAL, 888:67 (5pp), 2020 January 10
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<https://doi.org/10.3847/1538-4357/ab5799>



Constraining the Observer Angle of the Kilonova AT2017gfo Associated with GW170817: Implications for the Hubble Constant

S. Dhawan , M. Bulla, A. Goobar , A. Sagués Carracedo, and C. N. Setzer



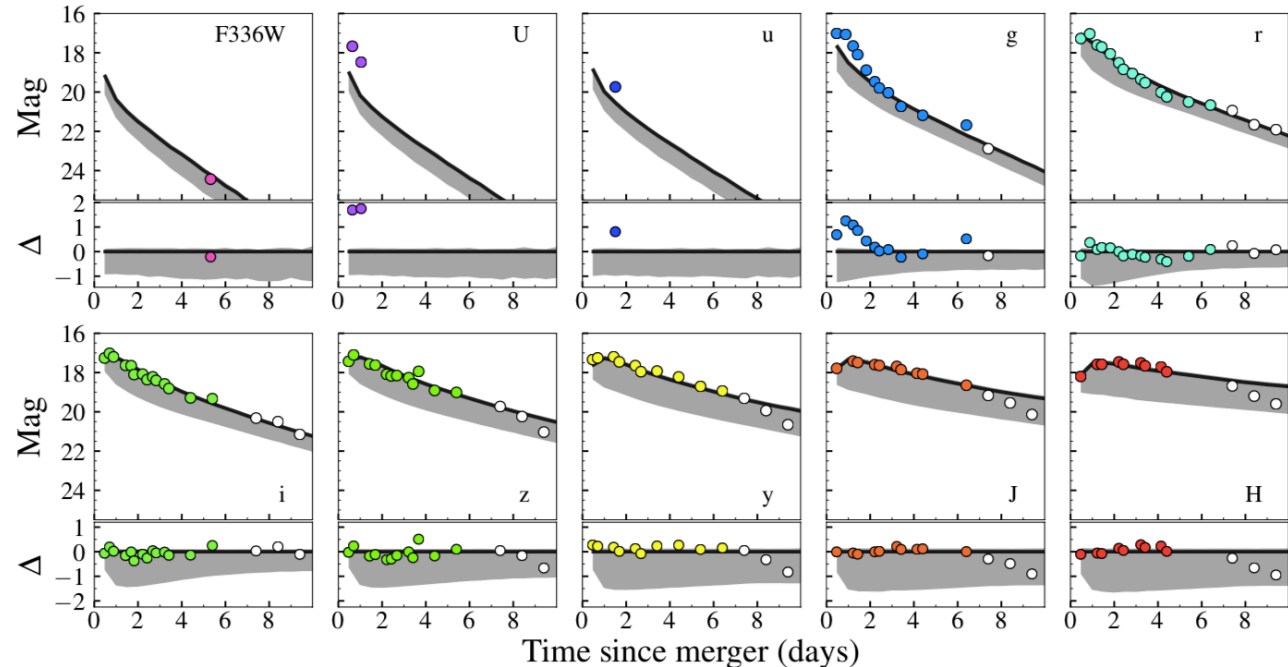
550 models varying
 M_{ej} , Φ and ϑ_{obs}

Best-fit model:

$$M_{ej} = 0.05 M_{\odot}$$

$$\Phi = 30 \text{ deg}$$

$$\cos(\vartheta_{obs}) = 0.9$$



1. Constrain inclination with kilonova light curves

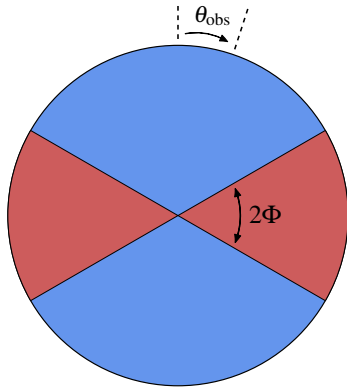
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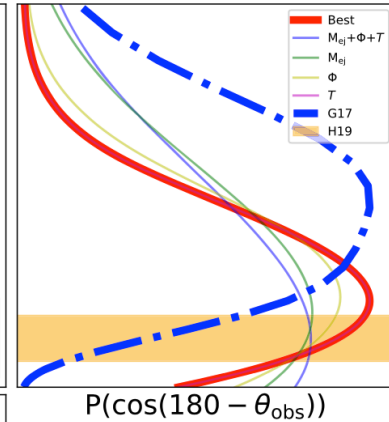
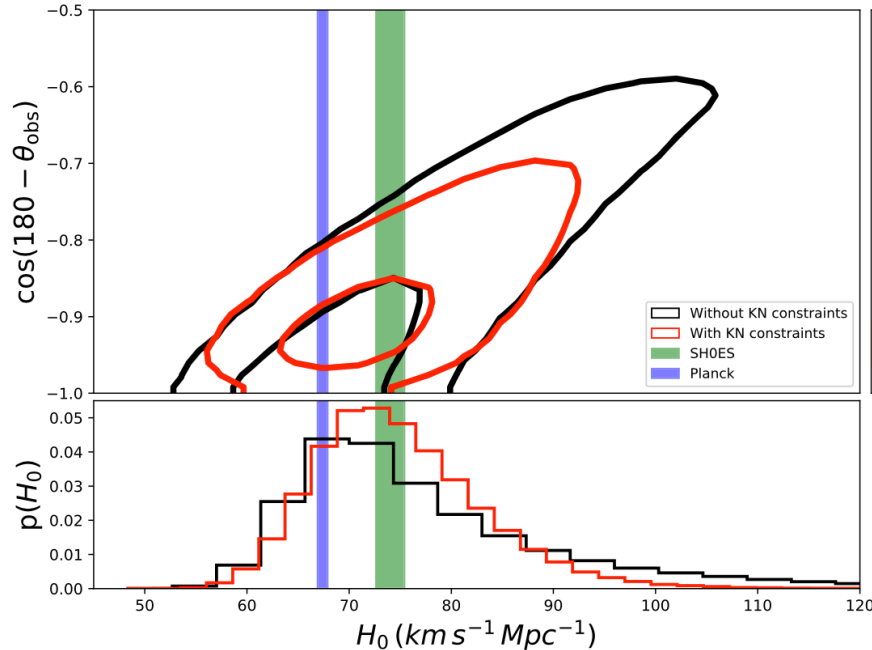
GW only

$$H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} / \text{Mpc}$$

GW + kilonova

$$H_0 = 72.4^{+7.9}_{-7.3} \text{ km s}^{-1} / \text{Mpc}$$

24% improvement on H_0



2. Constrain inclination with kilonova polarization

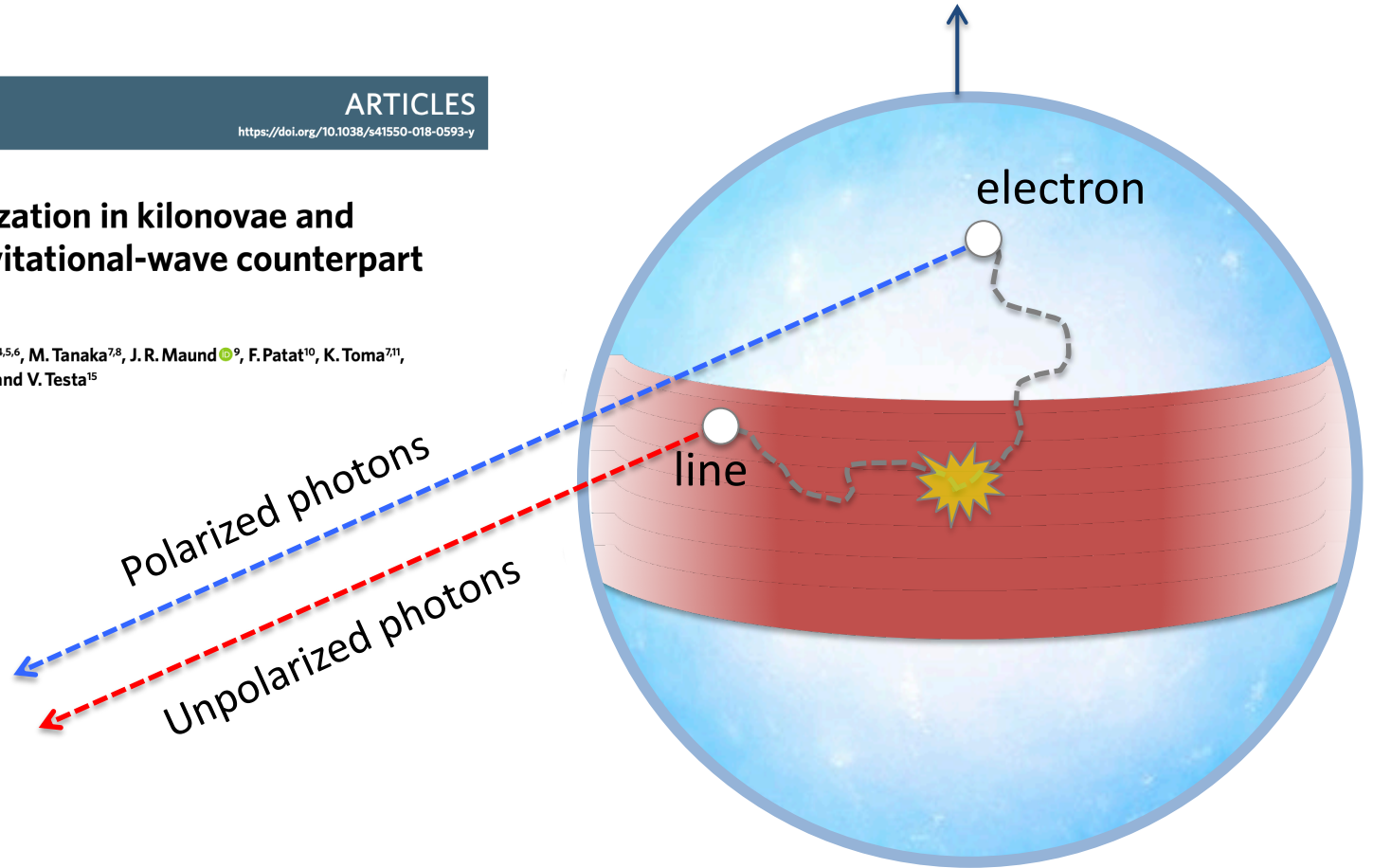
nature
astronomy

ARTICLES

<https://doi.org/10.1038/s41550-018-0593-y>

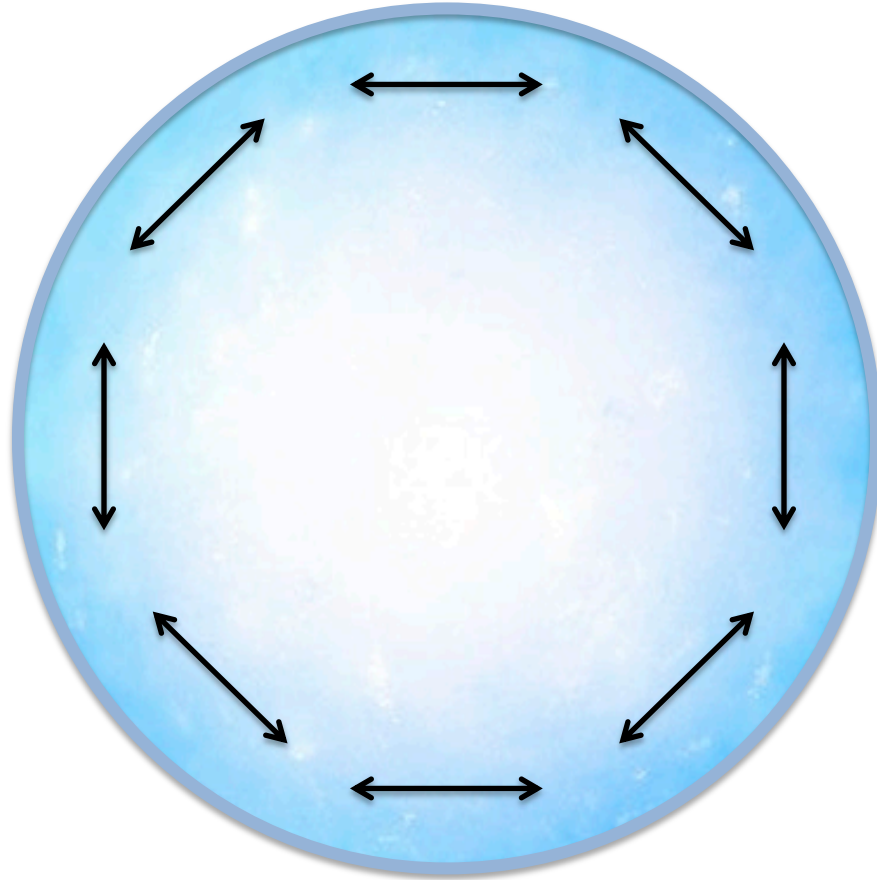
The origin of polarization in kilonovae and the case of the gravitational-wave counterpart AT 2017gfo

M. Bulla^{1*}, S. Covino^{2*}, K. Kyutoku^{3,4,5,6}, M. Tanaka^{7,8}, J. R. Maund⁹, F. Patat¹⁰, K. Toma^{7,11}, K. Wiersema^{12,13}, J. Bruten⁹, Z. P. Jin¹⁴ and V. Testa¹⁵



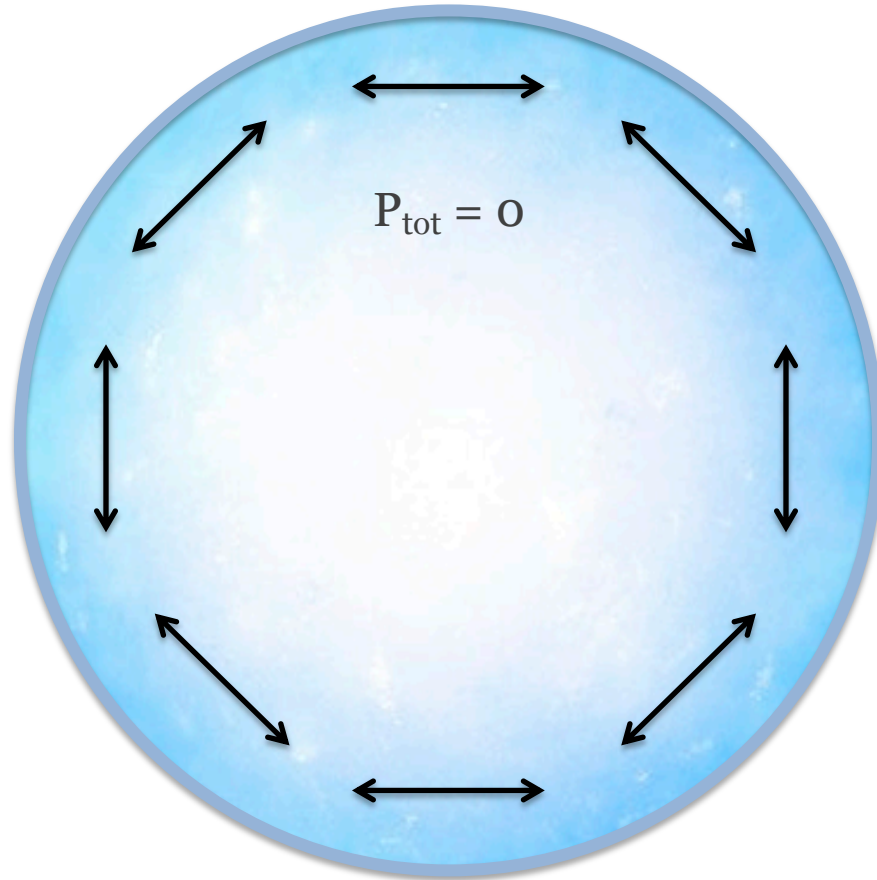
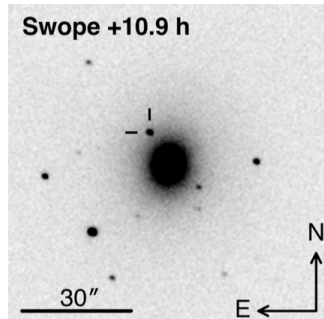
2. Constrain inclination with kilonova polarization

Polarizing
electron scattering:
each polarizing
contribution is cancelled by
one 90 degree away



2. Constrain inclination with kilonova polarization

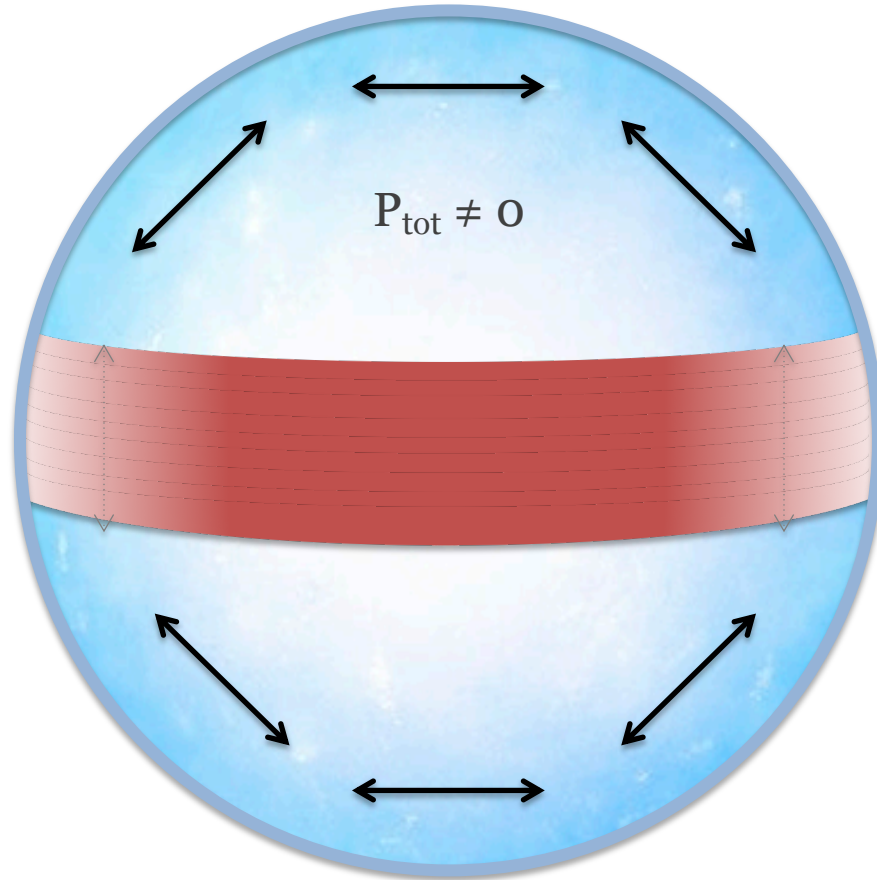
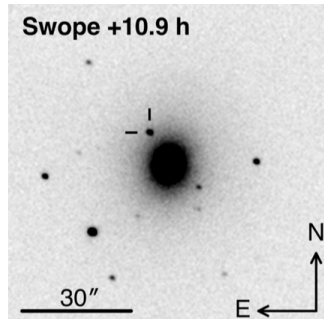
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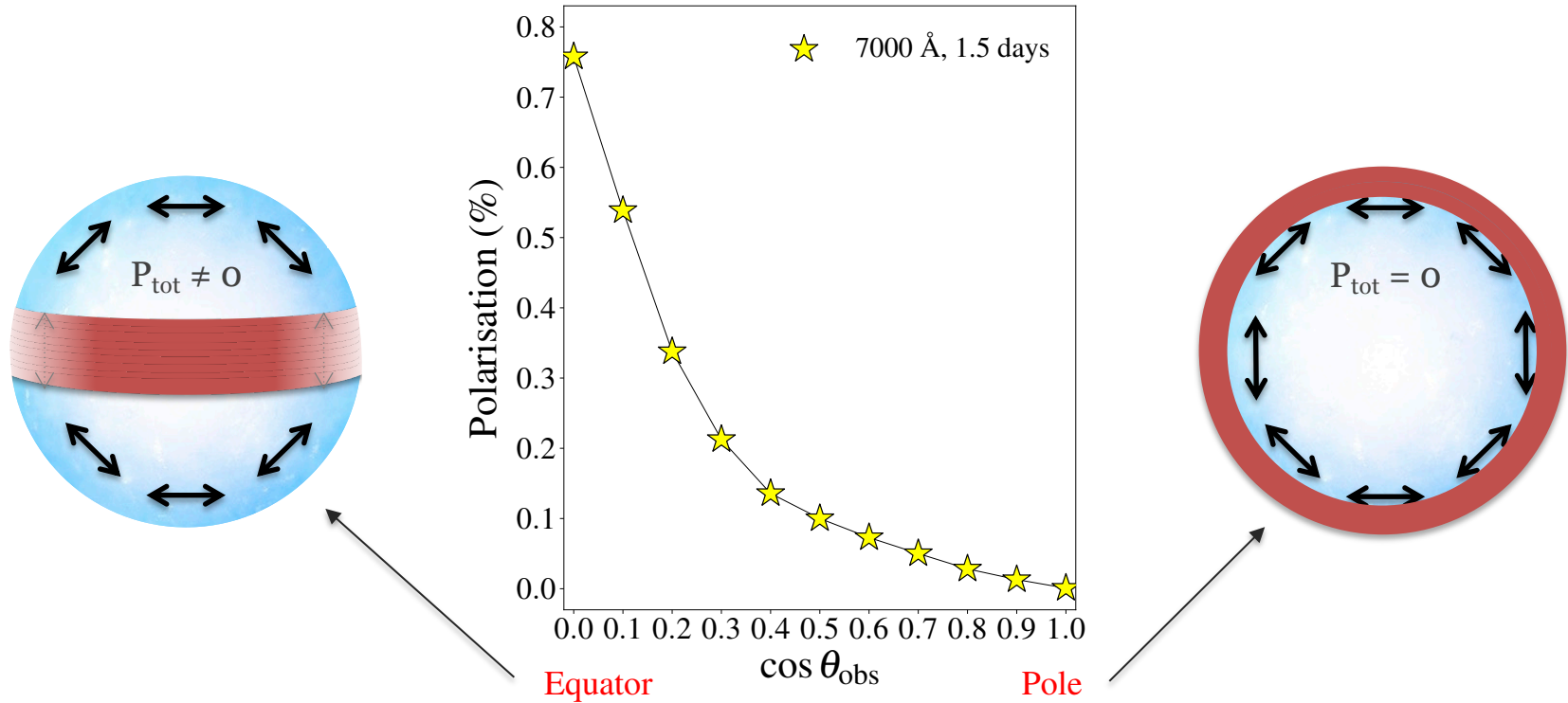
2. Constrain inclination with kilonova polarization

Polarizing
electron scattering
+ **depolarizing line**

Break of symmetry and
overall polarization signal

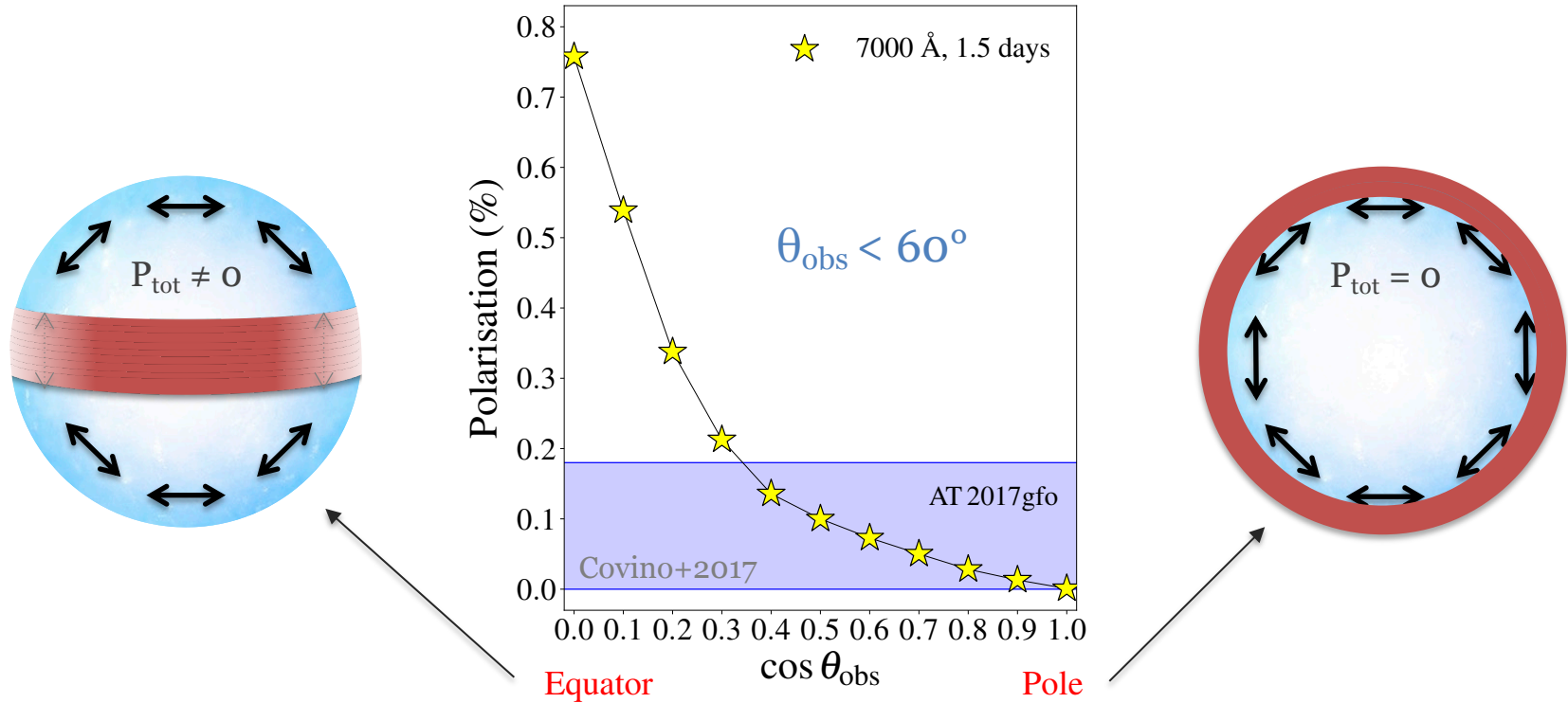


2. Constrain inclination with kilonova polarization



Polarization levels $\approx 1\%$ could be detected in future kilonovae seen from **favorable** viewing angles

2. Constrain inclination with kilonova polarization



Polarization levels $\approx 1\%$ could be detected in future kilonovae seen from **favorable** viewing angles

3. Constrain distance directly from kilonovae

PHYSICAL REVIEW RESEARCH 2, 022006(R) (2020)

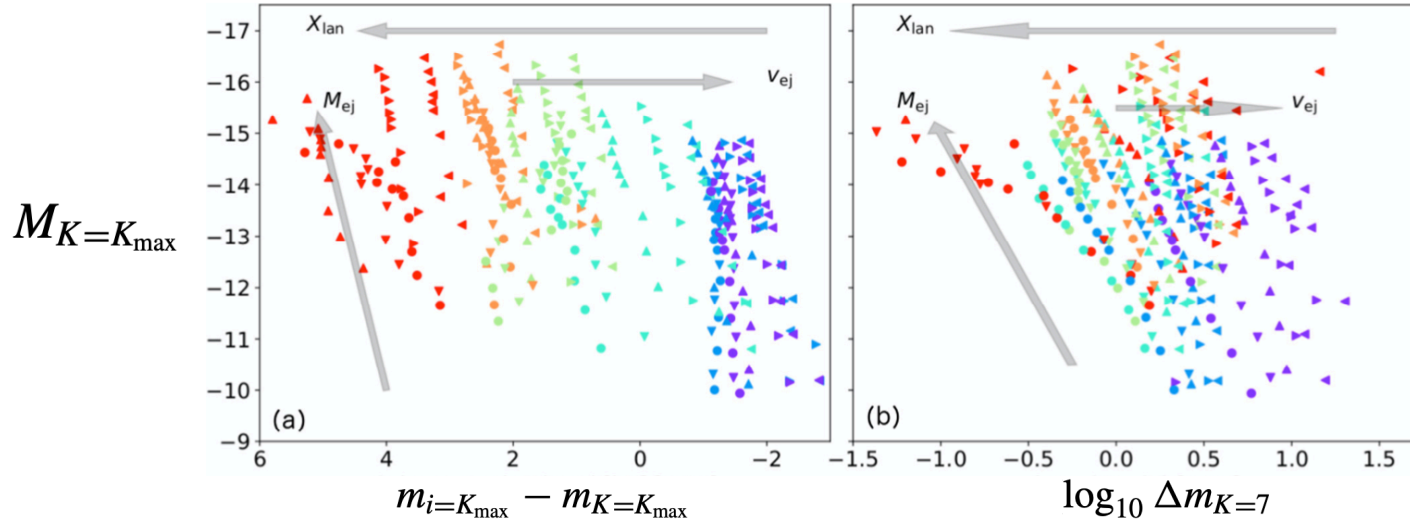
Rapid Communications

Standardizing kilonovae and their use as standard candles to measure the Hubble constant

Michael W. Coughlin^{1,2}, Tim Dietrich^{3,4}, Jack Heinzel^{5,6}, Nandita Khetan⁷, Sarah Antier⁸, Mattia Bulla⁹,
Nelson Christensen^{5,6}, David A. Coulter¹⁰ and Ryan J. Foley¹⁰



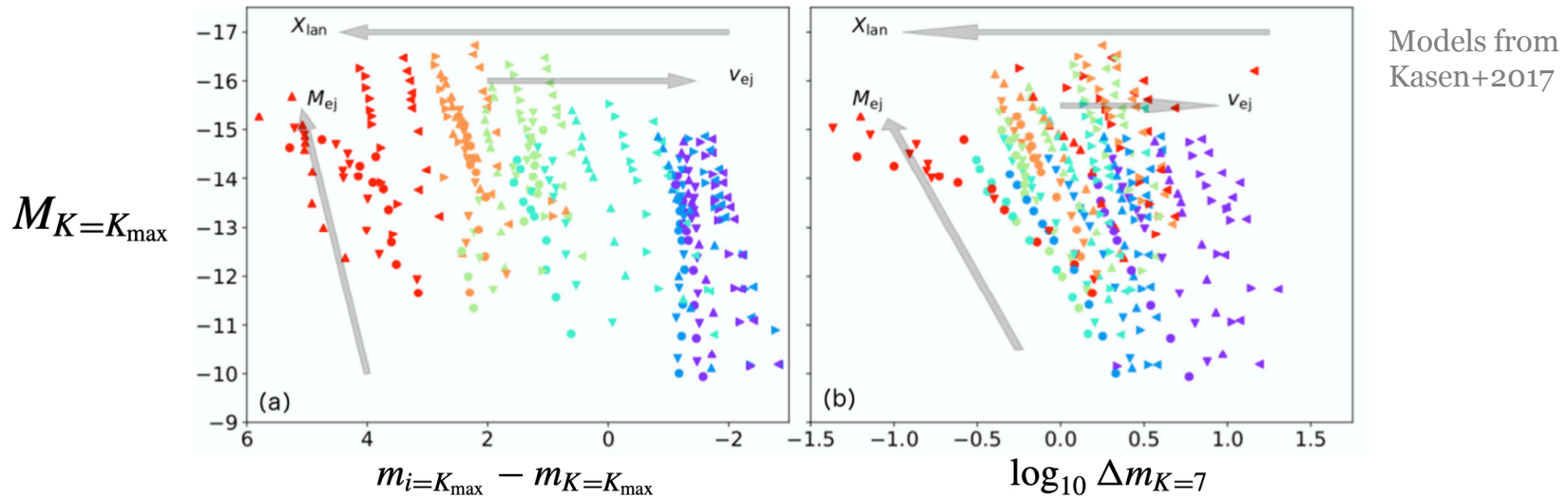
3. Constrain distance directly from kilonovae



Models from Kasen+2017

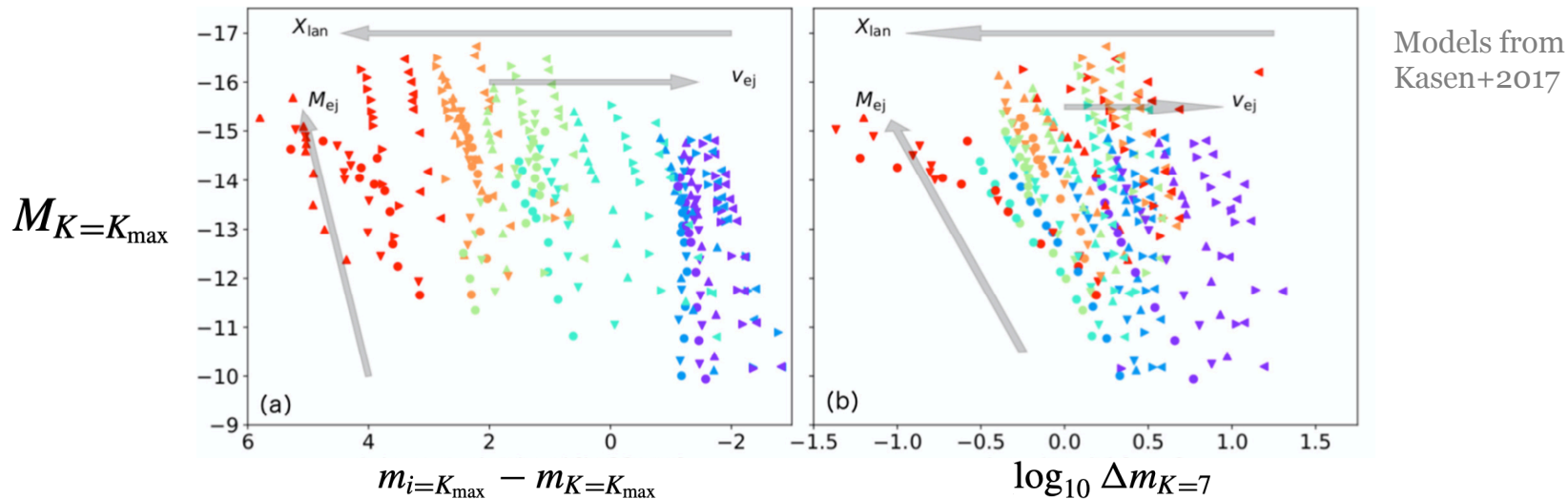
1. Use grid of kilonova models to infer absolute magnitude in the K-band

3. Constrain distance directly from kilonovae



- Use **grid of kilonova models** to infer **absolute magnitude in the K-band** as a function of:
 - Observed parameters ('measured') $M_{K=K_{max}} = f(\log_{10} \Delta m_{K=7}, \log_{10} \Delta m_{i=7}, m_{i=K_{max}} - m_{K=K_{max}})$
 - Model parameters ('inferred') $M_{K=K_{max}} = f(\log_{10} M_{ej}, v_{ej}, \log_{10} X_{lan})$

3. Constrain distance directly from kilonovae

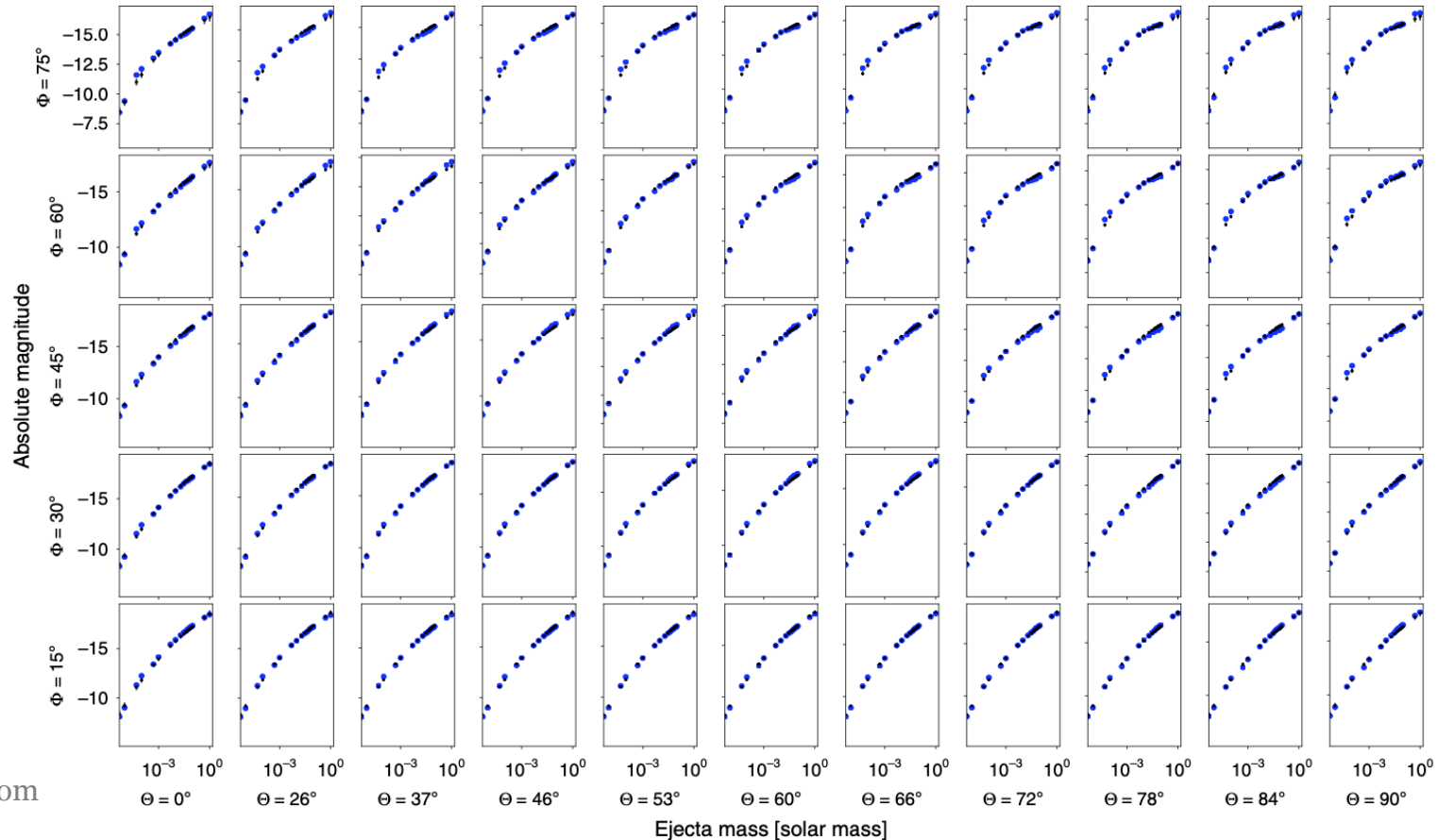


1. Use **grid of kilonova models** to infer **absolute magnitude in the K-band** as a function of:

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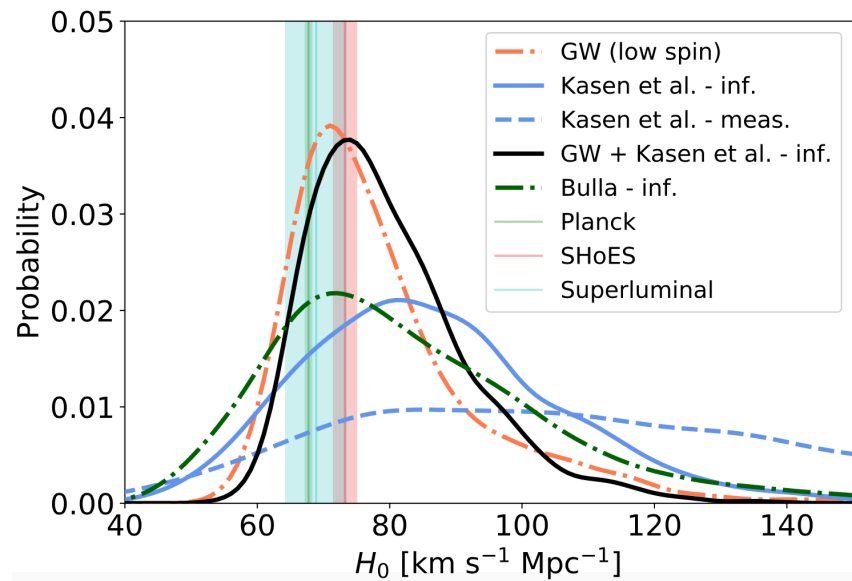
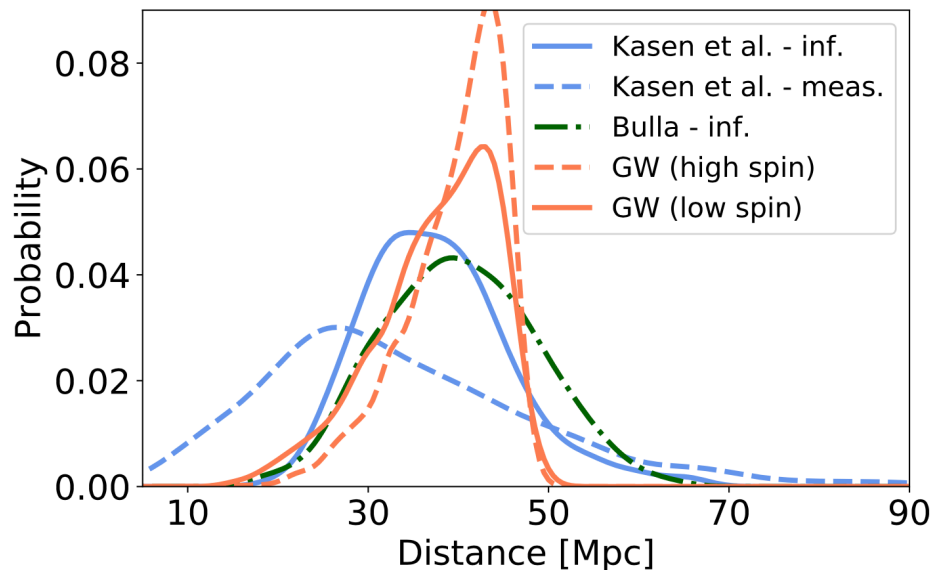
2. Infer distance modulus μ and thus **distance D**: $M_{abs} = m_{app} - \mu$ $\mu = 5 \log_{10} \left(\frac{D}{10 \text{ pc}} \right)$

3. Constrain distance directly from kilonovae



Models from
MB 2019

3. Constrain distance directly from kilonovae



GW only

$$H_0 = 74.0^{+16.0}_{-8.0} \text{ km s}^{-1} / \text{Mpc}$$

Kilonova only ('inferred')

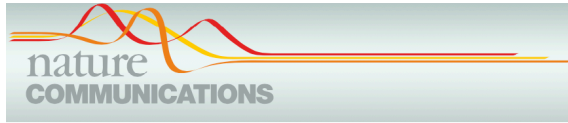
Kasen models

$$H_0 = 85.0^{+22.0}_{-17.0} \text{ km s}^{-1} / \text{Mpc}$$

Bulla models

$$H_0 = 79.0^{+23.0}_{-15.0} \text{ km s}^{-1} / \text{Mpc}$$

3. Constrain distance directly from kilonovae



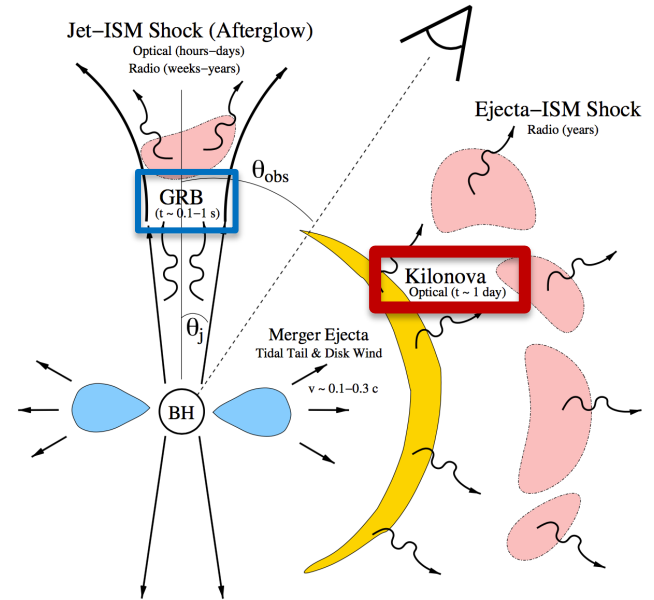
ARTICLE

<https://doi.org/10.1038/s41467-020-17998-5>

OPEN

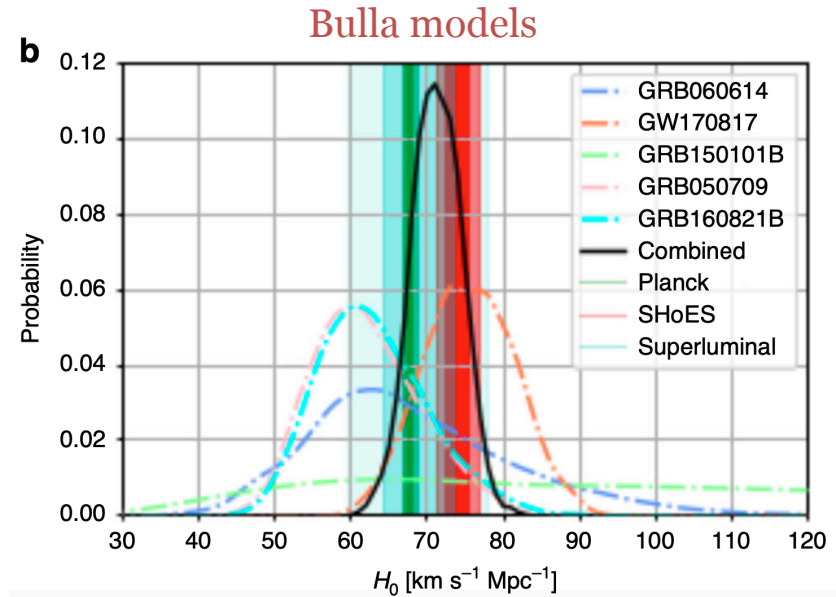
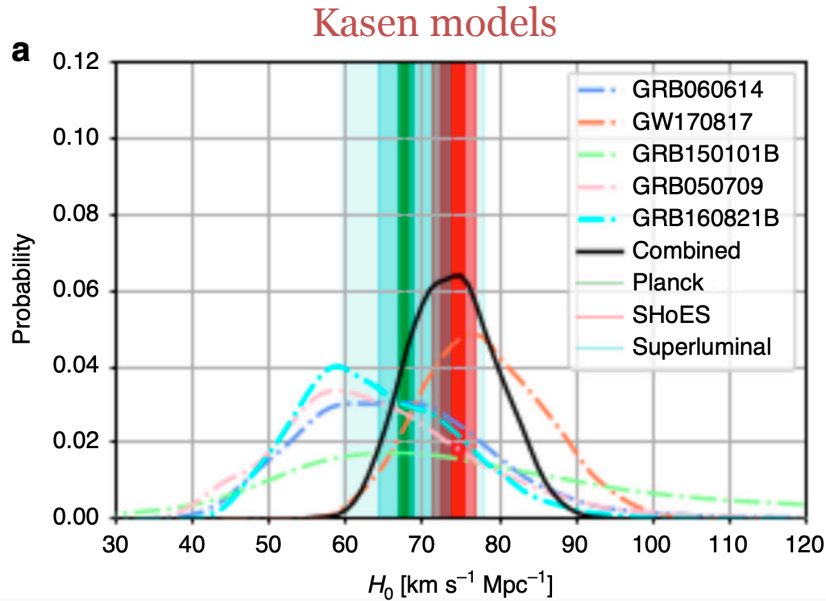
Measuring the Hubble constant with a sample of kilonovae

Michael W. Coughlin^{1,2}, Sarah Antier³, Tim Dietrich^{4,5}, Ryan J. Foley⁶, Jack Heinzel^{7,8}, Mattia Bulla⁹, Nelson Christensen^{7,8}, David A. Coulter⁶, Lina Issa^{9,10} & Nandita Khetan¹¹



Apply same technique to 4 GRBs from the literature + GW170817

3. Constrain distance directly from kilonovae



Kilonova only ('inferred')

GW only

$$H_0 = 74.0^{+16.0}_{-8.0} \text{ km s}^{-1} / \text{Mpc}$$

Kasen models

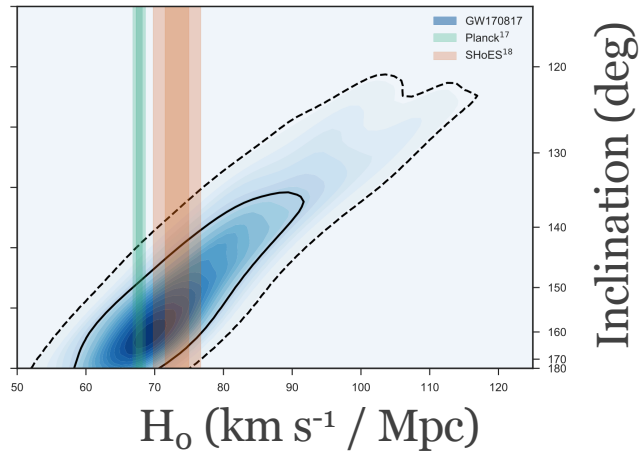
$$H_0 = 73.8^{+6.3}_{-5.8} \text{ km s}^{-1} / \text{Mpc}$$

Bulla models

$$H_0 = 71.2^{+3.2}_{-3.1} \text{ km s}^{-1} / \text{Mpc}$$

Conclusions

1. Constrain **inclination** with kilonova **light curves** -> GW + EM (improve standard sirens)
2. Constrain **inclination** with kilonova **polarization** -> GW + EM (improve standard sirens)
3. Constrain **distance** directly from **kilonovae** -> EM



$$H_0 = \frac{[\text{speed of light}] \times \text{Redshift}}{\text{Distance}}$$