Non-standard interaction effects for θ_{13} at reactor neutrino experiments

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Contents:

- Neutrino oscillations and non-standard interactions
- NSIs at sources and detectors
- Mimicking effects on θ_{13}

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Lepton flavor mixing



Dirac CP violating phase



There are now strong evidences that neutrinos are massive and lepton flavors are mixed. Since in the Standard Model neutrinos are massless particles, the SM must be extended by adding neutrino masses.

Neutrino oscillation parameters

parameter	best fit	2σ	3σ	
$\Delta m_{21}^2 \left[10^{-5} \mathrm{eV}^2 \right]$	$7.65_{-0.20}^{+0.23}$	7.25 - 8.11	7.05 - 8.34	Schwetz,
$ \Delta m_{31}^2 [10^{-3} \mathrm{eV}^2]$	$2.40^{+0.12}_{-0.11}$	2.18 - 2.64	2.07 – 2.75	Tortola,
$\sin^2 \theta_{12}$	$0.304_{-0.016}^{+0.022}$	0.27 – 0.35	0.25 – 0.37	Valle, 08
$\sin^2 \theta_{23}$	$0.50^{+0.07}_{-0.06}$	0.39 – 0.63	0.36 – 0.67	
$\sin^2 heta_{13}$	$0.01\substack{+0.016\\-0.011}$	≤ 0.040	≤ 0.056	

Unknowns:

- **1**. θ₁₃
- 3. Dirac or Majorana?
- 5. Leptonic CP violation?
- 2. Sign of Δm_{31}^2
- 4. Absolute masses
- 6. Sterile neutrino?

NSI Effects for theta_13 at Reactor Neutrino Experiments

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Experimental steps:

Improve present measurements of solar and atmospheric parameters.

Discover the last mixing angle θ_{13} (Daya Bay, Double Chooz) CP violating phase (δ) in the future Long baseline experiments (v-Factory, β -beam).

17 October 2008

NSI Effects for theta_13 at Reactor Neutrino Experiments

New physics for neutrino oscillations

• unitarity violation $UU^{\dagger} \neq 1$

Combined analysis of neutrino oscillations, W and Z decays, rare LFV modes and lepton universality tests. (Antusch, et al., 06) Natural consequence in seesaw models

 $|VV^{\dagger}| \approx \begin{pmatrix} 0.994 \pm 0.005 & < 7.0 \times 10^{-5} & < 1.6 \times 10^{-2} \\ < 7.0 \times 10^{-5} & 0.995 \pm 0.005 & < 1.02 \times 10^{-2} \\ < 1.6 \times 10^{-2} & < 1.02 \times 10^{-2} & 0.995 \pm 0.005 \end{pmatrix}$

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non-standard interactions at neutrino sources

$$\pi^+ \to \mu^+ + \nu_e, \quad \mu^+ \to e^+ + \overline{\nu}_\mu + \nu_\mu, \quad n \to p + e^- + \overline{\nu}_\mu$$

(standard:
$$\pi^+ \to \mu^+ + \nu_{\mu}, \quad \mu^+ \to e^+ + \overline{\nu}_{\mu} + \nu_e, \quad n \to p + e^- + \overline{\nu}_e$$
)

non-standard interactions at neutrino detectors

$$\nu_e + n \rightarrow p + \mu^-$$
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These effects can be measured even for L=0 (near detector $P_{\mu e}$ (L=0) \neq 0)

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non-standard interactions with matter during propagation

$$\mathcal{L}_{\text{eff}}^{\text{NSI}} = -2\sqrt{2}\,\varepsilon_{\alpha\beta}^{fP}G_F(\overline{\nu}_{\alpha}\gamma_{\mu}P_L\nu_{\beta})\,(\overline{f}\gamma^{\mu}Pf)$$

Constraint by experiments with neutrinos and charged leptons. (Davidson, et al., 03; M. Blennow, coming soon) $\begin{aligned} -0.9 < \varepsilon_{ee} < 0.75 \quad |\varepsilon_{e\mu}| \lesssim 3.8 \times 10^{-4} \quad |\varepsilon_{e\tau}| \lesssim 0.25 \\ -0.05 < \varepsilon_{\mu\mu} < 0.08 \quad |\varepsilon_{\mu\tau}| \lesssim 0.25 \\ |\varepsilon_{\tau\tau}| \lesssim 0.4 \end{aligned}$

• The neutrino states produced in the source and observed in the detector are the superpositions of pure orthonormal flavor states.

$$|\nu_{\alpha}^{s}\rangle = \frac{1}{N_{\alpha}^{s}} \left(|\nu_{\alpha}\rangle + \sum_{\beta=e,\mu,\tau} \varepsilon_{\alpha\beta}^{s} |\nu_{\beta}\rangle \right)$$
$$\langle \nu_{\beta}^{d}| = \frac{1}{N_{\beta}^{d}} \left(\langle \nu_{\beta}| + \sum_{\alpha=e,\mu,\tau} \varepsilon_{\alpha\beta}^{d} \langle \nu_{\alpha}| \right)$$

Normalization factors

$$N_{\alpha}^{s} = \sqrt{\left[\left(\mathbbm{1} + \varepsilon^{s}\right)\left(\mathbbm{1} + \varepsilon^{s\dagger}\right)\right]_{\alpha\alpha}}$$

$$N_{\beta}^{d} = \sqrt{\left[\left(\mathbbm{1} + \varepsilon^{d\dagger}\right)\left(\mathbbm{1} + \varepsilon^{d}\right)\right]_{\beta\beta}}$$

NSI Effects for theta_13 at Reactor Neutrino Experiments

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• Effective Hamiltonian in matter

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$$V_{\rm CC} = \sqrt{2}G_F N_e$$

$$\hat{H} = H_0 + H_m + H_{\text{NSI}} = \frac{1}{2E} U \text{diag}(m_1^2, m_2^2, m_3^2) U^{\dagger} + \text{diag}(V_{\text{CC}}, 0, 0) + V_{\text{CC}} \varepsilon^m$$

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• Effective mixing matrix and mass squared eigenvalues in matter.

$$\hat{H} = \frac{1}{2E} \hat{U} \text{diag} \left(\hat{m}_1^2, \hat{m}_2^2, \hat{m}_3^2 \right) \hat{U}^{\dagger}$$

For reactor neutrinos, $H_0 \gg H_m \otimes H_{NSI} \rightarrow \hat{U} \simeq U, \ \hat{m}_i \simeq m_i$

NSI Effects for theta_13 at Reactor Neutrino Experiments

- Amplitude for the process $\, \nu^s_{lpha}
ightarrow \, \nu^d_{eta} \,$

$$A_{\alpha\beta} = \sum_{i} \hat{U}_{\alpha i}^* \hat{U}_{\beta i} \mathrm{e}^{-\mathrm{i}\frac{\hat{m}_i^2 L}{2E}}$$

$$\begin{aligned} \mathcal{A}_{\alpha\beta}(L) &= \frac{1}{N_{\alpha}^{s}N_{\beta}^{d}} \langle \nu_{\beta}^{d} | \mathrm{e}^{-\mathrm{i}\hat{H}L} | \nu_{\alpha}^{s} \rangle = \frac{1}{N_{\alpha}^{s}N_{\beta}^{d}} (\mathbb{1} + \varepsilon^{d})_{\rho\beta} A_{\gamma\rho} (\mathbb{1} + \varepsilon^{s})_{\alpha\gamma} \\ &= \frac{1}{N_{\alpha}^{s}N_{\beta}^{d}} \left[(\mathbb{1} + \varepsilon^{d})^{T} A^{T} (\mathbb{1} + \varepsilon^{s})^{T} \right]_{\beta\alpha} = \frac{1}{N_{\alpha}^{s}N_{\beta}^{d}} \left[A + \varepsilon^{s} A + A\varepsilon^{d} + \varepsilon^{s} A\varepsilon^{d} \right]_{\alpha\beta} \end{aligned}$$

Oscillation probability

$$P(\nu_{\alpha}^{s} \rightarrow \nu_{\beta}^{d}) = |\mathcal{A}_{\alpha\beta}(L)|^{2}$$

$$= \sum_{i,j} \mathcal{J}_{\alpha\beta}^{i} \mathcal{J}_{\alpha\beta}^{j*} - 4 \sum_{i>j} \operatorname{Re}(\mathcal{J}_{\alpha\beta}^{i} \mathcal{J}_{\alpha\beta}^{j*}) \sin^{2} \frac{\Delta \hat{m}_{ij}^{2} L}{4E}$$

$$+ 2 \sum_{i>j} \operatorname{Im}(\mathcal{J}_{\alpha\beta}^{i} \mathcal{J}_{\alpha\beta}^{j*}) \sin \frac{\Delta \hat{m}_{ij}^{2} L}{2E} .$$

$$\overline{\mathcal{J}_{\alpha\beta}^{i}} = \frac{\hat{U}_{\alpha i}^{*} \hat{U}_{\beta i} + \sum_{\gamma} \varepsilon_{\alpha\gamma}^{s} \hat{U}_{\gamma i}^{*} \hat{U}_{\beta i} + \sum_{\gamma} \varepsilon_{\gamma\beta}^{d} \hat{U}_{\alpha i}^{*} \hat{U}_{\gamma i} + \sum_{\gamma,\rho} \varepsilon_{\alpha\gamma}^{s} \varepsilon_{\rho\beta}^{d} \hat{U}_{\gamma i}^{*} \hat{U}_{\rho i}}{N_{\alpha}^{s} N_{\beta}^{d}}$$

NSI Effects for theta_13 at Reactor Neutrino Experiments

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• Oscillation probability $P(\nu_{\alpha}^{s} \rightarrow \nu_{\beta}^{d}) = |\mathcal{A}_{\alpha\beta}(L)|^{2}$ $= \sum_{i,j} \mathcal{J}_{\alpha\beta}^{i} \mathcal{J}_{\alpha\beta}^{j*} - 4 \sum_{i>j} \operatorname{Re}(\mathcal{J}_{\alpha\beta}^{i} \mathcal{J}_{\alpha\beta}^{j*}) \sin^{2} \frac{\Delta \hat{m}_{ij}^{2} L}{4E}$ $+ 2 \sum_{i>j} \operatorname{Im}(\mathcal{J}_{\alpha\beta}^{i} \mathcal{J}_{\alpha\beta}^{j*}) \sin \frac{\Delta \hat{m}_{ij}^{2} L}{2E} .$ $\mathcal{J}_{\alpha\beta}^{i} = \frac{\hat{U}_{\alpha i}^{*} \hat{U}_{\beta i} + \sum_{\gamma} \varepsilon_{\alpha \gamma}^{s} \hat{U}_{\gamma i}^{*} \hat{U}_{\beta i} + \sum_{\gamma} \varepsilon_{\gamma \beta}^{d} \hat{U}_{\alpha i}^{*} \hat{U}_{\gamma i} + \sum_{\gamma, \rho} \varepsilon_{\alpha \gamma}^{s} \varepsilon_{\rho \beta}^{d} \hat{U}_{\gamma i}^{*} \hat{U}_{\rho i}}{N_{\alpha}^{s} N_{\beta}^{d}}$

NSI Effects for theta_13 at Reactor Neutrino Experiments



- Only V±A type of NSIs are involved at the source and detector.
- Average energy $E \approx 3 \text{ MeV} \rightarrow \text{matter effects are irrelevant.}$
- $\varepsilon^{s} = \varepsilon^{d\dagger}$ ($\varepsilon^{s} < 0.1$, $\varepsilon^{d} < 0.2$ from universality in lepton decay)

Short baseline experiments (Daya Bay & D-Chooz)

Oscillation probability

$$P(\bar{\nu}_e^s \to \bar{\nu}_e^d) \simeq 1 - \sin^2 2\tilde{\theta}_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

• Effective mixing angle

$$\tilde{s}_{13}^2 = s_{13}^2 + 2s_{13} \left[s_{23} \cos(\delta - \phi_{e\mu}) |\varepsilon_{e\mu}| + c_{23} \cos(\delta - \phi_{e\tau}) |\varepsilon_{e\tau}| \right]$$

 $+s_{23}^{2}|\varepsilon_{e\mu}|^{2}+c_{23}^{2}|\varepsilon_{e\tau}|^{2}+2|\varepsilon_{e\mu}||\varepsilon_{e\tau}|s_{23}c_{23}\cos(\phi_{e\mu}-\phi_{e\tau})+\mathcal{O}(\varepsilon^{3},\varepsilon s_{13}^{2})$

- Only $\varepsilon_{e\mu}$ and $\varepsilon_{e\tau}$ are involved
- Invariant with respect to the exchange $\epsilon_{e\mu} \leftrightarrow \epsilon_{e\tau}$
- A minimum exists at the position $s_{13}|_{\min} = -s_{23}\cos(\delta - \phi_{e\mu})|\varepsilon_{e\mu}| - c_{23}\cos(\delta - \phi_{e\tau})|\varepsilon_{e\tau}|$
- CP violating phases enter the oscillation probability explicitly

NSI Effects for theta_13 at Reactor Neutrino Experiments



- $\theta_{13} < 14^{\circ}$, which is larger than the Chooz bound 10°
- In despite a very small θ_{13} , a sizable effective mixing angle can be gained due to the mimicking effects.
- Even if the effective mixing angle is too small to be measured in a reactor experiment, a discovery search of a non-vanishing θ_{13} may still be carried out at future neutrino factories.

NSI Effects for theta_13 at Reactor Neutrino Experiments

Short baseline experiments (Daya Bay & D-Chooz)

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 The shadings correspond ε<0.05, ε<0.01 and ε<0.001, respectively.

NSI Effects for theta_13 at Reactor Neutrino Experiments

Medium baseline experiments (KamLAND)

• Oscillation probability

$$\overline{P(\bar{\nu}_e^s \to \bar{\nu}_e^d)} \simeq 1 - \sin^2 2\tilde{\theta}_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E}$$

• To improve the accuracy of current measurement, a baseline length ~ 50 km (the first minimum related with Δm_{21}^2) should be taken for next generation experiments.

• Effective mixing angle

$$\tilde{s}_{12}^2 = s_{12}^2 + 2s_{12}c_{12}\left[c_{23}\cos(\phi_{e\mu})|\varepsilon_{e\mu}| - s_{23}\cos(\phi_{e\tau})|\varepsilon_{e\tau}|\right] + \mathcal{O}(\varepsilon s_{13}, s_{13}^2)$$

- Only $\epsilon_{e\mu}$ and $\epsilon_{e\tau}$ are involved \rightarrow reactor experiments are not sensitive to ϵ_{ee}
- Since the magnitude of θ_{12} is more sizable compared to θ_{13} , NSI effects cannot mimic an effective mixing angle with a vanishing θ_{12} . However, NSIs may significantly modify the observed effective mixing angle.

NSI Effects for theta_13 at Reactor Neutrino Experiments



- The true value of θ_{12} may be remarkably different from the measured one, i.e., there exists a degeneracy in θ_{12}
- 26°<θ₁₂ < 42°, which is close to the bi-maximal mixing for its upper bound and deviates much from the tri-bimaximal mixing for its lower bound.

NSI Effects for theta_13 at Reactor Neutrino Experiments

Medium baseline experiments (KamLAND)





- Oscillation probabilities in a medium baseline experiment.
- The shadings correspond ε<0.05, ε<0.01 and ε<0.001, respectively.
- The oscillation behaviors around L≈0 are mainly induced by Δm₃₁² and θ₁₃

NSI Effects for theta_13 at Reactor Neutrino Experiments



• The true value of θ_{12} may achieve the range of Cabibbo angle. Some hints on the quark-lepton complementary?

NSI Effects for theta_13 at Reactor Neutrino Experiments

Conclusions

- Mixing angles measured in reactor neutrino experiments could be dramatically modified by NSIs at sources and detectors.
- The mimicking effects induced by NSIs play a very important role in short baseline experiments, especially in the case of a tiny θ_{13} . Even for a vanishing θ_{13} , the forthcoming Double Chooz and Daya Bay experiments could still perform a discovery search of an oscillation phenomenon.
- From the phenomenological point of view, two different and complementary oscillation experiments (e.g. reactor and neutrino factory) are needed in order to constrain corresponding NSIs.

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