



# Modeling the Evolutionary Dynamics of Novel Infectious Diseases

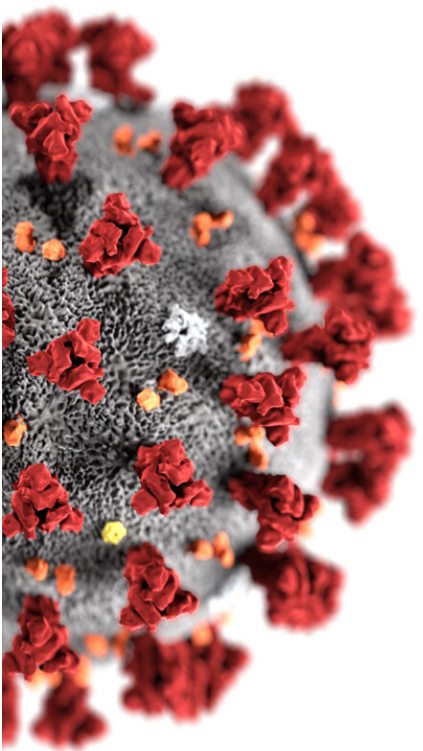
**Troy Day**

Dept. Mathematics and Statistics

Queen's University, Kingston, Canada



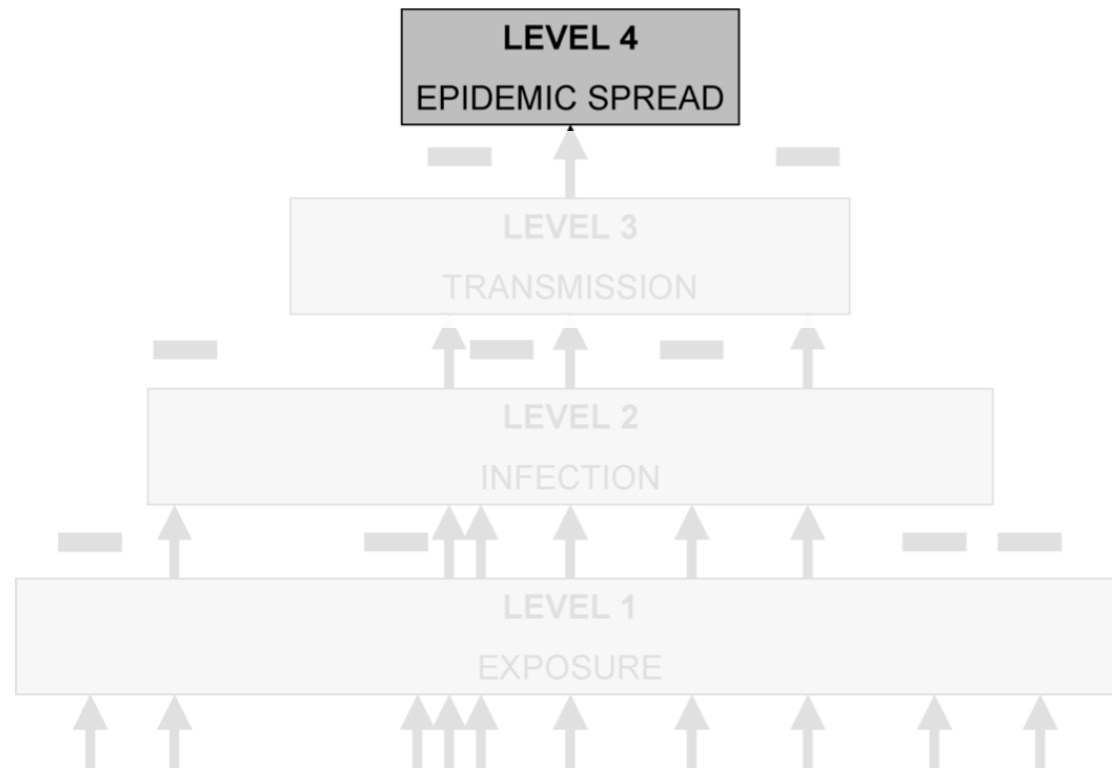
June 2023



# Outline

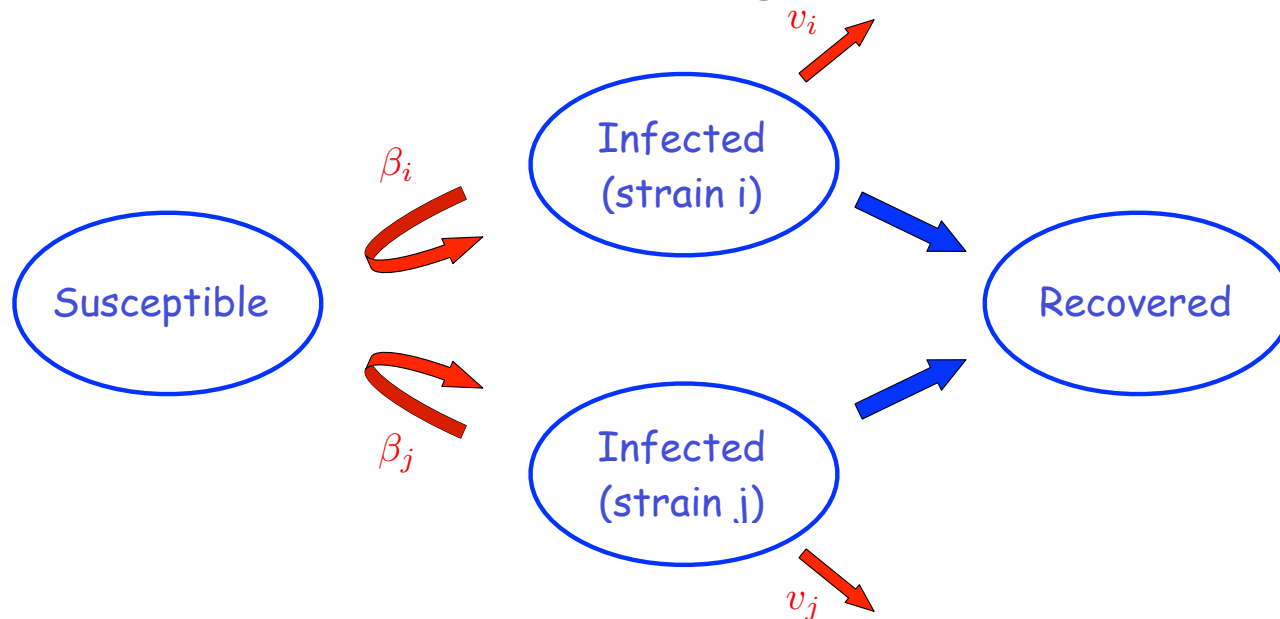
- Pathogen adaptation during epidemics
- Patterns of SARS-CoV-2 evolution
- Vaccination and pathogen evolution

# The Emergence of Infectious Diseases



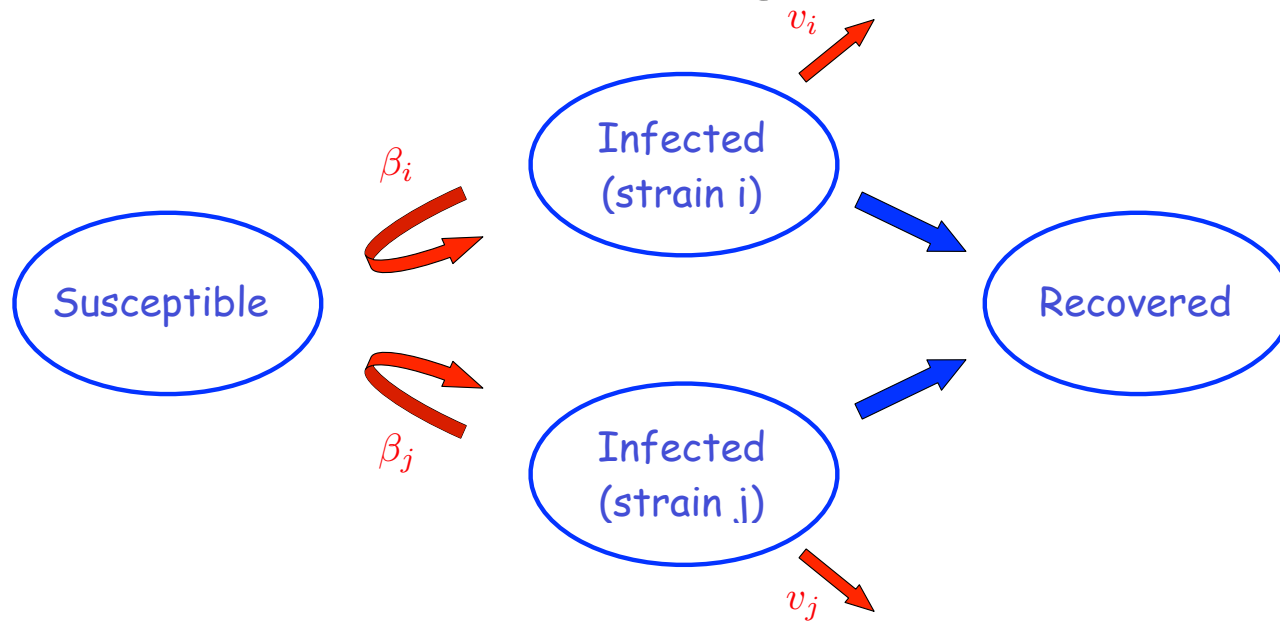
Wolfe et al. 2007. *Nature*, 447: 279; Woolhouse and Gaunt. 2007. *Critical Reviews in Microbiology*, 33:231

# Adaptation During Epidemics



$$\frac{dS}{dt} = -S \sum_i \beta_i I_i$$
$$\frac{dI_i}{dt} = S \beta_i I_i - (v_i + c) I_i$$

# Adaptation During Epidemics



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$$\frac{dS}{dt} = -S \bar{\beta} I$$

$$\frac{dI}{dt} = S \bar{\beta} I - (\bar{v} + c) I$$

$$\frac{dp_i}{dt} = p_i (r_i - \bar{r})$$

$$I = \sum_i I_i$$

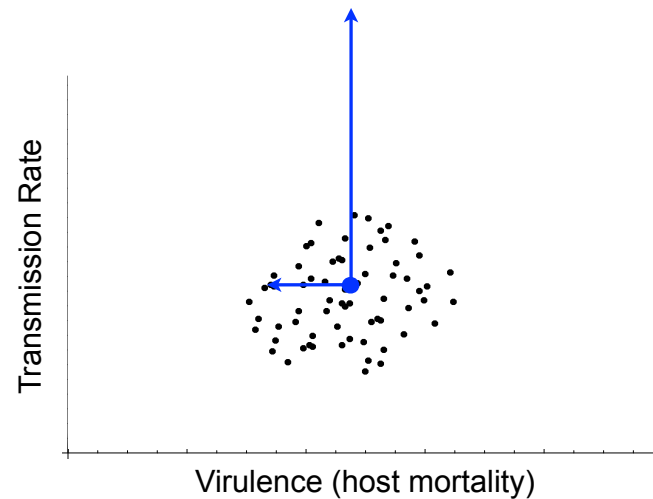
$$p_i = I_i / I$$

$$r_i = S \beta_i - (v_i + c)$$

$$\bar{x} = \sum_i x_i p_i$$

# Transmission and Virulence Evolution

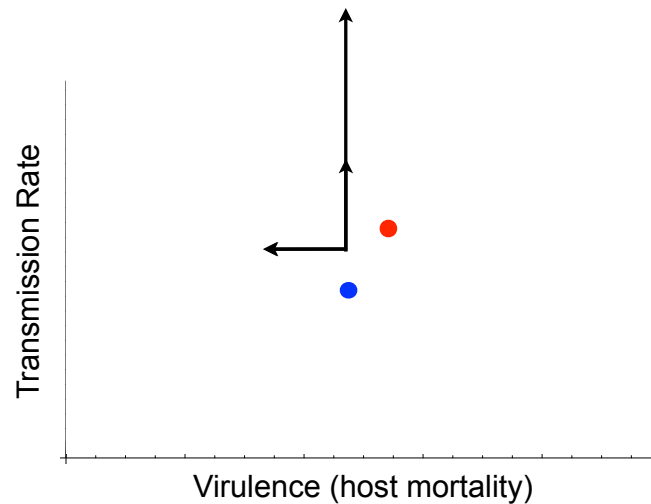
$$\begin{aligned} \frac{d\bar{\beta}}{dt} &= \sigma_{\beta\beta}S - \sigma_{v\beta} \\ \frac{d\bar{v}}{dt} &= \sigma_{v\beta}S - \sigma_{vv} \end{aligned} \quad \begin{bmatrix} d\bar{\beta}/dt \\ d\bar{v}/dt \end{bmatrix} = \mathbf{G} \cdot \begin{bmatrix} S \\ -1 \end{bmatrix}$$



# Transmission and Virulence Evolution

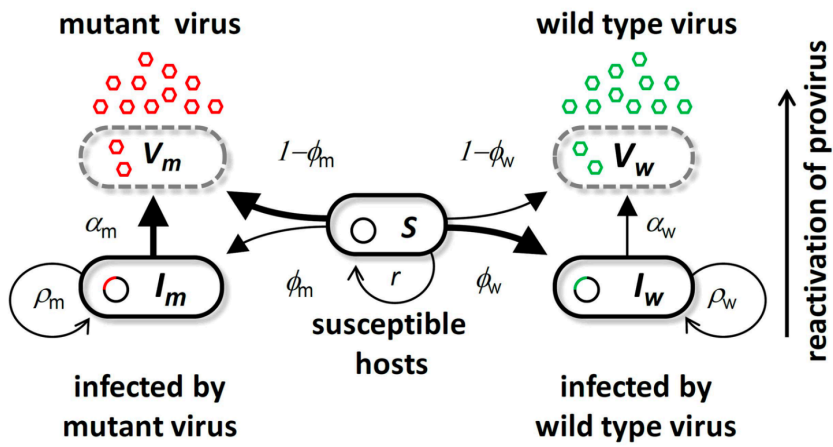
$$\frac{dp}{dt} = p(1 - p)\Delta r$$

$$\begin{aligned}\Delta r &= r_1 - r_2 \\ &= \Delta\beta S - \Delta v\end{aligned}$$

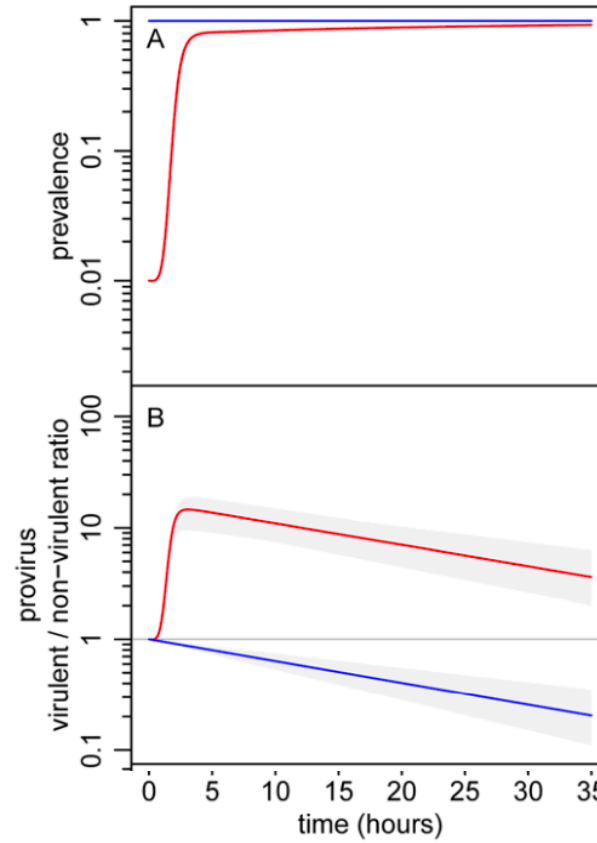


Lenski and May. 1994. *JTB* 169:253; Frank. 1996. *Quart Rev. Biol.* 71:37; Day and Proulx. 2004. *Am Nat* 163:E40; Day and Gandon. 2005. In *Disease Evolution: Models, Concepts, and Data Analysis*; Day and Gandon, 2007. *Ecology Letters* 10: 876; Bull and Ebert 2008. *Evol App* 1:172

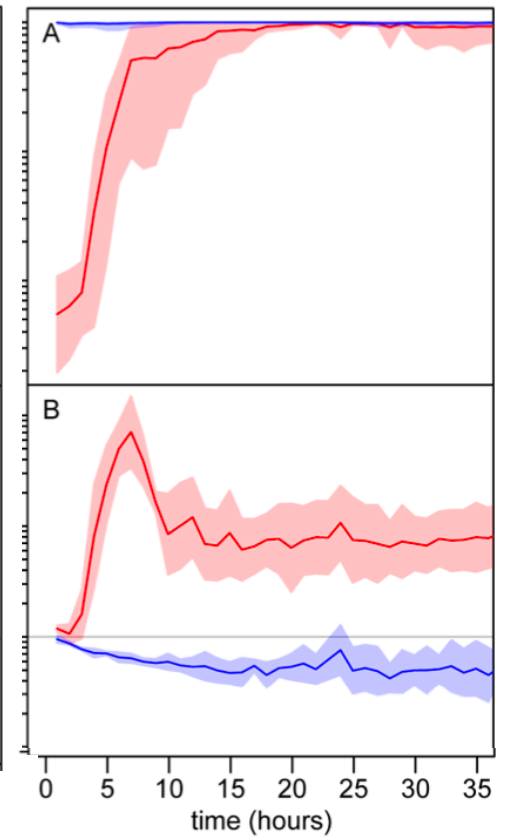
### Lambda phage and *E. coli*



### Model

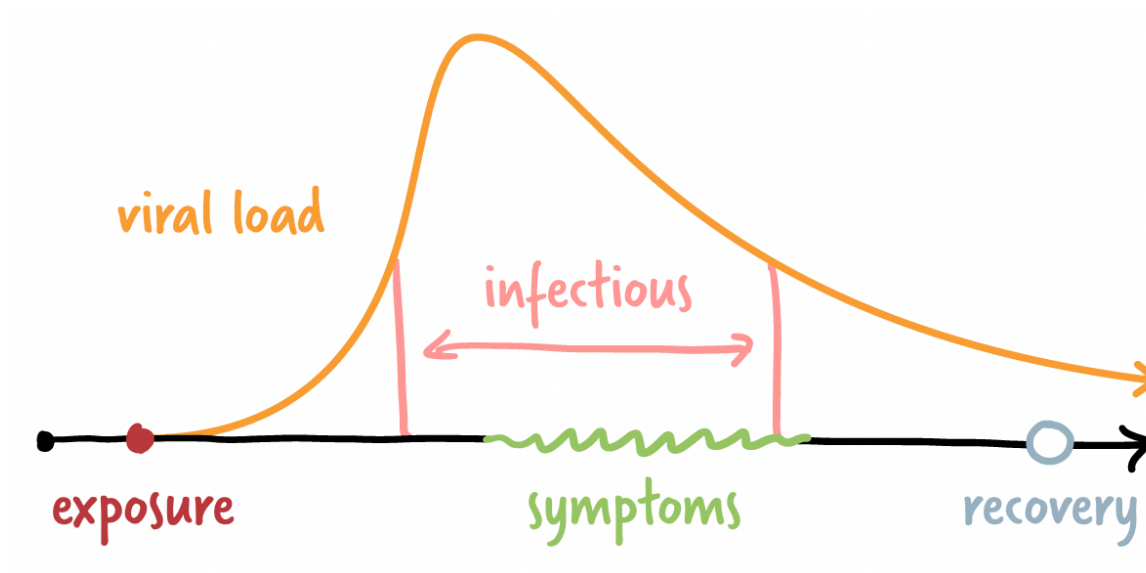


### Experiment





# What About Timing of Transmission and Virulence?



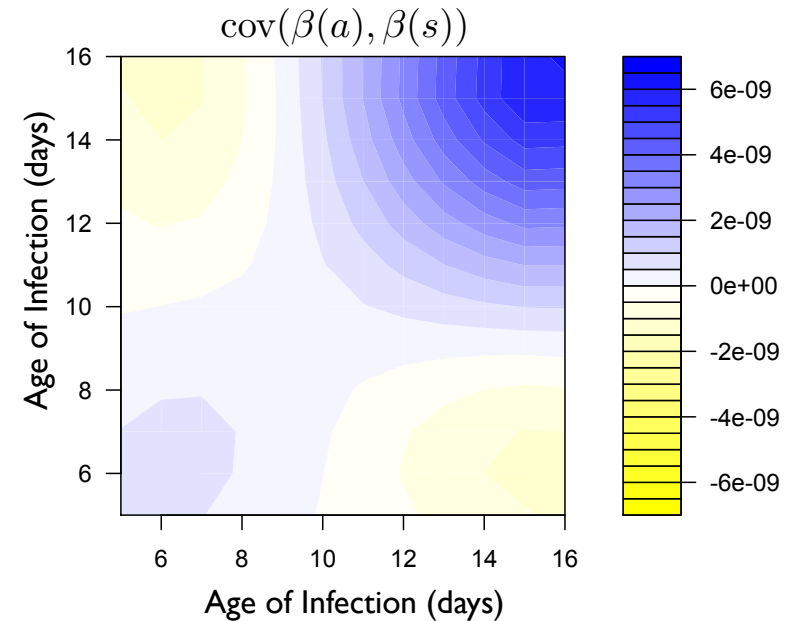
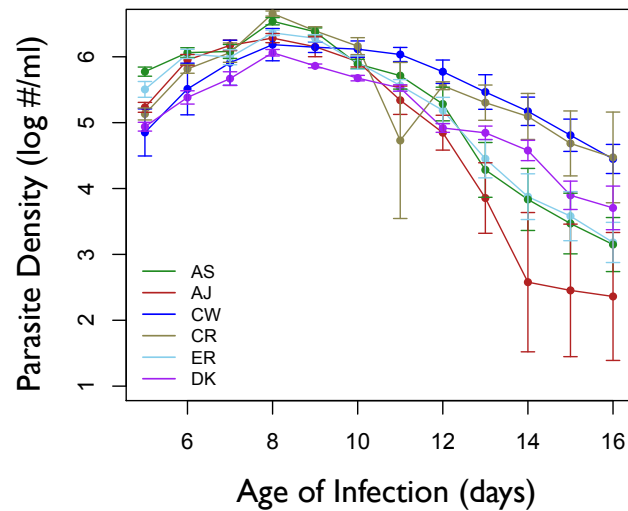
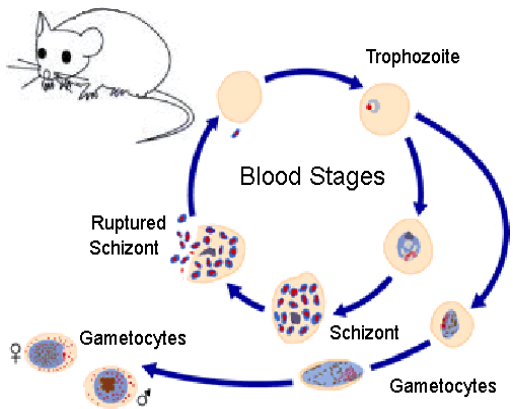
# Transmission Rate Evolution

$$\dot{\beta} \propto S \sigma_{\beta\beta}$$

$$\dot{\beta}(a) \propto S \int_0^\infty q(s) G_{\beta,\beta}(a, s) ds$$

$$G_{\beta,\beta} = \text{cov}(\beta(a), \beta(s))$$

$$q(s) = I(s) / \int I(a) da$$



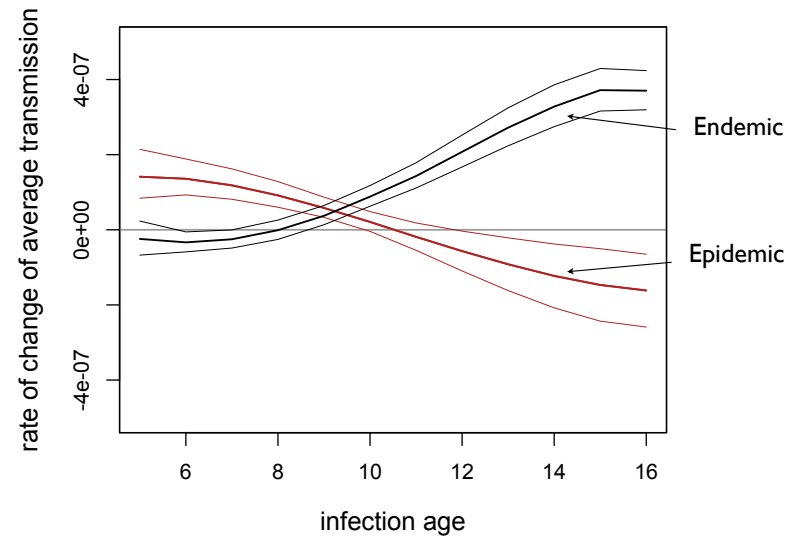
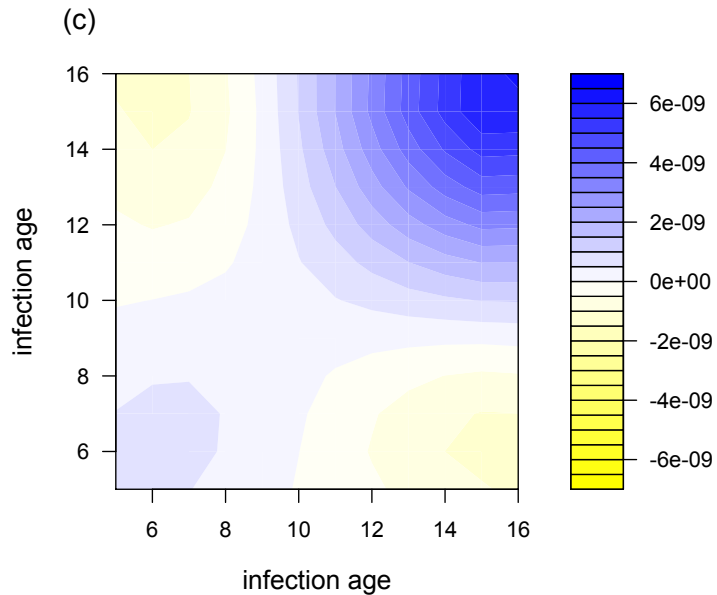
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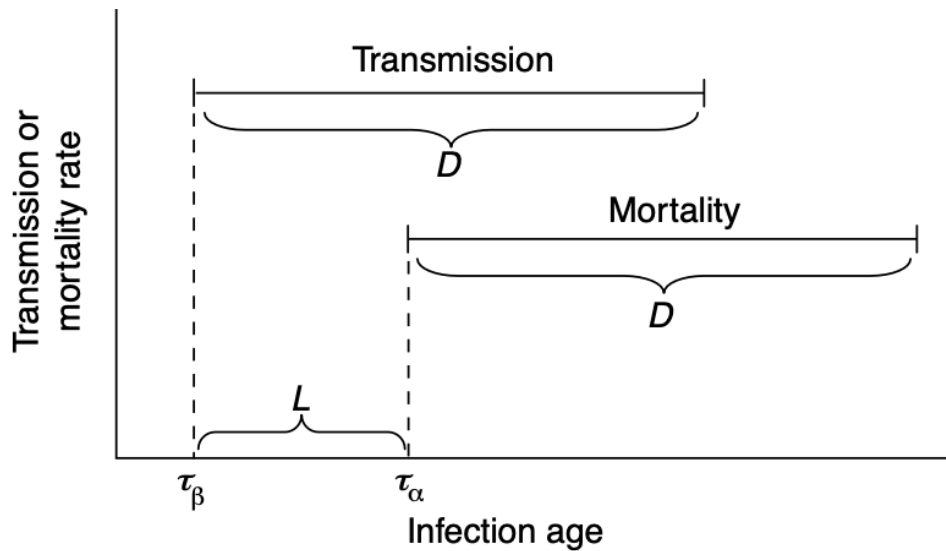
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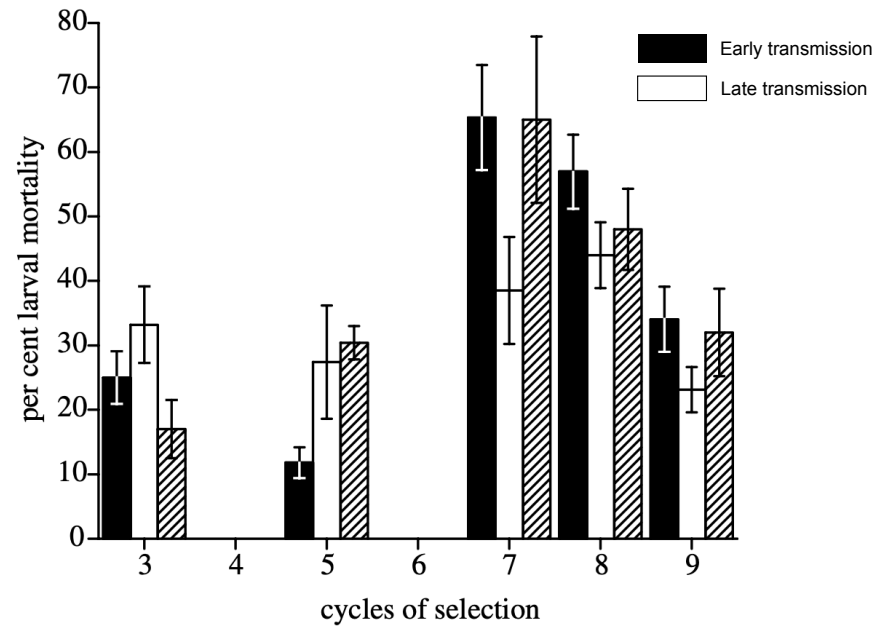
# Virulence Evolution



*TRENDS in Ecology & Evolution*

Day. 2003. *TREE* 18:113

Virulence of nuclear polyhedrosis virus in gypsy moths

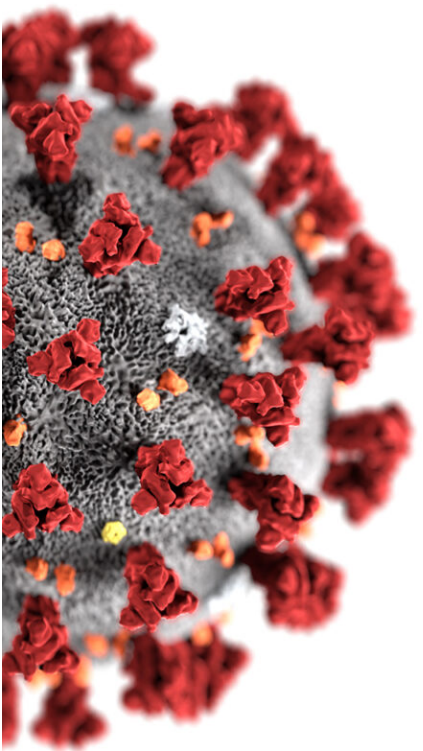


Cooper, V.S. et al. 2002. *Proc R Soc Lond B* 269:1161

# Adaptation During Epidemics

## - General Predictions -

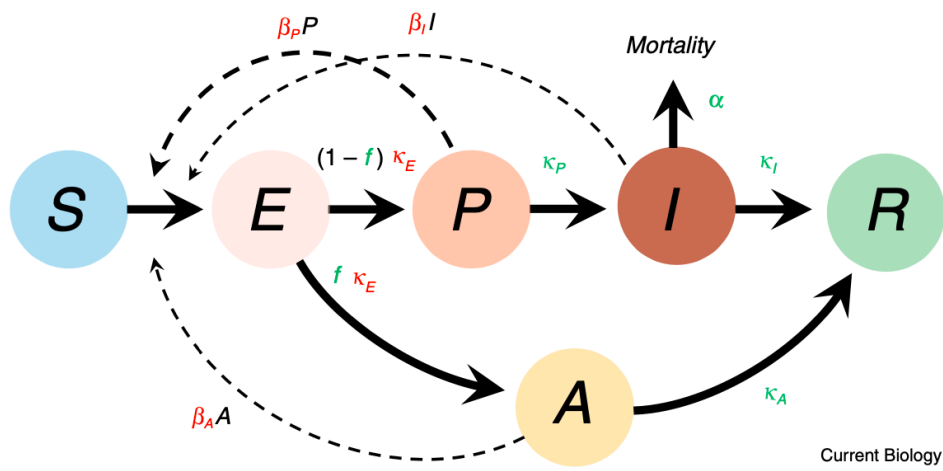
1. Strong selection for increased transmission rate during pandemic.
2. Strong selection for earlier transmission during a pandemic.
3. Weak selection against virulence if transmission occurs before symptoms.



# Outline

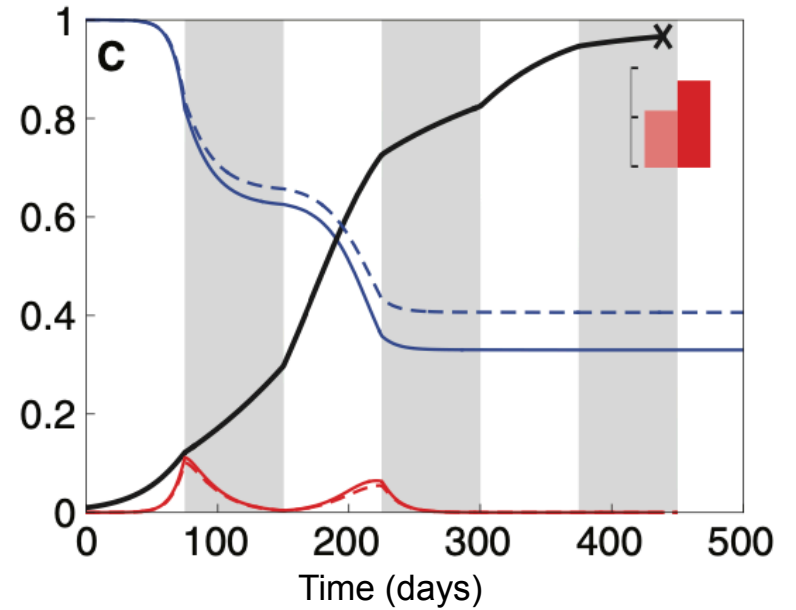
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# Evolution in SARS-CoV-2



Current Biology

Transmission & Virulence



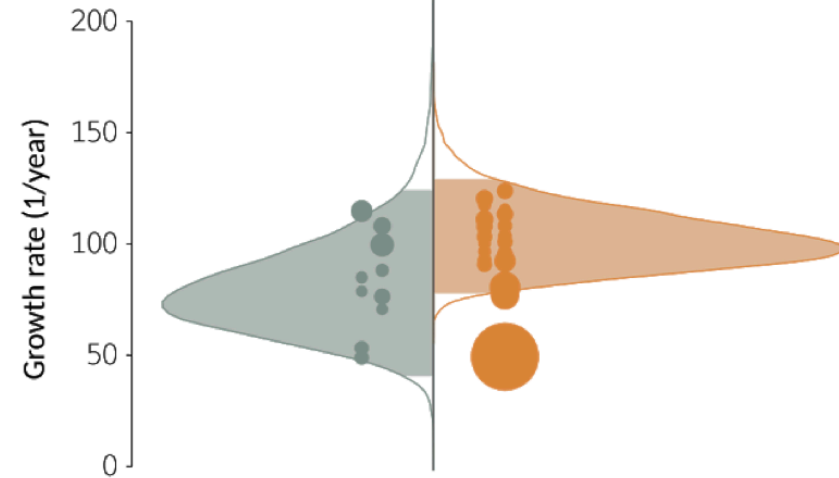
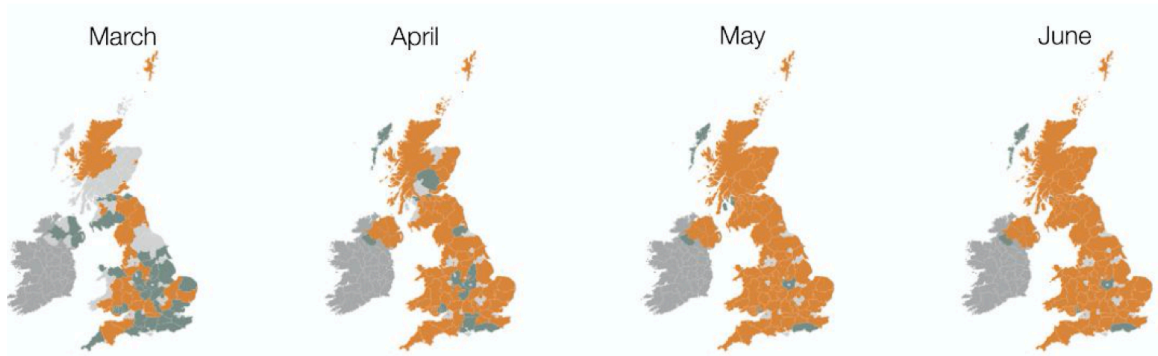
$$\frac{dp}{dt} = p(1-p)\Delta r$$

$$\begin{aligned} \Delta r &= r_1 - r_2 \\ &= \Delta\beta S - \Delta v \end{aligned}$$

# D614G Spike Mutation

 -wildtype

 -D614G spike mutation



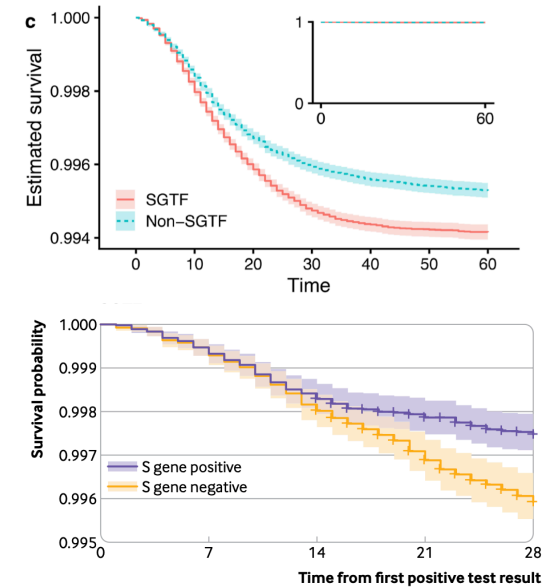
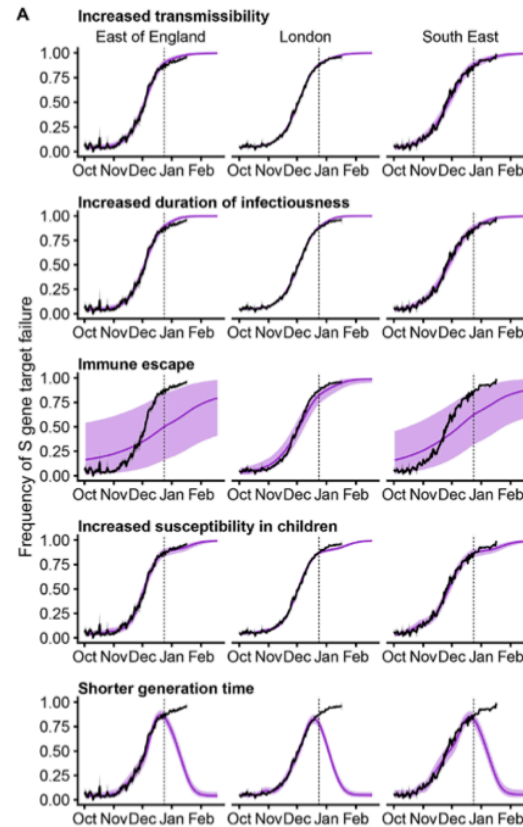
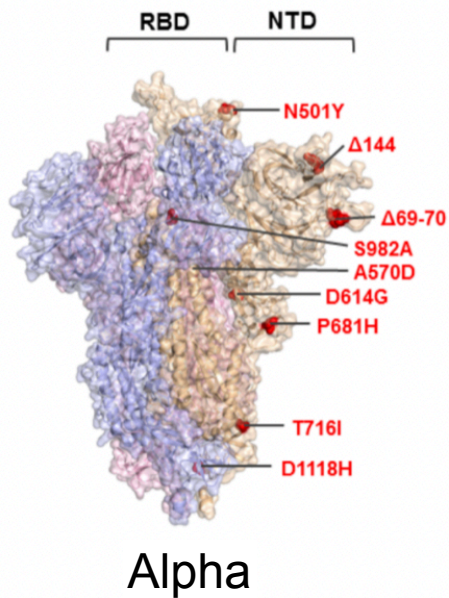
## Evaluating the effects of SARS-CoV-2 Spike mutation D614G on transmissibility and pathogenicity

### Authors:

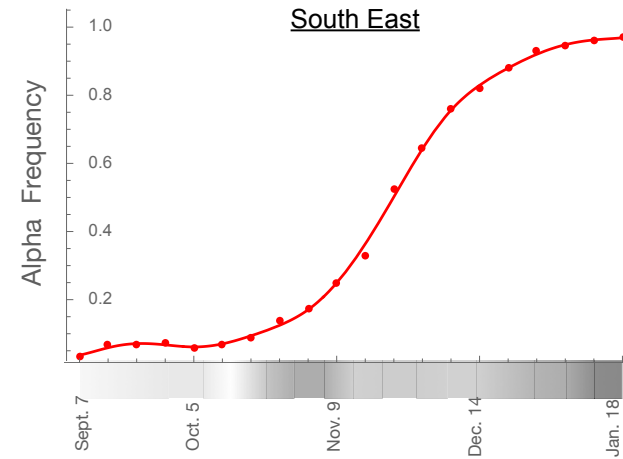
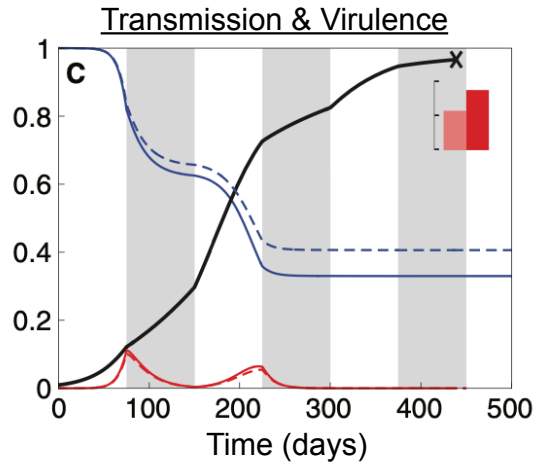
Erik Volz<sup>\*1</sup>, Verity Hill<sup>2</sup>, John T. McCrone<sup>2</sup>, Anna Price<sup>3</sup>, David Jorgensen<sup>1</sup>, Áine O'Toole<sup>2</sup>, Joel Southgate<sup>3,4</sup>, Robert Johnson<sup>1</sup>, Ben Jackson<sup>2</sup>, Fabricia F. Nascimento<sup>1</sup>, Sara M. Rey<sup>4</sup>, Samuel M. Nicholls<sup>5</sup>, Rachel M. Colquhoun<sup>2</sup>, Ana da Silva Filipe<sup>5</sup>, James Shepherd<sup>6</sup>, David J. Pascall<sup>7</sup>, Rajiv Shah<sup>6</sup>, Natasha Jesudason<sup>6</sup>, Kathy Li<sup>6</sup>, Ruth Jarrett<sup>6</sup>, Nicole Pacchiarini<sup>4</sup>, Matthew Bull<sup>4</sup>, Lily Geidelberg<sup>1</sup>, Igor Siveroni<sup>1</sup>, Ian Goodfellow<sup>8</sup>, Nicholas J. Loman<sup>5</sup>, Oliver G. Pybus<sup>8,9</sup>, David L. Robertson<sup>6</sup>, Emma C. Thomson<sup>6</sup>, Andrew Rambaut<sup>\*2</sup>, Thomas R. Connor<sup>\*3,4,11</sup>, on behalf of the CoG-UK consortium<sup>12</sup>



# Transmission-Virulence Evolution in SARS-CoV-2



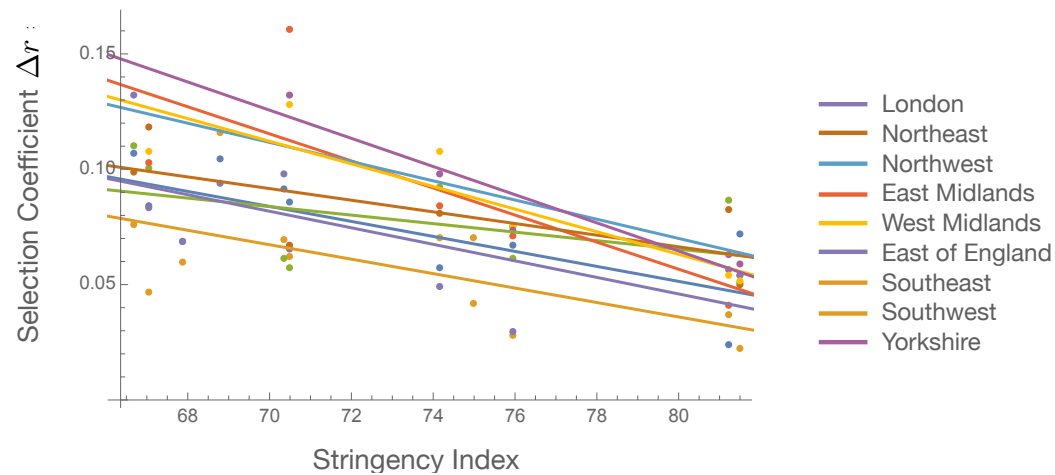
# Transmission-Virulence Evolution in SARS-CoV-2



$$\frac{dp}{dt} = p(1-p)\Delta r$$

$$\Delta r = r_1 - r_2$$

$$= \Delta\beta S - \Delta v$$

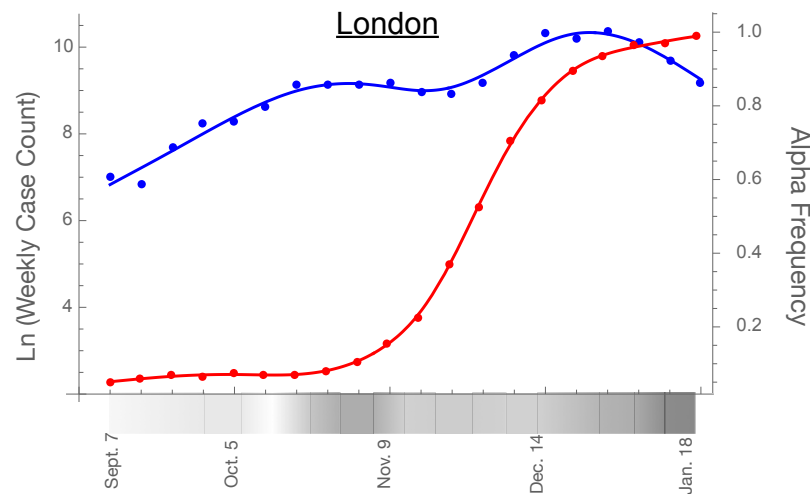


Day and Gandon, 2007. *Ecol. Lett.* 10: 876

Day et al. 2020. *Current Biology* 30:R849

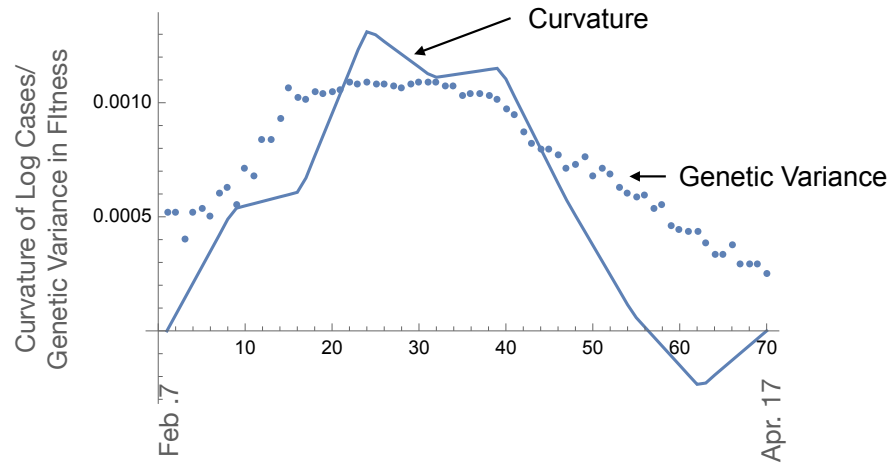
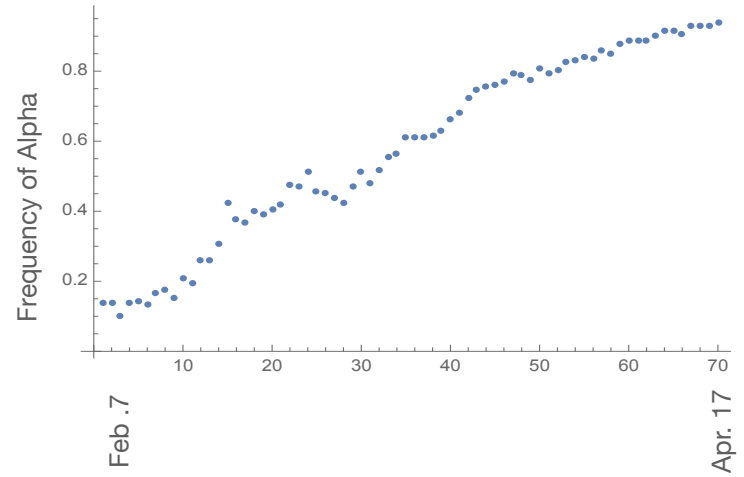
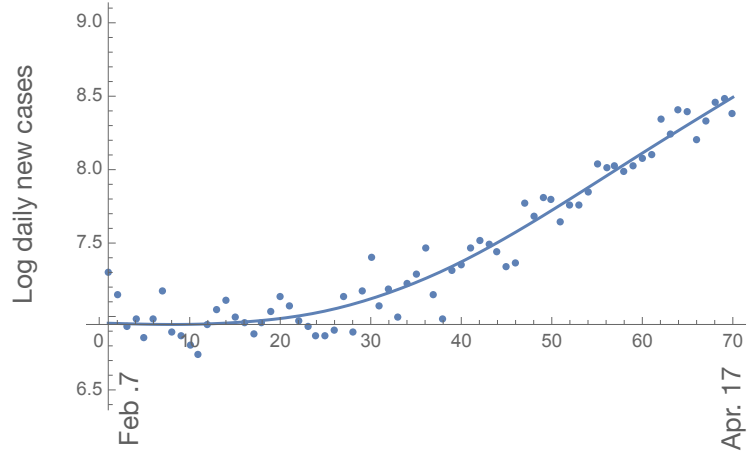
Otto et al. 2021. *Current Biology* 31:R918

# Fisher's Fundamental Theorem

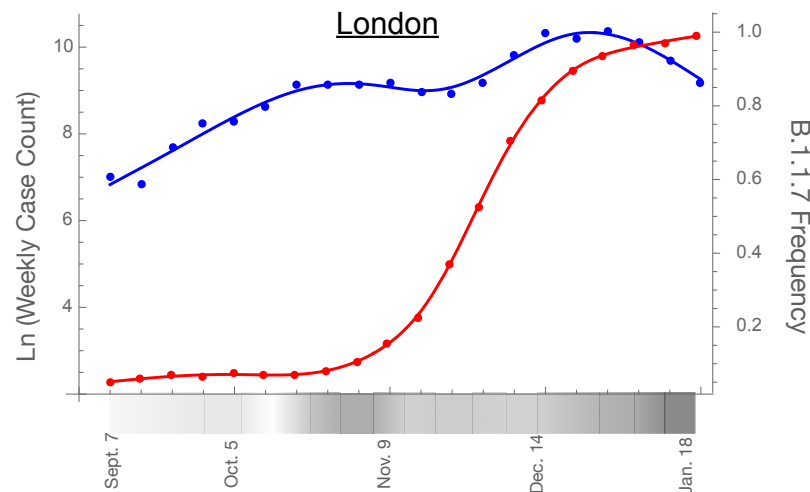


- (FFT) Rate of change of intrinsic growth rate  $r$  (curvature of blue plot) equals genetic variance in fitness
- In general,  $n$ th derivative equals  $n$ th cumulant of the distribution of fitness values

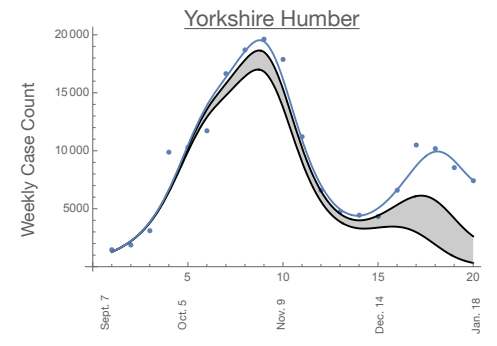
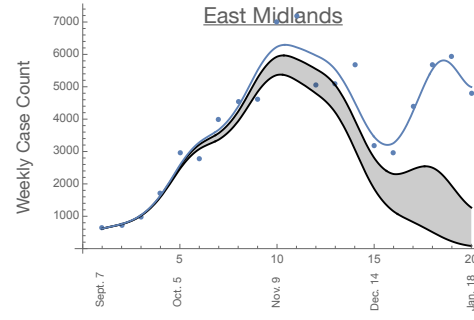
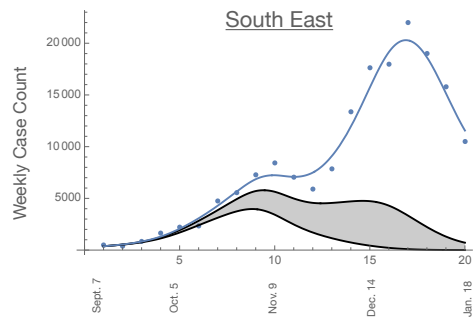
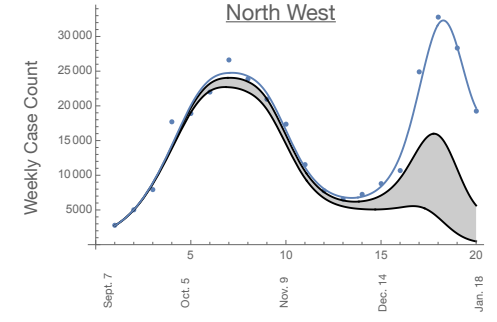
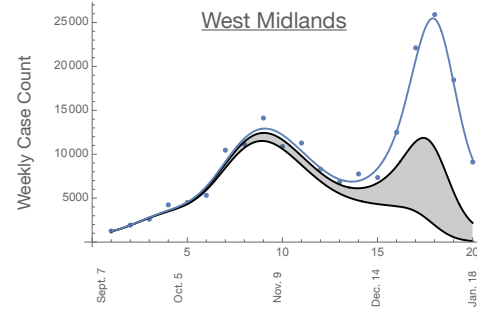
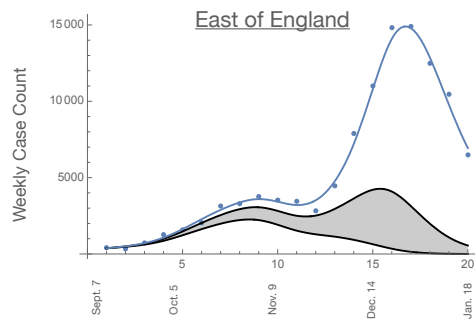
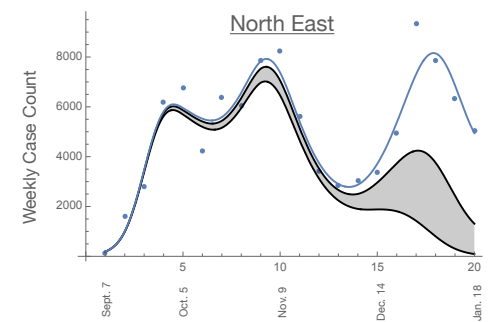
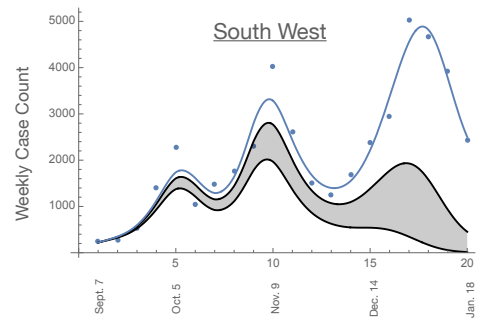
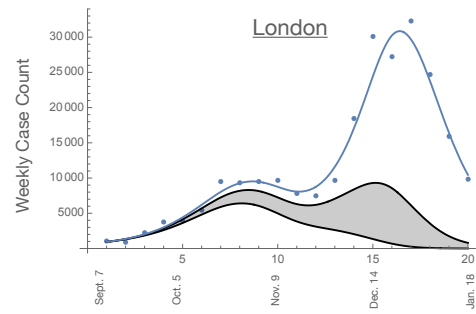
# Ontario Data, 2021

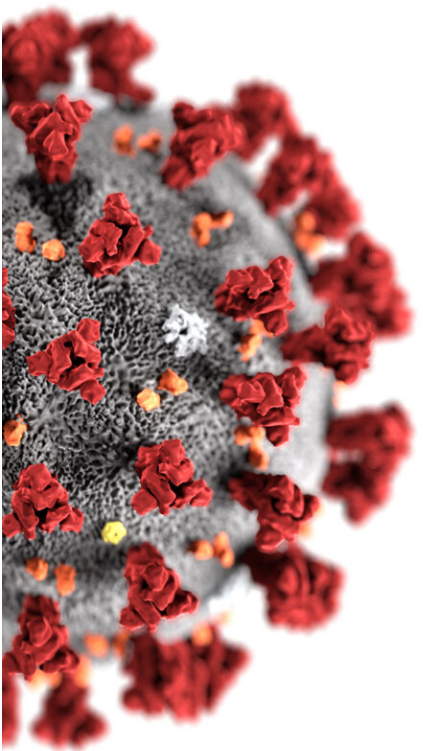


# Quantifying the Epidemiological Effect of Evolution



- What would have happened if there had been no evolution?
- Keep all interventions as they occurred but go back and “remove” evolution.
  - intrinsic growth rate is  $r_{WT}(t) + s(t) p(t)$ . Subtract  $s(t) p(t)$  from slope at each point in time and integrate this “corrected” growth rate forward

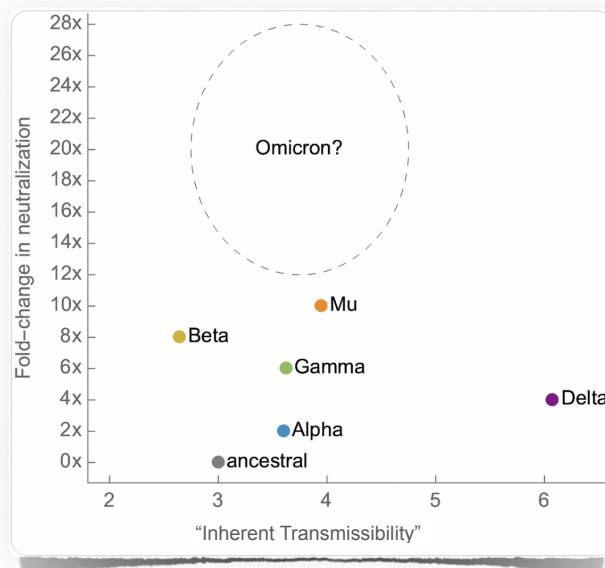
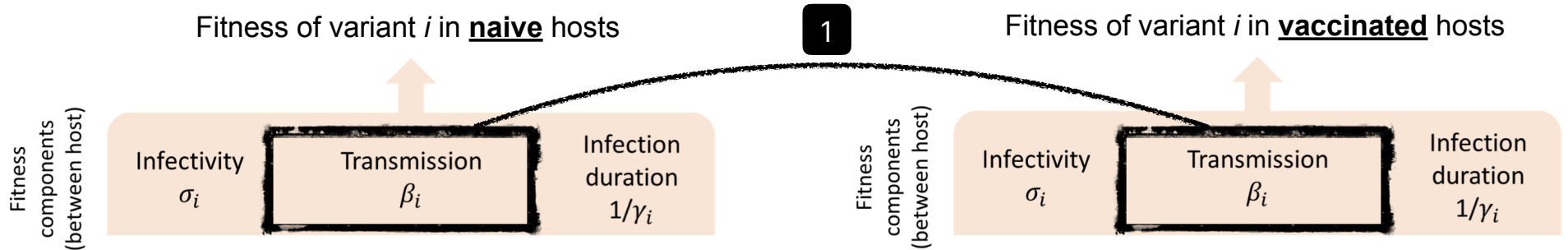




# Outline

- Pathogen adaptation during epidemics
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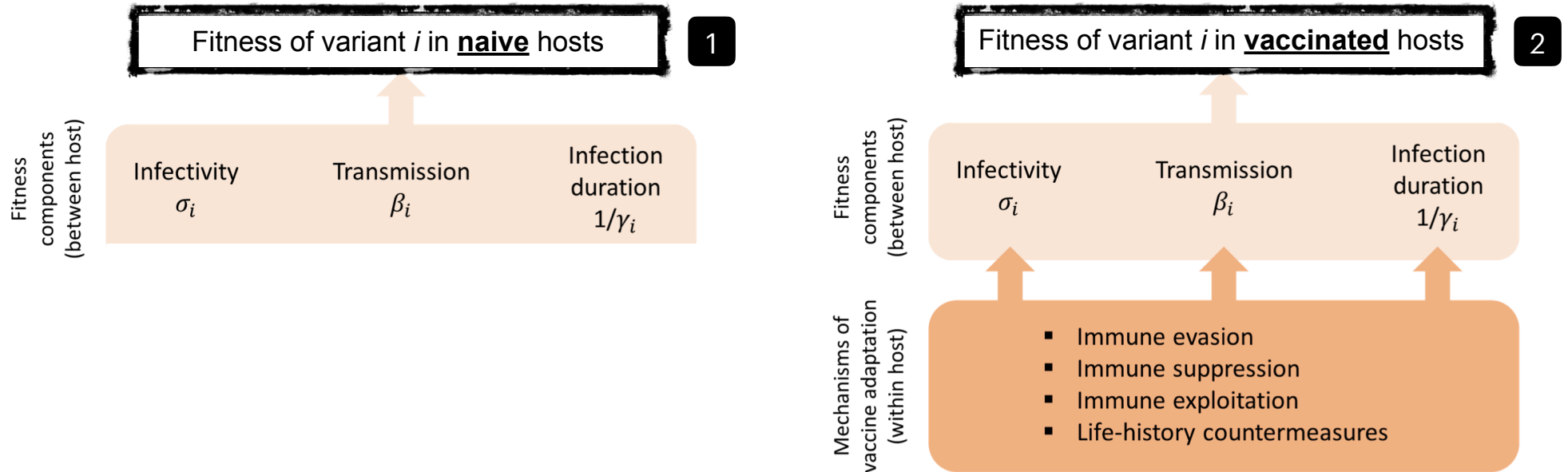
# Categorizing Vaccine-Adapted Variants



Day et al. 2022. Pathogen evolution under vaccination campaigns. PLoS Biology 20(9): e3001804

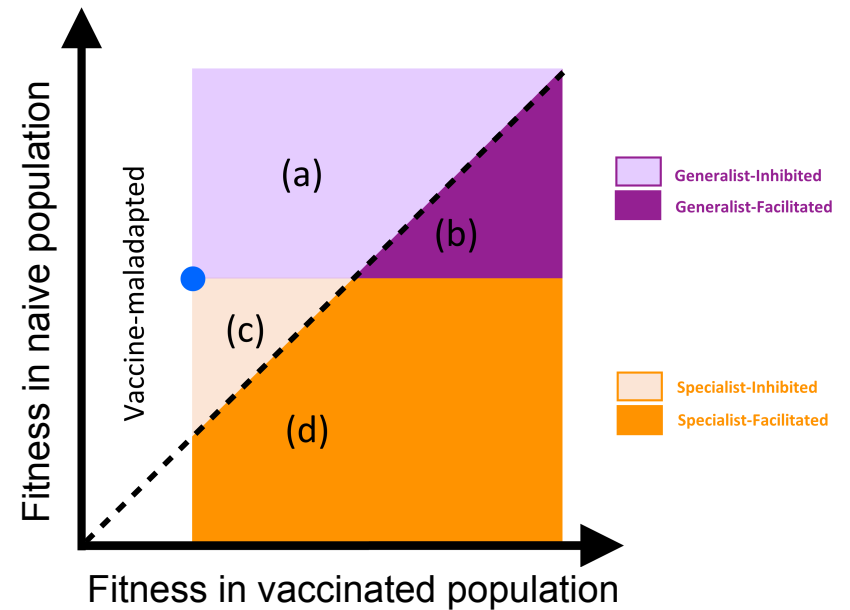
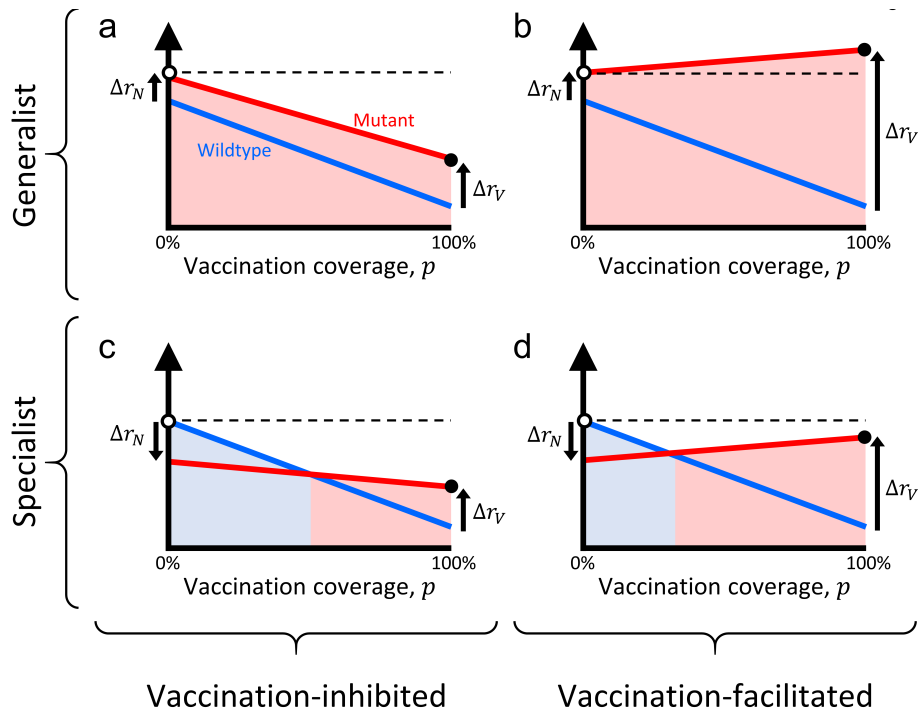


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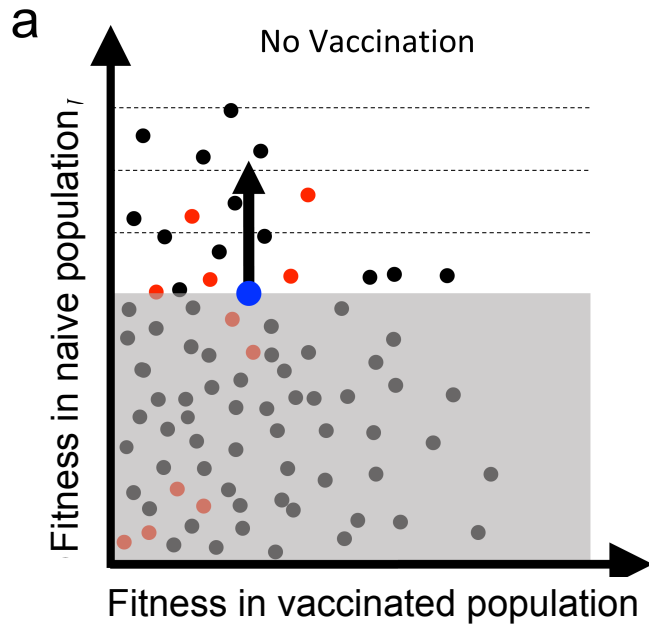
# Categorizing Vaccine-Adapted Variants

## Two axes of categorization



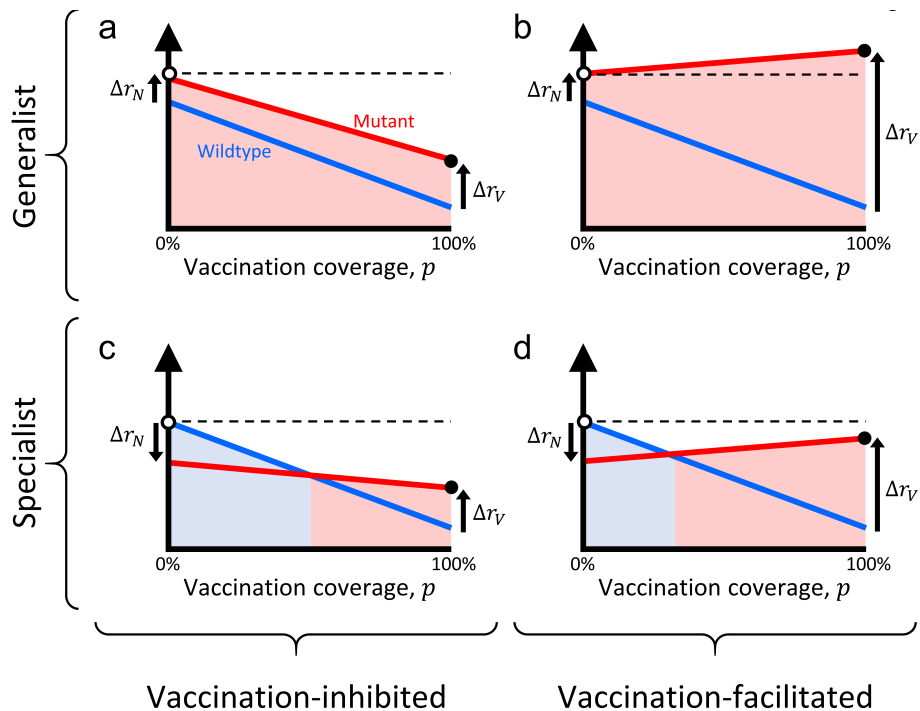
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# Pathogen Evolution under Vaccination



# Pathogen Evolution under Vaccination

## Two axes of categorization



- Successful variants tend to transition over time from generalist to specialists
- Predictions about inhibited/facilitated less clear

# Evidence From Other Pathogens

Vaccine-driven pathogen evolution is relatively rare. Where it has occurred we typically have:

- Vaccines that are “leaky”.
- Vaccines that target a small number of epitopes.

Both are true for SARS-CoV-2.

# Evidence From Other Pathogens

Tendency to go from generalist to specialist over time

- Malaria
- Hep B
- Bordetella pertussis
- Wildlife/agricultural
- Streptococcus pneumoniae
- Influenza (less clear)



Generalist-Inhibited



Specialist-Inhibited

Very few cases of vaccine-facilitation

- Marek's disease virus
- Myxoma virus?



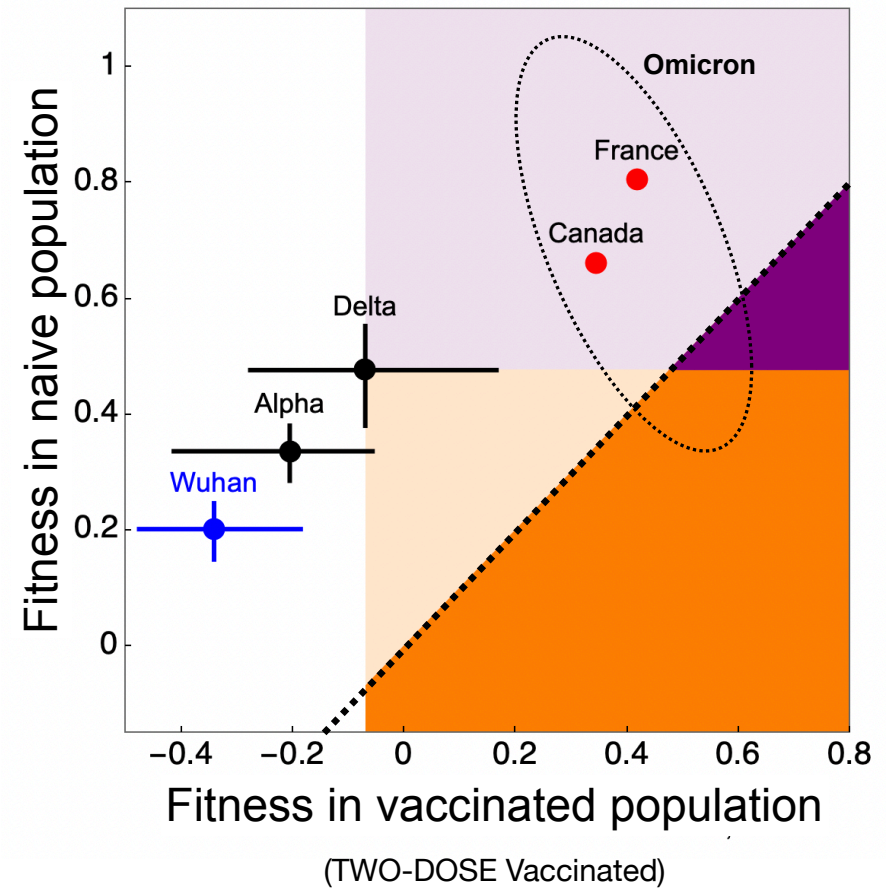
Generalist-Facilitated

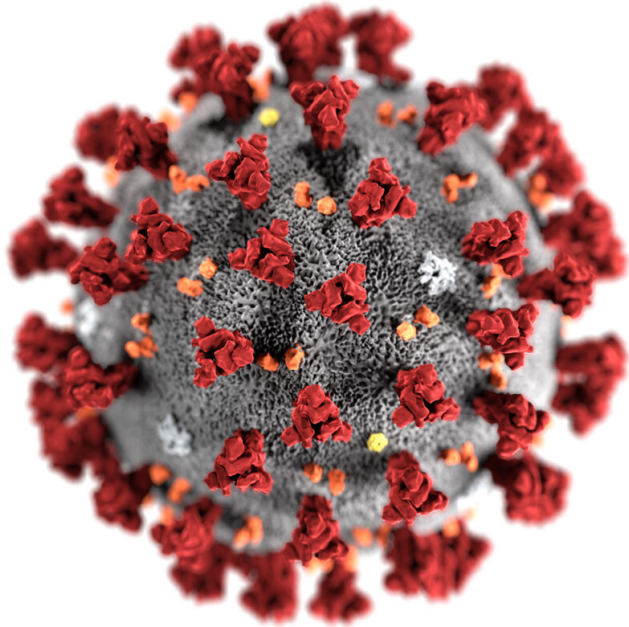


Specialist-Facilitated

# SARS-CoV-2

*(Can use SARS-CoV-2 surveillance data to categorize VOCs in real time)*





## Summary

- Pathogen adaptation during epidemics
- Patterns of SARS-CoV-2 evolution
- Vaccination and pathogen evolution

## Acknowledgements

Helen Alexander, Samuel Alizon, Andy Bell, **Sylvain Gandon**,  
**Dave Kennedy**, **Seb Lion**, Nicole Mideo, Bill Nelson, **Sally Otto**,  
Steve Proulx, **Andrew Read**, Sarah Reece, Paul Williams

