

# Probing the Cosmic Dawn using the redshifted 21-cm bispectrum

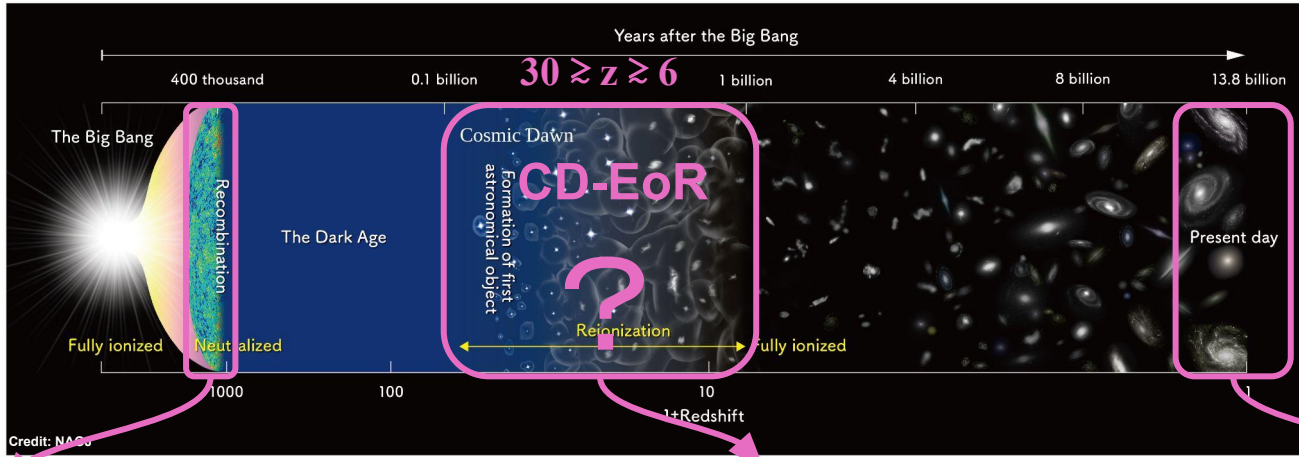
Mohd Kamran



UPPSALA  
UNIVERSITET

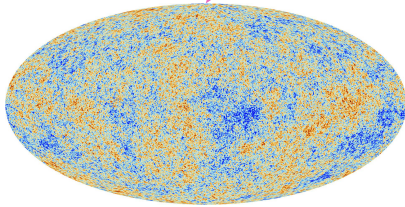
**Co-authors:** Suman Majumdar (**IIT Indore**), Raghunath Ghara (**Technion Israel**), Garrelt Mellema (**Stockholm University**), Somnath Bharadwaj (**IIT KGP**), Jonathan R. Pritchard (**Imperial College London**), Rajesh Mondal (**Tel Aviv University**), Ilian T. Iliev (**University of Sussex**)

# Cosmic History: Cosmic Dawn and Epoch of Reionization (CD-EoR)

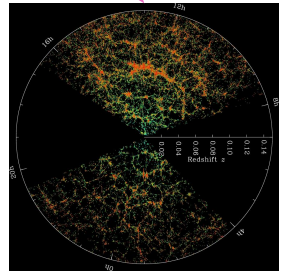


**INTERMEDIATE PHASES**  
**Cosmic Dawn:** First stars and X-ray sources; Neutral Universe.  
**Epoch of Reionization:** Earliest galaxies; Neutral hydrogen starts to disappear.

**During first Byr**

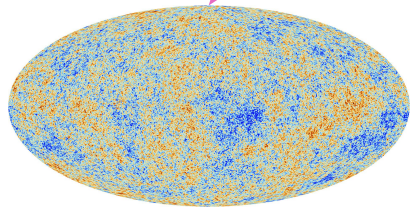
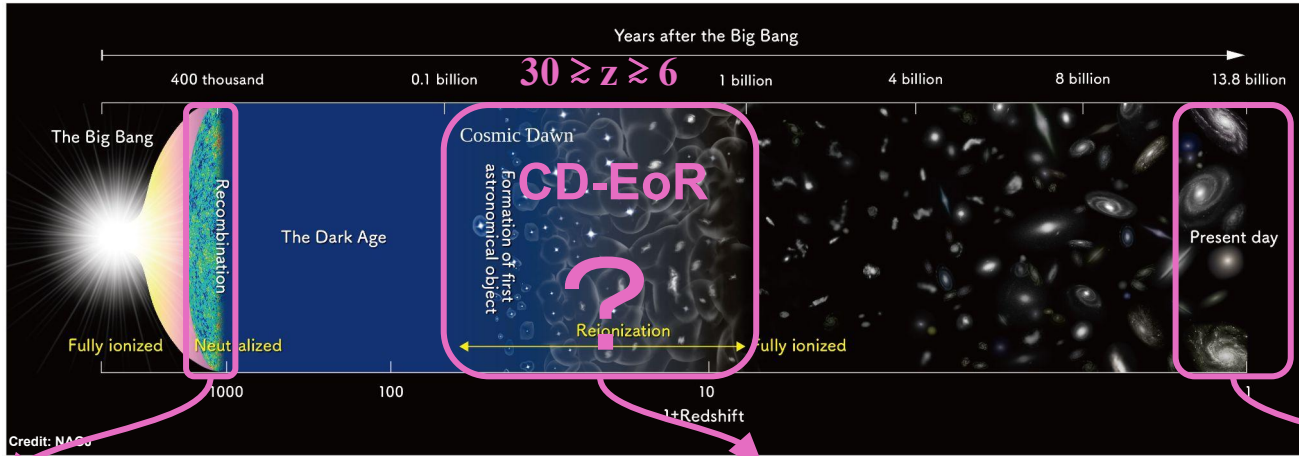


Cosmic Microwave Background (Planck)



Galaxy Redshift Survey (SDSS)

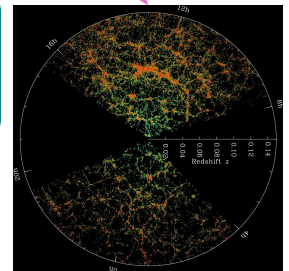
# Cosmic History: Cosmic Dawn and Epoch of Reionization (CD-EoR)



Cosmic Microwave Background (Planck)

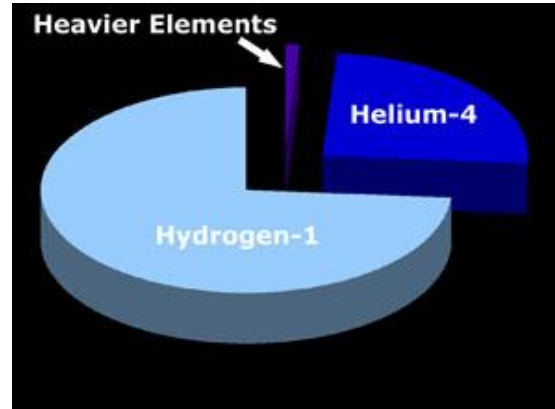
**INTERMEDIATE PHASES**  
**Cosmic Dawn:** First stars and X-ray sources; Neutral Universe.  
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**Least Known Chapters**  
**Largely untested by the observations**



Galaxy Redshift Survey (SDSS)

## Neutral Hydrogen (HI) is abundant in the IGM:

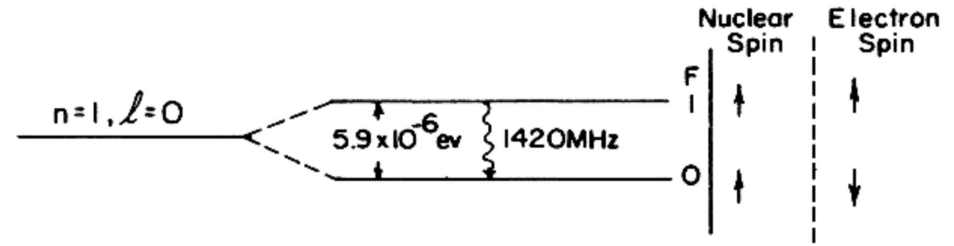
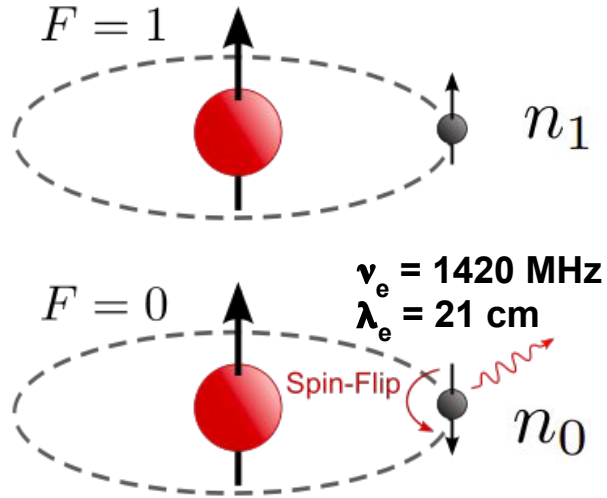


**Elemental composition of baryons in the Universe**

Source: [universeadventure.org](http://universeadventure.org)

# How can we see the hydrogen?

## HI 21-cm line



Source: Wikimedia.org



# Differential brightness temperature

$$\delta T_b(\mathbf{r}, z) = 27 x_{\text{HI}}(\mathbf{r}, z) \left(1 - \frac{T_{\text{CMB}}(z)}{T_S(\mathbf{r}, z)}\right) (1 + \delta_b(\mathbf{r}, z)) \left(\frac{\Omega_b h^2}{0.023}\right) \left(\frac{0.15}{\Omega_m h^2} \frac{1+z}{10}\right)^{1/2} \text{mK}$$

21-cm fluctuations!

Astrophysics

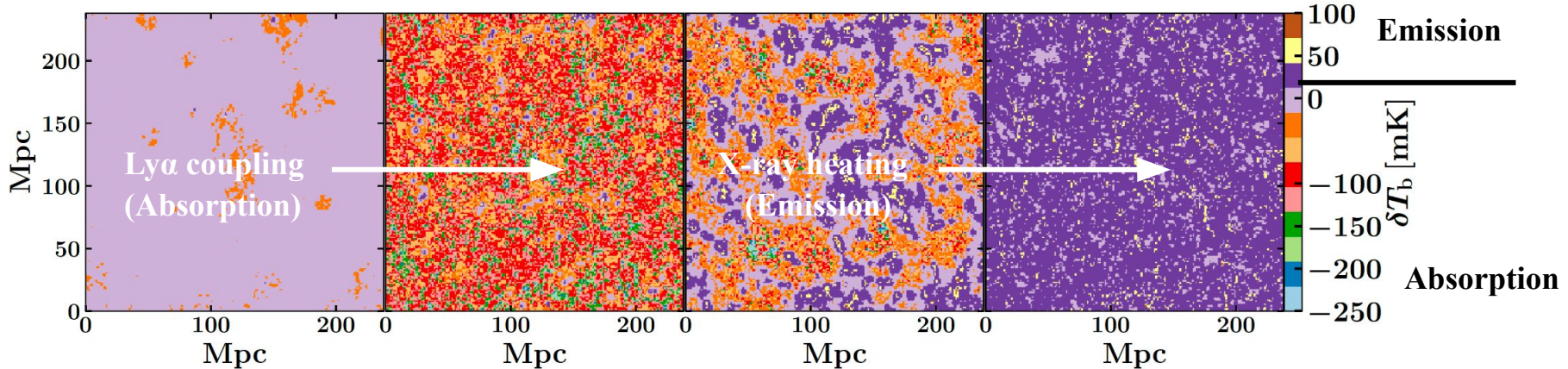
Early CD stage

$z = 15.60$

← Redshift ( $z$ )

Late CD stage

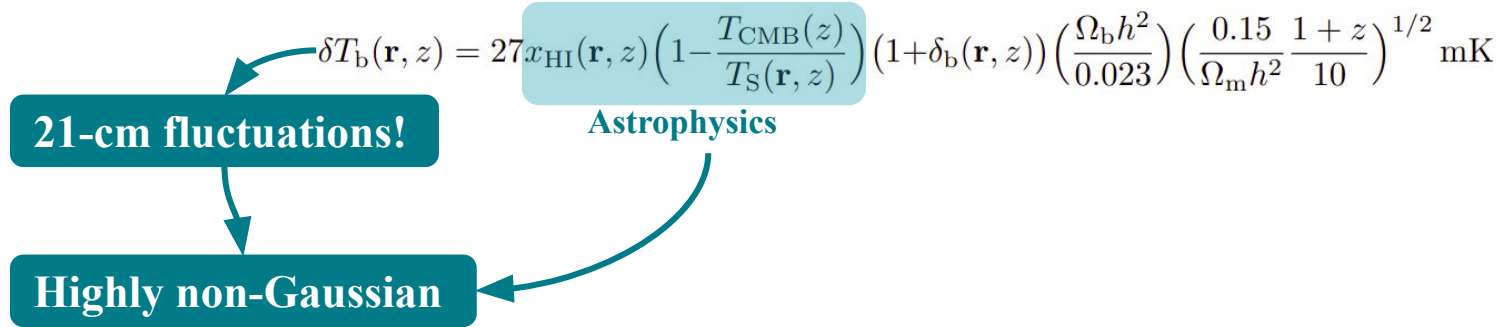
$z = 9.03$



Absorption:  $\delta T_b < 0$

Emission:  $\delta T_b > 0$

## The non-Gaussianity:



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**21-cm fluctuations!**

Astrophysics

**Highly non-Gaussian**

**Non-Gaussianity:**

- Intrinsic
- Time-evolving



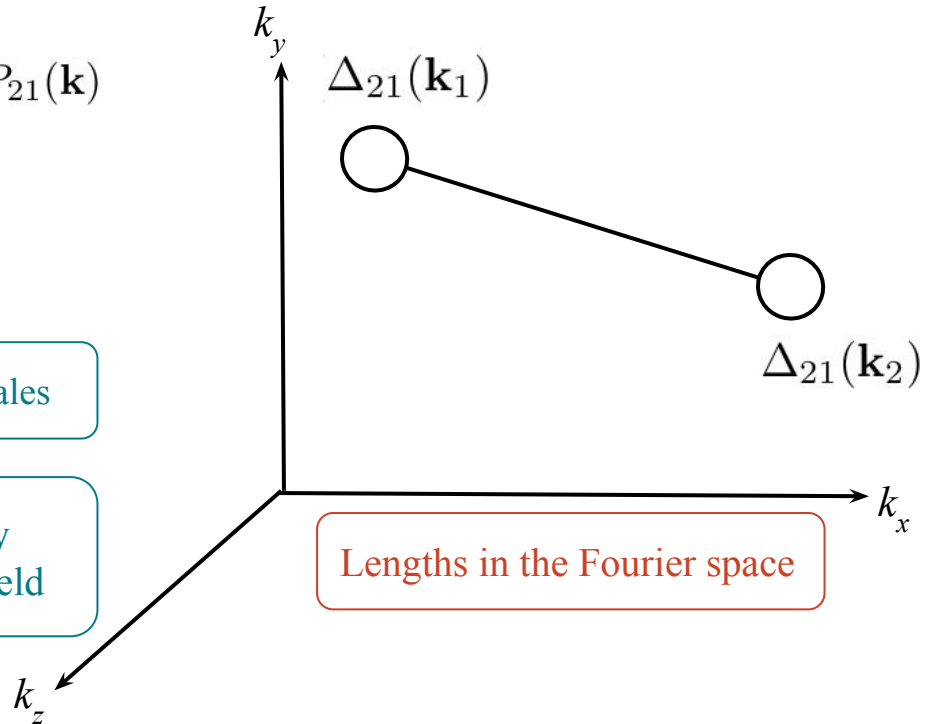
# The Power Spectrum: A conventional statistical measure of the 21-cm signal

$$\langle \Delta_{21}(\mathbf{k}_1) \Delta_{21}(\mathbf{k}_2) \rangle = (2\pi)^3 \delta_{\text{D}}^3(\mathbf{k}_1 - \mathbf{k}_2) P_{21}(\mathbf{k})$$

$$\Delta_{21}(\mathbf{k}) \xleftrightarrow{\text{FT}} \delta T_{\text{b}}(\mathbf{r})$$

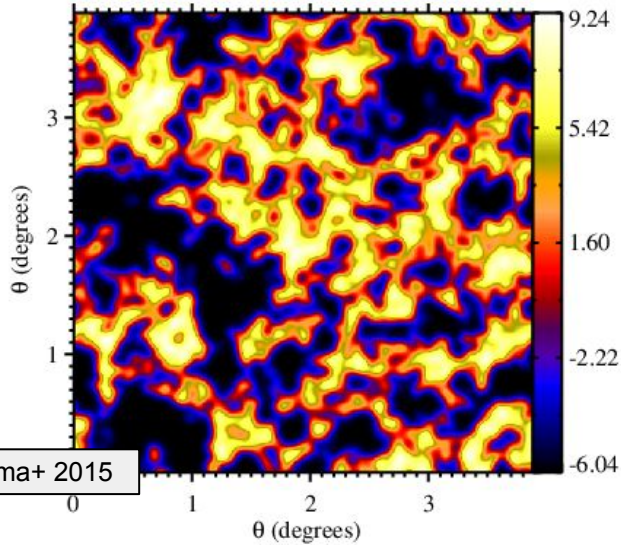
Amplitude of fluctuations at different length scales

Power spectrum describes a field completely only when it is a **pure Gaussian random field**

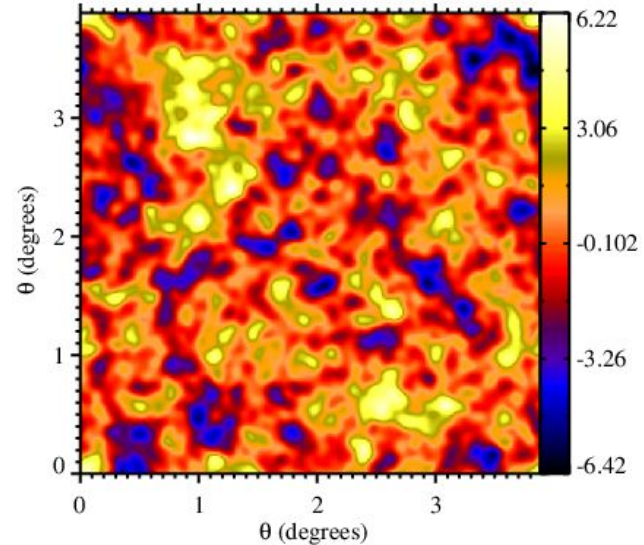


# The non-Gaussianity:

Non-Gaussian 21-cm map



Gaussian fluctuations

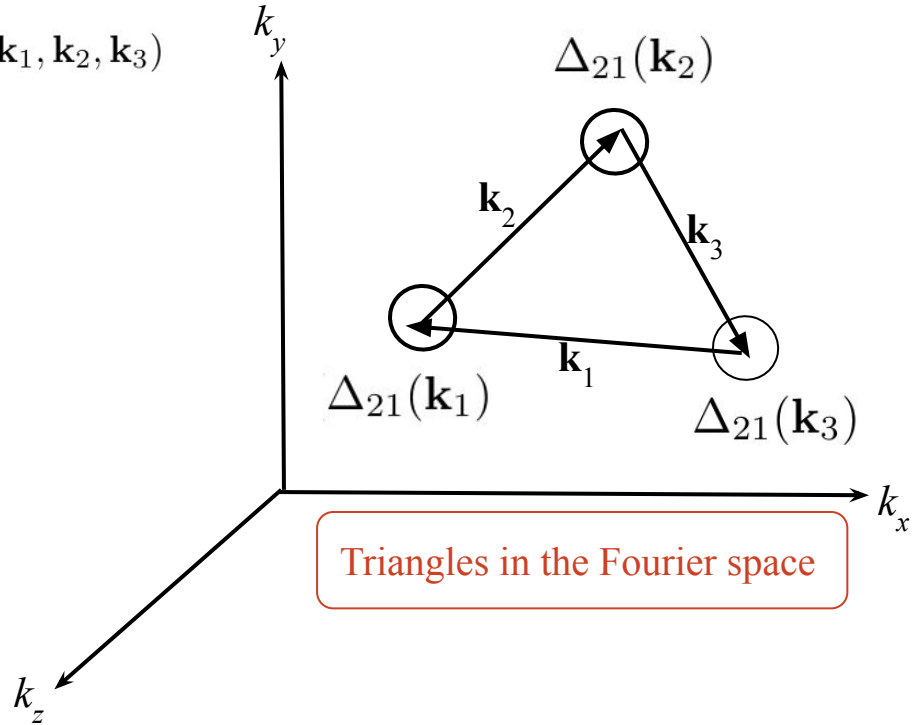


Same power spectrum but different images

# The Bispectrum:

$$\langle \Delta_{21}(\mathbf{k}_1) \Delta_{21}(\mathbf{k}_2) \Delta_{21}(\mathbf{k}_3) \rangle = V \delta_{\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3, 0}^K B_{21}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)$$

$$\Delta_{21}(\mathbf{k}) \quad \overset{\text{FT}}{\longleftrightarrow} \quad \delta T_b(\mathbf{r})$$



# The Bispectrum:

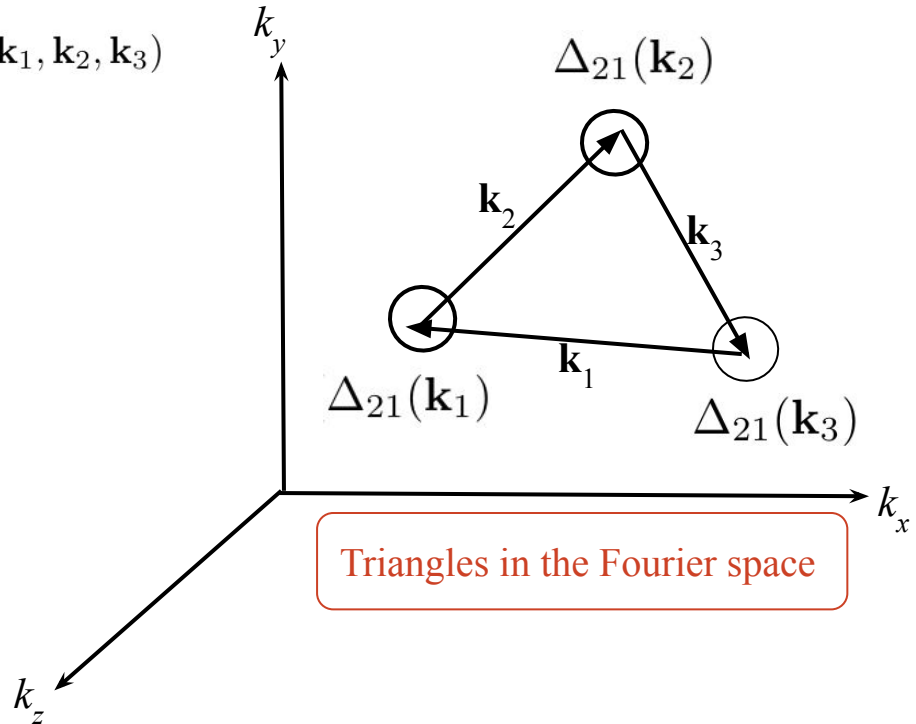
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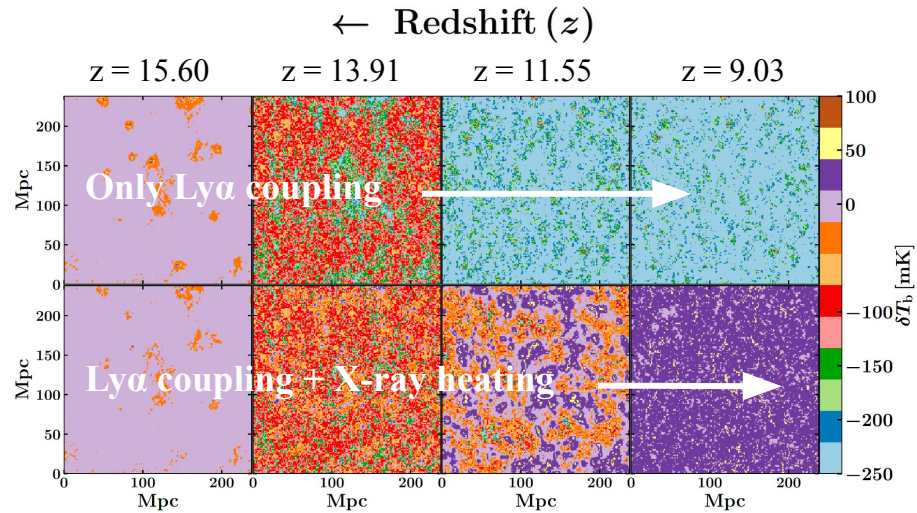
- $B_{21} \neq 0$ , iff 3  $\mathbf{k}$  modes in the definition form a closed triangle.

$$\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3 = 0$$

- $B_{21}$  can attain both positive and negative values



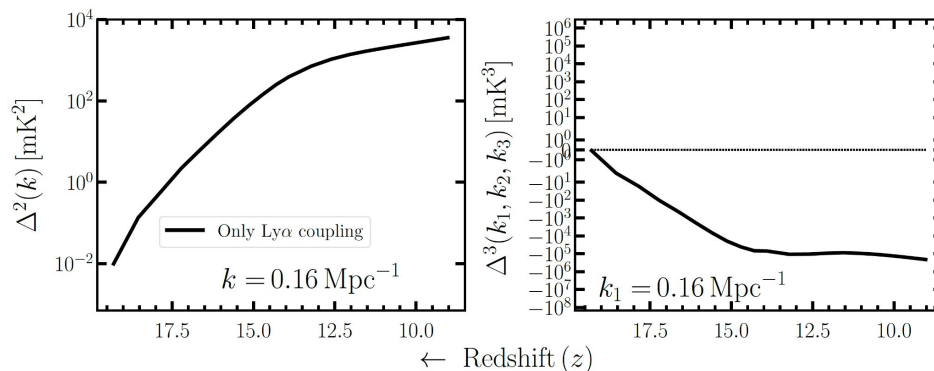
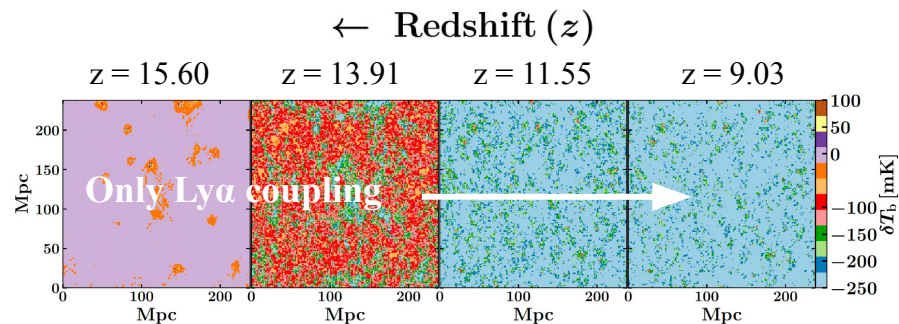
## Two simulated CD scenarios:



Results from GRIZZLY simulation (Ghara et al. 2015a, 2018)

# Results

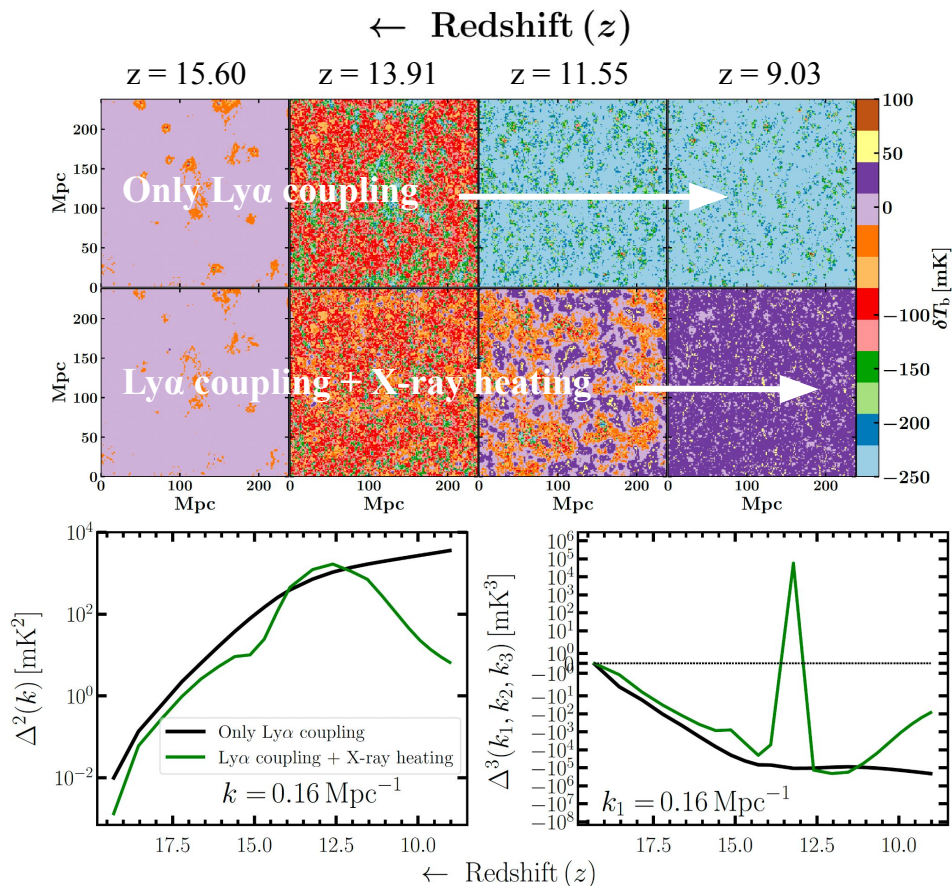
# The Bispectrum as a probe of IGM physics:



Kamran+2021b (under review in PRL)

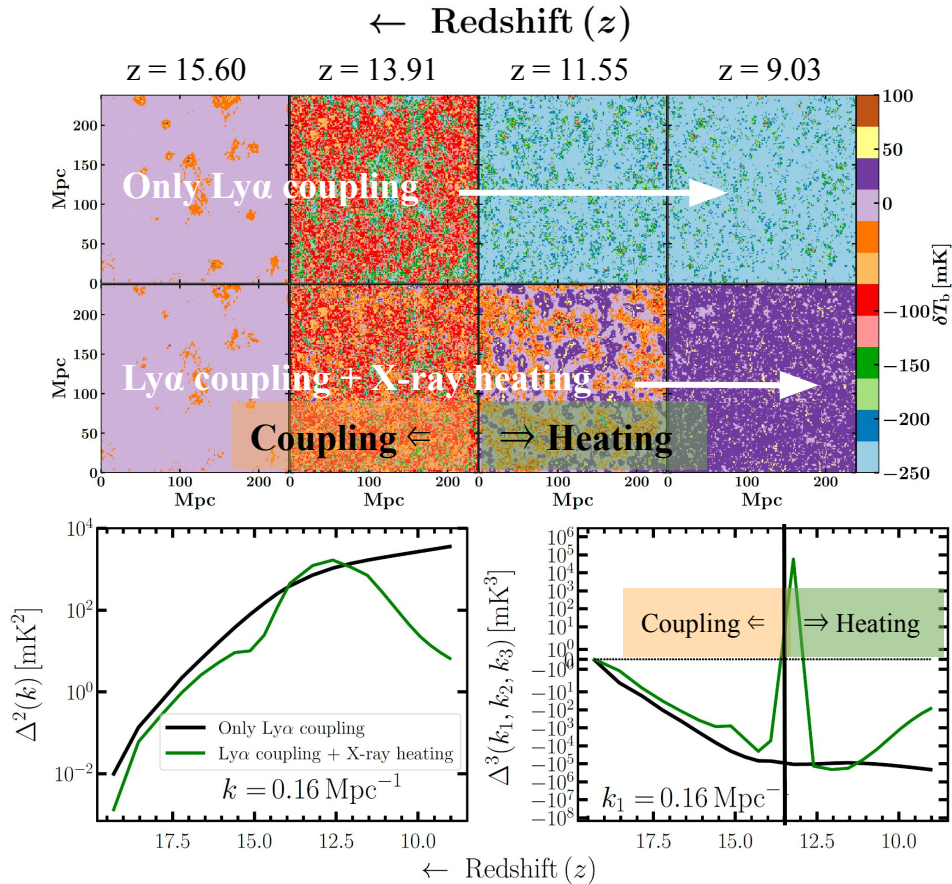


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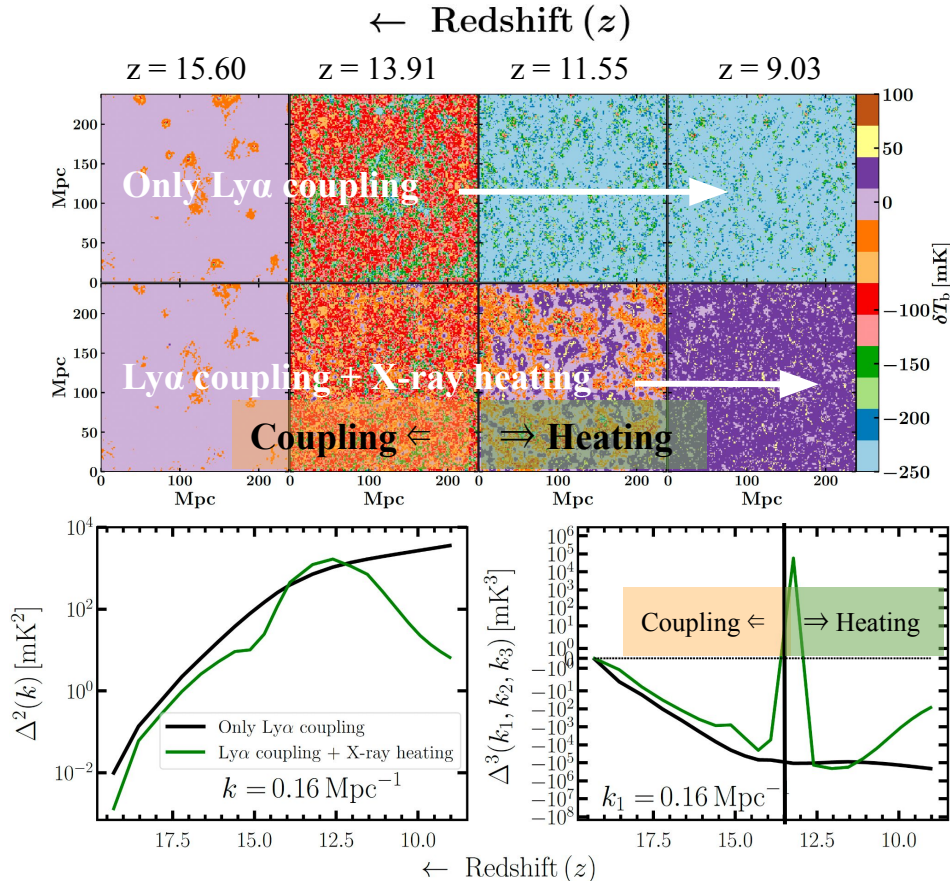
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# The Bispectrum as a probe of IGM physics:



These features can be used as a test of confirmative detection of the 21-cm fluctuations in the future SKA observations

Kamran+2021b (under review in PRL)

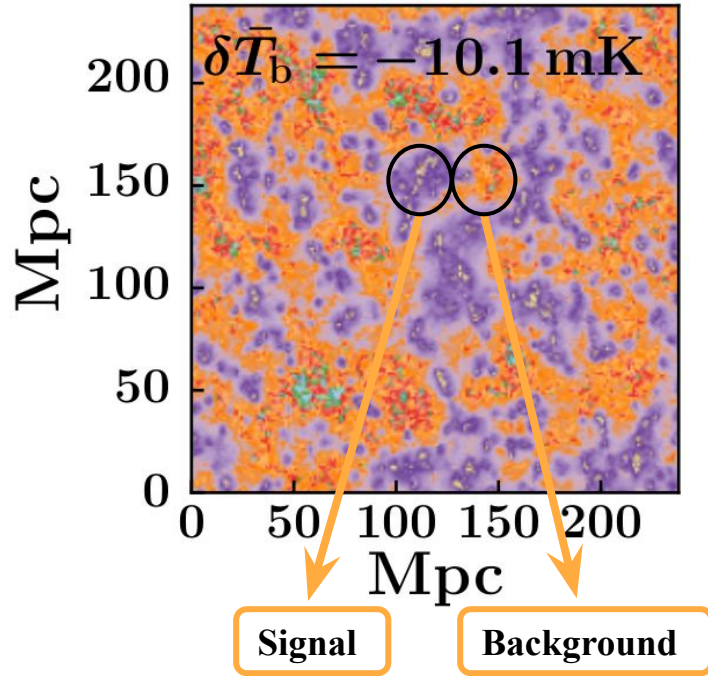
# Detectability predictions of the bispectrum using the SKA-Low:

**Mondal+Mellema+Kamran et al. 2021**

More than a  $5\sigma$  detection is possible using 1000 hrs of SKA observations of the bispectra for a few special k-triangles

# Summary

- CD-EoR 21-cm signal is highly non-Gaussian in nature.
- The bispectrum statistic can potentially capture this time evolving non-Gaussianity.
- The bispectrum being the potential probe of the non-Gaussianity – > can probe the IGM physics that sources the non-Gaussianity in the signal.



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**The sign of the bispectrum can tell us the relative contrast of the fluctuations in the 21-cm signal with respect to its background.**







