



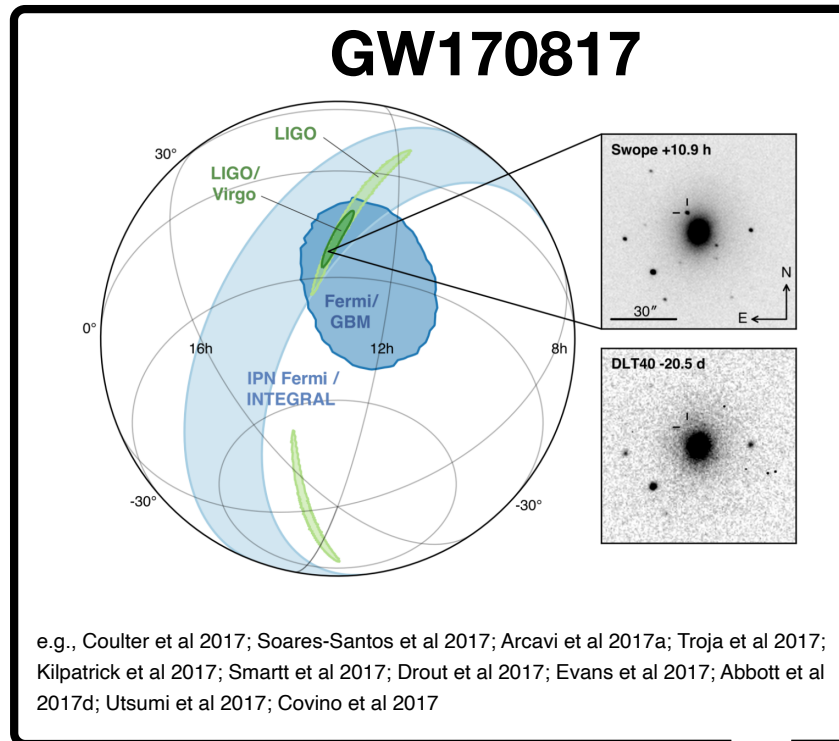
The radiative transfer and atomic physics of kilonovae  
6<sup>th</sup> September, 2023

# Atomic calculations and radiative transfer simulations for modelling kilonova

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In collaboration with  
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Jon Grumer (Uppsala U.)

# Kilonova observations



Li & Paczynski 1998

**GRB130603B**

e.g., Tanvir et al. 2013, Berger et al. 2013

**GRB211211A**

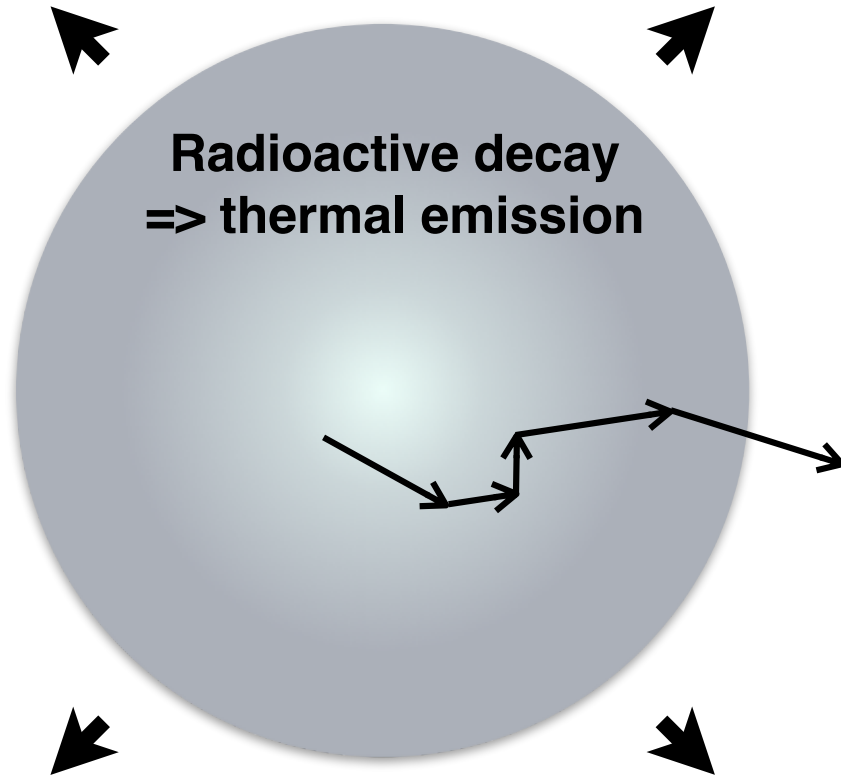
e.g., Rastinejad et al. 2022

**GRB230307A**

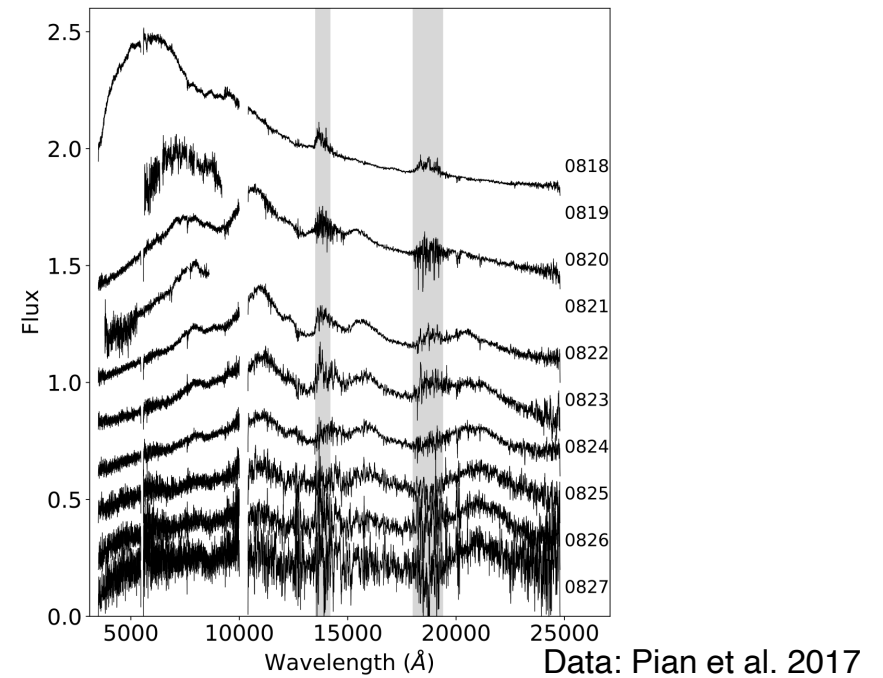
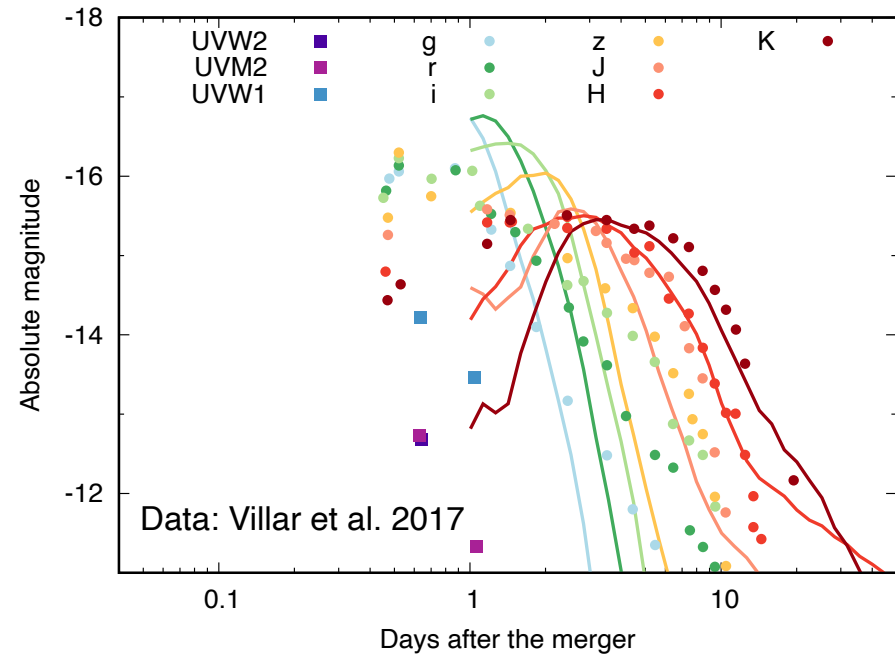
e.g., Levan et al. 2023, Gillanders et al. 2023



# Kilonova

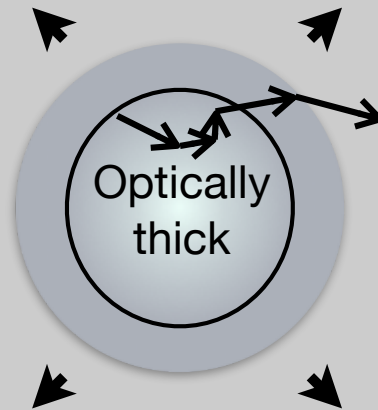


**Determined by microphysics:  
requires atomic cross-sections**



# What is needed?

## Photospheric phase



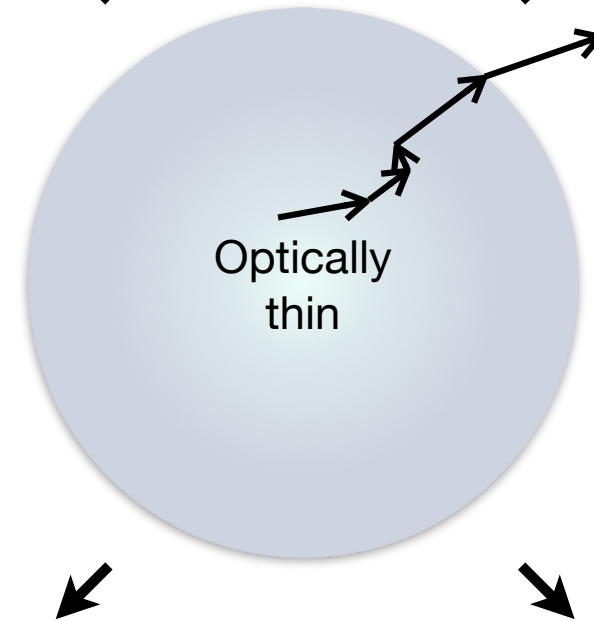
Early time (LTE):

### Required atomic data:

- Energy levels
- E1 transitions

$t \sim$  a few days

## Nebular phase



Late time (Non-LTE):

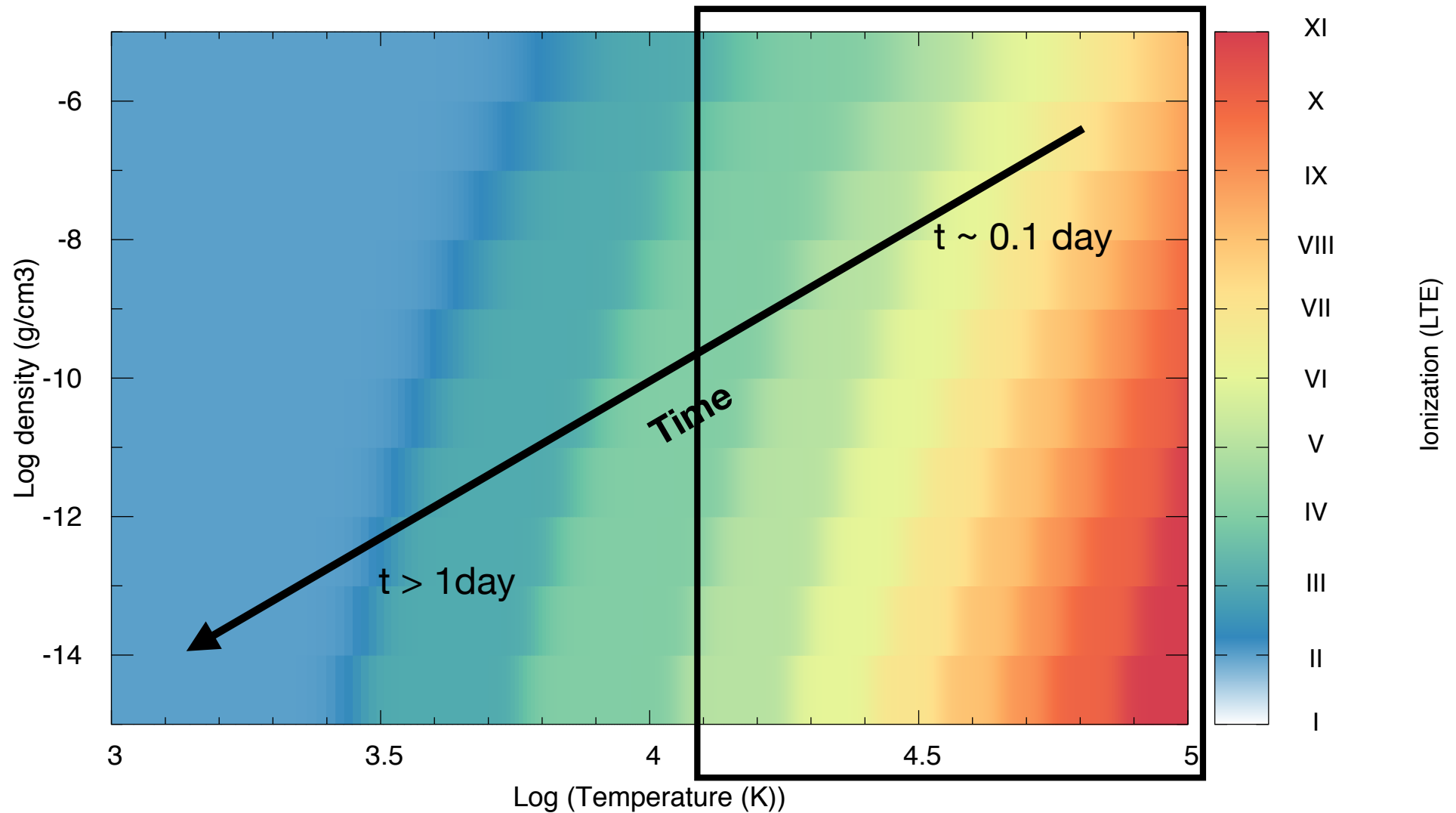
### Required atomic data:

- E1+ M1 transitions
- Collisional cross-sections
- Recombination coefficients
- Photo-ionization cross-sections...

$t \geq$  week

Time

# Physical conditions



## Ionized to I-IV:

Kasen et al. 2013; Tanaka & Hotokezaka 2013; Fontes et al. 2017, 2020, 2022; Wollaeger et al. 2017; Gaigalas et al. 2019; Tanaka et al. 2018, 2020; Rynkun et al. 2022a,b; Flors et al. 2023

See talks by M. Tanaka, D. Kasen, C. Fontes, R. Silva, A. Flors

# Atomic calculation

- **Code: HULLAC (Hebrew University Lawrence Livermore Atomic Code)**

Bar-Shalom et al. 2001

We design a method to determine ground configuration of lanthanides

Obtain atomic orbitals for multiple central potential  
=> systematically vary  $4f^{N_1} 5p^{N_2}, N_1 + N_2 = \text{constant}$

Banerjee et al. 2022, ApJ  
Banerjee et al. 2023, submitted

## Example : Gd V

Gd IV has ground configuration  $4f^7 5p^6$  (NIST ASD)

## Gd V test configurations : $4f^6 5p^6$ and $4f^7 5p^5$

(Energy level calculated for both configurations in all cases)

Cases	Potential felt by last electron	Minimization	Ground configuration
A	$4f^6 5p^5$	$4f^6 5p^6$	$4f^6 5p^6$
B	$4f^5 5p^6$	-- --'' --	$4f^6 5p^6$
C	$4f^7 5p^4$	$4f^7 5p^5$	$4f^6 5p^6$
D	$4f^6 5p^5$	-- --'' --	$4f^6 5p^6$

## Our finding:

=> Ground energy level always coming from one set of  $N_1, N_2$

# Ground states of Lanthanides

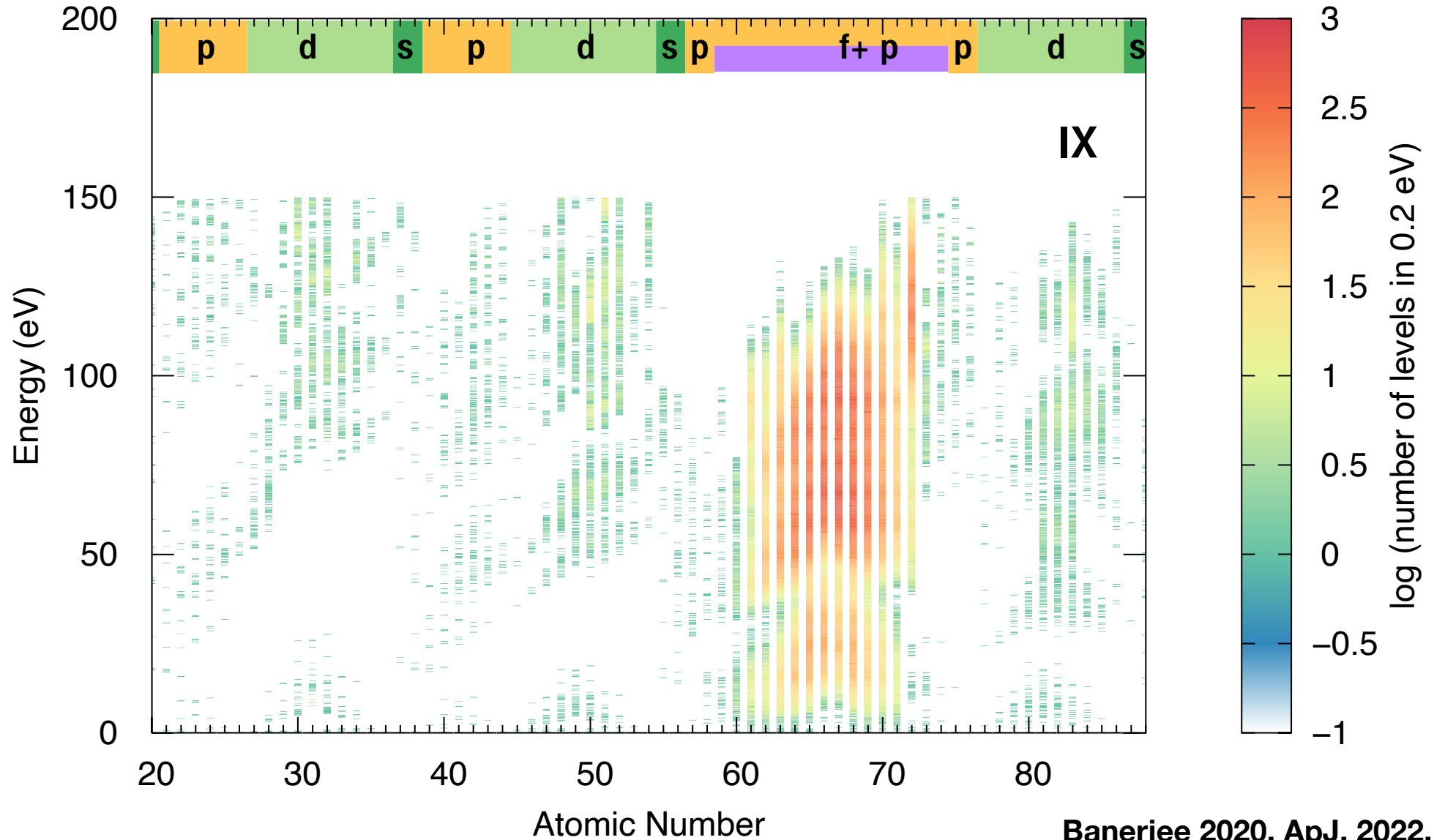
**Our work => Systematic theoretical calculation  
for the highly ionized lanthanides**

Ion	La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
V	$5p^5$	$5p^6$	$4f^1 5p^6$	$4f^2 5p^6$	$4f^3 5p^6$	$4f^4 5p^6$	$4f^5 5p^6$	$4f^6 5p^6$	$4f^7 5p^6$	$4f^8 5p^6$	$4f^9 5p^6$	$4f^{10} 5p^6$	$4f^{11} 5p^6$	$4f^{12} 5p^6$	$4f^{13} 5p^6$
VI	$5p^4$	$5p^5$	$5p^6$	$4f^1 5p^6$	$4f^2 5p^6$	$4f^3 5p^6$	$4f^4 5p^6$	$4f^5 5p^6$	$4f^6 5p^6$	$4f^7 5p^6$	$4f^8 5p^6$	$4f^9 5p^6$	$4f^{10} 5p^6$	$4f^{11} 5p^6$	$4f^{12} 5p^6$
VII	$5p^3$	$5p^4$	$5p^5$	$5p^6$	$4f^2 5p^{5*}$	$4f^3 5p^{5*}$	$4f^4 5p^{5*}$	$4f^5 5p^{5*}$	$4f^6 5p^{5*}$	$4f^7 5p^{5*}$	$4f^7 5p^6$	$4f^8 5p^6$	$4f^9 5p^6$	$4f^{10} 5p^6$	$4f^{11} 5p^6$
VIII	$5p^2$	$5p^3$	$5p^4$	$4f^1 5p^{4*}$	$4f^2 5p^{4*}$	$4f^3 5p^4$	$4f^4 5p^4$	$4f^5 5p^4$	$4f^6 5p^4$	$4f^7 5p^4$	$4f^7 5p^5$	$4f^7 5p^6$ $4f^8 5p^5$	$4f^9 5p^{5*}$	$4f^{10} 5p^{5*}$	$4f^{10} 5p^6$ $4f^{11} 5p^5$
IX	$5p^1$	$5p^2$	$5p^3$	$4f^1 5p^3$	$4f^2 5p^3$	$4f^3 5p^3$	$4f^4 5p^3$	$4f^5 5p^3$	$4f^6 5p^3$	$4f^7 5p^3$	$4f^7 5p^4$	$4f^8 5p^{4*}$	$4f^9 5p^4$	$4f^{10} 5p^4$	$4f^{11} 5p^{4*}$
X	$5s^2$	$5p^1$	$5p^2$	$4f^1 5p^2$	$4f^2 5p^2$	$4f^3 5p^2$	$4f^4 5p^2$	$4f^5 5p^2$	$4f^6 5p^2$	$4f^7 5p^2$	$4f^7 5p^{3*}$	$4f^8 5p^3$	$4f^9 5p^3$	$4f^{10} 5p^3$	$4f^{11} 5p^3$
XI	$5s^1$	$5s^2$	$5p^1$	$4f^1 5p^1$	$4f^2 5p^1$	$4f^3 5p^1$	$4f^4 5p^1$	$4f^5 5p^1$	$4f^6 5p^1$	$4f^7 5p^1$	$4f^7 5p^2$	$4f^8 5p^2$	$4f^9 5p^2$	$4f^{10} 5p^2$	$4f^{11} 5p^2$

# Energy level

- **Atomic calculations: HULLAC (Hebrew University Lawrence Livermore Atomic Code)**

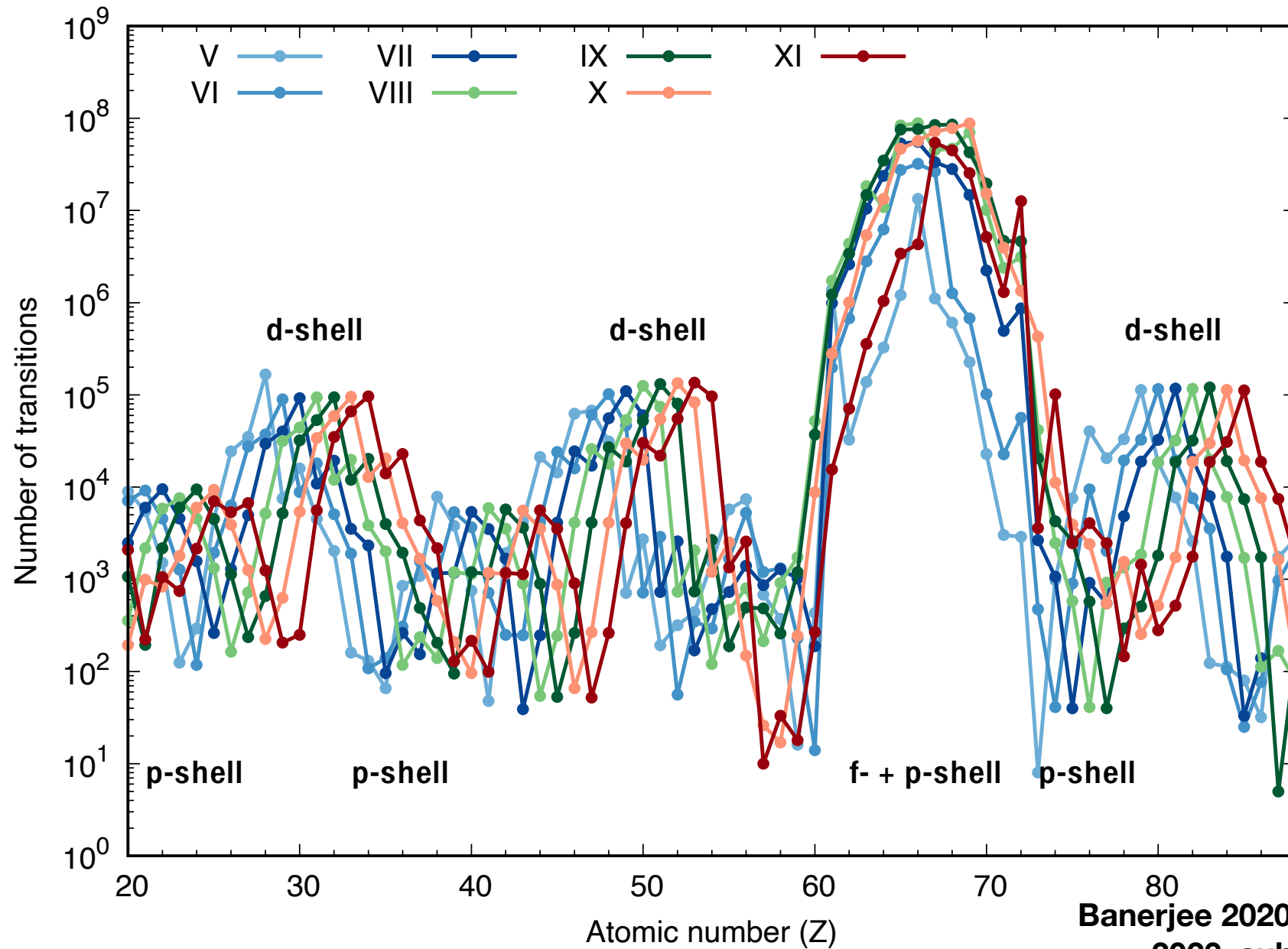
Bar-Shalom et al. 2001



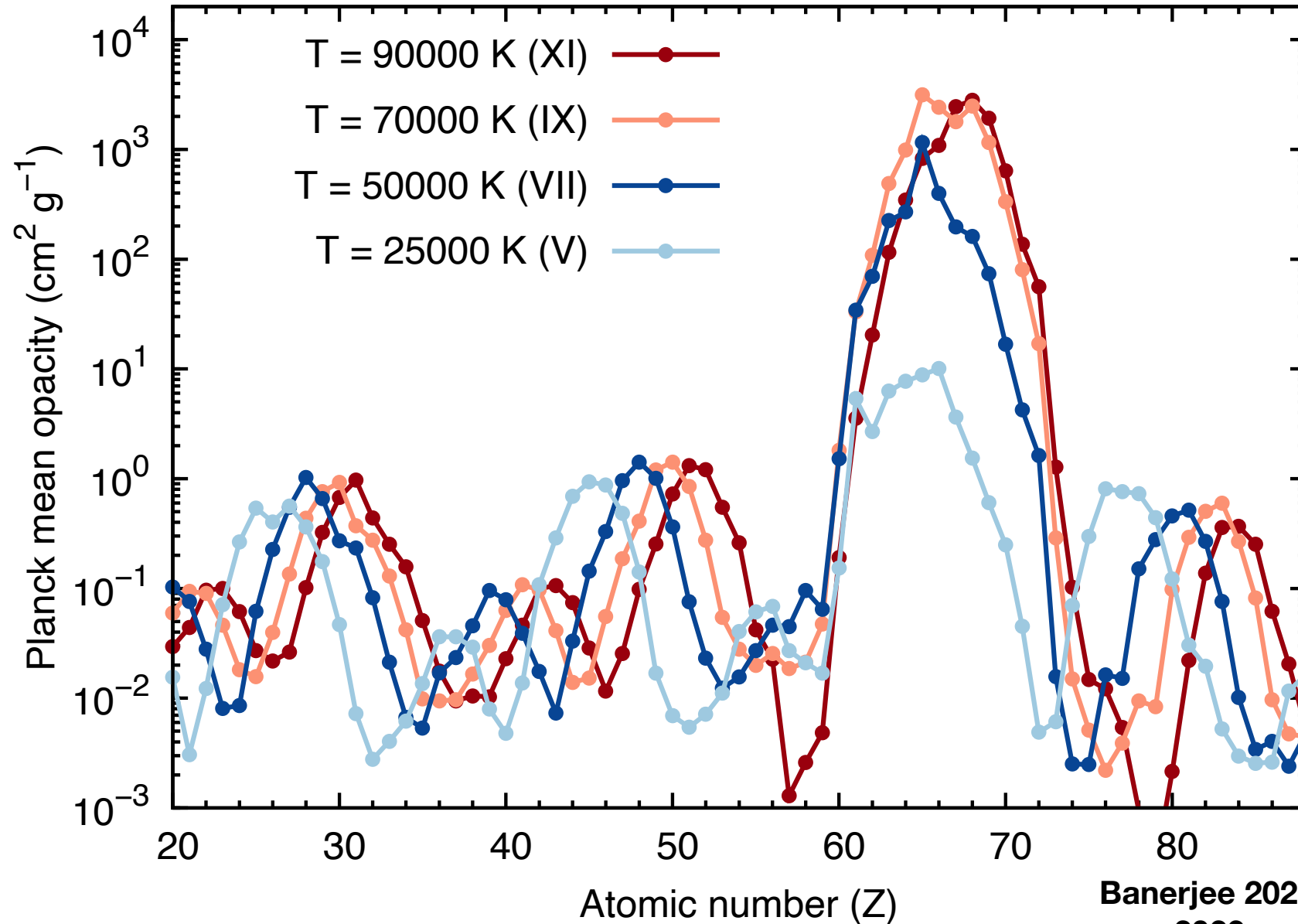
Banerjee 2020, ApJ, 2022,  
2023, submitted



# Transitions

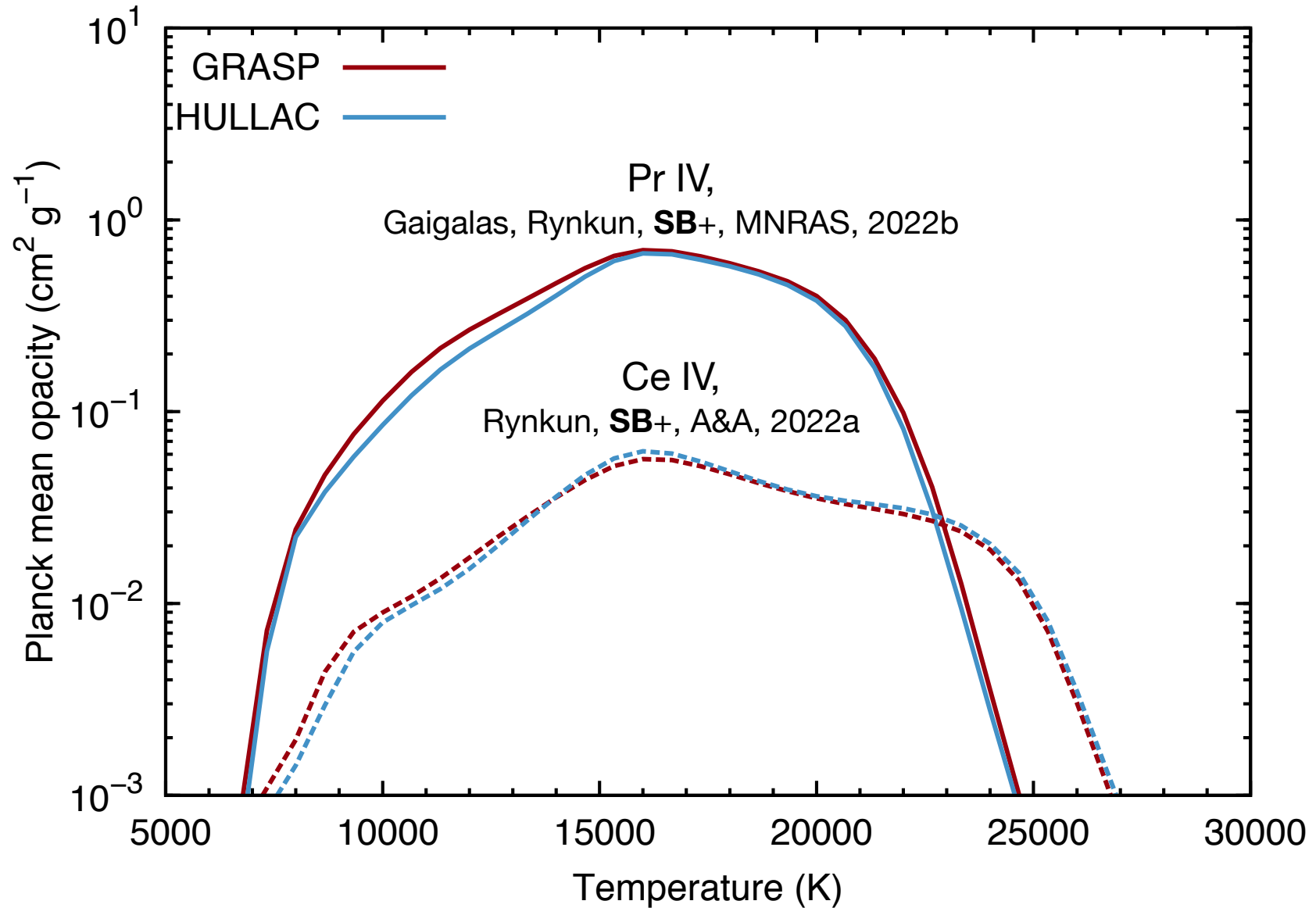


# Opacity



# Uncertainties

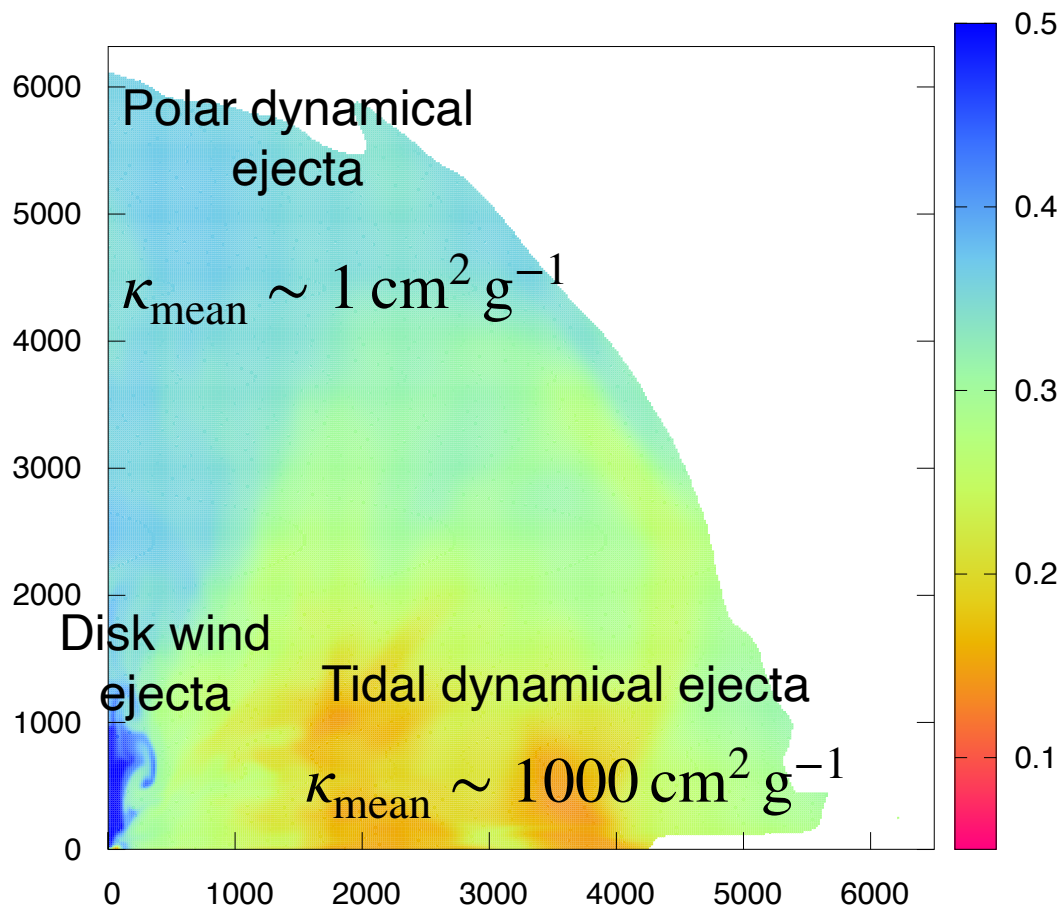
Calculations between different atomic calculations matches well



# Modelling light curves

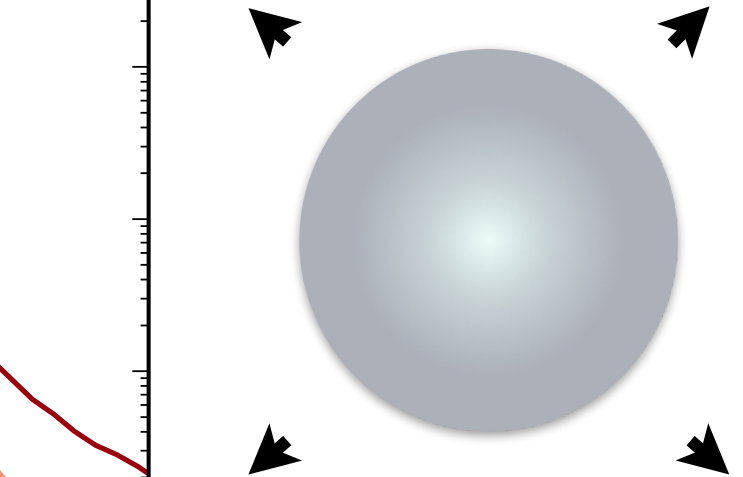
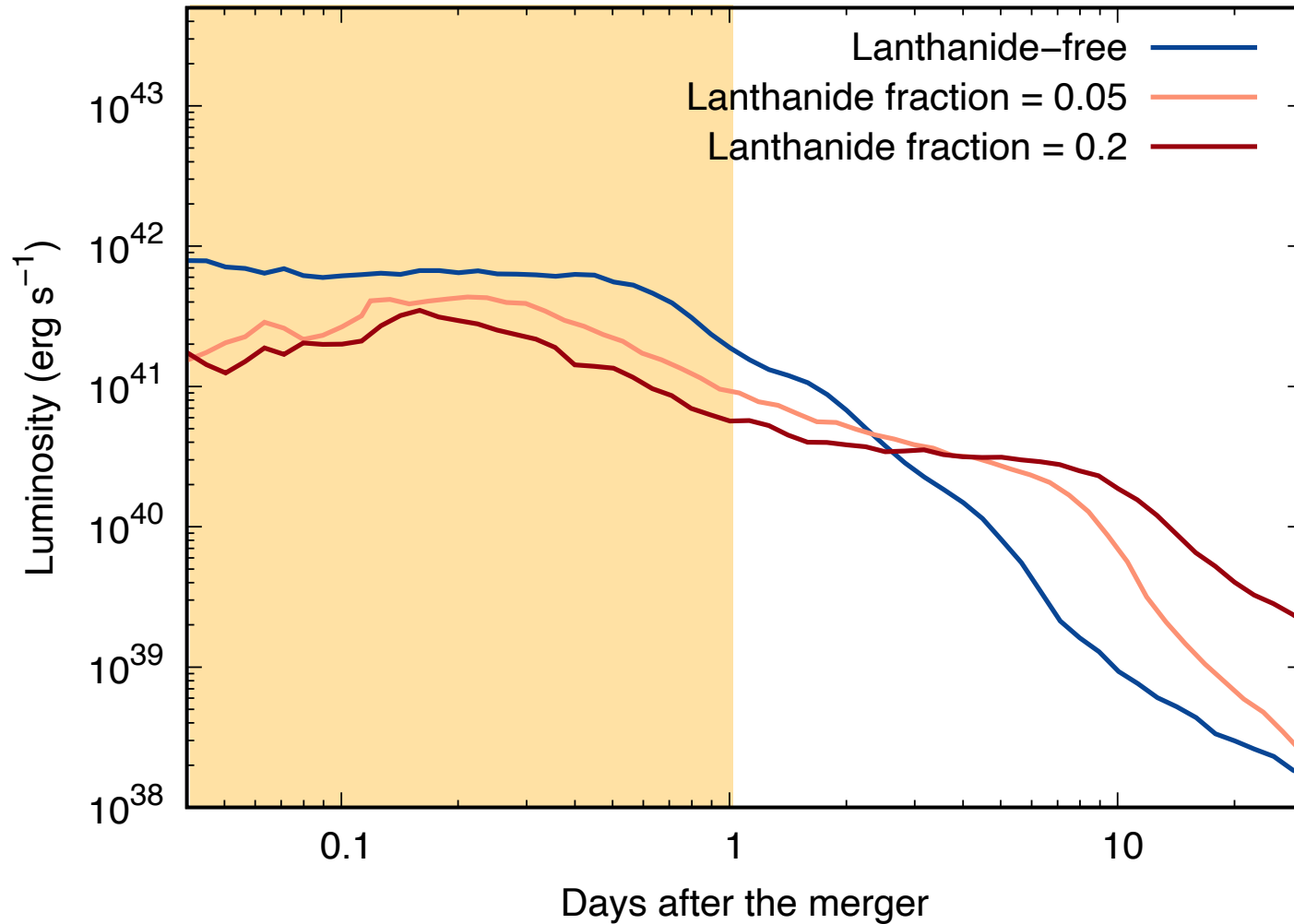
$$Y_e = \frac{n_e}{n_n + n_e}$$

= 1- neutron fraction



- Opacity vastly different across different components
- Angle dependence in light curves expected

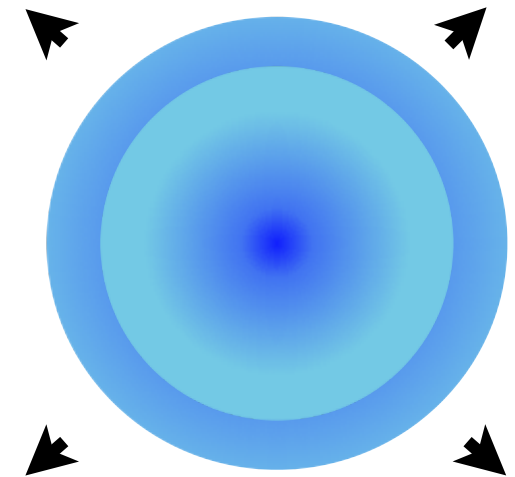
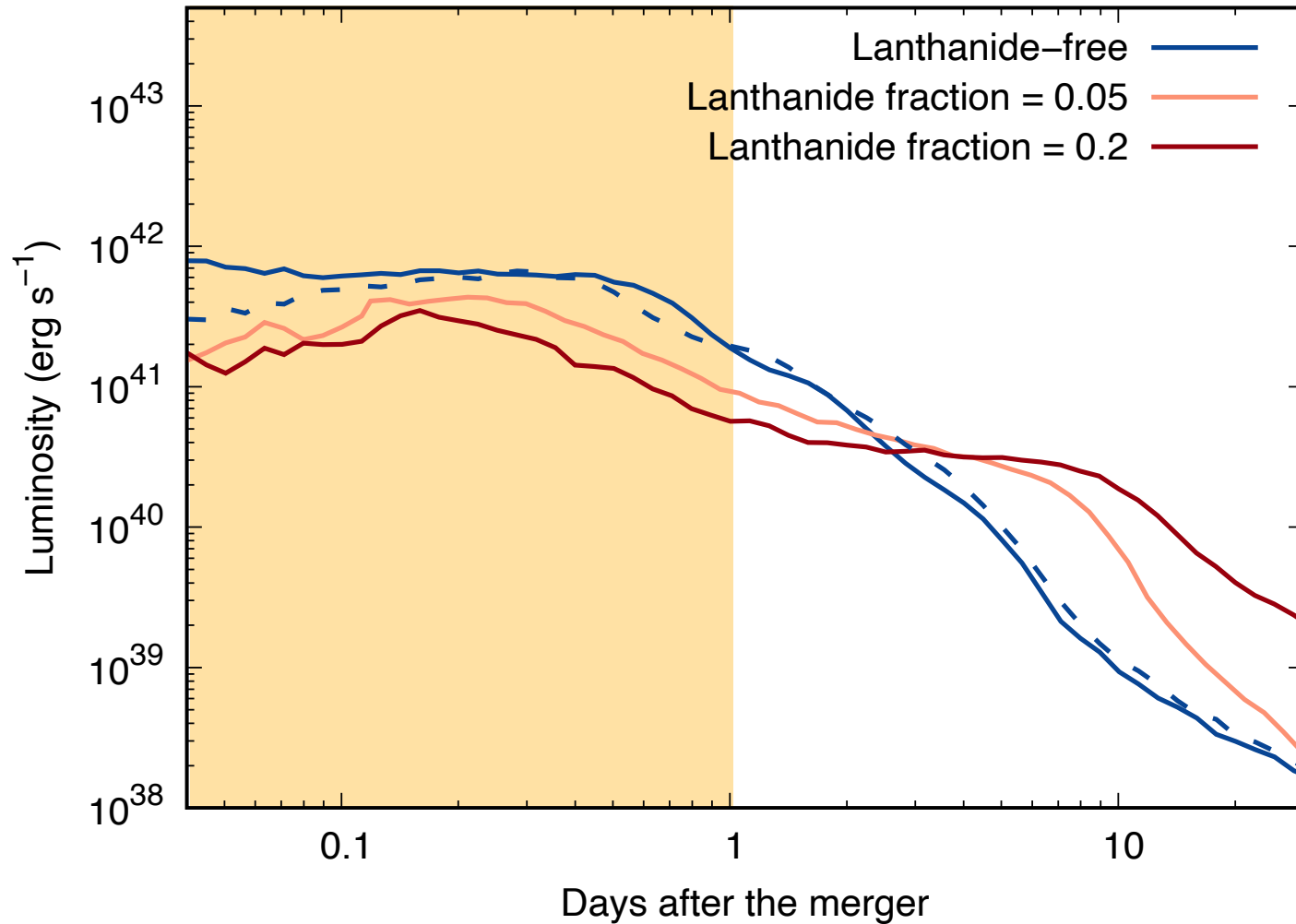
# Bolometric light curve



Banerjee+ 2020, 2022,  
2023, submitted

**Presence of lanthanides  
=> Unique signature in kilonova at first few (~ 4) hours**

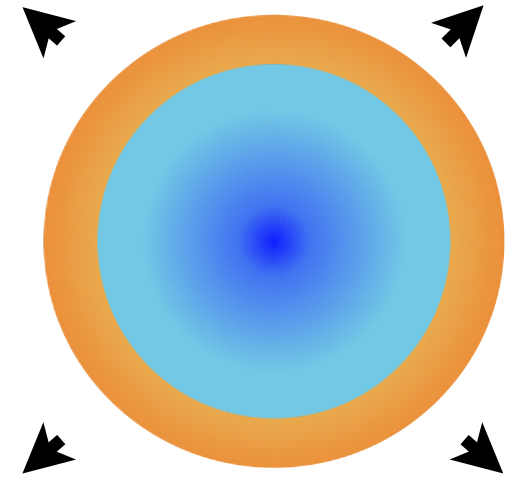
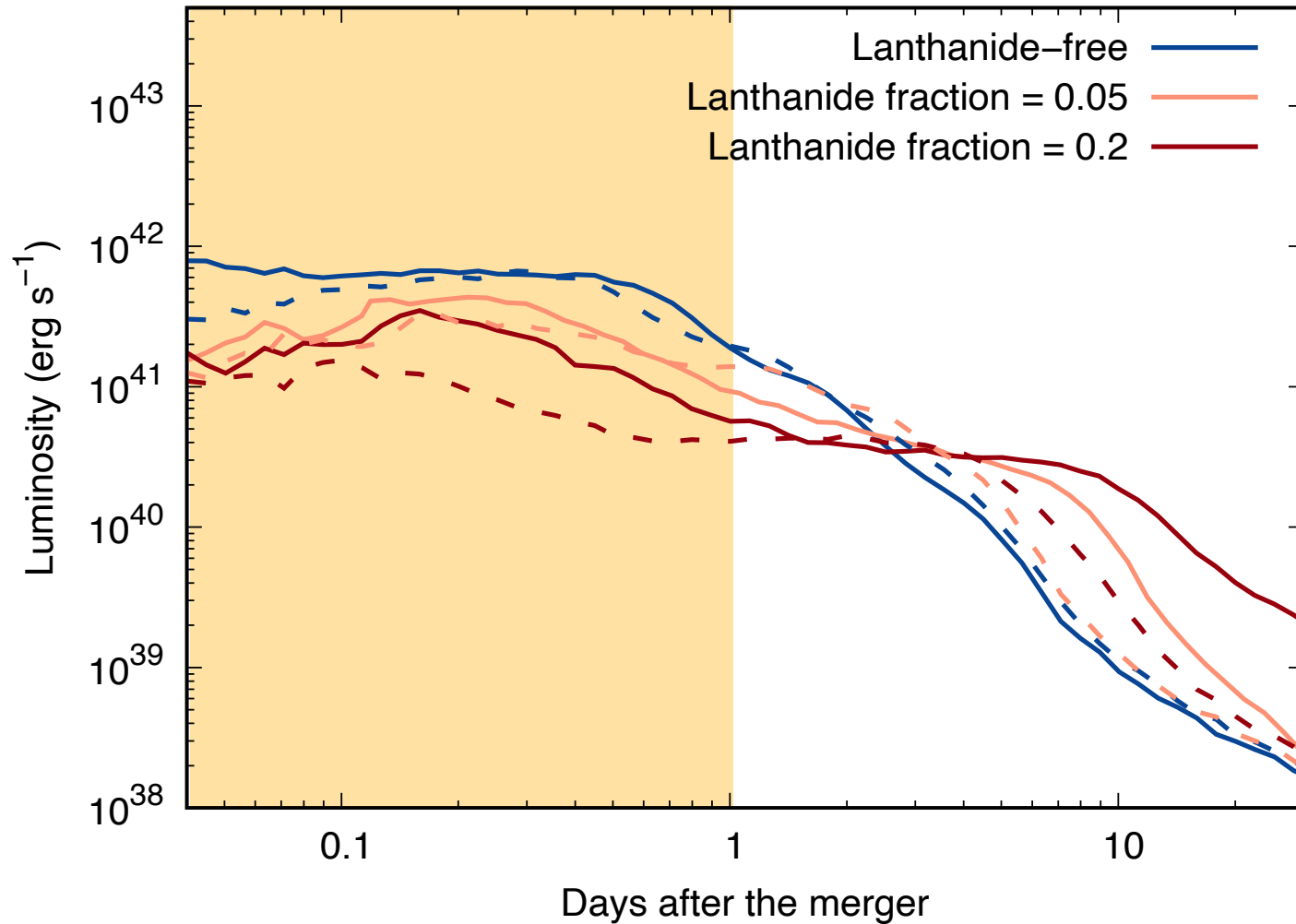
# Bolometric light curve



Banerjee+ 2020

**Detectable ejecta structure signature in kilonova at first few (~ 4) hours**

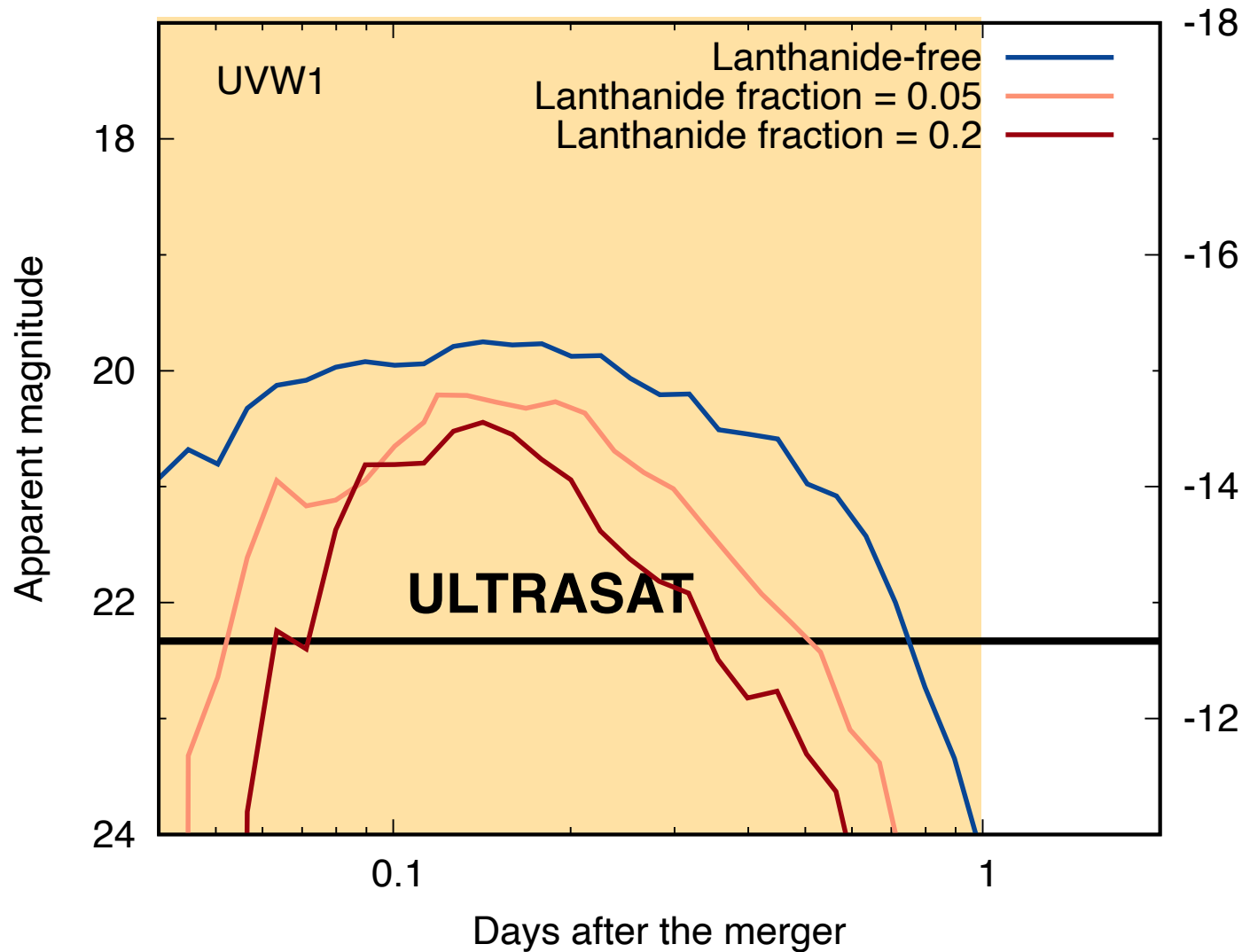
# Bolometric light curve



Banerjee+ 2023, submitted

**Detectable ejecta structure signature in kilonova at first few (~ 4) hours**

# Future prospects (UV)



Mission	$5\sigma$ (AB)
<i>Dorado</i>	20.5 (10 min. exp.)
ULTRASAT	22.3 (15 min. exp.)
UVEX	25 (15 min. exp.)

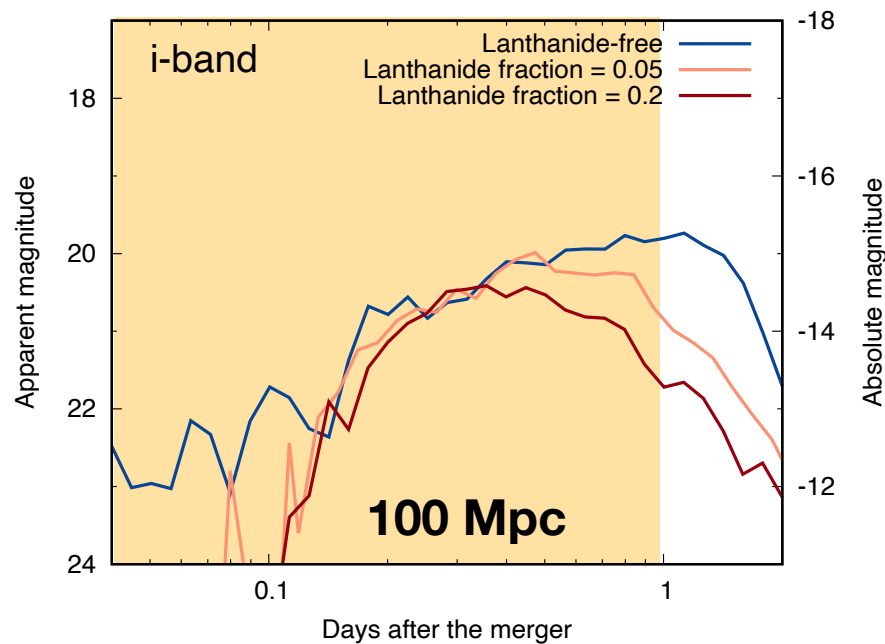
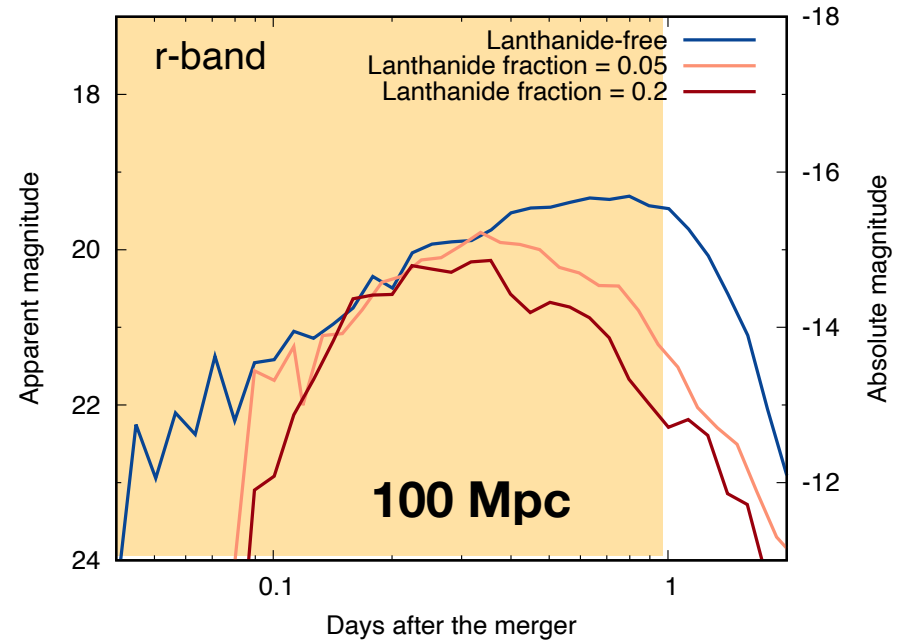
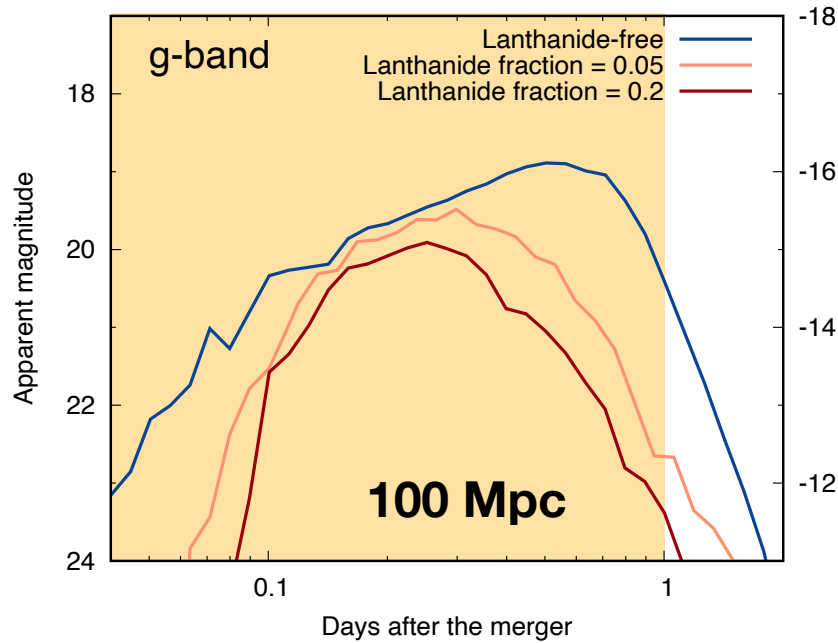
Dorsman et al. 2022

**Multiple upcoming UV missions: ULTRASAT, Dorado, UVEX**

**Our model predicts detectable early bright UV emission**



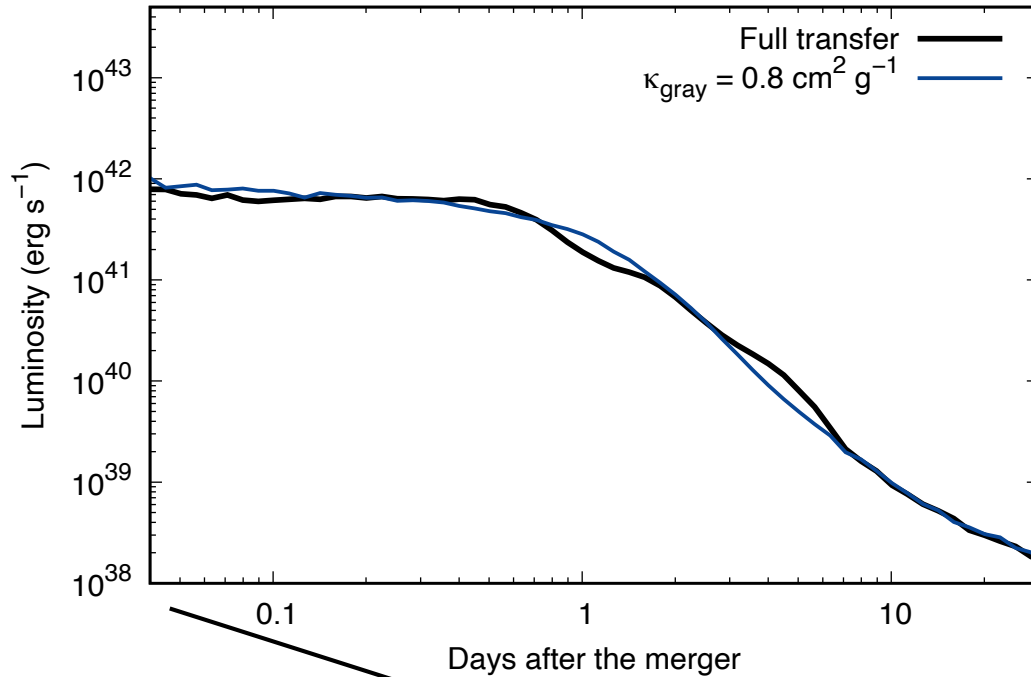
# Lanthanide-rich kilonova (optical)



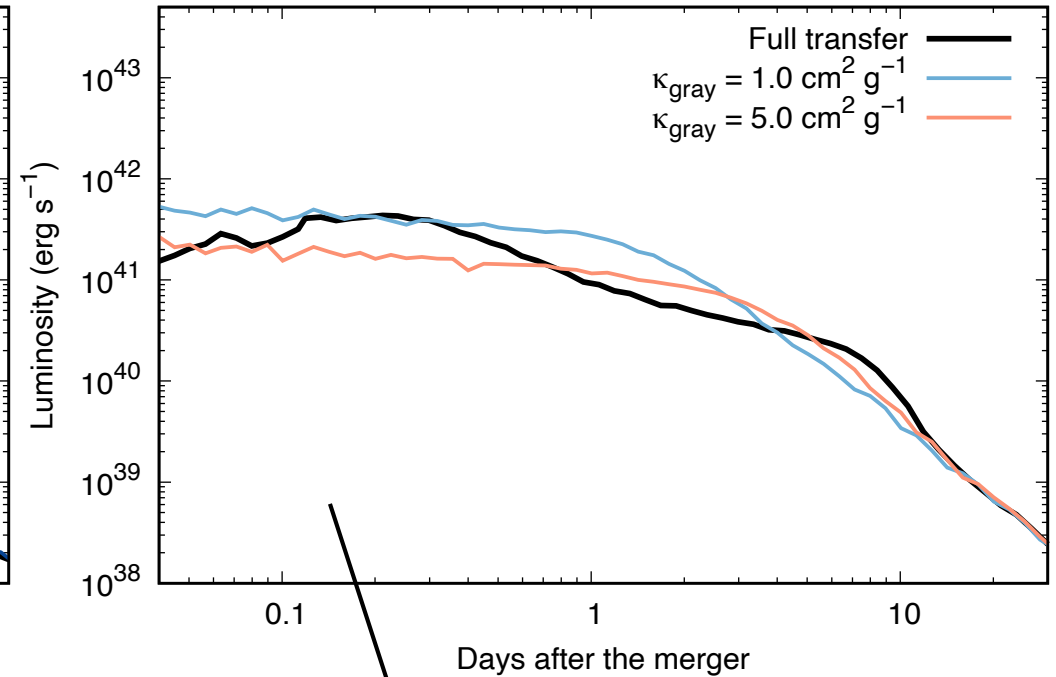
- **Detectable by ZTF, DECam, Subaru HSC**
- **Easily detectable by the upcoming wide-field survey (e.g., Vera Rubin Observatory)**

# Suggested gray opacities

## Lanthanide-free



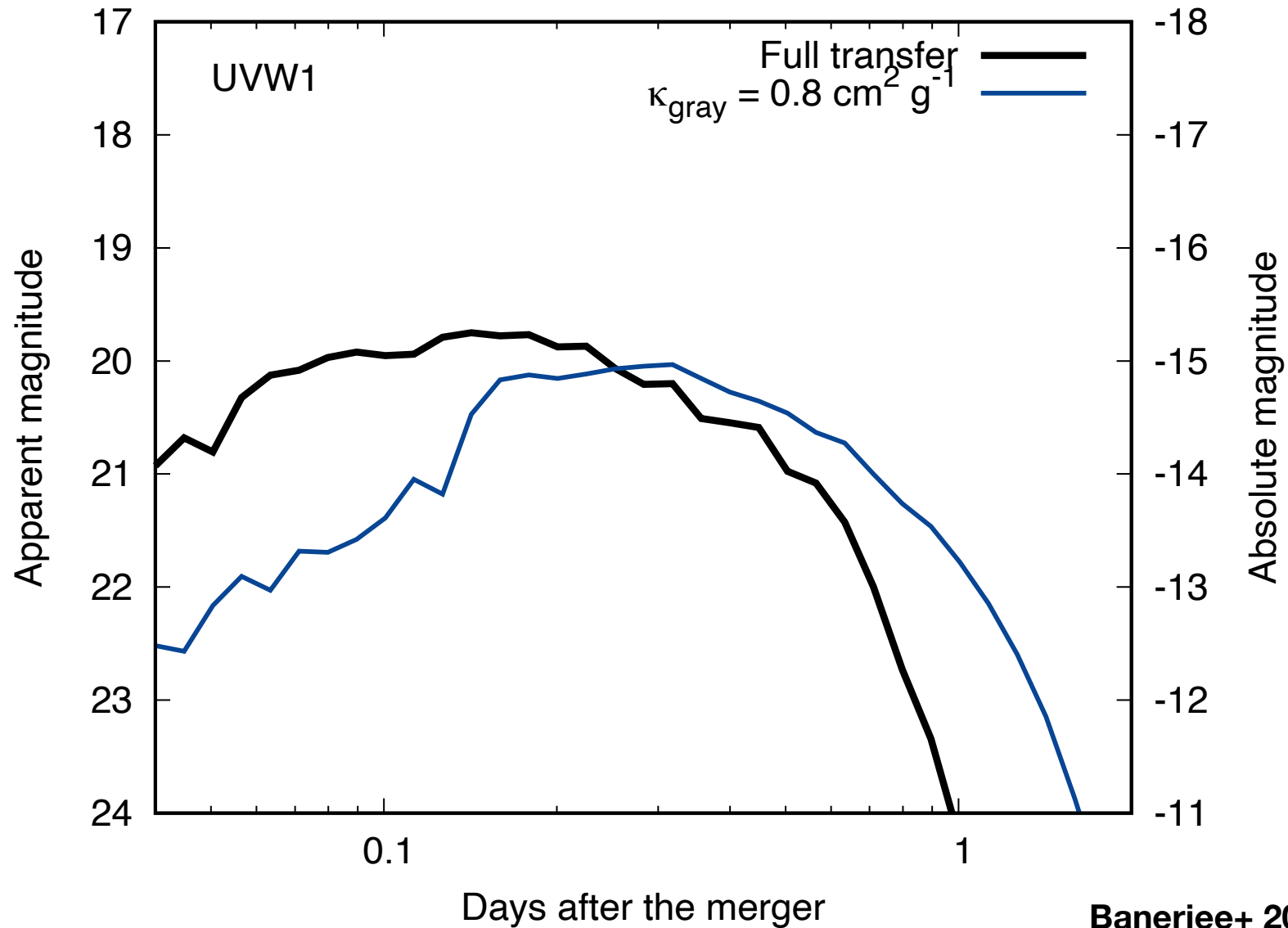
## Lanthanide fraction = 0.05



**Banerjee+ 2023, submitted**

Models	Electron fraction		Suggested gray opacities ( $\text{cm}^2 \text{g}^{-1}$ )
	$Y_{e,\text{in}}$ ( $v = 0.05c - 0.2c$ , $M_{\text{ej},\text{in}} = 0.01M_{\odot}$ )	$Y_{e,\text{out}}$ ( $v = 0.2c - 0.33c$ , $M_{\text{ej},\text{out}} = 0.001M_{\odot}$ )	
Model 1	0.10 – 0.20	–	2.0 – 10.0
Model 2	0.20 – 0.30	–	1.0 – 5.0
Model 3	0.30 – 0.40	–	0.8
Model 4	0.30 – 0.40	0.10 – 0.20	5.0 – 20.0
Model 5	0.30 – 0.40	0.20 – 0.30	3.0 – 10.0
Model 6	0.30 – 0.40	0.30 – 0.40	0.8 – 1.0

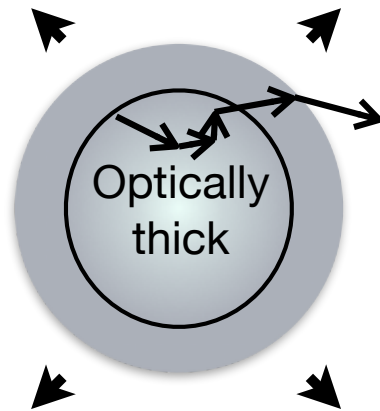
# Suggested gray opacities



Banerjee+ 2023, submitted

**Multi-color light curves cannot be reproduced**

# Ongoing works



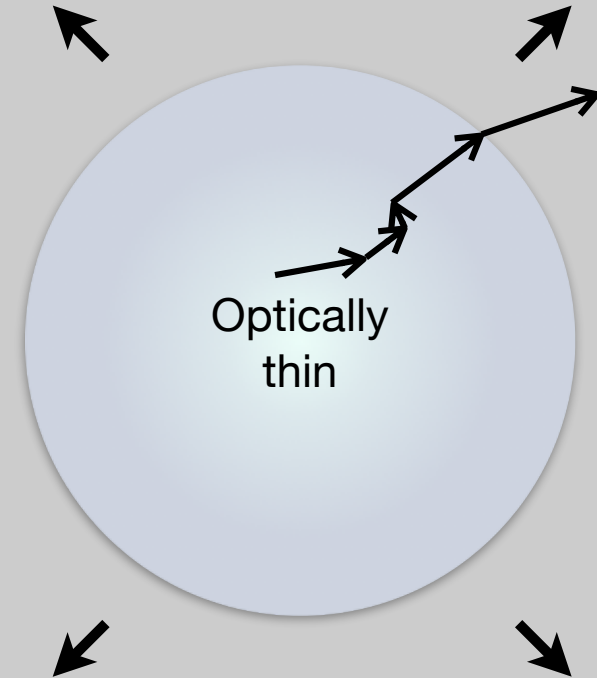
Early time (LTE):

**Required atomic data:**

- Energy levels
- E1 transitions

**All elements Ca - Ra: Tanaka+2020 (I -IV),  
Banerjee+ 2020, 2022, 2023, submitted (V -XI)**

$t \sim$  a few days



Late time (Non-LTE):

**Required atomic data:**

- E1+ M1 transitions
- Collisional cross-sections
- Recombination coefficients
- Photo-ionization cross-sections...

e.g., Hotokezaka et al. 2021, Pognan et al. 2022a,b

$t \geq$  week

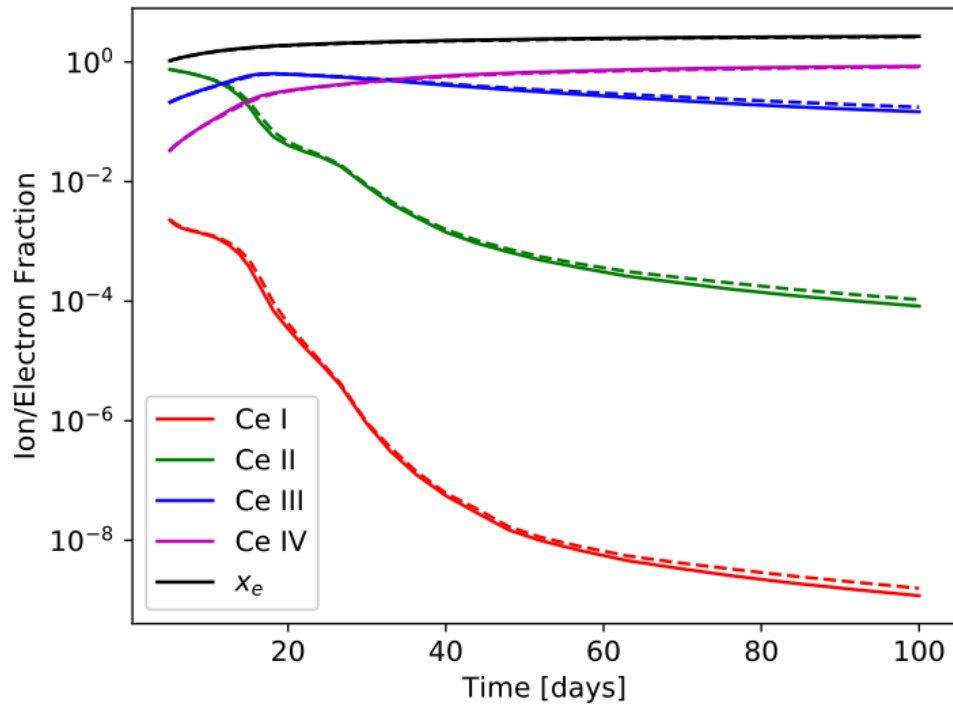
**Time**

See Q. Pognan's talk

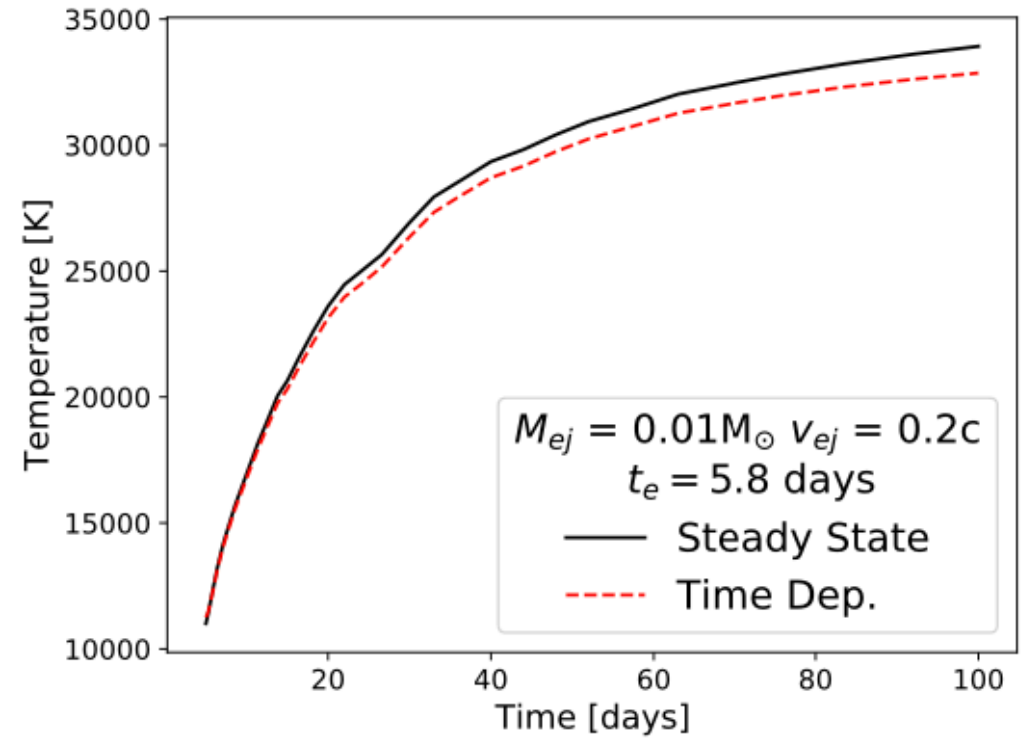
# Physical conditions

For a AT2017gfo-like kilonova

By solving rate equation



By balancing radioactive heating + cooling



**Spectra  $\Leftarrow$  Ionization and temperature  
 $\Leftarrow$  Recombination rate**

Pognan et al. 2022a

# Conclusion

- Towards more observations  $\leq$  More detailed physics calculations required
- Atomic data for heavy elements required for modelling all phases
- Huge efforts to understand photospheric phase ongoing
- Nebular phase is relatively unexplored..  
slowly but surely has started now!