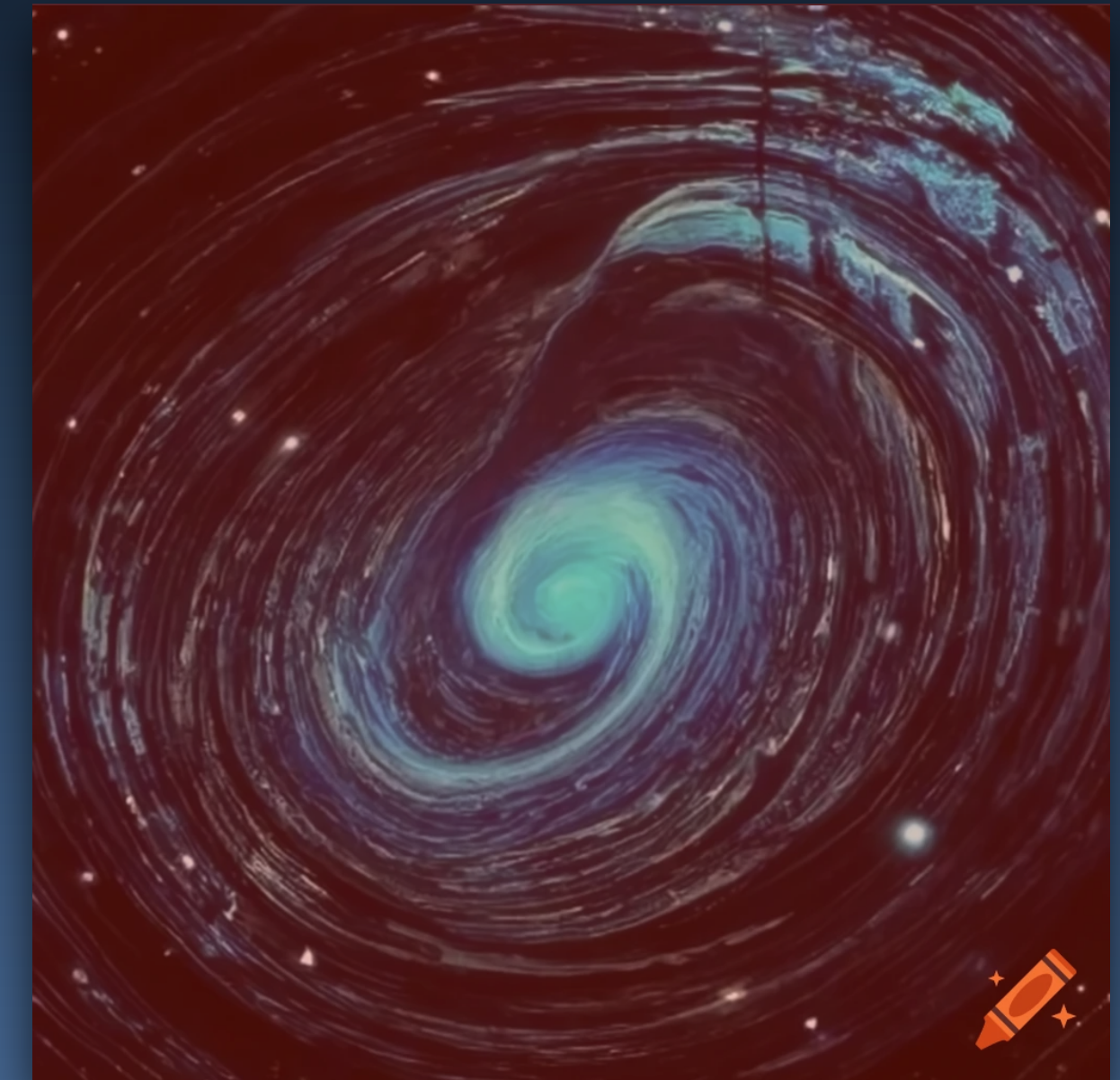
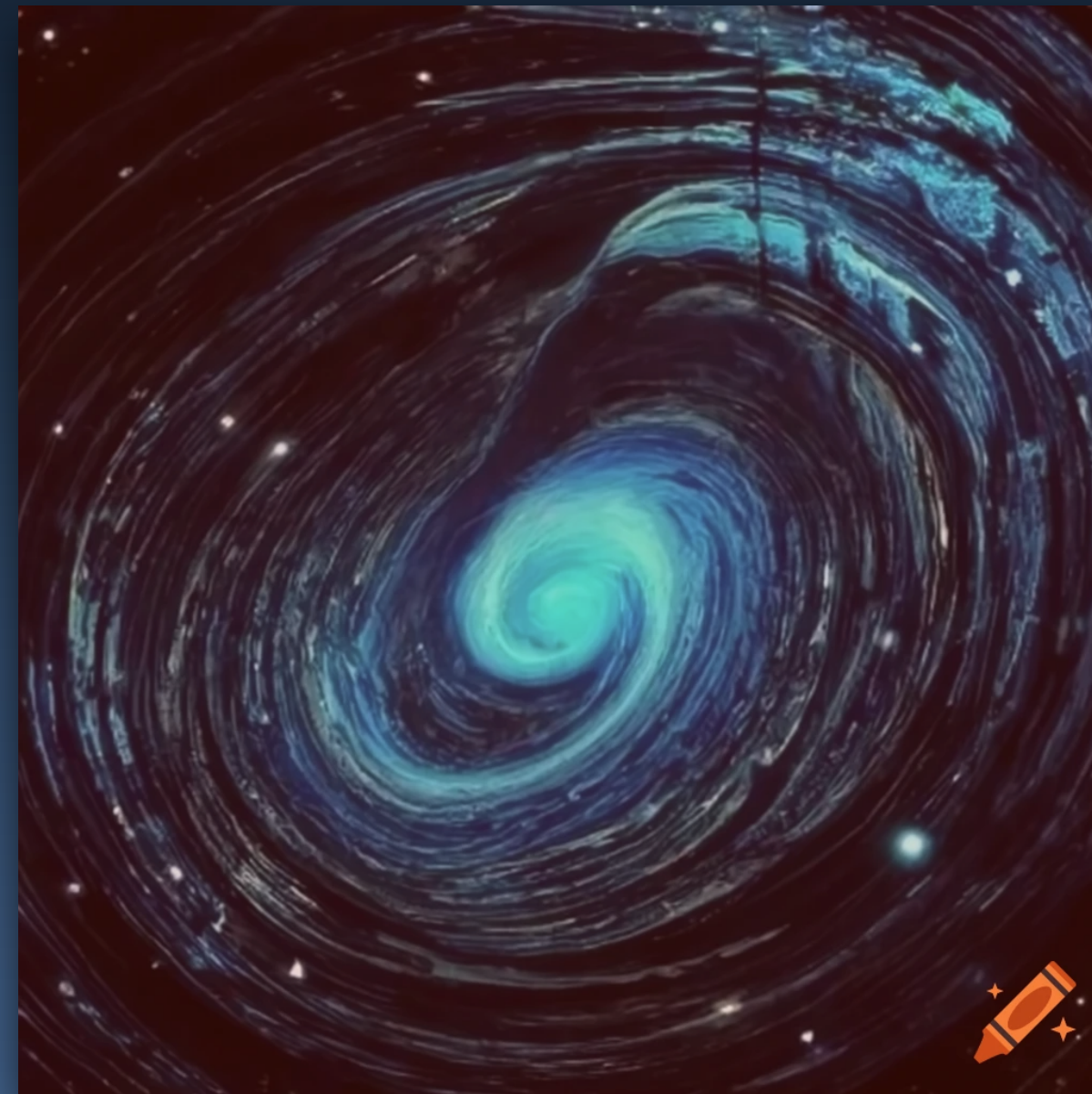


Testing Gravity through the Distortion of Time



Sveva Castello

sveva.castello@unige.ch



UNIVERSITÉ
DE GENÈVE

FACULTÉ DES SCIENCES

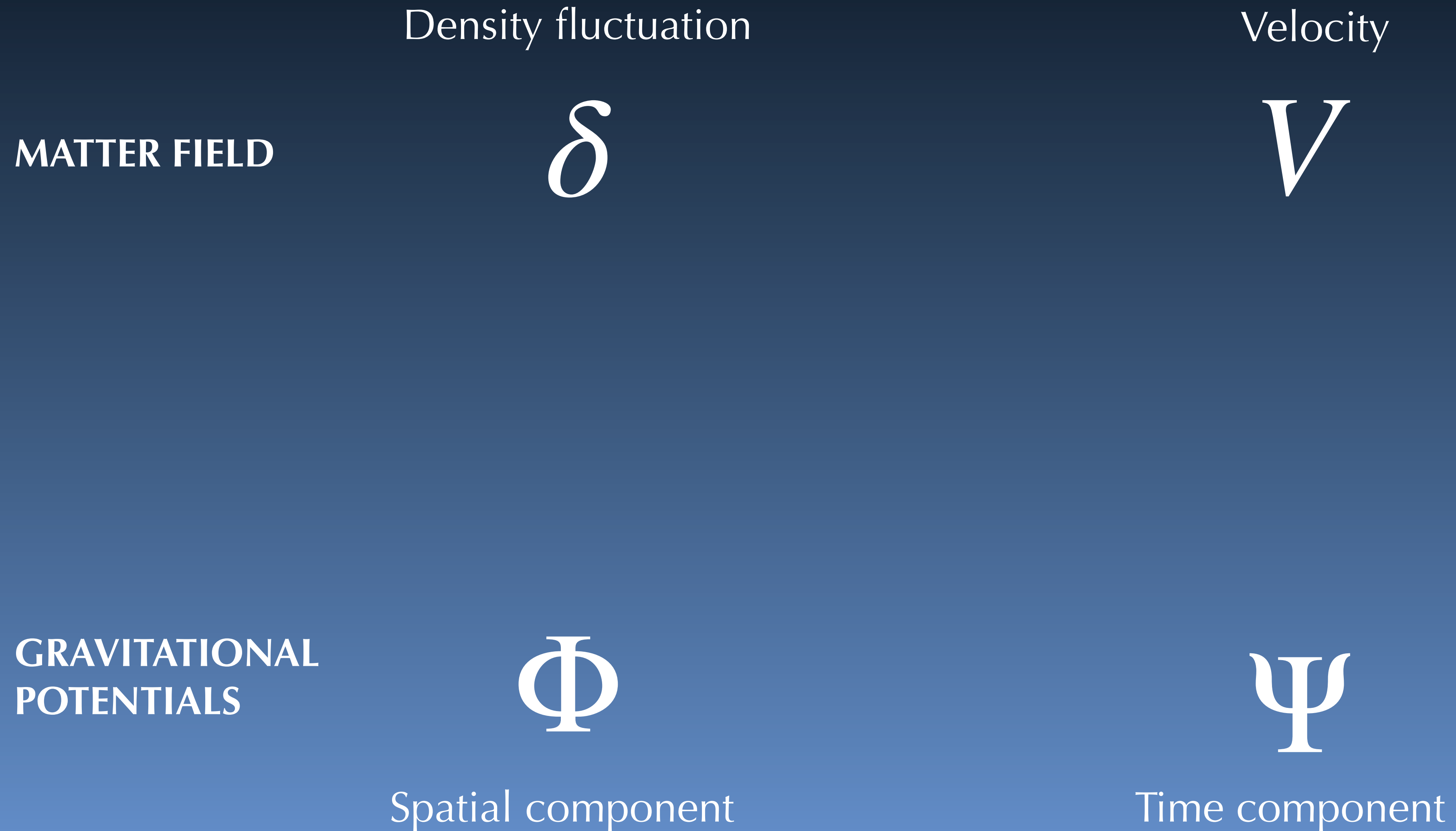
Nordic Cosmology Meeting

October 23rd, 2023



European Research Council
Established by the European Commission

Describing the Universe with four fields



Describing the Universe with four fields

Density fluctuation

Velocity

MATTER FIELD

δ

V

Relations in GR

GRAVITATIONAL
POTENTIALS

Φ

Ψ

Spatial component

Time component

Describing the Universe with four fields

Density fluctuation

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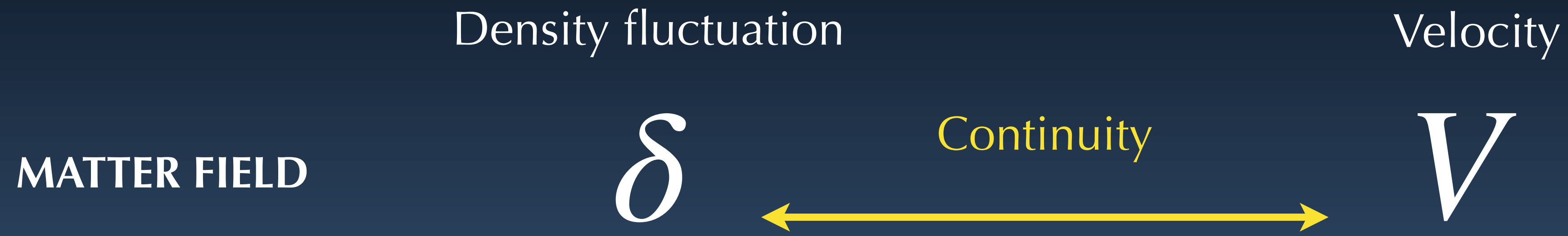
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Ψ

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Describing the Universe with four fields



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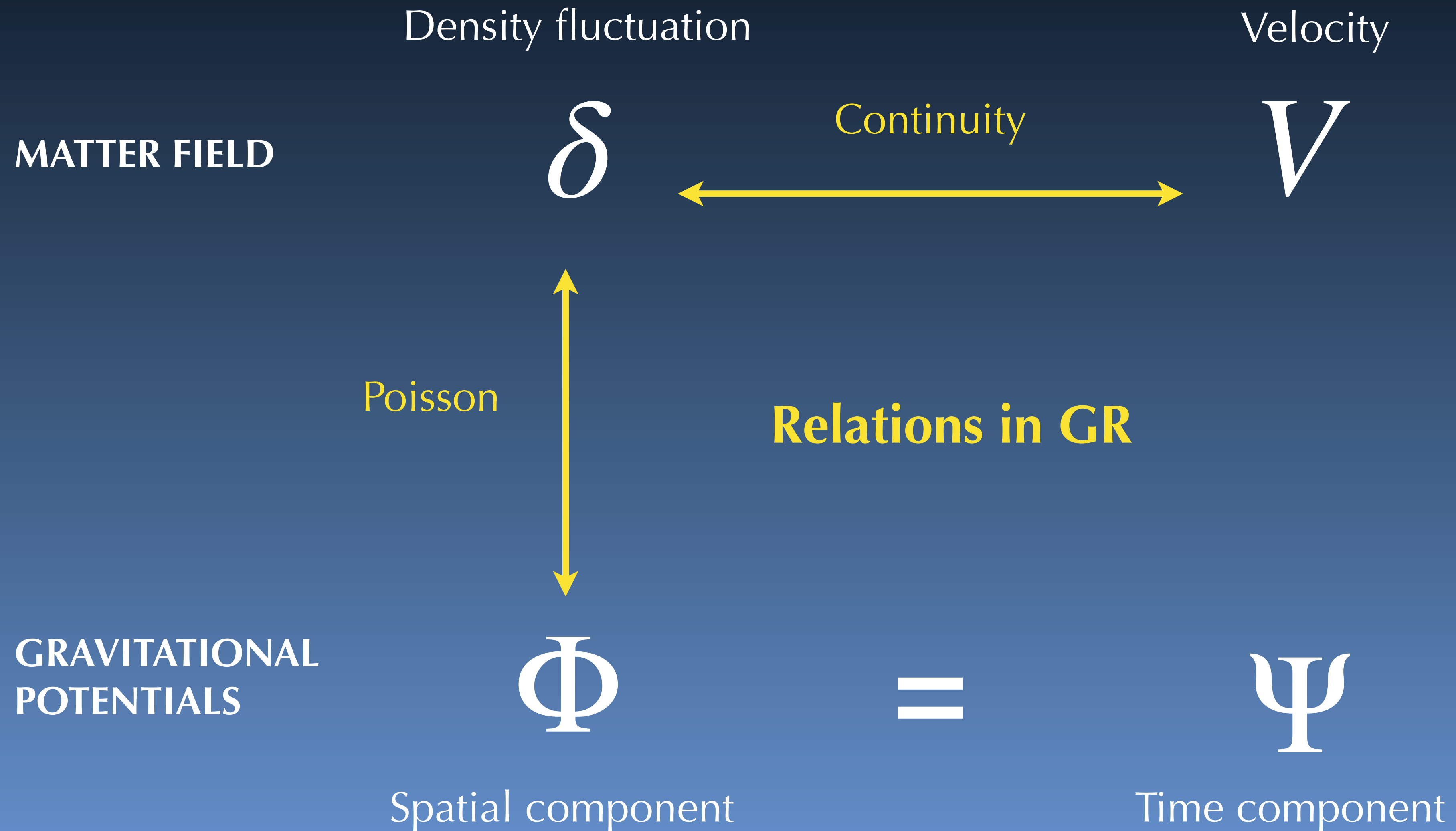
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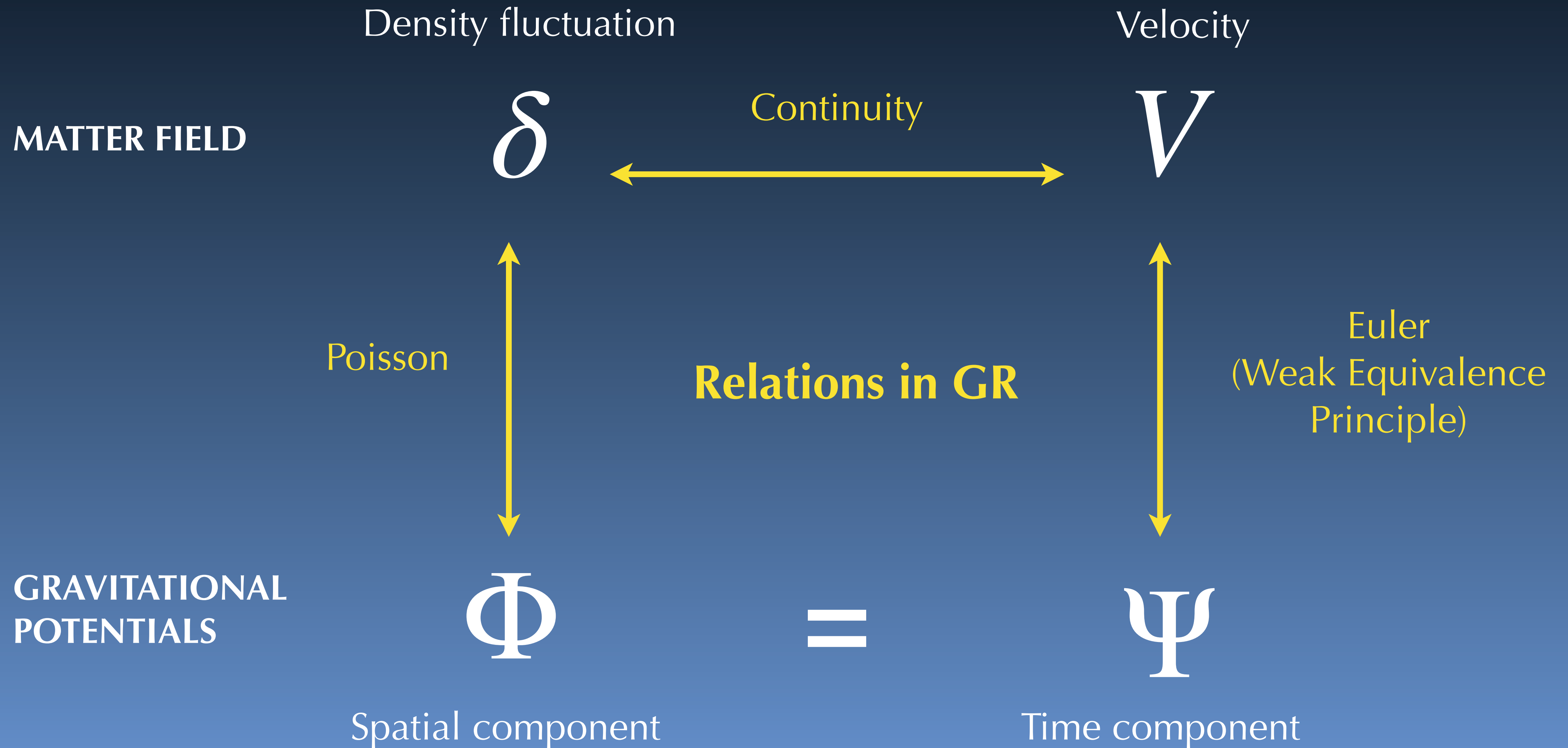
Spatial component

Time component

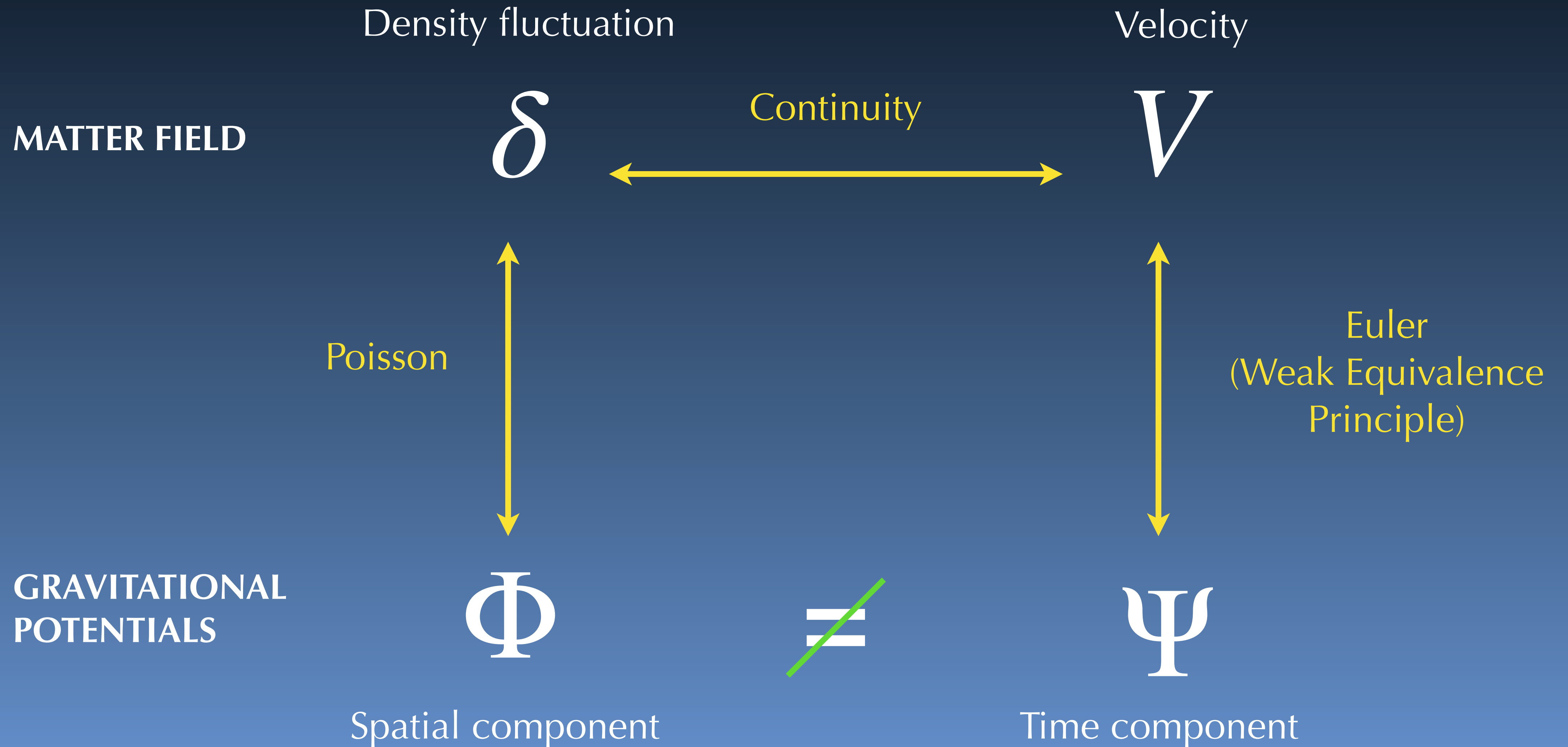
Describing the Universe with four fields



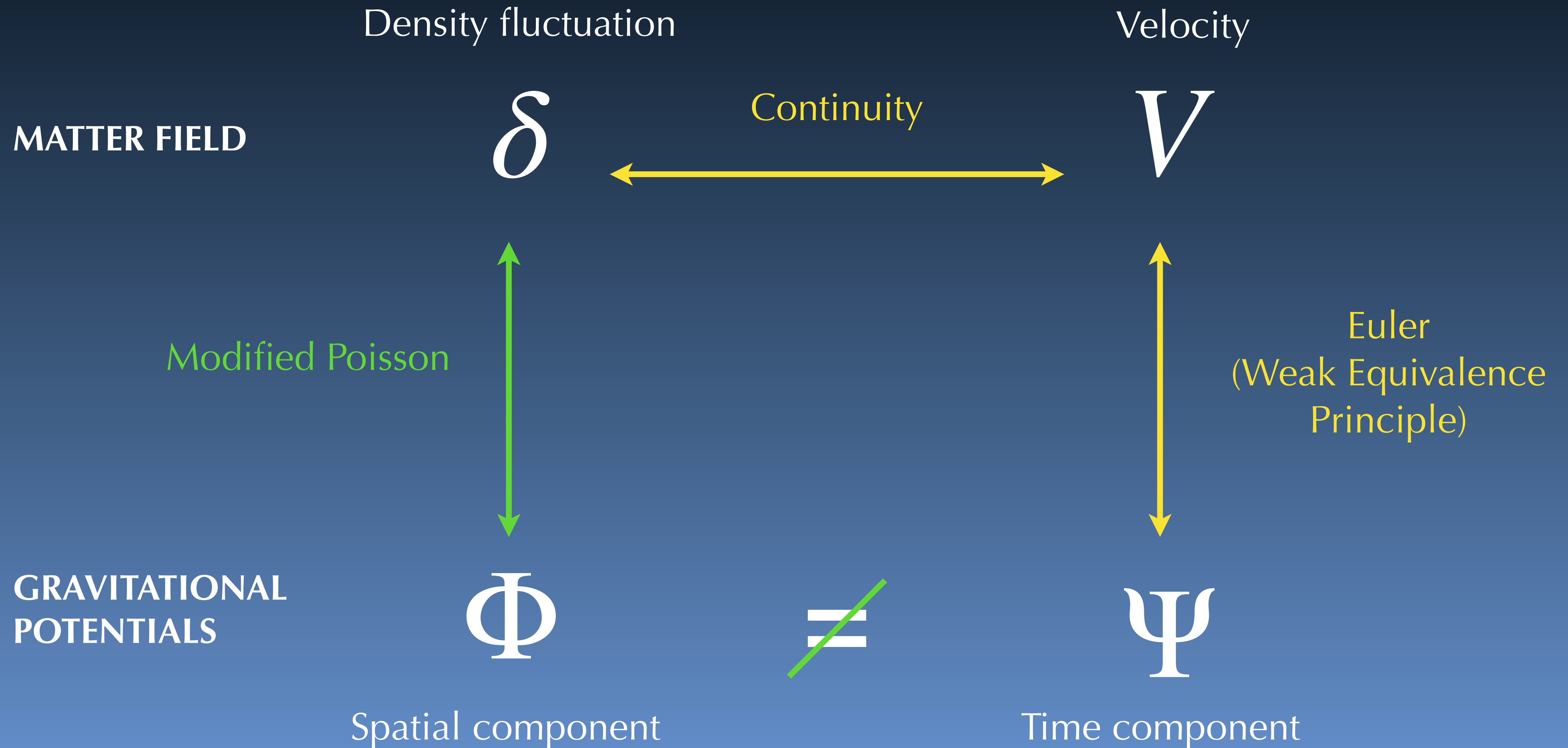
Describing the Universe with four fields



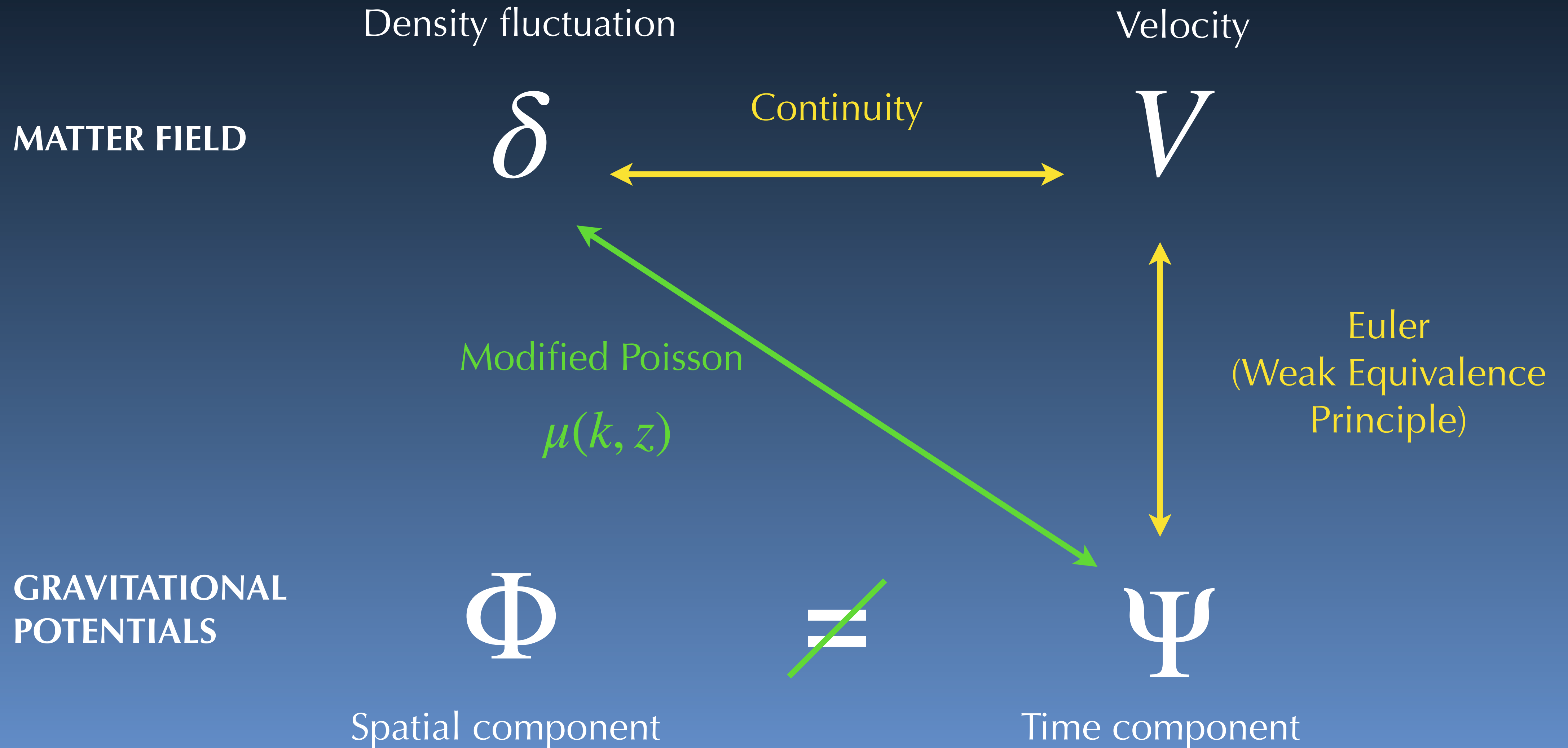
Describing the Universe with four fields



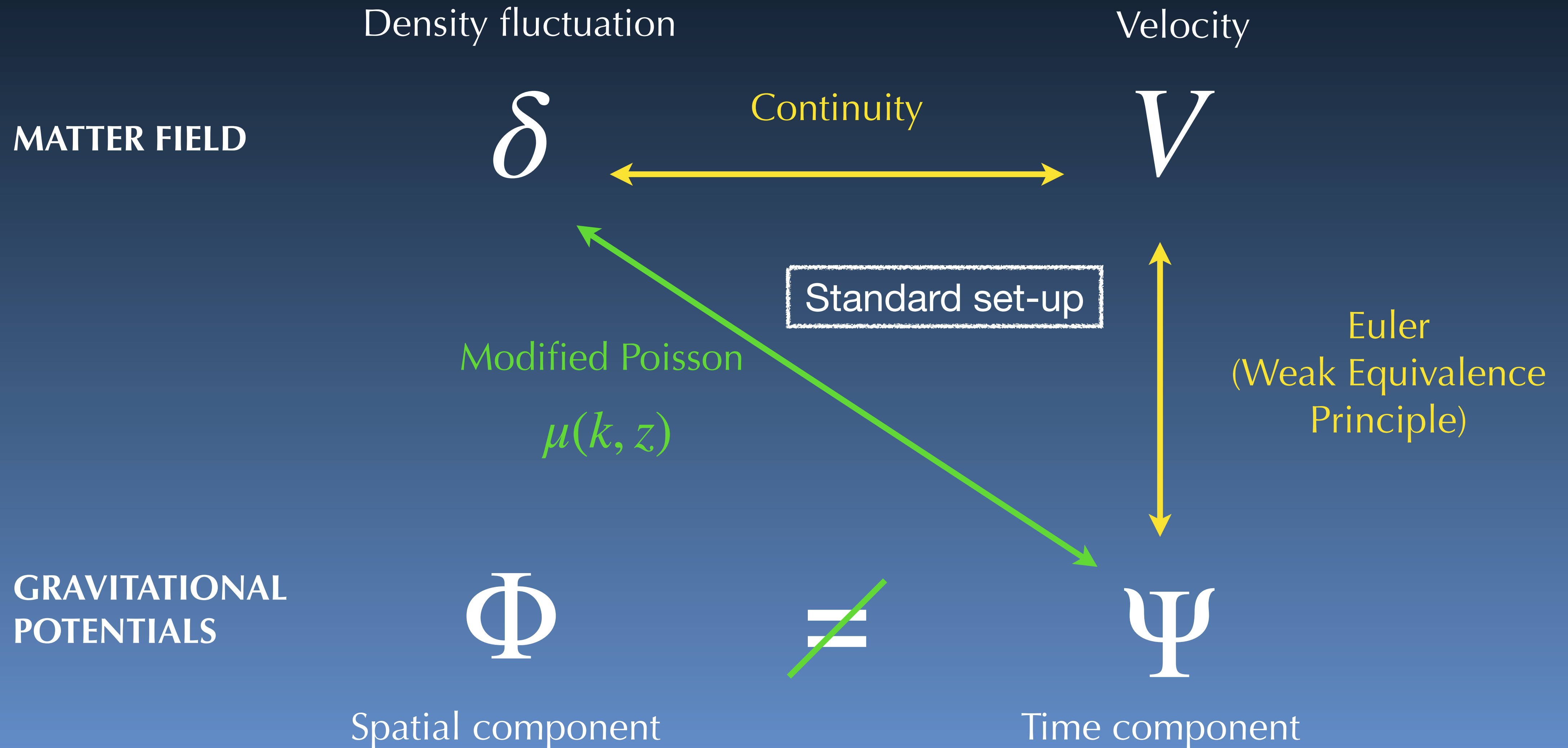
Describing the Universe with four fields



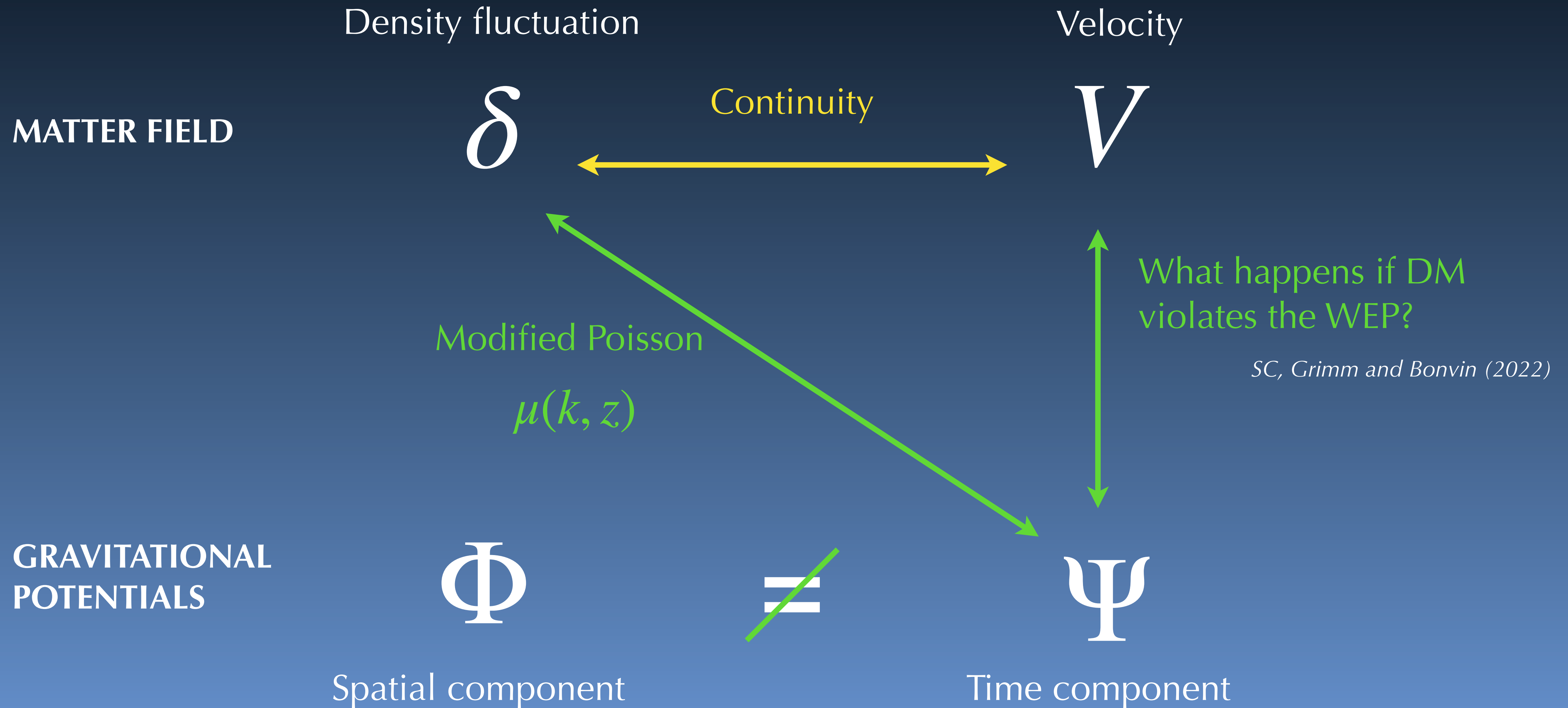
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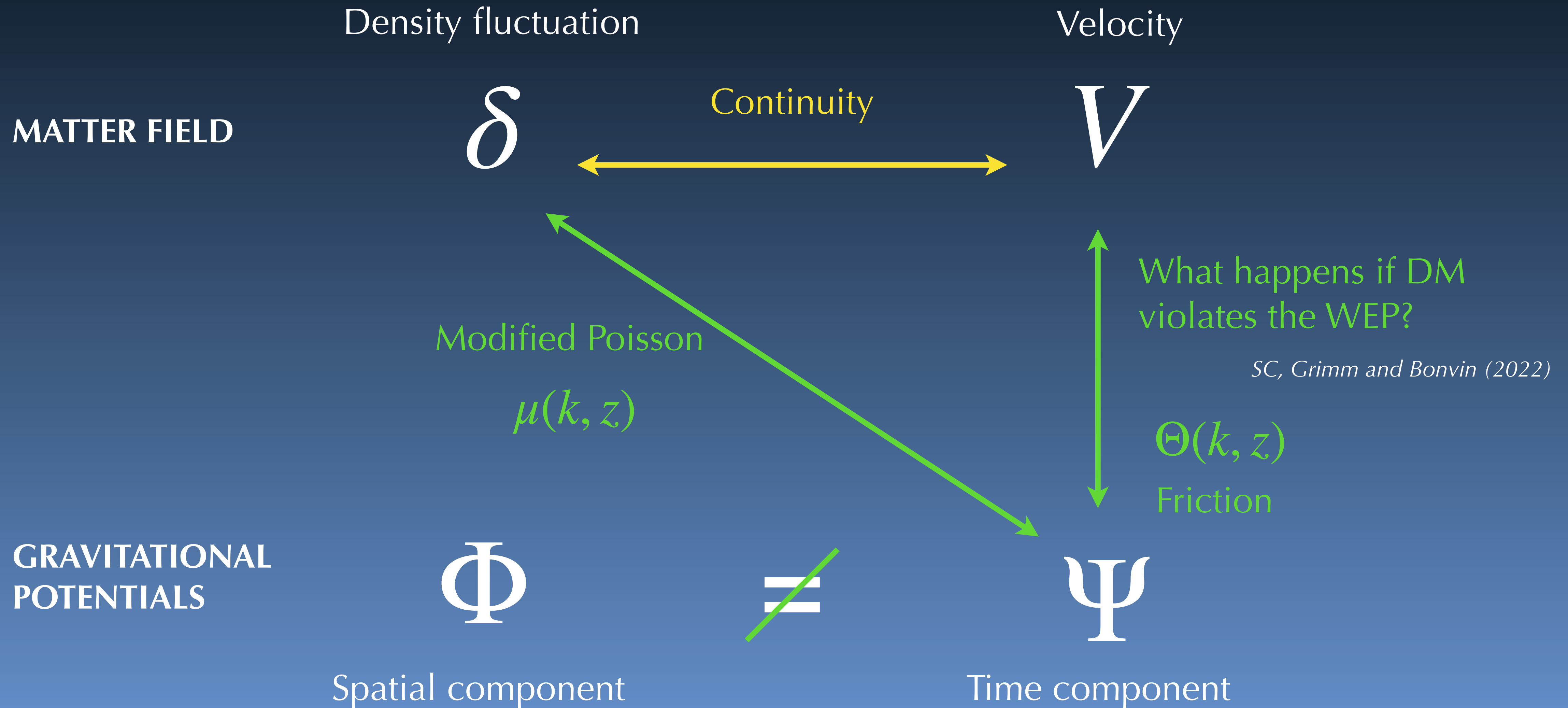
Describing the Universe with four fields



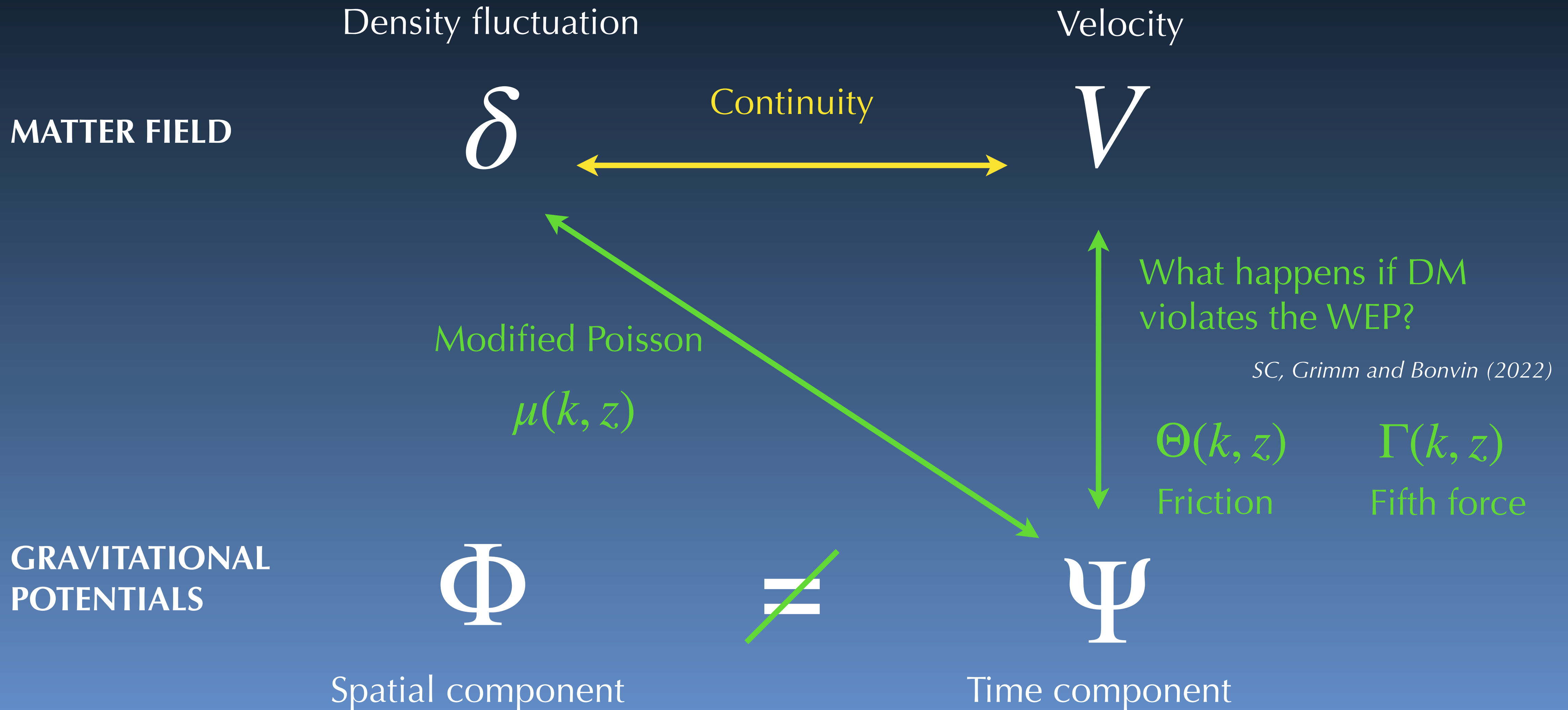
Describing the Universe with four fields



Describing the Universe with four fields



Describing the Universe with four fields



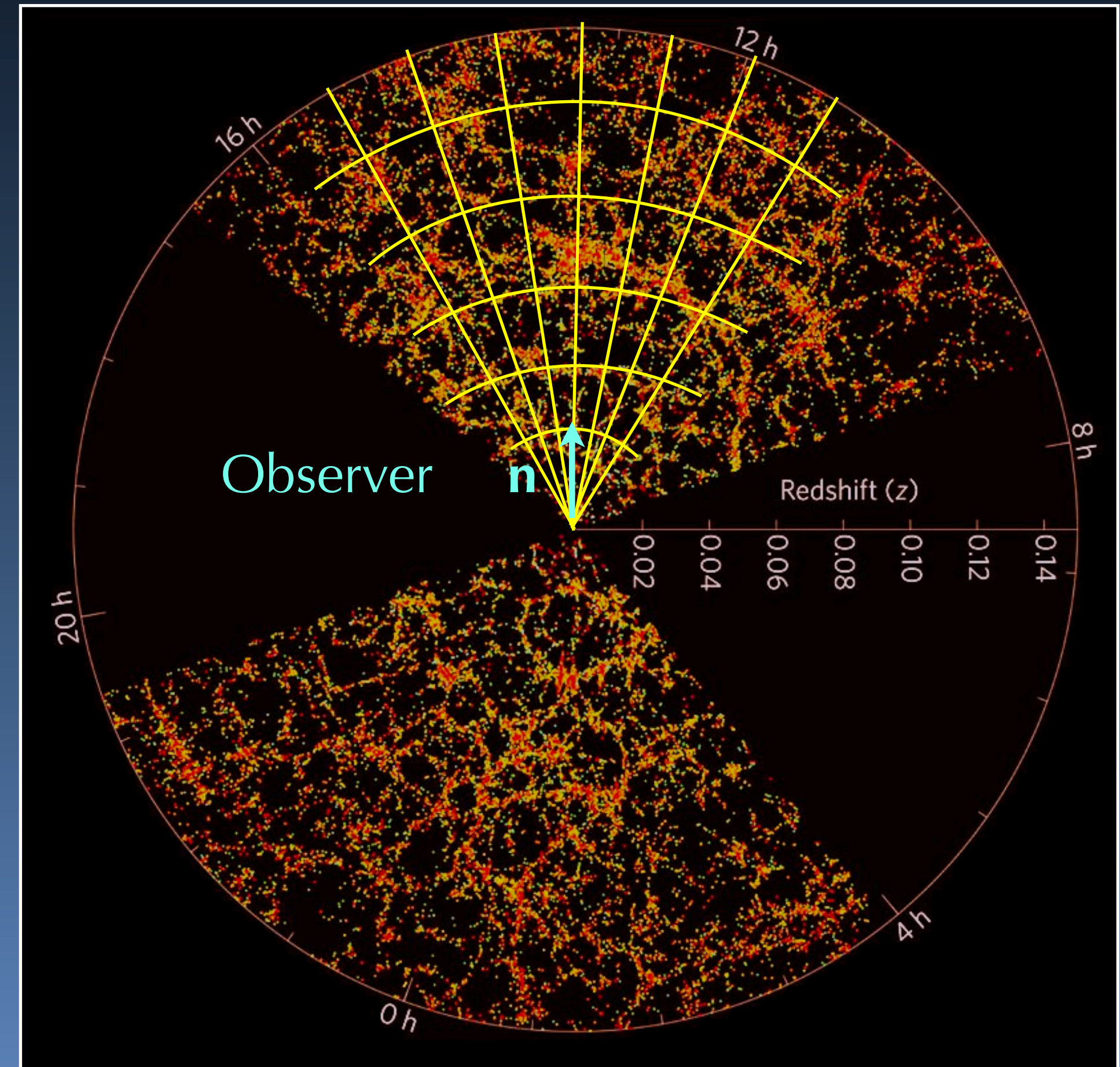
Comparison with observations

Fluctuations in galaxy number counts

$$\Delta(z, \mathbf{n}) = b \delta_{\text{DM}} - \frac{1}{\mathcal{H}} \partial_r (\mathbf{V} \cdot \mathbf{n})$$

DM density
x galaxy bias

Redshift-space
distortions (RSD)



Credits: M.Blanton, SDSS

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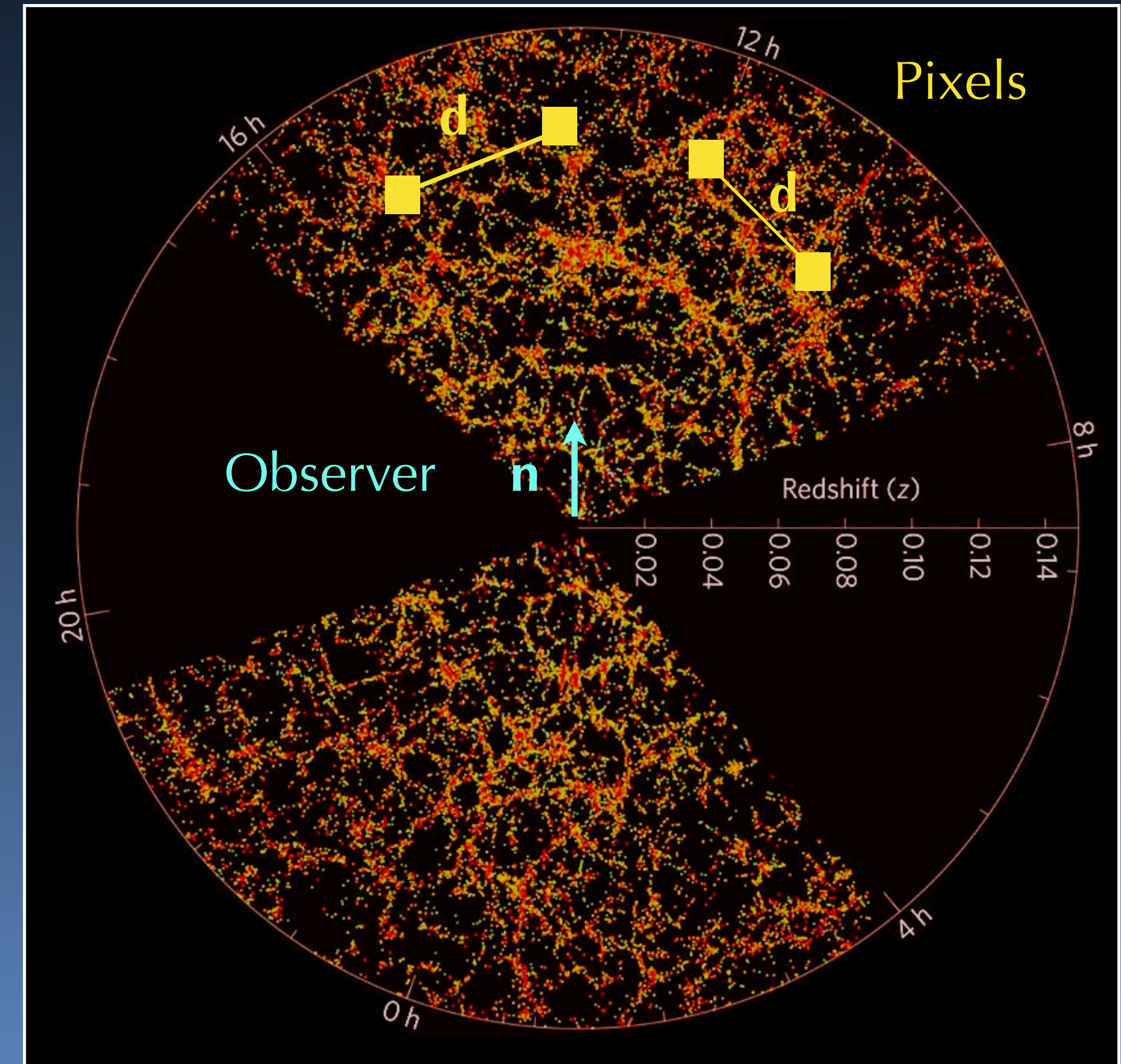
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Two-point correlation function

$$\xi \equiv \langle \Delta(z, \mathbf{n}) \Delta(z', \mathbf{n}') \rangle$$



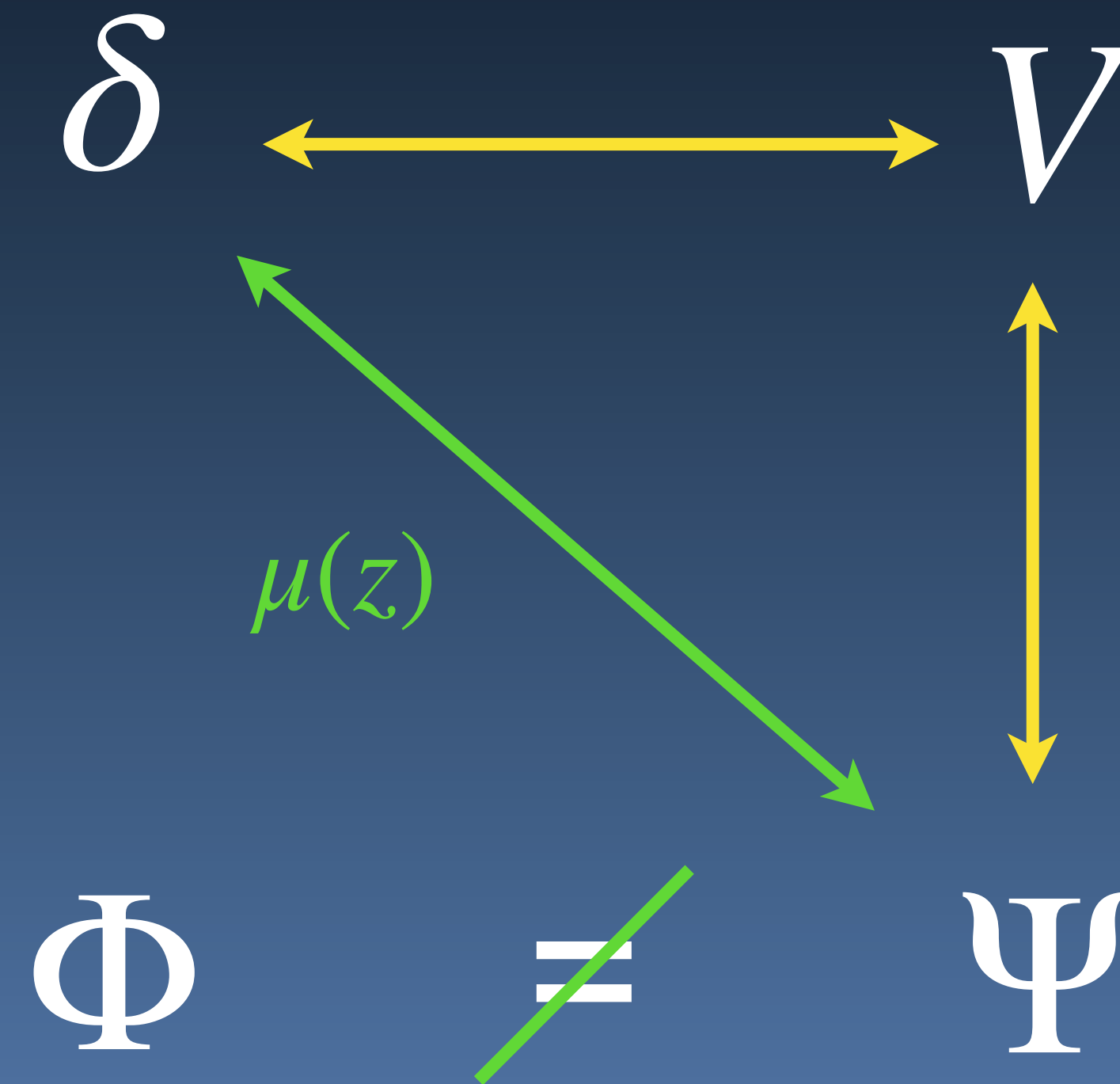
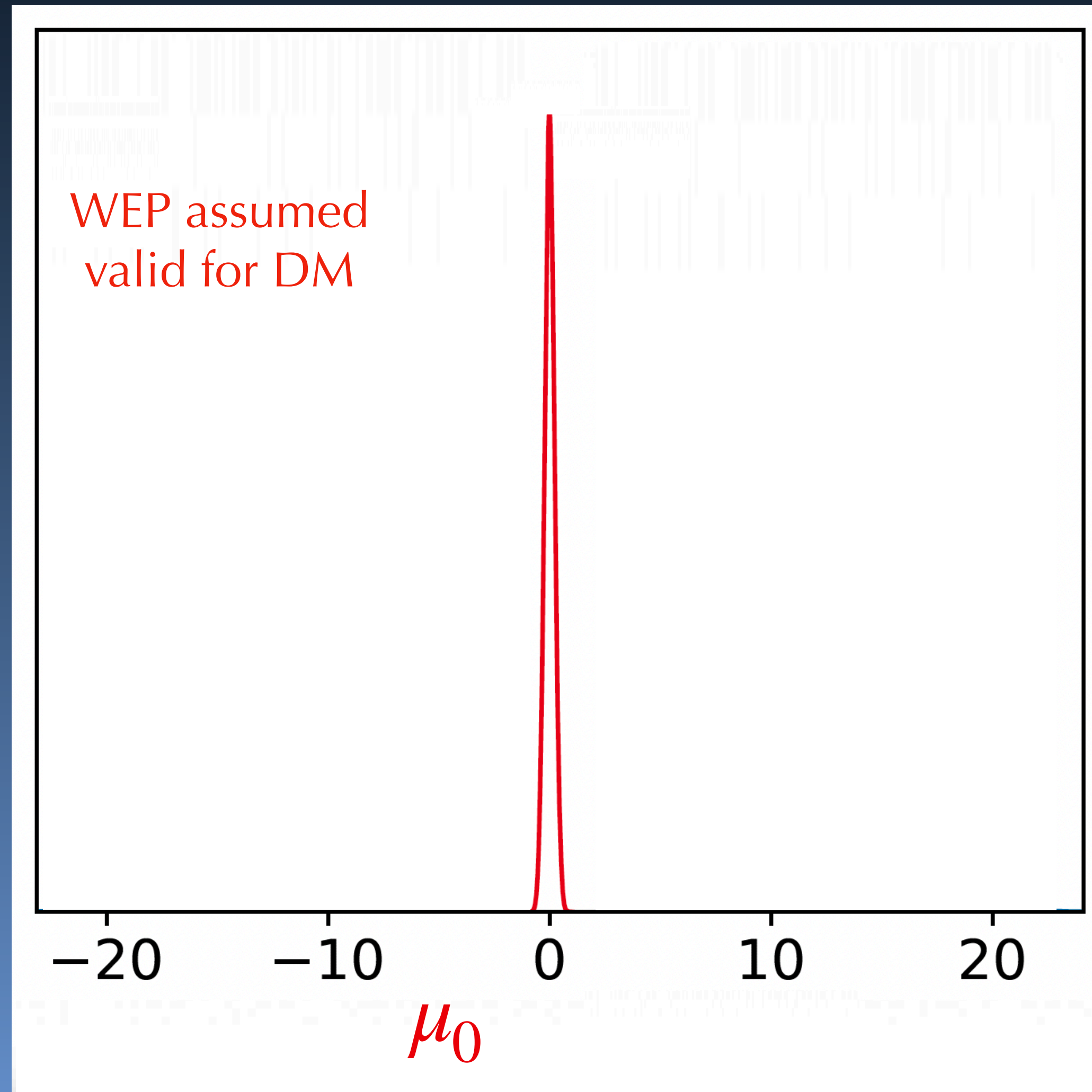
Extracted from observations and compared with theoretical predictions



Credits: M.Blanton, SDSS

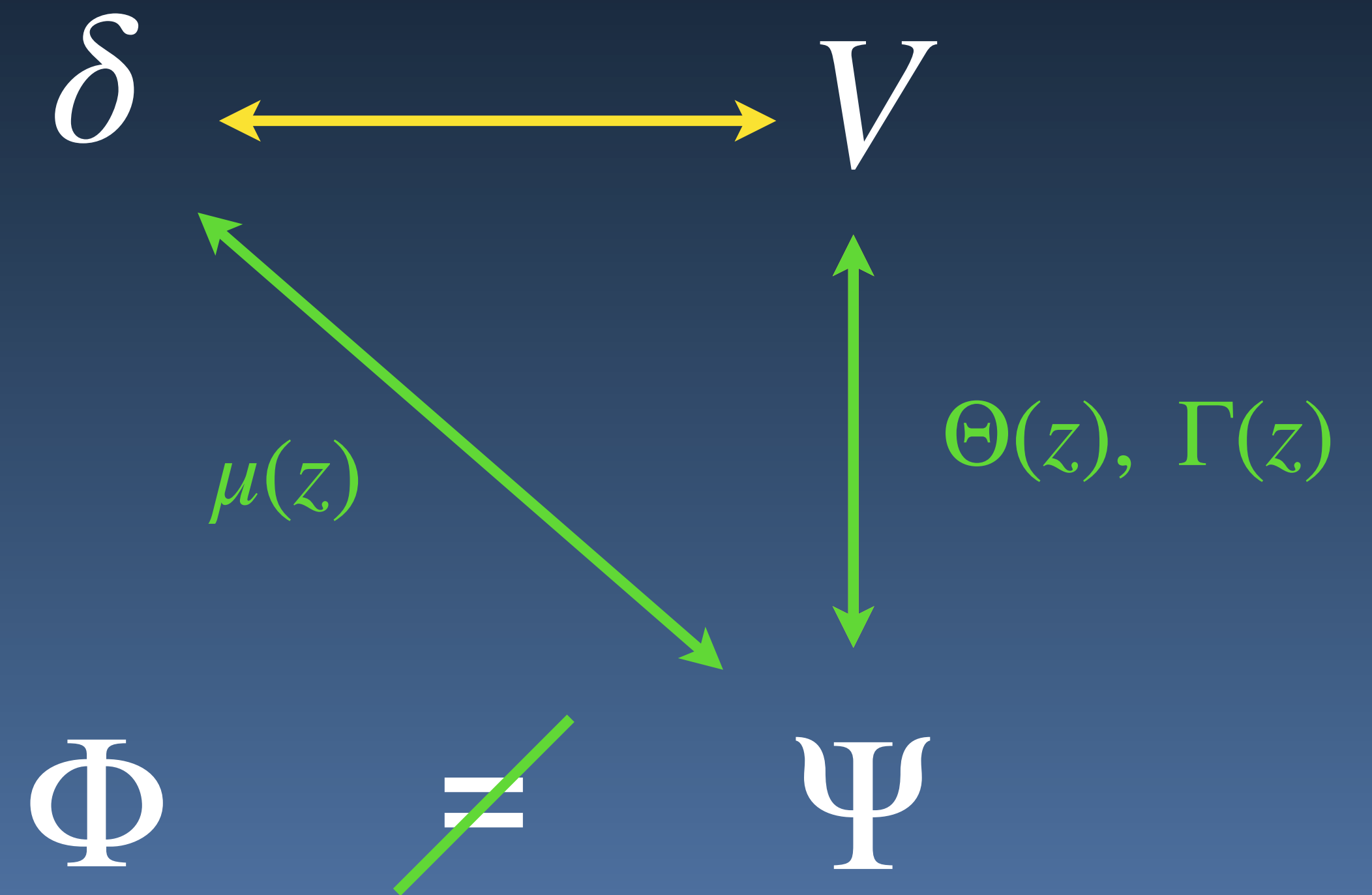
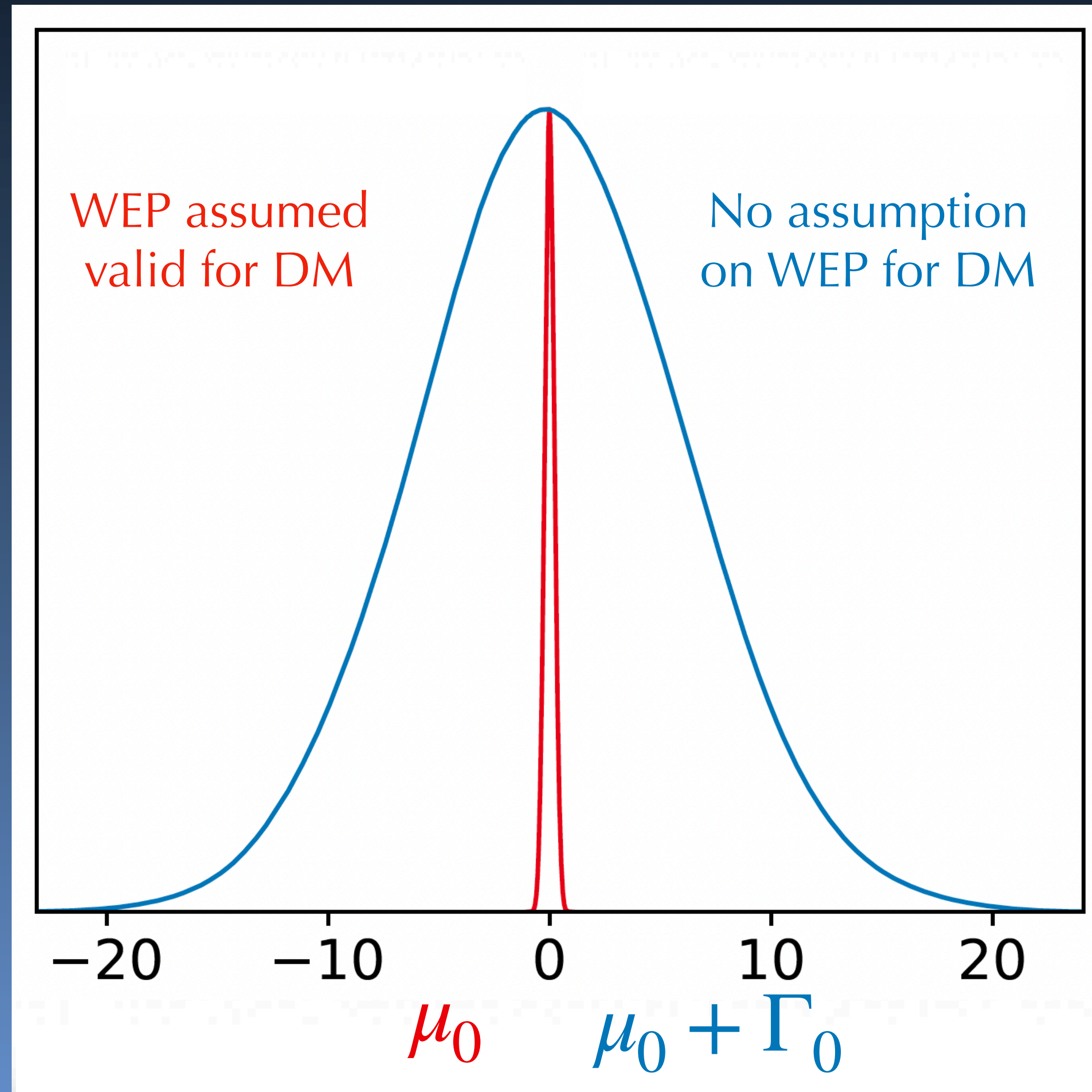
Constraints from SDSS data

SC, Grimm and Bonvin (2022)



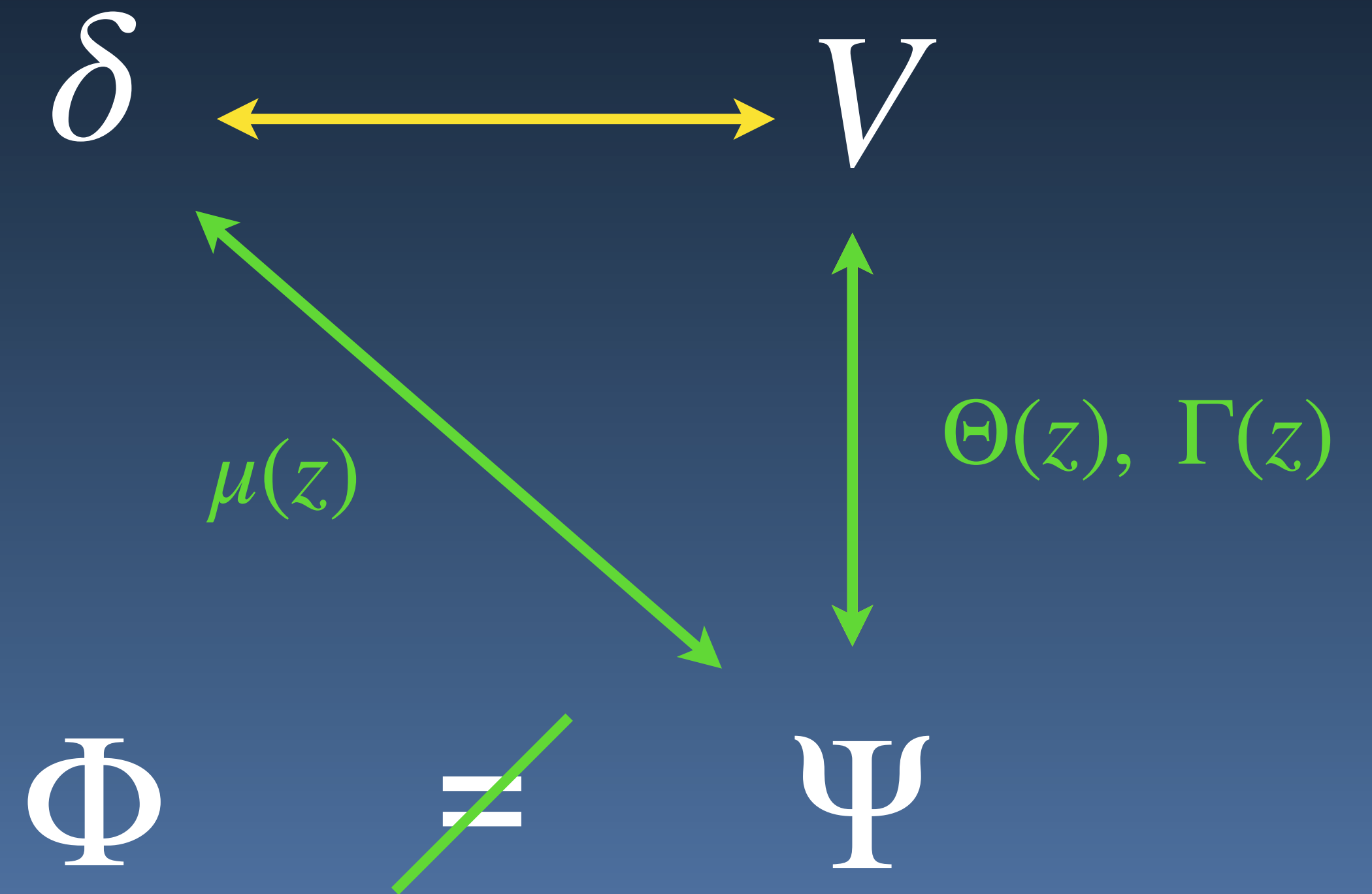
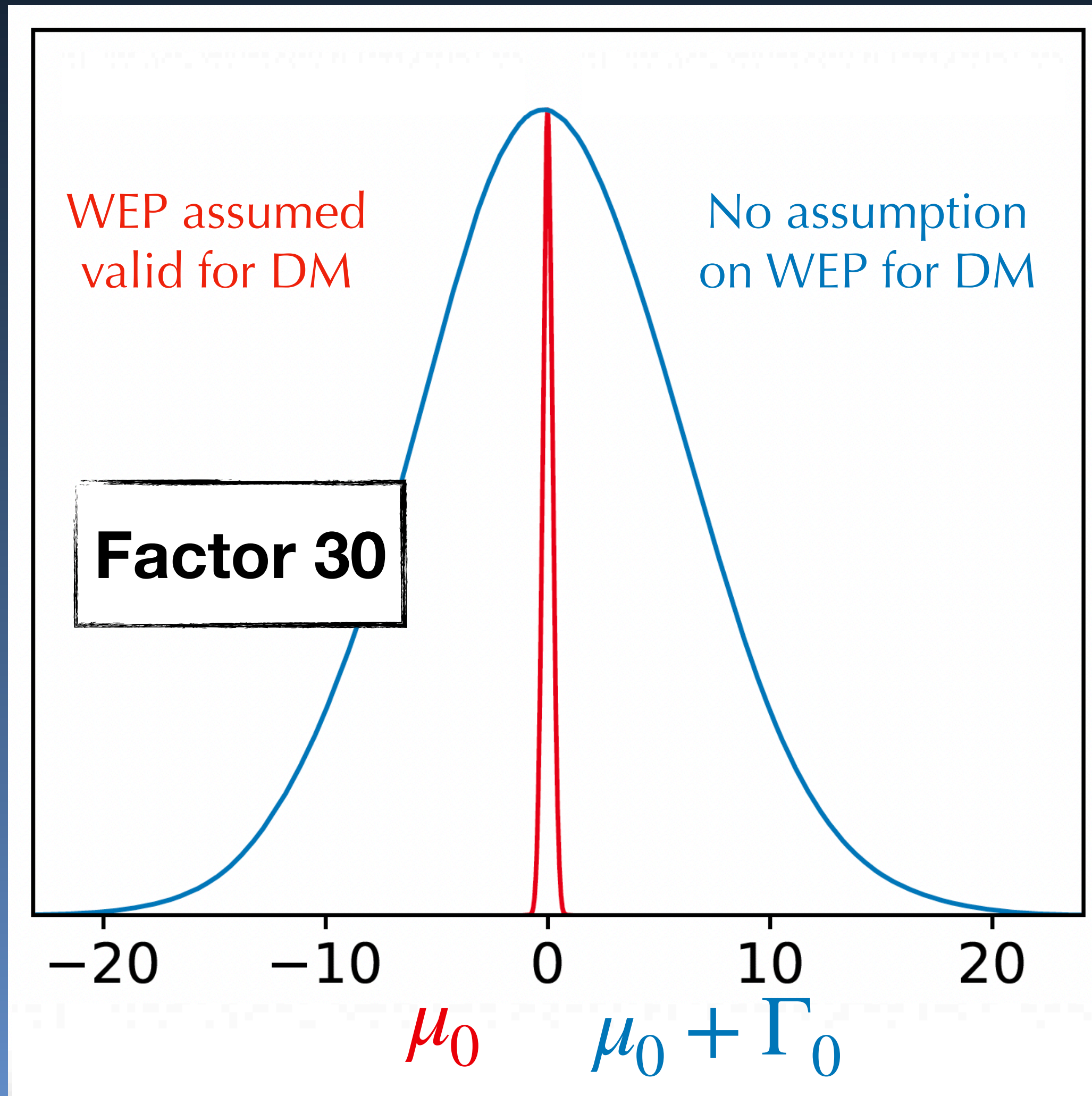
Constraints from SDSS data

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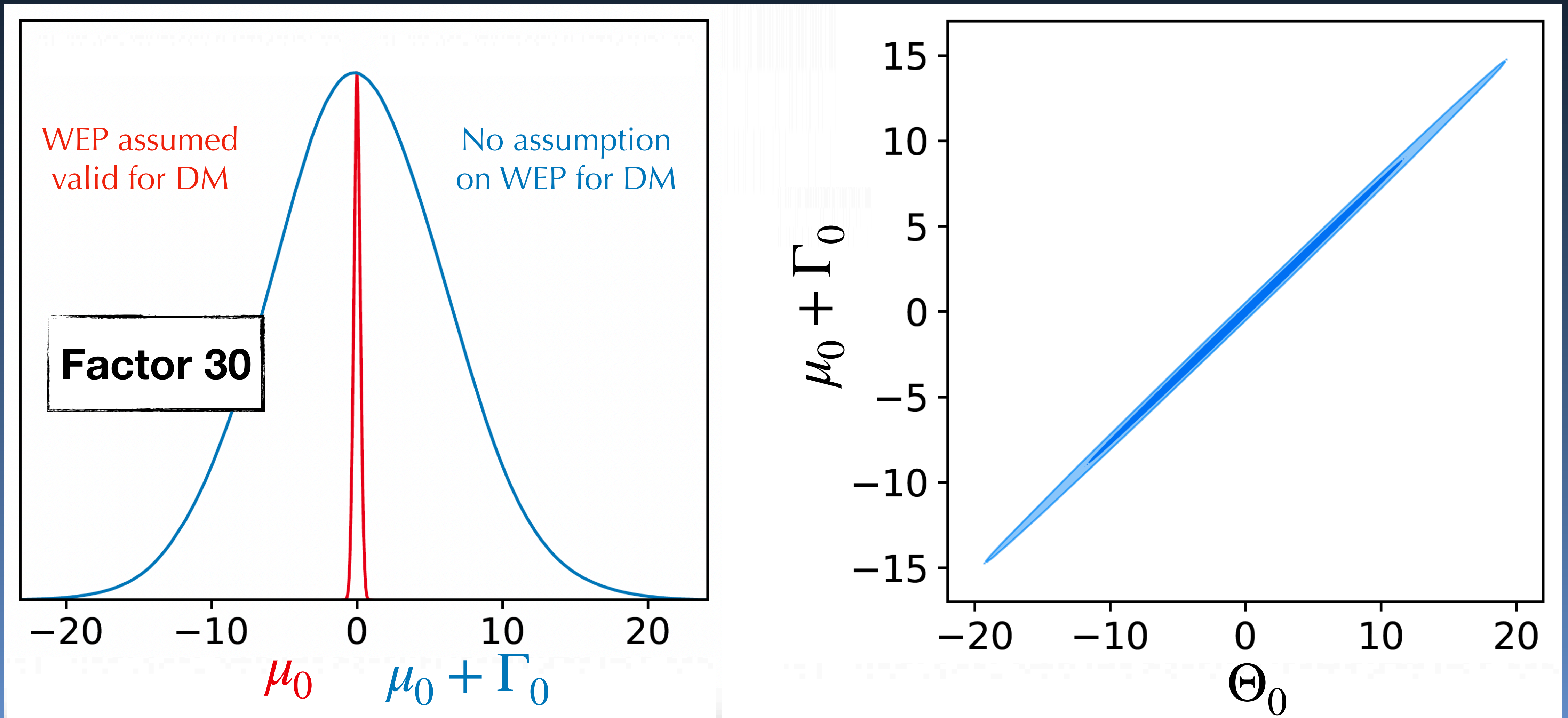
Constraints from SDSS data

SC, Grimm and Bonvin (2022)



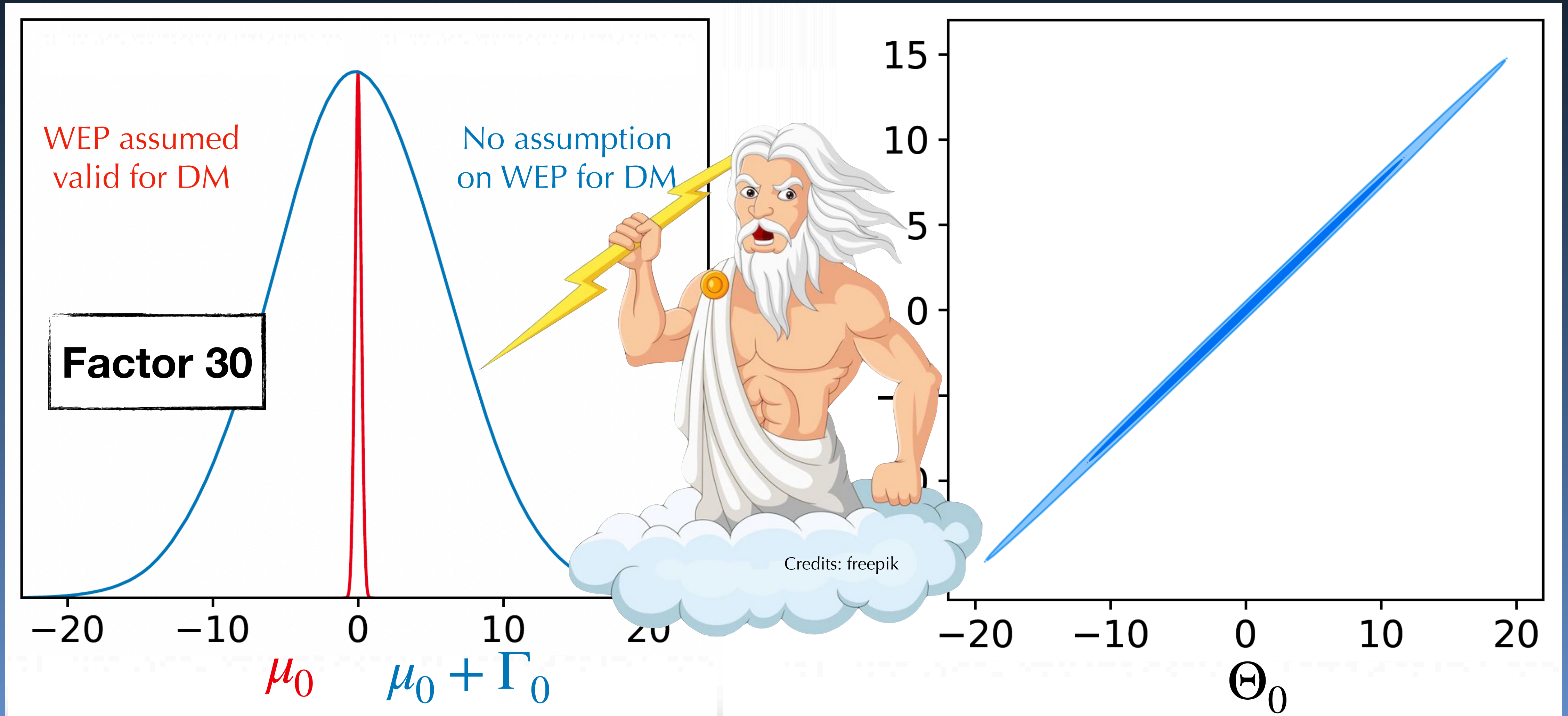
Constraints from SDSS data

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Constraints from SDSS data

SC, Grimm and Bonvin (2022)



Deus ex machina: gravitational redshift



Deus ex machina: gravitational redshift



$$\Delta_{\text{gr}} = \frac{1}{\mathcal{H}} \partial_r \Psi$$

McDonald (2009)

Yoo et al. (2012)

Bonvin, Hui and Gaztañaga (2014)

- Much smaller than RSD
- Observable by future surveys

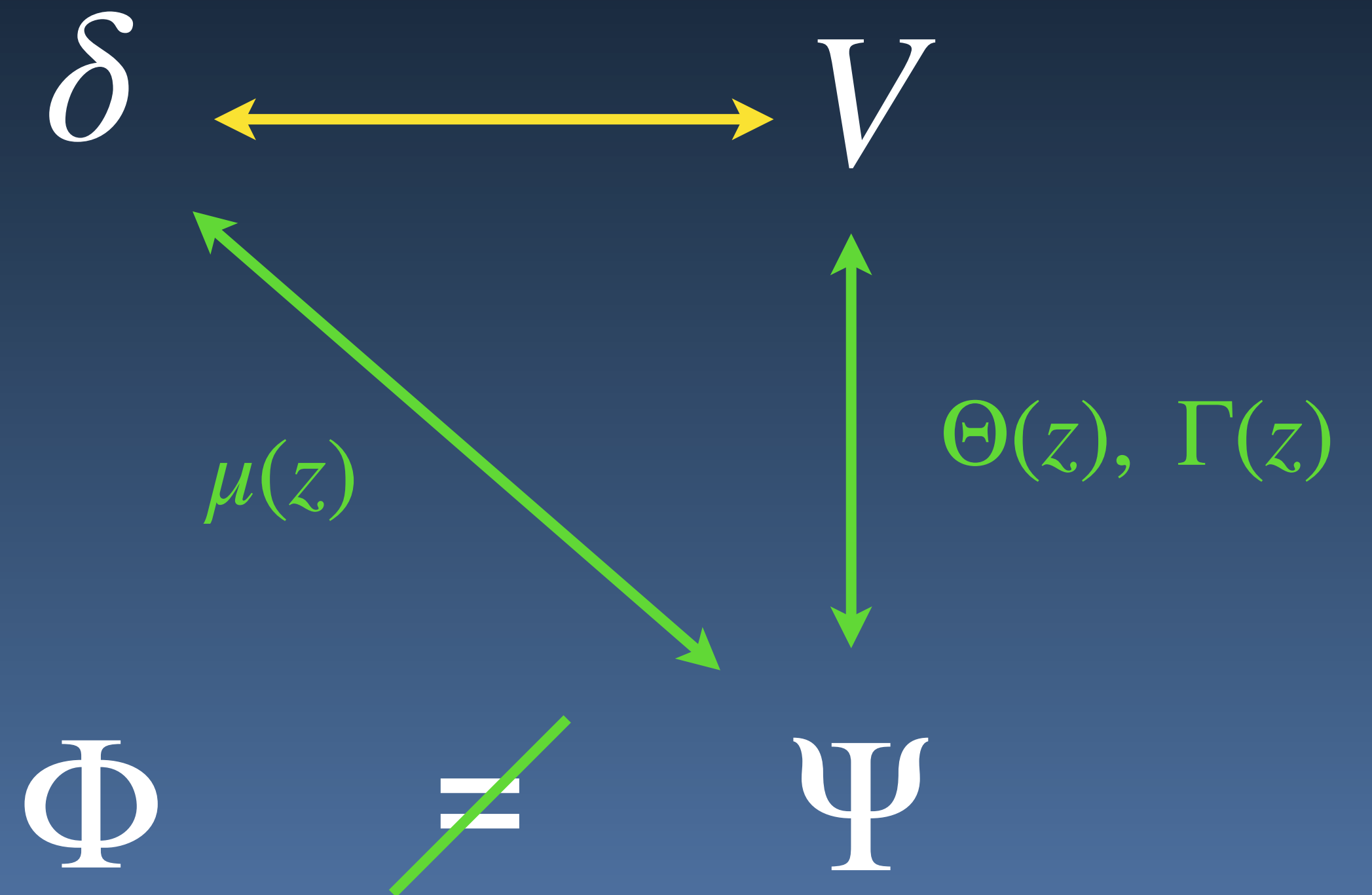
Deus ex machina: gravitational redshift



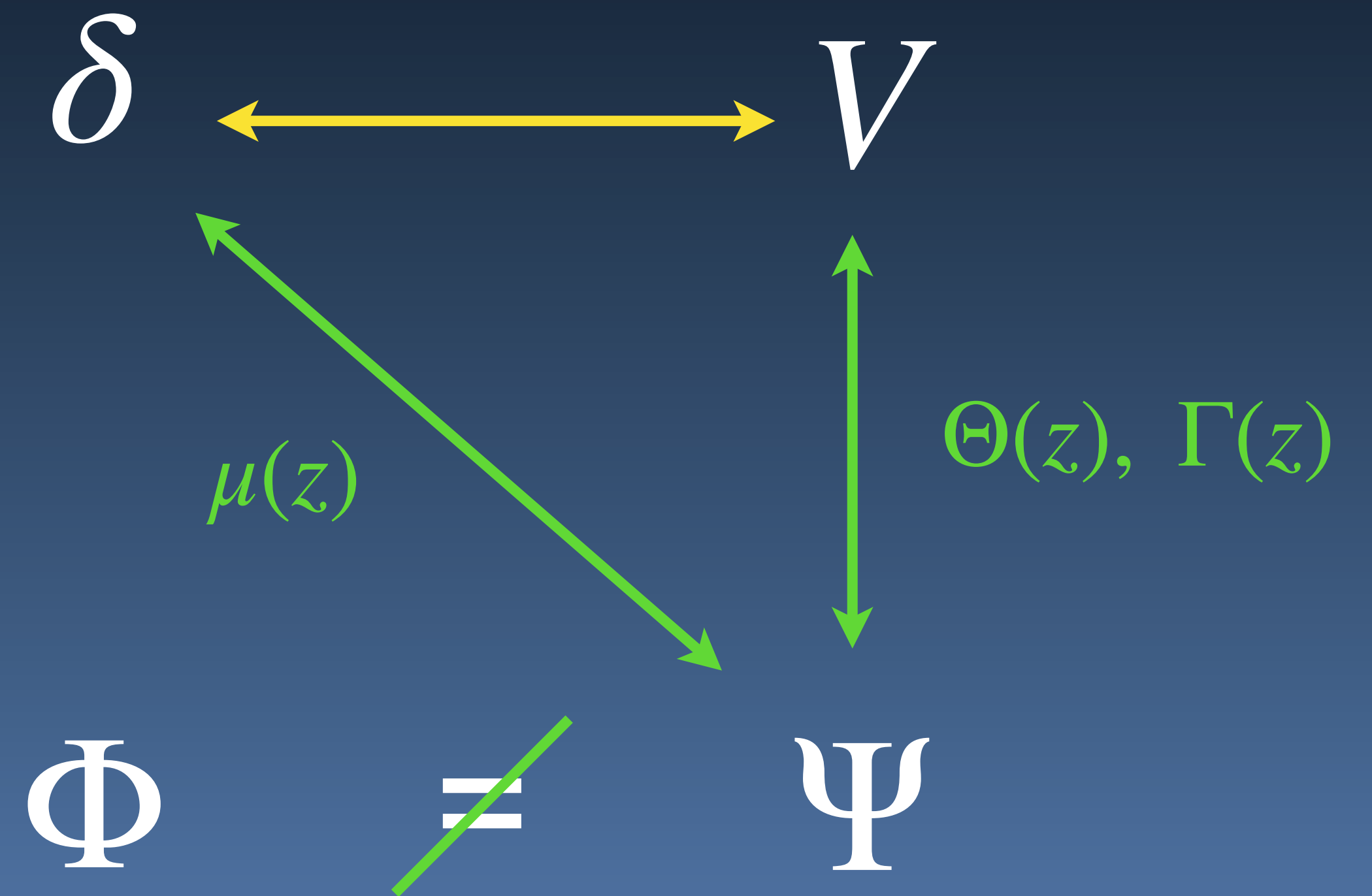
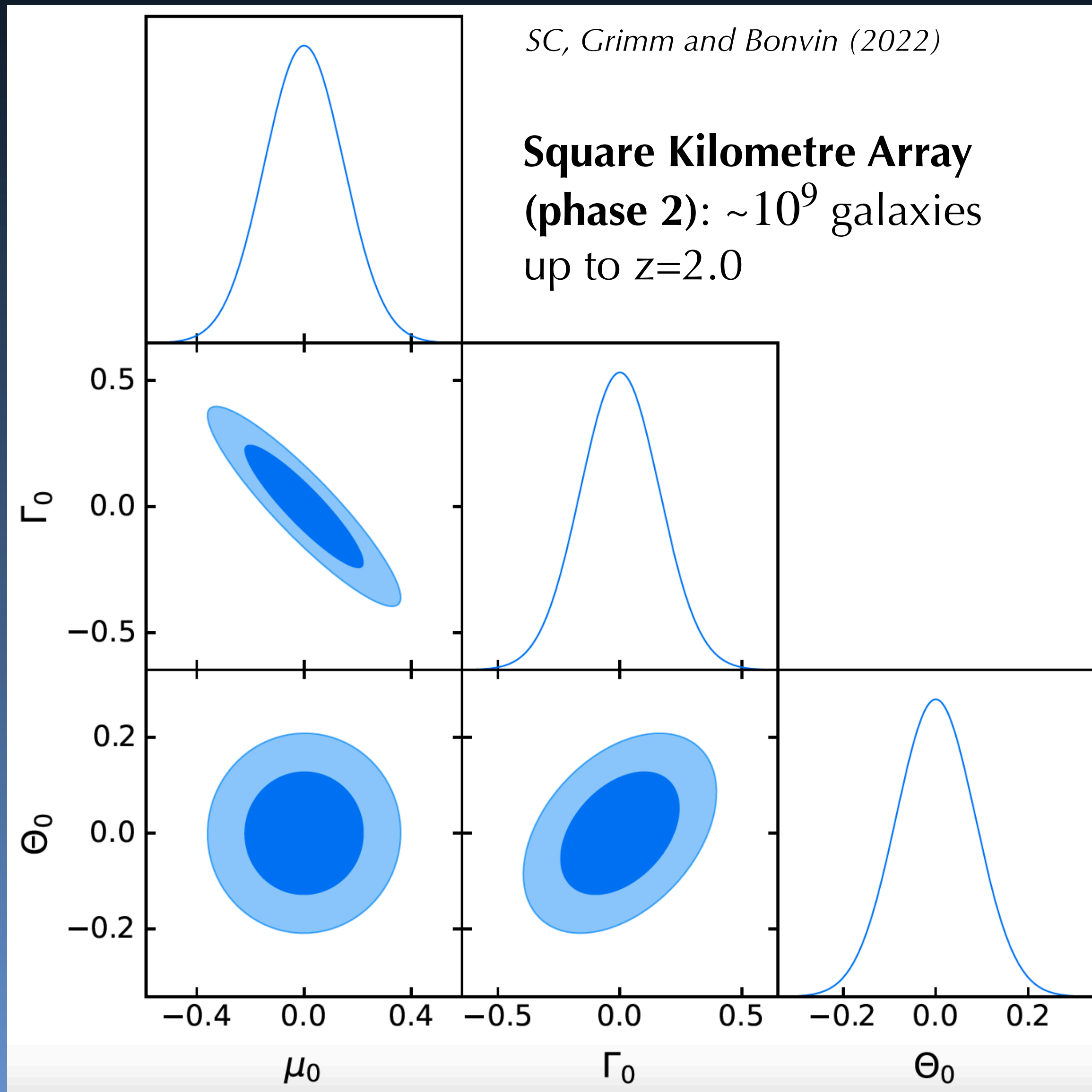
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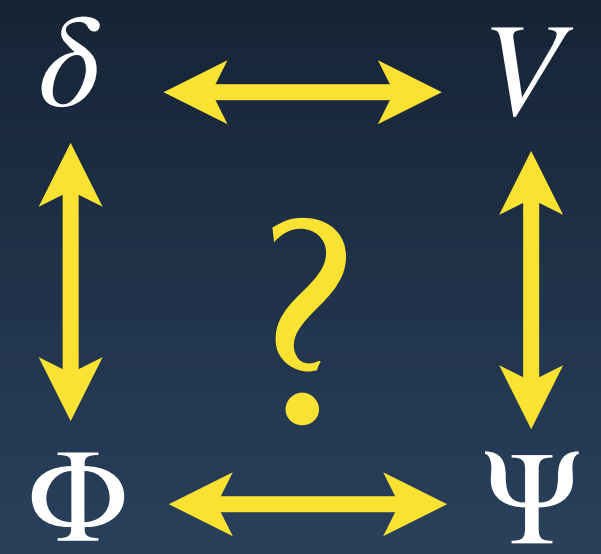
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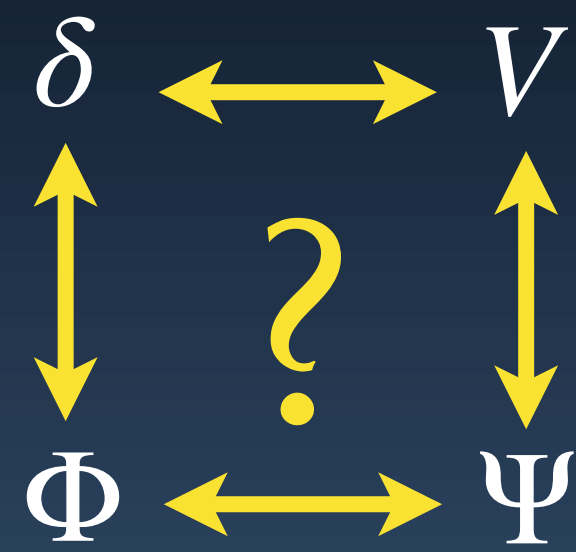
Deus ex machina: gravitational redshift



Two approaches to test modified gravity



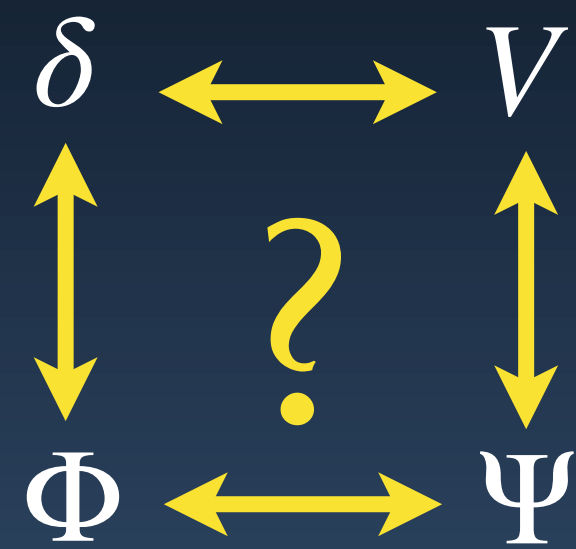
Two approaches to test modified gravity



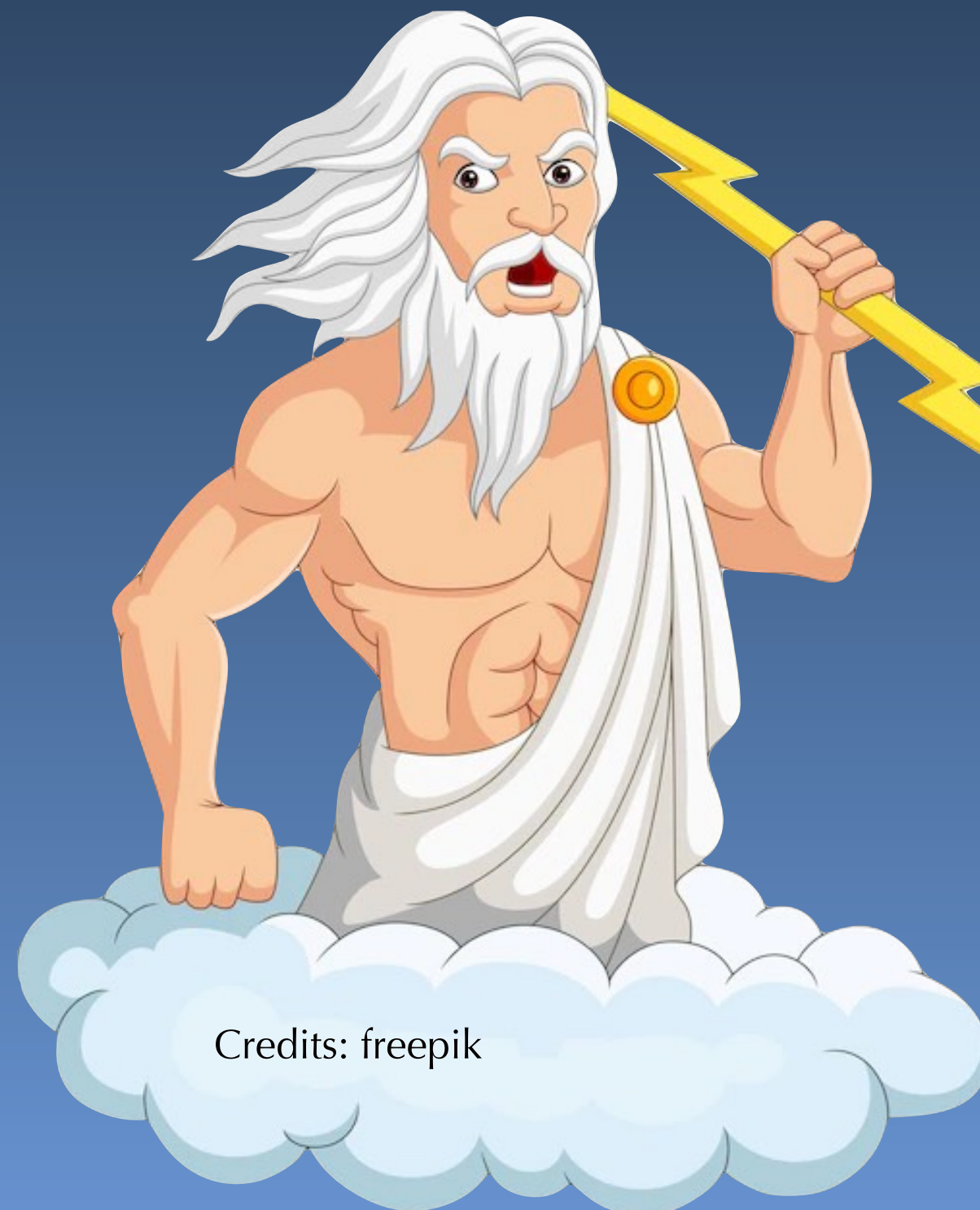
VS



Two approaches to test modified gravity



VS



What happens if we start from a Lagrangian?

Effective theory of interacting dark energy

Gleyzes et al. (2015)

Gleyzes et al. (2016)



\mathcal{L}

Effective theory of interacting dark energy

Gleyzes et al. (2015)

Gleyzes et al. (2016)



\mathcal{L}

Gravitational sector

Metric + scalar field *Bellini and Sawicki (2014)*

- α_K : Kinetic scalar term
- α_B : Scalar-tensor kinetic mixing
- α_M : Planck-mass run rate

Effective theory of interacting dark energy

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} Encompass all
Horndeski theories

Effective theory of interacting dark energy

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Matter sector

CDM coupled differently to the metric

⇒ Breaking of the WEP encoded in γ_c

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Gravitational sector

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Encompass all
Horndeski theories

Matter sector

CDM coupled differently to the metric

\Rightarrow Breaking of the WEP encoded in γ_c



Exact relations with μ, Θ, Γ

Forecasts for SKA2 in Λ CDM

SC, Mancarella, et al. (in preparation)

Gravity modifications

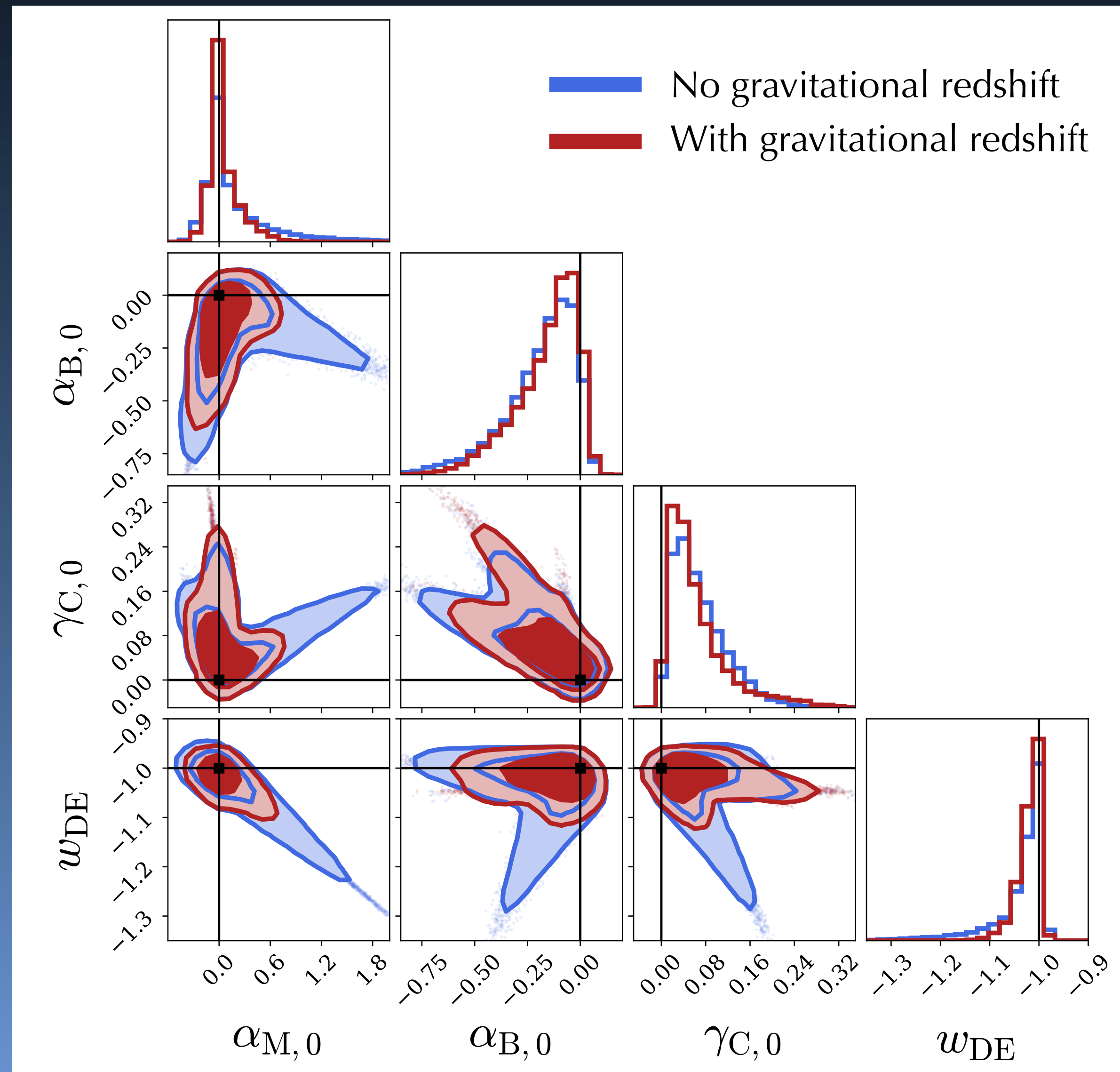
α_M, α_B

WEP breaking

γ_C

Modifications in DE background evolution

w_{DE}



Take-home messages

Standard constraints on modified gravity from galaxy number counts rely on the assumption that DM obeys the WEP.



Credits: freepik

Take-home messages

Standard constraints on modified gravity from galaxy number counts rely on the assumption that DM obeys the WEP.

Dropping this restrictive assumption leads to modifications that are fully degenerate with deviations from the Poisson equation.



Credits: freepik

Take-home messages

Standard constraints on modified gravity from galaxy number counts rely on the assumption that DM obeys the WEP.

Dropping this restrictive assumption leads to modifications that are fully degenerate with deviations from the Poisson equation.

Gravitational redshift, which will be observable by future surveys, can break this degeneracy and provide tight constraints!



Credits: freepik

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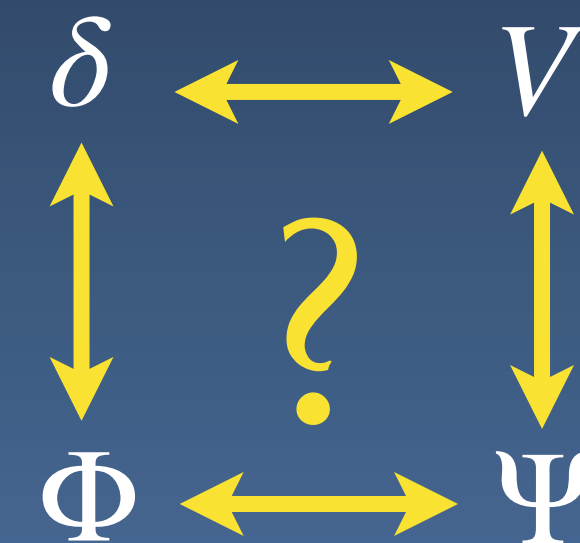
Additional slides

Two approaches to test modified gravity

Constrain the parameters in a specific model



Test the relations between the four fields describing the Universe



Direct link between theory and observations



Each model must be tested separately



Model-independent approach

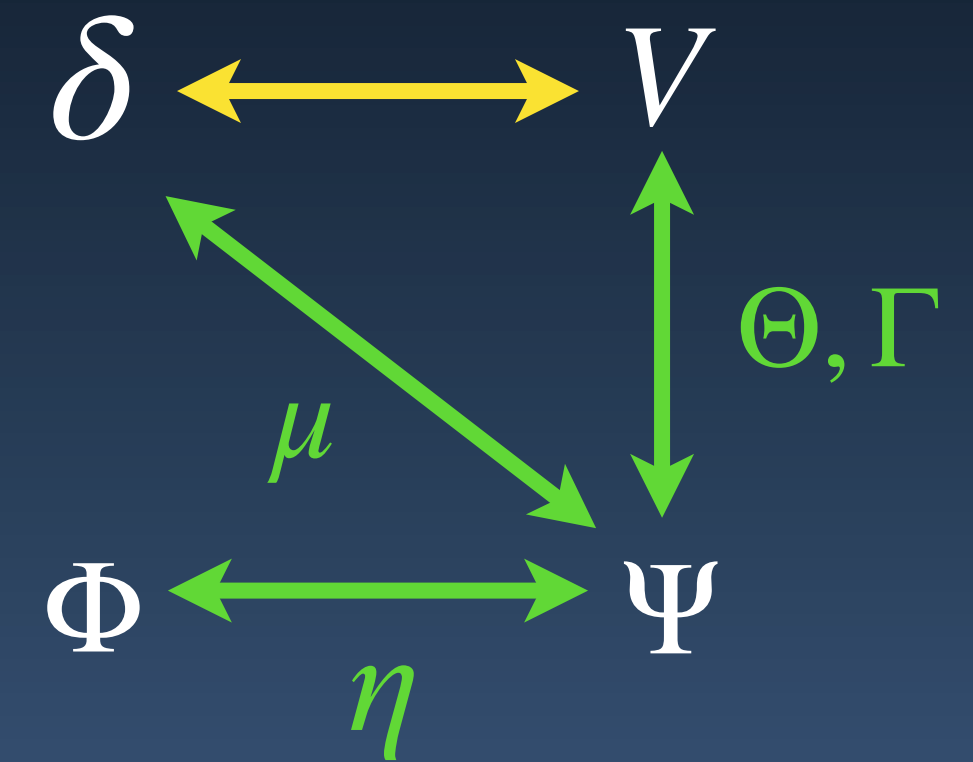


No clear relation to any model

Impact on the growth of cosmic structures

$$\delta'' + \left(1 + \frac{\mathcal{H}}{\mathcal{H}'} + \Theta \right) \delta' - \frac{3}{2} \frac{\Omega_{m,0}}{a} \left(\frac{\mathcal{H}_0}{\mathcal{H}} \right)^2 \mu (\Gamma + 1) \delta = 0$$

Assumption throughout	$\mu(z) = 1 + \mu_0 \Omega_{\Lambda}(z) / \Omega_{\Lambda,0}$ $\Theta(z) = \Theta_0 \Omega_{\Lambda}(z) / \Omega_{\Lambda,0}$ $\Gamma(z) = \Gamma_0 \Omega_{\Lambda}(z) / \Omega_{\Lambda,0}$
-----------------------	---



Enhancement of structure growth

1. Fifth force acting on DM ($\Gamma > 0$)
2. Increasing the depth of the gravitational potentials ($\mu > 1$)

} DEGENERACY

→ Impact on $f = \frac{d \ln \delta}{d \ln a}$ and σ_8

Two-point correlation function

Extract information through correlations:

$$\xi \equiv \langle \Delta(\mathbf{n}, z) \Delta(\mathbf{n}', z') \rangle$$

→ Expansion in Legendre polynomials:

With $\Delta = \delta + \text{RSD}$,

Kaiser (1987)
Hamilton (1992)

$$\xi = C_0(z, d) P_0(\cos \beta)$$

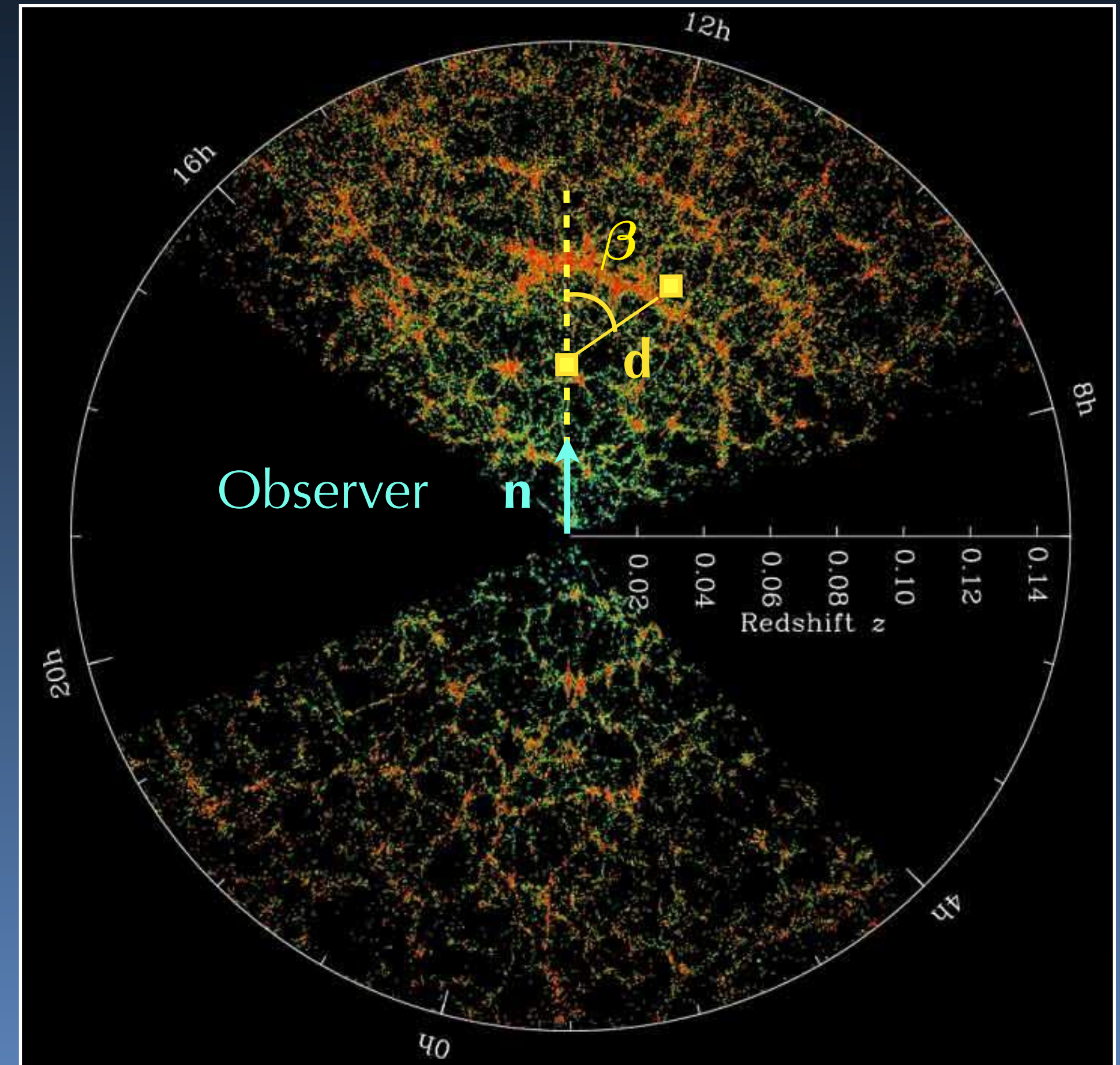
Monopole

$$+ C_2(z, d) P_2(\cos \beta)$$

Quadrupole

$$+ C_4(z, d) P_4(\cos \beta)$$

Hexadecapole



Credits: M.Blanton, SDSS

Relation with gravity modifications

Monopole

$$C_0(z, d) = \left[\tilde{b}^2(z) + \frac{2}{3} \tilde{b}(z) \tilde{f}(z) + \frac{1}{5} \tilde{f}^2(z) \right] \mu_0(z_*, d)$$

Quadrupole

$$C_2(z, d) = - \left[\frac{4}{3} \tilde{f}(z) \tilde{b}(z) + \frac{4}{7} \tilde{f}^2(z) \right] \mu_2(z_*, d)$$

Hexadecapole

$$C_4(z, d) = \frac{8}{35} \tilde{f}^2(z) \mu_4(z_*, d)$$

→ $\mu_l(z_*, d) = \int \frac{dk k^2}{2\pi^2} \frac{P_{\delta\delta}(k, z_*)}{\sigma_8^2(z_*)} j_l(kd)$ constrained by CMB

→ $\tilde{f}(z) = f(z) \sigma_8(z)$ and $\tilde{b}(z) = b(z) \sigma_8(z)$ measured Affected by gravity modifications

$$\delta'' + \left(1 + \frac{\mathcal{H}}{\mathcal{H}'} + \Theta \right) \delta' - \frac{3}{2} \frac{\Omega_{m,0}}{a} \left(\frac{\mathcal{H}_0}{\mathcal{H}} \right)^2 \mu (\Gamma + 1) \delta = 0$$

Deus ex machina: relativistic effects

Standard terms

Gravitational redshift

$$\Delta(\mathbf{n}, z) = b\delta - \frac{1}{\mathcal{H}}\partial_r(\mathbf{V} \cdot \mathbf{n}) + \frac{1}{\mathcal{H}}\partial_r\Psi + \frac{1}{\mathcal{H}}\dot{\mathbf{V}} \cdot \mathbf{n} + \mathbf{V} \cdot \mathbf{n}$$

$$+ \left(5s + \frac{5s - 2}{\mathcal{H}r} - \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} + f^{\text{evol}} \right) \mathbf{V} \cdot \mathbf{n}$$

Doppler terms



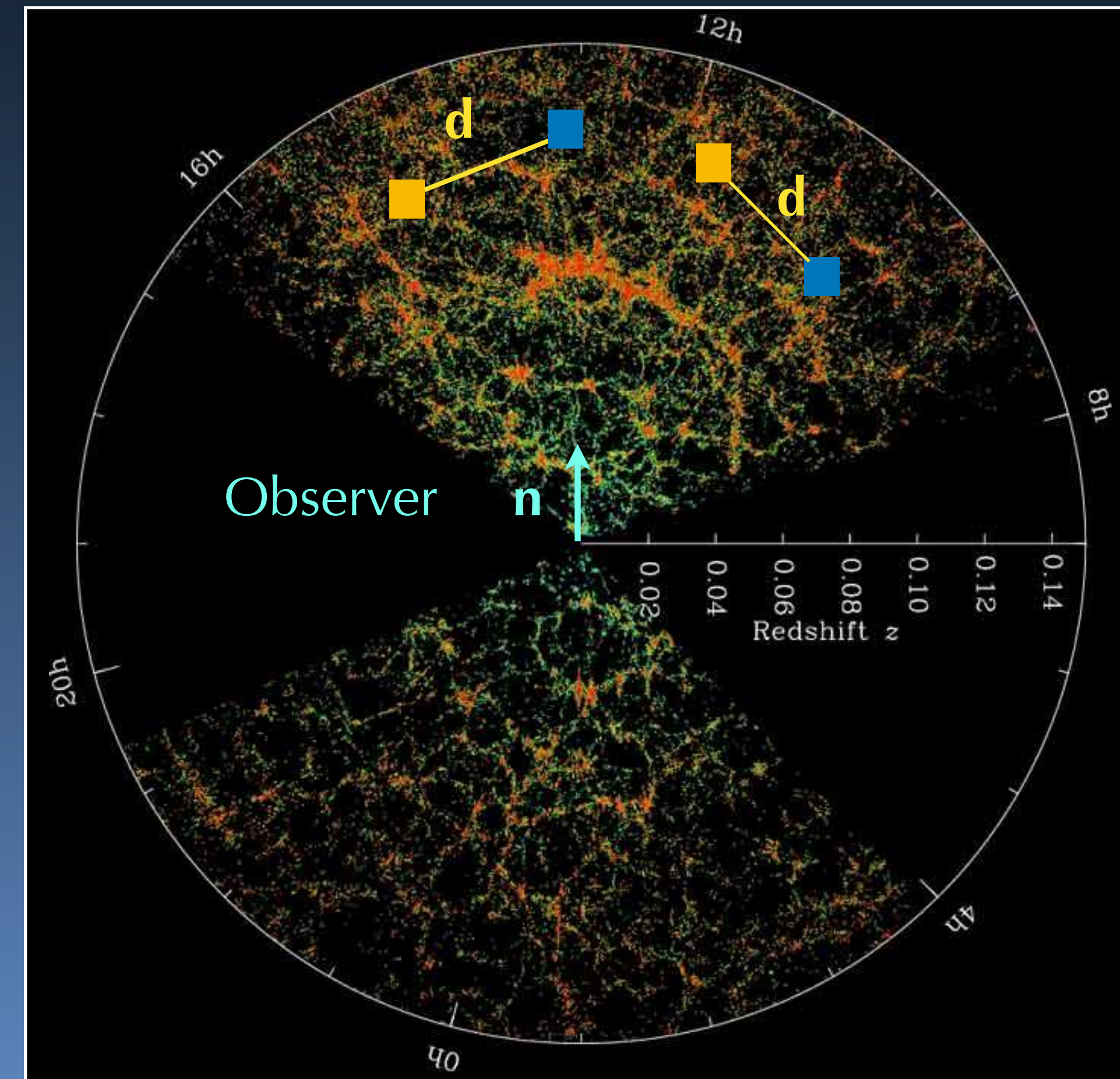
Extracting the signal from observations

Relativistic effects break the symmetry of ξ

Bonvin, Hui and Gaztanaga (2014)

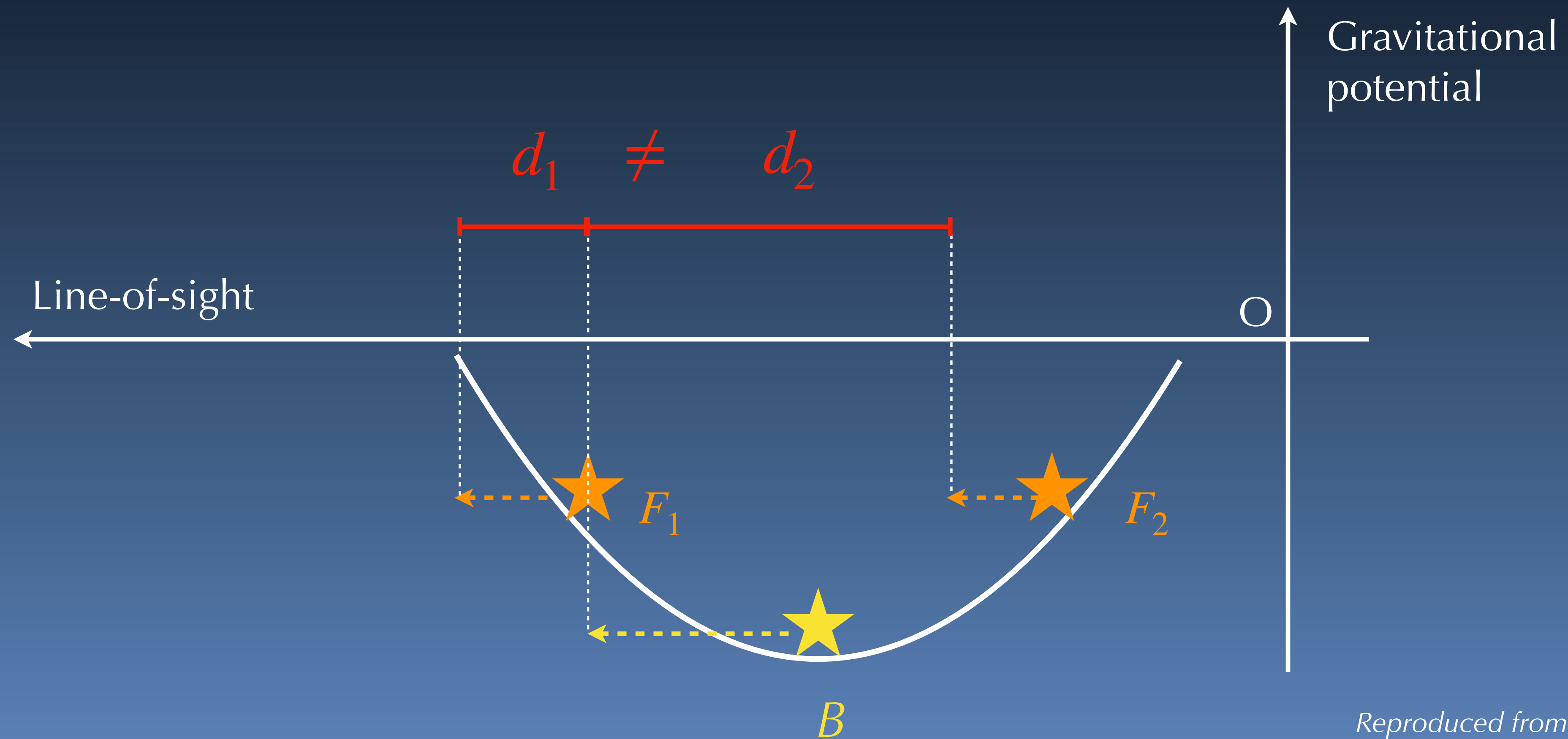
$$C_1(z, d) = \frac{\mathcal{H}}{\mathcal{H}_0} \nu_1(d, z_*) \left[5\tilde{f} \left(\tilde{b}_{BSF} - \tilde{b}_{FSB} \right) \left(1 - \frac{1}{r\mathcal{H}} \right) \right. \\ \left. - 3\tilde{f}^2 \Delta s \left(1 - \frac{1}{r\mathcal{H}} \right) + \tilde{f} \Delta \tilde{b} \left(\frac{2}{r\mathcal{H}} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} \right) \right. \\ \left. + \Delta \tilde{b} \left(\ominus \tilde{f} - \frac{3}{2} \frac{\Omega_{m,0}}{a} \frac{\mathcal{H}_0^2}{\mathcal{H}^2} \Gamma \mu \sigma_8 \right) \right] - \frac{2}{5} \Delta \tilde{b} \tilde{f} \frac{d}{r} \mu_2(d, z_*)$$

Compare $\mu(\Gamma + 1)$ term in the evolution equation



Credits: M.Blanton, SDSS

Symmetry breaking by gravitational redshift



*Reproduced from
Bonvin, Hui and Gaztañaga (2014)*

Survey specifications

	SDSS-IV	DESI	SKA2
σ_{μ_0} (restricted to WEP validity)	0.21	0.02	0.004
$\sigma_{\mu_0+\Gamma_0}$ (no assumption on WEP)	6.05	0.42	0.068

DESI (Bright Galaxy Sample):

- 10 million galaxies up to $z=0.5$.
- Galaxy bias: $b_{\text{BGS}}(z) = b_0 \delta(0)/\delta(z)$.
 $b_0 = 1.34$ (fiducial value)

SKA, phase 2:

- ~1 billion galaxies up to $z=2.0$.
- Galaxy bias: $b_{\text{SKA}}(z) = b_1 \exp(b_2 z)$.
 $b_1 = 0.554$, $b_2 = 0.783$ (fiducial value)

Fisher analysis:

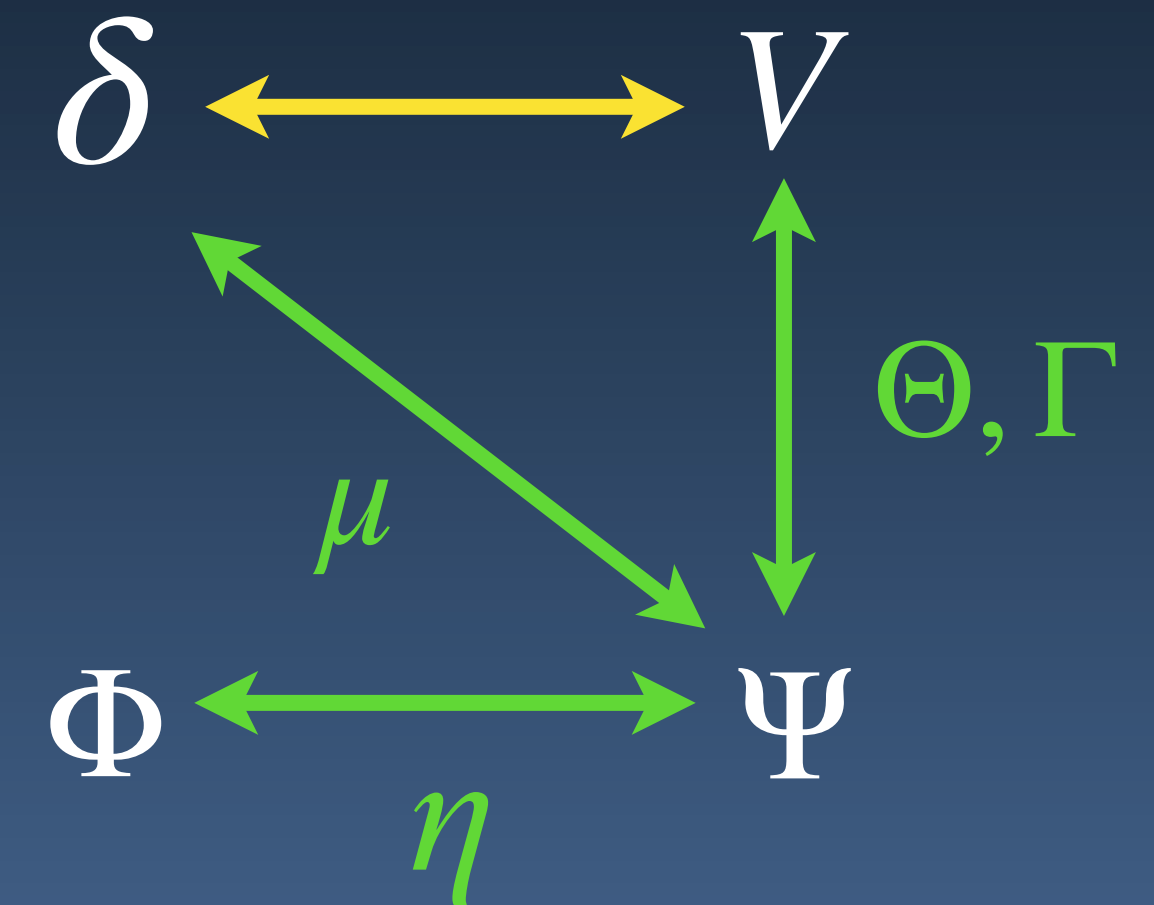
- minimum separation $d_{\text{min}} = 20 \text{ Mpc}/h$.
- include shot noise, cosmic variance, cross-correlations between different multipoles

Relations to μ, Θ, Γ

$$\mu = 1 + \frac{2}{c_s^2 \alpha} (\alpha_B - \alpha_M) (\alpha_B - \alpha_M + 3\gamma_c \omega_c b_c)$$

$$\Theta = 3\gamma_c$$

$$\Gamma = 3\gamma_c \frac{2}{c_s^2 \alpha} \frac{(\alpha_B - \alpha_M) + 3\gamma_c \omega_c b_c}{\mu}$$



α : total kinetic term of the scalar mode

c_s^2 : speed of propagation

In addition: modifications in the background evolution encoded in an effective w_{DE}