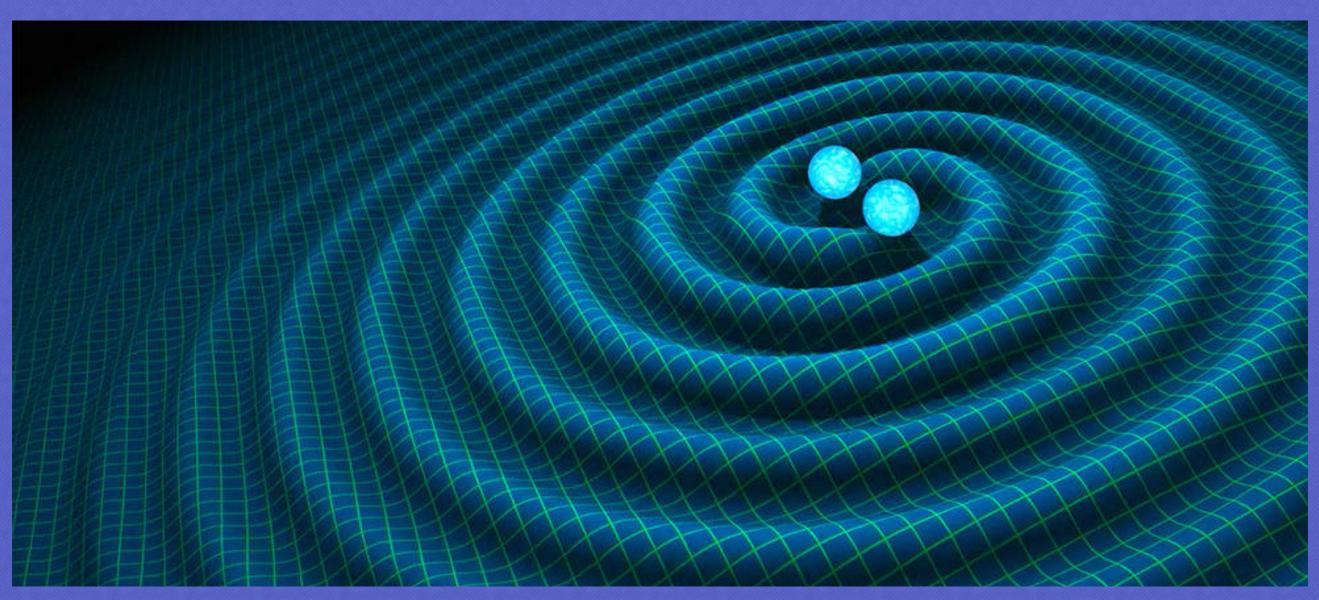
Multimessenger inference of neutron star equation of state and gravity



OKC@15, Stockholm

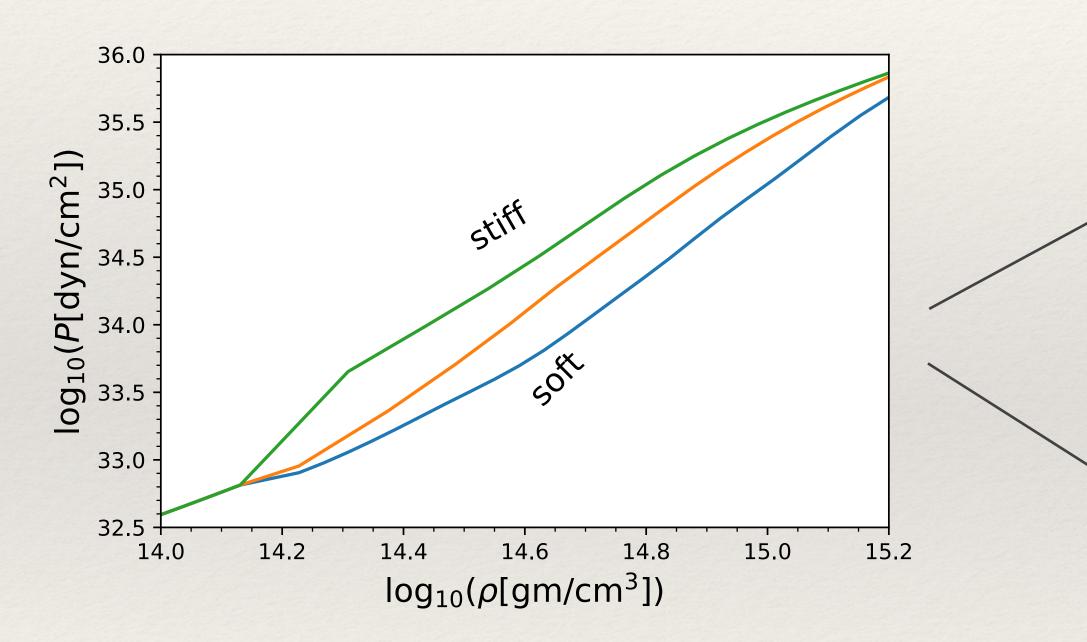
October 17, 2023

Bhaskar Biswas | Hamburg observatory

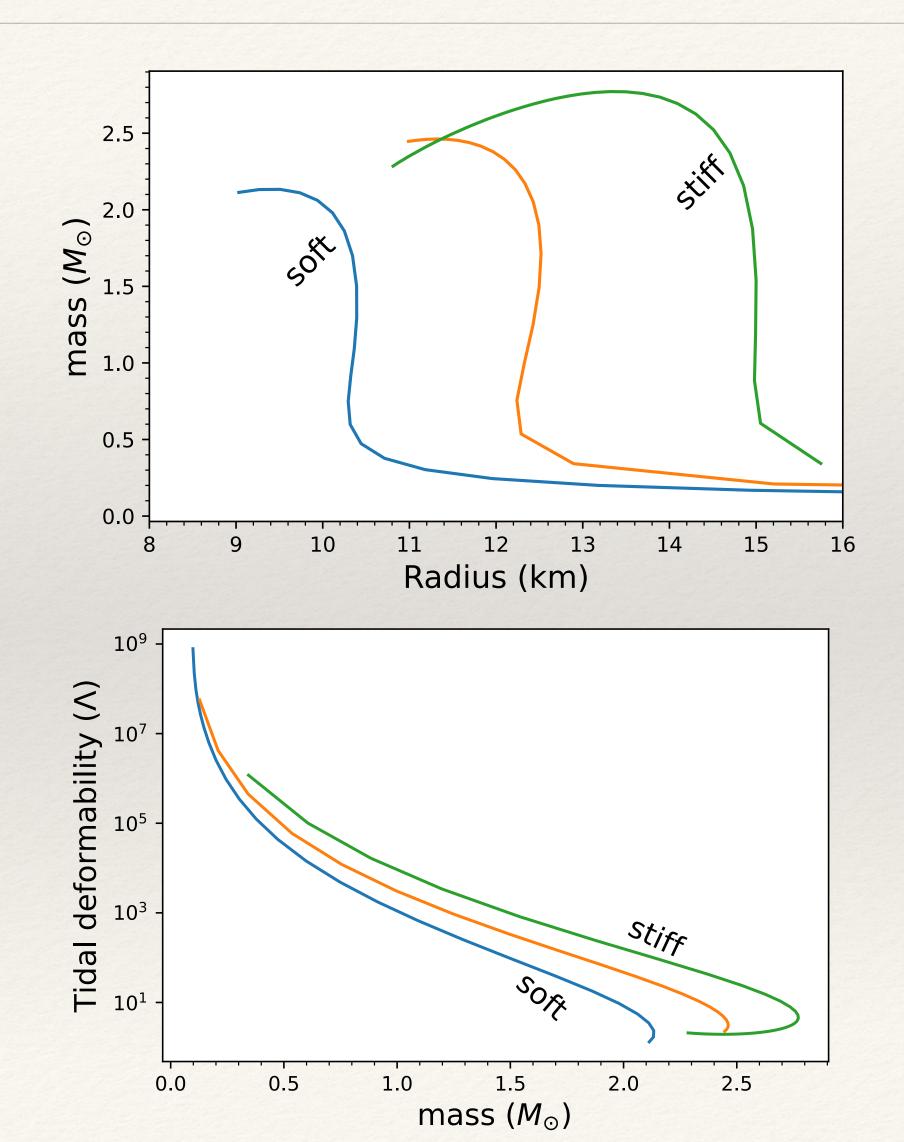


EOS & observables

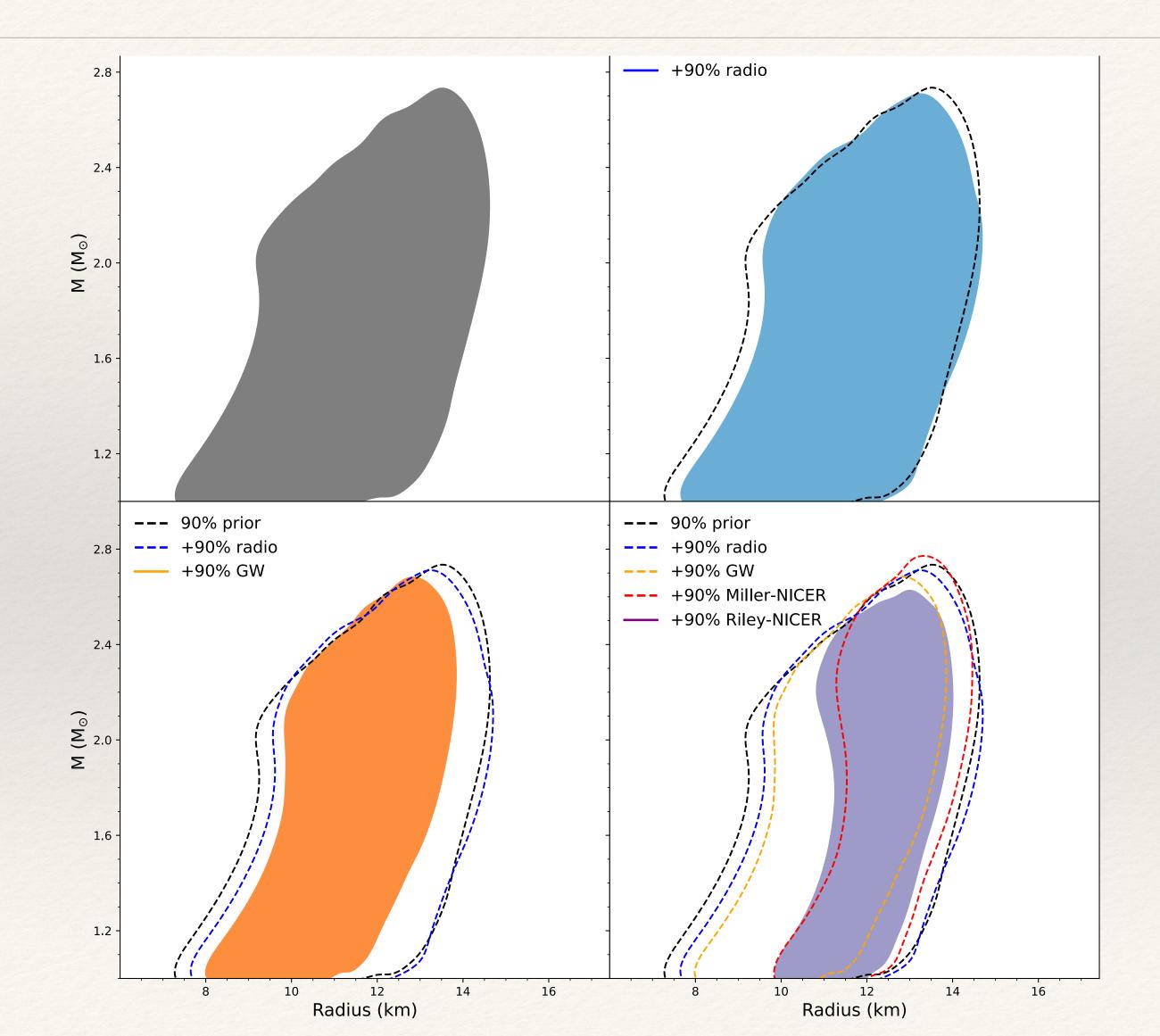




- * Radio observables M
- * X-ray observables M , R
- * GW observables M, Λ



Current mass-radius constraints



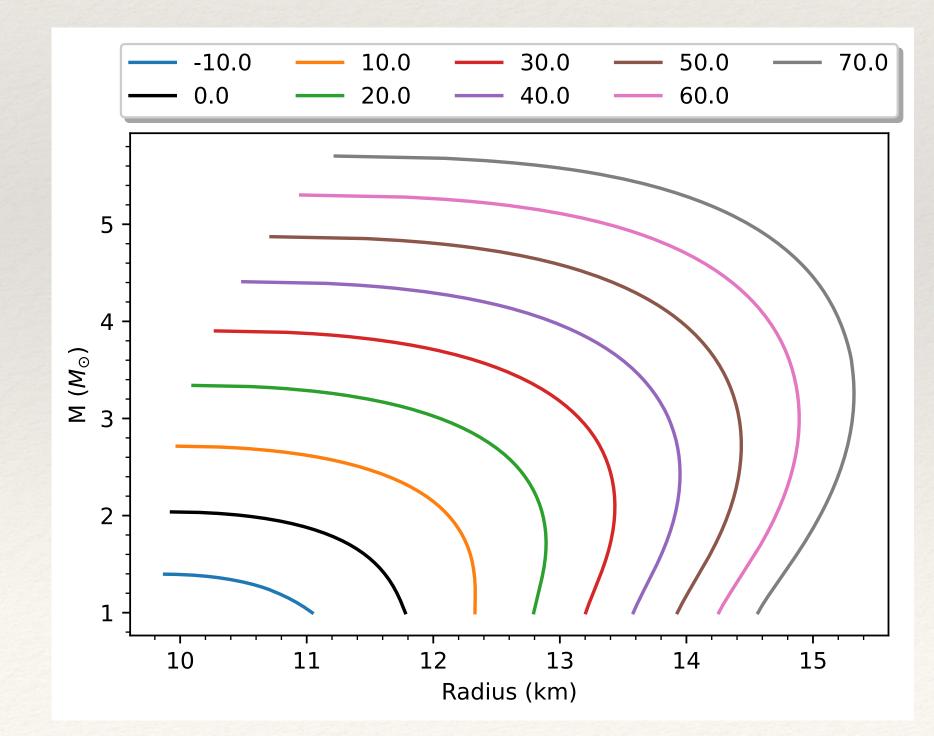
B. Biswas and S. Datta, PRD 2022



* We consider a particular 4D Horndeski scalar-tensor theory originating from higher-order EGB gravity with action

$$S = rac{1}{2\kappa} \int \mathrm{d}^4 x \sqrt{-g} \{R + lpha [\phi G$$

The coupling constant α has units of [km²].



EOS-gravity degeneracy

$\mathcal{G} + 4G_{\mu u} abla^{\mu} \phi abla^{ u} \phi - 4(abla \phi)^2 \Box \phi + 2(abla \phi)^4] \} + S_{ m m}$

* Where $\kappa = 8\pi G/c^4$, $\mathcal{G} = R^2 - 4R_{\mu\nu}R^{\mu\nu} + R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}$ is the Gauss-Bonnet scalar and S_m is the matter Lagrangian.

- * M-R sequences in 4D EGB gravity with varying couling constant α
- Similar effect to EOS with varying stiffness
- * a minimum black hole mass of $M = 5.7 \pm 1.8 M_{\odot}$ of GW200115, yields $\alpha = 285^{+207}_{-171}$ [km²].

Charmousis, Lehébel, Smyrniotis & Stergioulas, JCAP 2, 33 (2022)



Hierarchical Bayesian statistics

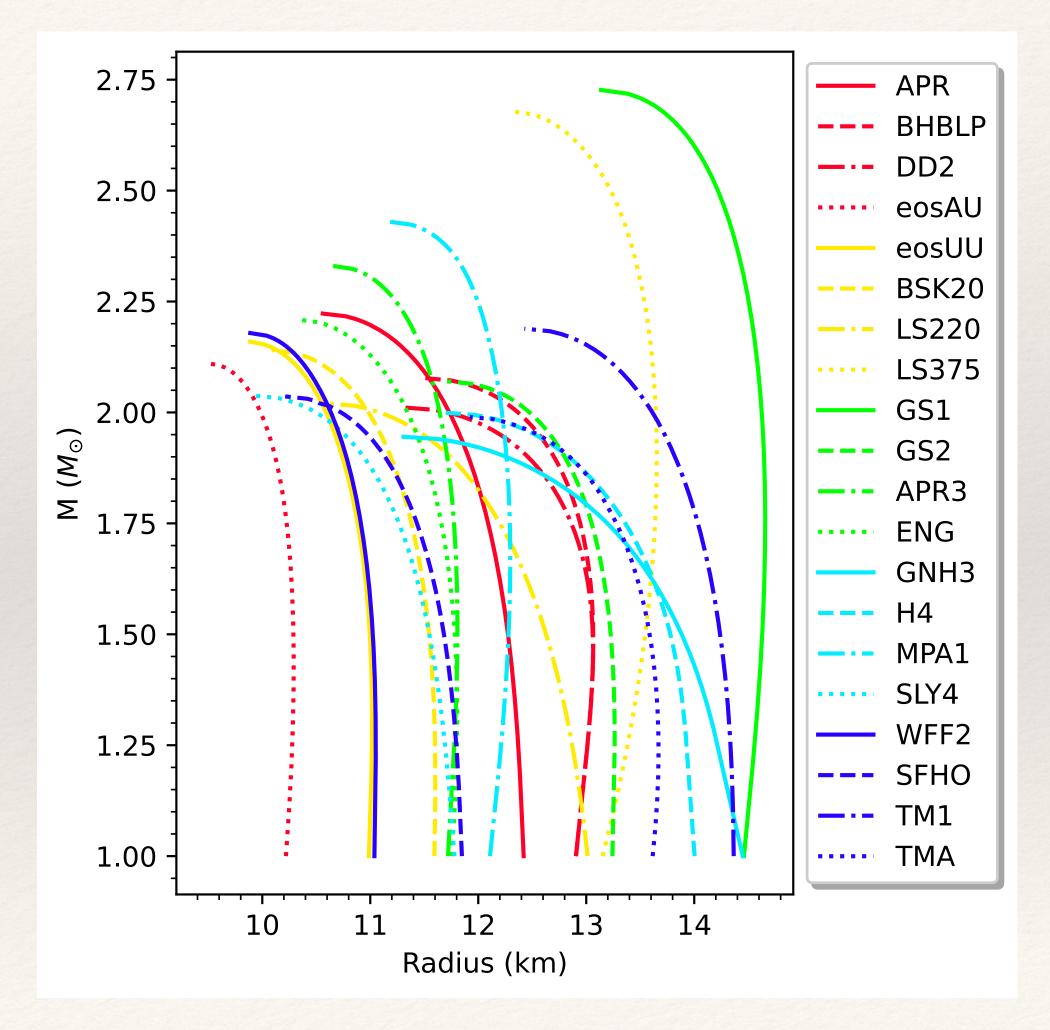
* $P(\theta \mid d) \propto P(\theta) \prod_i P(d_i \mid \theta)$,

 $\theta \in (EOS, \alpha, population parameters)$

* We have 20 EOSs; each EOSs are assigned with an integer index. A uniform prior on EOS_index is considered between 1 and 20.

- * Uniform prior on $\alpha \in (-10,70) \, \mathrm{km}^2$.
- * Population parameters: kept fixed for this work.

Methodology & EOS catalogues



Constraints using current observations

* We consider three models of NS mass distribution:

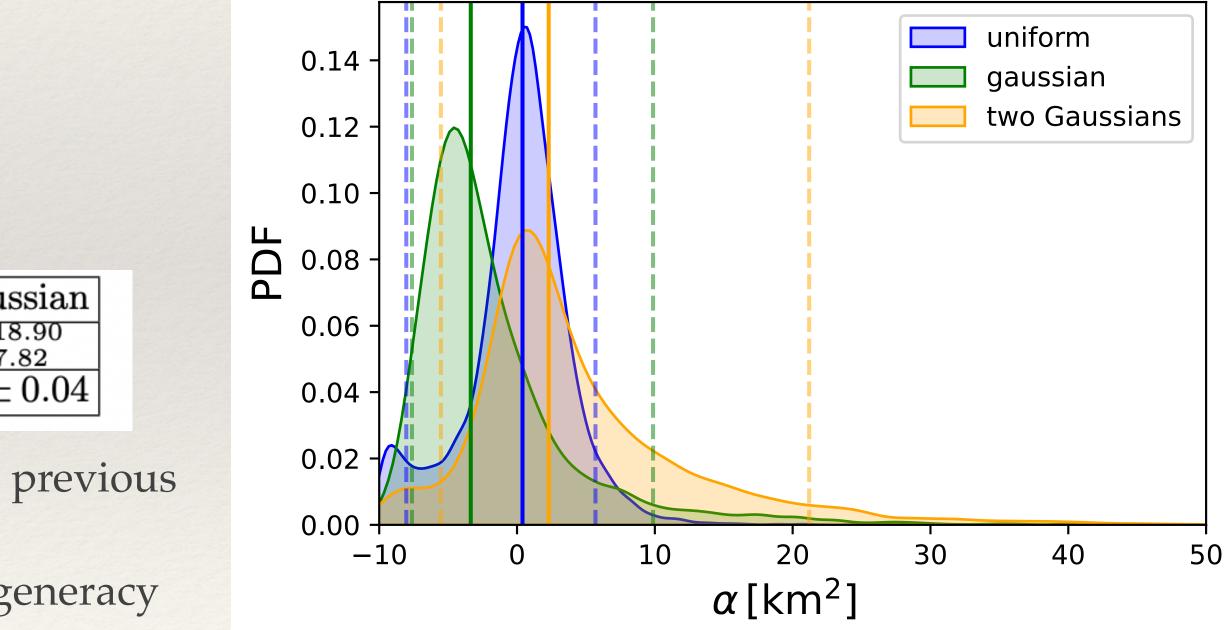
$$p_{\mathrm{U}}(m \mid m_{\mathrm{min}} = 1, m_{\mathrm{max}}) := U(m \mid m_{\mathrm{min}}, m_{\mathrm{max}})
onumber \ p_{\mathrm{N}}(m \mid \mu, \sigma, m_{\mathrm{min}}, m_{\mathrm{max}}) := \mathcal{N}(m \mid \mu, \sigma)U(m \mid m_{\mathrm{min}}, m_{\mathrm{max}})/A
onumber \ p_{\mathrm{NN}}ig(m \mid \mu, \sigma, \mu', \sigma', w, m_{\mathrm{min}}, m_{\mathrm{max}}ig) := ig[w\mathcal{N}(m \mid \mu, \sigma)/B + (1 - w)\mathcal{N}ig(m \mid \mu', \sigma'ig)/Cig]U(m \mid m_{\mathrm{min}}, m_{\mathrm{max}})$$

Datasets used

GWs : GW170817, GW190425 Xrays : PSR J0451, PSR J0740

| Quantity | uniform | Gaussian | two gaus |
|-------------------------------------|------------------------------|--------------------------|-------------------|
| $90\%{ m CI}{ m of}lpha[{ m km}^2]$ | $0.40\substack{+5.29\-8.43}$ | $-3.36^{+13.22}_{-4.27}$ | 2.30^{+18}_{-7} |
| $\log_{10} Z$ | -10.82 ± 0.02 | -31.90 ± 0.02 | $-9.25 \pm$ |

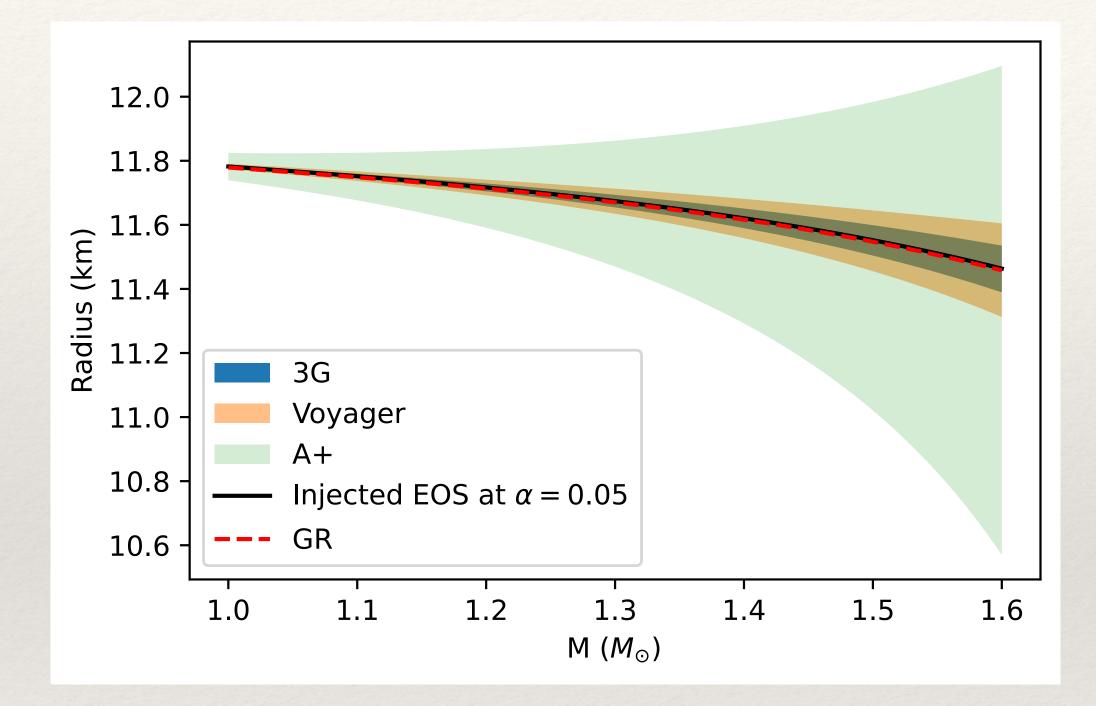
- * Posterior of α is consistent with GR and improves previous constraints.
- * Need more observations to break EOS-gravity degeneracy



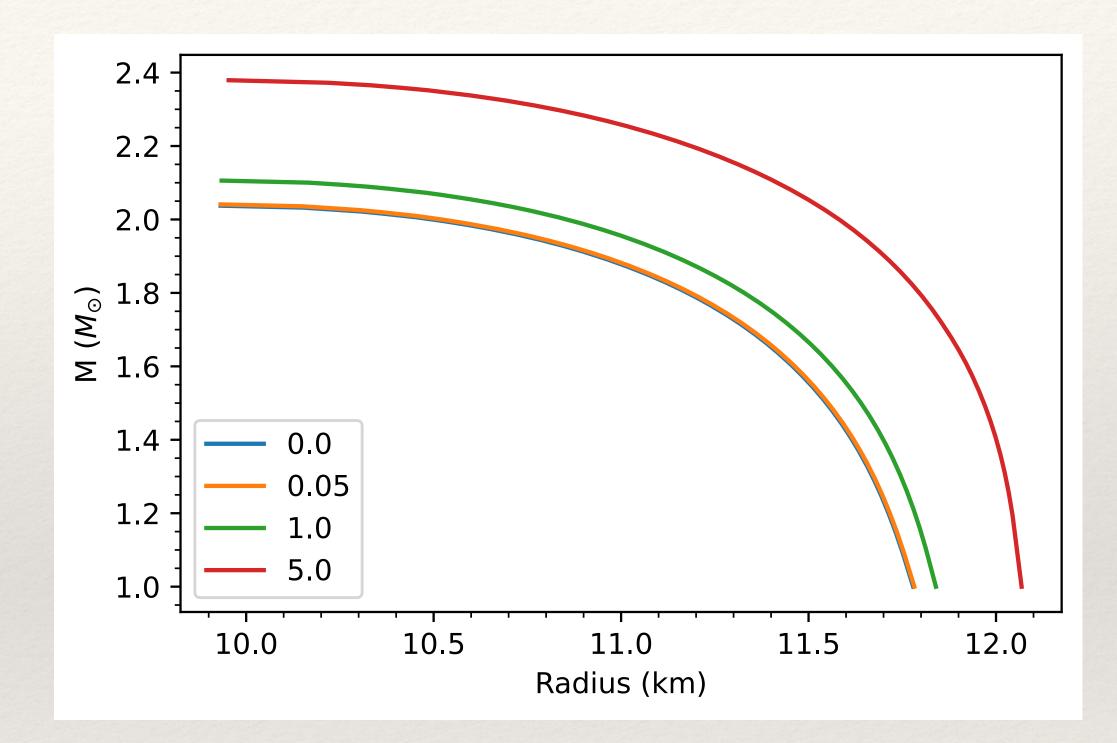
B. Biswas, E. Smyrniotis, I. Liodis, and N. Stergioulas, arXiv: 2309.05420 (2023)



Expected NS radius constraints with future GW detectors



Based on the calculations done by K. Chatziioannou, Phys. Rev. D. 105, 084021 (2022)



Mass vs. radius sequences for the different injected values of α (the GR case corresponds to $\alpha = 0$).

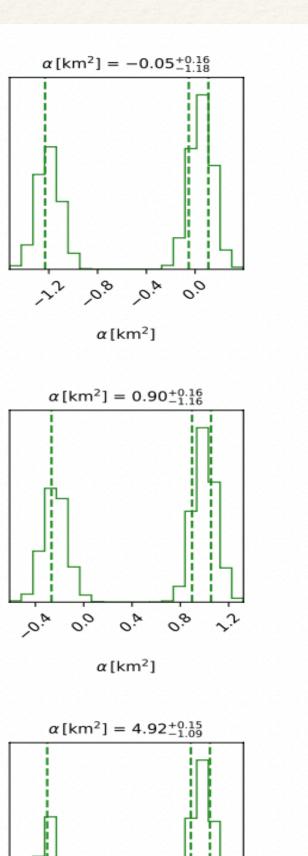


Constraints with future GW detectors

 α [km²]

+5

A+



3.0

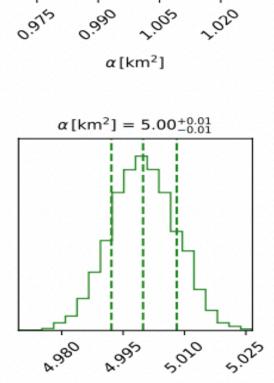
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D.D

 α [km²]

28

52



Voyager

 α [km²] = 0.05^{+0.01}_{-0.01}

0.045

 α [km²]

 α [km²] = 1.00^{+0.01}_{-0.01}

0.030

0,060

0.015

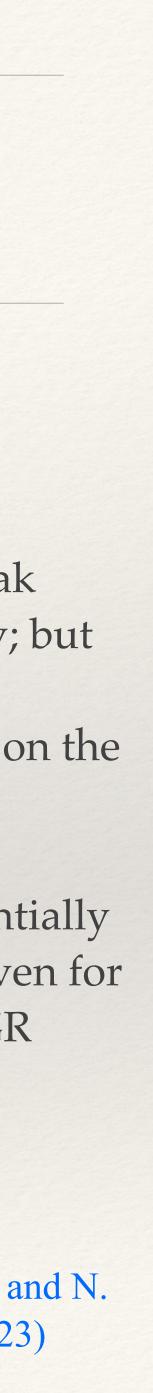


Injected value of 3G coupling constant α [km²] = 0.05^{+0.00}_{-0.00} $\alpha = 0.05$ 0.0500 0.0505 0.0495 0.0510 α [km²] α [km²] = 1.00^{+0.00}_{-0.00} $\alpha = 1$ 0.995 2.000 2.005 0.990 2.020 α [km²] α [km²] = 5.00^{+0.00}_{-0.00} $\alpha = 5$ 0.0008 ,0000A 0.000 0,0004 0,0001

 A+ does not strictly break
 EOS-gravity degeneracy; but can place constraints or disfavor GR depending on the value of α

 Voyager or 3G can potentially break the degeneracy, even for small deviations from GR

B. Biswas, E. Smyrniotis, I. Liodis, and N. Stergioulas, arXiv: 2309.05420 (2023)



EOS-gravity degeneracy: future directions

Following improvements needs to be made in the future

NS EOS will be used

needs to be performed for future detectors.

- *Instead of using a finite number of EOS candidates, a parametrization of

*Instead of using an expected radius uncertainty, a proper injection study