# <span id="page-0-0"></span>Oscar Klein Centre, Stockholm U., 2023

Can we explain cosmic birefringence without a new [light field beyond](#page-25-0) Standard Model?

Yu-Cheng QIU

# Can we explain cosmic birefringence without a new light field beyond Standard Model?

Yu-Cheng QIU



November 16, 2023

2310.09152 with Yuichiro Nakai, Ryo Namba, Ippei Obata, Ryo Saito

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#### @ twitter CMB polarization

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[Introduction](#page-1-0)

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Figure: Copyright: ESA and the Planck Collaboration

# Isotropic Cosmic Birefringence

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$$
\langle C_l^{EB,obs} \rangle \neq 0 \implies \beta \neq 0
$$

 $\beta=0.35^{\circ}\pm0.14^{\circ}\ (2.4\sigma)$ (Minami and Komatsu 2011.11254)

 $\beta=0.34^{\circ}\pm0.09^{\circ}\ (3.6\sigma)$ (Eskilt and Komatsu 2205.13962)

- · · · ٠
- **4** Isotropic
- 2 Frequency-blind



Figure: Credit: Yuto Minami

### **@** 全战起阵之下 Axion (ALP) Explanation

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Consider Axion-photon coupling (Carroll and Field,1991)

$$
\mathcal{L}=-\frac{1}{4}F_{\mu\nu}F^{\mu\nu}-\frac{1}{4}\theta(t)F_{\mu\nu}\tilde{F}^{\mu\nu}
$$

This modifies equation of motion of photon (Choosing  $A^0=0$  and  $\nabla\cdot\vec{A}=0)$ ,

$$
\left(\frac{\partial^2}{\partial \eta^2} - \nabla^2 + \dot{\theta} \nabla \times \right) \vec{A} = 0 \quad \implies \quad \omega_{\pm}^2 = k^2 \mp k \dot{\theta}
$$

In the limit  $\frac{|\dot{\omega}_{\pm}|}{\omega_{\pm}^2}\ll 1$ , WKB approximation gives

$$
A_{\pm} \propto e^{-i \int d\eta k} \exp\left(\pm i \int d\eta \frac{\dot{\theta}}{2}\right) \implies \beta = \frac{1}{2} \int_{\eta_{LSS}}^{\eta_0} d\eta \dot{\theta} = \frac{1}{2} \left[\theta(\eta_0) - \theta(\eta_{LSS})\right]
$$

## @tud4£7 Axion (ALP) Explanation

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Figure: Fujita et al. 2011.11894  $(12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.11894 + 12.118$ 



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#### [SM?](#page-5-0)

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Figure: Artwork by Sandbox Studio, Chicago.



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[Relevant Operators](#page-6-0)

[A New Light Field?](#page-22-0)

- <span id="page-6-0"></span>• ICB is a propagating effect. Relevant operators are quadratic in  $\vec{E}$  and  $\vec{B}$ . In the vacuum, only  $F_{\mu\nu}F^{\mu\nu}$  is relevant. Therefore, we need medium.
- Observed isotropy  $\implies$  medium is homogeneous.
- Derivative on  $\vec{E}$  and  $\vec{B}$  shall lead to frequency-dependent  $\beta$ , which do not fit the observation.

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$$
\mathcal{L} \sim c_{\mathsf{EE}}(t)\vec{E}\cdot\vec{E} + c_{\mathsf{BB}}(t)\vec{B}\cdot\vec{B} + c_{\mathsf{EB}}(t)\vec{E}\cdot\vec{B}
$$

 $\cdot \vec{E} \cdot \vec{B}$ -term violates parity, produces ICB.

Any operator that relevant to ICB should be reduced to  $c_{EB}(t)\vec{E}\cdot\vec{B}$  in a cosmological background.



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[Relevant Operators](#page-6-0)







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• Of course,  $\tilde{\mathcal{O}}F_{\mu\nu}\tilde{F}^{\mu\nu} \rightarrow \tilde{\mathcal{O}}\vec{E}\cdot\vec{B}$ . Is it the only one?

 $\mathcal{J}_{\mu\nu\alpha\beta}F^{\mu\nu}\tilde{F}^{\alpha\beta}$  under the cosmological background,  $\mathcal J$  could be formed by  $g_{\mu\nu}$  and  $u_{\mu} \propto \nabla_{\mu} t$ , t is cosmic time.

$$
\mathcal{J}_{\mu\nu\alpha\beta} = \frac{1}{2} \left( g_{\mu\alpha} J_{\nu\beta} + g_{\mu\beta} J_{\nu\alpha} - g_{\nu\alpha} J_{\mu\beta} - g_{\nu\beta} J_{\mu\alpha} \right) , \quad J_{\mu\nu} = f(g_{\mu\nu}, u_{\mu})
$$

This reduce to

$$
J_{\alpha\beta}F^{\alpha\mu}\tilde{F}^{\beta}{}_{\mu}\;\rightarrow\;\tilde{\mathcal{O}}F_{\mu\nu}\tilde{F}^{\mu\nu}\;,\quad\tilde{\mathcal{O}}=\frac{J_{\mu}{}^{\mu}}{4}=\frac{\mathcal{J}_{\alpha\beta}{}^{\alpha\beta}}{6}
$$





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$$

 $J_{\mu}K^{\mu}$ , where  $K^{\mu}=2A_{\nu}\tilde{F}^{\mu\nu}$ . It is not  $U(1)$  invariant unless  $\nabla_{[\mu}J_{\nu]}=0$ , which means that  $J_{\mu} \propto \nabla_{\mu}\tilde{\mathcal{O}}$ . This makes  $J_{\mu}K^{\mu}\ \rightarrow\ \tilde{\cal O}F_{\mu\nu}\tilde{F}^{\mu\nu}$  . K ロ ▶ K 何 ▶ K ヨ ▶ K ヨ ▶ - ヨ 出 → 9 Q (^



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 $J_{\mu\nu}F^{\mu\nu}$  may give rise to P-violating effect in the loop level. Formally,  $\delta J_{\mu\nu}=\hat{K}_{\mu\nu\alpha\beta}F^{\alpha\beta}\ \rightarrow\ F^{\mu\nu}\hat{K}_{\mu\nu\alpha\beta}F^{\alpha\beta}.$ If  $\hat K_{\mu\nu\alpha\beta}\supset\tilde{\cal O}_\epsilon\epsilon_{\mu\nu\alpha\beta}/2$ , then  $F^{\mu\nu}\hat K_{\mu\nu\alpha\beta}F^{\alpha\beta}\ \to\ \tilde{\cal O}_\epsilon F_{\mu\nu}\tilde F^{\mu\nu}$ . However,  $\tilde{\mathcal{O}}_\epsilon$  is non-local, produces frequency-dependent ICB angle.



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**• Cosmic Magnetic field breaks parity.** 

However, it will produces Anisotropic Cosmic birefringence angle.



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**• Cosmic Magnetic field breaks parity.** 

However, it will produces Anisotropic Cosmic birefringence angle.

To explain the observed frequency-independent ICB, only CS-type operator  $\tilde{\mathcal{O}}F_{\mu\nu}\tilde{F}^{\mu\nu}$  should be considered.





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[Relevant Operators](#page-6-0)

$$
\mathcal{L}_{\text{CS}} = \frac{\alpha}{8\pi} \sum_{a} \frac{\tilde{\mathcal{O}}_a}{\Lambda_a^n} F_{\mu\nu} \tilde{F}^{\mu\nu} , \quad n = \text{dim}[\tilde{\mathcal{O}}_a]
$$

Building Blocks:

 $H(\text{dim } 1)$ ,  $D_u(\text{dim } 1)$ ,  $\psi(\text{dim } 3/2)$ ,  $X_{\mu\nu}(\text{dim } 2)$ 



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$$
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$$

Building Blocks:

 $H(\text{dim } 1)$ ,  $D_{\mu}(\text{dim } 1)$ ,  $\psi(\text{dim } 3/2)$ ,  $X_{\mu\nu}(\text{dim } 2)$  $n=2$ :  $H^{\dagger}H$ 

 $n=3$ : (LEFT)  $\mathcal{C}^{ij} \bar{e}^i P_{\mathsf{L}} e^j + \text{h.c.}, \quad (e \to \nu, d, u).$ One does not have hypercharge singlet in SM. Therefore, one has to go down to  $SU(3)_c \times U(1)_{\text{EM}}$ . (Low-energy EFT)

• 
$$
n = 4
$$
:  $\sum_{X = F, Z, W, G} X_{\alpha\beta} X^{\alpha\beta} + X_{\alpha\beta} \tilde{X}^{\alpha\beta}$ 

## <span id="page-16-0"></span>ICB from  $\tilde{\mathcal{O}}$  F $\tilde{F}$ ? @txi4\*\*

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[Possible ICB](#page-16-0)

$$
\frac{\alpha}{8\pi}\tilde{\mathcal{O}}F_{\mu\nu}\tilde{F}^{\mu\nu} \stackrel{\text{Cosmos bg.}}{\rightarrow} \frac{1}{4}\phi_{\tilde{\mathcal{O}}}F_{\mu\nu}\tilde{F}^{\mu\nu}, \quad \phi_{\tilde{\mathcal{O}}} = \frac{\alpha}{2\pi}\langle\tilde{\mathcal{O}}\rangle
$$
\nThe ICB effect is given by (same as the axion)

\n
$$
\beta = \frac{1}{2}\left[\phi_{\tilde{\mathcal{O}}}(t_{\text{LSS}}) - \phi_{\tilde{\mathcal{O}}}(t_0)\right]
$$

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#### @方法出身名示  $n = 2$  ICB

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$$
\frac{\alpha}{8\pi} \frac{H^{\dagger} H}{\Lambda_H} F_{\mu\nu} \tilde{F}^{\mu\nu} \implies \phi_{\tilde{\mathcal{O}}_2} = \frac{\alpha v^2}{2\pi \Lambda_H^2}, \quad v \equiv \langle H \rangle
$$

$$
\beta \simeq \frac{\alpha v_0^2}{2\pi \Lambda_H^2} \delta v \ , \quad \delta v \equiv \frac{v - v_0}{v_0}
$$

CMB gives  $\frac{\Delta m_e}{m_e} < (4 \pm 11) \times 10^{-3}$ , this indicates  $\delta v \lesssim 10^{-3}$ – $10^{-2}$ . • Collider gives  $\Lambda_H > 1$  TeV.

 $\beta < (4 \times 10^{-5})^\circ \ll \beta_\mathsf{obs}$ 

#### @ 本版【4文件  $n = 3$  ICB

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Charged particle are suppressed by baryon-to-photon ratio  $\eta \sim 10^{-10}$ . Thus, the only possible candidate here is Cosmic Neutrino Background( $C\nu B$ ). Assume Dirac neutrino.

$$
\frac{\alpha}{8\pi}\frac{\tilde{\mathcal{O}}_{\nu}}{\Lambda_{\nu}}\mathcal{F}_{\mu\nu}\tilde{\mathcal{F}}^{\mu\nu}\;,\quad \tilde{\mathcal{O}}_{\nu}=\frac{(\tilde{\mathcal{C}}_{\nu}^{\dagger}+\tilde{\mathcal{C}}_{\nu})^{ij}}{2}\bar{\nu}^{i}\nu^{j}+\frac{(\tilde{\mathcal{C}}_{\nu}^{\dagger}-\tilde{\mathcal{C}}_{\nu})^{ij}}{2}\bar{\nu}^{i}\gamma^{5}\nu^{j}
$$

• 
$$
\langle \bar{\nu}^i \gamma^5 \nu^j \rangle = 0
$$
 and  $\langle \bar{\nu}^i \nu^j \rangle = \delta^{ij} \mathcal{F}(t)$ ,

$$
\mathcal{F}(t) = \int \frac{d^3p}{(2\pi)^3} \frac{m_i}{E_p} \left[ n^i(p, t) + \bar{n}^i(p, t) \right] ,
$$

where  $m_i$  is the *i-*th neutrino mass and  $n^i$  is phase-space number density. ( $\bar{n}$  is that for anti-neutrino.)

**o** This indicates that

$$
\phi_{\tilde{\mathcal{O}}_{\nu}}(t) = \frac{\alpha}{4\pi} \frac{\text{tr}\left[ (\tilde{\mathcal{C}}_{\nu}^{\dagger} + \tilde{\mathcal{C}}_{\nu}) \mathcal{F}(t) \right]}{\Lambda_{\nu}^3}
$$

Majorana case with an extra  $1/2$ .

#### @ 本はまみを示  $n = 3$  ICB

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- Due to cosmic expansion,  $\phi_{\tilde{\mathcal{O}}_{\nu}}(t_0)\ll\phi_{\tilde{\mathcal{O}}_{\nu}}(t_{\textsf{LSS}}).$
- At recombination  $T_{LSS} \sim 0.3 \text{ eV}$ ,

$$
\mathcal{F}(t_{LSS}) \simeq 0.5 \frac{m_i}{T_{LSS}} \left(N^i + \bar{N}^i\right) , \quad m_i \ll T_{LSS}
$$

where N and  $\overline{N}$  are number density for neutrino and anti-neutrino. • Possible ICB angle is

$$
\beta \simeq \frac{1}{2} \phi_{\tilde{\mathcal{O}}_{\nu}}(t_{\text{LSS}}) \simeq 0.008^{\circ} \frac{\alpha}{137^{-1}} \sum_{i} \frac{m_{i}}{\mathcal{T}_{\text{LSS}}} \left( \tilde{\mathcal{C}}_{\nu} + \tilde{\mathcal{C}}_{\nu}^{\dagger} \right) \frac{N^{i} + \bar{N}^{i}}{\Lambda_{\nu}^{3}} \;,
$$

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#### @各位是研究所  $n = 3$  ICB

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$$
\beta \simeq 0.008^\circ \frac{\alpha}{137^{-1}} \sum_i \frac{m_i}{\mathcal{T}_{\rm LSS}} \left( \tilde{\mathcal{C}}_\nu + \tilde{\mathcal{C}}_\nu^\dagger \right) \frac{N^i + \bar{N}^i}{\Lambda_\nu^3} \; ,
$$

- C $\nu$ B neutrino number density today is  $\sim$  56 cm $^{-3}.$ Tracing back to LSS gives  $N^{1/3} \sim \mathcal{O}(10^{-10})$  GeV.
- Collider gives  $\Lambda_{\nu} \simeq 10^{-2}$ –10<sup>2</sup> GeV.
- Taking  $\tilde{\mathcal{C}} \sim \mathcal{O}(1)$ ,  $m_i \sim 0.1$  eV and  $T_{LSS} \sim 0.3$  eV, one has

 $\beta < (10^{-27})^{\circ} \ll \beta_{\mathsf{obs}}$ 

#### @子は【4之下  $n = 4$  ICB

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[Possible ICB](#page-16-0) [A New Light Field?](#page-22-0)

$$
\frac{\alpha}{8\pi}\frac{F_{\alpha\beta}F^{\alpha\beta}+F_{\alpha\beta}\tilde{F}^{\alpha\beta}}{\Lambda_F^4}F_{\mu\nu}\tilde{F}^{\mu\nu}
$$

Cosmic Background magnetic field. Let  $F \to F^{(0)} + F$ . Then, quadratic terms are

- $(\mathit{F}^{(0)}_{\alpha\beta}F^{\alpha\beta})(F^{(0)}_{\mu\nu}\tilde{F}^{\mu\nu})\propto \vec{E_{\parallel}}\cdot\vec{B_{\parallel}}\quad\Longrightarrow\quad$  Anistropic CB  $(\bar{F}^{(0)}_{\mu\nu}\tilde{F}^{\mu\nu})^2 \propto \vec{E_{\parallel}}\cdot\vec{E_{\parallel}}$
- CS-type term  $(\mathit{F}^{(0)}_{\alpha\beta}\mathit{F}^{(0)}{}^{\alpha\beta})(\mathit{F}_{\mu\nu}\tilde{F}^{\mu\nu}) \propto \vec{E}\cdot\vec{B} \quad \implies \quad \text{ICB}$ They are of the same order!

<span id="page-22-0"></span>Yu-Cheng QIU

[A New Light Field?](#page-22-0)

- $\alpha$  Φ $^\dagger$ Φ 8π Λ2 for a scalar Φ α  $8\pi$  $\bar{\chi}\chi$ Λ3 for a fermion  $\chi$
- $\langle\Phi^\dagger\Phi\rangle$  and  $\langle\bar{\chi}\chi\rangle$  should be time-dependent backgrounds:
	- **o** Classical fields similar to Axion
	- Pair condensates : effectively the same to Axion & Require exotic cosmological scenario.
	- Particles : like  $C\nu B$ .

## Possible New Light Field

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For a single particle,  $E_p > m$ . In the cosmological background

$$
\langle \Phi^\dagger \Phi \rangle \lesssim \frac{\rho}{m^2} \; , \quad \langle \bar{\chi} \chi \rangle \lesssim \frac{\rho}{m}
$$

At the LSS, one should have  $\rho<\rho_\mathsf{c,LSS}\simeq (3\times 10^{-13}\,\mathsf{TeV})^4$ . Therefore,

$$
m \lesssim 10^{-14} \,\mathrm{eV} \left(\frac{|\beta|}{0.3^\circ}\right)^{-1/2} \left(\frac{\Lambda}{\mathrm{TeV}}\right)^{-1} \quad \text{(Scalar)}
$$
\n
$$
m \lesssim 10^{-40} \,\mathrm{eV} \left(\frac{|\beta|}{0.3^\circ}\right)^{-1} \left(\frac{\Lambda}{\mathrm{TeV}}\right)^{-3} \quad \text{(Fermion)}
$$



## <span id="page-24-0"></span>Takeaway

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[Summary](#page-24-0)

- From EFT point of view, only CS-type operator could give frequency-blind ICB.
- SM particle could not give observed ICB under standard cosmology.

<span id="page-25-0"></span>

[Summary](#page-24-0)

Thank You!



## $ICB$  from  $B'$ @各位选择名环

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$$
\frac{1}{2}\int d^4 k_1 d^4 k_2 A_\mu(k_1) \Pi^{\mu\nu}(k_1,k_2) A_\nu(k_2)
$$

- Introduce helicity basis with respect to **k**,  $\{ \epsilon_{1}^{\mu} \}$  $_{\mathsf{L}}^{\mu},\epsilon_{+}^{\mu},\epsilon_{-}^{\mu}\}.$ So  $\epsilon_{\mathsf{I}}^{\mu}$  $\mu_{\mathsf{L},\pm}^{\mu}u_{\mu}=0$ ,  $k_{\mu}\epsilon_{\pm}^{\mu}=0\neq k_{\mu}\epsilon_{\mathsf{L}}^{\mu}$  $\frac{\mu}{L}$ .
- Including the background, one has  $k_1^{\mu} + k_2^{\mu} \propto u^{\mu} \neq 0$ . Expand  $k_1^{\mu} = \omega_1 u^{\mu} + |\mathbf{k}| \epsilon_{\mathsf{L}}^{\mu}$  $\mu_{\mathsf{L}}^{\mu}$  and  $k_2^{\mu} = \omega_2 u^{\mu} - |\mathbf{k}| \epsilon_{\mathsf{L}}^{\mu}$  $\frac{\mu}{L}$ .
- With the background unit vector  $u_\mu\propto \nabla_\mu t$ , one has  $\overline B^\mu=u_\nu\tilde F^{(0)\mu\nu}.$
- One could expand  $\overline{B}^{\mu} = \overline{B}_{L} \epsilon_{L}^{\mu} + \overline{B}_{+} \epsilon_{+}^{\mu} + \overline{B}_{\epsilon-}^{\mu}$ .
- $\mathcal{F}_{\mu\nu}\tilde{\mathcal{F}}^{\mu\nu}\implies\Pi^{\mu\nu}\supset\epsilon^{\mu\nu\alpha\beta}(k_1)_{\alpha}(k_2)_{\beta}\propto\epsilon^{\mu\nu\alpha\beta}u_{\alpha}(\epsilon_{\mathsf{L}})_{\beta}\propto\epsilon_+^{*\mu}\epsilon_+^{\nu}-\epsilon_-^{*\nu}\epsilon_-^{\mu}$ −  $(F^{(0)}_{\alpha\beta}F^{(0)}{}^{\alpha\beta})(F_{\mu\nu}\tilde{F}^{\mu\nu})=|\overline{B}|^2F\tilde{F}$  term gives ICB if  $|\overline{B}|$  is uniform.

### ACB from  $\overline{B}$ @ twitter

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$$
(F_{\alpha\beta}^{(0)}F^{\alpha\beta})(F_{\mu\nu}^{(0)}\tilde{F}^{\mu\nu}) = (\overline{B}_{\alpha}u_{\beta}F^{\alpha\beta})(\overline{B}_{\mu}u_{\nu}\tilde{F}^{\mu\nu})
$$
\n•  $F^{\alpha\beta} \rightarrow k_1^{\alpha}A^{\beta}(k_1) - k_1^{\beta}A^{\alpha}(k_1)$  and  $\tilde{F}^{\mu\nu} \rightarrow \epsilon^{\mu\nu\alpha\beta}(k_2)_{\alpha}A_{\beta}(k_2)$ .  
\n•  $\overline{B}_{\alpha}u_{\beta}F^{\alpha\beta} \rightarrow [(\overline{B} \cdot k_1)u^{\mu} - (u \cdot k_1)\overline{B}^{\mu}]A_{\mu}(k_1)$   
\n $\propto (\overline{B}_{+}\epsilon_{+}^{\mu} + \overline{B}_{-}\epsilon_{-}^{\mu})A_{\mu}(k_1) + \cdots$   
\n•  $\overline{B}_{\mu}u_{\nu}\tilde{F}^{\mu\nu} \propto (\overline{B}_{+}\epsilon_{+}^{\nu} - \overline{B}_{-}\epsilon_{-}^{\nu})A_{\nu}(k_2)$   
\n•  $(F_{\alpha\beta}^{(0)}F^{\alpha\beta})(F_{\mu\nu}^{(0)}\tilde{F}^{\mu\nu}) \supset C\overline{B}_{+}\overline{B}_{-}(\epsilon_{+}^{*\mu}\epsilon_{+}^{\nu} - \epsilon_{-}^{*\mu}\epsilon_{-}^{\nu})A_{\mu}A_{\nu}.$ 

This gives ACB due to the dependence on components of  $\overline{B}$ .

## Can we explain cosmic birefringence without a new [light field beyond](#page-0-0)

@txi4%F

Dipole operator

 $A_{\mu}$ 

Standard Model? Yu-Cheng QIU

$$
J_{\mu\nu}F^{\mu\nu}, J_{\mu\nu} = \bar{\nu}^i \lambda^{ij} \sigma_{\mu\nu} \nu^j, \quad \lambda = \underbrace{\mathfrak{M}}_{\text{magnetic}} + \underbrace{i \mathfrak{E} \gamma^5}_{\text{electric}}
$$
\n
$$
\sum_{\nu \in \mathcal{N}} \mathfrak{K}_{\mu\nu\alpha\beta} F^{\alpha\beta} \rightarrow \tilde{\mathcal{O}}_{\epsilon} F_{\mu\nu} \tilde{F}^{\mu\nu}, \quad \tilde{\mathcal{O}}_{\epsilon} \propto \epsilon^{\mu\nu\alpha\beta} \hat{K}_{\mu\nu\alpha\beta}
$$
\n
$$
\hat{K}_{\mu\nu\alpha\beta} \propto (\bar{\nu}^i)^{(\text{bg})} \sigma_{\mu\nu} \lambda^{ij} \frac{1}{i \partial - m_j} \sigma_{\alpha\beta} \lambda^{jk} (\nu^k)^{(\text{bg})}
$$
\n
$$
\tilde{\mathcal{O}}_{\epsilon} \propto (\bar{\nu}^i)^{(\text{bg})} \epsilon^{\mu\nu\alpha\beta} \sigma_{\mu\nu} \lambda^{ij} (i \partial - m_j)^{-1} \sigma_{\alpha\beta} \lambda^{jk} (\nu^k)^{(\text{bg})}
$$
\n
$$
= -4im_j(\bar{\nu}^i)^{(\text{bg})} \lambda^{ij} \gamma^5 (\partial^2 + m_j^2)^{-1} \lambda^{jk} (\nu^k)^{(\text{bg})}
$$

Using  $\epsilon^{\mu\nu\alpha\beta}\sigma_{\mu\nu} = -2i\gamma^5\sigma^{\alpha\beta}$ ,  $\sigma^{\mu\nu}\sigma_{\mu\nu} = 12$  and  $\sigma^{\mu\nu}\gamma^{\alpha}\sigma_{\mu\nu} = 0$ .

#### **Otal425** Dipole operator

Can we explain cosmic birefringence without a new [light field beyond](#page-0-0) Standard Model?

$$
\langle \tilde{\mathcal{O}}_{\epsilon} \rangle \propto m_j \left\langle (\bar{\nu}^j)^{(\text{bg})} \lambda^{ij} \gamma^5 (\partial^2 + m_j^2)^{-1} \lambda^{jk} (\nu^k)^{(\text{bg})} \right\rangle
$$
  

$$
\langle \bar{\nu} \gamma^5 \nu \rangle = 0 \neq \langle \bar{\nu} \nu \rangle, \text{ this implies that}
$$
  

$$
\langle \tilde{\mathcal{O}}_{\epsilon} \rangle \propto m_j (\mathfrak{M}^{ij} \mathfrak{E}^{ji} + \mathfrak{E}^{ij} \mathfrak{M}^{ji}) \int \frac{d^3 p_{\nu}}{(2\pi)^3} \frac{m_i}{E_{\nu}} \frac{n^i (p_{\nu}) + \bar{n}^i (p_{\nu})}{(p_{\nu} + p_{\gamma})^2 - m_j^2}
$$
  
Let  $p_{\nu} = (E_{\nu}, \mathbf{p}_{\nu})$  and  $p_{\gamma} = (\omega, \omega \mathbf{n})$ , where  $|\mathbf{n}| = 1$ .  

$$
(p_{\mu} + p_{\gamma})^2 - m_j^2 = 2\omega (E_{\nu} - \mathbf{n} \cdot \mathbf{p}_{\nu}) + m_i^2 - m_j^2 \stackrel{\text{LSS}}{\simeq} 2\omega (E_{\nu} - \mathbf{n} \cdot \mathbf{p}_{\nu})
$$

$$
\beta \propto \langle \tilde{\mathcal{O}}_{\epsilon} \rangle \big|_{\mathsf{LSS}} \propto \frac{1}{\omega} , \quad \text{Frequency-dependent ICB}
$$

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$$
\nu(x) = \int \frac{d^3 p}{(2\pi)^3} \frac{1}{\sqrt{2E_p}} \sum_s \left[ a_p^s u^s(p) e^{-ipx} + b_p^{s\dagger} v^s(p) e^{ipx} \right]
$$

$$
\bar{\nu}(x) = \int \frac{d^3 p}{(2\pi)^3} \frac{1}{\sqrt{2E_p}} \sum_s \left[ b_p^s \bar{v}^s(p) e^{-ipx} + a_p^{s\dagger} \bar{u}^s(p) e^{ipx} \right]
$$

with  $\{a_{\bf p}^r, a_{\bf q}^{s\dagger}\} = \{b_{\bf p}^r, b_{\bf q}^{s\dagger}\} = (2\pi)^3 \delta^{(3)}({\bf p}-{\bf q})\delta^{rs}.$ Dirac equation gives

$$
u^s(p) = \begin{pmatrix} \sqrt{p \cdot \beta} \xi^s \\ \sqrt{p \cdot \beta} \xi^s \end{pmatrix} , \quad v^s(p) = \begin{pmatrix} \sqrt{p \cdot \beta} \eta^s \\ -\sqrt{p \cdot \beta} \eta^s \end{pmatrix} , \quad \xi^{\dagger} \xi = \eta^{\dagger} \eta = 1 ,
$$

where  $\beta^\mu = (1,\vec\beta)$ ,  $\bar\beta^\mu = (1,-\vec\beta)$  and  $\vec\beta$  are Pauli matrices. Using  $\bar{u}^s u^r = -\bar{v}^s v^r = 2m\delta^{sr}$  and  $\bar{u}^s \gamma^5 u^r = \bar{v}^s \gamma^5 v^r = 0$ , one has

$$
\langle \bar{\nu}\gamma^5 \nu \rangle = 0 \ , \quad \langle \bar{\nu}\nu \rangle = \int \frac{d^3p}{(2\pi)^3} \frac{m}{E_p} \left[ n(p) + \bar{n}(p) \right]
$$

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