

Particle Accelerators: Diagnostics and Correction

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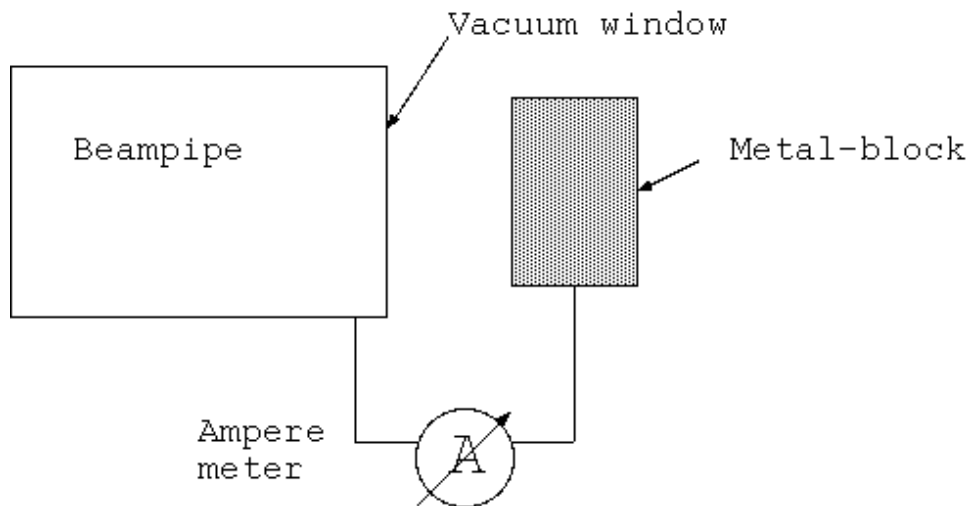
Diagnostics and Correction

- Zeroth Moment: Current
- First Moment: Position
- Second Moment: Size
- Emittance and Beta function
- Tune
- Beam-beam diagnostics
- Orbit correction
- Tune correction



Faraday Cup

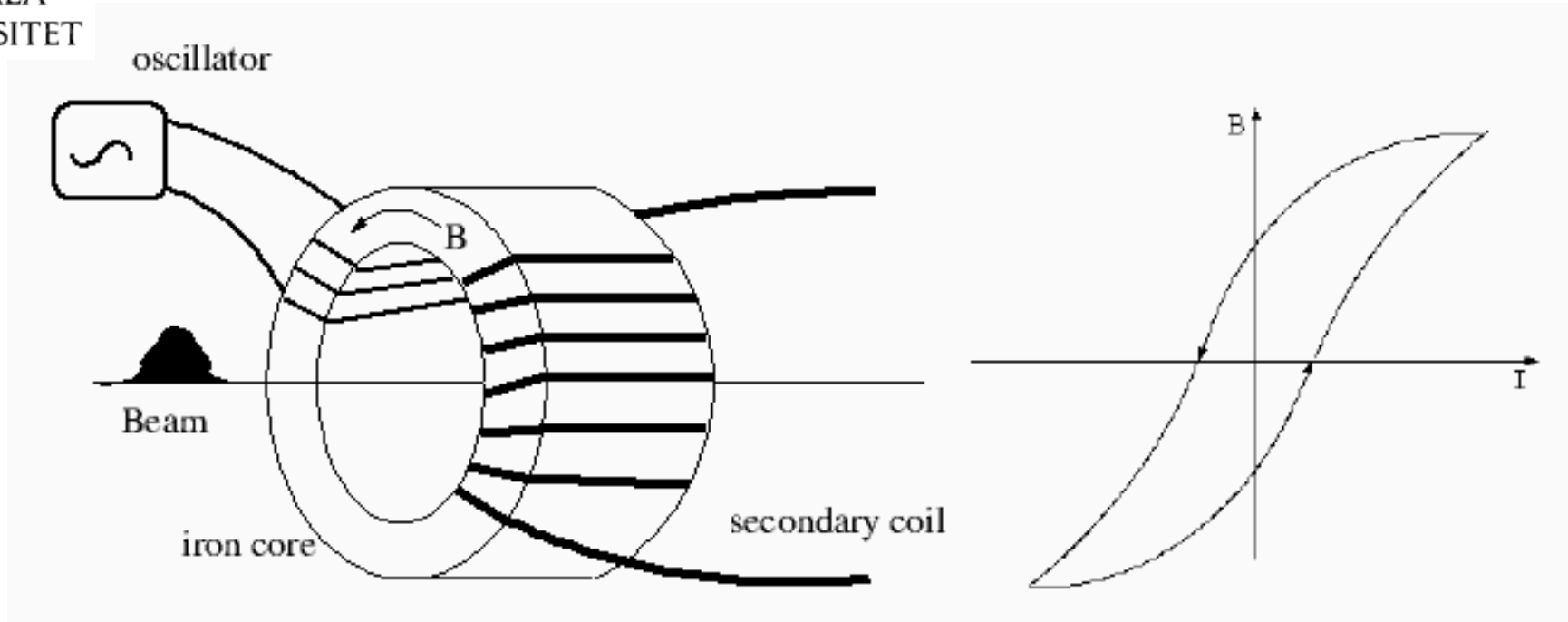
- Dump current in a shielded metal block that stops the beam and measure current to ground



- Invasive
- Needs to be thick enough to stop beam
- Might need cooling
- Need to shield secondary electrons
- Needs careful attention if time-resolved signal is required



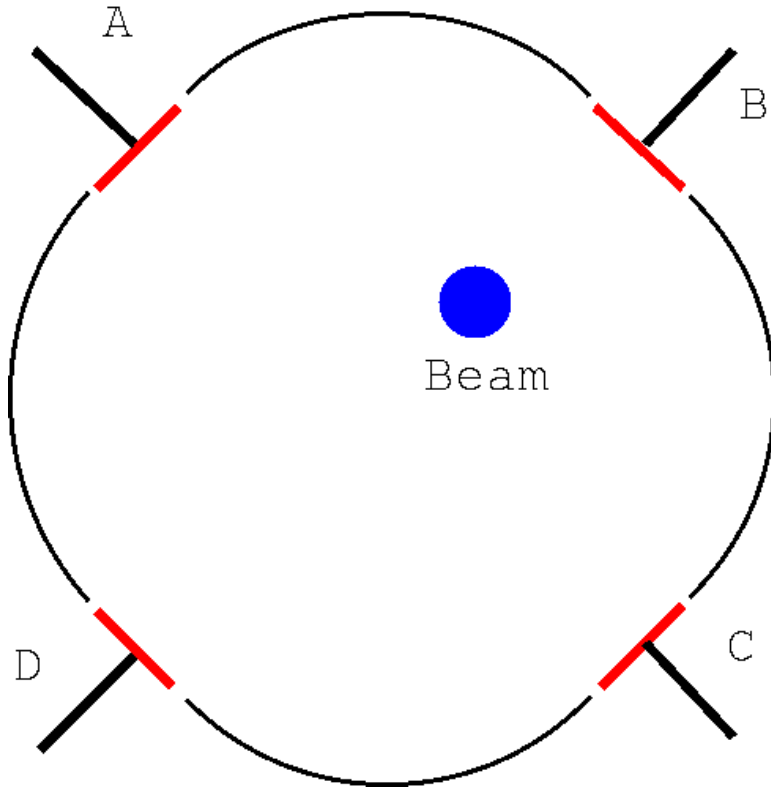
DCCT



- External oscillator drives the core through hysteresis curve
- Without beam only odd harmonics in secondary coil
- With beam the hysteresis-curve is displaced and even harmonics are generated and can be compensated to zero with extra current that can be measured.



Beam Position Monitor

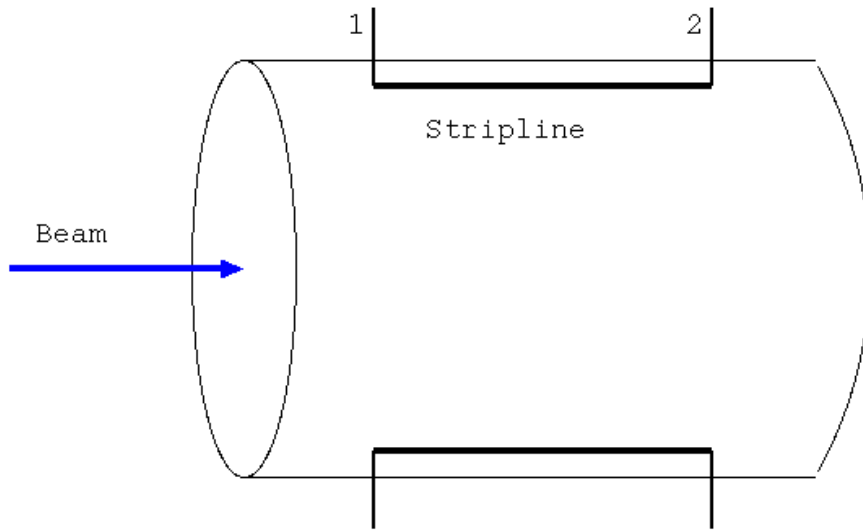


- Picks up the wall currents at several positions
- If more signal on the left (A+D) compared to (B+C) then the beam is further to the left.
- $k_x = k_y = R/\sqrt{2}$
- Small signal in small buttons
- Used in high intensity machines with short bunches. Synchrotron light sources
- Non-linear at large amplitudes

$$x = k_x \frac{(A + D) - (B + C)}{A + B + C + D} , \quad y = k_y \frac{(A + B) - (C + D)}{A + B + C + D}$$



Stripline BPM



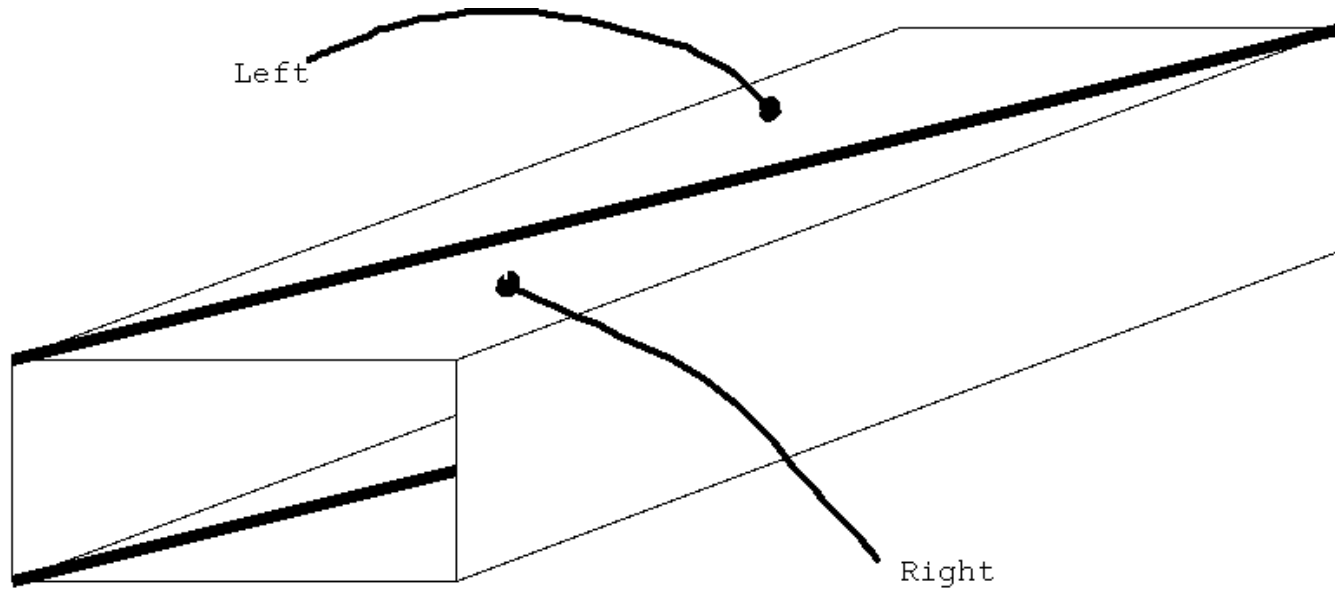
$$V_1(t) = \frac{Z_s \phi}{4\pi} [I(t) - I(t - l/v_b - l/v_s)]$$

$$V_2(t) = \frac{Z_s \phi}{4\pi} [I(t - l/v_s) - I(t - l/v_b)]$$

- Magnetic flux in the small area between strip and wall changes and induces a voltage in wires.
- Signals with opposite polarity from the ends.
- Directional if bunch length smaller than stripline.
- Can be used to separate signals from counter-propagating beams.
- Position information from four striplines similar to button BPM.



Shoebox BPM

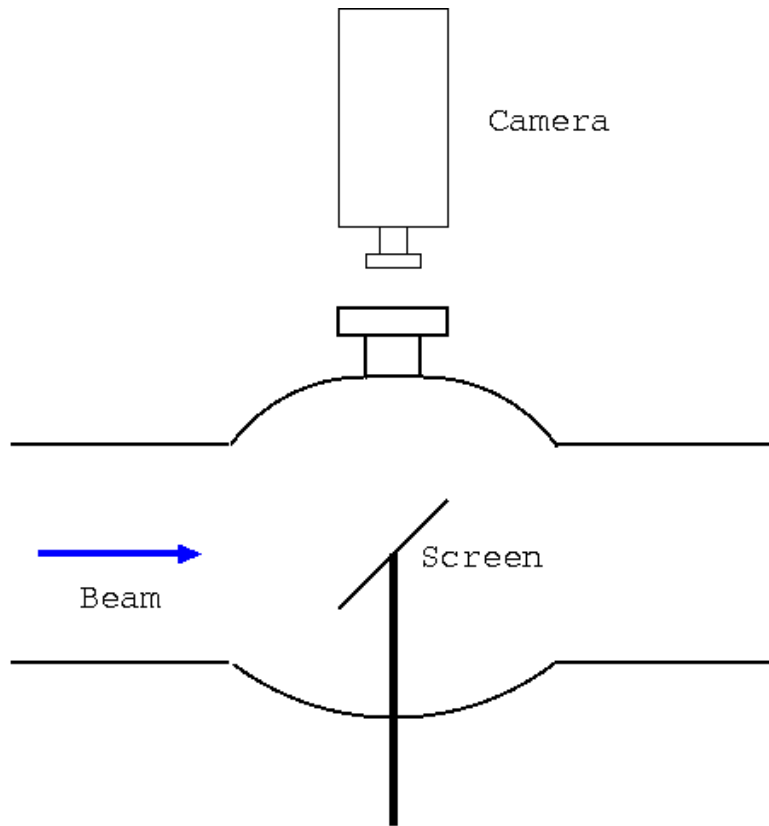


- Large electrodes make it sensitive to weak currents in ion storage rings
- CELSIUS used these



Luminescent and OTR Screen

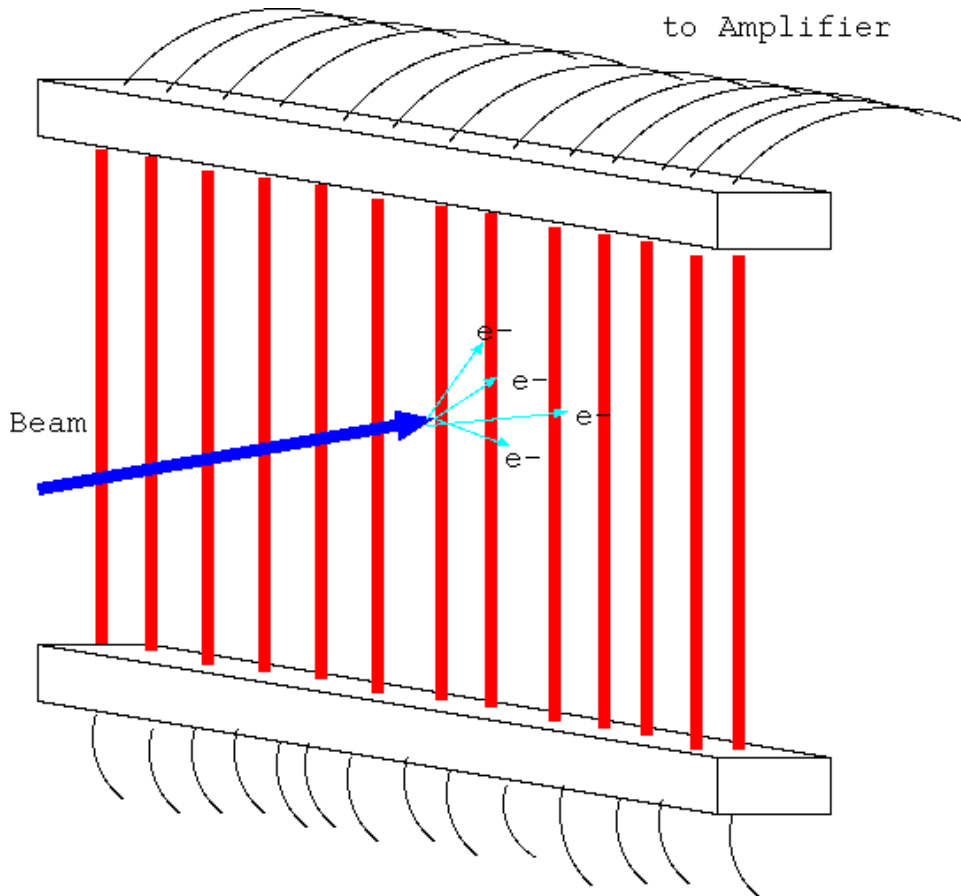
- Now to 2nd Moments



- Place either movable or static luminescent screen in path of beam → invasive
- Blind spots and burn-out
- Limited dynamic range
- Failing cameras
- Optical transition radiation due to refractive index of screen
- thin foil of e.g. AlO_2
- Disturbs high energy beams very little if thin enough



SEM Grid



- Secondary emission monitor
- Beam intercepts thin wires and knocks out electrons
- Parallel readout of many wires
- One amplifier per wire makes this expensive
- Heat deposition in wires
- Plot current from wire as function of wire number
- Histogram
- Position and size of beam



Other size measurements

- Wire scanner, use single movable wire instead
 - position encoder
 - need to move fast in ring
- Magnesium Jet Profile Monitor
 - use evaporated MG as 'wire'
 - record the ionized electrons
- Residual gas profile monitor
 - ionize residual gas and catch electrons on position sensitive sensors
 - use magnetic fields to guide the electrons



Tune

- Kick the beam with a pulsed magnet
- Measure the position on every turn with beam position monitor
- Time series: $x_1, x_2, x_3, \dots, x_n$
- Fourier transform, usually FFT is used.
- Aliasing: can observe only fractional tune.
- Alternatively: Observe tune sideband of the revolution harmonics in spectrum analyzer

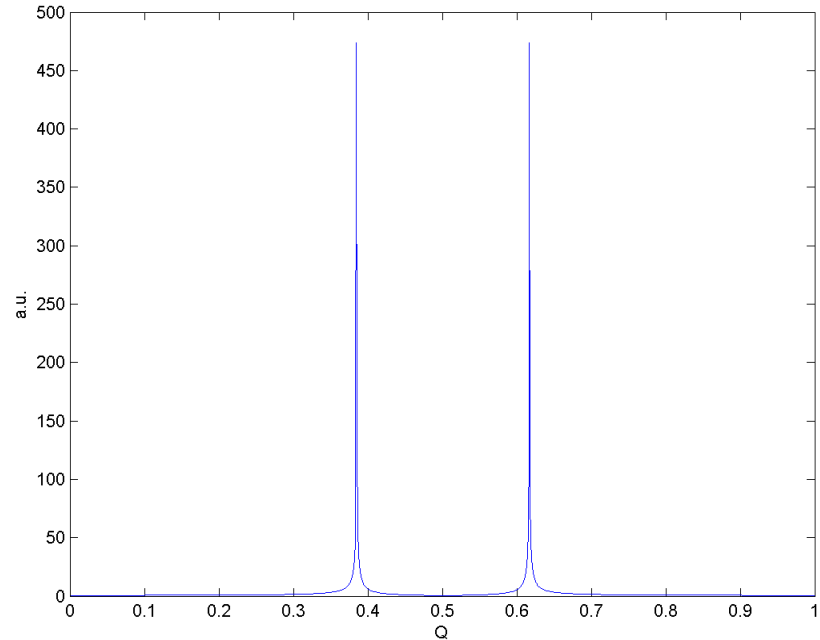


Example: Tune from time series

$$\begin{aligned}x_n &= \sin(\omega_\beta t_n) \\ &= \sin(\omega_\beta nT_0) \\ &= \sin(Q_x 2\pi f_0 nT_0) \\ &= \sin(2\pi n Q_x) \\ &= \sin(2\pi n [Q_x])\end{aligned}$$

[Q]= fractional part of tune

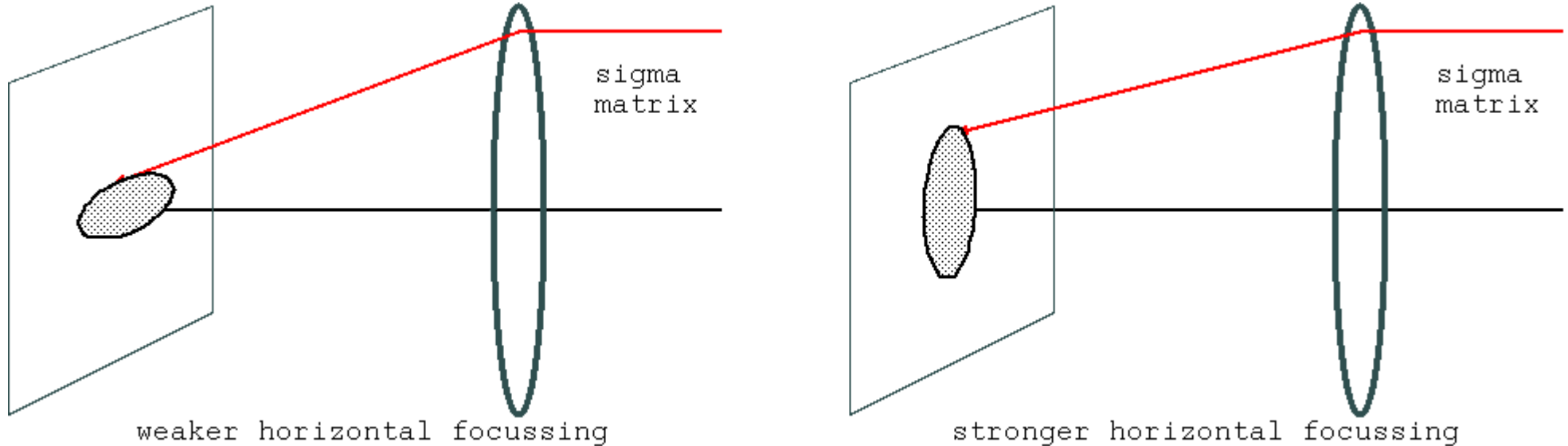
```
Qx=0.616  
n=1:1:1024;  
x=sin(2*pi*Qx*n);  
plot(n/1024,abs(fft(x)));
```



- cannot distinguish Q and 1-Q
- change QF and see how tune line moves



Emittance and Beta function

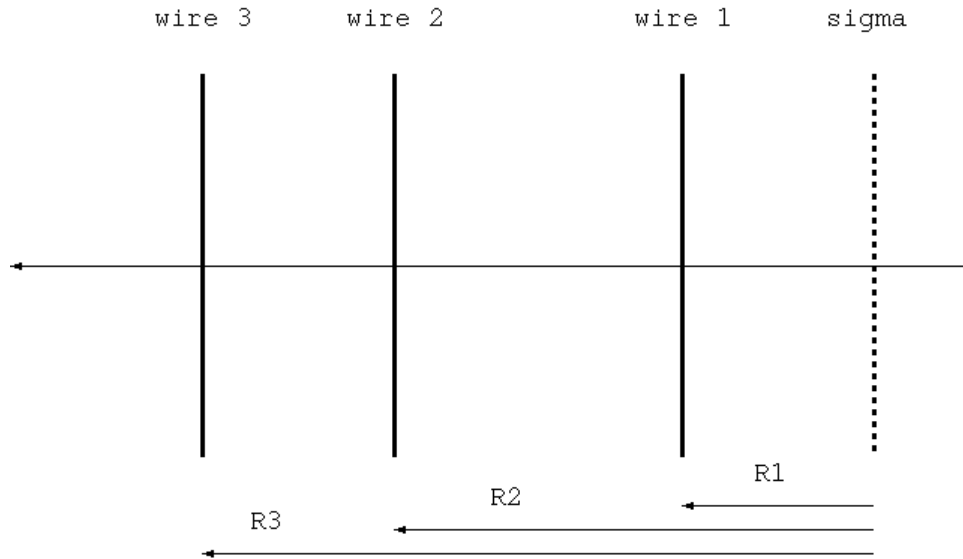


- Quadrupole scan: vary quadrupole and observe how the measured spot size changes
- Depends on all parameters of the beam before the quadrupole

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{12} & \sigma_{22} \end{pmatrix} = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle \end{pmatrix} = \varepsilon \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}$$



Several wire scanners



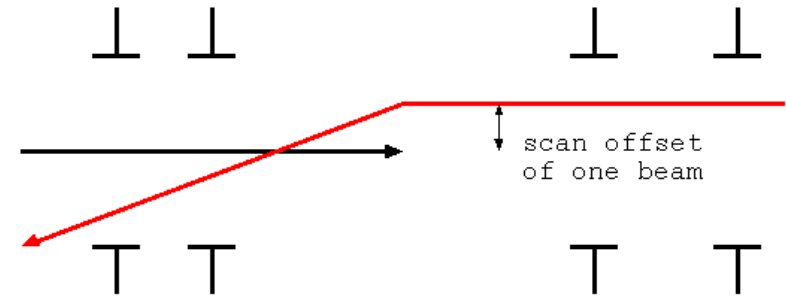
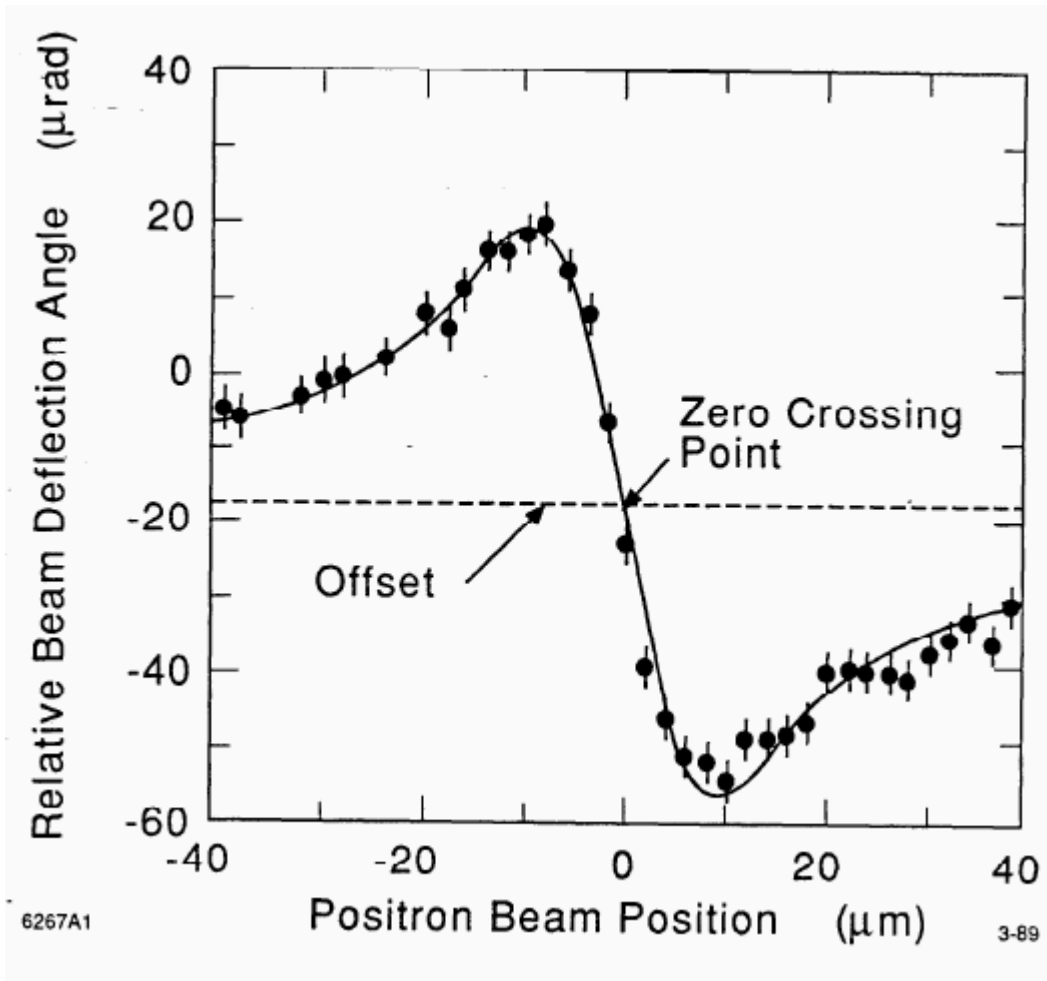
$$\begin{aligned}\sigma_1^2 &= (R^1)_{11}^2 \sigma_{11} + 2R_{11}^1 R_{12}^1 \sigma_{12} + (R^1)_{12}^2 \sigma_{22} \\ \sigma_2^2 &= (R^2)_{11}^2 \sigma_{11} + 2R_{11}^2 R_{12}^2 \sigma_{12} + (R^2)_{12}^2 \sigma_{22} \\ \sigma_3^2 &= (R^3)_{11}^2 \sigma_{11} + 2R_{11}^3 R_{12}^3 \sigma_{12} + (R^3)_{12}^2 \sigma_{22}\end{aligned}$$

$$\begin{pmatrix} \sigma_1^2 \\ \sigma_2^2 \\ \sigma_3^2 \end{pmatrix} = \begin{pmatrix} (R^1)_{11}^2 & 2R_{11}^1 R_{12}^1 & (R^1)_{12}^2 \\ (R^2)_{11}^2 & 2R_{11}^2 R_{12}^2 & (R^2)_{12}^2 \\ (R^3)_{11}^2 & 2R_{11}^3 R_{12}^3 & (R^3)_{12}^2 \end{pmatrix} \begin{pmatrix} \sigma_{11} \\ \sigma_{12} \\ \sigma_{22} \end{pmatrix}$$

- $(A^t A)^{-1} A^t$ - gymnastics with error bar estimates
- Derive emittance in same way, once σ is known
- Can use several more wire scanners which allows χ^2 calculation for goodness-of-fit estimate



SLC Beam-beam Diagnostics

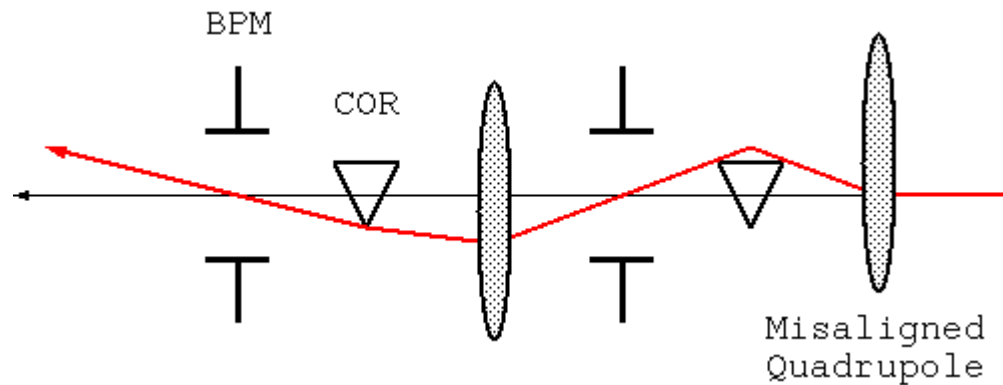


- Micron-size bunches deflect each other
- deflection angle is a measure of size and intensity
- Centering
- Beam size
- Luminosity



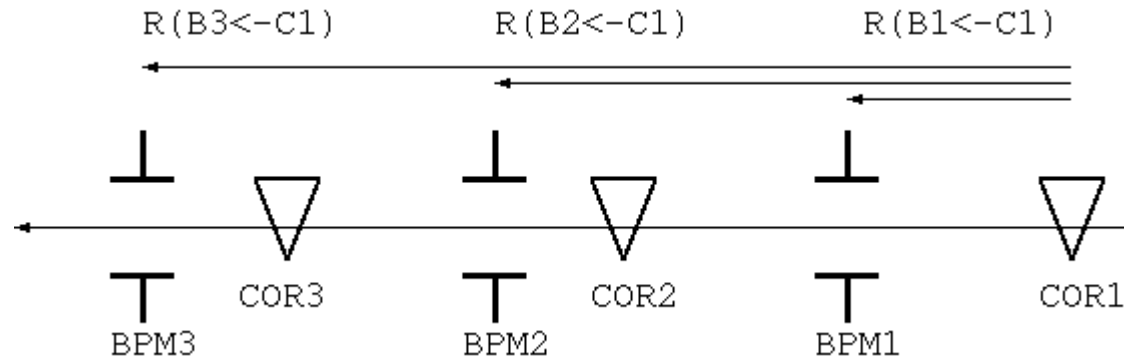
Correction: Orbit

- Observe the orbit on beam-position monitors
- and correct with steering dipoles
- How much do we have to change the steering magnets in order to compensate the observed orbit either to zero or some other 'golden orbit'.
- In beam line the effect of a corrector on the downstream orbit is given by transfer matrix R_{12}
- One-to-one steering





Orbit correction in a Beamline

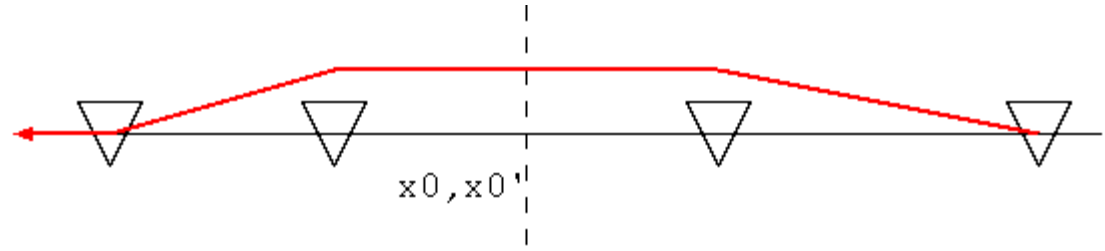


$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} R^{11} & 0 & 0 \\ R^{21} & R^{22} & 0 \\ R^{31} & R^{32} & R^{33} \end{pmatrix} \begin{pmatrix} \theta_1 \\ \theta_2 \\ \theta_3 \end{pmatrix}$$

- Observed beam positions x_1 , x_2 , and x_3
- Implicitly assume 12 or 34 matrix element in R
- Only downstream BPM can be affected
- Linear algebra problem $(A^t A)^{-1}$, etc to find required corrector excitations θ_j to explain x_i
- Reverse sign of calculated θ_j to correct the orbit to zero



4-Bump



- Use four steerers to adjust angle and position at a center point and then flatten orbit downstream of the last steerer.

$$\begin{pmatrix} x_0 \\ x'_0 \\ x_f = 0 \\ x'_f = 0 \end{pmatrix} = \begin{pmatrix} R_{12}^{01} & R_{12}^{02} & 0 & 0 \\ R_{22}^{01} & R_{22}^{02} & 0 & 0 \\ R_{12}^{f1} & R_{12}^{f2} & R_{12}^{f3} & R_{12}^{f4} \\ R_{22}^{f1} & R_{22}^{f2} & R_{22}^{f3} & R_{22}^{f4} \end{pmatrix} \begin{pmatrix} \theta_1 \\ \theta_2 \\ \theta_3 \\ \theta_3 \end{pmatrix}$$

- Solve upper part first, insert into third and fourth equation and solve that.
- Gives the required steering excitations θ_j as a function of x_0 and x'_0 → Multiknob



Multi-knobs

```
! =====  
! SCNFF IP: CLOSED BUMP Y POSITION KNOB  
! USING A3Y AND A6Y NORTH AND SOUTH  
! UNITS: BDES[KG-M]/MICROMETER  
! IN ELECTRON COORDINATE SYSTEM  
!  
SET/LABEL=YIP36  
SET/SENS=64  
SET/NOWARN  
DEF/DEV=(YCOR,FF11,5180,BDES)/COEF= -52,039E-6 ! A6Y NORTH  
DEF/DEV=(YCOR,FB69, 530,BDES)/COEF= 532,812E-6 ! A3Y NORTH  
DEF/DEV=(YCOR,FB69, 570,BDES)/COEF= 532,812E-6 ! A3Y SOUTH  
DEF/DEV=(YCOR,FF01,5180,BDES)/COEF= -52,039E-6 ! A6Y SOUTH
```

- Linear combination of device excitations as a function of a physics parameter
- Examples:
 - two steerer power supply that change position without changing the angle at IP.
 - two quadrupoles to change the z-position of one waist at the IP without changing the other.
 - two quadrupole power supplies that change the horizontal and vertical tunes independently.
- Orthogonal control of physics parameters



Correcting the Orbit in Ring

$$\begin{pmatrix} x_1 - \hat{x}_1 \\ x_2 - \hat{x}_2 \\ \vdots \\ x_N - \hat{x}_N \end{pmatrix} = \begin{pmatrix} C_{12}^{11} & C_{12}^{12} & \cdots & C_{12}^{1M} \\ C_{12}^{21} & C_{12}^{22} & \cdots & C_{12}^{2M} \\ \vdots & \vdots & \ddots & \vdots \\ C_{12}^{N1} & C_{12}^{N2} & \cdots & C_{12}^{NM} \end{pmatrix} \begin{pmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_M \end{pmatrix}$$

- x_i are the measured positions
- x^\wedge is the desired orbit
- Its back to linear algebra again
- Bad placement, $M < N$, $N < M \rightarrow$ least squares, SVD, Micado



Inversion Algorithms

- $N=M$ and response matrix well-behaved

$$\vec{\theta} = -A^{-1}(\vec{x} - \hat{\vec{x}})$$

- $M < N$: too few correctors, least squares

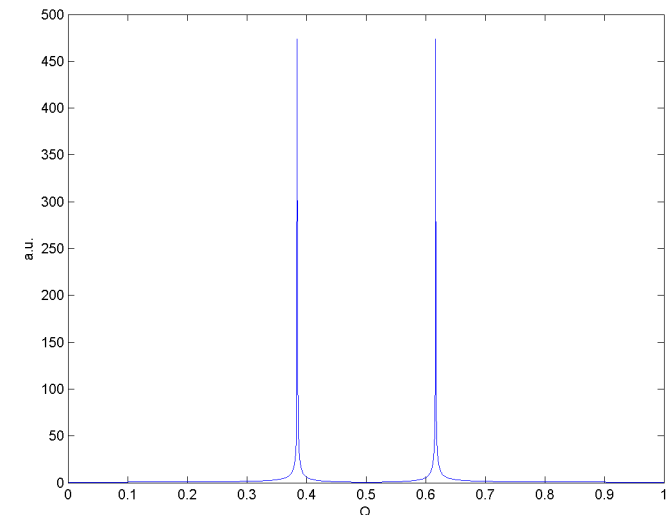
$$\vec{\theta} = (A^T A)^{-1} A^T \Delta \vec{x}$$

- $M > N$ or degenerate , SVD
- Micado: pick the most effective, fix orbit, the next effective,... (Householder transformations)
 - good for large rings with many BPM and COR



Tune Errors

- Solenoidal fields
- Unknown quadrupole geometry (eff. length)
- Power supply calibration errors
- Off-center orbit in Sextupoles
- Measure tune by exciting transverse oscillations and looking at FFT of positions
- Is it Q or $1-Q$?
- Fix by tweaking quads.





Tune correction

- Consider effect of single quadrupole on the tune

$$\begin{aligned} R &= \begin{pmatrix} 1 & 0 \\ -1/f & 1 \end{pmatrix} \begin{pmatrix} \cos(2\pi Q) & \beta \sin(2\pi Q) \\ -\sin(2\pi Q)/\beta & \cos(2\pi Q) \end{pmatrix} \\ &= \begin{pmatrix} \cos(2\pi Q) & \beta \sin(2\pi Q) \\ -\sin(2\pi Q)/\beta - \sin(2\pi Q)/f & \cos(2\pi Q) - \beta \sin(2\pi Q)/f \end{pmatrix} \end{aligned}$$

- $Tr(R) = 2 \cos(2\pi(Q+\Delta Q))$
- $\Delta Q \approx \beta/4\pi f$ (\sim beta and quad strength $1/f$)
- Use 2 quadrupoles with different β_x and β_y to correct both horizontal and vertical tune



Summary

- Discussed several devices that determine
 - position,
 - size
 - tune
- Methods to correct errors of
 - position, or the orbit
 - tune
- These are the two correction procedures that are most commonly done in a storage ring