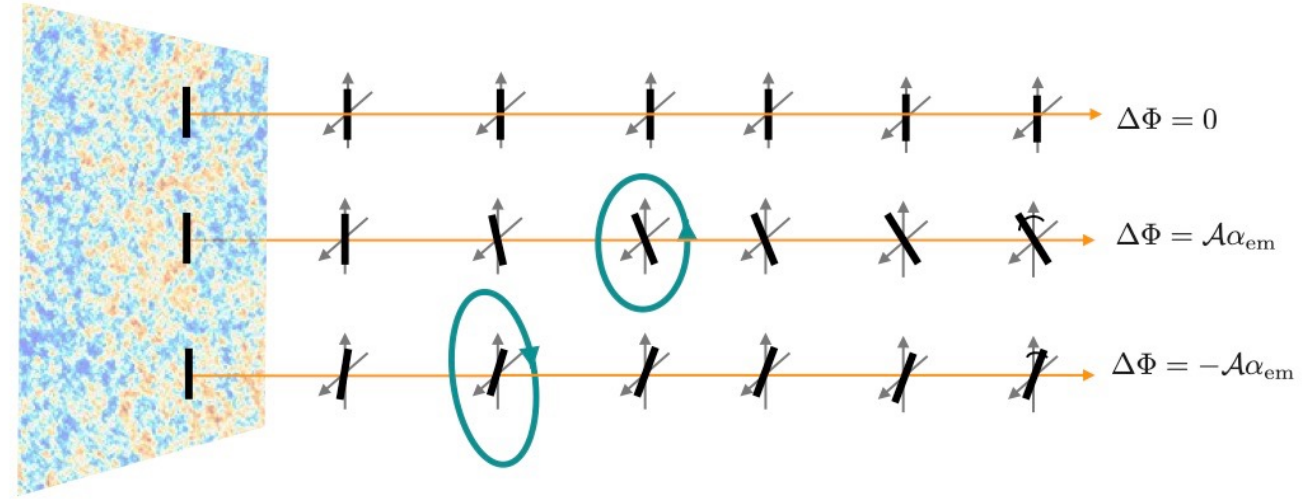


Looking through loops: CMB birefringence from axion strings



Andrew Long
Rice University
@ Axions in Stockholm
June 30, 2025



[2103.10962, 2208.08391, 2306.07351, 2411.05002]



Mudit Jain
(Kings postdoc)

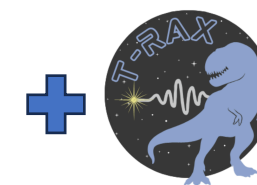


Ray
Hagimoto
(Rice U grad)

+ Mustafa Amin (Rice U faculty)

Summary

- If a [hyper-light axion-like particle](#) exists in Nature, the associated cosmological [network of axion strings](#) can leave an imprint on [CMB polarization](#) through birefringence
- We use existing [measurements of anisotropic birefringence](#) (Planck, SPT, ...) to place constraints on this scenario. Next-generation telescopes (CMB-S4) will probe $O(1)$ electromagnetic anomaly coefficients and thereby probe the axion's UV embedding
- We find that it is difficult (but not impossible!) to reconcile the [detection of isotropic birefringence](#) with strong limits on anisotropic birefringence coming from axion strings
- We argue that measurements of anisotropic birefringence could not only reveal the presence of a hyper-light ALP in Nature, but also lead to a [measurement of its mass](#)
- [Machine learning](#) methods (spherical CNN) may prove useful to help to detect the subtle non-Gaussian signal of axion strings in next-generation CMB polarization data



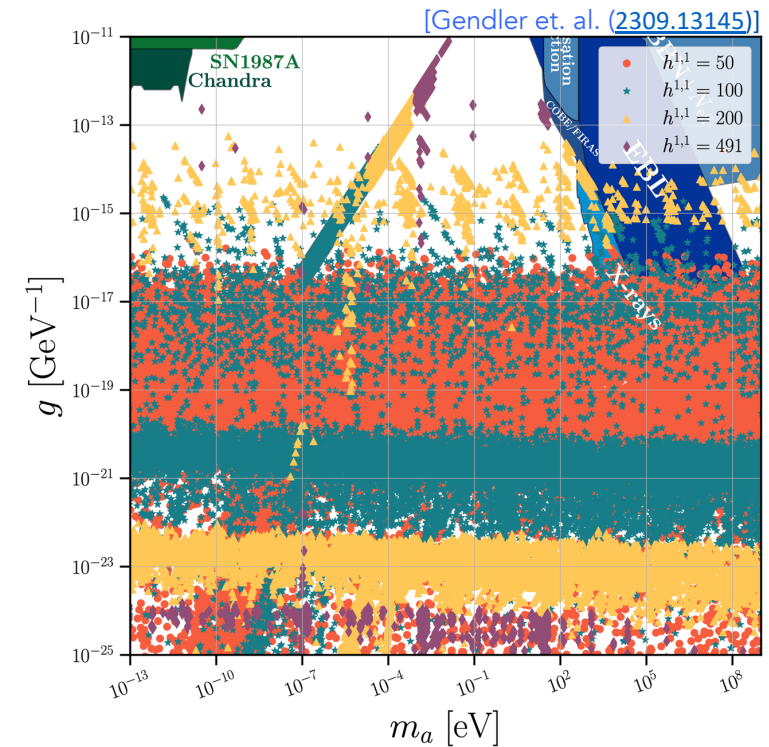
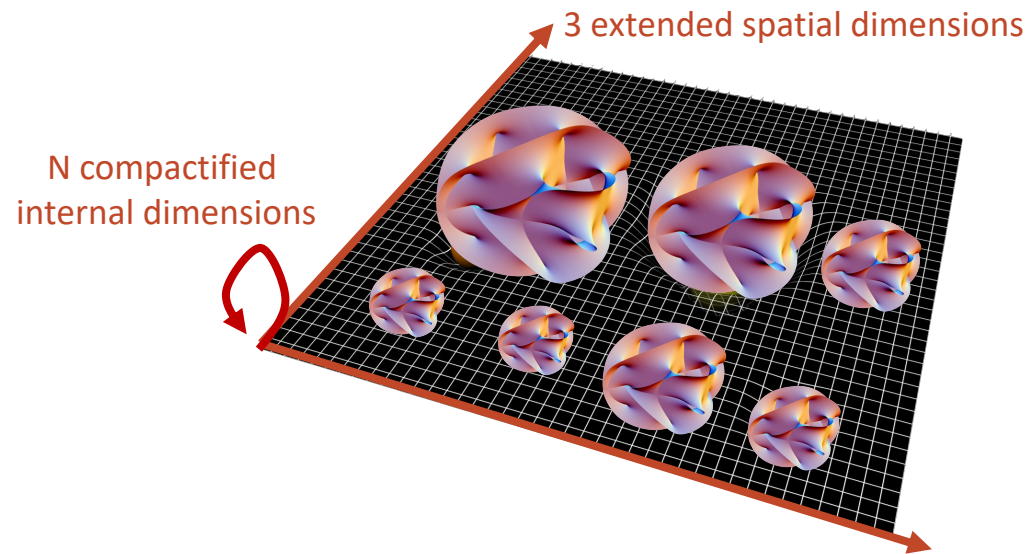
axion-like particles & cosmic axion strings

Theory landscape: axion-like particles

axion-like
particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

ALPs from extra dimensions
(such as string theory)

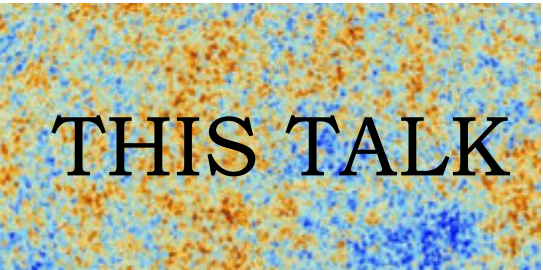


Theory landscape: axion-like particles

axion-like
particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

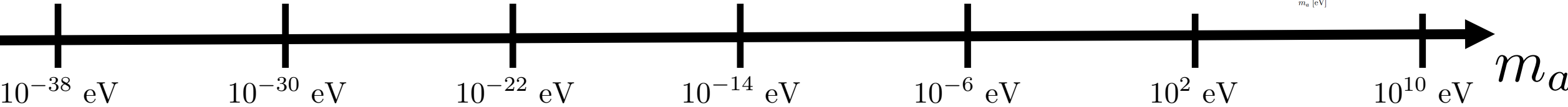
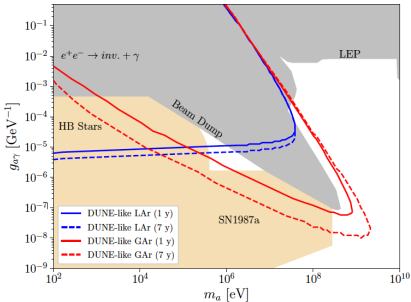
hyper-light axion-like particles
(testable with cosmology)



ultra-light axion-like particles
(dark matter candidate)

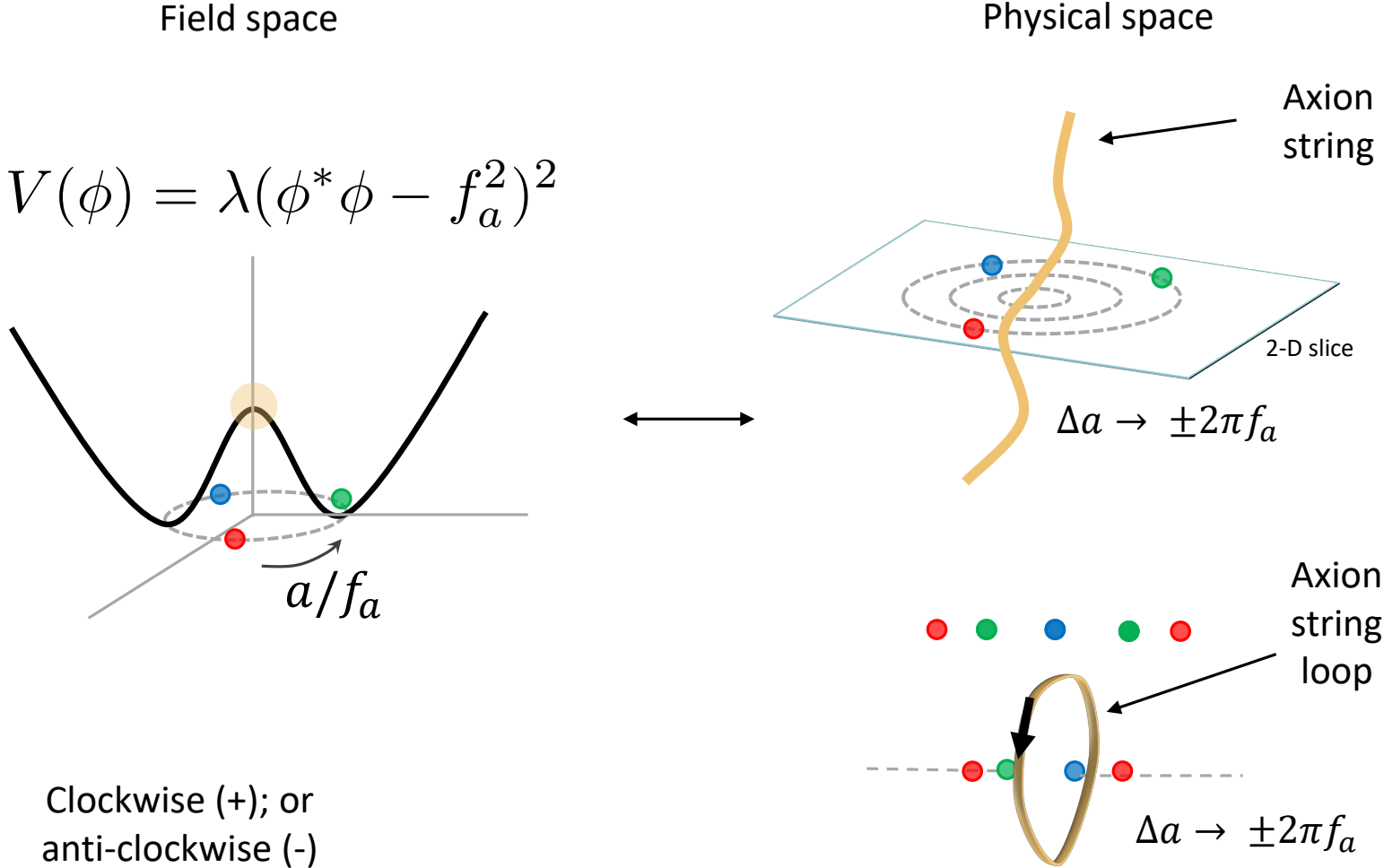


heavy axion-like particles
(testable in the lab)



ALPs can form axion strings

[Kibble (1976)]
[Vilenkin & Vachaspati (1987)]



string thickness
= microscopic

string length
= cosmological

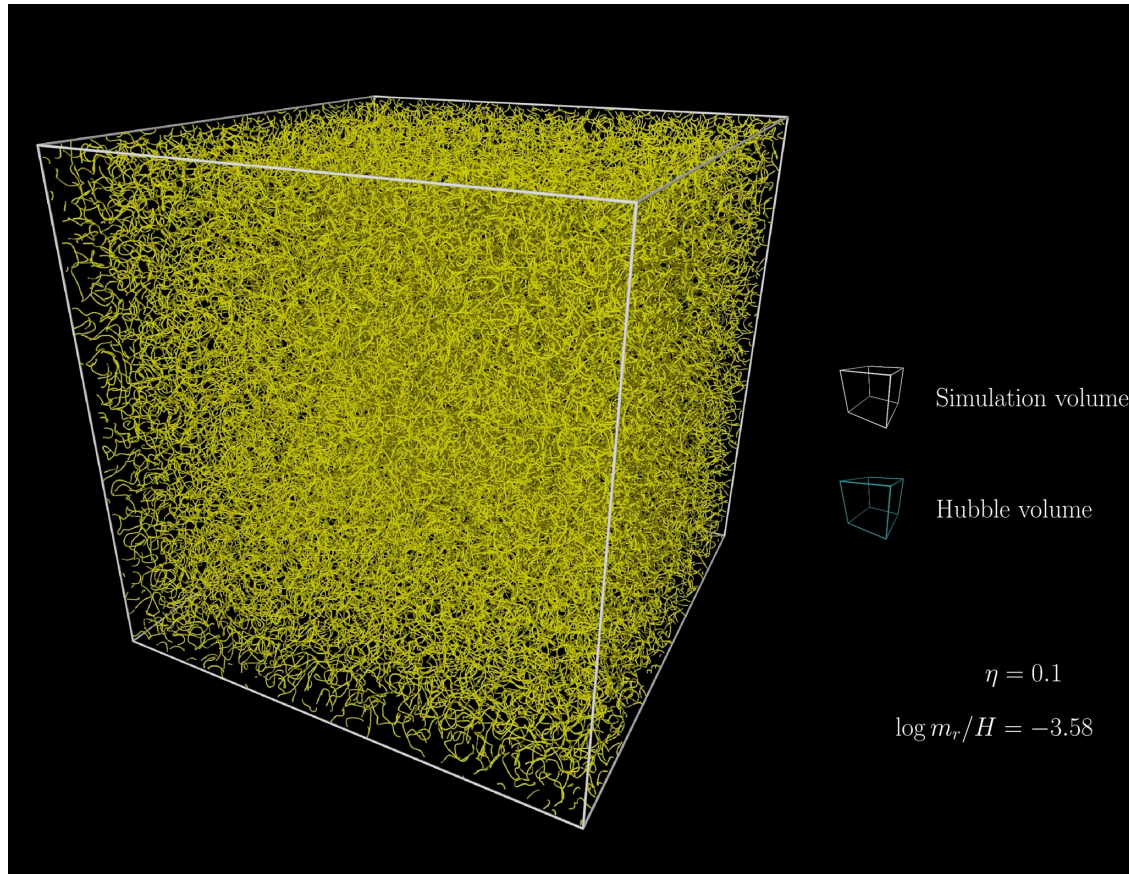
assume: $T_{RH} > f_a$

image credit: Mudit Jain (2021)

A cosmic string network

[Buschmann et. al. (2022)]

string network simulation:



simulations show:

- long strings intersect and reconnect
- reconnections form loops
- loops emit axions and collapse

so, the network evolves into the scaling regime:

- typical string length tracks Hubble
- average energy density tracks Hubble

so, in the universe today we expect:

- order 10 strings per Hubble volume
- string loops with length $\sim$ Hubble scale

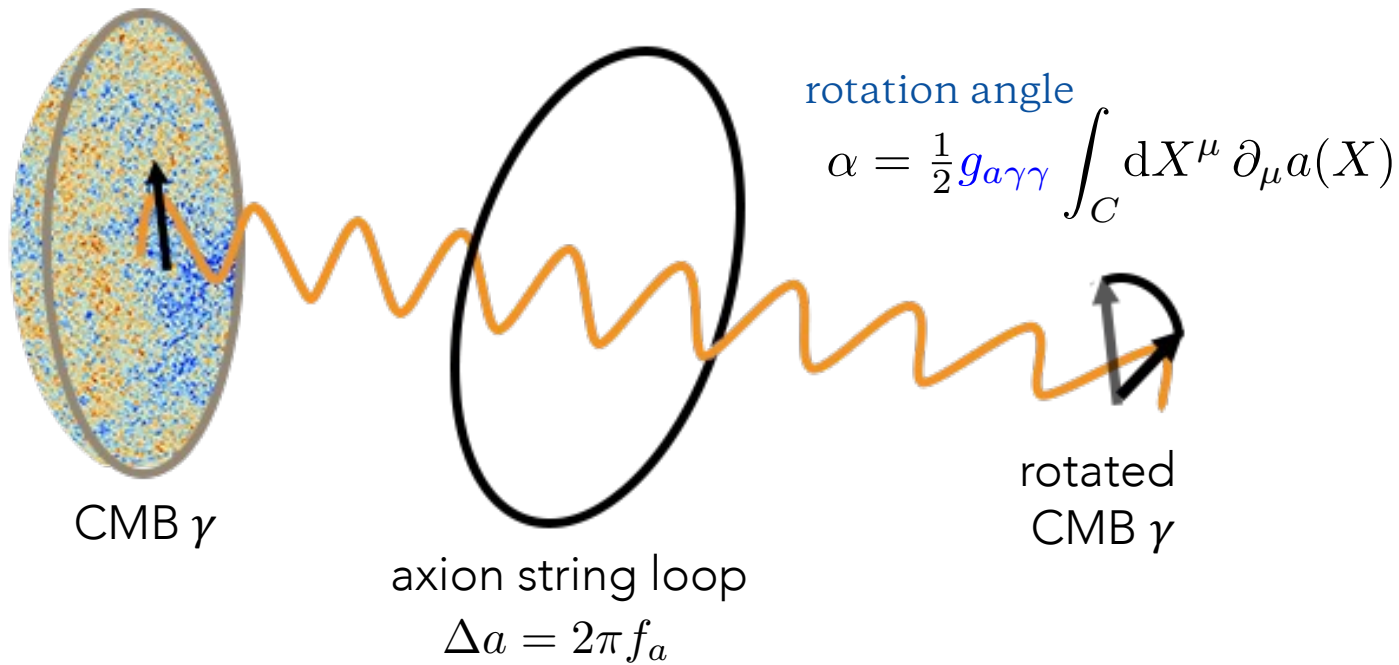
How can we detect axion strings in the Universe today?

birefringence
from axion strings

How could we detect an axion string?

[Harvey & Naculich (1989)], [Carroll, Field, Jackiw (1990,91)], [Harari, Sikivie (1992)]
 [Fedderke, Graham, Rajendran (2019)], [Agrawal, Hook, Huang (2019)]
 [Yin, Dai, Ferraro (2021) & (2023)]

axion-induced birefringence:
 an electromagnetic wave
 traveling through a varying axion field
 has its plane of polarization rotated



assume interaction
 with electromagnetism:
 standard Chern-Simons coupling

$$\mathcal{L}_{\text{int}} = -\frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$$

$$g_{a\gamma\gamma} = -\mathcal{A} \frac{\alpha_{\text{em}}}{\pi f_a}$$

$$\mathcal{A} = \sum Q_{\text{PQ}} Q_{\text{em}}^2 \sim \# / 9$$

$$\alpha = g_{a\gamma\gamma} \pi f_a$$

$$\equiv -\mathcal{A} \alpha_{\text{em}}$$

$$\approx -0.42^\circ \mathcal{A}$$

* birefringence can be measured through E-B cross correlation

Modeling anisotropic birefringence from strings

[Jain, AL, Amin (2021)]

The loop-crossing model

- Circular & planar loops
- Randomize loop orientation
- Randomize loop location in space
- All loops same radius at any time
- Loop radius evolves tracking Hubble

$$R(t) = \zeta_0 / H(t)$$

- Number of loops tracks Hubble

$$\rho(t) = \xi_0 \mu(t) H(t)^2$$

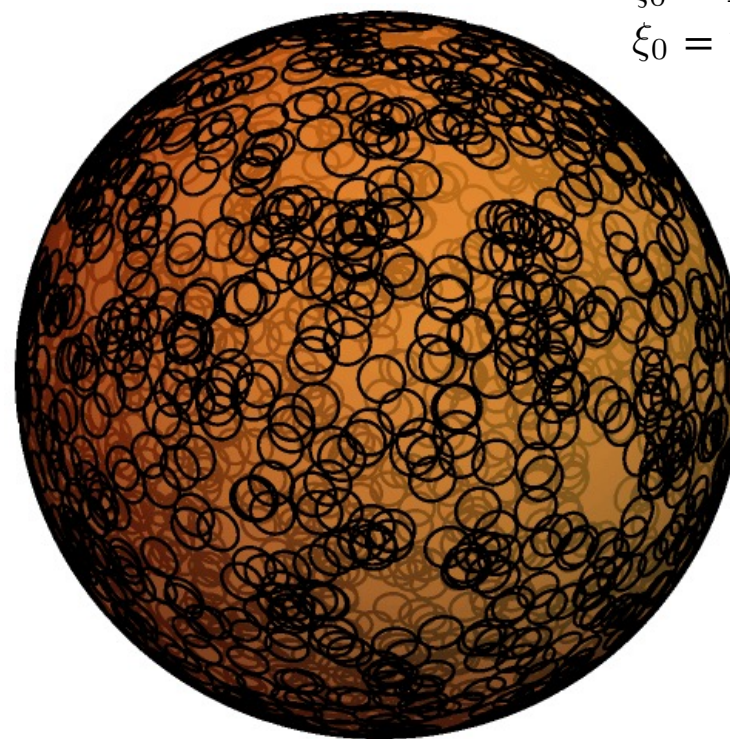
Model Parameters

$$\{m_a, \mathcal{A}, \zeta_0, \xi_0\}$$

loop-crossing model

$$\zeta_0 = 1.0$$

$$\xi_0 = 1.0$$

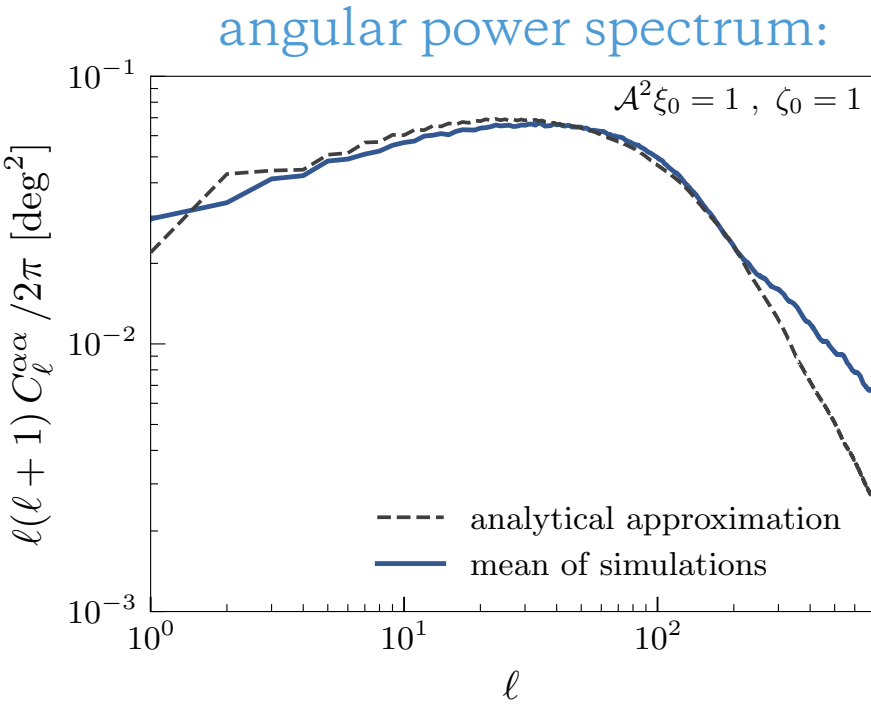
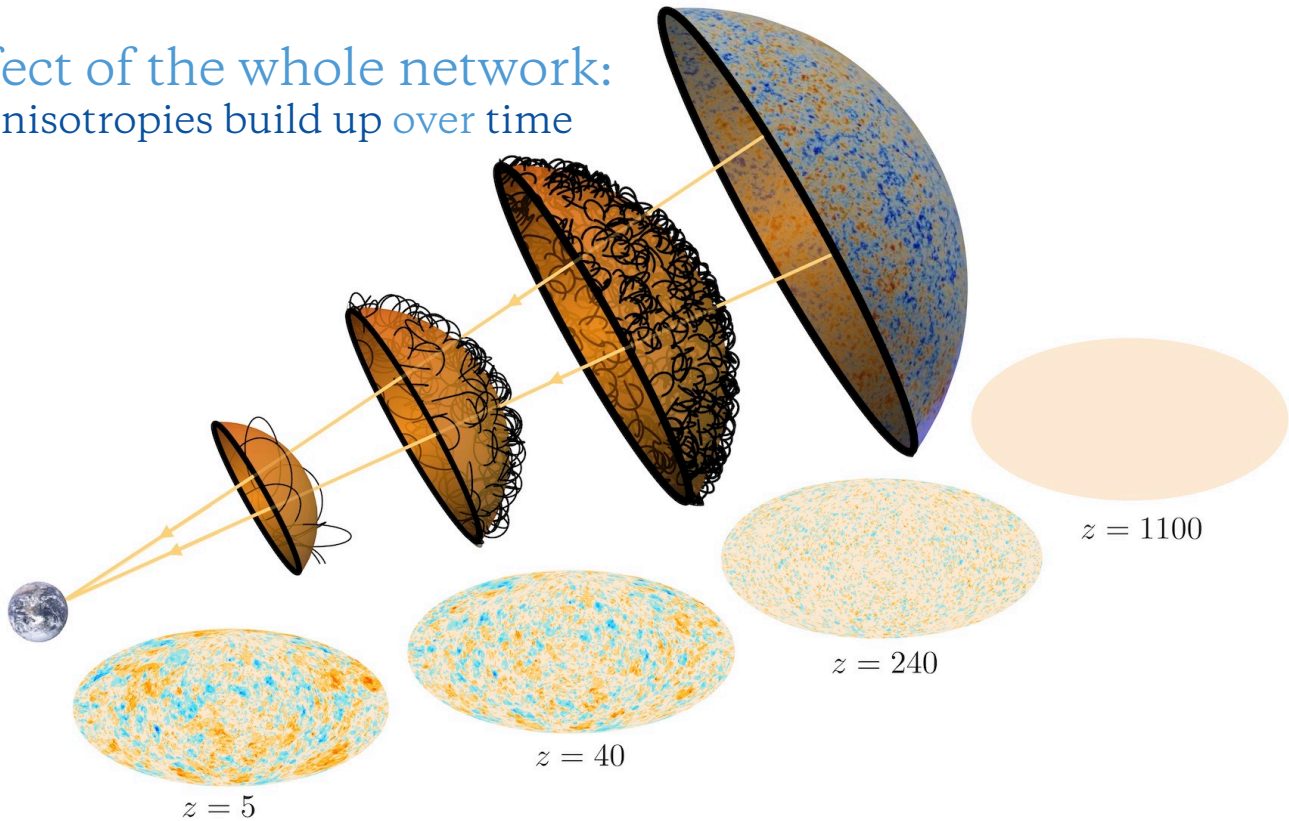


early time -> small loops
late time -> large loops

Expected birefringence signal

[Jain, AL, Amin, arXiv:2103.10962]
[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

effect of the whole network:
anisotropies build up over time



approx. scale invariant up to $l \sim 100$

degeneracy: $\langle \alpha\alpha \rangle \sim \mathcal{A}^2 \xi_0$

* need $m_a \lesssim 3H_{\text{cmb}} \approx 10^{-28}$ eV for the network to survive until after recombination

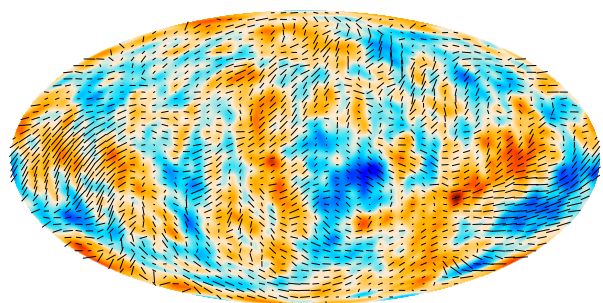
Effect on CMB polarization

How does birefringence affect the CMB's temperature and polarization?

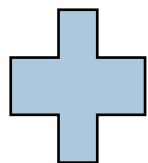
$$T(\hat{n}) \rightarrow T(\hat{n})$$

$$[Q \pm iU](\hat{n}) \rightarrow [(Q \pm iU)e^{\pm 2i\Delta\Phi}](\hat{n})$$

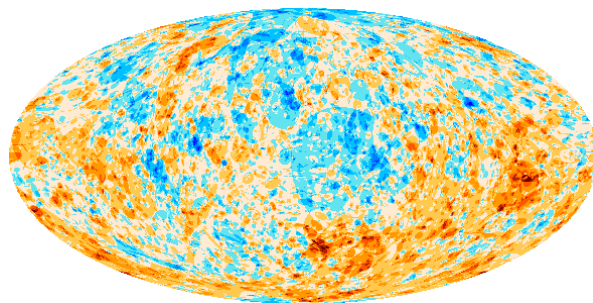
primordial CMB sky



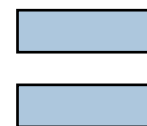
-160 160



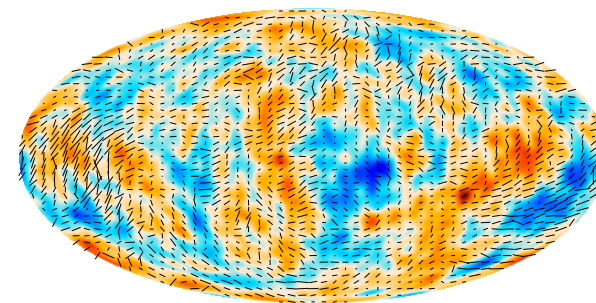
axion string-induced birefringence angle



-60 60
α [deg]
(exaggerated by ~30x)

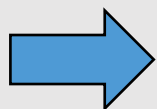
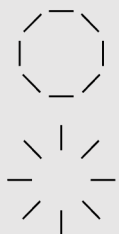


Planck's CMB sky



-160 160

E – mode
pol pattern



B – mode
pol pattern



Signal of axion string-induced cosmological birefringence

$$\begin{cases} \langle TB \rangle \neq 0 \\ \langle EB \rangle \neq 0 \end{cases}$$

$$C_{\ell}^{\text{EB}} \sim \sin(4\Delta\Phi) (C_{\ell}^{\text{EE}} - C_{\ell}^{\text{BB}})$$

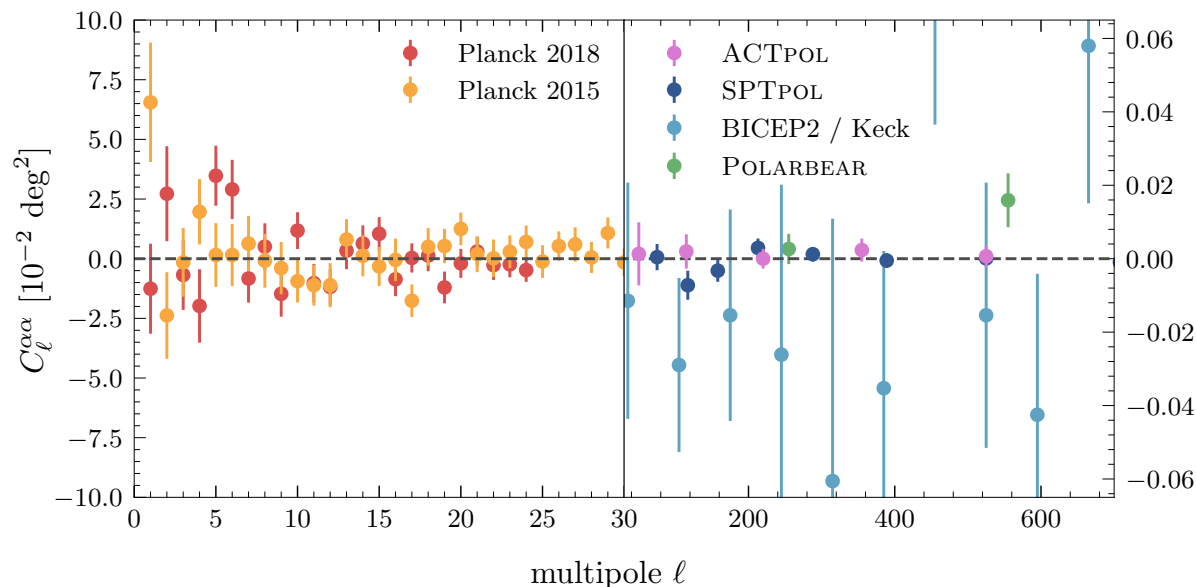
Constraints from anisotropic birefringence

[Jain, AL, Amin, arXiv:2103.10962]

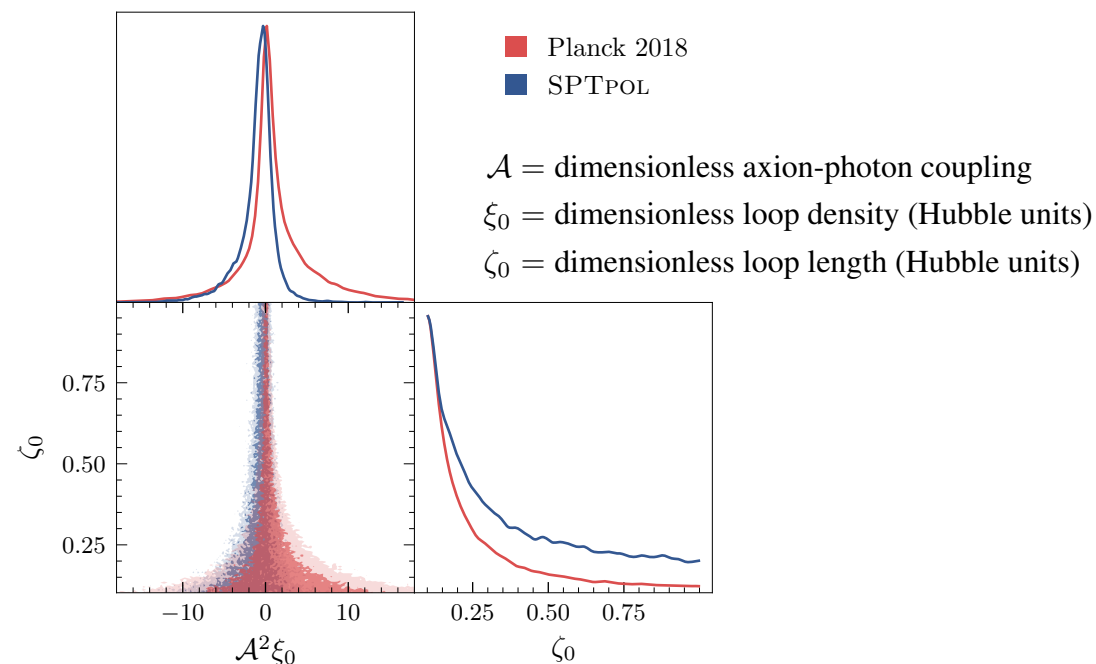
[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

see also: Yin, Dai, & Ferraro (2111.12741)

measurements of CMB polarization:
no evidence for anisotropic birefringence



a constraint on axion strings networks
& their coupling to electromagnetism:



constraints:

SPTPOL: $\mathcal{A}^2 \xi_0 < 3.7$ at 95% CL

Implications

CMB observations constrain:

$$\text{SPTPOL: } \mathcal{A}^2 \xi_0 < 3.7 \text{ at 95\% CL}$$

Typical axion-photon coupling:

$$\mathcal{A} = 1/3$$

Typical loop abundance:

$$\xi_0 = 30$$


$$\mathcal{A}^2 \xi_0 \approx 3.3$$

... already probing an O(1) anomaly coefficient!
... but still large uncertainties in ξ_0 (from sims)

Projected sensitivity

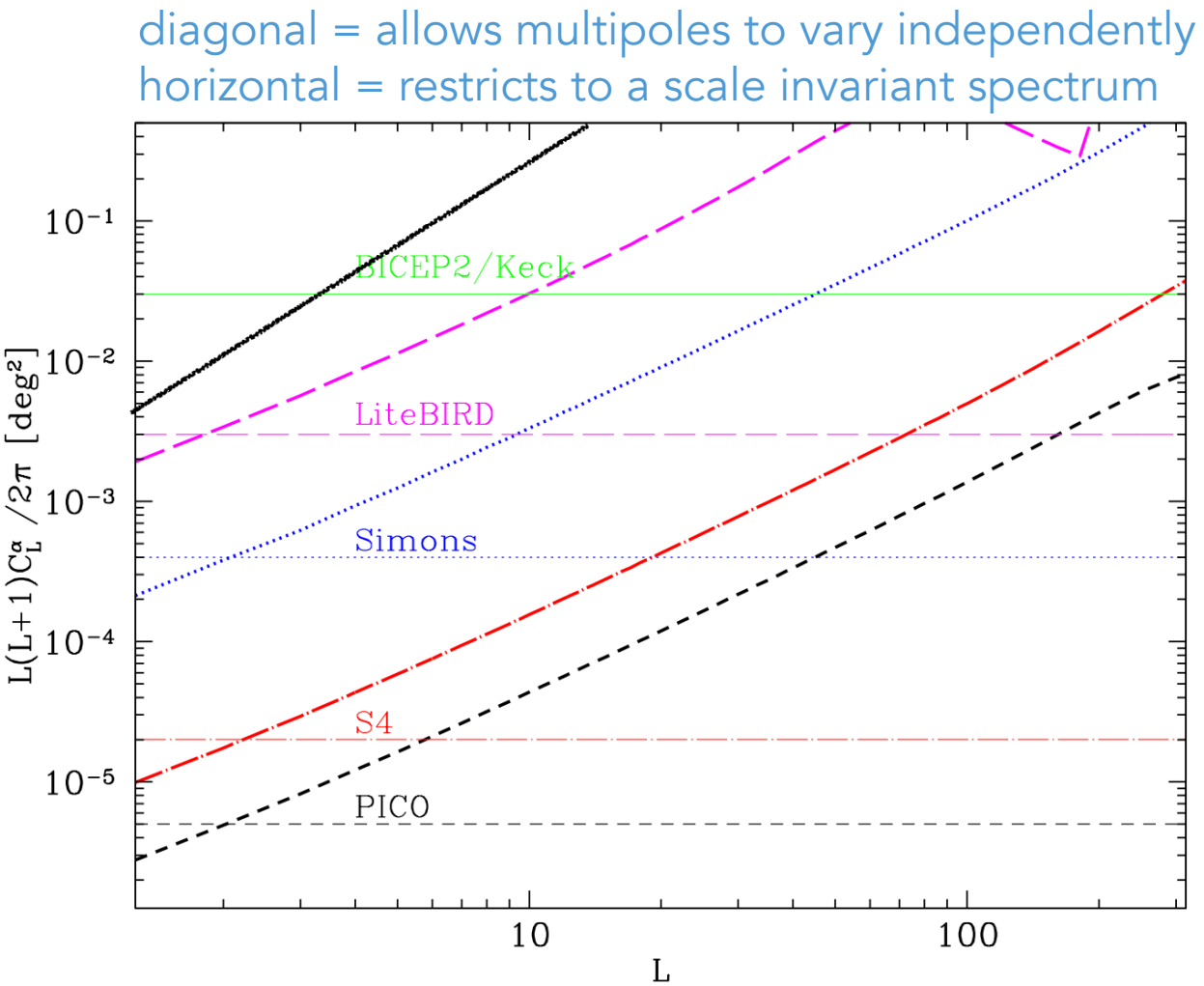
Pogosian et. al. (2019)

future telescopes
probes of isotropic + aniso. birefringence

Current			LiteBIRD			SO			CMB-S4-like			PICO		
α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$
-	-	-	1.3	2.7	0.9	0.56	3	0.29	0.1	1.4	0.065	0.05	0.4	0.035
-	-	-	1.5	3.3	1.0	0.66	4	0.35	0.11	2.0	0.08	0.06	0.5	0.04
-	-	-	1.4	3.5	1.0	0.64	5.0	0.4	0.13	2.5	0.09	0.08	1.2	0.06
30	2	3	1.6	4.0	1.1	0.71	5.5	0.4	0.15	3.3	0.1	0.09	1.4	0.065

BLE II. Current and forecasted 68% CL bounds on the uniform and the anisotropic CPR parameters.

$$A_\alpha = L(L + 1)C_L^\alpha/2\pi$$



what about
isotropic
birefringence

Are strings responsible for isotropic birefringence?

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

reported detection of isotropic birefringence:
same rotation angle across the whole sky
(using *Planck* & *WMAP* data)

$$\alpha_{00} = -1.21^\circ \pm_{-0.32^\circ}^{+0.33^\circ} \text{ (68\% CL)}$$

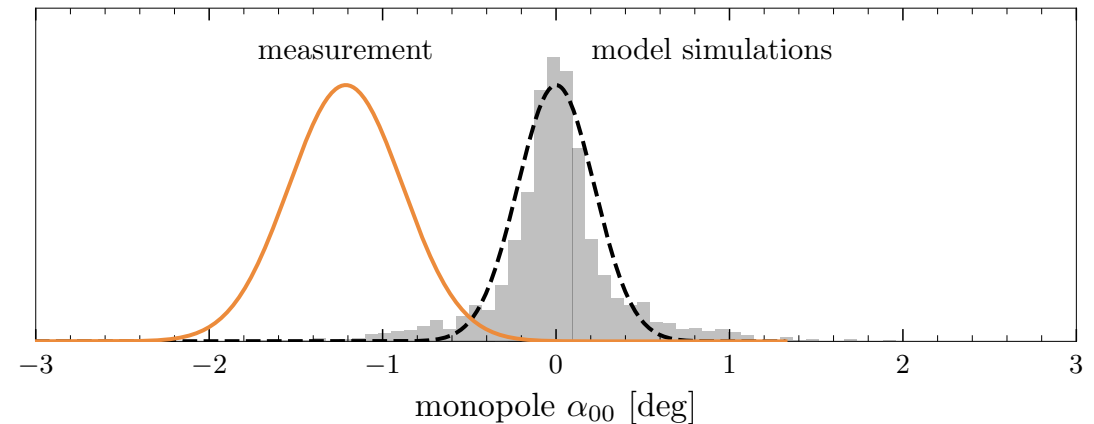
[Minami & Komatsu (2020)]

[Diego-Palazuelos et. al. (2022)]

[Eskilt (2022)], [Eskilt & Komatsu (2022)]

[Eskilt et. al. (2023)]

our conclusion: the isotropic signal is in tension
with limits on anisotropic BF if they both arise
from axion-string induced birefringence



note that: $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^\circ$

Are strings responsible for isotropic birefringence?

[Ferreira, Gasparotto, Hiramatsu, Obata, & Pujolas (2023)]

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[Minami & Komatsu (2020)]

[Diego-Palazuelos et. al. (2022)]

[Eskilt (2022)], [Eskilt & Komatsu (2022)]

[Eskilt et. al. (2023)]

loopholes allowing large iso-BF

(1) environmental effects

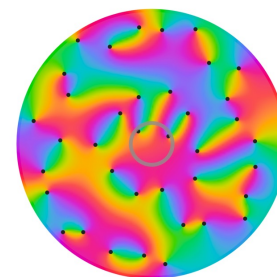
a nearby loop in our Hubble volume
would dominate the isotropic signal

(2) Hubble-scale gradients

the massless axion field is expected to be
inhomogeneous on the Hubble scale

(3) late-forming network

if the string network is not present just after
recombination, the small-scale BF is suppressed



note that: $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^\circ$

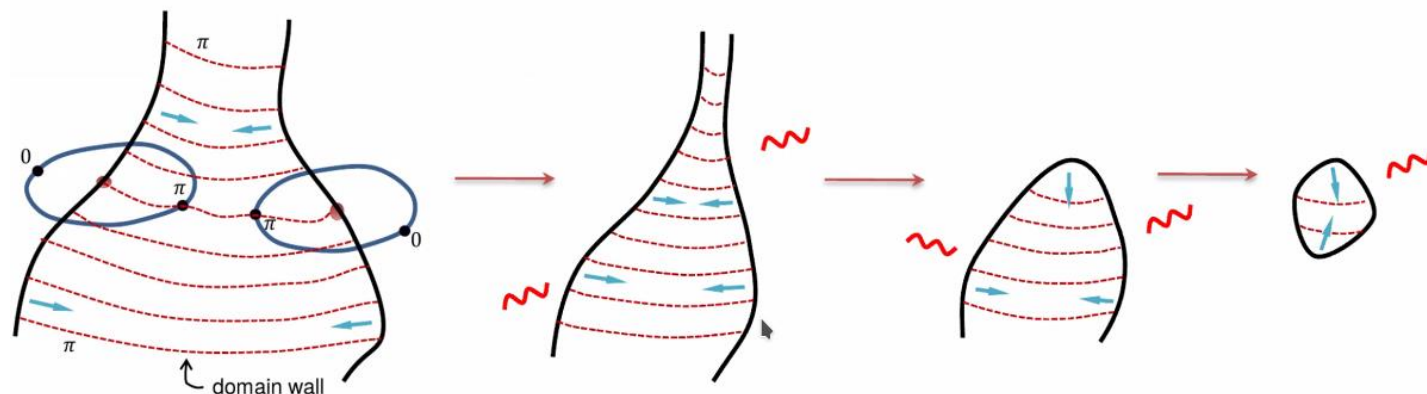
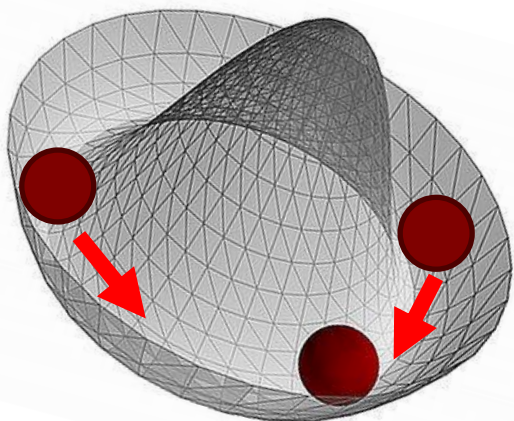
effect of
varying ALP mass

Collapse of the string-wall network

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

Axion strings become connected together by domain walls

... the string-wall network collapses (for $N_{\text{dw}} = 1$)



let's consider: $\begin{cases} m_a \lesssim 3H_{\text{CMB}} \simeq 3 \times 10^{-29} \text{ eV} & \text{(string network survives until after recombination)} \\ m_a \gtrsim 3H_0 \simeq 5 \times 10^{-33} \text{ eV} & \text{(string network collapses before today)} \end{cases}$

after the network collapses at redshift z_c the accumulation of birefringence is shut off

Impact on birefringence

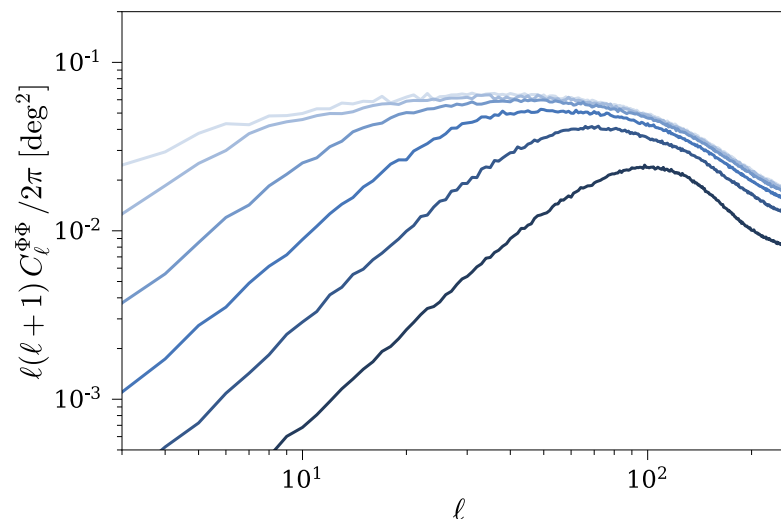
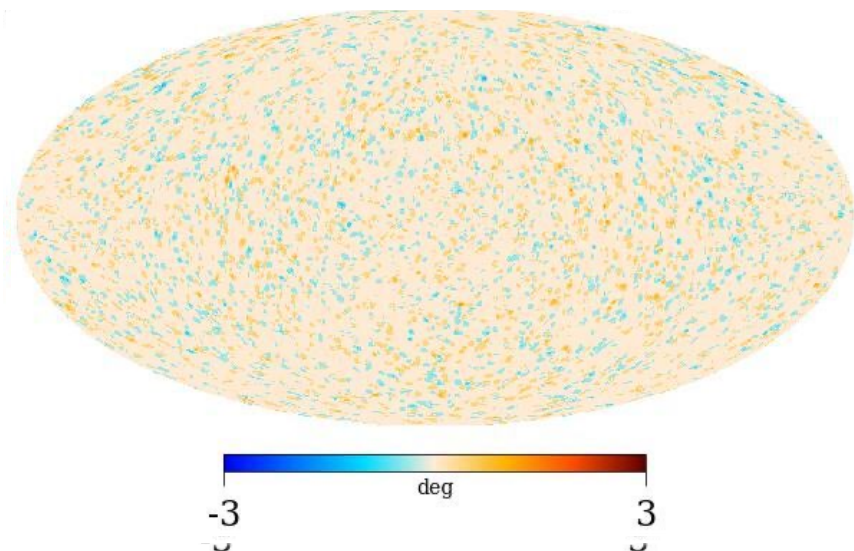
(assuming $N_{\text{DW}} = 1$)

raise the ALP mass
(network collapses earlier)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

see also: [Ferreira, Gasparotto, Hiramatsu, Obata, & Pujolas (2023)]

$$m_a = 2 \times 10^{-29} \text{ eV} \quad (z_c = 404)$$



strong scale dependence $\rightarrow$ possible to measure m_a

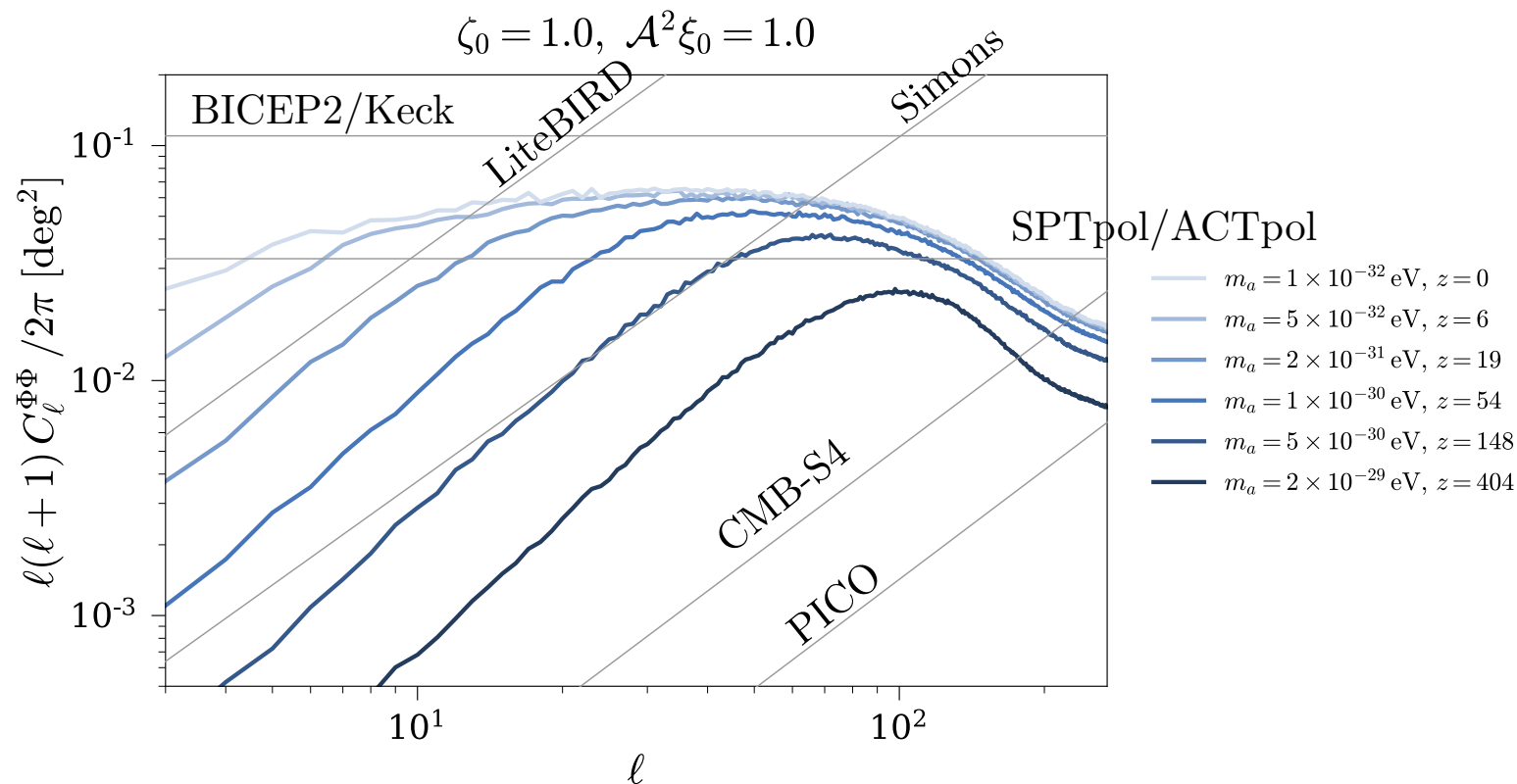
Implications

(assuming $N_{\text{DW}} = 1$)

raise the ALP mass
(network collapses earlier)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

projections: [Pogosian et. al. (2019)]



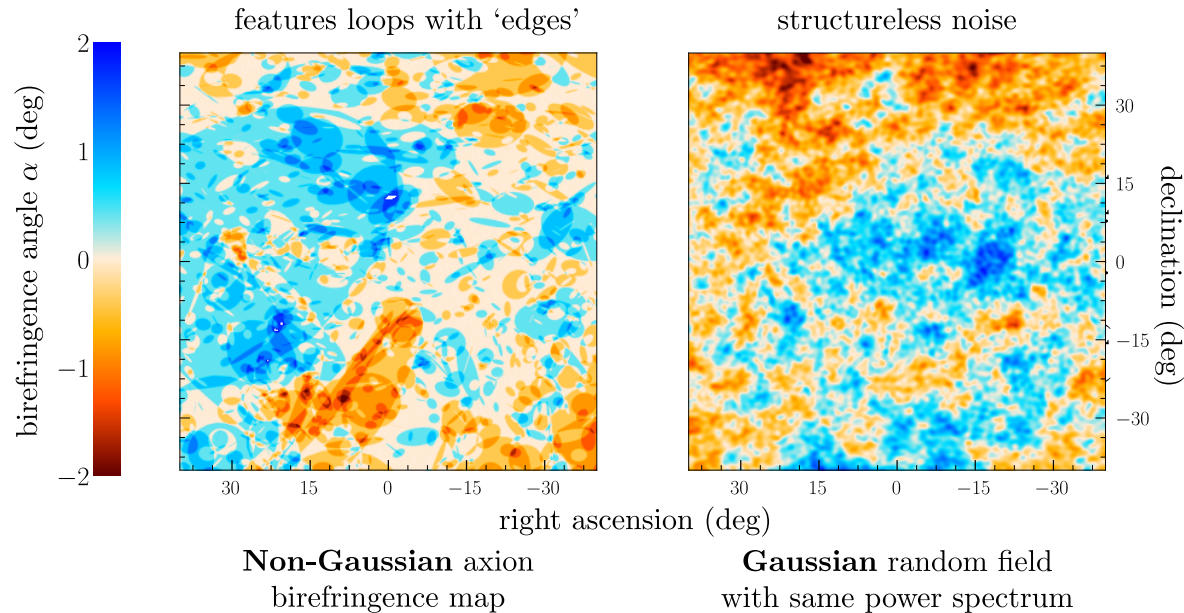
strong scale dependence $\rightarrow$ possible to measure m_a

signatures of non-Gaussianity

Birefringence non-Gaussianity

[Hagimoto & AL, arXiv:2306.07351]
see also: Yin, Dai, Ferraro (2305.02318)

axion-string induced birefringence:
loop-like features are visibly non-Gaussian



How to best quantify the non-Gaussian birefringence and develop tests to extract these features from the data?

Probing non-Gaussianity with scattering transform

[Yin, Dai, Ferraro (2023)]

std. method
power spectrum

signal: $I_0(\mathbf{x})$

plane wave: $\phi_{\mathbf{k}}(\mathbf{x})$

$$P_{\mathbf{k}}(\mathbf{x}) = \langle |I_0 * \phi_{\mathbf{k}}|^2 \rangle(\mathbf{x})$$

new method
scattering transform

wavelet: $\psi^{j,l}(\mathbf{x})$

$$I_1^{j,l}(\mathbf{x}) = \langle |I_0 * \psi^{j,l}|^2 \rangle(\mathbf{x})$$

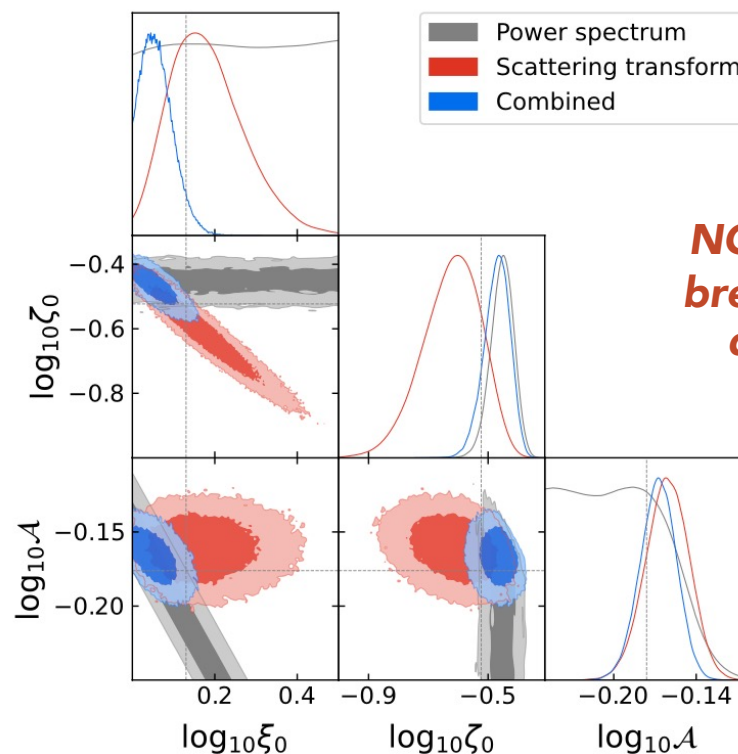
$$I_2^{j_1,l_1,j_2,l_2}(\mathbf{x}) = \langle |I_1^{j_1,l_1} * \psi^{j_2,l_2}|^2 \rangle(\mathbf{x})$$

$$s_1^j = \langle I_1^{j,l} \rangle_{\mathbf{x},l}$$

$$s_2^{j_1,j_2} = \langle I_2^{j_1,l_1,j_2,l_2} \rangle_{\mathbf{x},l_1,l_2}$$

comparison

pow-spec vs. scatt-transform



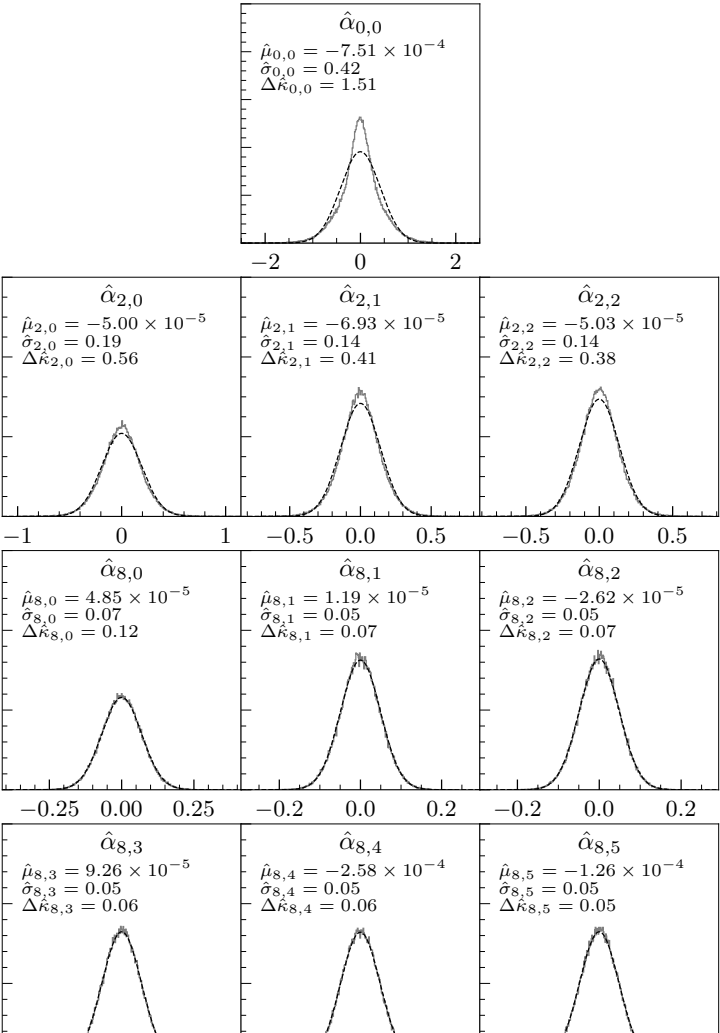
**NG information
breaks the $A^2 \xi_0$
degeneracy**

(b) $\mathcal{A}^2 \xi_0 = 0.6$, $\mathcal{A} = 2/3$, $\zeta_0 = 0.3$

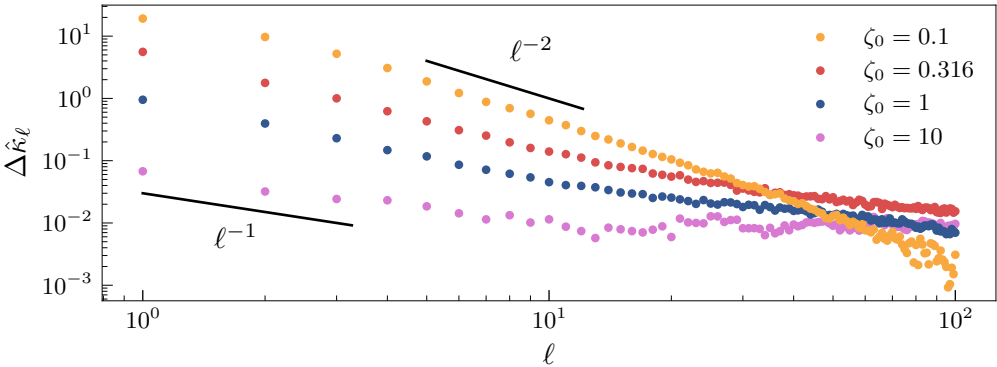
Birefringence non-Gaussianity

[Hagimoto & AL, arXiv:2306.07351]

excess kurtosis
can be O(1) at low multipoles

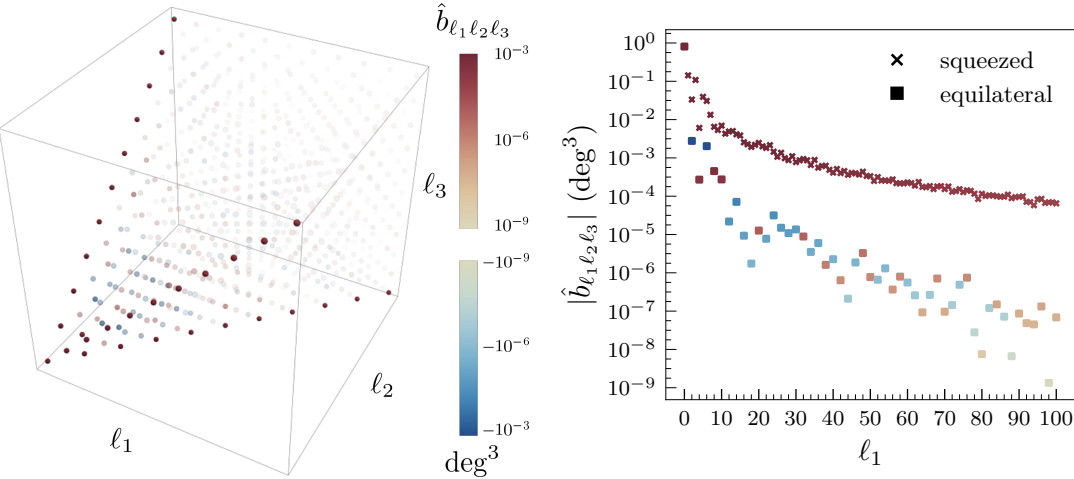


scaling with multipole index
matches well an analytic toy model



**smaller NG on smaller
scales (b/c of central
limit theorem)**

bispectrum
largest in squeezed triangle form



**NG information
breaks the $A^2 \xi_0$
degeneracy**

**a measurement of
non-G will help to tell
apart axion strings &
other sources of
birefringence**

Machine learning for axion strings

package: DeepSphere (Python)
architecture: 3 conv+pool layers

train 3 SCNN's to identify 3 LCM parameters

$$Z = \log_{10}(\zeta_0), \quad A = \log_{10}(\mathcal{A}^2 \xi_0), \quad X = \log_{10}(\xi_0^2 / \mathcal{A})$$

model parameters

mock data

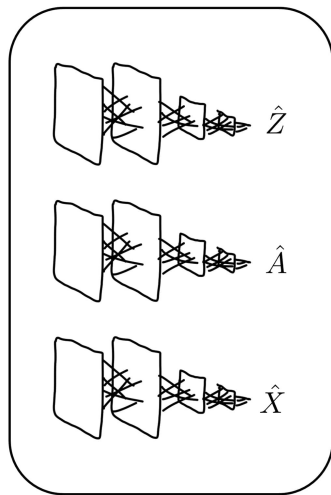
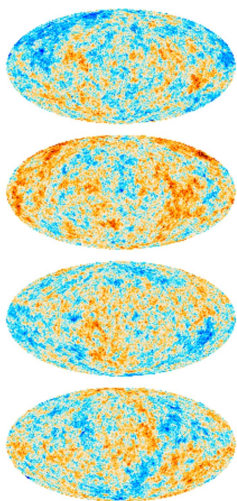
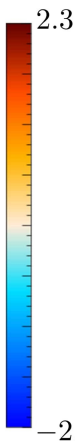
SCNN

$$Z = 0$$

$$A = 0$$

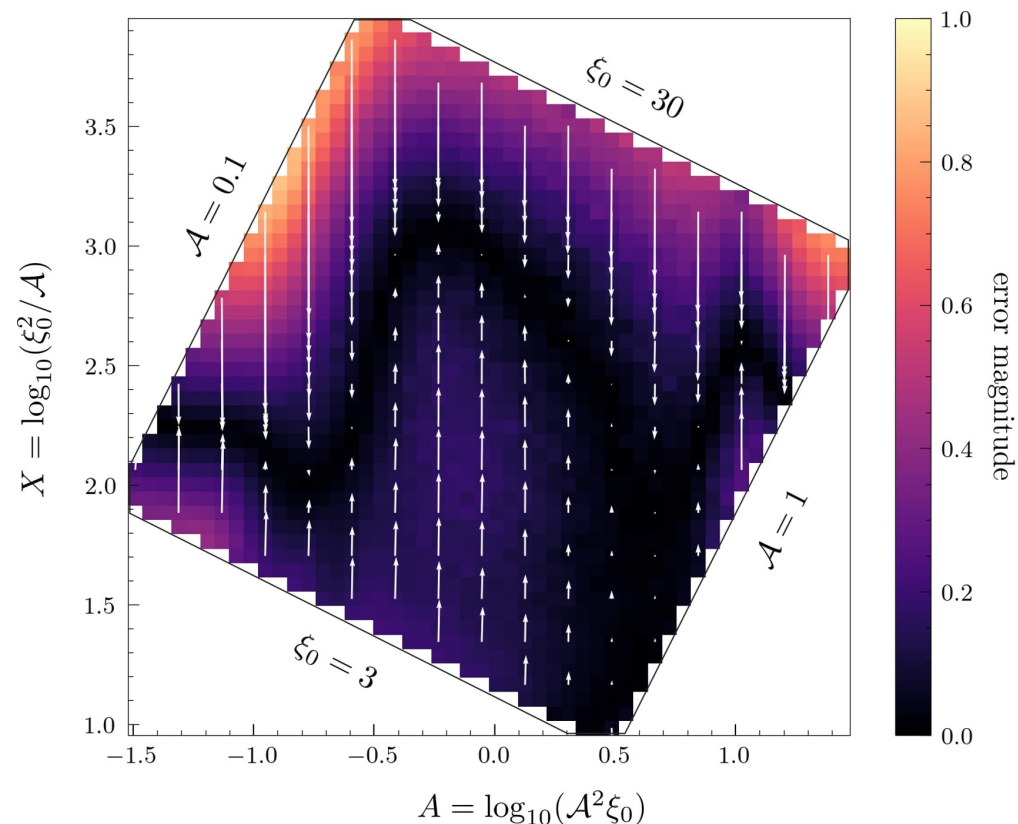
$$X = 2.5$$

$\alpha(\hat{n})$ [deg]



SCNN estimates

$\hat{Z}$	$\hat{A}$	$\hat{X}$
0.038	-0.003	2.23
0.074	-0.015	2.94
-0.030	0.020	2.88
0.031	-0.022	2.51



summary & conclusion

Terahertz-Radiometer for Axions (T-RAx)

something completely different: a proposal to search for axion dark matter in the THz gap



Andrey Baydin
(Rice)



Henry Everitt
(Rice)



Shengxi Huang
(Rice)



Junichiro Kono
(Rice)



Michael Manfra
(Purdue)



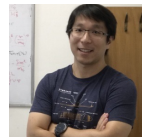
Andrew Long
(Rice)



Jaanita Mehrani
(Rice)



Kuver Sinha
(Oklahoma)

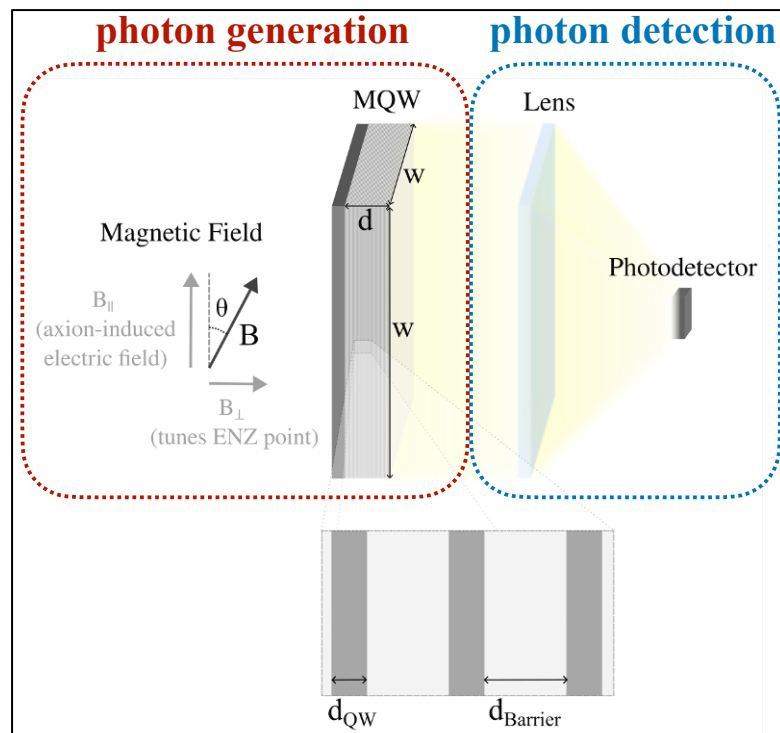


Tao Xu
(Oklahoma)

lead author

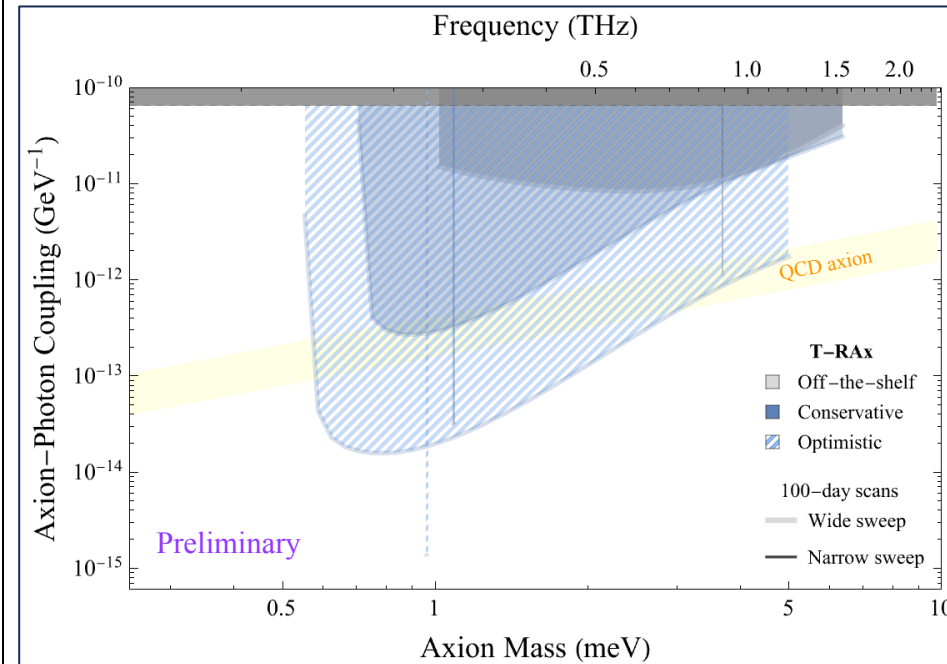


to appear on arXiv
later this summer



Epsilon-Near-Zero (ENZ) material

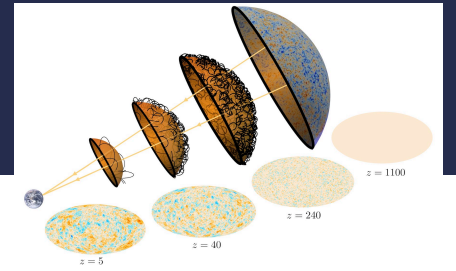
- small permittivity → boosts E-field
- realized w/ multiple quantum wells
- B-field tunes ENZ resonant freq.



Projected sensitivity

- easily beats CAST limit
- with low-enough DC rate and strong-enough B-field, T-RAx will probe QCD axion dark matter at $m_a \sim \text{meV}$

Summary



- If a [hyper-light axion-like particle](#) exists in Nature, the associated cosmological [network of axion strings](#) can leave an imprint on [CMB polarization](#) through birefringence
- We use existing [measurements of anisotropic birefringence](#) (Planck, SPT, ...) to place constraints on this scenario. Next-generation telescopes (CMB-S4) will probe $O(1)$ electromagnetic anomaly coefficients and thereby probe the axion's UV embedding
- We find that it is difficult (but not impossible!) to reconcile the [detection of isotropic birefringence](#) with strong limits on anisotropic birefringence coming from axion strings
- We argue that measurements of anisotropic birefringence could not only reveal the presence of a hyper-light ALP in Nature, but also lead to a [measurement of its mass](#)
- [Machine learning](#) methods (spherical CNN) may prove useful to help to detect the subtle non-Gaussian signal of axion strings in next-generation CMB polarization data

backup slides

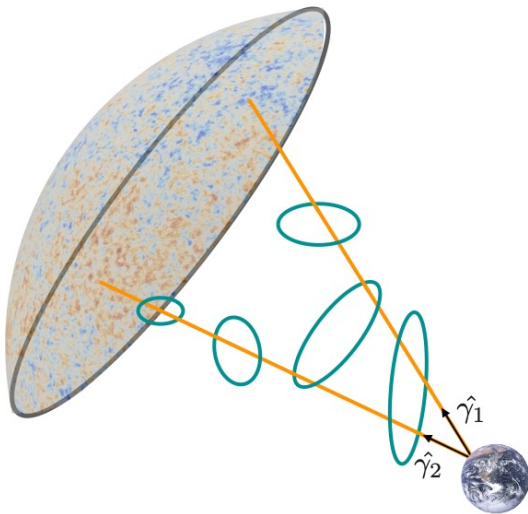


Analytical understanding

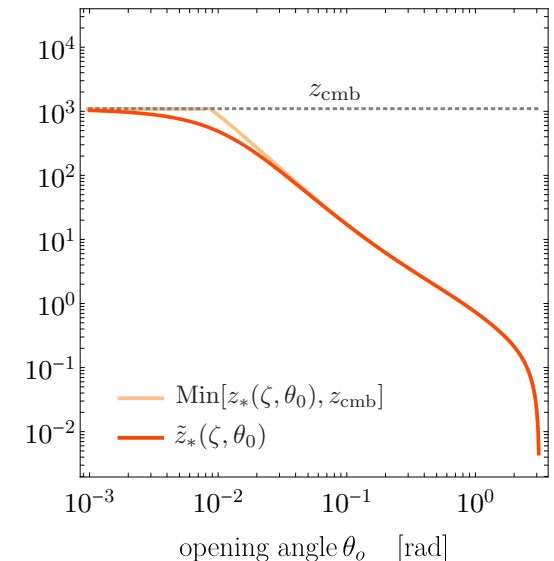
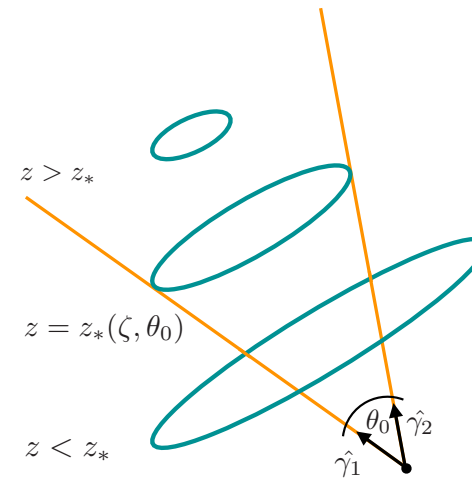
[Jain, AL, Amin, arXiv:2103.10962]

correlations accumulate
when both photons pass
through the same loops

$$\langle \alpha(\hat{\gamma}_1) \alpha(\hat{\gamma}_2) \rangle = (\mathcal{A} \alpha_{\text{em}})^2 N_{\text{both}}(\hat{\gamma}_1 \cdot \hat{\gamma}_2)$$



large-angle correlations are
established later (small z)

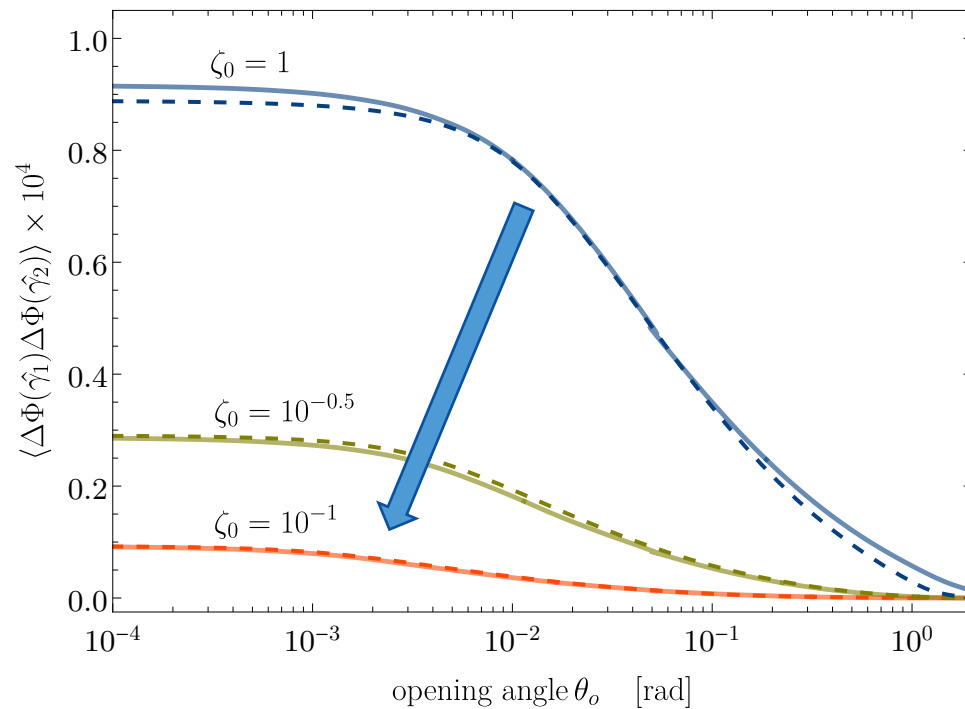


Analytical understanding

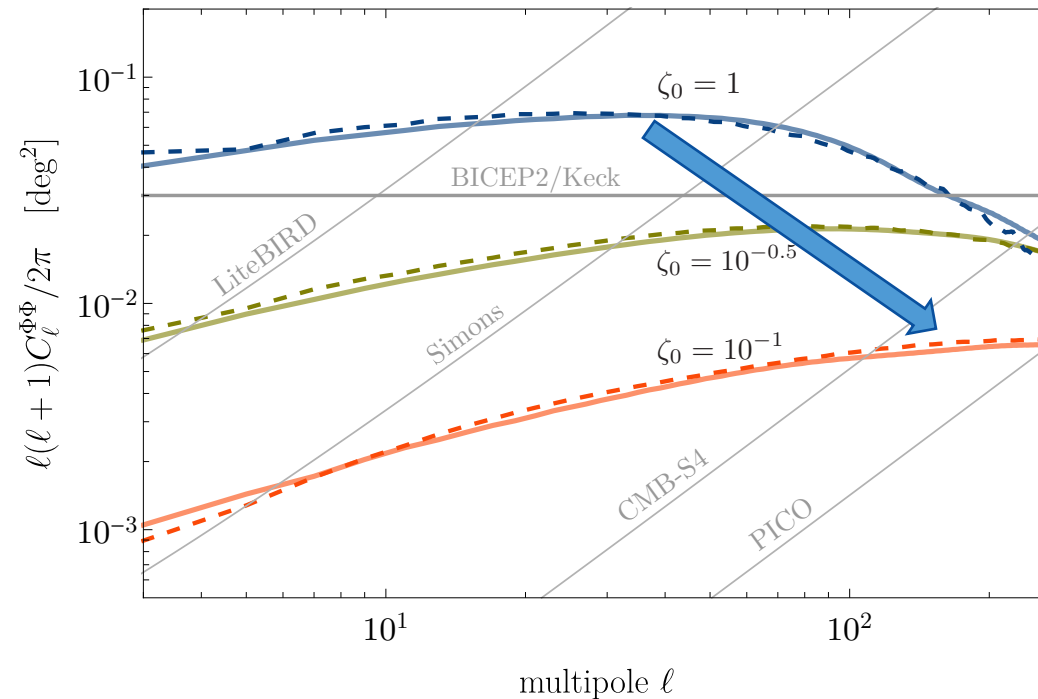
[Jain, AL, Amin, arXiv:2103:10962]

vary the loop radius: $R(t) = \zeta_0 / H(t)$

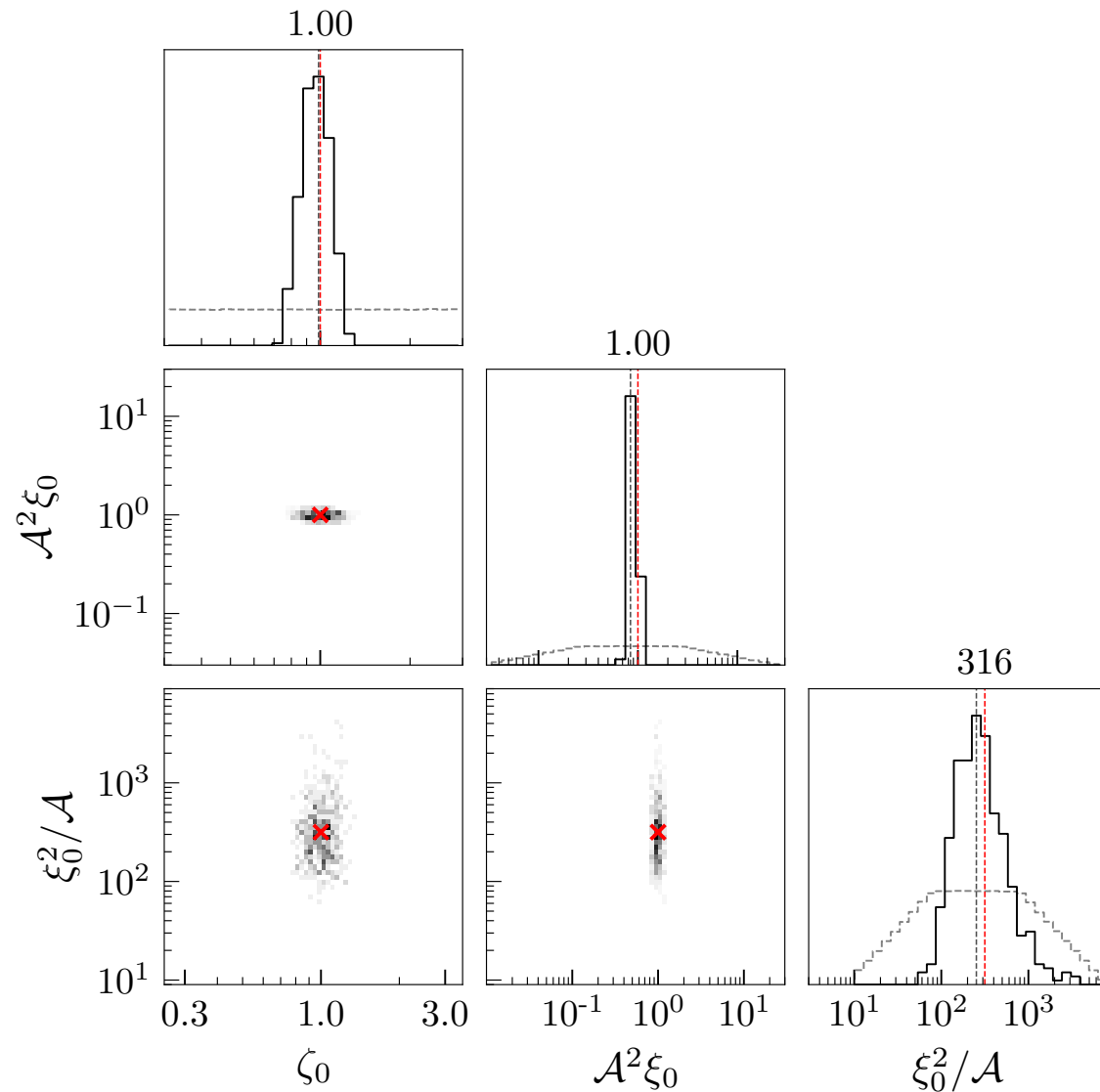
correlation function



angular power spectrum



Machine learning for axion strings



How well does the SCNN reproduce a known input?

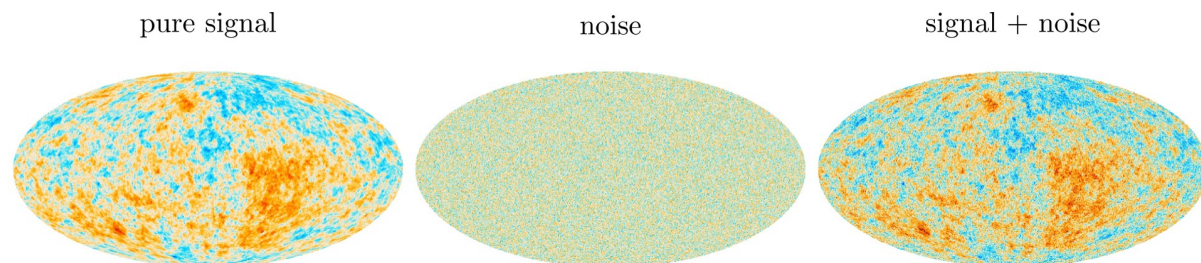
SCNN's for Z & A work well

SCNN for X struggles

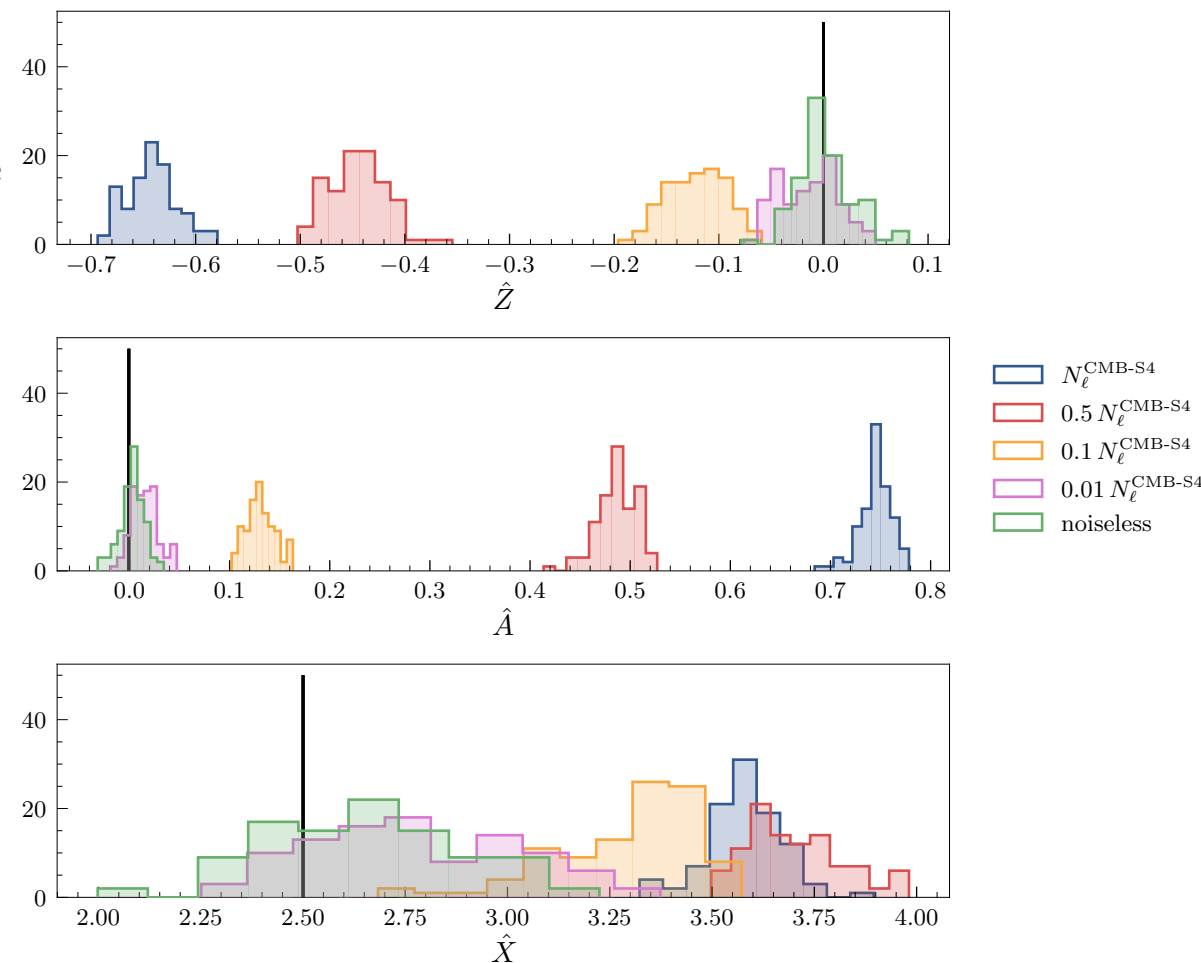
Machine learning for axion strings

How well would the SCNN perform on noisy data?

SCNN trained on noise-less sims ... then shown sim + Gaussian noise

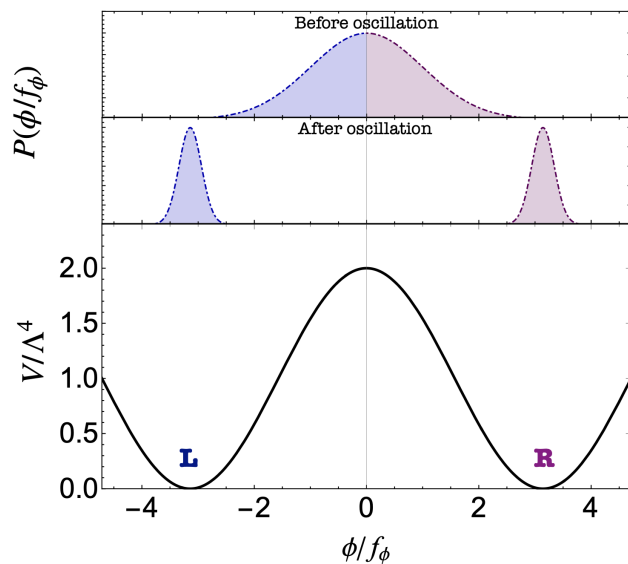


an SCNN trained on noise-less sims would require noise reduction to a level below the CMB-S4 projection to function (needs to be trained on noisy sims)



Complementary studies: stable axion domain walls

domain walls without strings
expected if $H_{\text{inf}} \sim f_a$

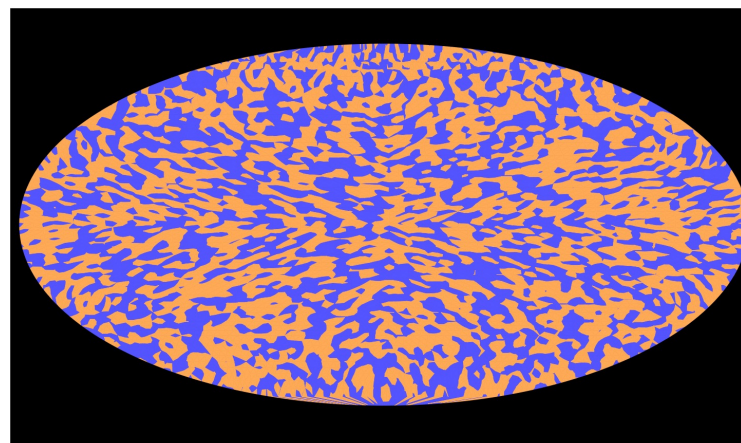


possible to evade DW problem
imposes bound on mass & decay constant

$$\sigma_{\text{DW}} \simeq 8f_\phi^2 m_\phi \lesssim (1 \text{ MeV})^3,$$

$$f_\phi \lesssim 4 \times 10^9 \text{ GeV} \sqrt{\frac{10^{-20} \text{ eV}}{m_\phi}}.$$

birefringence signal
independent of propagation



$$\Delta\Phi = 0 \quad \text{if LS}\gamma \text{ is from the vacuum } R$$

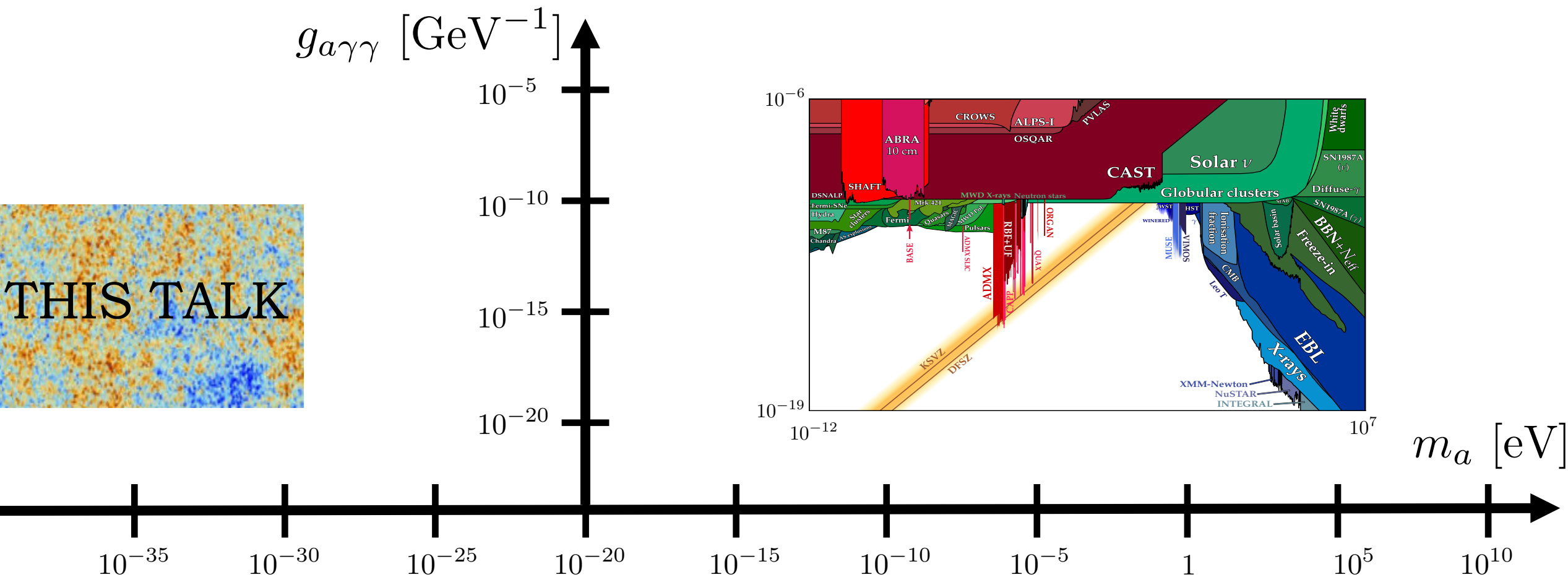
$$\Delta\Phi = c_\gamma \alpha \quad \text{if LS}\gamma \text{ is from the vacuum } L.$$

**possible to accommodate detection of
isotropic BF and evade limits on anisotropic BF
(no random-walk enhancement)**

[Takahashi & Yin (2020)]
[Nakagawa, Takahashi, & Yamada (2021)]
[Kitajima, Kozai, Takahashi, & Yin (2022)]
[Gonzalez, Kitajima, Takahashi, & Yin (2022)]

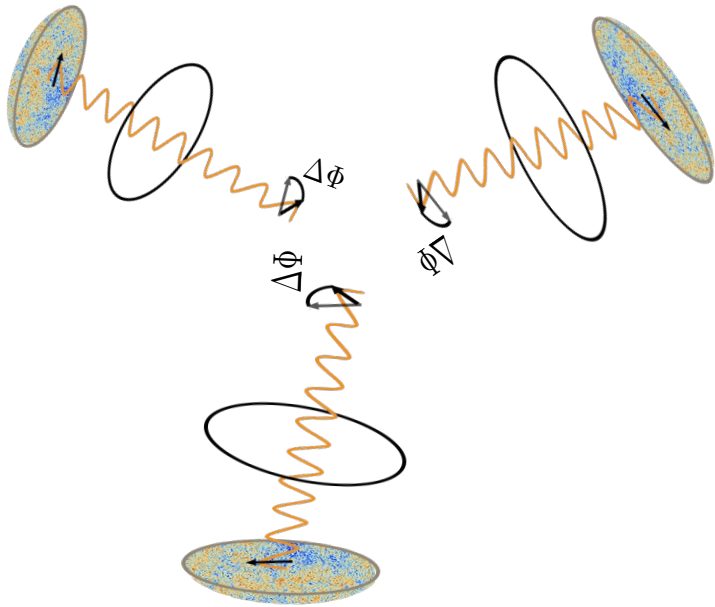
Theory landscape: axion-like particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu}$$



Net birefringence from the whole string network

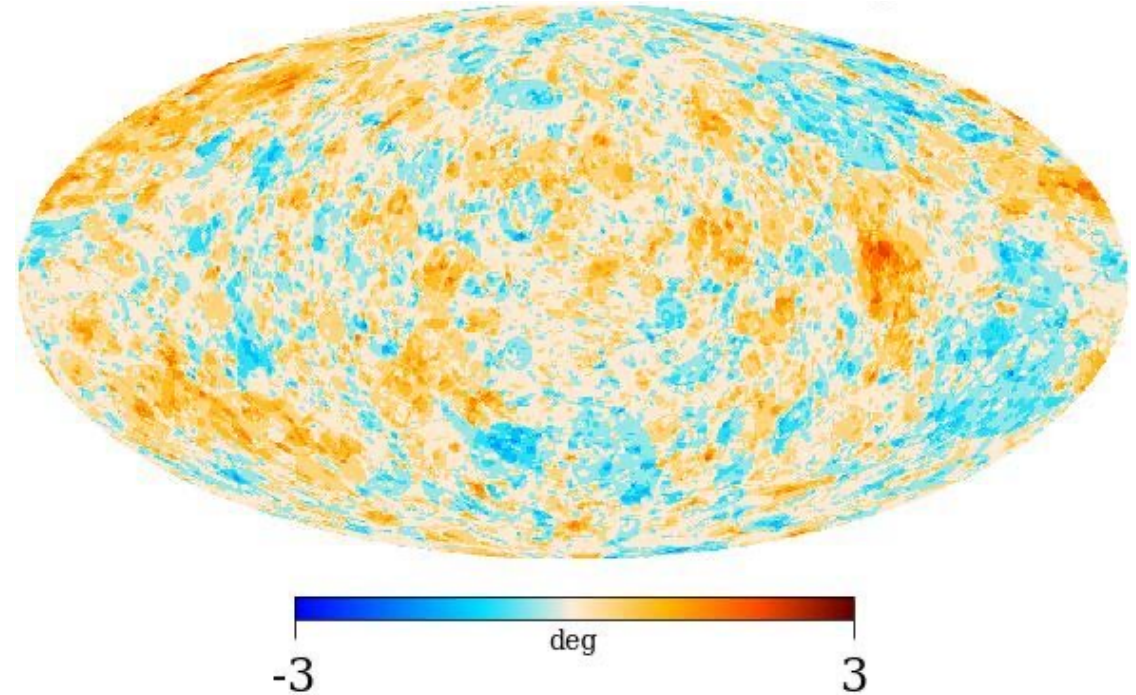
[Ray Hagimoto (2022)]



parameters:

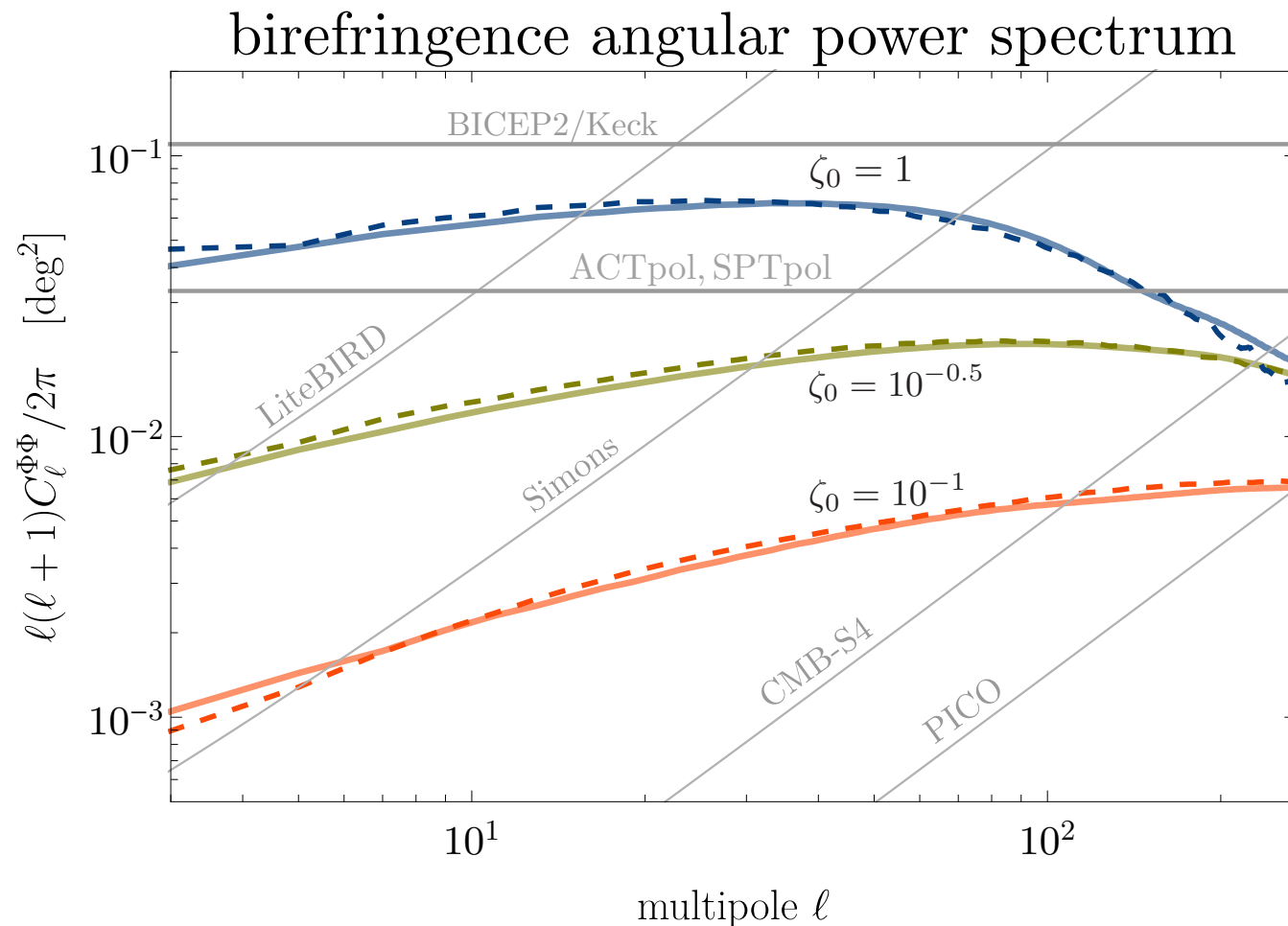
$$\begin{cases} m_a = 0 \\ \mathcal{A} = 1 \\ \zeta_0 = 1 \\ \xi_0 = 1 \end{cases}$$

a map of $\Delta\Phi$ over the sky



Axion-string induced birefringence signal

[Jain, AL, Amin (2103.01962)]



assumes: $m_a = 0$ and $\xi_0 \mathcal{A}^2 = 1$

Key features

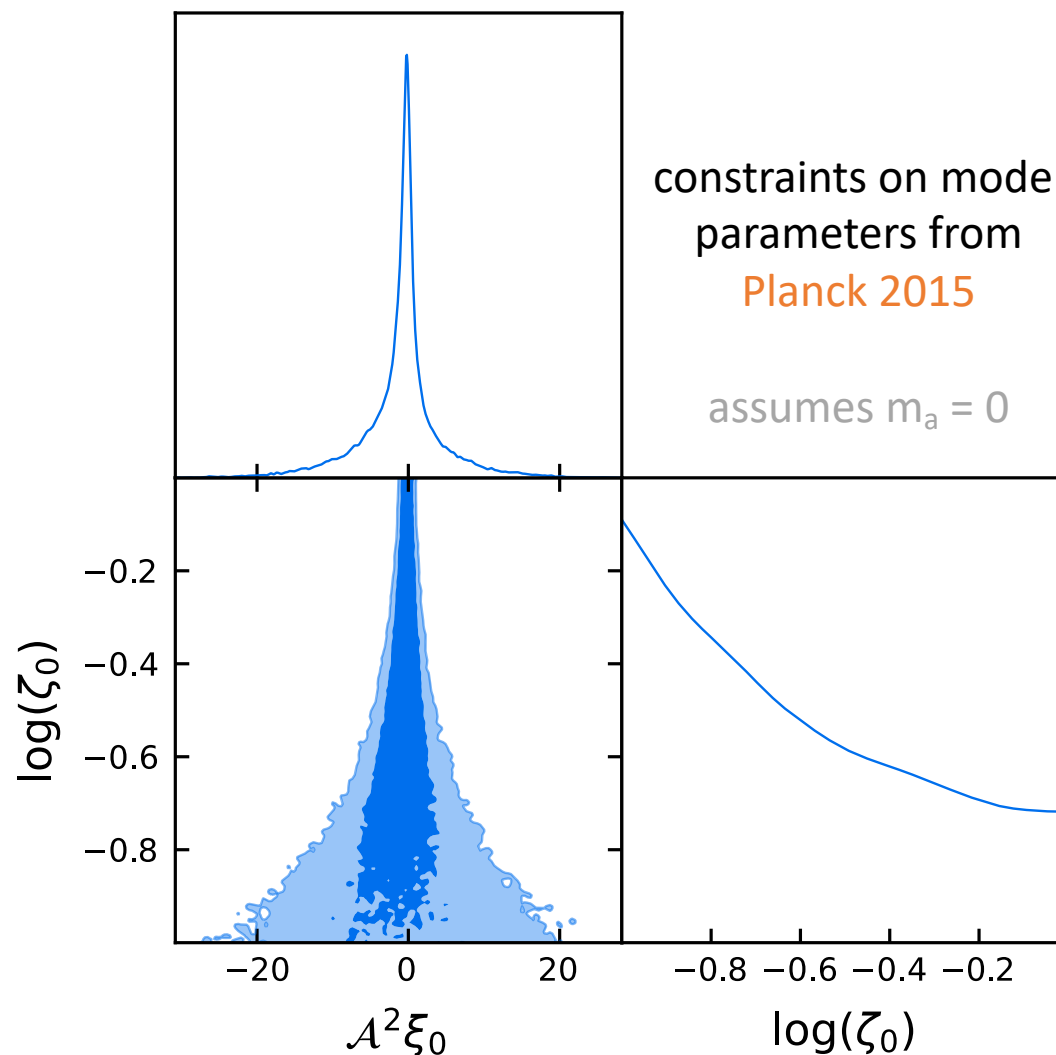
- Power spectrum is almost scale invar.
- Characteristic scale (l @ the peak) set by loop size at LSS
- Smaller loops (ζ_0) => weaker signal
- Trivial dependence on loop density (ξ_0) and anomaly coefficient (A) ... power scales with $\xi_0 A^2$

Testability

- Current telescopes (SPT/ACT) are already sensitive enough to test large loops ($\zeta_0=1$)
- Future surveys will be very powerful

CMB probes of axion strings: constraints

[Yin, Dai, Ferraro (2111.12741)]



Projected sensitivity

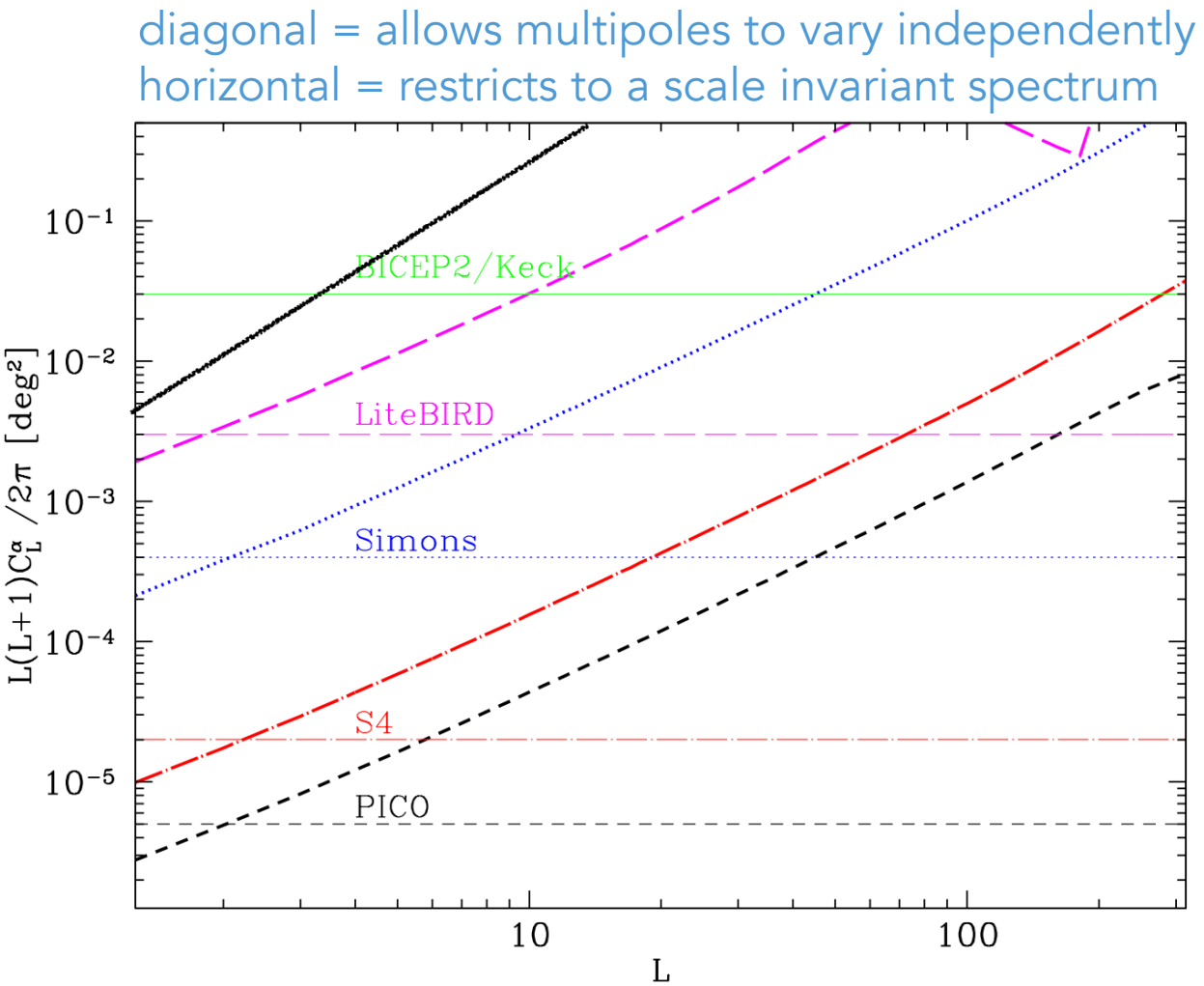
Pogosian et. al. (2019)

future telescopes
probes of isotropic + aniso. birefringence

Current			LiteBIRD			SO			CMB-S4-like			PICO		
α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$	α	A_α	$\sqrt{C_2^\alpha/4\pi}$
-	-	-	1.3	2.7	0.9	0.56	3	0.29	0.1	1.4	0.065	0.05	0.4	0.035
-	-	-	1.5	3.3	1.0	0.66	4	0.35	0.11	2.0	0.08	0.06	0.5	0.04
-	-	-	1.4	3.5	1.0	0.64	5.0	0.4	0.13	2.5	0.09	0.08	1.2	0.06
30	2	3	1.6	4.0	1.1	0.71	5.5	0.4	0.15	3.3	0.1	0.09	1.4	0.065

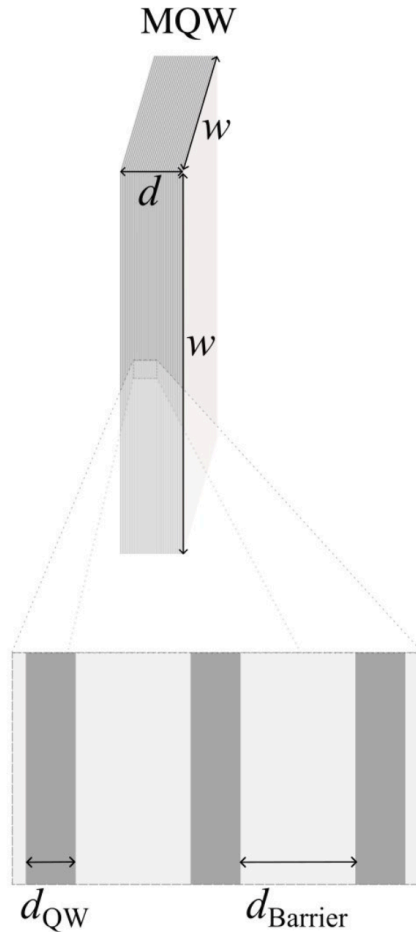
BLE II. Current and forecasted 68% CL bounds on the uniform and the anisotropic CPR parameters.

$$A_\alpha = L(L + 1)C_L^\alpha/2\pi$$



T-RAx

Photon generation: MQW emitter

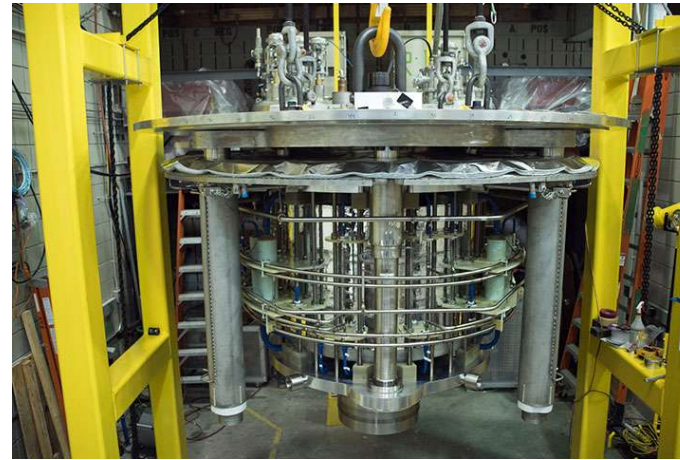
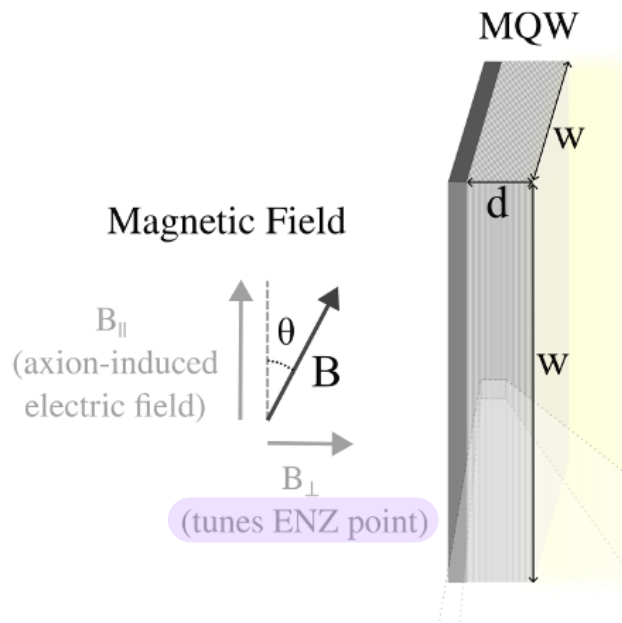


- Doping density about $O(10^{11}) \text{ cm}^{-2}$
- MQW layer at nm thickness
- T-RAX emitter at mm thickness
- Emission area of cm scale is viable

Parameter	Off-shelf	Conservative	Optimistic
n (10^{11}cm^{-2})	3	3	3
d (mm)	0.2	1	2
Area (cm^2)	3×3	3×3	5×5
d_{QW} (nm)	30	30	10

Photon generation: Magnetic field

- Considering the 36-T NMR magnetic field at National Magnetic Lab
- Magnetic field in two directions responsible for conversion and tuning



NATIONAL HIGH
MAGNETIC
FIELD LABORATORY

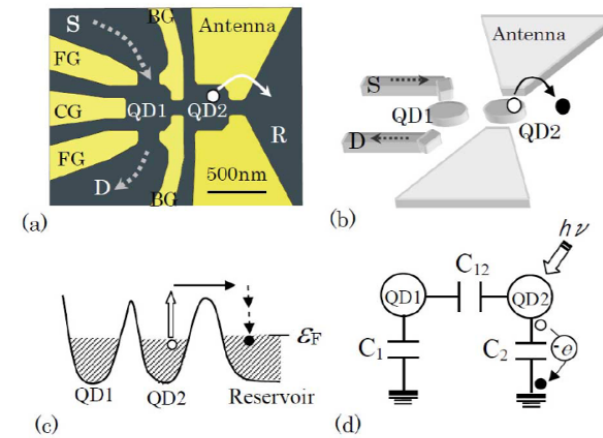
Parameter	Off-shelf	Conservative	Optimistic
Temp. (K)	0.3	0.3	0.3
B (T)	36	36	50

This slide was created by Tao Xu and reproduced here with his permission.
See <https://indico.cern.ch/event/1488822/contributions/6480040/> for his full talk.

Photon detection: single-photon detector

- Quantum dot photodetector made of GaAs/AlGaAs
 - Measure changes in capacitance
 - **Works in high magnetic fields**

Will also consider single-photon detector options capable of operating in a strong magnetic field.



Parameter	Off-shelf	Conservative	Optimistic
Γ_{dark} (Hz)	10^{-2}	10^{-3}	10^{-4}
η	7%	20%	90%