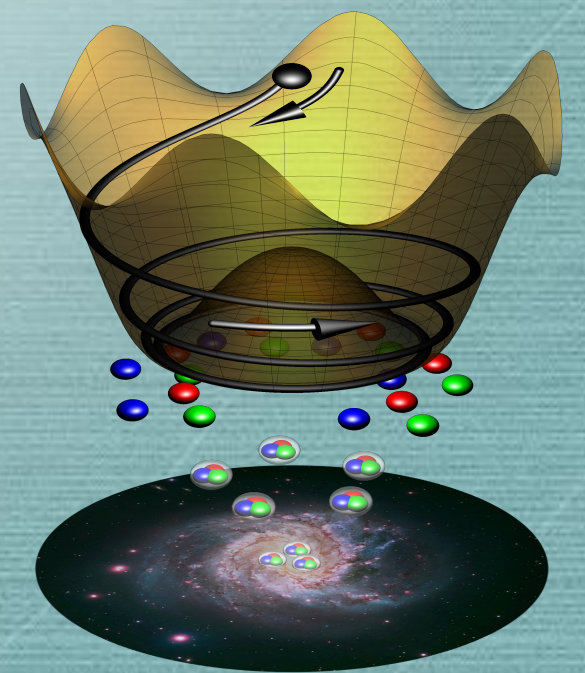


03/07/2025, Axions in Stockholm

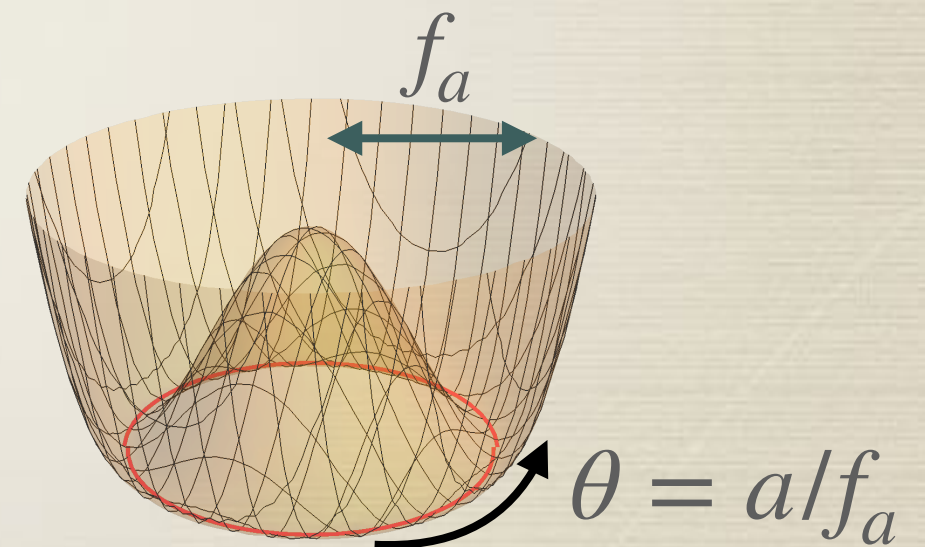
Kinetic/Acoustic Misalignment and baryon asymmetry

Keisuke Harigaya (UChicago)



Spontaneously broken continuous symmetry

- * PQ symmetry: strong CP problem
- * Lepton symmetry : neutrino mass models
- * Flavor symmetry: flavor hierarchy
- * ...

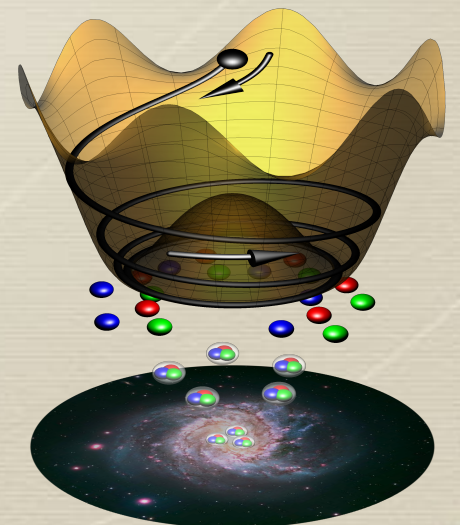


(Pseudo) Nambu-Goldstone bosons are predicted

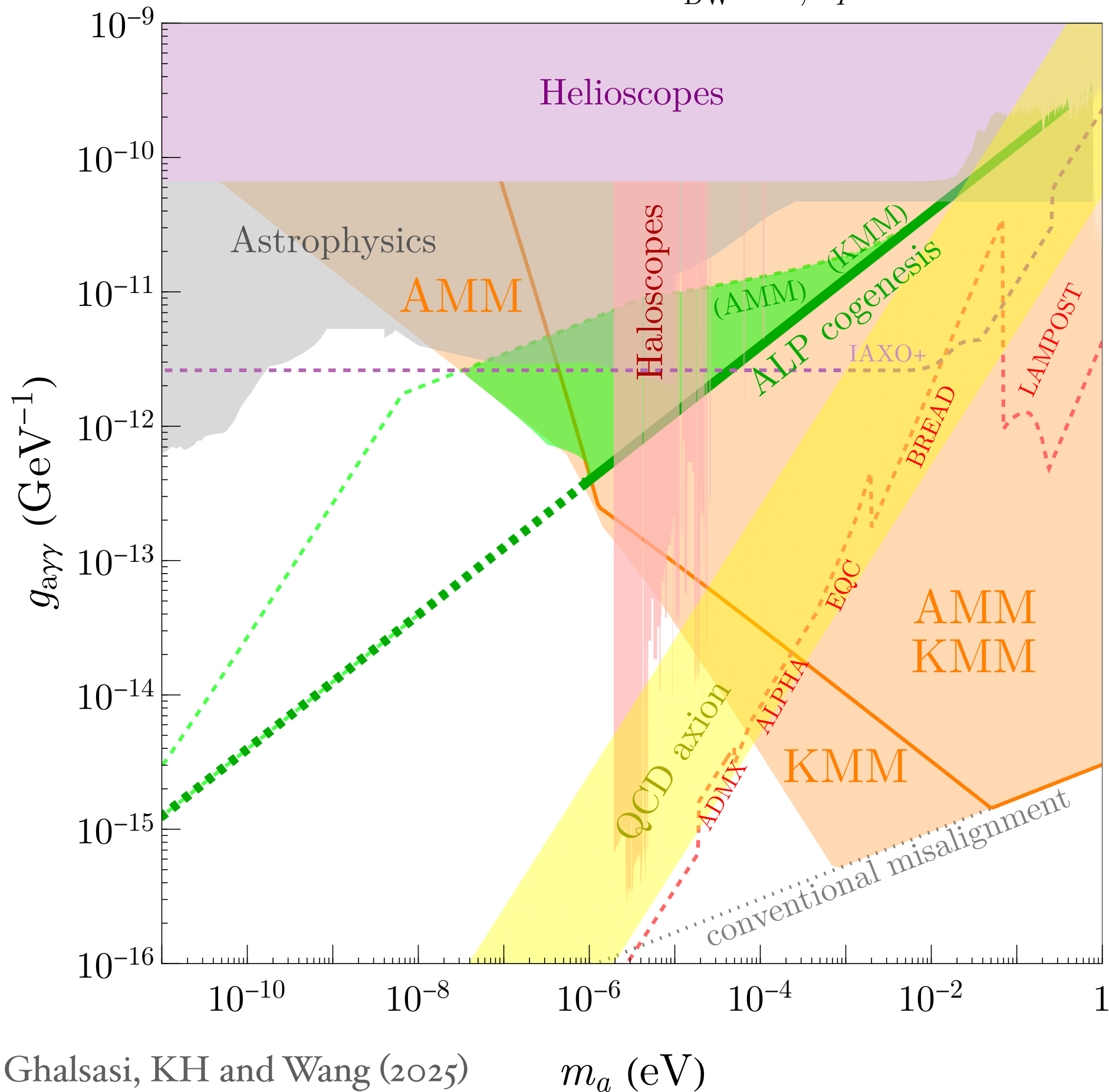
Axions

Summary

- * Rotation of axion in the field space can create matter-antimatter asymmetry
- * Rotation produces axion dark matter through phonon mode excitation from cosmic perturbations or through parametric resonance
- * Axions couplings are predicted to be larger than the prediction of the misalignment mechanism
- * Gravitational waves may be affected or created



Two-field model: $N_{\text{DW}} = 1, r_P \rightarrow 1$



Outline

- * Axion rotation and baryon asymmetry
- * Axion rotation and dark matter
- * Gravitational waves
- * Summary

Outline

- * Axion rotation and baryon asymmetry

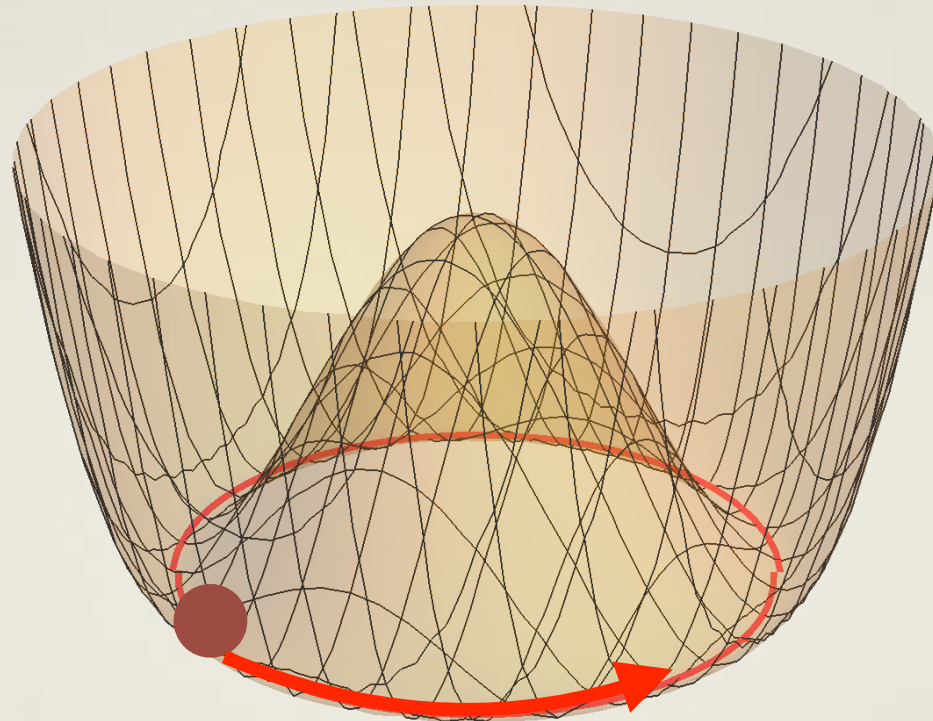


- * Axion rotation and dark matter

- * Gravitational waves

- * Summary

Axion rotation

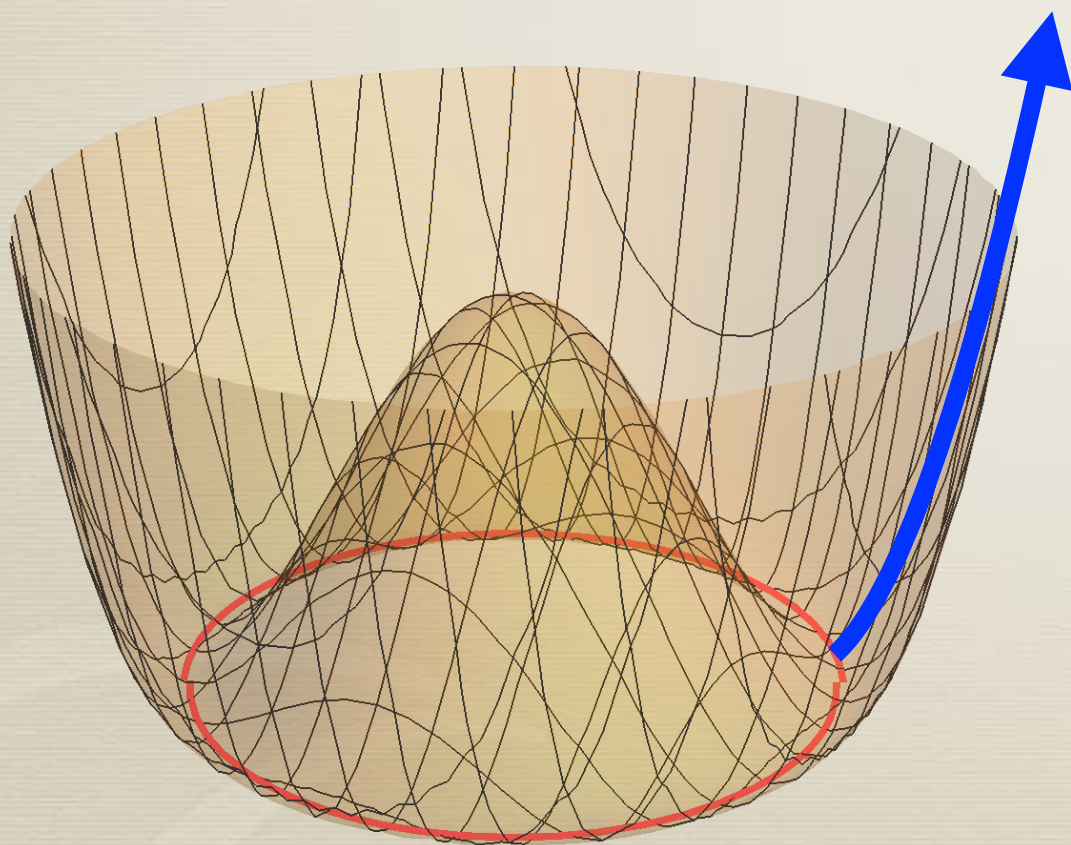


Non-zero angular momentum / U(1) charge

$$n_{\theta} = \dot{\theta} r^2$$

Initiation of rotation

Similar to Affleck-Dine mechanism (1985)
with rotating super-partners of quarks and leptons



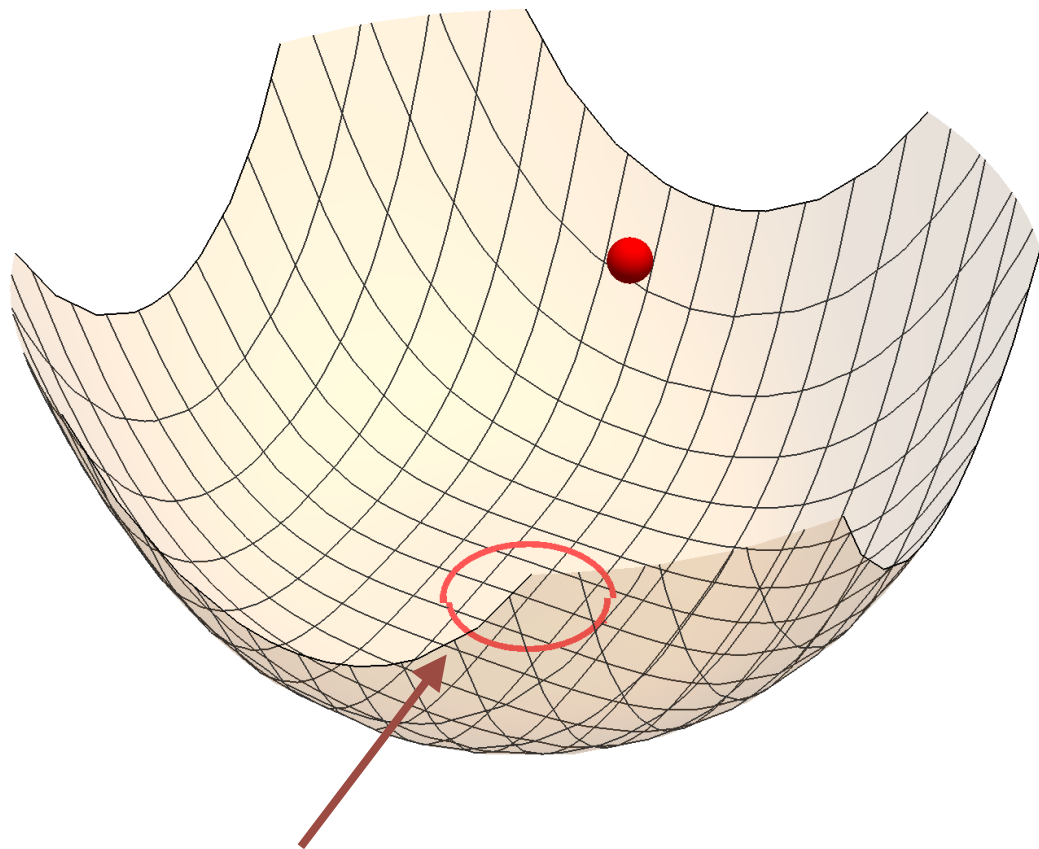
Consider the dynamics of
the **radial** direction

$$P = \textcolor{blue}{r} \exp(i \textcolor{red}{\theta})$$

Initiation of rotation

$$P = r \times \exp(i\theta)$$

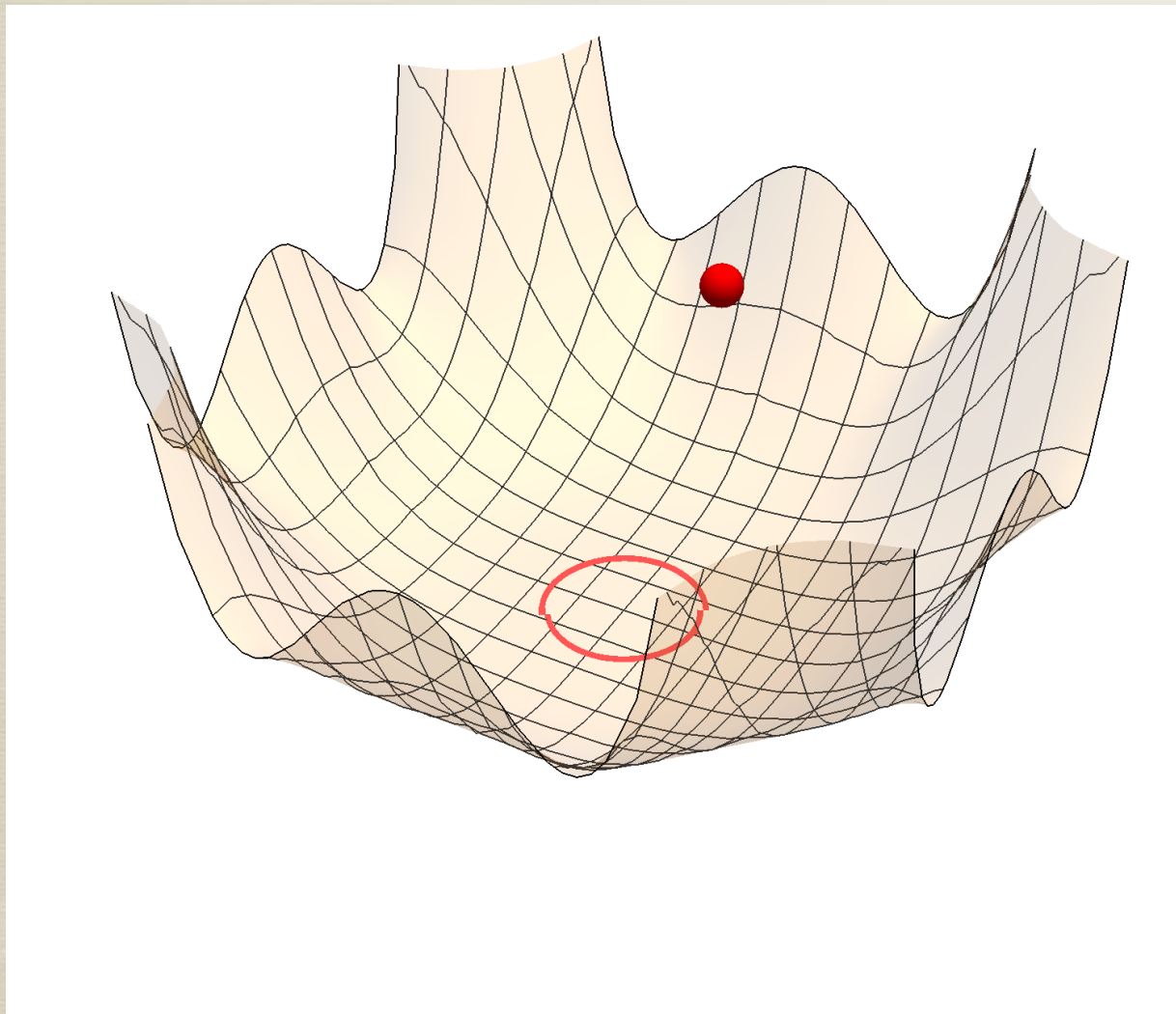
Assume a large initial
radial field value



minimum $|P| \sim f_a$

Initiation of rotation

$$P = r \times \exp(i\theta)$$



Assume a large initial
radial field value



Higher order terms

$$V \sim P^n \sim r^n \cos(n\theta)$$

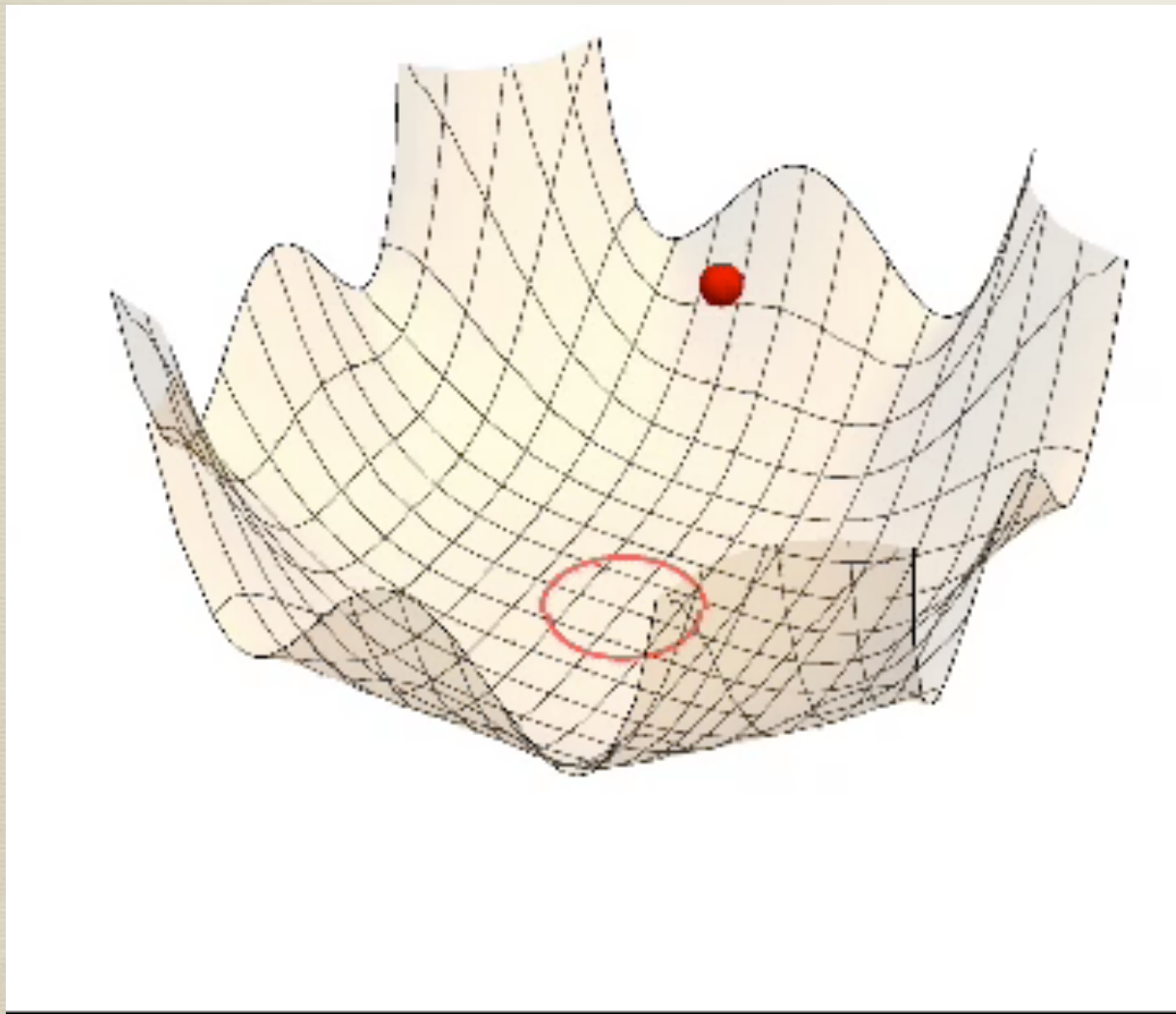
may be effective

Such terms are expected to be present
if the PQ symmetry is an accidental one

e.g., Kolb+ (1992), Barr and Seckel (1992), Kamionkowski and March-Russel (1992),
Dine (1992), KH+ (2013, 2015), Quilez+ (2018),

Initiation of rotation

$$P = r \times \exp(i\theta)$$



Assume a large initial
radial field value



Higher order terms

$$V \sim P^n \sim r^n \cos(n\theta)$$

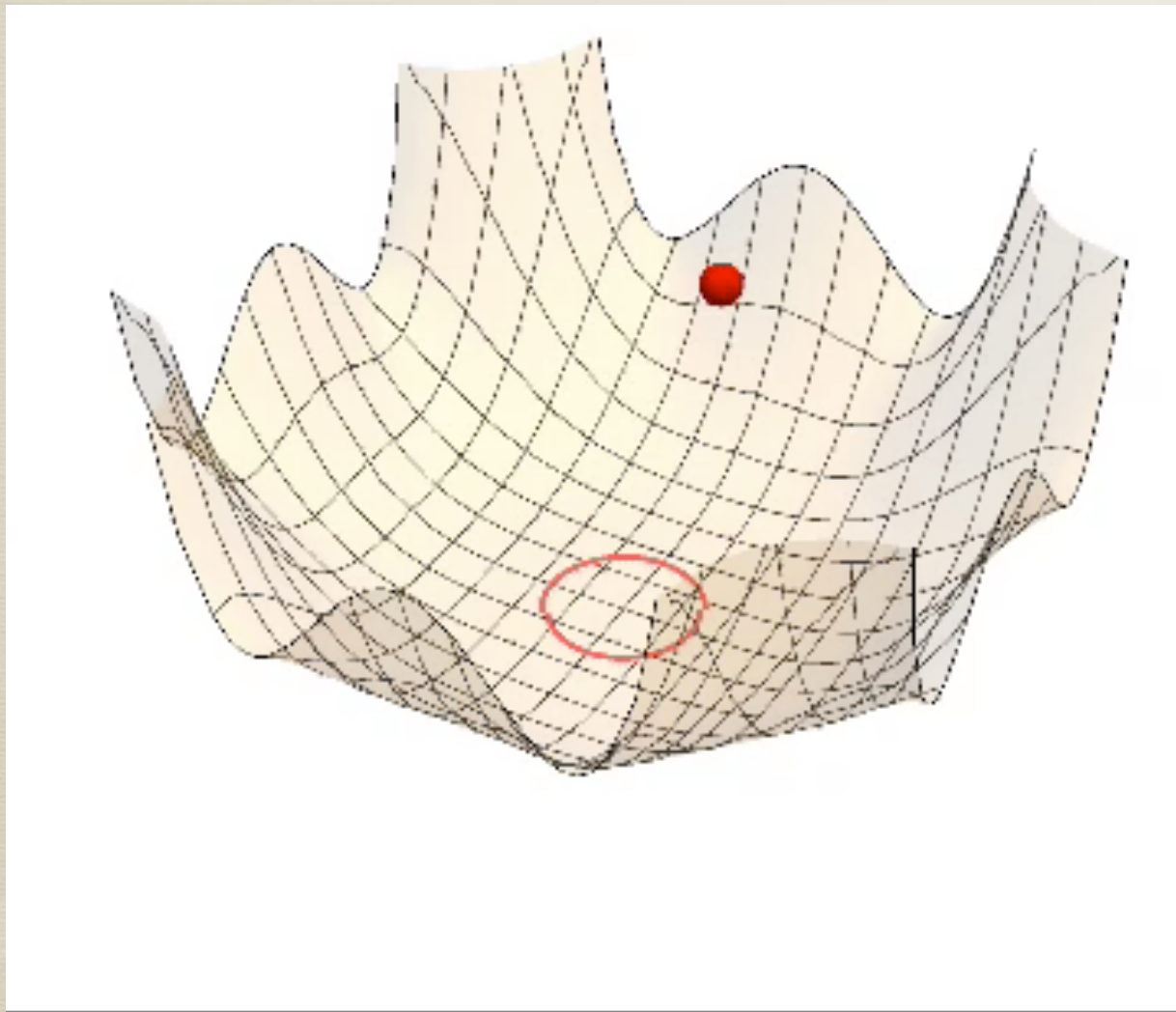
may be effective



Angular motion is induced
by the potential gradient

Initiation of rotation

$$P = r \times \exp(i\theta)$$



r decreases by
expansion of the universe



$V \simeq P^n$
is no longer effective



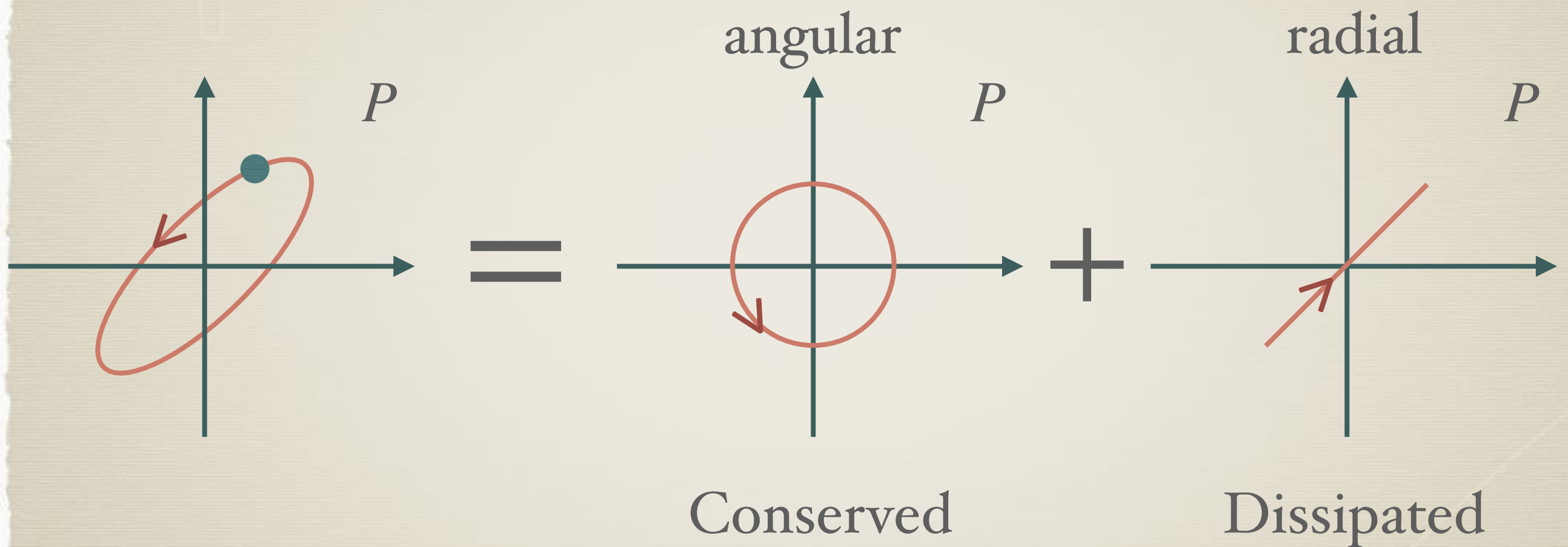
P continues to rotate,
conserving the angular momentum

$$n_\theta = \dot{\theta} r^2 \propto R^{-3}$$

Thermalization

Co and KH (2019)

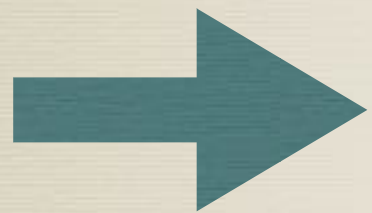
Assume P couples to the thermal bath



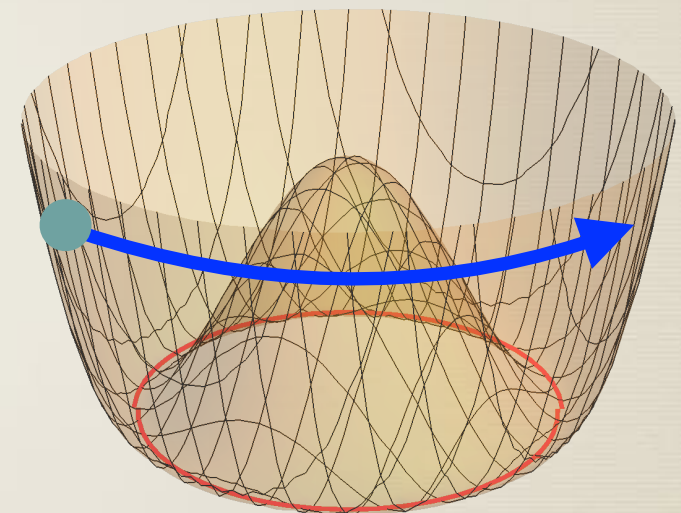
The motion becomes circular

Rotation as a BEC

Rotation = U(1) charge in the zero-mode



Bose-Einstein Condensate

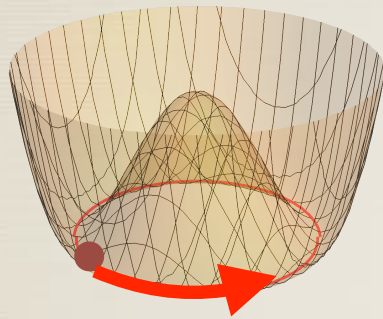


Can it evaporate into excitations
at high temperature in the early universe?

Stability of the rotation

Co and KH (2019)

Rotation



particle-antiparticle
asymmetry in the bath

$$\mu_{\text{rot}} \sim \frac{\dot{\theta}^2 r^2}{\dot{\theta} r^2} = \dot{\theta}$$

chemical eq.



$$\mu_{\text{bath}} \sim \dot{\theta}$$

$$n_{\text{rot}} = \dot{\theta} r^2$$

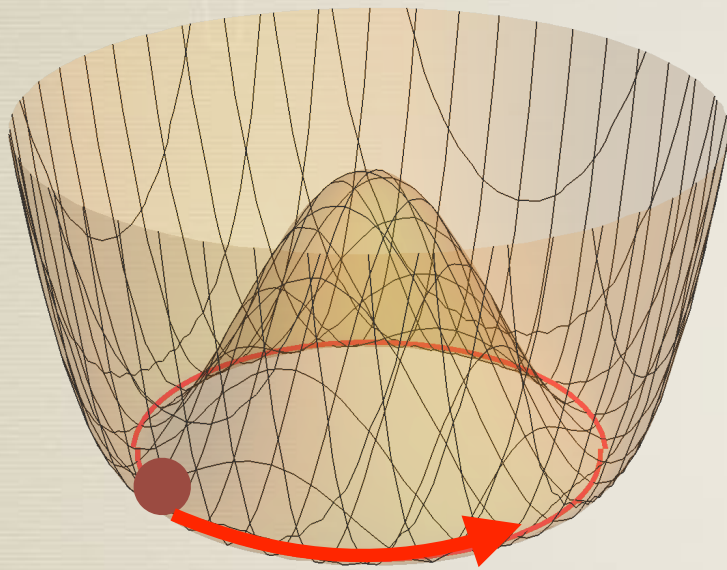


$$n_{\text{bath}} \sim \dot{\theta} T^2$$

as long as $r \gg T$

Axiogenesis

Co and KH (2019)



QCD, electroweak,
yukawa, BSM interactions

$U(1)$



Baryon

c.f. Leptogenesis

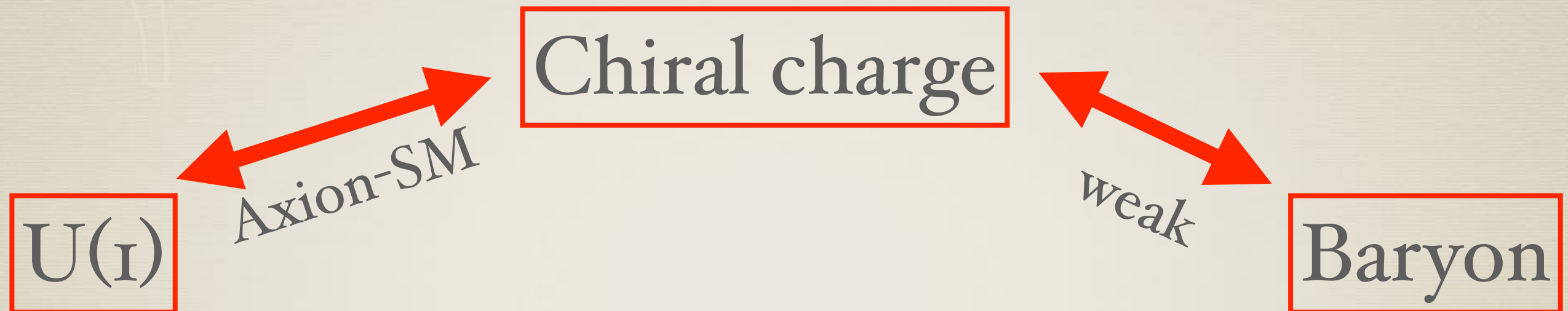
Lepton



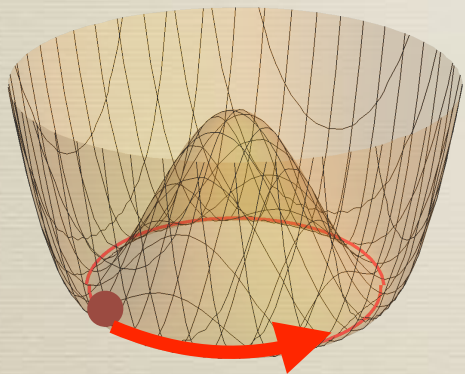
Baryon

Minimal axiogenesis

Co and KH (2019)



Transfer processes are effective before
the electroweak phase transition.
B at thermal eq.

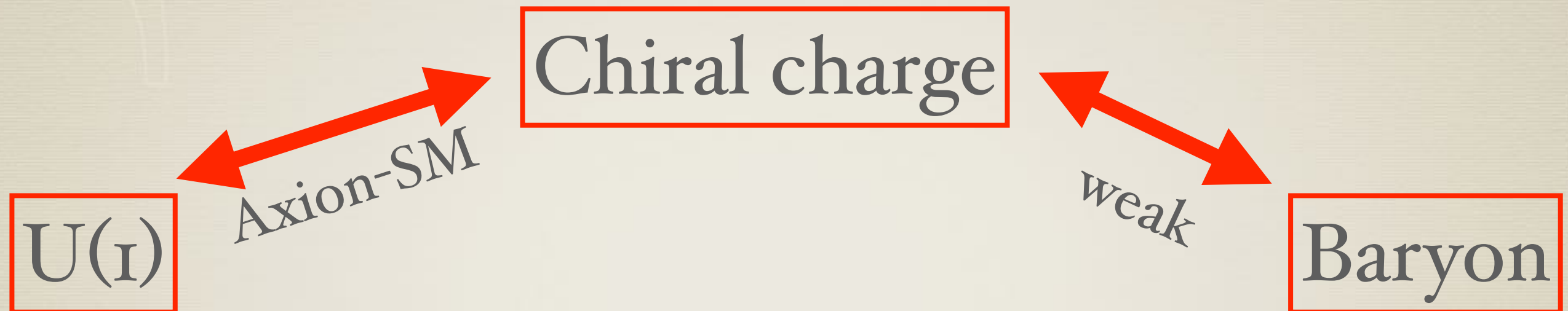


$$\mu_{\text{rot}} \sim \frac{\dot{\theta}^2 r^2}{\dot{\theta} r^2} = \dot{\theta}$$

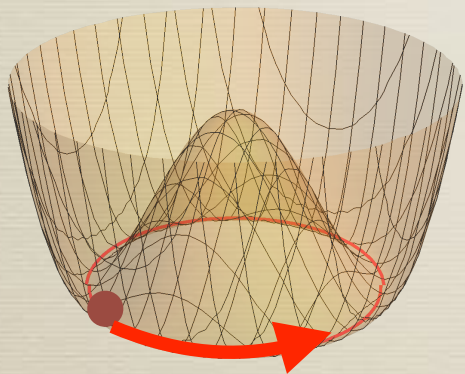
$$\begin{aligned} \mu_B &\sim \dot{\theta} \\ n_B &\sim \dot{\theta} T^2 \end{aligned}$$

Minimal axiogenesis

Co and KH (2019)

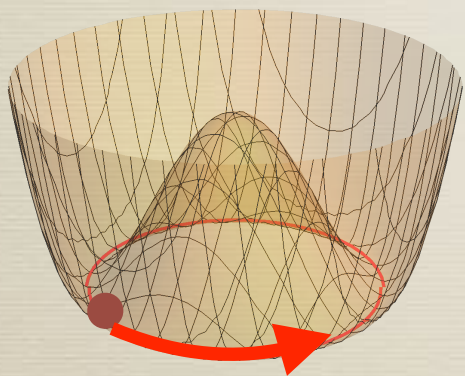
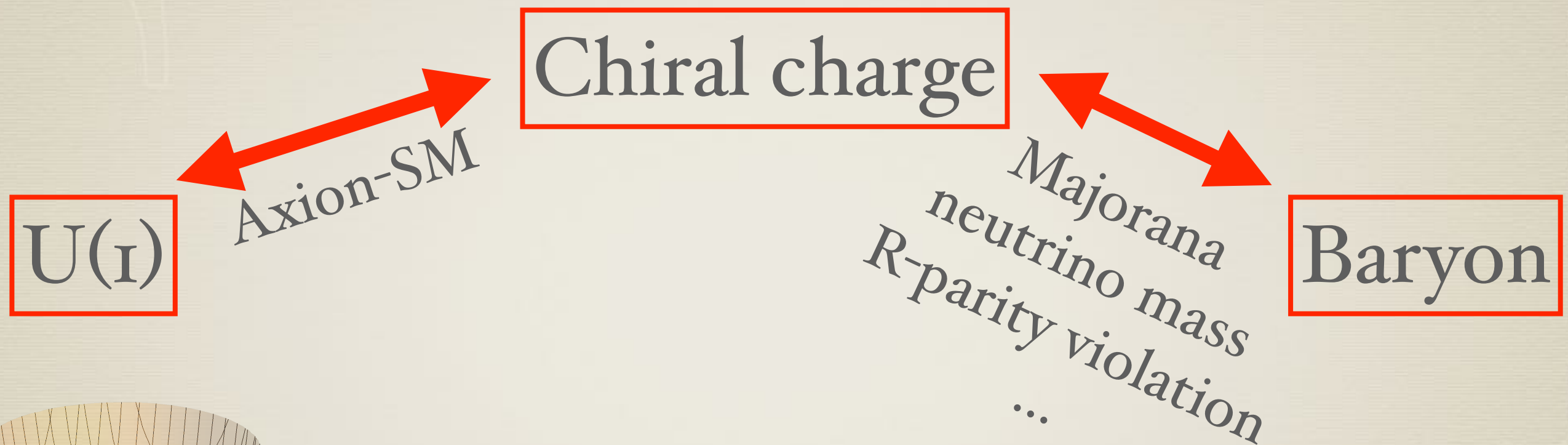


Transfer processes are effective before
the electroweak phase transition.
B at thermal eq.



$$\left. \frac{n_B}{s} \simeq \frac{\dot{\theta} T^2}{s} \right|_{\text{EW}} = n_\theta \times \frac{T_{\text{EW}}^2}{f_a^2}$$

Axiogenesis and BSM

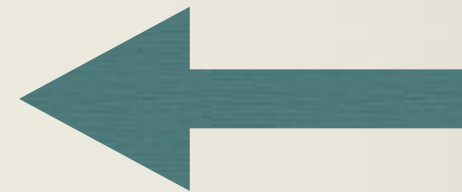


Axion $\longleftrightarrow$ other BSM

2006.05687, 2107.09679, 2108.04293, 2109.08605,
2110.05487, 2208.07878, 2307.14121, 2311.09005,
2402.10263, 2404.10283, 2405.07003

Outline

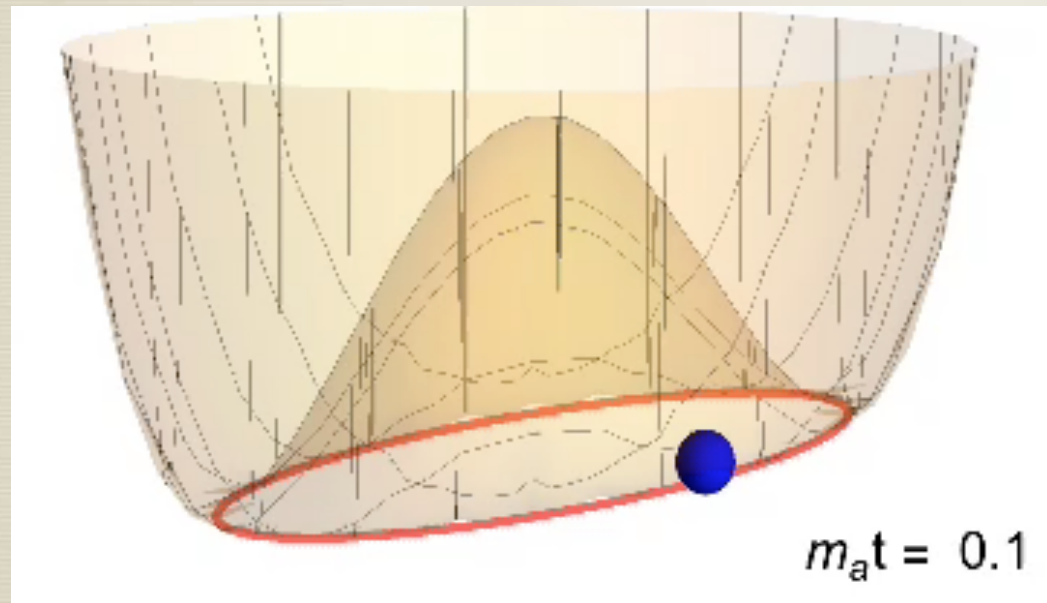
- * Axion rotation and baryon asymmetry
- * Axion rotation and dark matter
- * Gravitational waves
- * Summary



Enhanced dark matter density

Co, Hall and KH(2019)

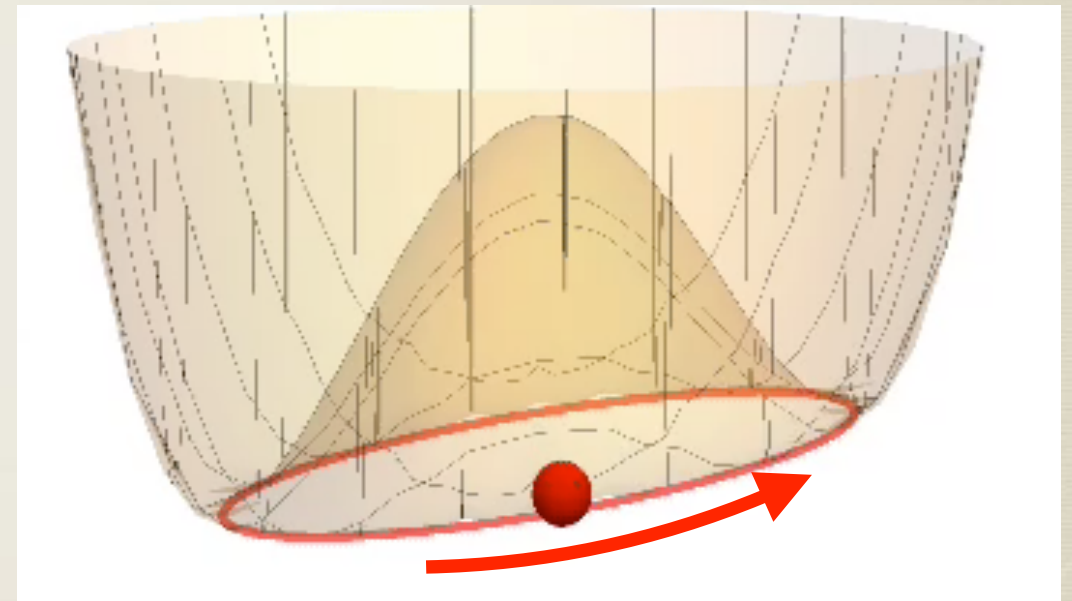
Misalignment mechanism



$$\dot{\theta}_i = 0$$

V

Non-zero kinetic energy



$$\dot{\theta}_i \neq 0$$

$V + K$

If the kinetic energy goes to axion dark matter, axion dark matter abundance will be enhanced

Enhanced dark matter density

Two sources of axion dark matter:

* Kinetic misalignment mechanism

Co, Hall and KH(2019), Co, Hall, Olive, Verner (2020)
Eroncel, Sato, Servant and Sorensen (2022)

Axion fluctuations are produced when
the axion mass becomes non-negligible

~~$U(1)$~~

* Acoustic misalignment mechanism

Bodas, Co, Ghalsasi, KH and Wang (2025)
Eroncel, Gouttenoire, Sato, Servant and Simakachorn (2025)

Axion fluctuations are produced from
cosmic perturbations of the $U(1)$ charge

$U(1)$

Enhanced dark matter density

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Axion fluctuations are produced from
cosmic perturbations of the $U(1)$ charge

$U(1)$

Axion fragmentation

Fonseca, Morgante, Sato, Servant (2019)
Morgante, Ratzinger, Sato, Stefanek (2021)

$$V(a) = m_a^2 f_a^2 \left(1 - \cos \frac{a}{f_a}\right)$$

$$a \rightarrow \dot{\theta}t + a(t, x)$$

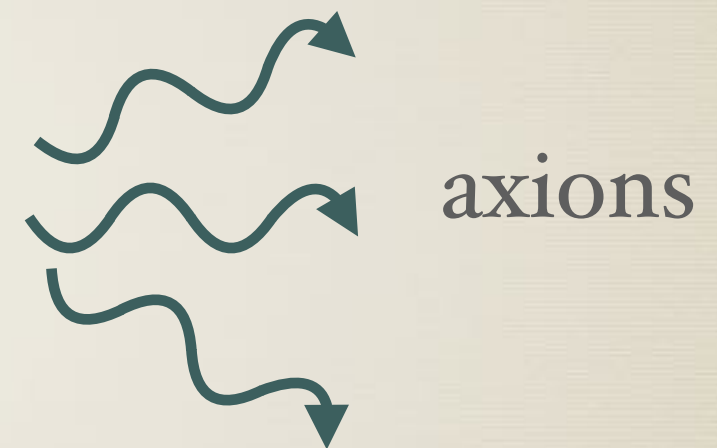
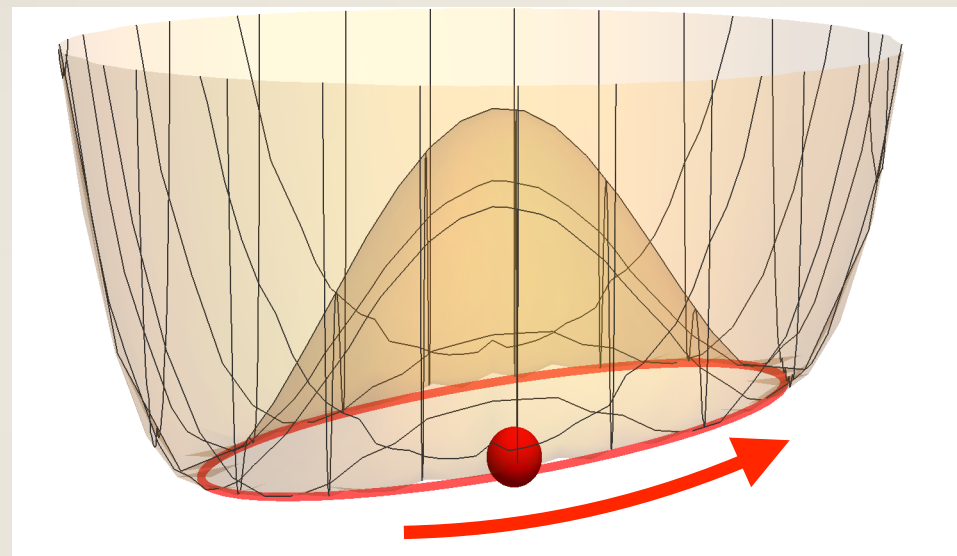
EOM of the fluctuation at the linear level:

$$\ddot{a}_k + \left(k^2 + m_a^2 \cos \dot{\theta}t\right) a_k = 0$$

oscillating frequency

Resonant production

Resonance at a natural frequency $k_{\text{PR}} \sim \dot{\theta}$



$$n_{a,\text{PR}} = \frac{\rho_{\text{rot}}}{k_{\text{PR}}} \simeq \frac{\dot{\theta}^2 f_a^2}{\dot{\theta}} = \dot{\theta} f_a^2 = n_{\theta}$$

Co, KH and Pierce (2021)

Eroncel, Sato, Servant and Sorensen (2022)

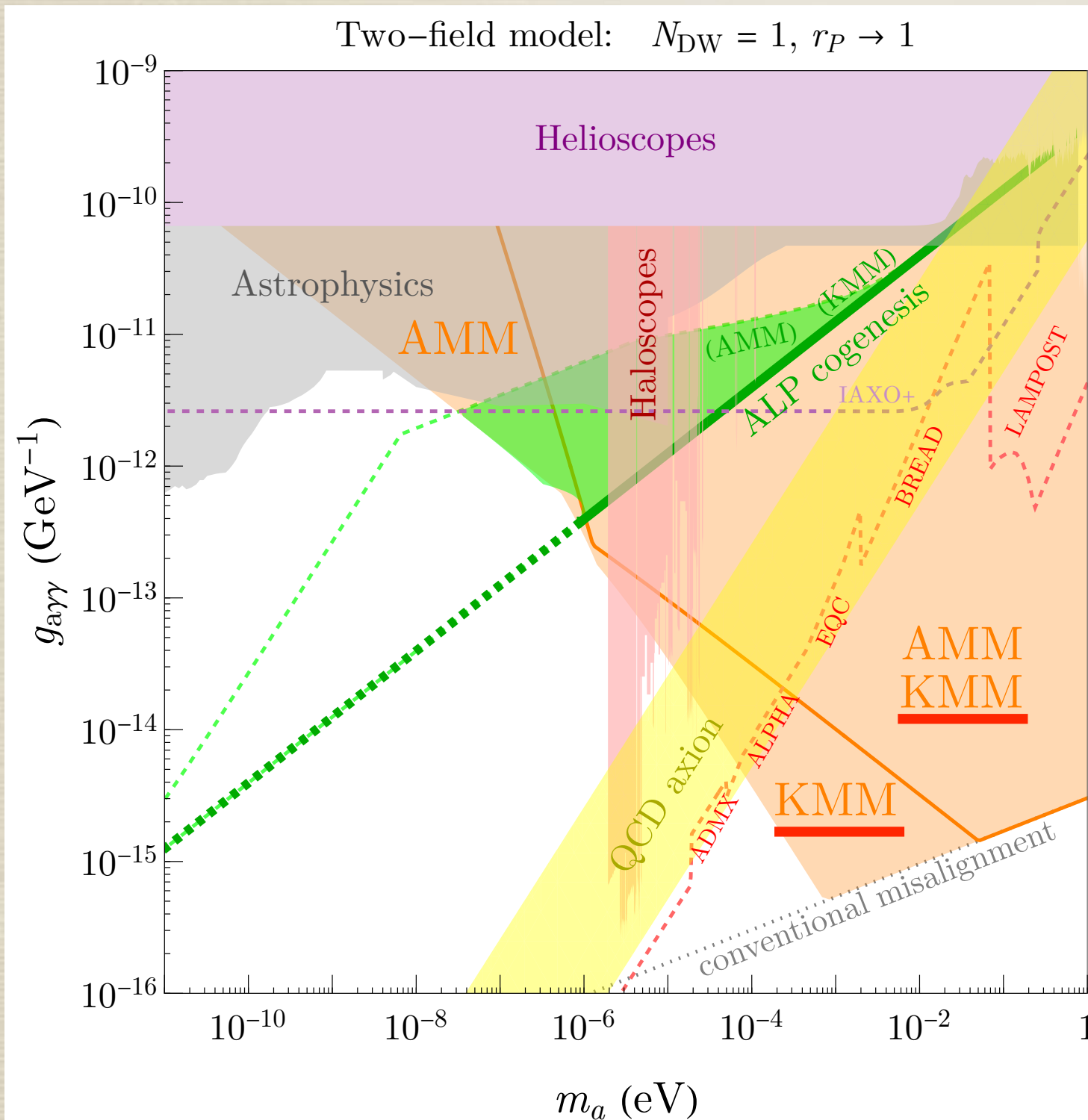
Axion number density $\simeq$ U(1) charge density

It's important to determine the relation precisely

(2507.01822 just appeared today)

Dark matter

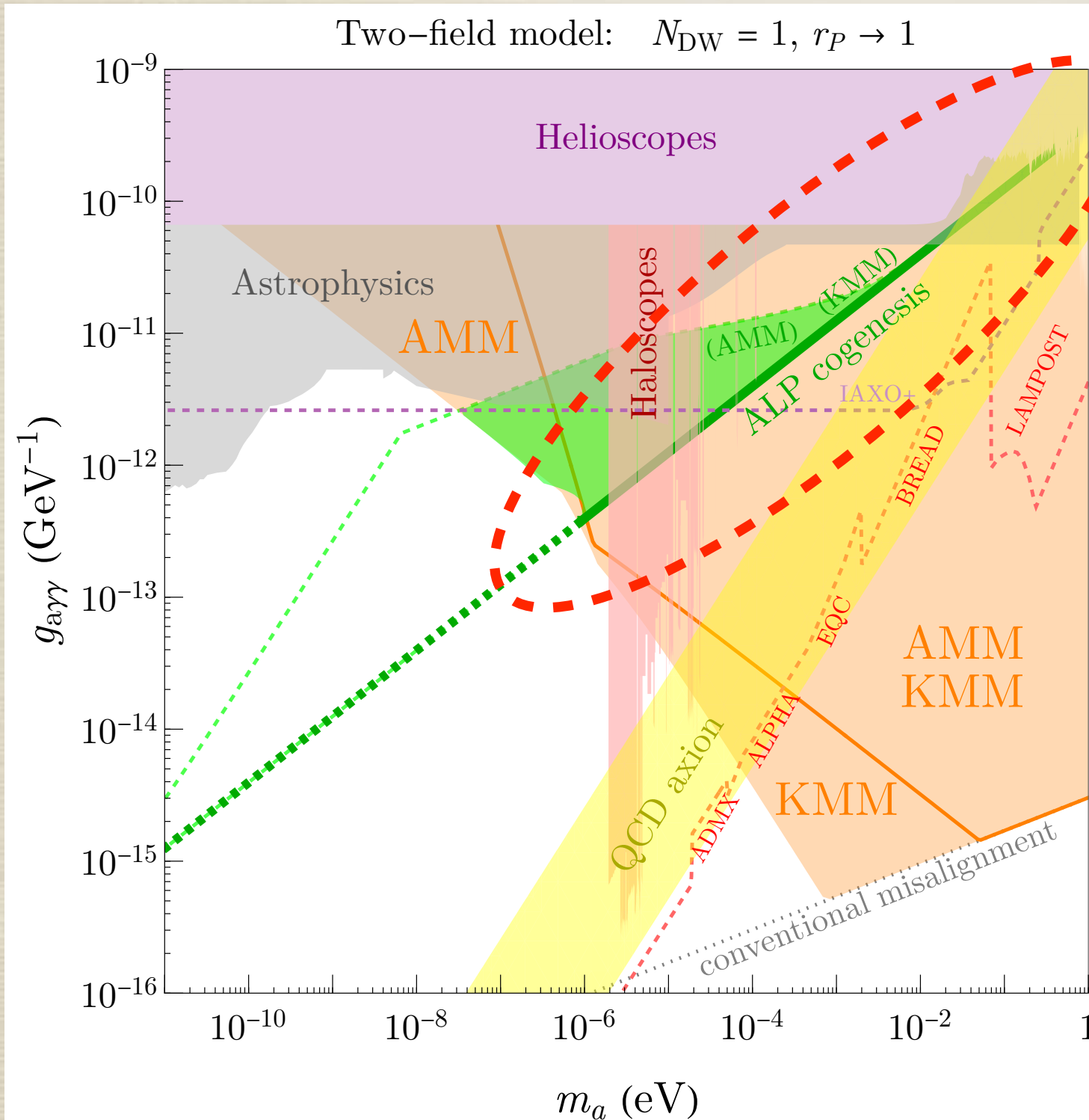
Bodas, Co, Ghalsasi, KH and Wang (2025)



In the orange-shaded region with “KMM”, the observed dark matter density can be explained by kinetic misalignment

Cogenesis of DM and baryon

Bodas, Co, Ghalsasi, KH and Wang (2025)
Co, Hall and KHH (2020)



On the green line, kinetic misalignment and axiogenesis by an electroweak process can explain both dark matter and baryon asymmetry

$$n_{a,\text{PR}} \sim n_\theta$$

Exact relation?

Enhanced dark matter density

Two sources of axion dark matter:

* Kinetic misalignment mechanism

Co, Hall and KH(2019), Co, Hall, Olive, Verner (2020)
Eroncel, Sato, Servant and Sorensen (2022)

Axions are produced when
the axion mass becomes non-negligible

~~$U(1)$~~

* Acoustic misalignment mechanism

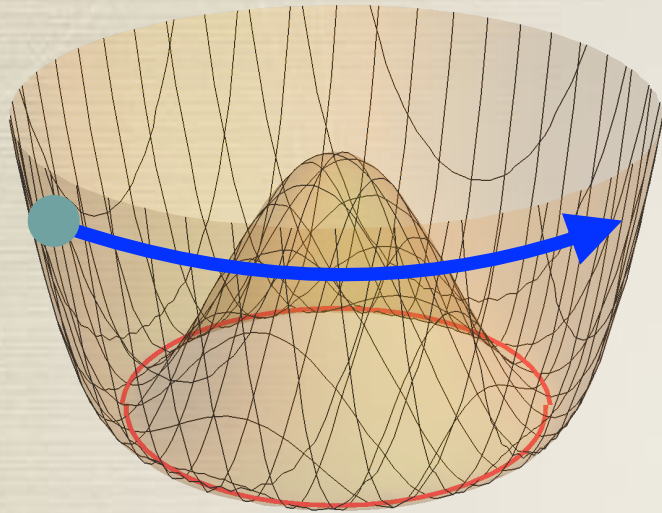
Bodas, Co, Ghalsasi, KH and Wang (2025)
Eroncel, Gouttenoire, Sato, Servant and Simakachorn (2025)

Axion fluctuations are produced from
cosmic perturbations of the $U(1)$ charge

$U(1)$

Phonon mode

$$\dot{\theta} = \omega$$



$U(1) \times$ time translation



$U(1)'$

$$\left[\begin{array}{l} \theta \rightarrow \theta + \alpha \\ t \rightarrow t + \delta \end{array} \right]$$

$$\left[\begin{array}{l} \theta \rightarrow \theta - \omega\delta \\ t \rightarrow t + \delta \end{array} \right]$$

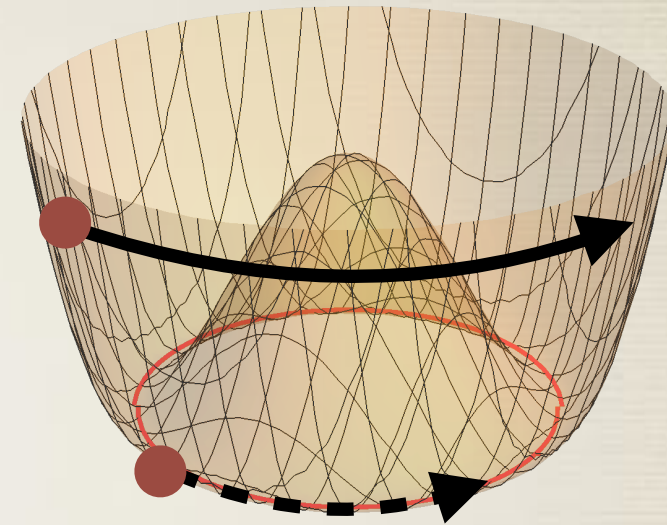
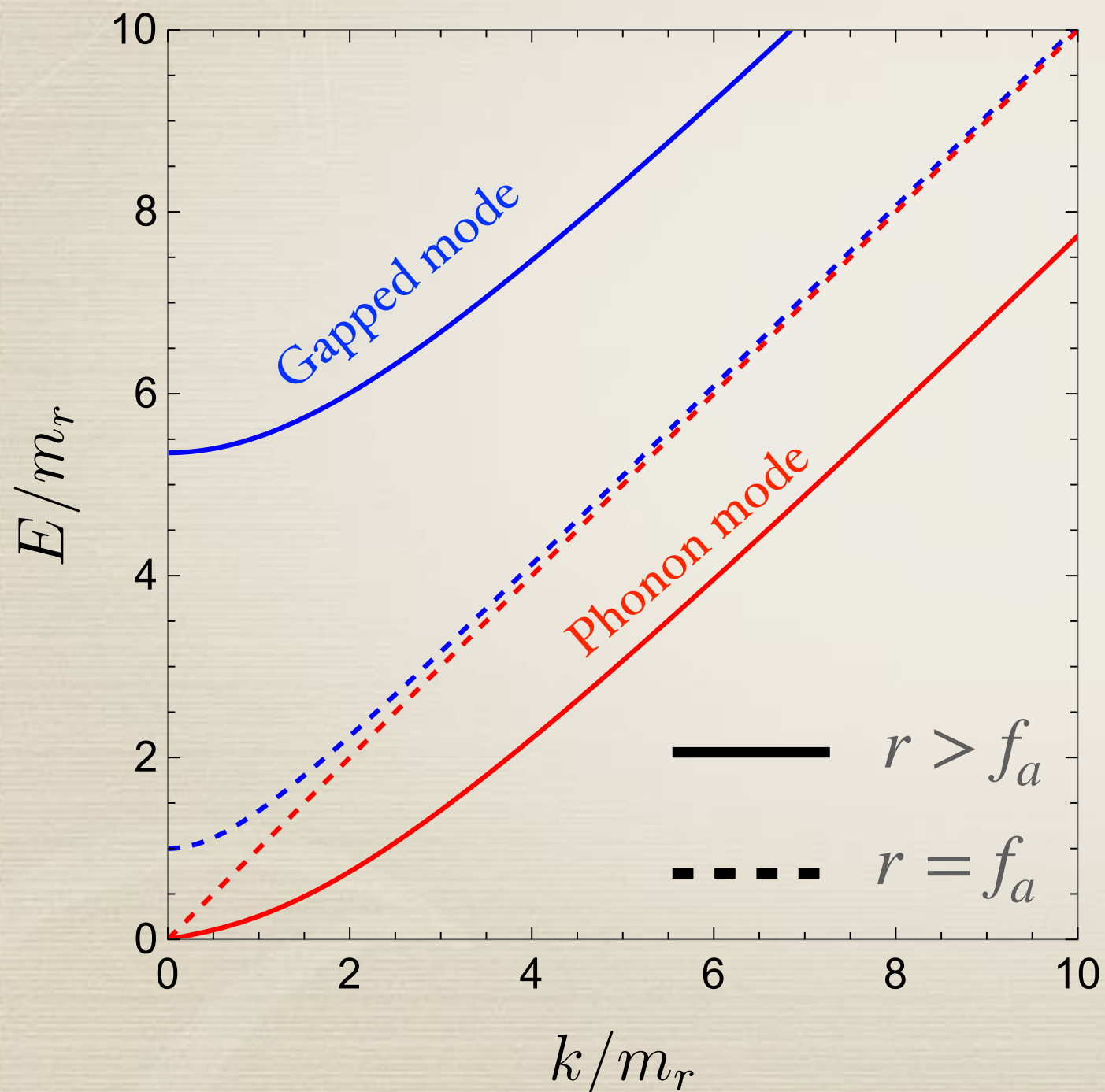
One Nambu-Goldstone mode is predicted

Phonon

Phonon mode

Bodas, Co, Ghalsasi, KH and Wang (2025)

Dispersion relation



Sound velocity

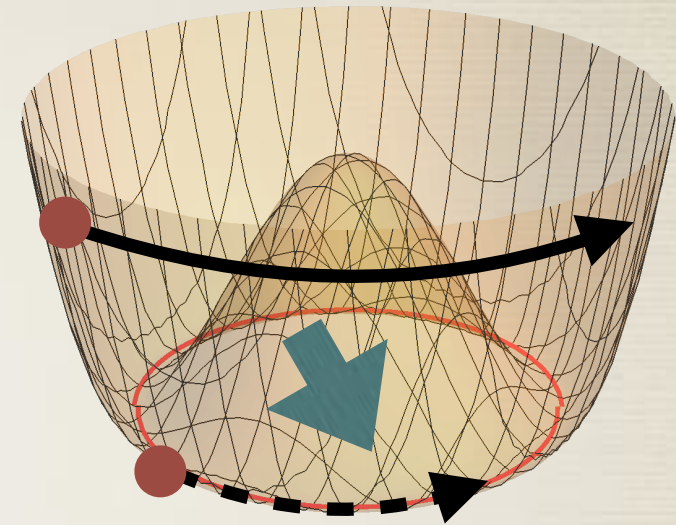
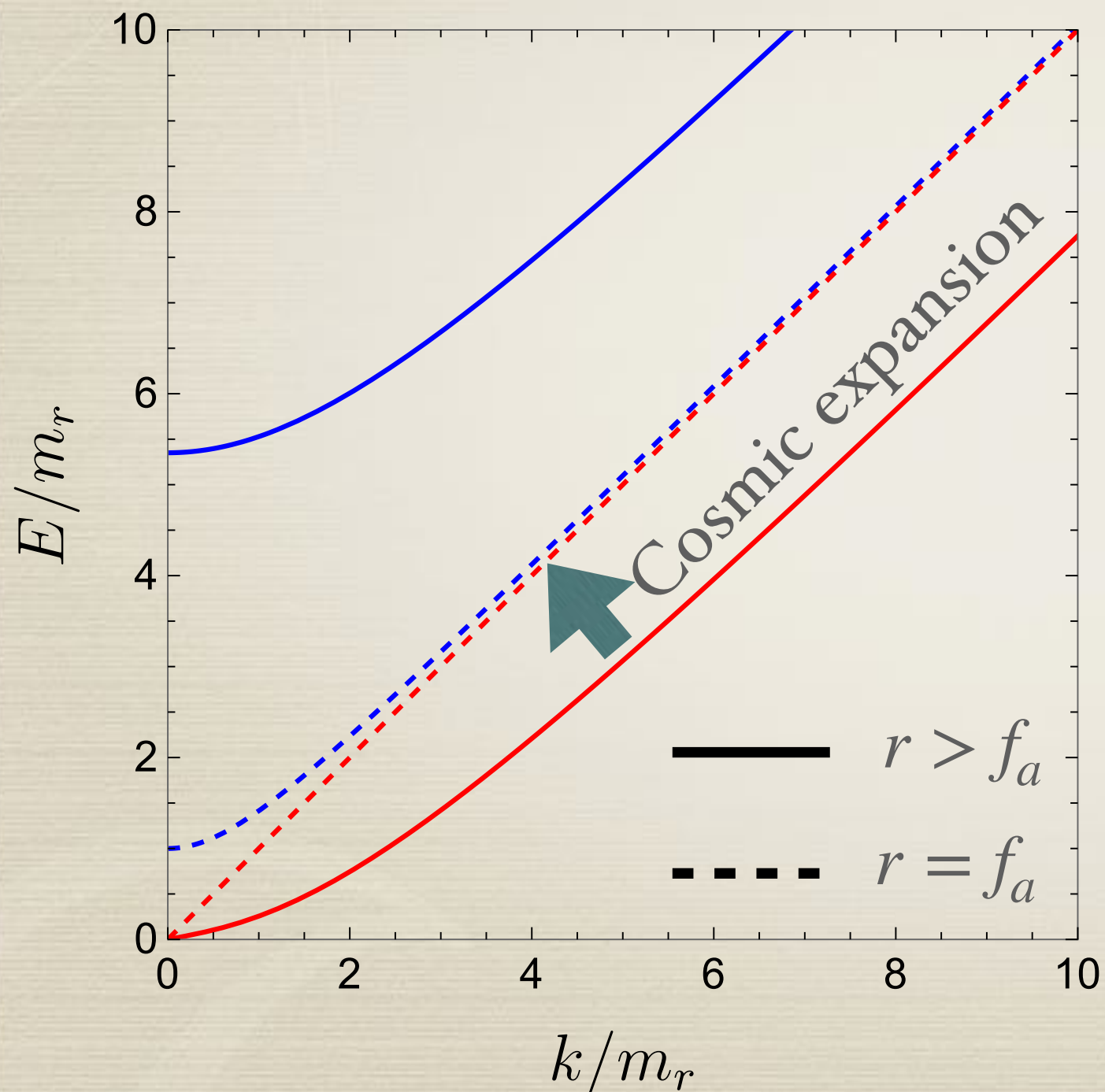
$$c_s^2 = \frac{V_{rr} - V_r/r}{V_{rr} + 3V_r/r}$$

At the minimum, where $V_r = 0$,
 $c_s = 1$: axion

Phonon mode

Dispersion relation

Bodas, Co, Ghalsasi, KH and Wang (2025)



Sound velocity

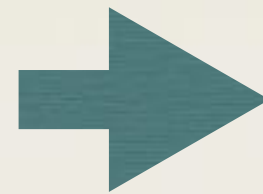
$$c_s^2 = \frac{V_{rr} - V_r/r}{V_{rr} + 3V_r/r}$$

At the minimum, where $V_r = 0$,
 $c_s = 1$: axion

Phonon production

Bodas, Co, Ghalsasi, KH and Wang (2025)

Inflaton perturbation
(curvature perturbation)

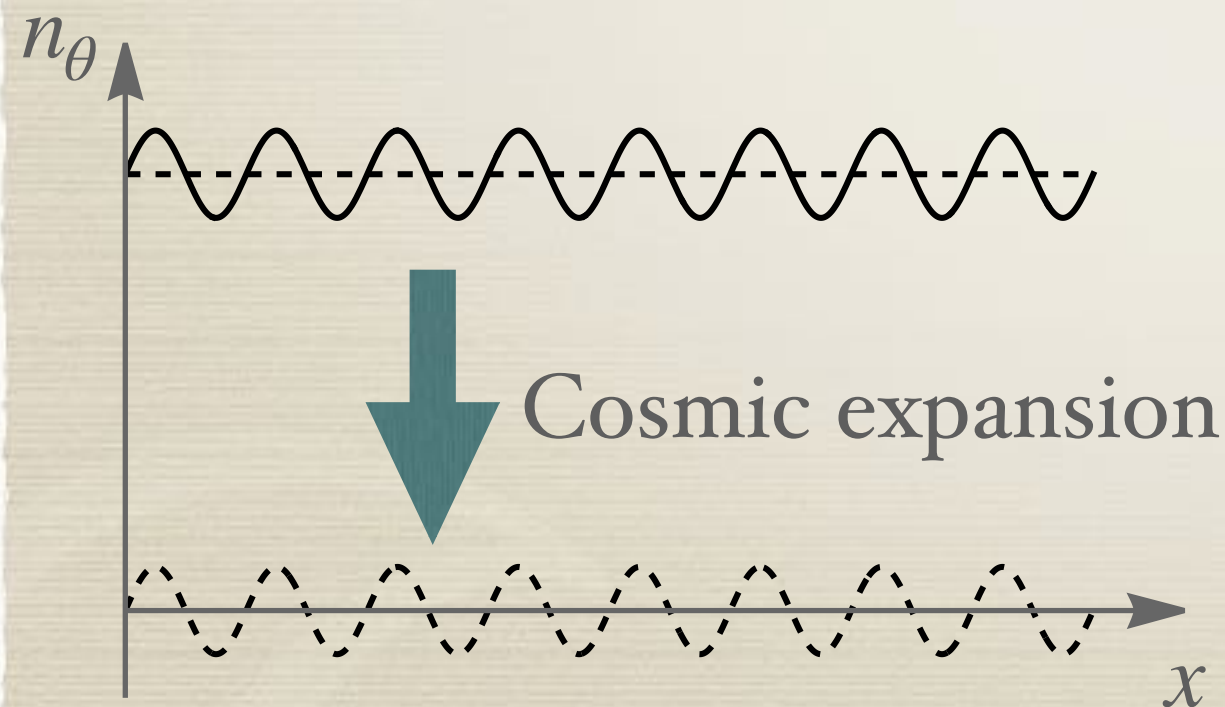


Perturbation of $U(1)$ charge density
= phonon (i.e., sound wave)

Axion perturbation
(isocurvature perturbation)



Axions



Acoustic misalignment

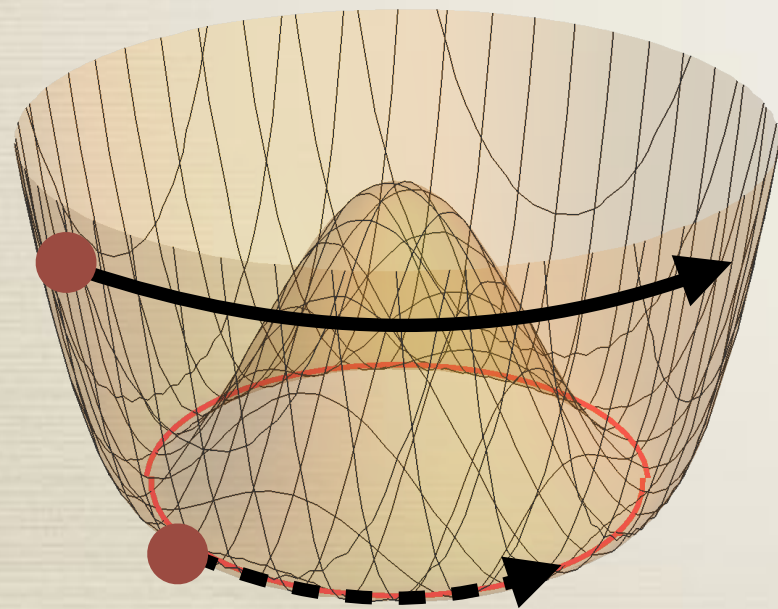
Evolution of perturbations

Co, Dunskey, Fernandez, Ghalsasi, Hall, KH and Shelton (2021)

Co, Fernandez, Ghalsasi, KH and Shelton (2021)

The axion abundance is sensitive to the equation of state of rotation and the sound velocity of the phonon mode

Ex. $V(r) \propto (r^2 - f_a^2)^2$



Radiation-like:

$$w = c_s^2 = 1/3$$

No growth of fluctuations

Kination

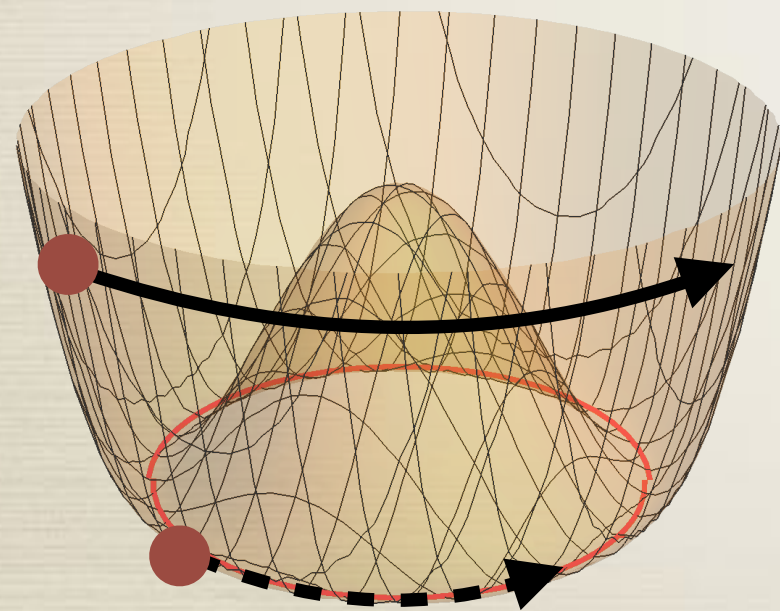
Evolution of perturbations

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Co, Fernandez, Ghalsasi, KH and Shelton (2021)

The axion abundance is sensitive to the equation of state of rotation and the sound velocity of the phonon mode

Ex. Supersymmetric model with $V(r) \propto m_r^2 r^2$ for $r \gg f_a$



Matter-like:

Kination

$$w \simeq c_s^2 \ll 1$$

Growth of fluctuations
if the rotation
dominates the universe

Evolution should be carefully computed
using cosmological perturbation theory

δ/δ_i 10^5 10^4

1000

100

10

1

0.1

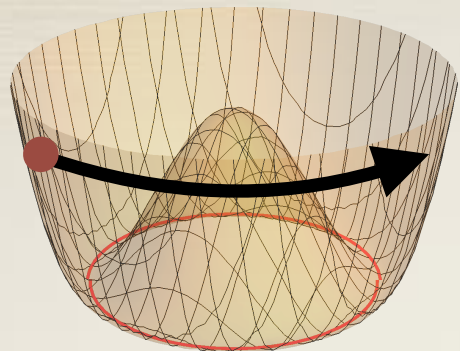
0.1

1

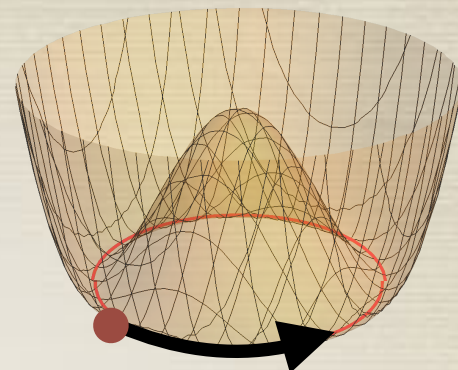
10

100

1000

 10^4 R 

$$c_s k \sim H$$



$$V(r) \sim m_r^2 r^2$$

Linear growth

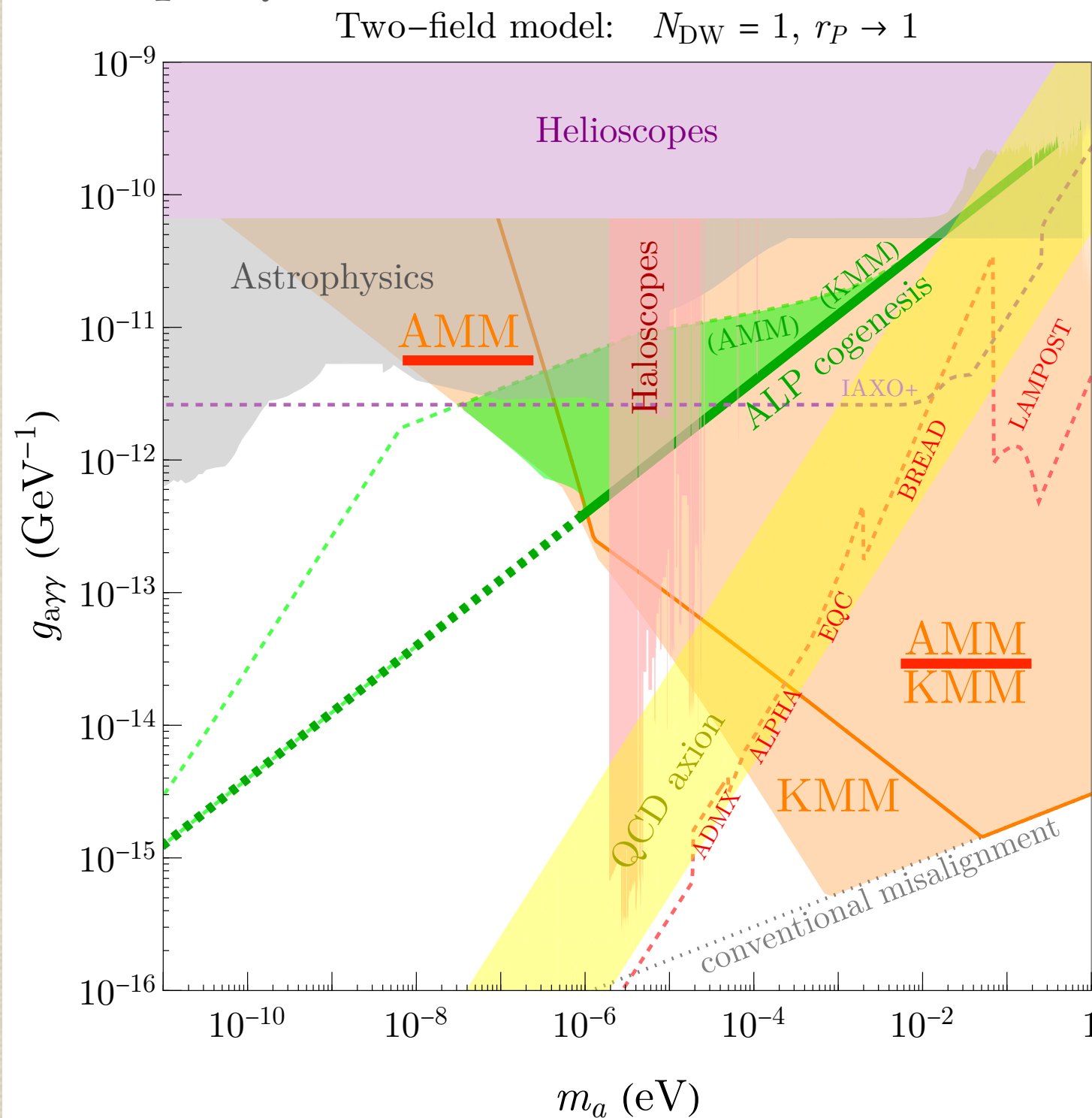
$$k \sim H$$

zero-mode
decreases
quickly

Dark matter

A supersymmetric model

Bodas, Co, Ghalsasi, KH and Wang (2025)



In the orange-shaded region with “AMM”, the observed dark matter density can be explained by acoustic misalignment

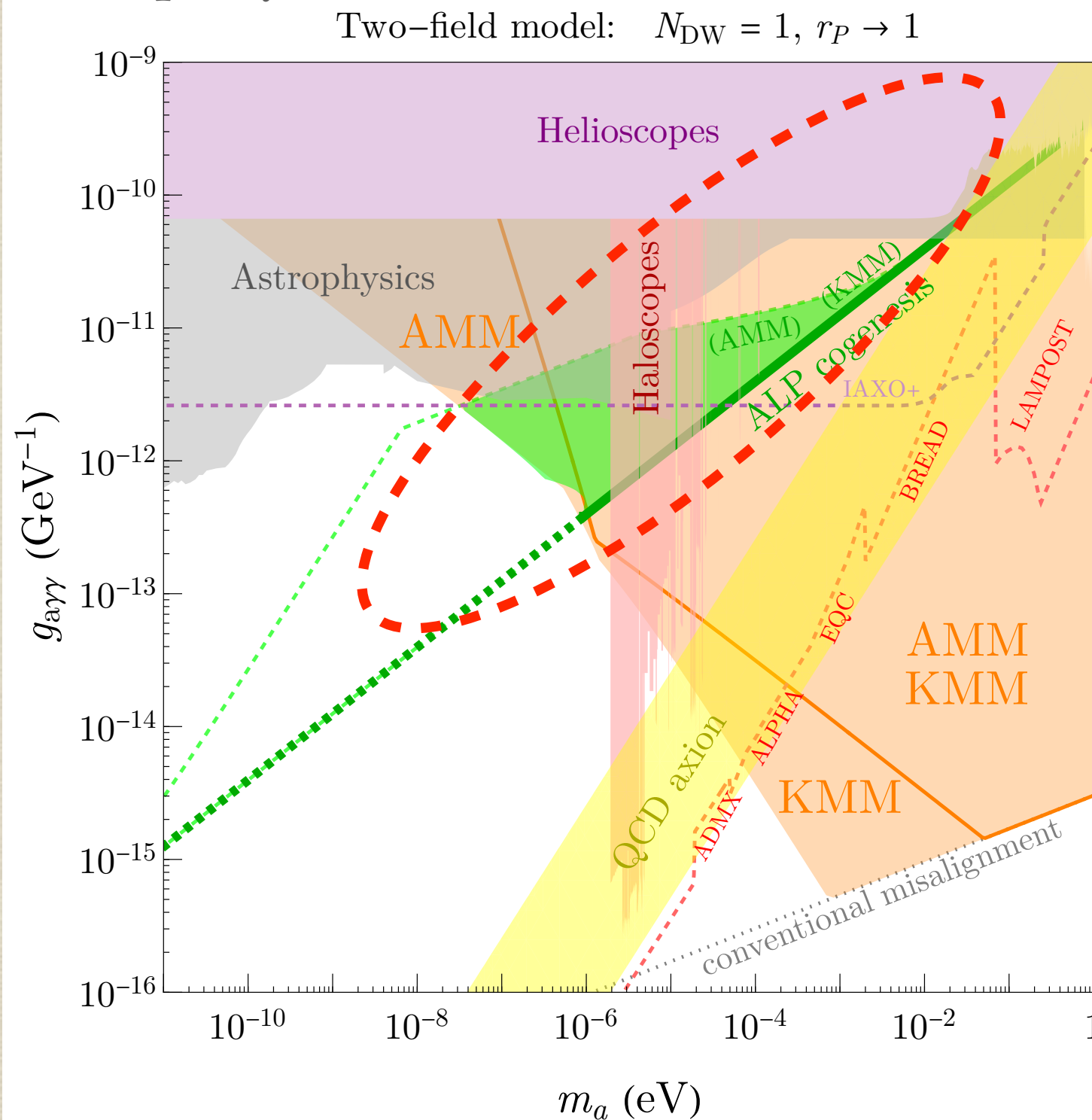
Outside the region, thermalization is not efficient or baryon asymmetry is overproduced by chiral plasma instability

Inflaton perturbation is assumed to be the only source of perturbations

Cogenesis of DM and baryon

A supersymmetric model

Bodas, Co, Ghalsasi, KH and Wang (2025)



In the green-shaded region, acoustic misalignment and axiogenesis by an electroweak process can explain both dark matter and baryon asymmetry

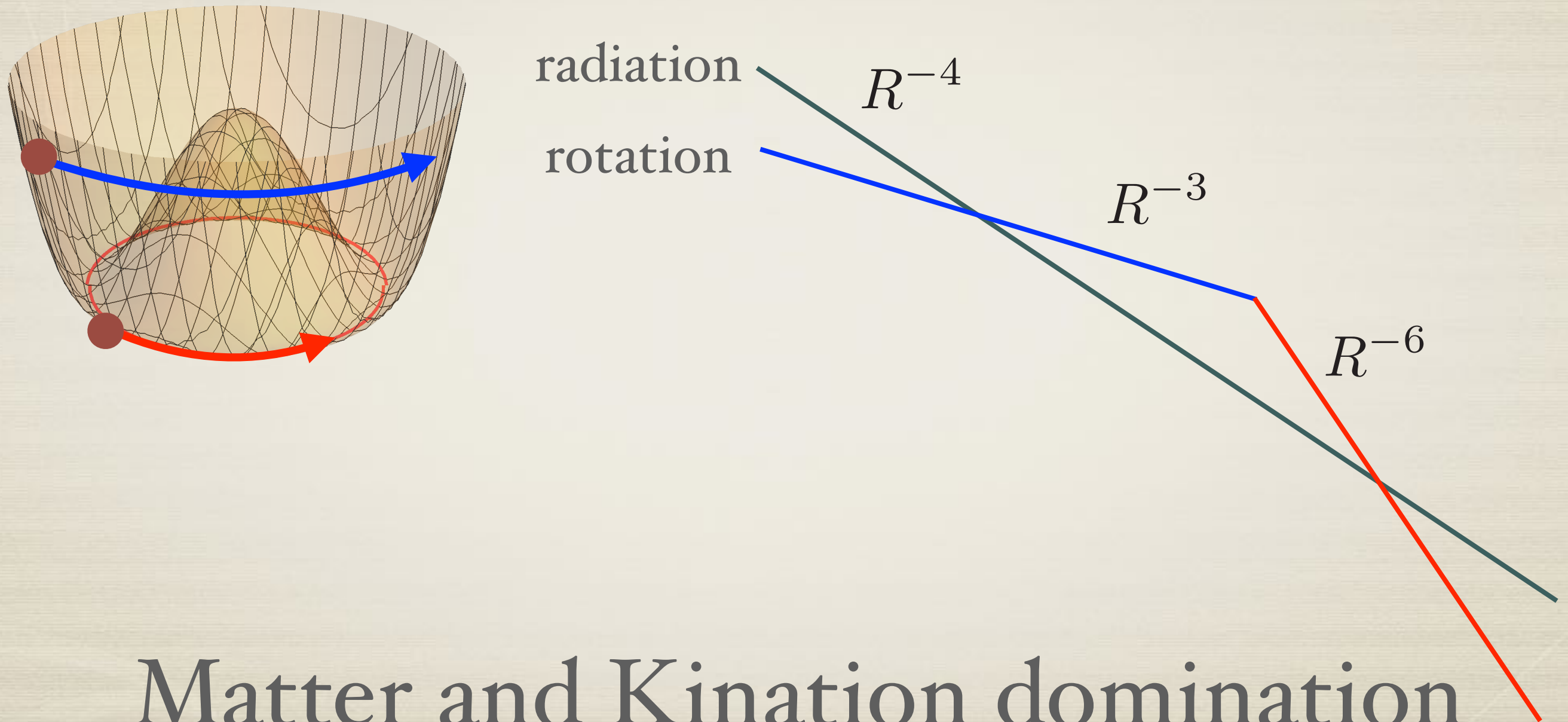
Outline

- * Axion rotation and baryon asymmetry
- * Axion rotation and dark matter
- * Gravitational waves
- * Summary



Equation of state

In a class of models (e.g. supersymmetric theories),



Primordial gravitational waves

Fluctuation of energy density
Quantum fluctuation
during inflation

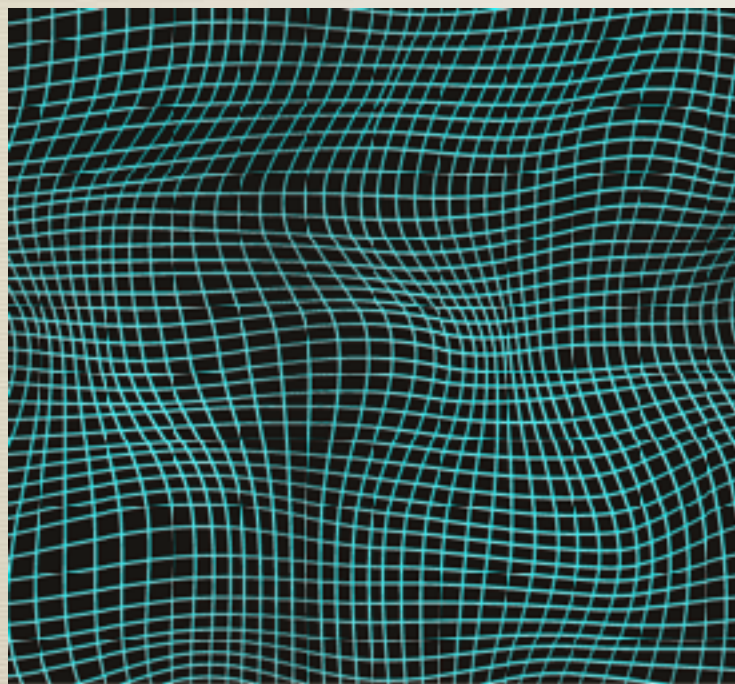
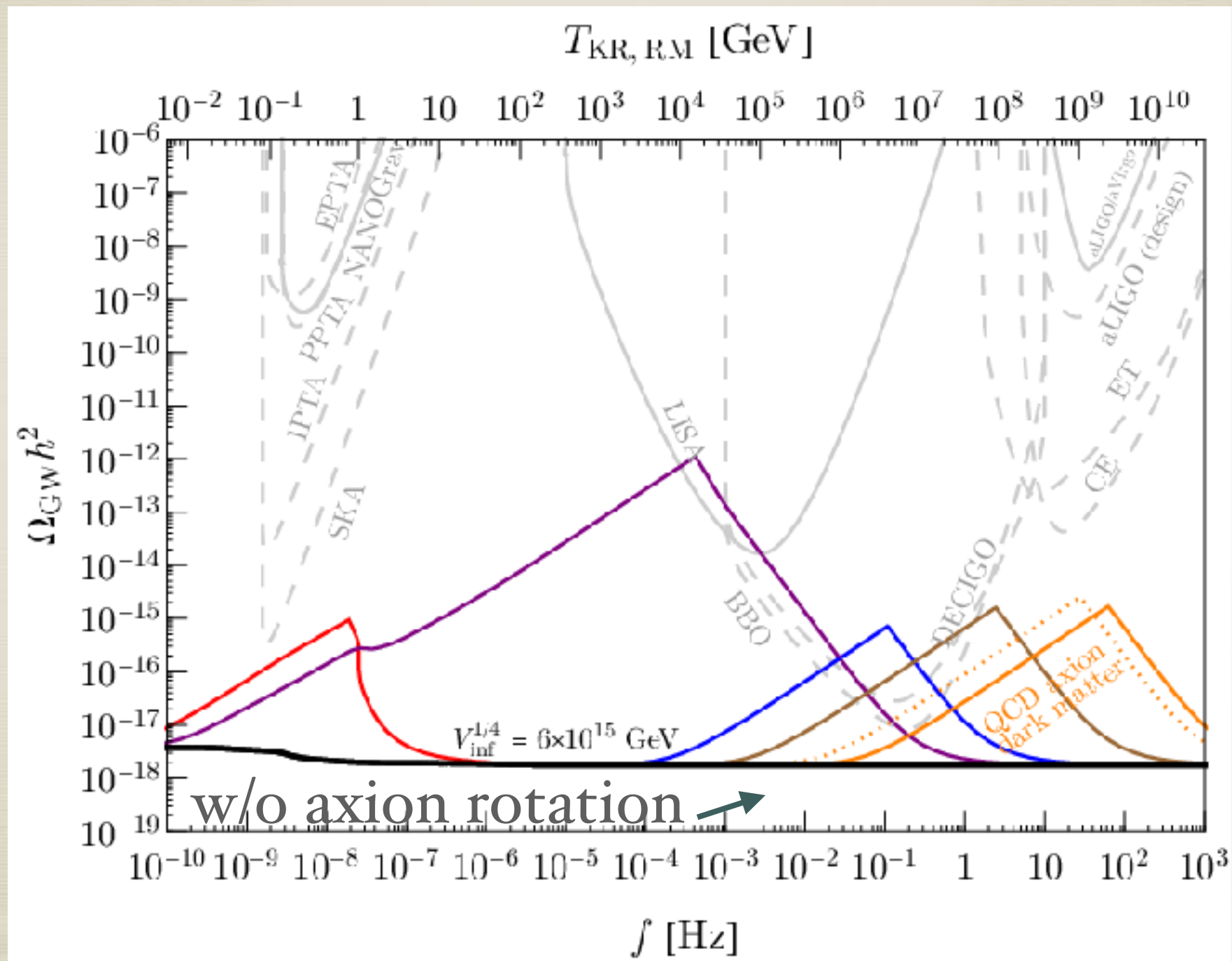


figure from ipmu.jp



Evolution/production of them depends on how the universe expanded, which is sensitive to axion kination

Ex. Inflation

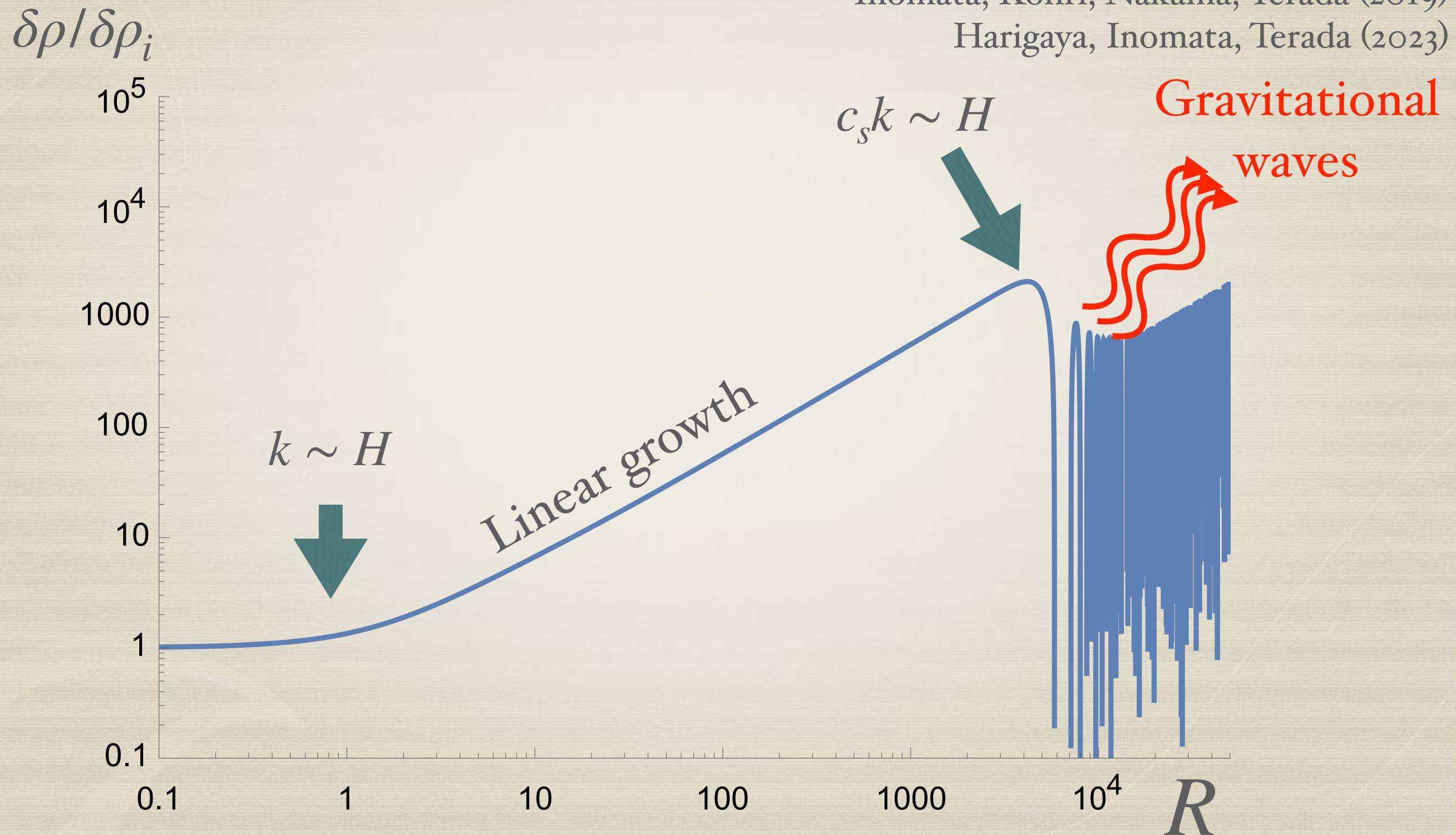


Co, Dunsky, Fernandez, Ghalsasi, Hall, KH and Shelton (2021)
 Gouttenoire, Servant, and Simakachorn (2021)

Production from rotation

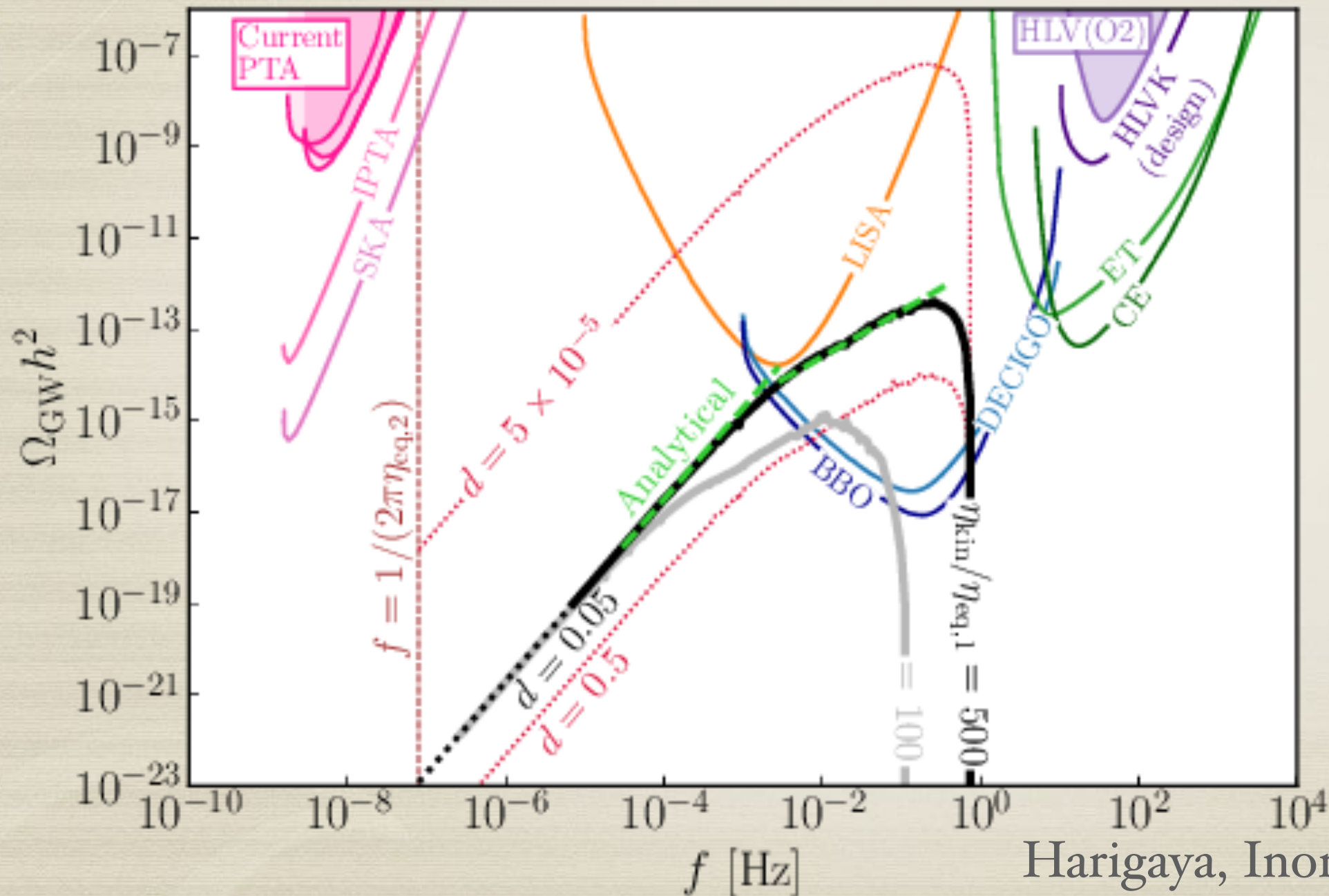
Inomata, Kohri, Nakama, Terada (2019)

Harigaya, Inomata, Terada (2023)



Spectrum

A sample point for an ALP



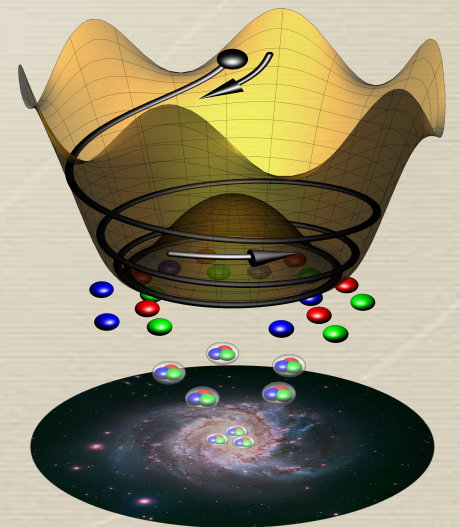
Inflaton perturbation
is assumed to be
the only source of
perturbations

Harigaya, Inomata, and Terada (2023)

d parameterize the rapidness of matter-kination transition

Summary

- * Rotation of axion in the field space can create matter-antimatter asymmetry
- * Rotation produces axion dark matter through phonon mode excitation from cosmic perturbations or through parametric resonance
- * Axions couplings are predicted to be larger than the prediction of the misalignment mechanism
- * Gravitational waves may be affected or created



Backup

Supersymmetric models

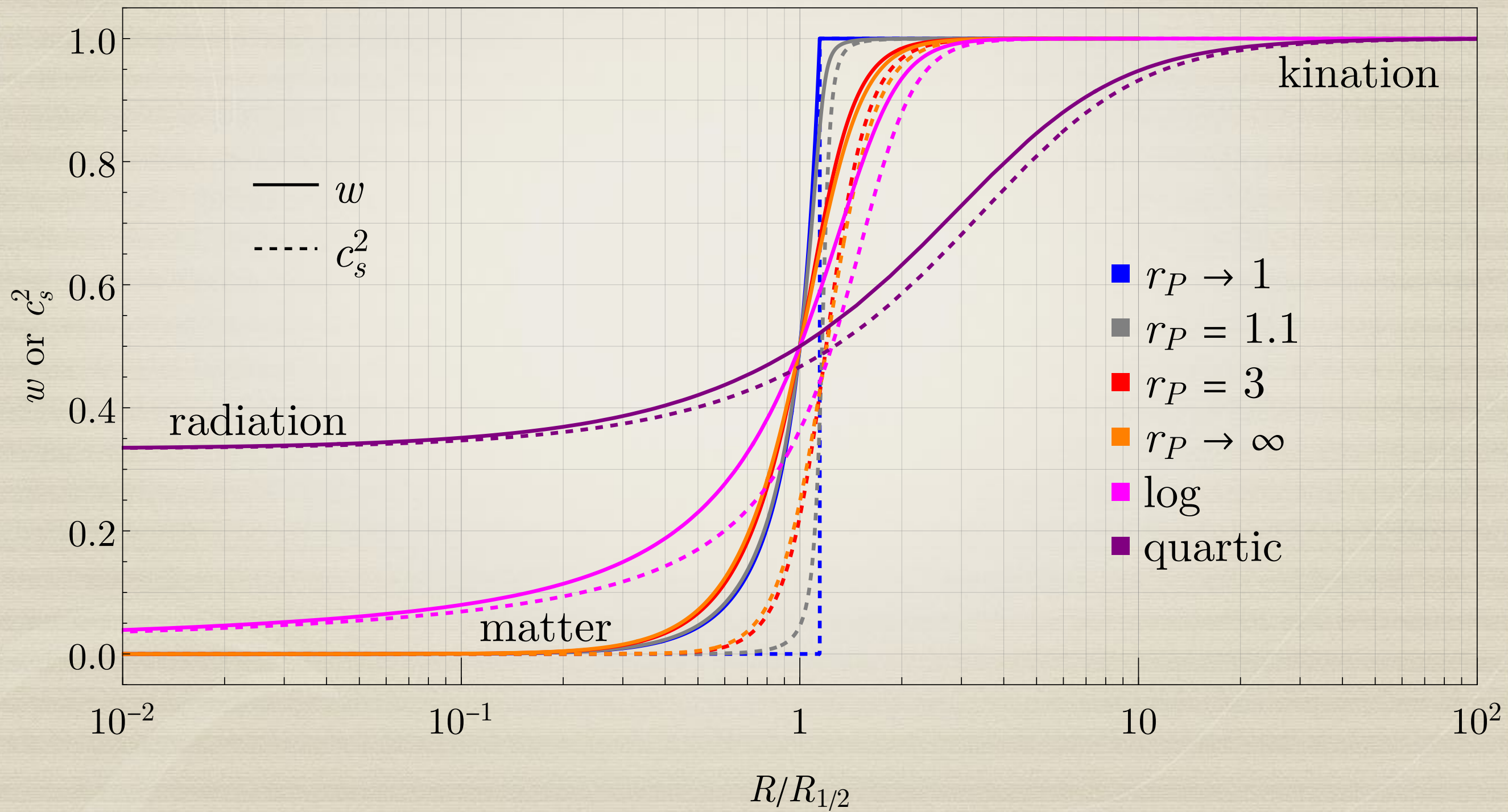
Log-potential model

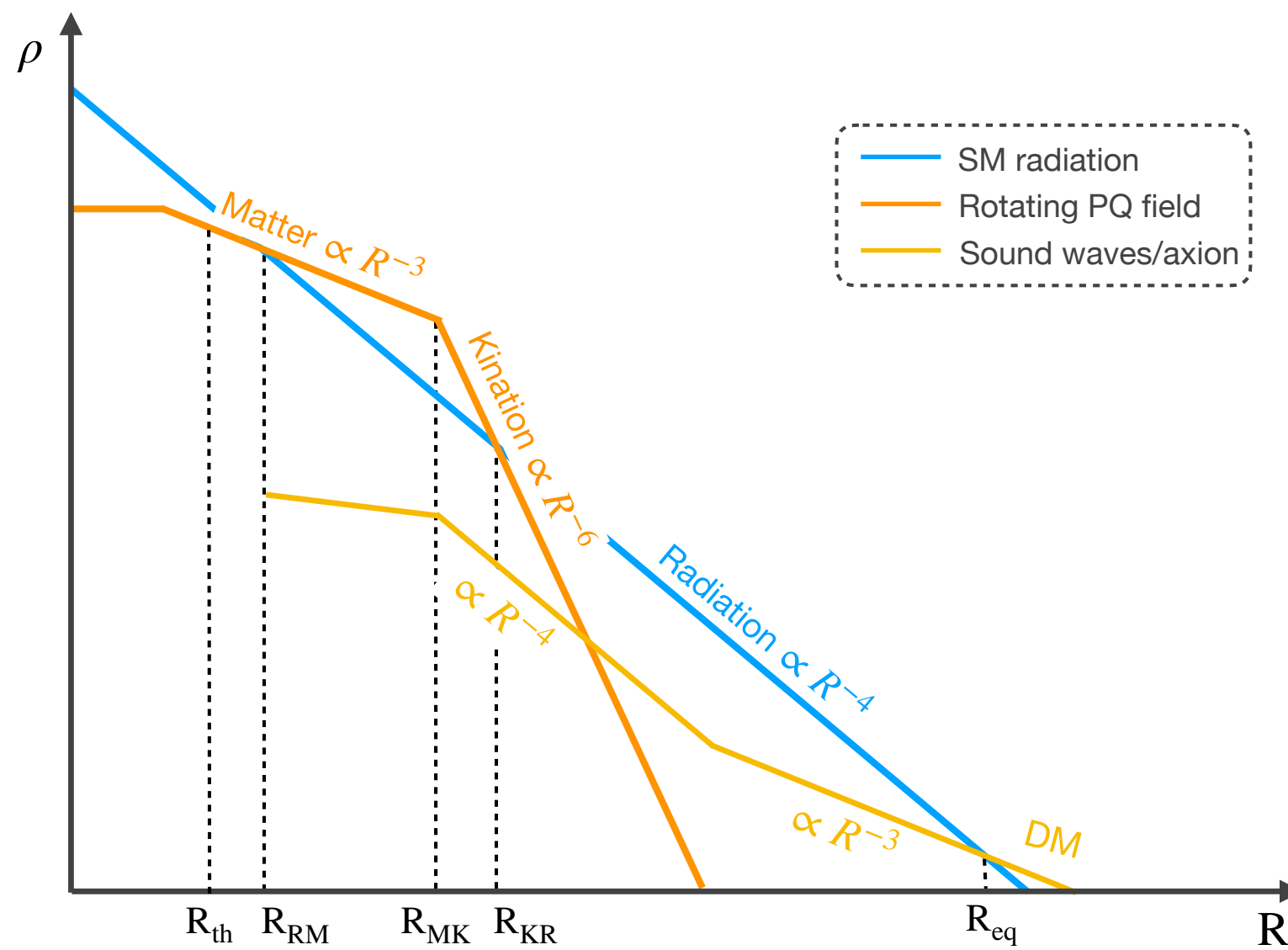
$$V(P) = \frac{1}{2} m_r^2 |P|^2 \left(\ln \frac{2 |P|^2}{f_a^2} - 1 \right)$$

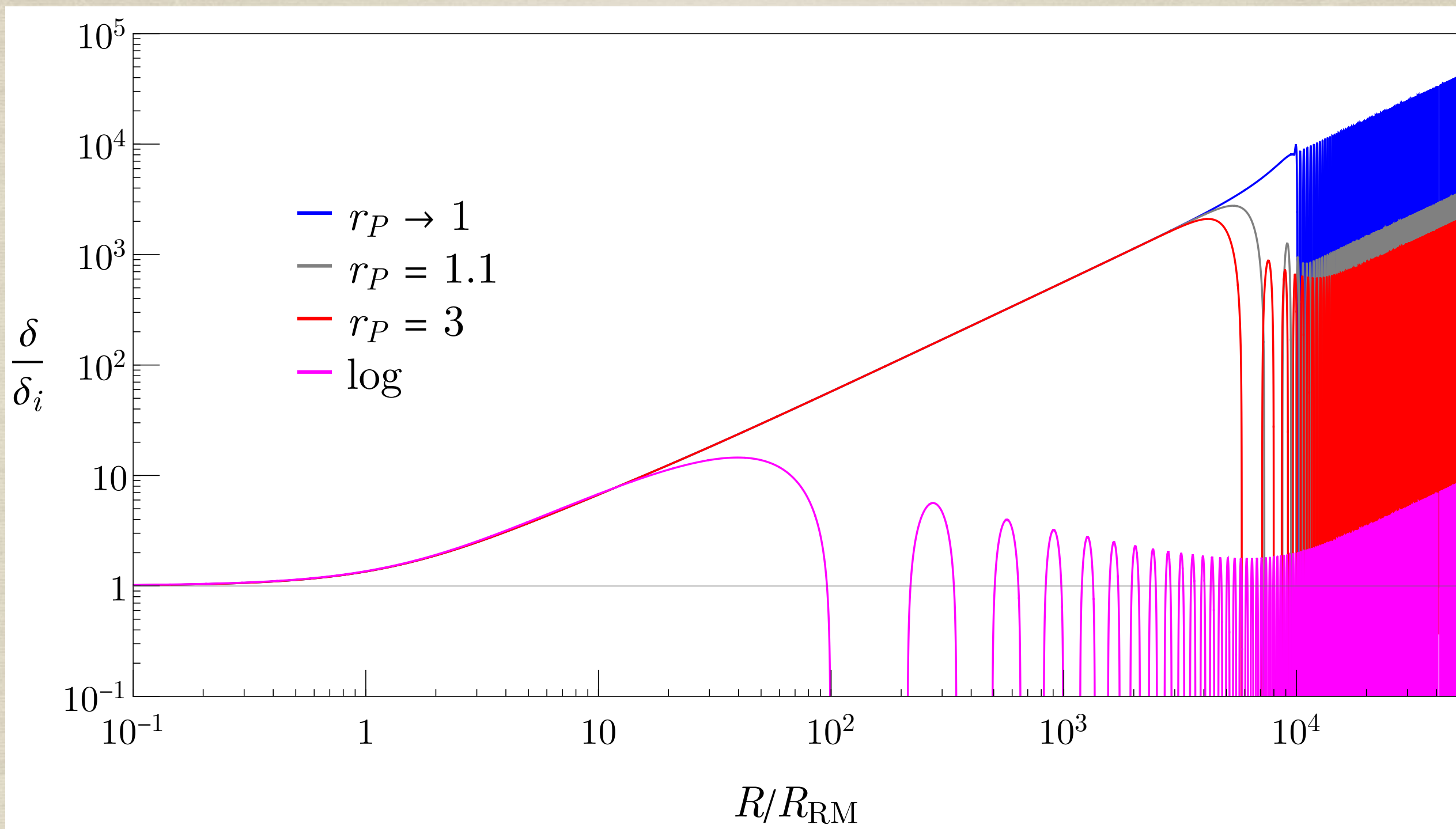
Two-field model

$$W = \lambda X (P \bar{P} - v_{PQ}^2), \quad V_{\text{soft}}(P) = m_P^2 |P|^2 + m_{\bar{P}}^2 |\bar{P}|^2.$$

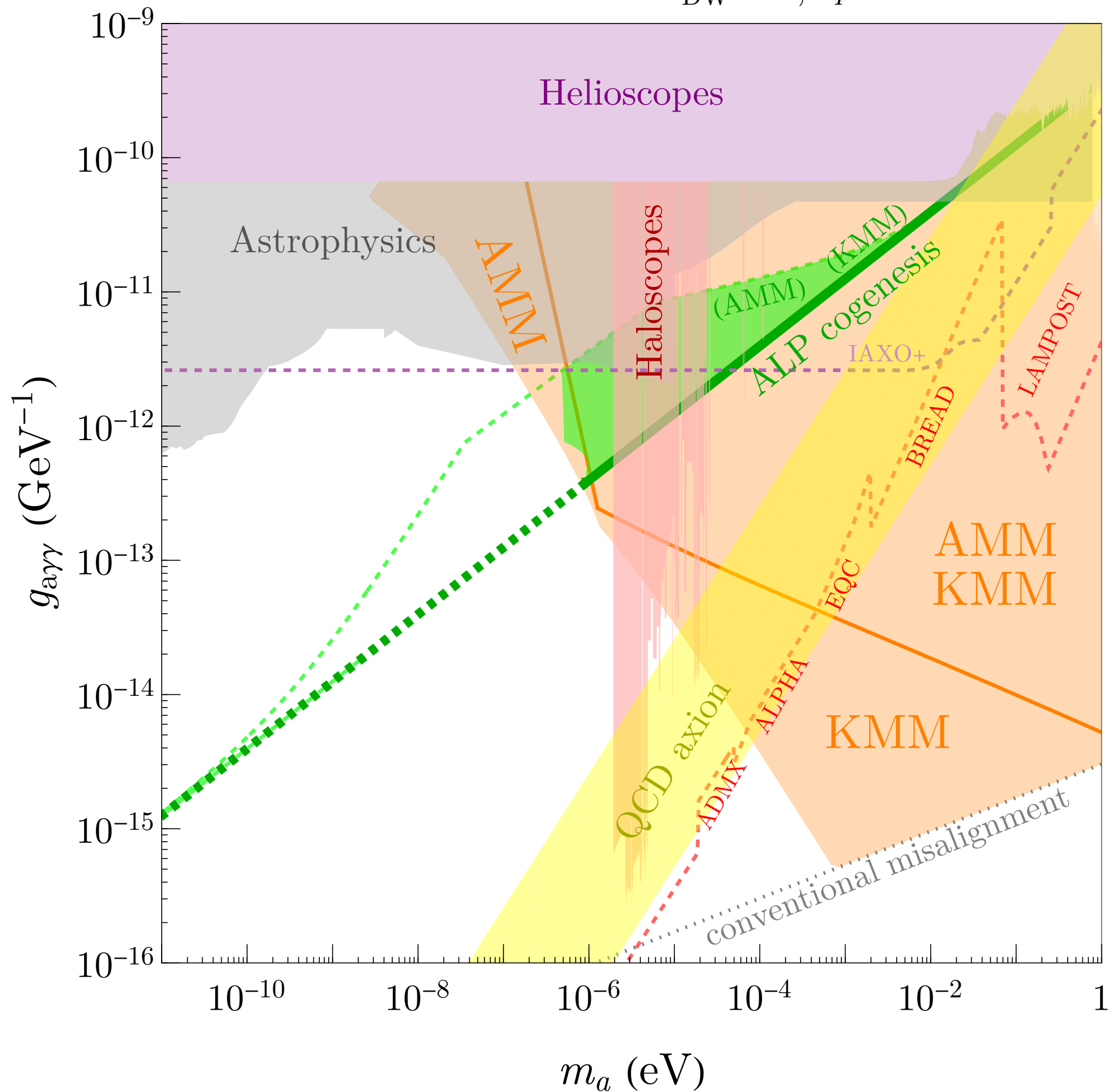
$$r_P \equiv m_{\bar{P}}/m_P$$



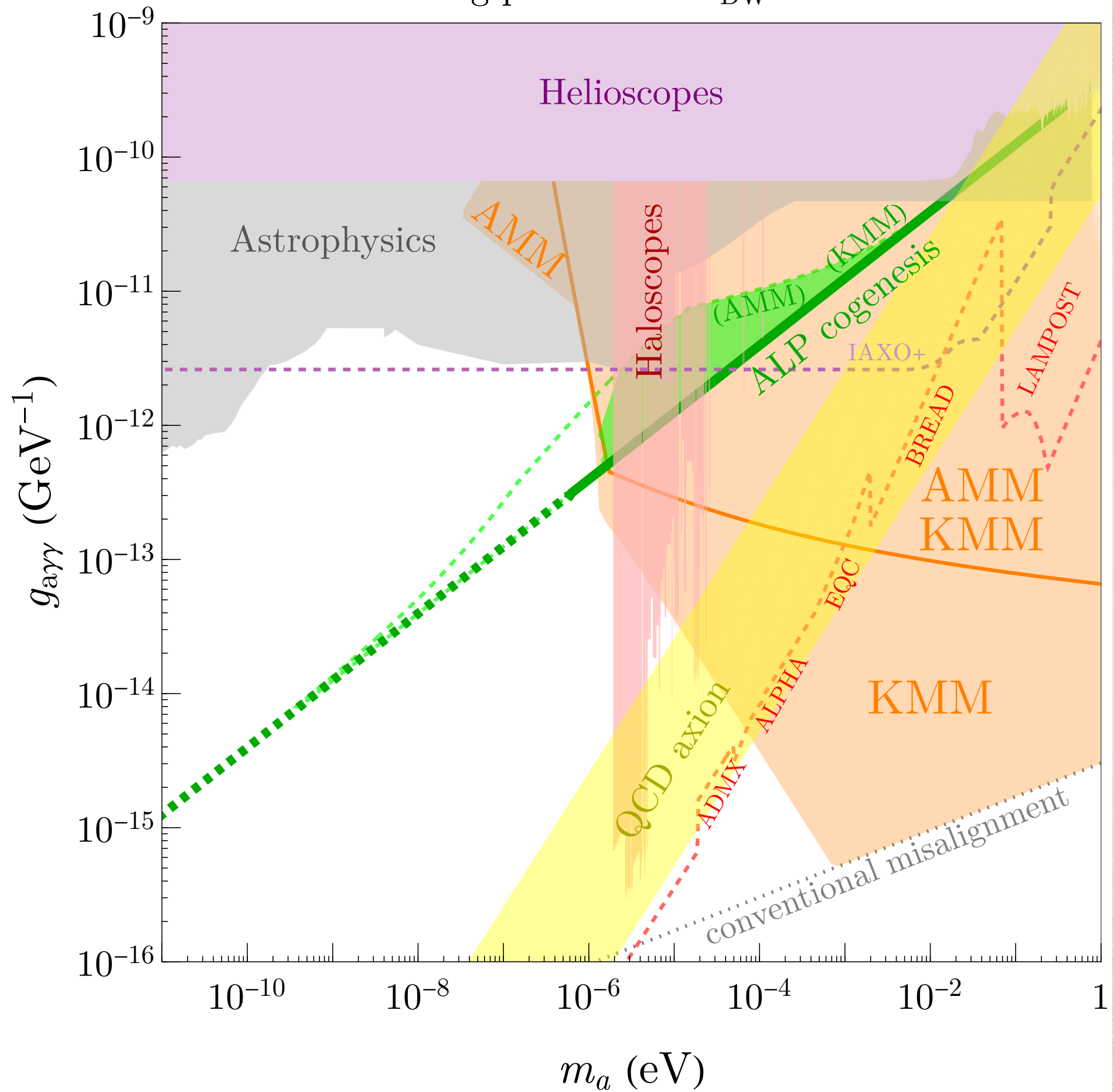




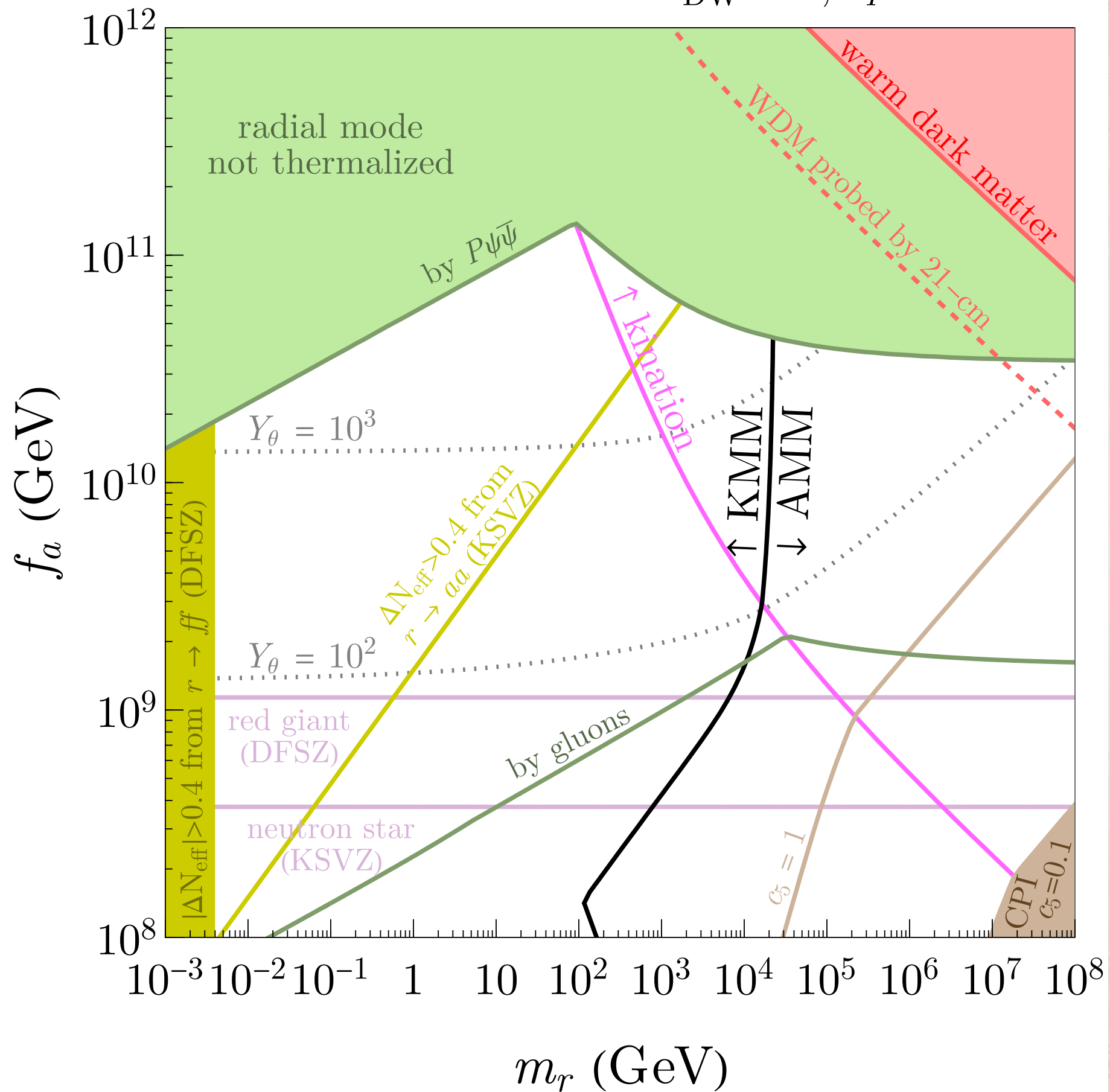
Two-field model: $N_{\text{DW}} = 1, r_P \gg 1$



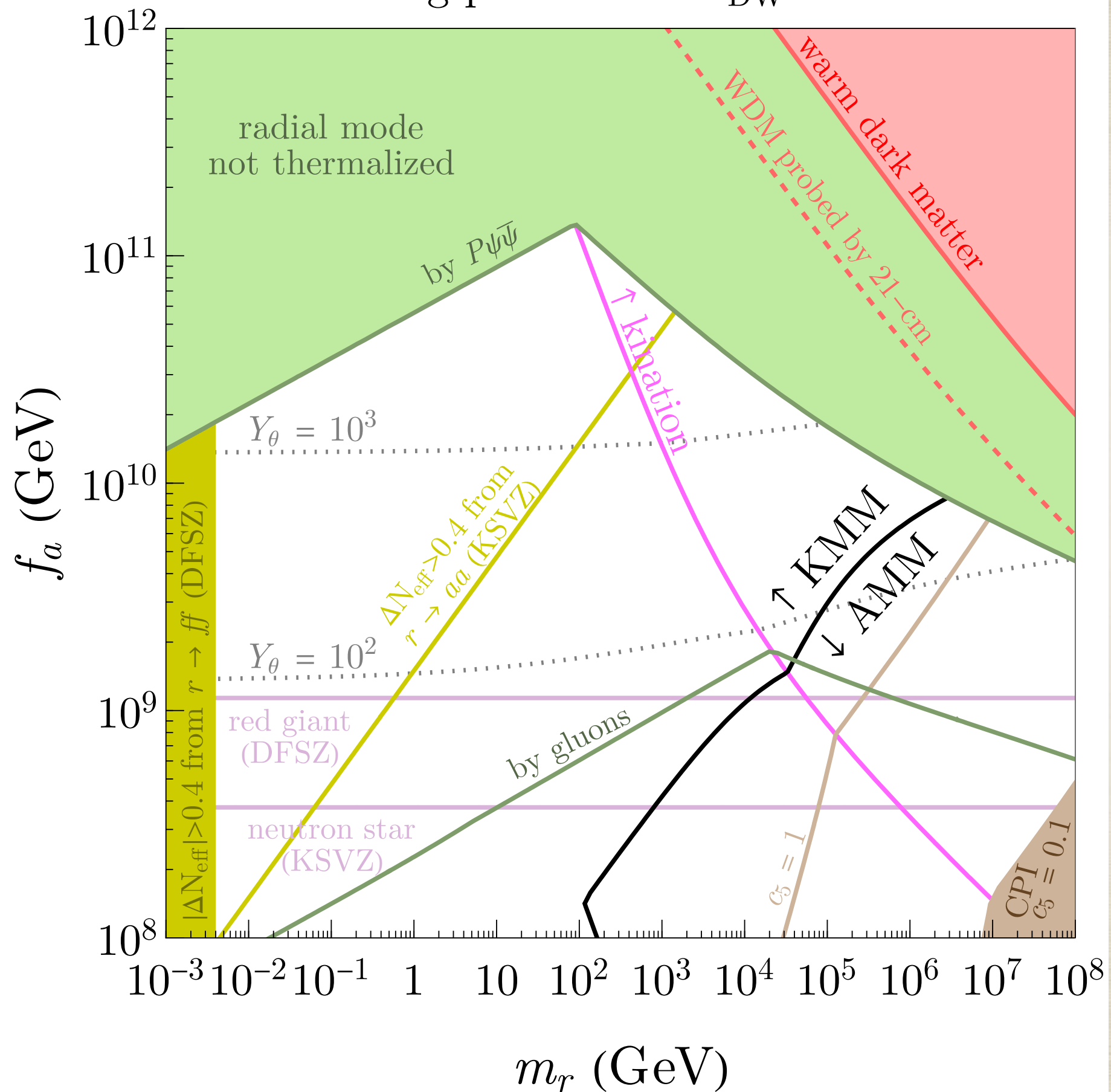
Log potential: $N_{\text{DW}} = 1$



Two-field model: $N_{\text{DW}} = 1$, $r_P \rightarrow 1$

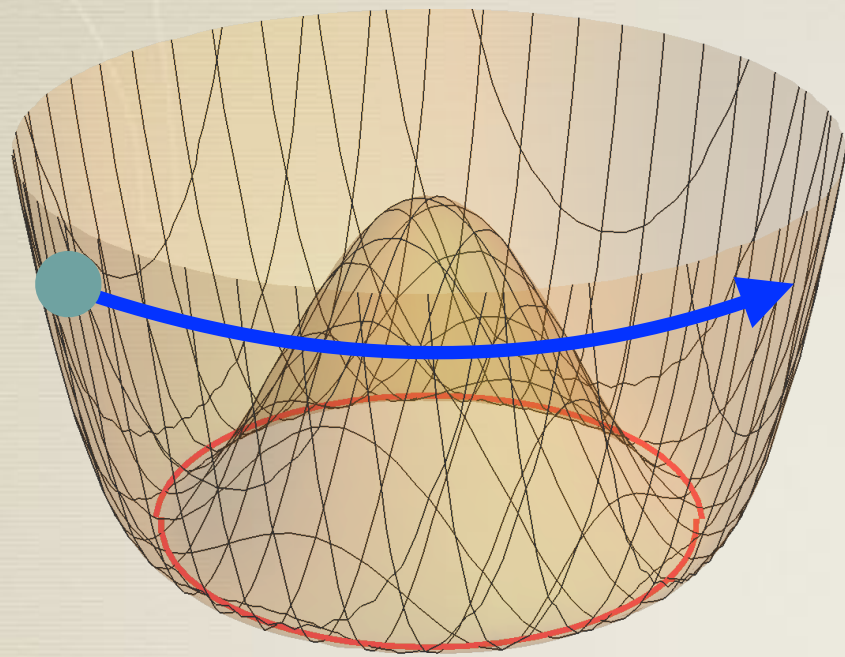


Log potential: $N_{\text{DW}} = 1$



Evolution of energy density

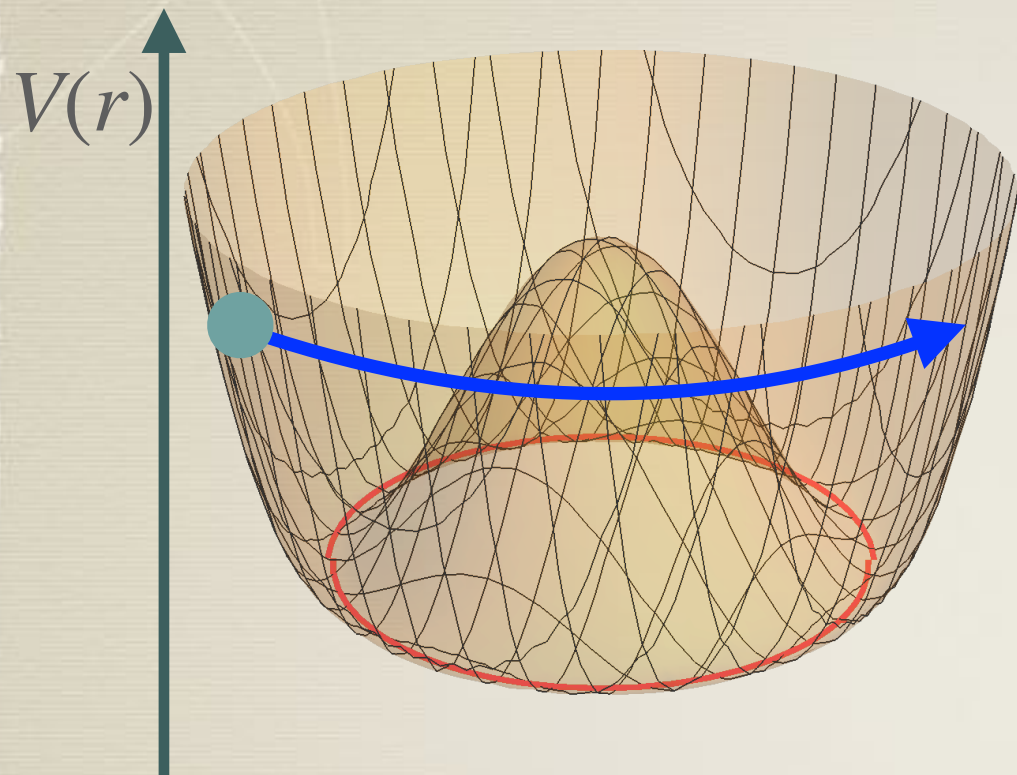
Co and KH (2019)



Classical mechanics

Evolution of energy density

Co and KH (2019)



$$\frac{dV}{dr} = \dot{\theta}^2 r$$

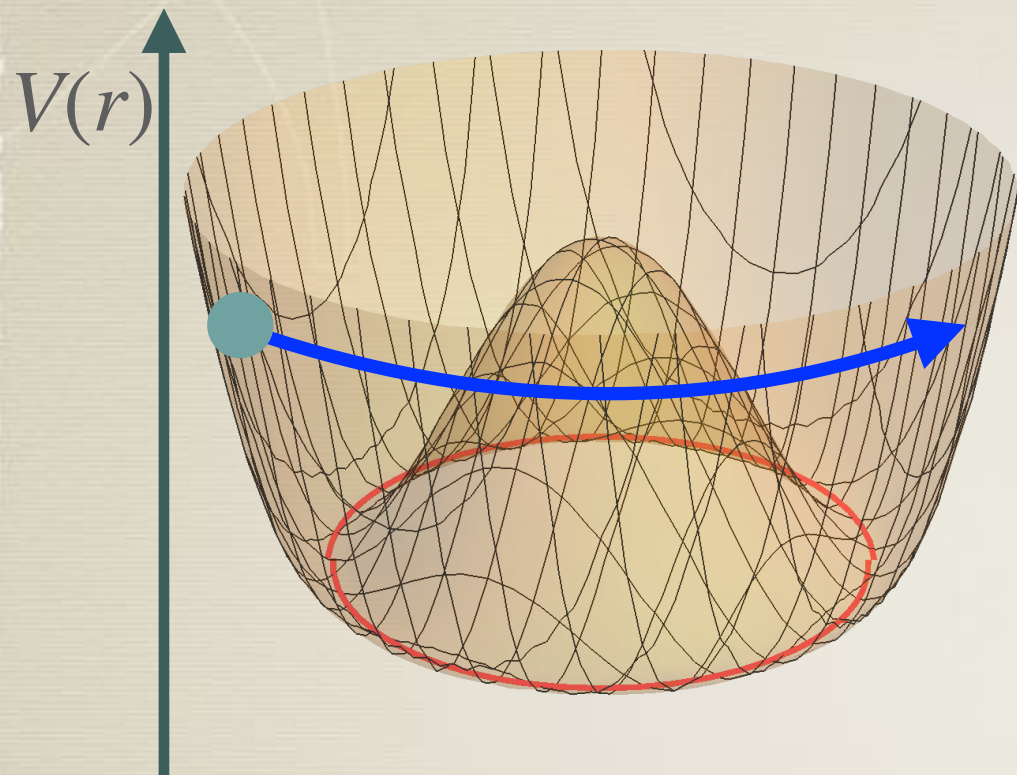
Centripetal force Centrifugal force

$$\dot{\theta} r^2 \propto R^{-3}$$

Angular momentum conservation
(up to dilution by cosmic expansion)

Evolution of energy density

Co and KH (2019)



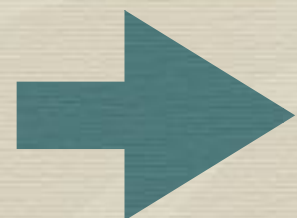
$$\frac{dV}{dr} = \dot{\theta}^2 r$$

$$m_P^2 r = \dot{\theta}^2 r \rightarrow \dot{\theta} = m_P$$

$$\dot{\theta} r^2 \propto R^{-3} \\ \rightarrow r^2 \propto R^{-3}$$

$$V(r) \sim \frac{1}{2} m_P^2 r^2$$

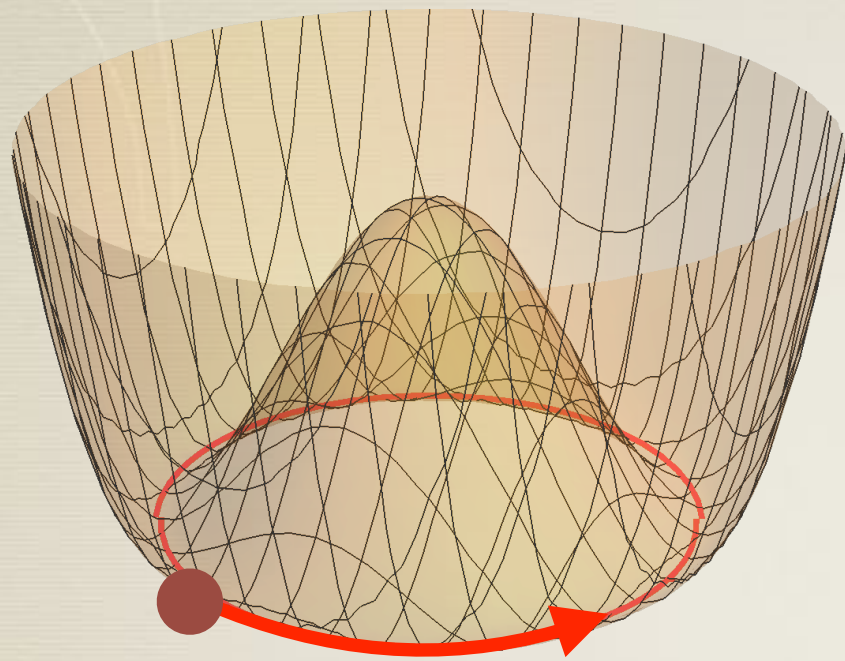
(supersymmetric theory)



$$\rho \sim m_P^2 r^2 + \dot{\theta}^2 r^2 \propto R^{-3} \text{ matter}$$

Evolution of energy density

Co and KH (2019)



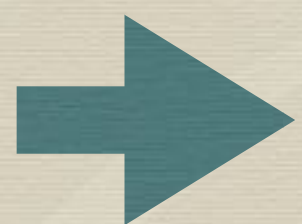
r is nearly fixed

$$\frac{dV}{dr} = \dot{\theta}^2 r$$

$\rightarrow \dot{\theta}$ decreases

$$\dot{\theta} r^2 \propto R^{-3}$$

$$\rightarrow \dot{\theta} \propto R^{-3}$$



$$\rho = \dot{\theta}^2 r^2 \propto R^{-6} \quad \text{kination}$$