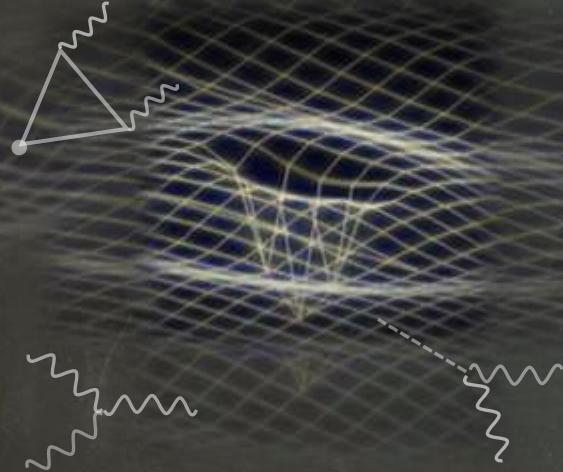


The Particle Physics of Axion Inflation

From Theory to Observation



Azadeh Maleknejad
Swansea University

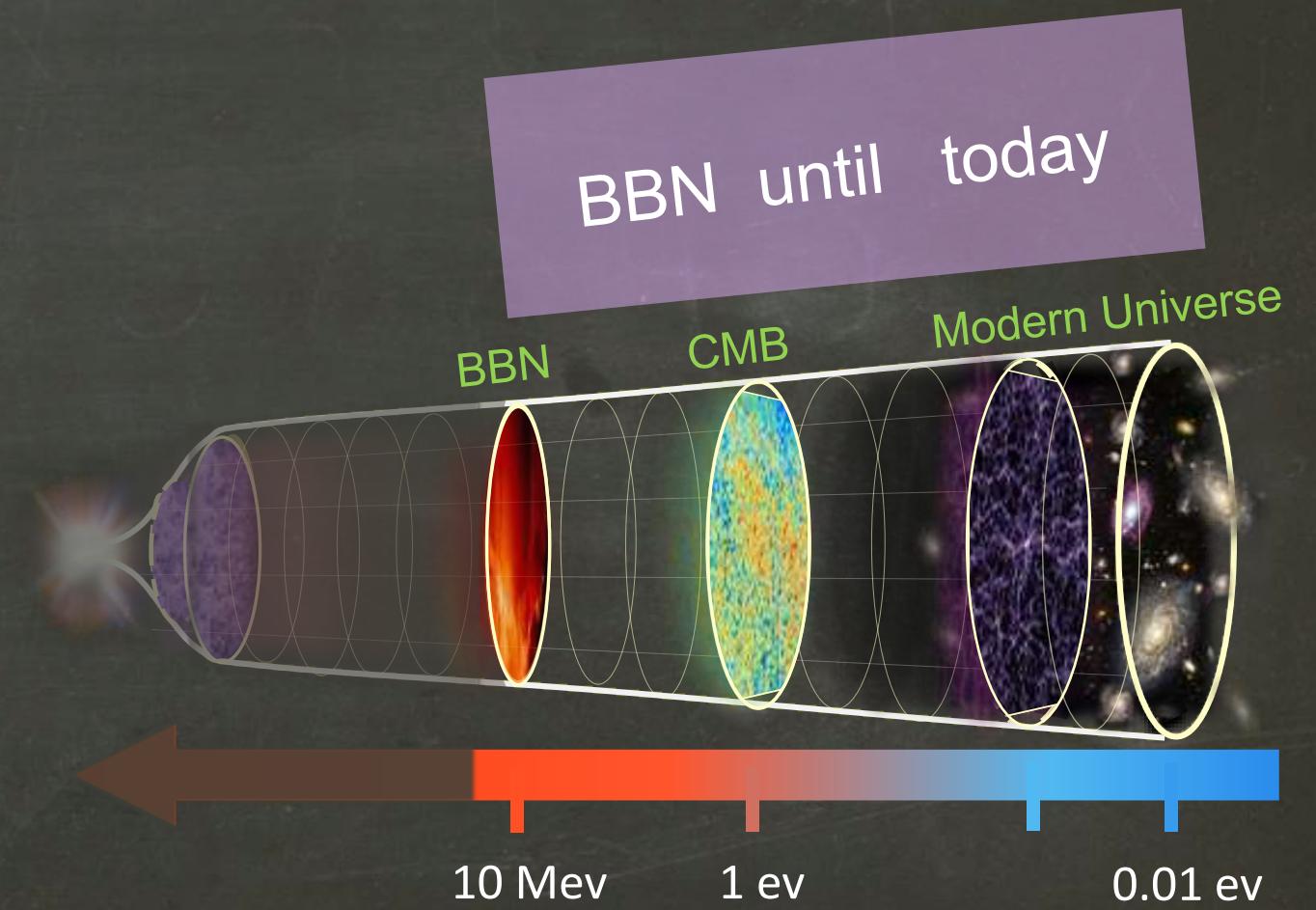


Cosmic History

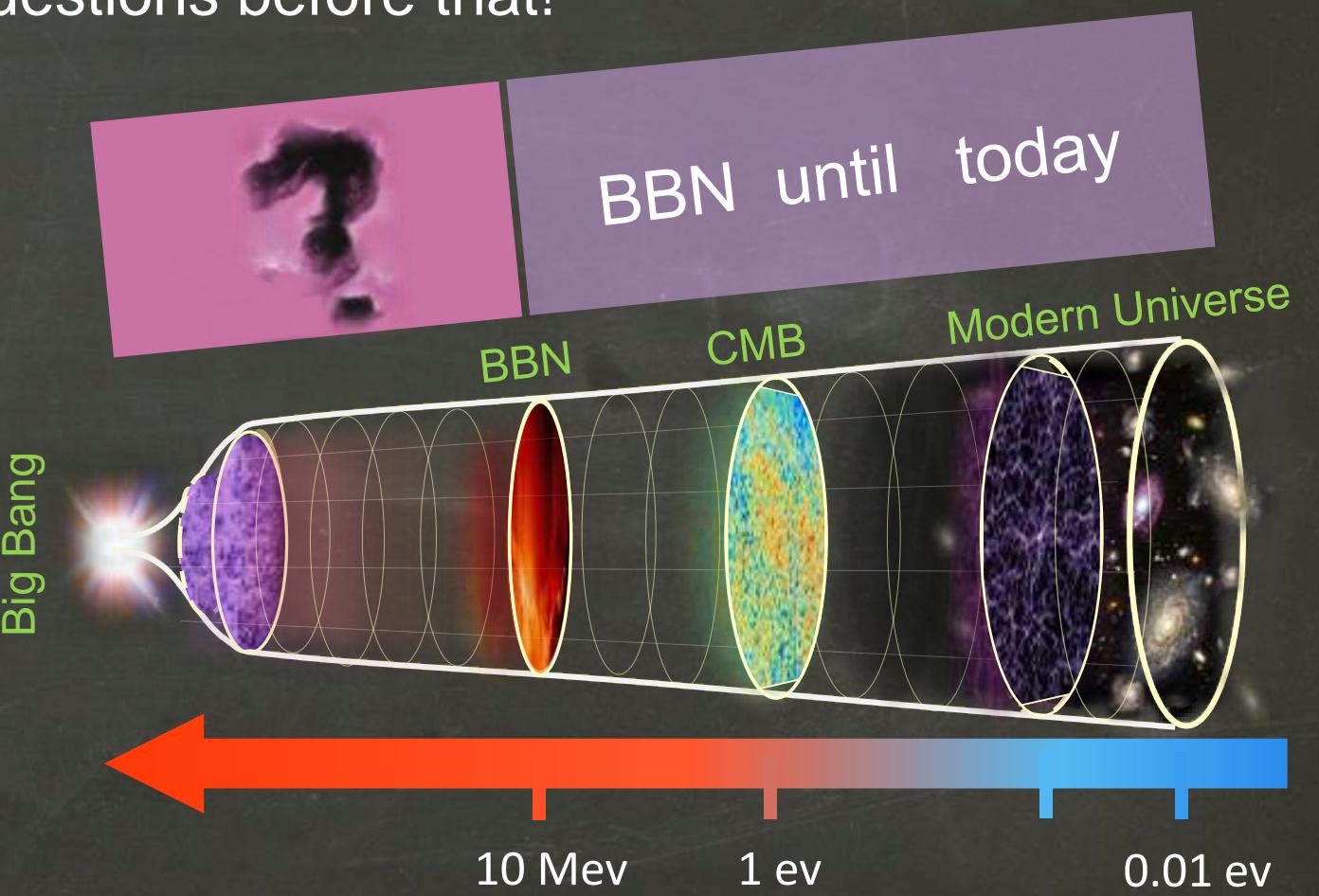


What we know so far?

Particle cosmology is successful in explaining our universe from BBN onward.

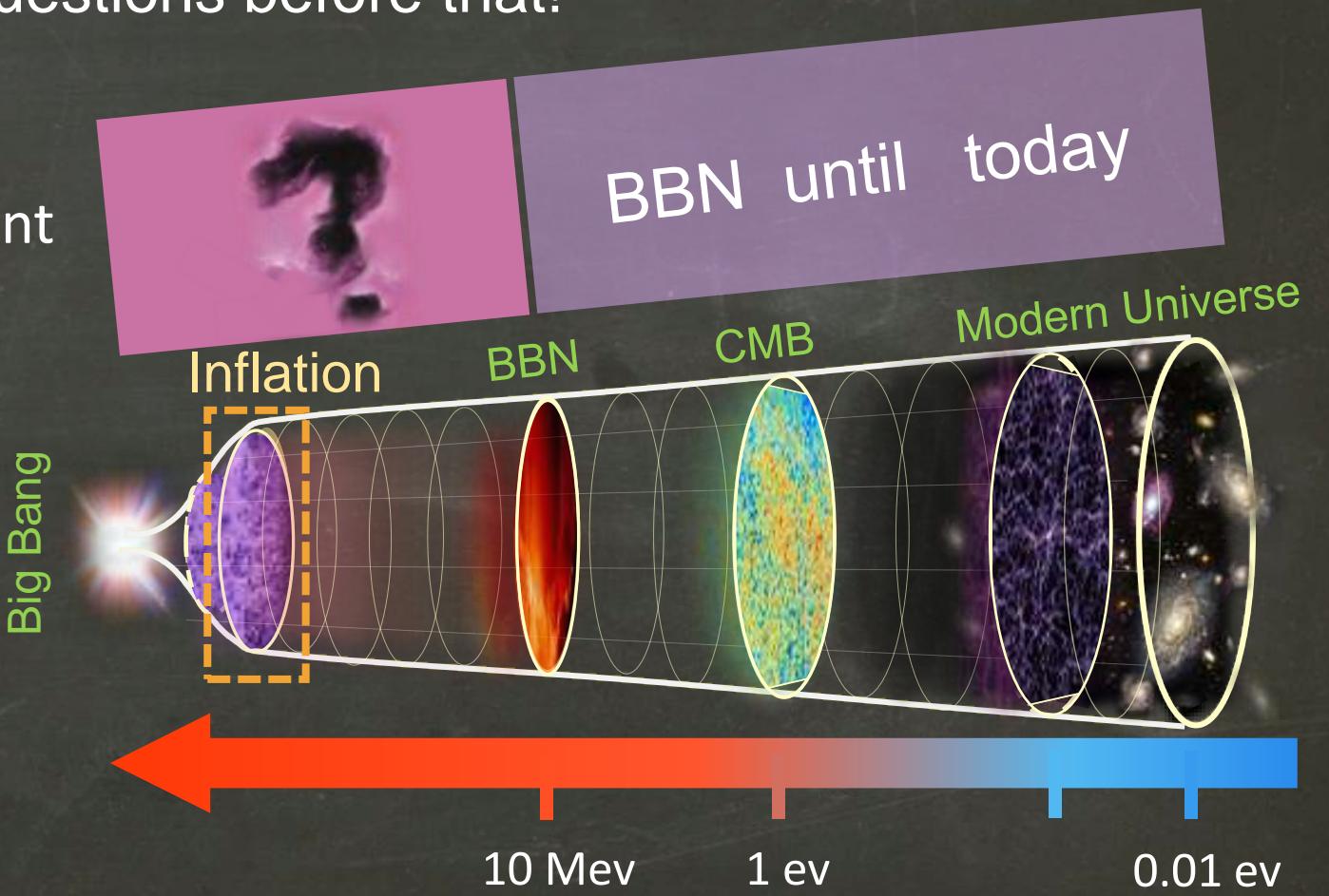


Particle cosmology is successful in explaining our universe from BBN onward.
But there are still major open questions before that!



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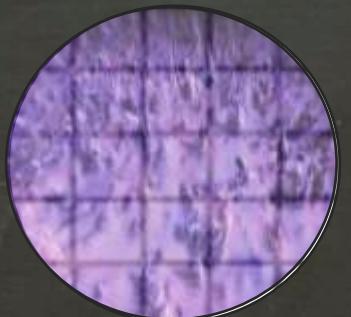
Current observations are in agreement
with the paradigm of inflation.



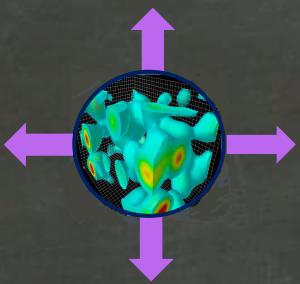
Density Perturbations

Cosmic inflation turns initial quantum vacuum fluctuations

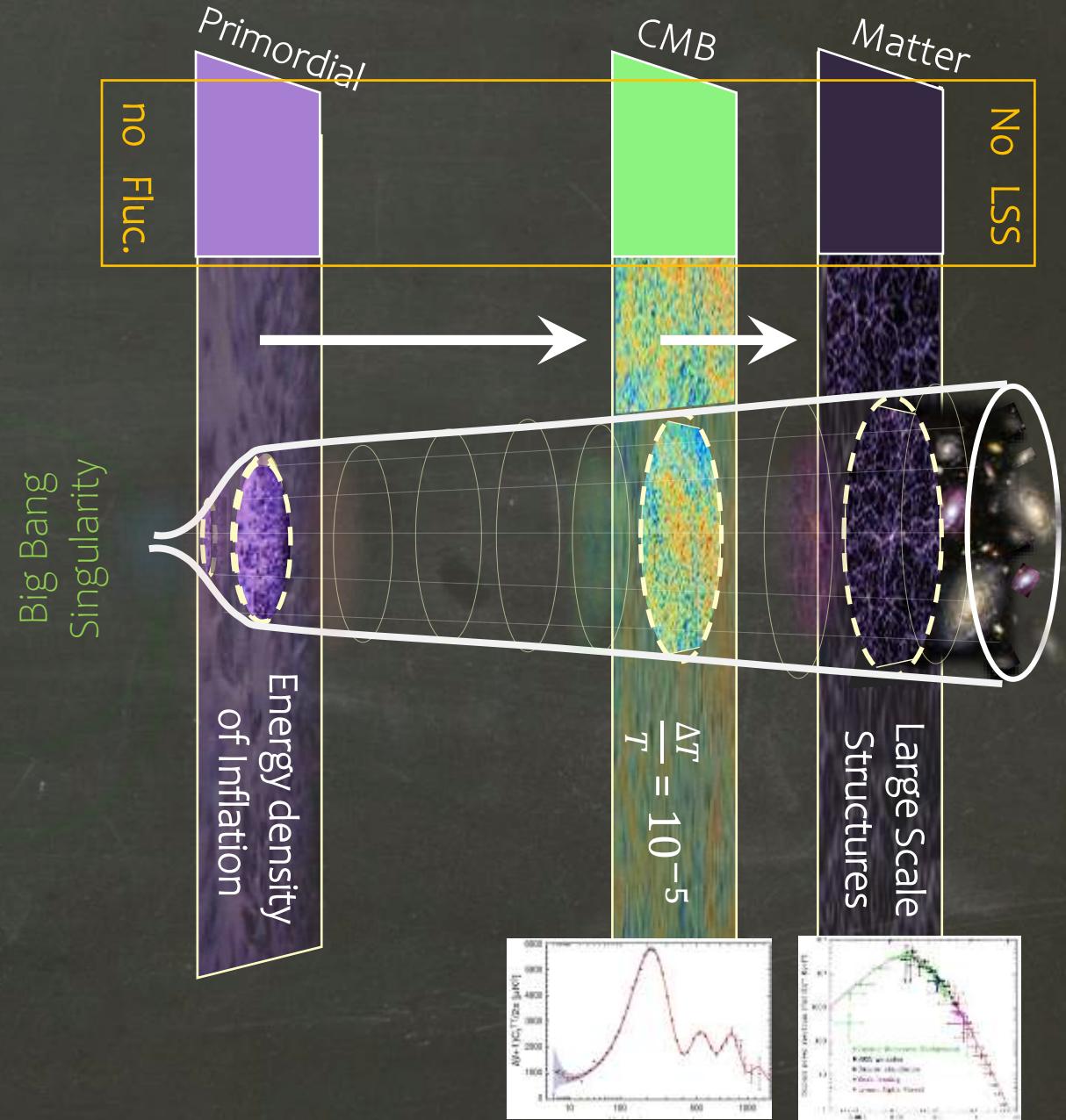
into actual cosmic perturbations.



a_f

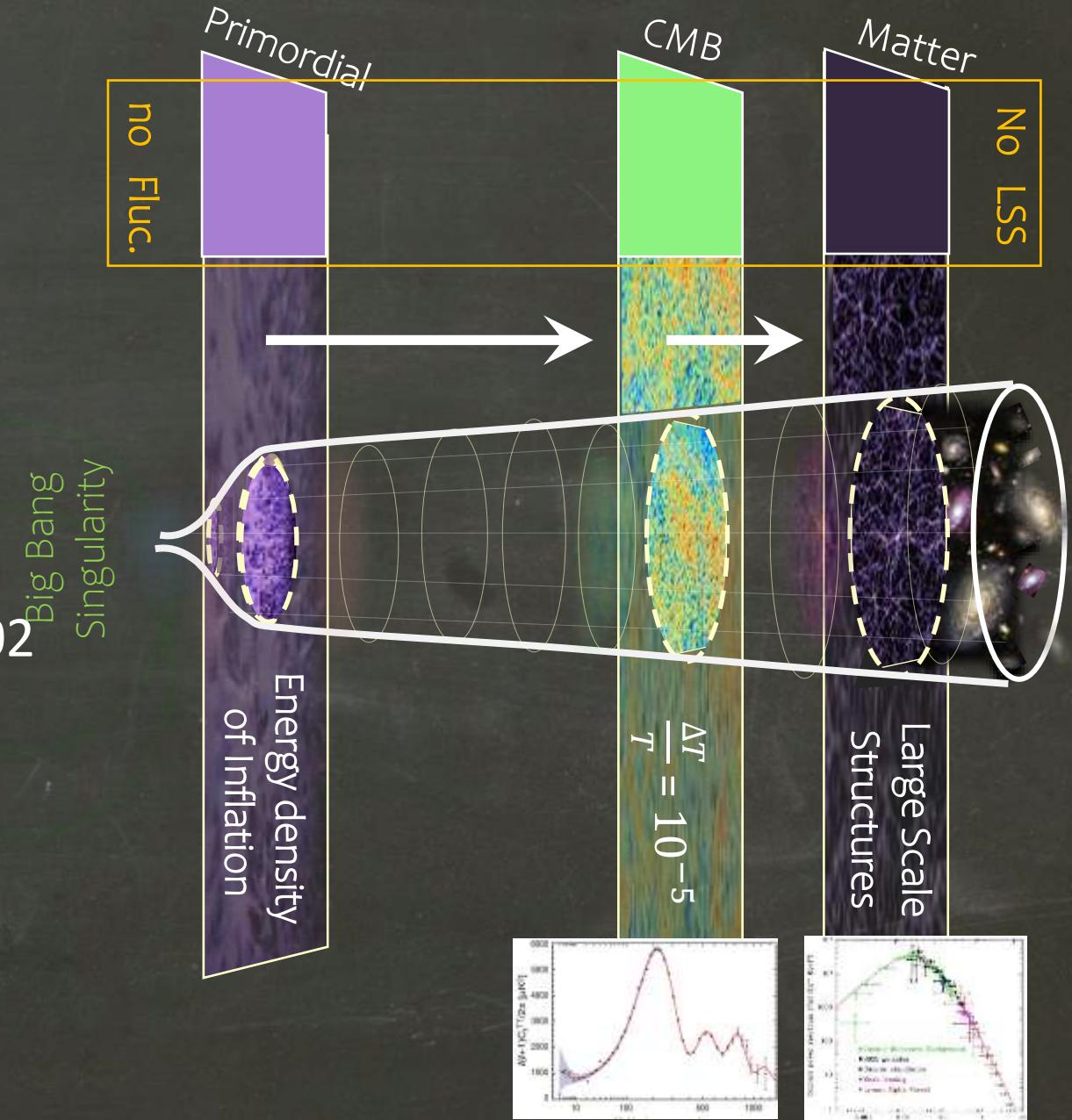


a_i



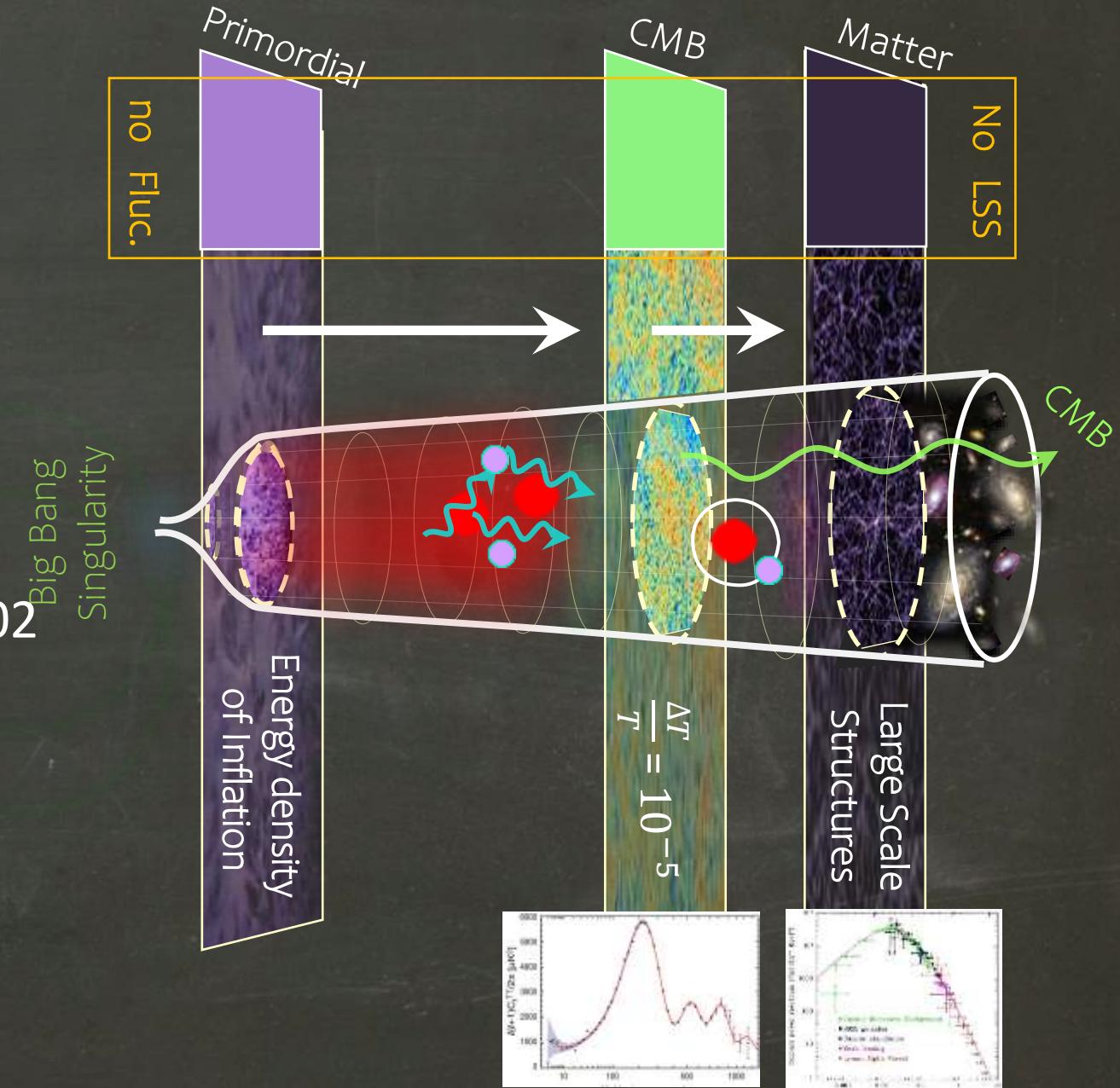
Density Perturbations

- ✓ red-tilted adiabatic spectrum
- ✓ Gaussianity,
- ✓ spatial flatness $\Omega_K = 0.001 \pm 0.002$
- ✓ no isocurvature $\beta_{iso} \lesssim 10^{-2}$



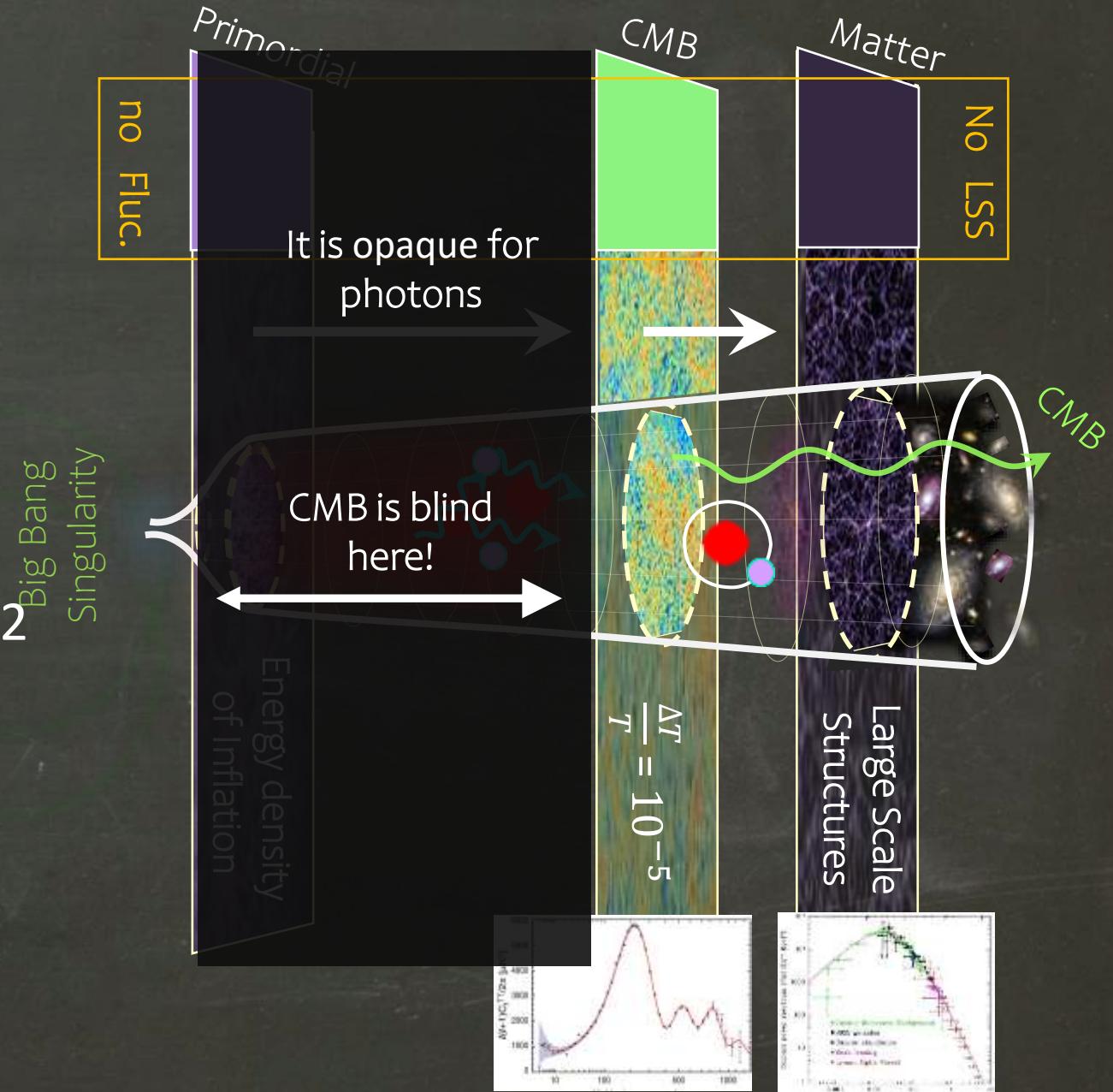
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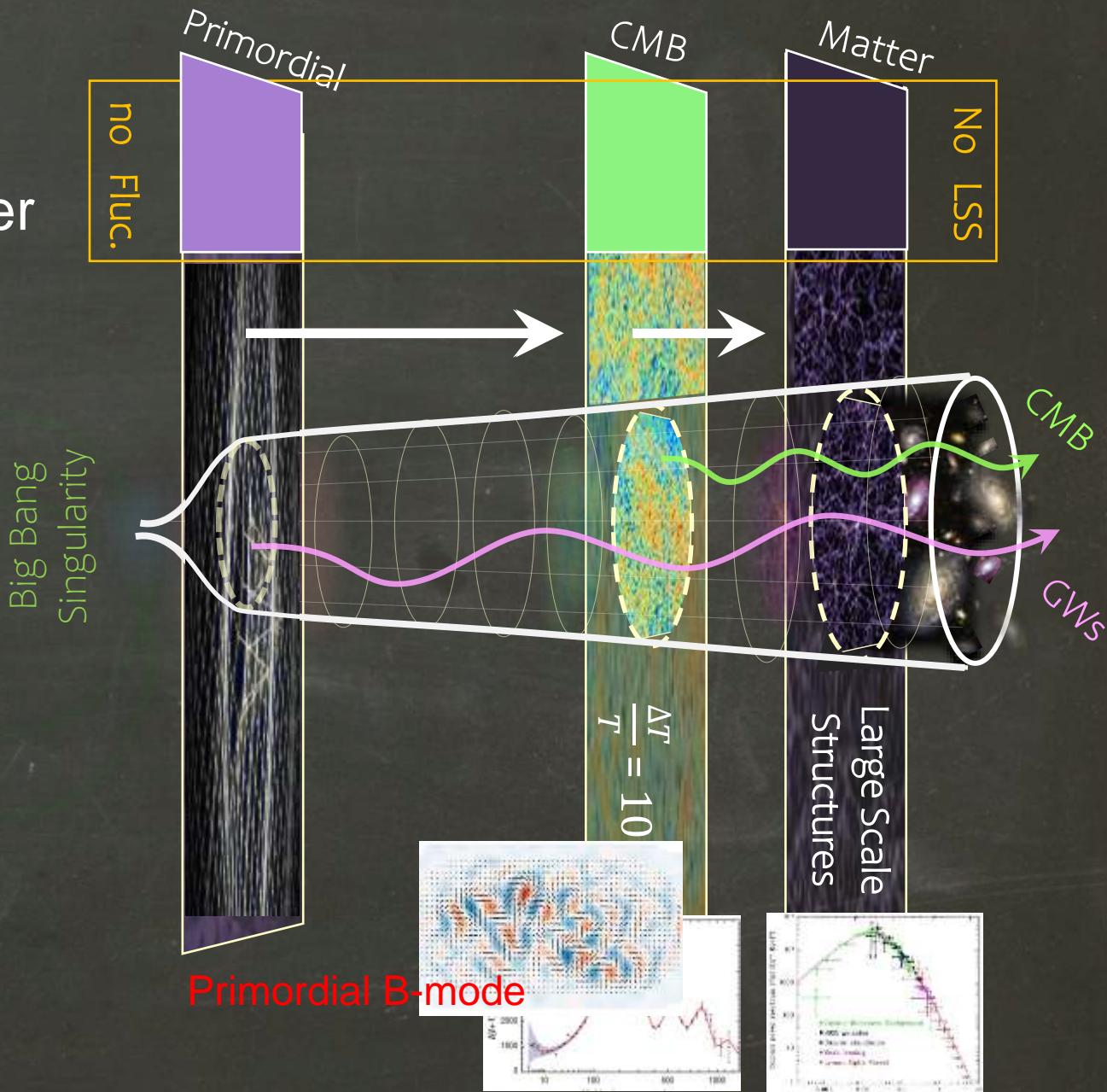
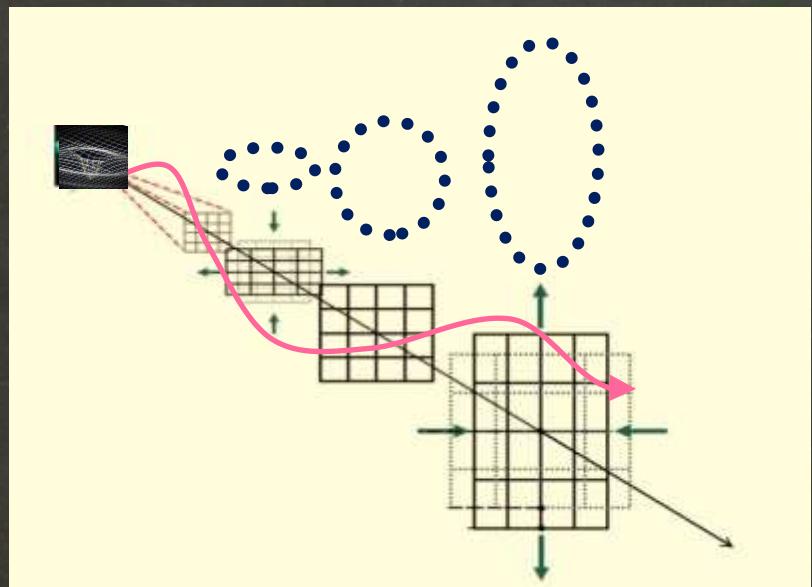
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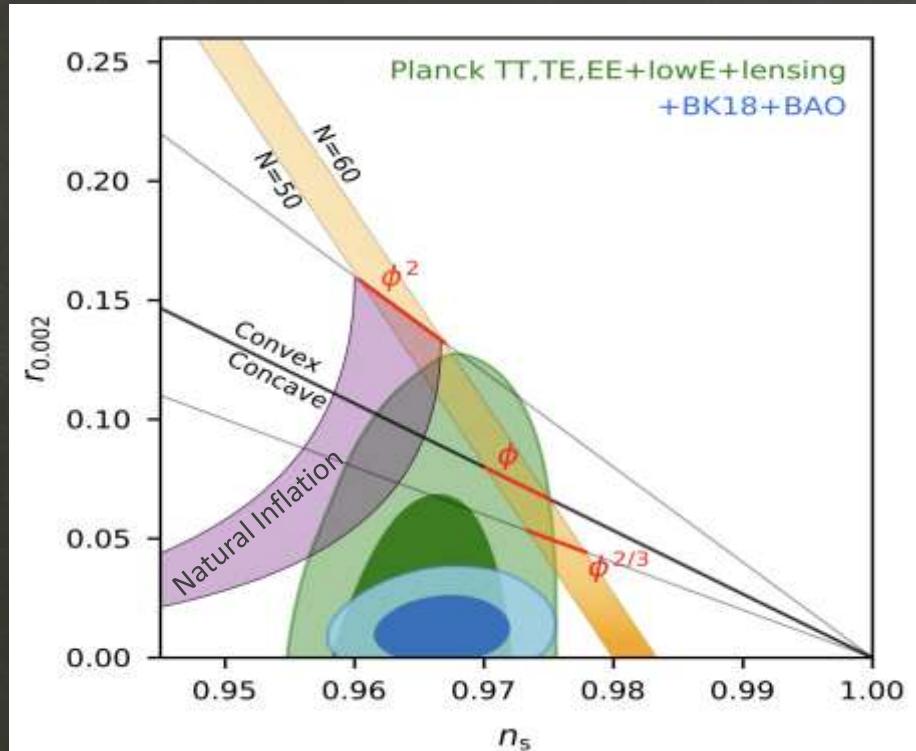
Tensor Perturbations

Nature generously gave us yet another observable: Primordial GWs



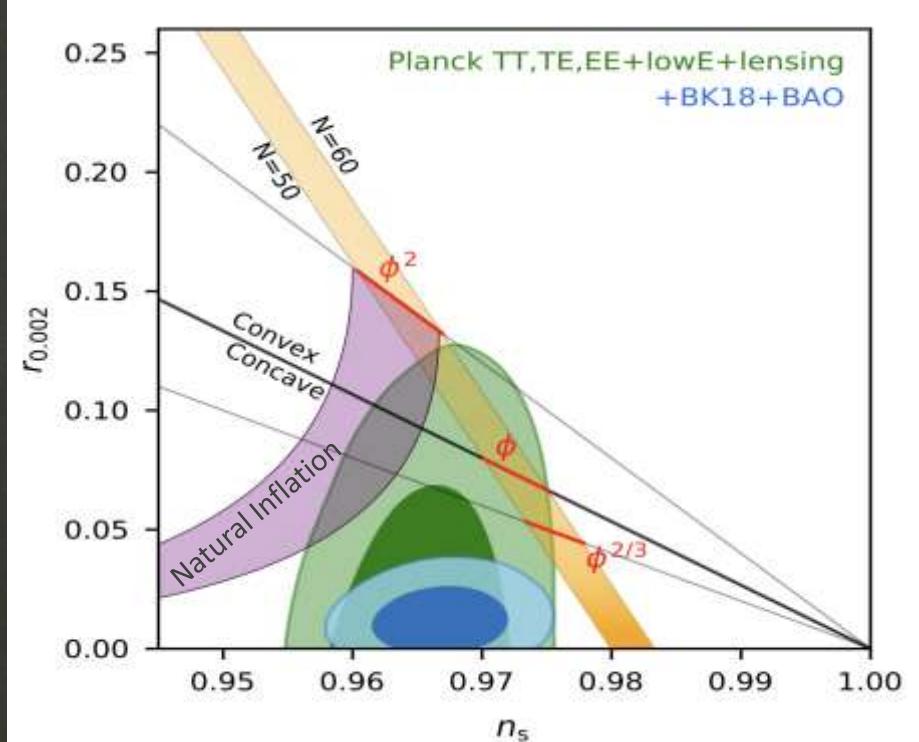
n_s - r plane

$r_{0.05} < 0.036$ (95% CL)
 $n_s = 0.9649 \pm 0.0042$ (95% CL)



n_s - r plane

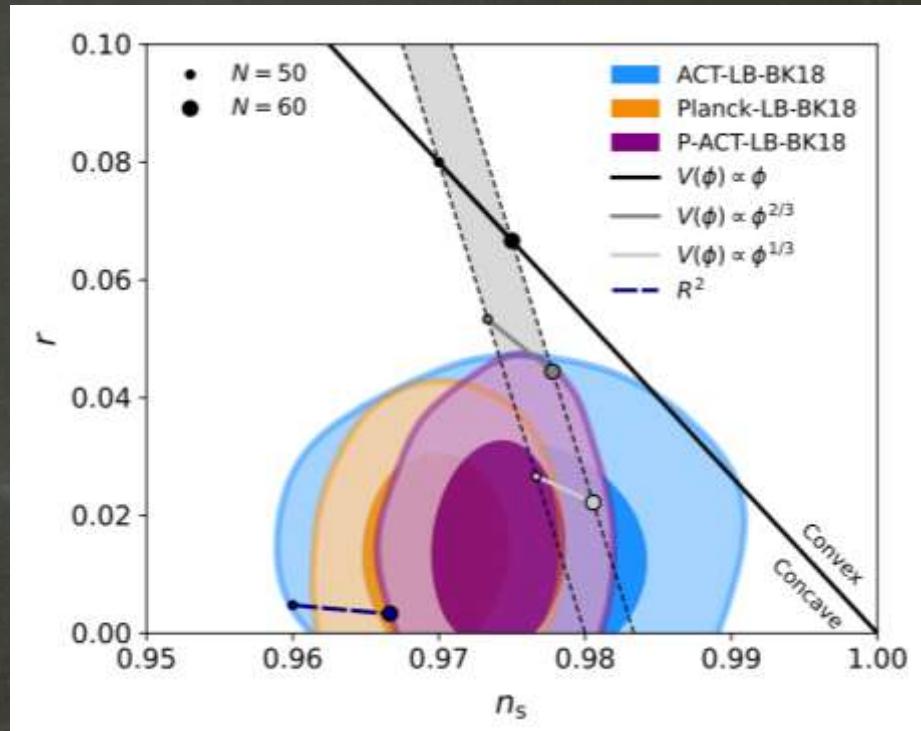
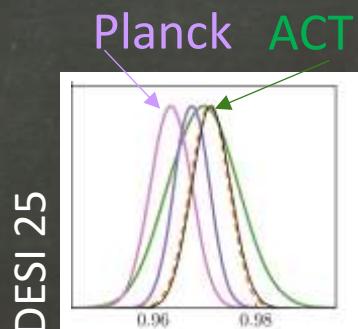
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█ Planck 2018 + lensing
█ w\ BICEP2/Keck Array (BK18) & BAO data

ACT shifted n_s !

$n_s = 0.9743 \pm 0.0034$ (95% CL)

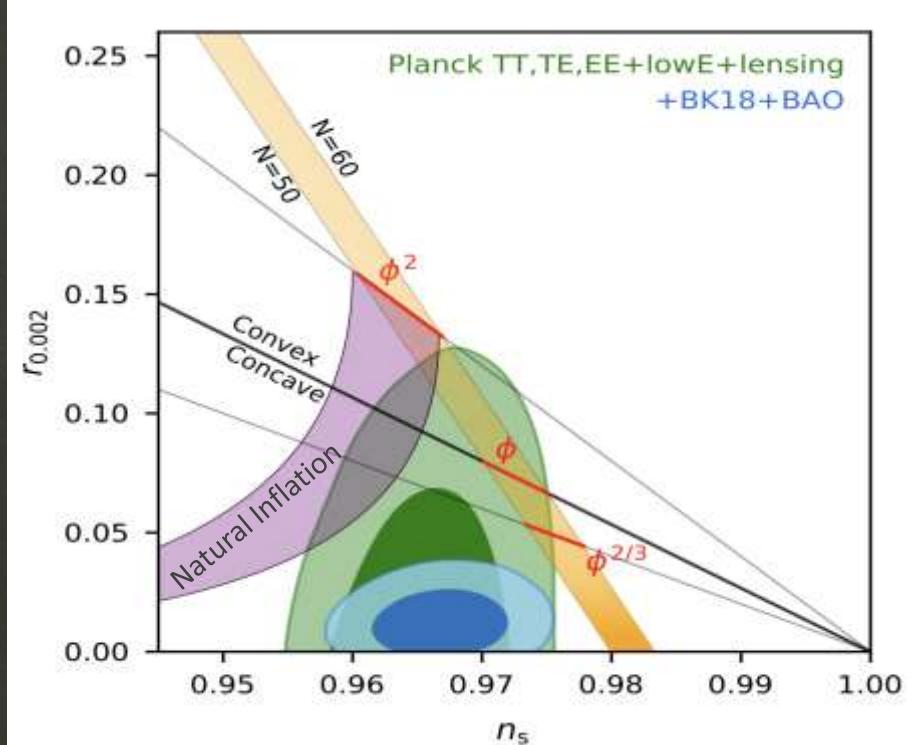


█ Planck + lensing + BK18 + BAO data
█ w/ ACT

A big goal remains! Primordial B-modes

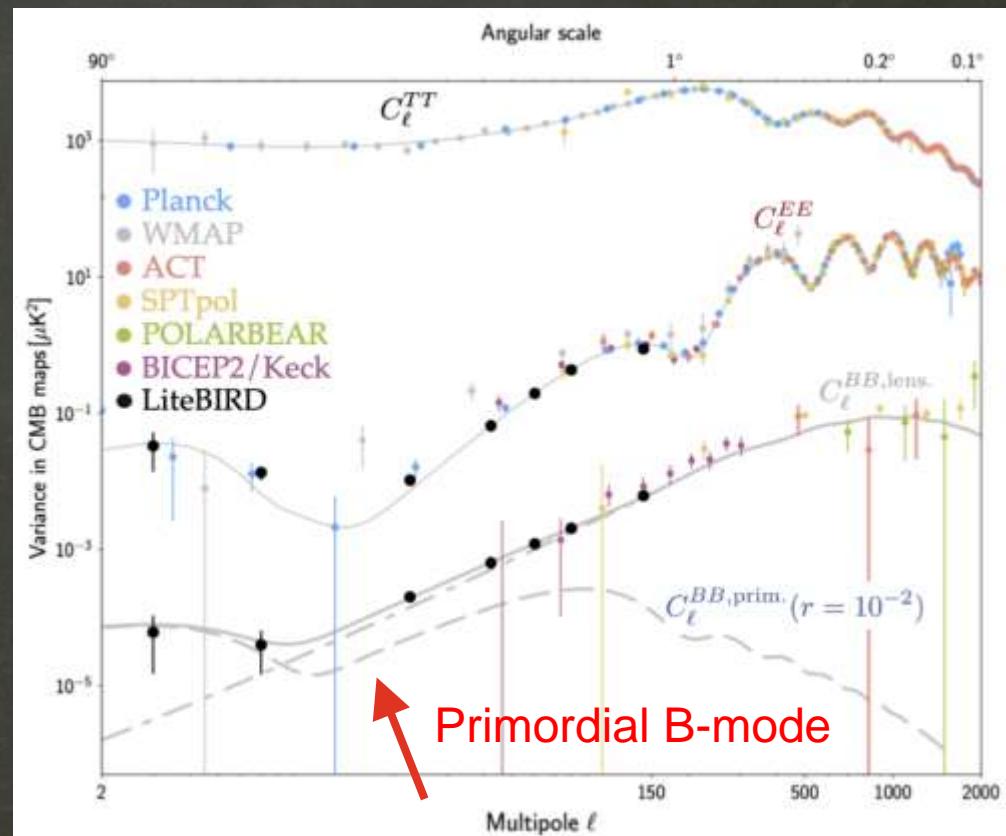
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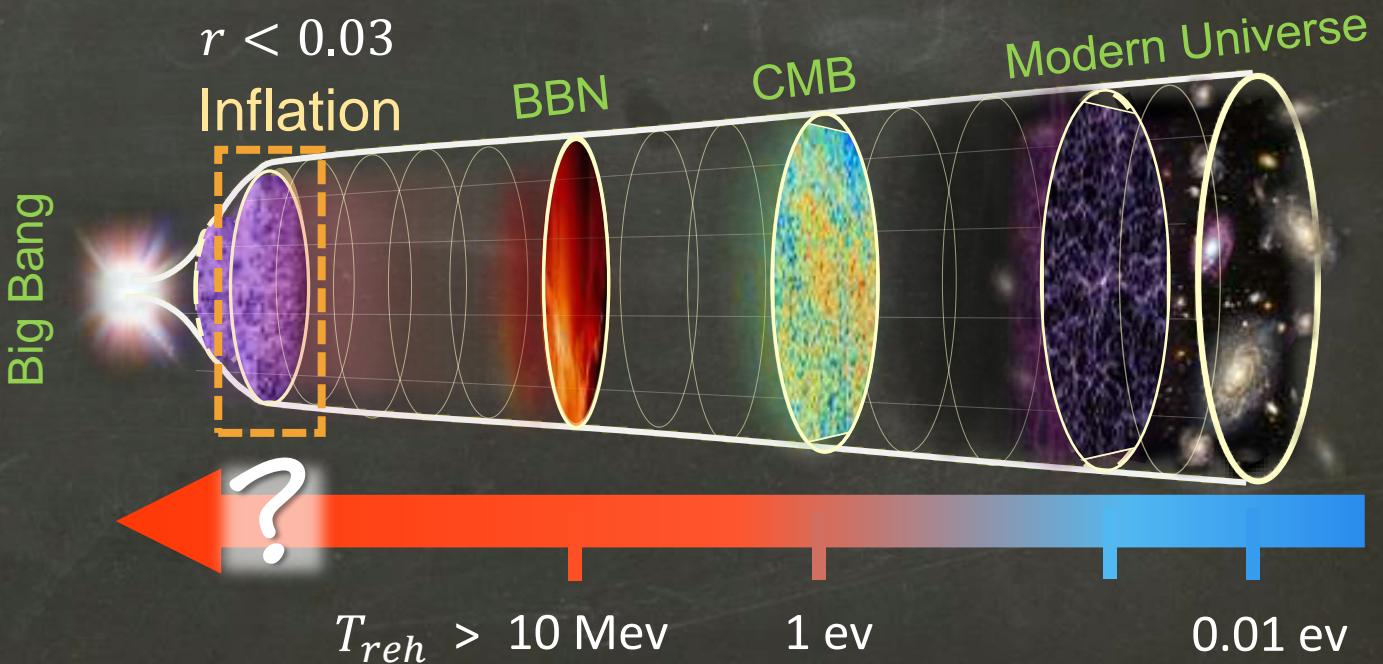
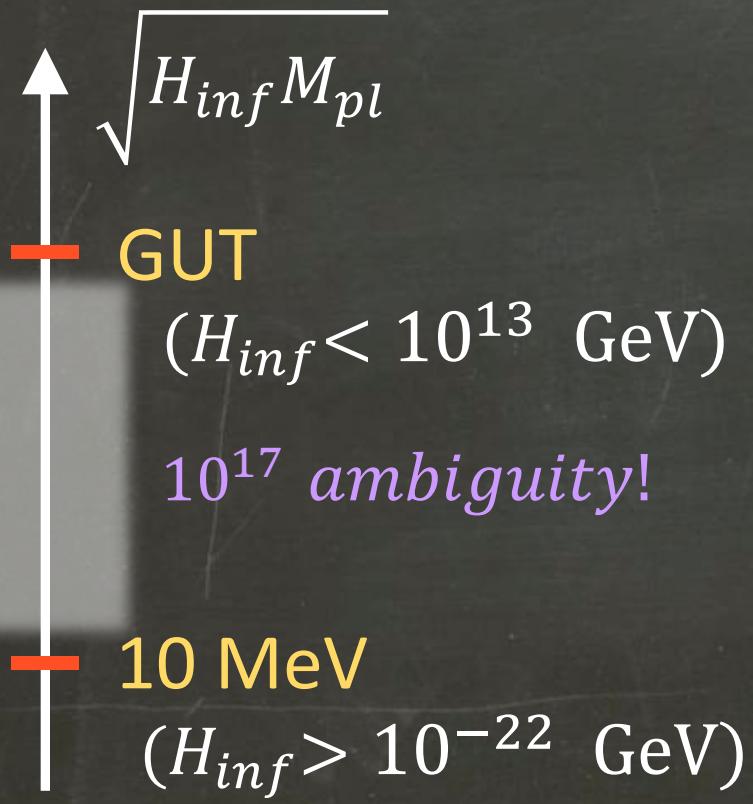
CMB-S4 & LiteBird expected to reach $r < 10^{-3}$



What is the scale of Inflation? From MeV to GUT

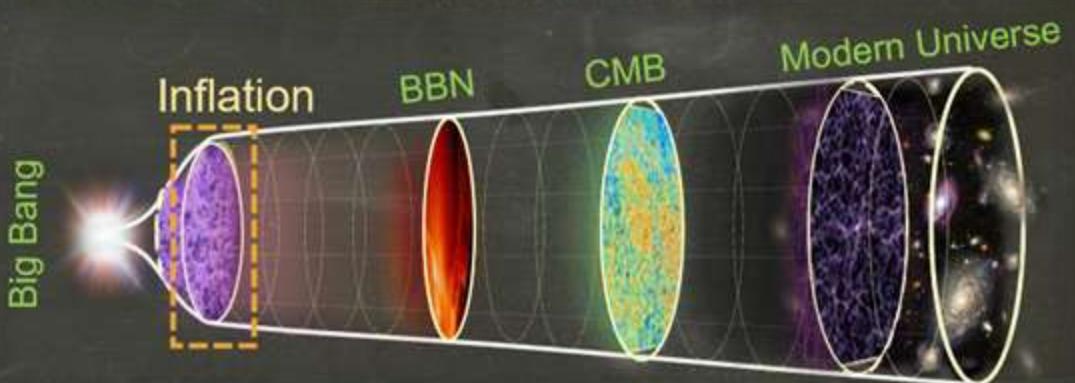
A 17-Order Window of Ignorance Still Surrounds the Inflationary Energy Scale!

Energy Scale of Inflation



As yet:

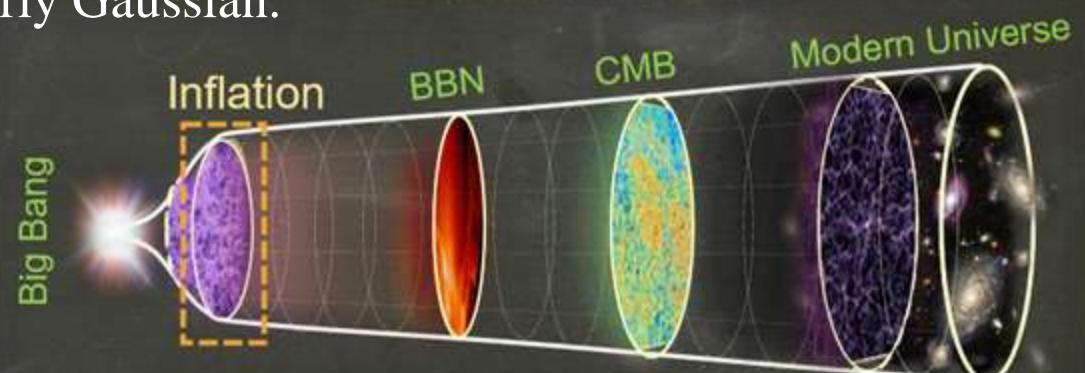
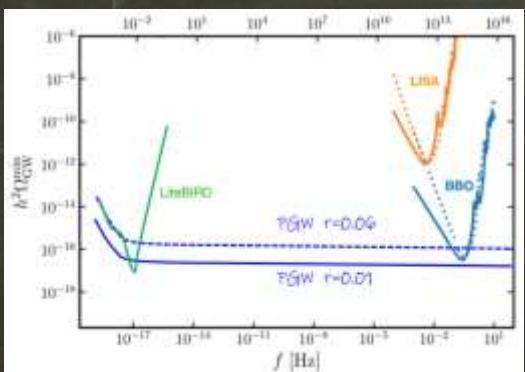
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- The Particle Physics of Inflation is still unknown.
- The Standard models of inflation are based on
a scalar field beyond the SM. (**axion** is a natural candidate)



As yet:

- Observations are in perfect agreement with Inflation.
- The Particle Physics of Inflation is still unknown.
- The Standard models of inflation are based on
a scalar field beyond the SM. (**axion** is a natural candidate)
- Parity is a symmetry in inflation
- Primordial Gravitational Waves (PGW):

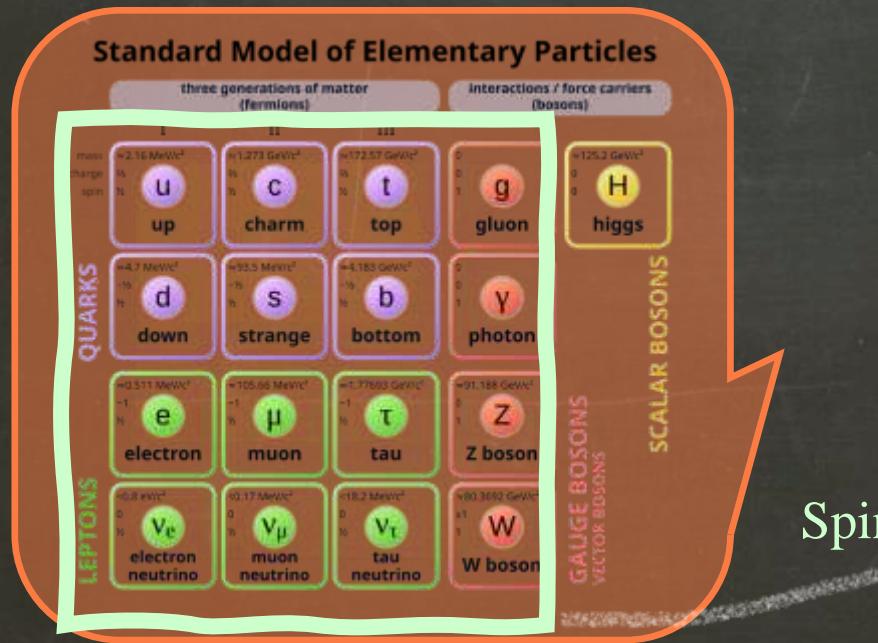
Vacuum fluctuations: unpolarized, red-tilted, and nearly Gaussian.



But wait!

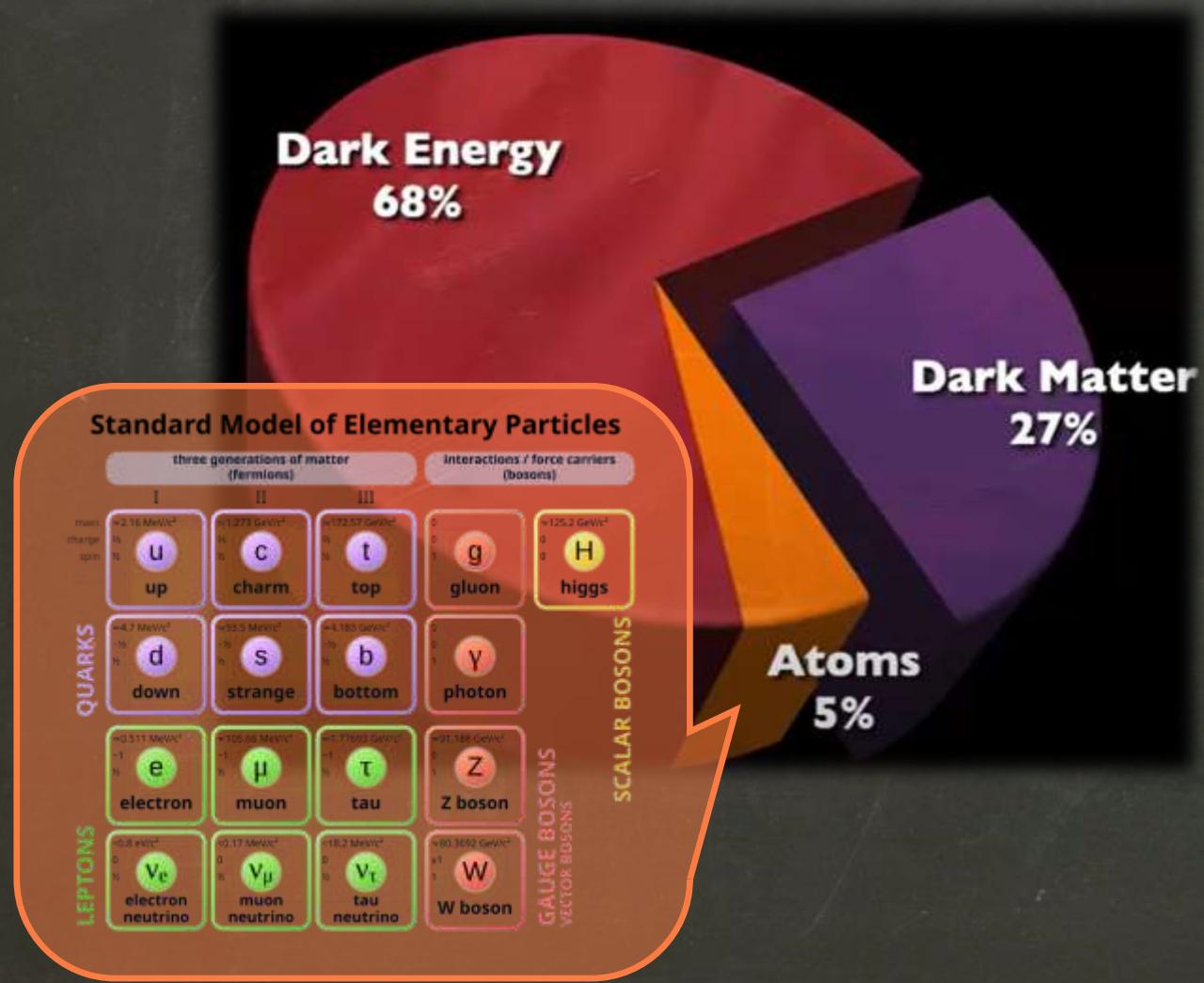
What about all other matter fields in the Universe?

Gauge fields are the carries of fundamental forces, and
Fermions are the matter fields.

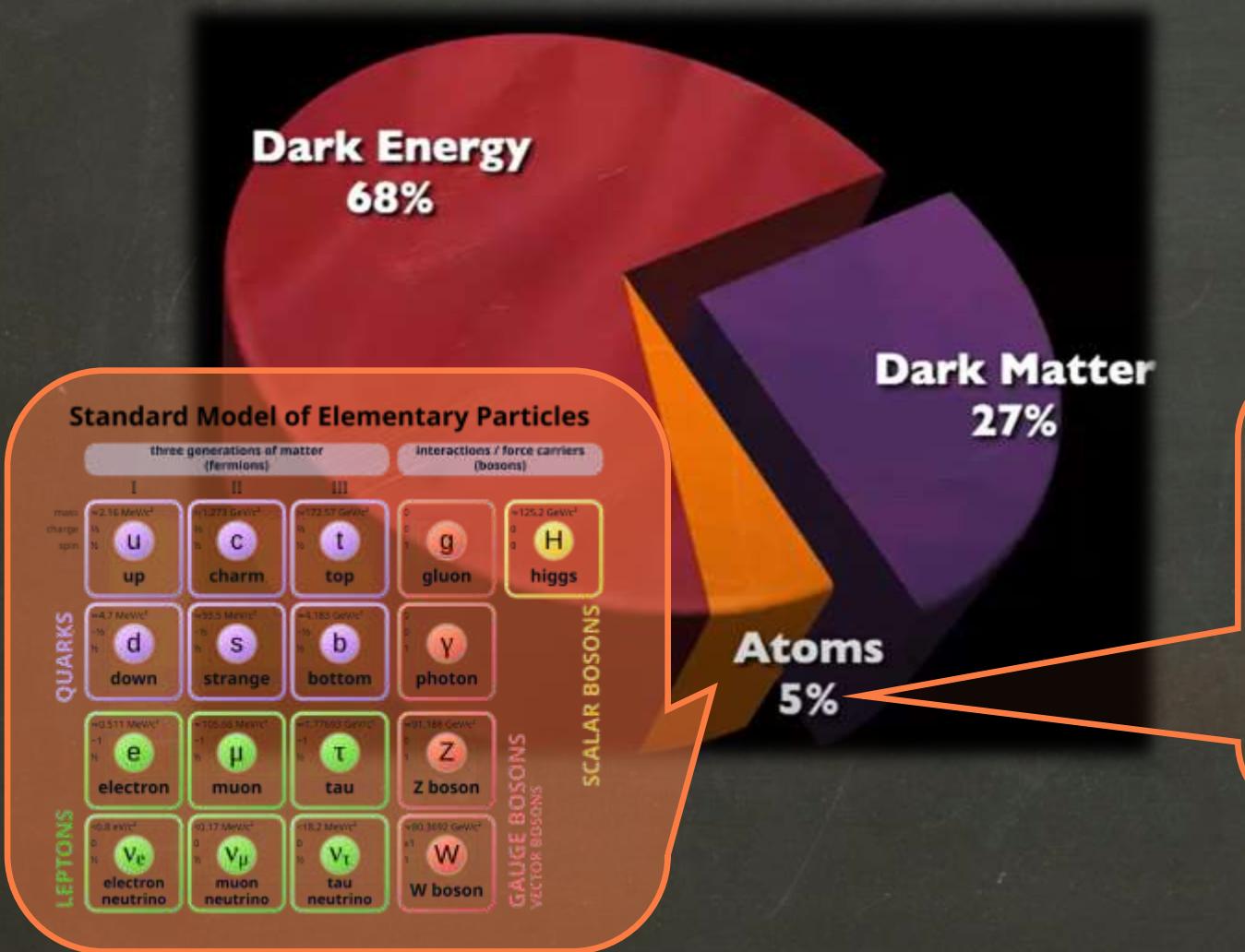


Spinning fields

The Matter content of Universee today!



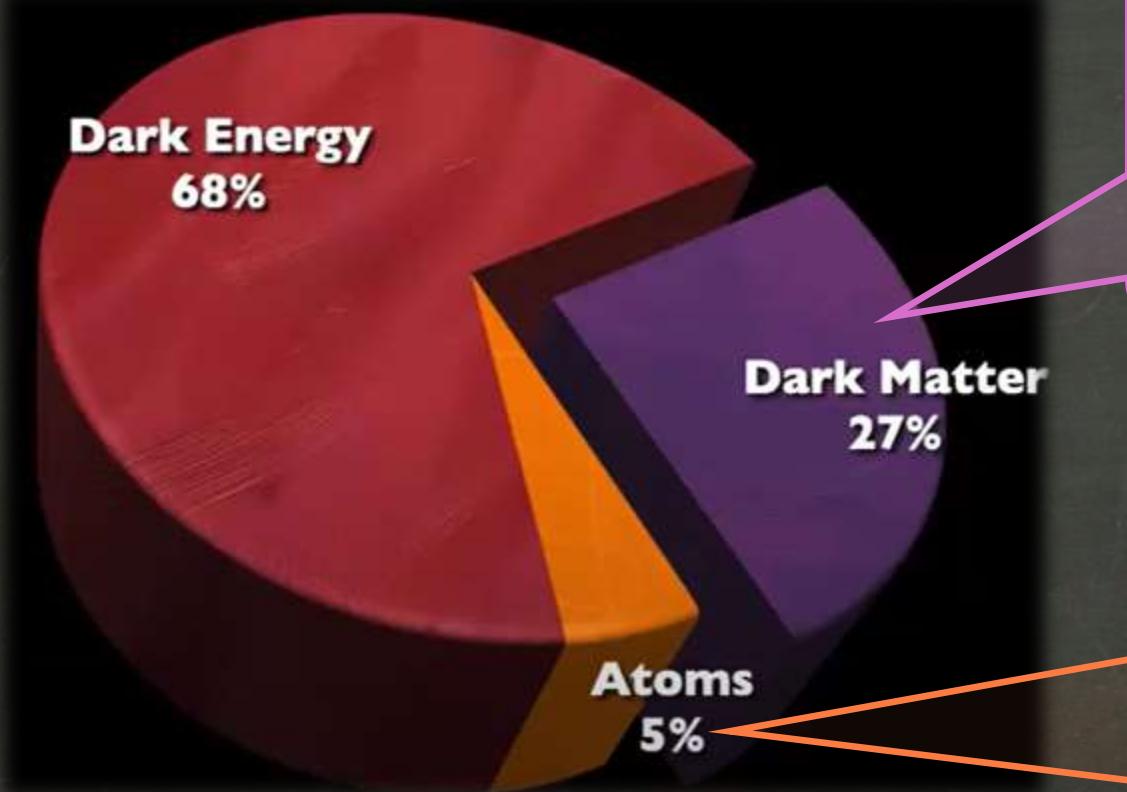
The Matter content of Universee today!



Requires
Matter - antimatter Asymmetry!

$$10^{10} + 1 \quad \bar{b} \quad b \quad 10^{10}$$

The Matter content of Universee today!



Open questions

- i) Particle Nature of DM
- ii) Its Production mechanism

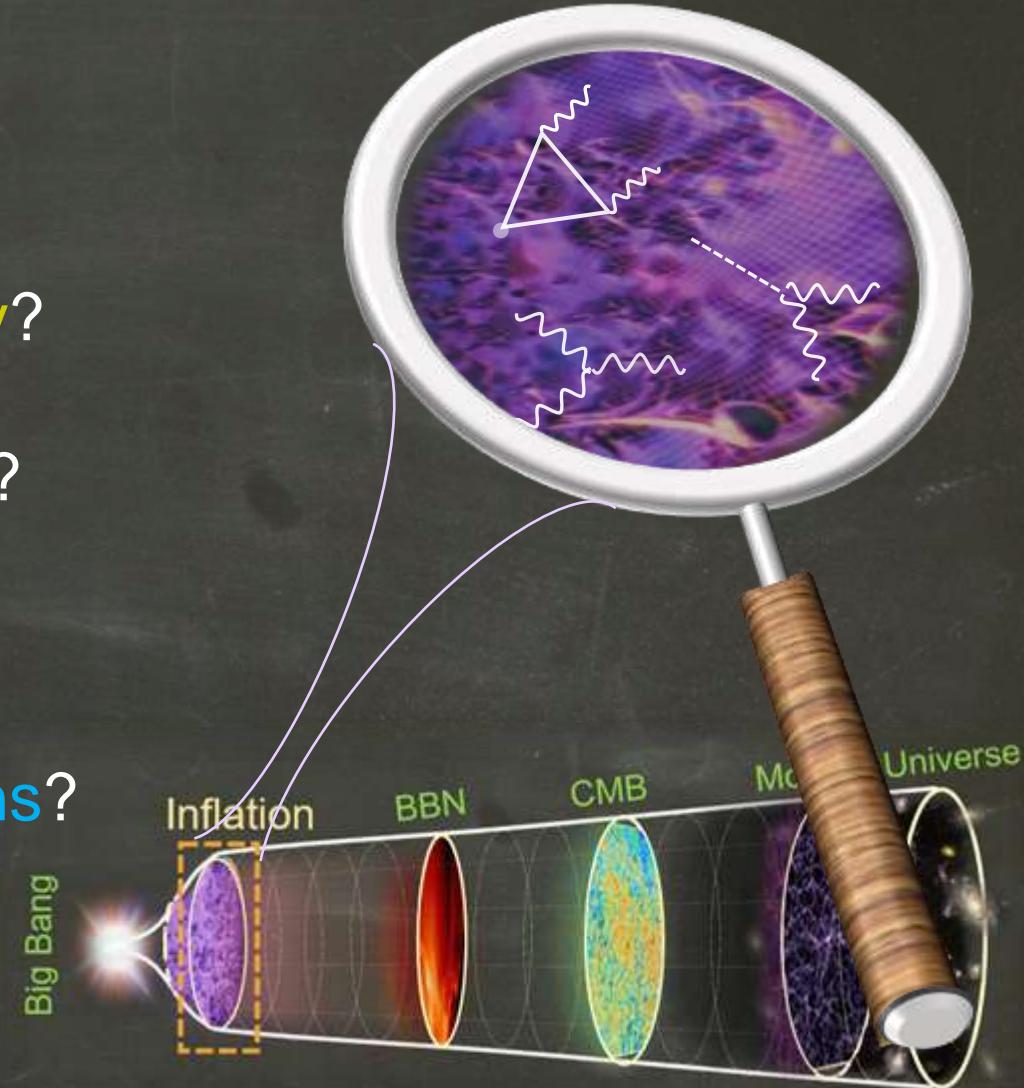
Requires

Matter - antimatter Asymmetry!



Particle Physics of Inflation?

- Gauge fields in inflation: what do they do?
- Could inflation create the matter asymmetry?
- Which model-building frameworks realize it?
- When did the Universe actually thermalize?
- How can we confront them with observations?



Axion Inflation



Toward a Particle Physics for Inflation

Setup

1- Theory and Model building

- Axion-gauge field models
- Thermalization

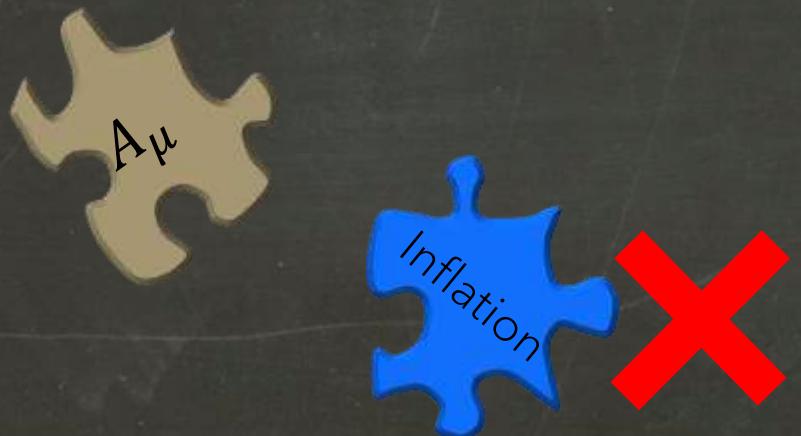
2- Phenomenology & Observation

- Gauge field & matter production
- Baryogenesis in axion inflation
- Schwinger effect
- GWs

Gauge Fields in Inflation

Gauge fields given by Yang-Mills

dilutes like radiation $A_\mu \sim 1/a$



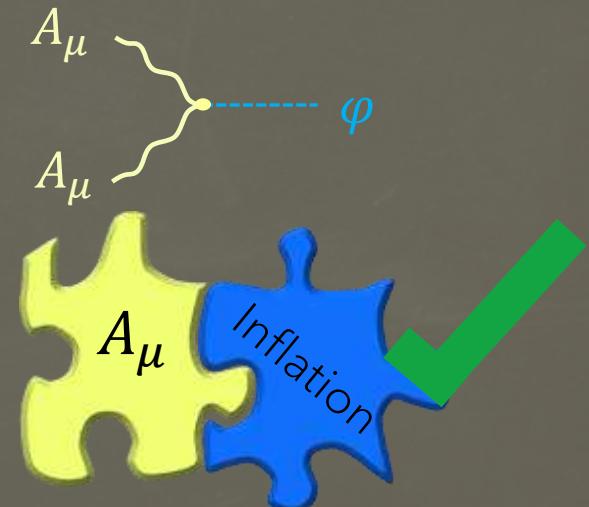
Gauge fields coupled to inflaton
are generated in inflation.

$$\frac{\lambda}{8f} F \tilde{F} \varphi$$

Axion

(Axion fields are naturally
coupled to gauge fields.)

Kaloper & Sorbo 2009



Gauge Fields in Inflation

Gauge fields given by Yang-Mills

dilutes like radiation $A_\mu \sim 1/a$

Spatial isotropy & homogeneity

U(1) vacuum A_μ

$$A_i = Q(t) \delta_i^3$$



Gauge fields coupled to inflaton
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$$\frac{\lambda}{8f} F \tilde{F} \varphi \cancel{\text{L}} \quad \text{Axion}$$

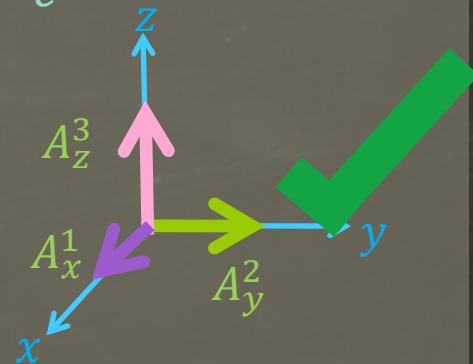
(Axion fields are naturally
coupled to gauge fields.)

so(3) & su(2) are isomorphic

SU(2) vacuum $A_\mu = A_\mu^a T_a$
 $[T_a, T_b] = i \epsilon^{abc} T_c$

Spatially isotropic

$$A_i^a = Q(t) \delta_i^a$$

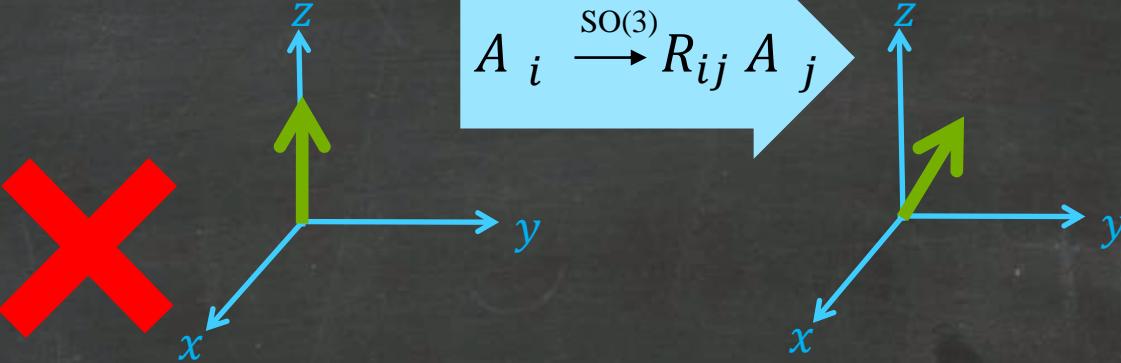


How $SU(2)$ restores isotropy?

Let us work in temporal gauge, $A_0 = 0$.

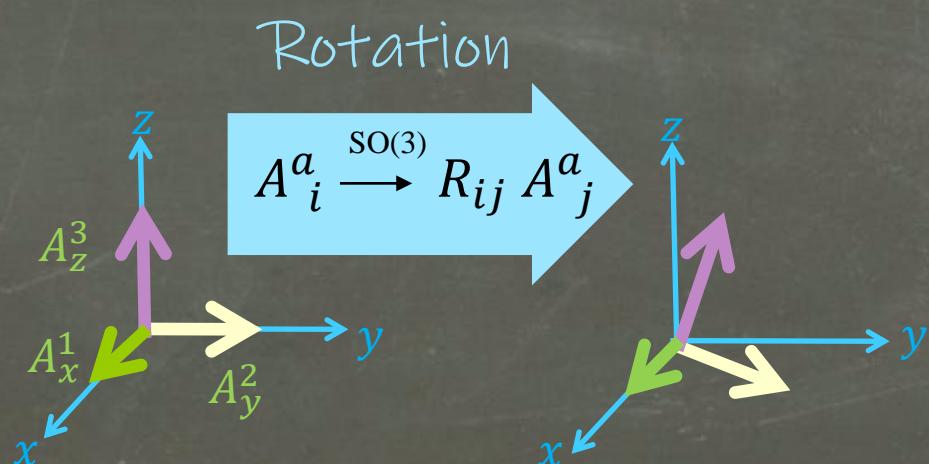
$U(1)$ vacuum A_μ

$$A_i = Q(t) \delta_i^3$$



$SU(2)$ VEV, $A_\mu = A_\mu^a T_a$

$$A_i^a = Q(t) \delta_i^a$$

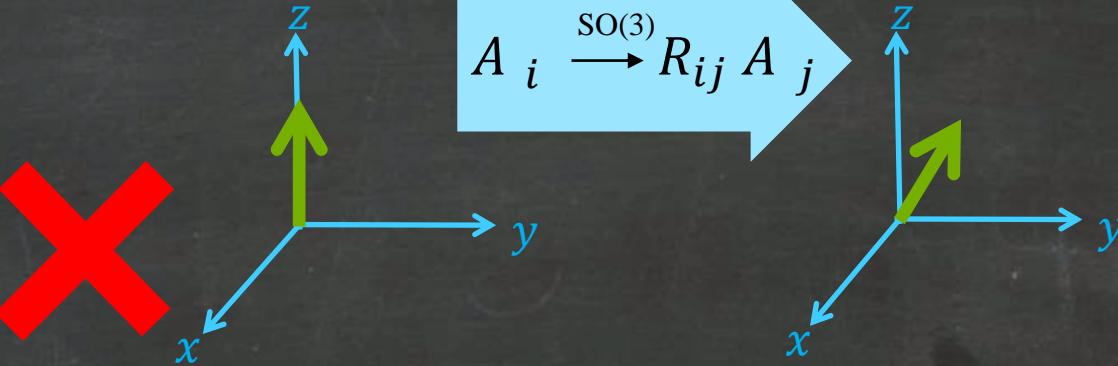


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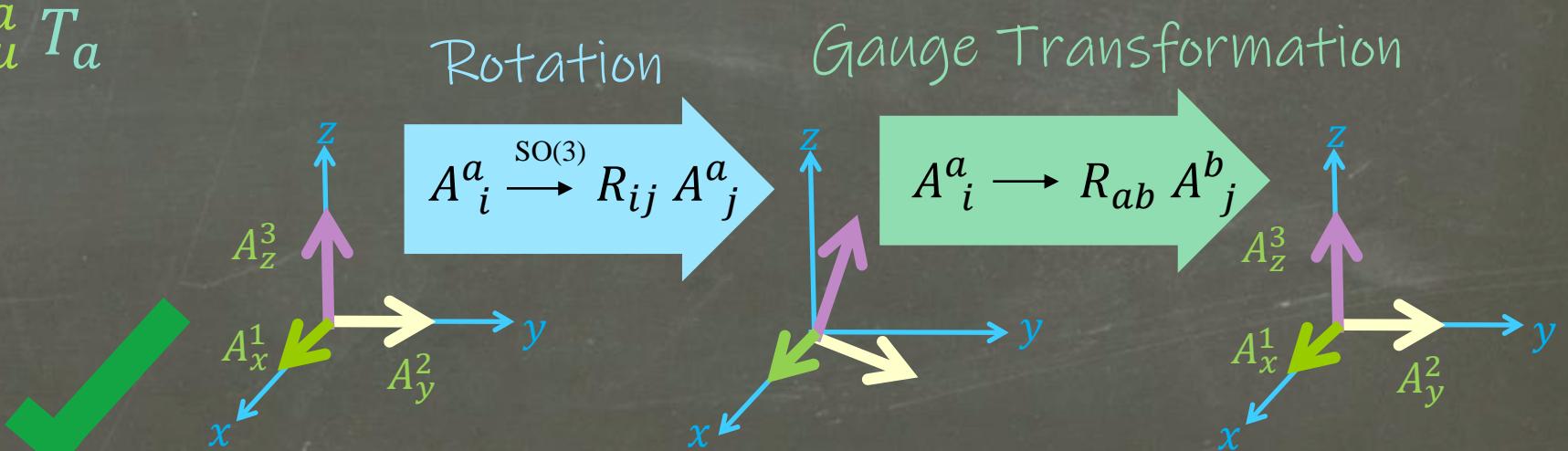
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Gauge Fields in Inflation

Given the spatial isotropy of the Universe

Gauge fields in inflation must satisfy:

	Abelian	Non-Abelian
Background	$A_i = 0$	$A_{\textcolor{brown}{i}}^{\textcolor{teal}{a}} = Q(t) \delta_{\textcolor{brown}{i}}^a$
Fluctuations	$\langle A_\mu A_\nu \rangle \neq 0$	$\langle A_\mu^a A_\nu^a \rangle \neq 0$

SU(2)-Axion Model Building

- **Gauge-flation** A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

- **Chromo-natural** P. Adshead, M. Wyman, 2012

$$S_{Cn} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{2} \left((\partial_\mu \varphi)^2 - \mu^4 \left(1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F \tilde{F} \right)$$

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$\xi = -P$

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Natural inflation

Friction

K. Freese, J. A. Frieman and A. V. Olinto 1990

SU(2)-Axion Model Building

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Ruled-out by the data

R. Namba, E. Dimastrogiovanni, M. Peloso 2013
P. Adshead, E. Martinec, M. Wyman 2013

+ Theoretical issue:
Very large $\lambda \sim 100!$

D. Baumann & L. McAllister 2014

Inspired by them, several different models with SU(2) fields have been proposed & studied.

SU(2)-Axion Model Building

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A. M., & Sheikh-Jabbari, 2011

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- Minimal Scenario of SU(2)-axion inflation

A. M., 2016

$$S_{AM} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{2} ((\partial_\mu \varphi)^2 - V(\varphi)) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F \tilde{F} \right) \quad f < 0.1 \text{ MPl} \& \lambda < 0.1$$

Axion Monodromy or any mechanism that gives a flat potential

SU(2)-Axion Model Building

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2. P. Adshead, M. Wyman, Phys. Rev. Lett.(2012) [[arXiv:1202.2366](#)]
3. **A. M.** JHEP 07 (2016) 104 [[arXiv:1604.03327](#)]
4. C. M. Nieto and Y. Rodriguez Mod. Phys. Lett. A31 (2016) [[arXiv:1602.07197](#)]
5. E. Dimastrogiovanni, M. Fasiello, and T. Fujita JCAP 1701 (2017) [[arXiv:1608.04216](#)]
6. P. Adshead, E. Martinec, E. I. Sfakianakis, and M. Wyman JHEP 12 (2016) 137 [[arXiv:1609.04025](#)]
7. P. Adshead and E. I. Sfakianakis JHEP 08 (2017) 130 [[arXiv:1705.03024](#)]
8. R. R. Caldwell and C. Devulder Phys. Rev. D97 (2018) [[arXiv:1706.03765](#)]
9. E. McDonough, S. Alexander, JCAP11 (2018) 030 [[arXiv:1806.05684](#)]
10. L. Mirzagholi, E. Komatsu, K. D. Lozanov, and Y. Watanabe, [[arXiv:2003.04350](#)]
11. Y. Watanabe, E. Komatsu, [[arXiv:2004.04350](#)]
12. J. Holland, I. Zavala, G. Tasinato, [[arXiv:2009.00653](#)]
13. **A. M.** **SU(2)R –axion inflation** [[arXiv:2012.11516](#)]
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SU(2)-Axion Model Building

Chromo-Natural Inflation

Natural Inflation+ SU(2)

Minimal Axion-SU(2)

MA 2016

Axion inflation with flat potential+ SU(2)

Spectator Chromo-natural

Inflation + Axion-SU(2) with Cos potential

Dimastrogiovanni, Fasiello, Fujita, 2016

Higgsed Chromo-natural

Chromo-natural + Higgs

Adshead, Martinec, Sfakianakis, Wyman 2016

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SU(2)-Axion inflation has a very rich phenomenology:

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- All Sakharov conditions are satisfied in inflation: a new baryogenesis mechanism
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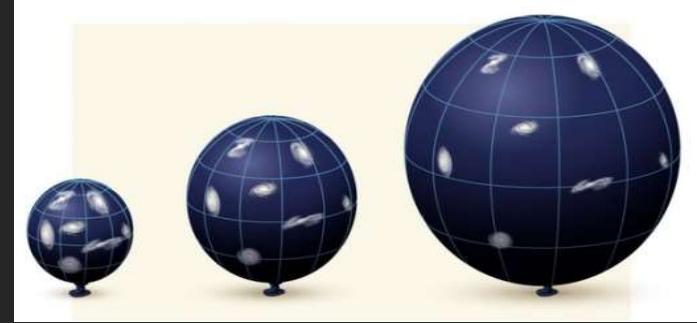
Brandenburg, Iarygina, Sfakianakis, Sharma 2024

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SU(2) Gauge fields and Initial Anisotropies

- SU(2) gauge fields are **FRW friendly**: (respect isotropy & homogeneity)

$$A_\mu^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_i^a & \mu = i \end{cases}$$



- How stable is the isotropic ansatz against initial anisotropies, i.e. Bianchi

$$A_\mu^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_j^a e^{\lambda_{ij}(t)} & \mu = i \end{cases}$$

Anisotropies in gauge field $\text{Tr}[\lambda_{ij}(t)] = 0$

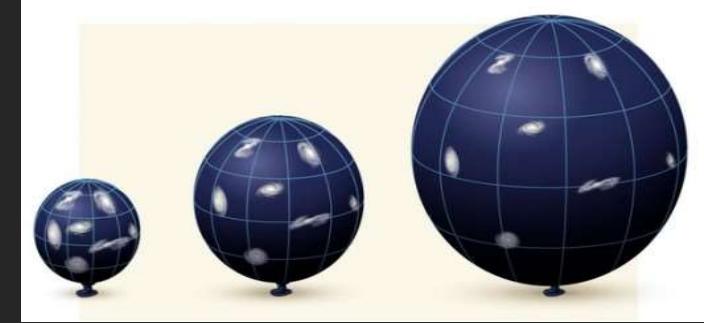


Isotropic Background
Anisotropic Background

SU(2) Gauge fields and Initial Anisotropies

- SU(2) gauge fields are **FRW friendly**: (respect isotropy & homogeneity)

$$A_\mu^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_i^a & \mu = i \end{cases}$$



- How stable is the isotropic ansatz against initial anisotropies, i.e. Bianchi

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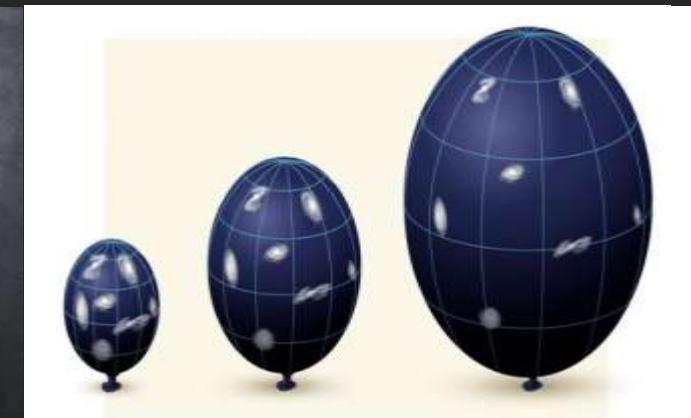
Anisotropies in gauge field $\text{Tr}[\lambda_{ij}(t)] = 0$

$$(2 + \lambda^6)\left(\frac{\lambda''}{\lambda} + 3\frac{\lambda'}{\lambda}\right) - 6\frac{\lambda'^2}{\lambda^2} + (\lambda^6 - 1)(2 + \lambda^2\gamma) \simeq 0,$$

$\lambda = \pm 1$ Is the attractor solution!

A. M. and M.M. Sheikh-Jabbari, J. Soda, 2012

A. M. and E. Erfani, 2013



Isotropic Background
Anisotropic Background

SU(2) Gauge fields and Initial Anisotropies

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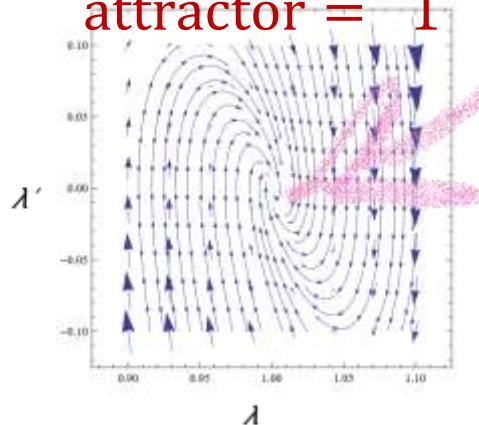


- How stable is the isotropic ansatz against **initial anisotropies**, i.e. Bianchi

I. Wolfson, A. M., T. Murata, E. Komatsu, T. Kobayashi arXiv:2105.06259

Axion is only coupled to the isotropic part of the gauge field,

attractor = 1



Anisotropic part decays like radiation and

 Isotropic Solution is the
Attractor!

A. M. and M.M. Sheikh-Jabbari, J. Soda, 2012
A. M. and E. Erfani, 2013



Isotropic
Background

Anisotropic
Background

SU(2) Gauge fields and Initial Anisotropies

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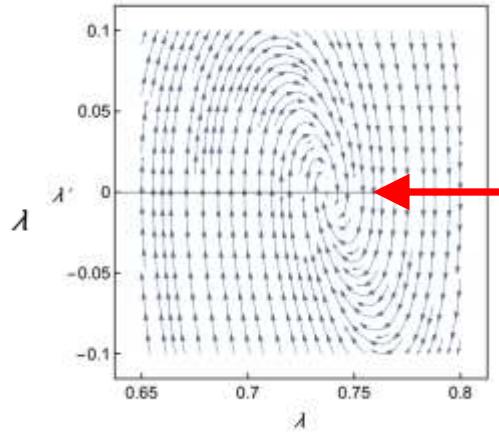
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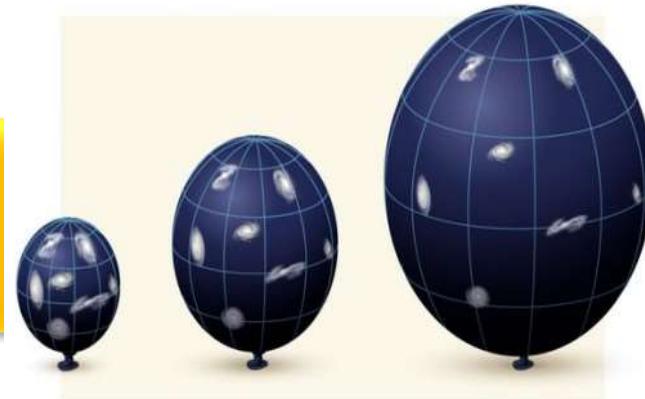
Adshead & Liu 1803.07168

Higgsed axion-SU(2) with different masses for 2 colors $M_1 \neq M_2$



attractor $\neq 1$

Anisotropic Solution is
Attractor!



Isotropic
Background

Isotropic
Background

Warm Inflation



Warm Inflation

The effective description of warm inflation Berera, 1995

$$\ddot{\phi} + (3H + \Upsilon)\dot{\phi} + V' = 0,$$

dissipation $\dot{\rho}_R + 4H\rho_R = \Upsilon\dot{\phi}^2.$

The axion inflation with $SU(N)$ gauge field backreaction

$$\ddot{\phi} + 3H\dot{\phi} + V' = -\frac{\alpha_s}{8\pi f} \langle G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \rangle.$$

$$\frac{\alpha_s}{8\pi f} \langle G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \rangle \equiv \Upsilon_{\text{sph}} \dot{\phi} = \frac{\Gamma_{\text{sph}}}{2Tf} \frac{\dot{\phi}}{f}$$

$$\Upsilon_{\text{sph}} \simeq (\alpha_s N_c)^5 \frac{T^3}{2f^2}$$

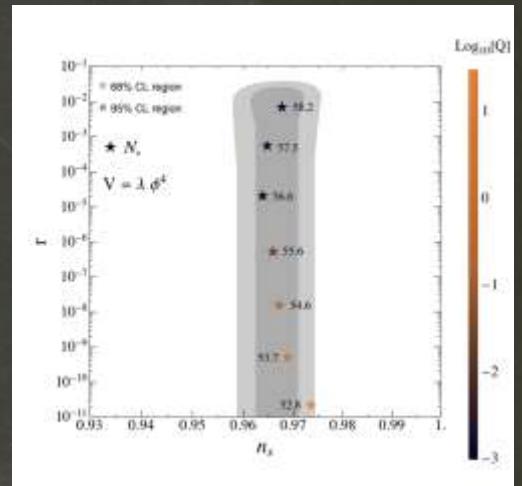
Warm Inflation

SM+axion

The effective description of warm inflation Berera, 1995

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dissipation $\dot{\rho}_R + 4H\rho_R = \Upsilon\dot{\phi}^2.$



Berghaus , Drewes , & Zell 25

The axion inflation with SU(N) gauge field backreaction

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$$\Upsilon_{\text{sph}} \simeq (\alpha_s N_c)^5 \frac{T^3}{2f^2}$$

Berghaus, Graham & Kaplan 2020

Sphaleron rate

2- Phenomenology & Observation



Quantum Vacuum $\hbar \neq 0$

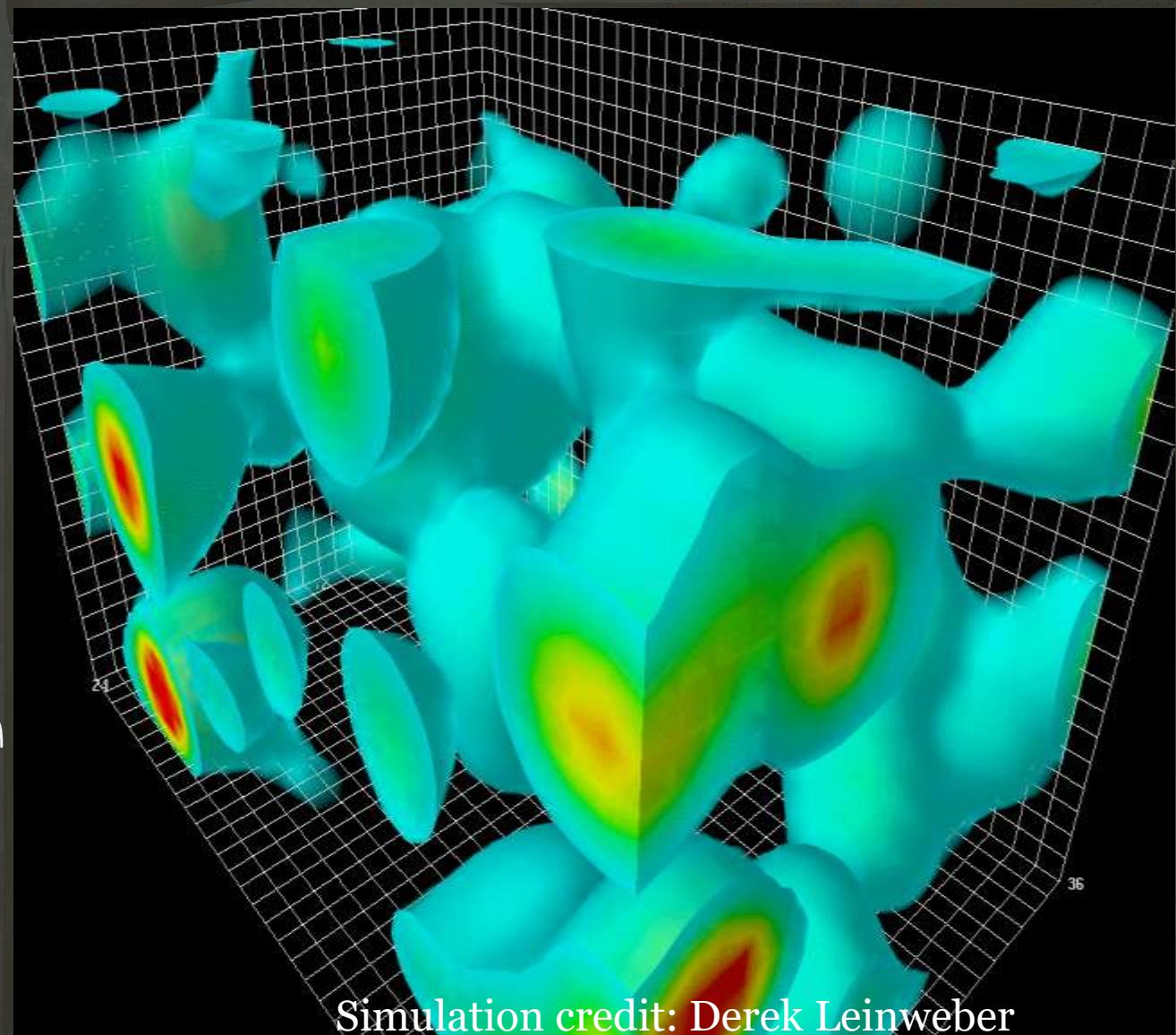
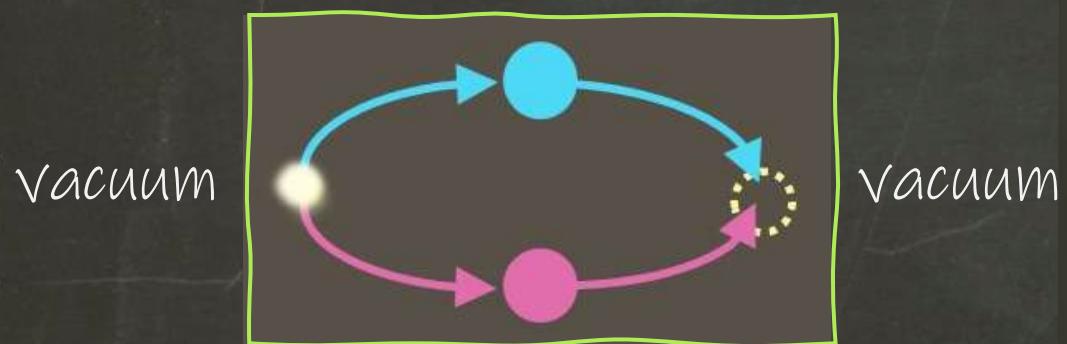
Due to Uncertainty Principle

$$\Delta x \Delta p \geq \hbar/2$$

quantum vacuum is NOT nothing!

But, a vast ocean made of

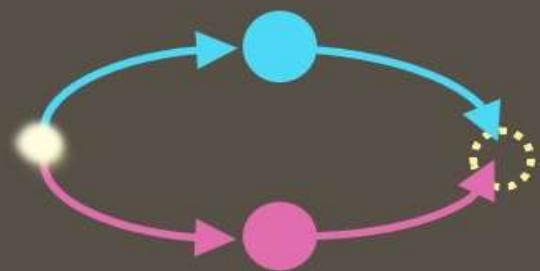
Virtual particles



Simulation credit: Derek Leinweber

Quantum Vacuum

Virtual particles

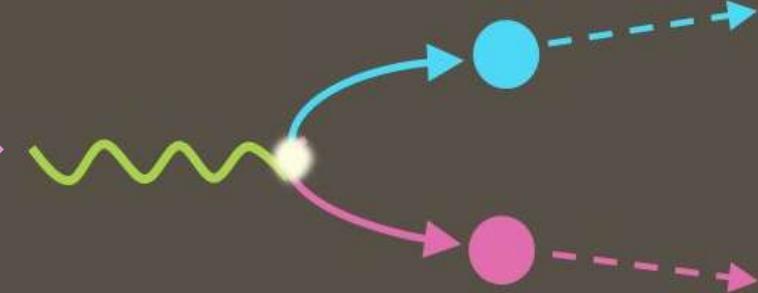


background field

Background field can upgrade them into actual particles!

Particle Production

Actual particles

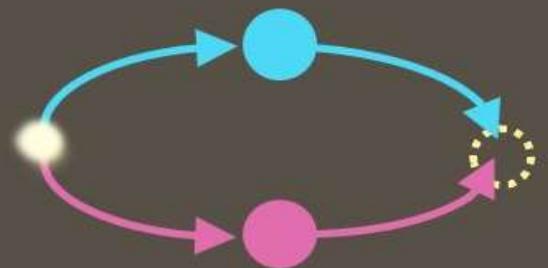


$$\langle J \rangle = 0$$

$$\langle J \rangle \neq 0$$

Quantum Vacuum

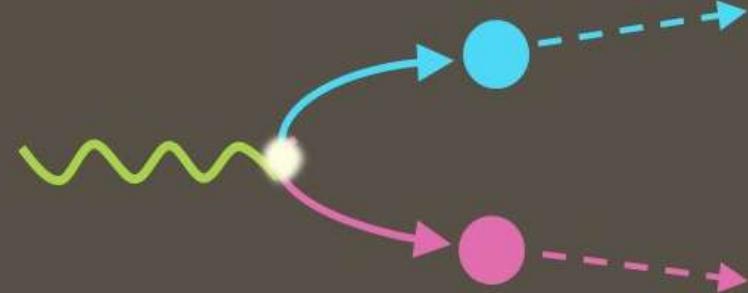
Virtual particles



background field

Particle Production

Actual particles



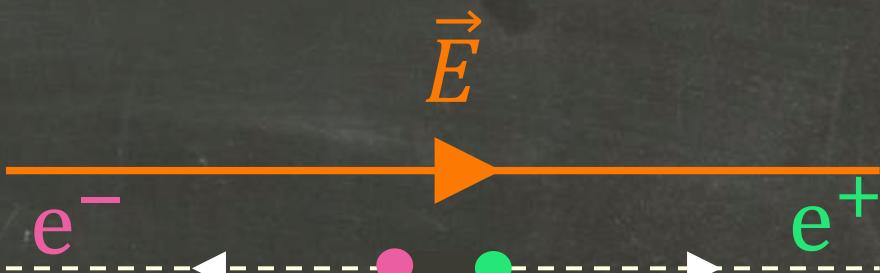
Background field can upgrade them into actual particles!

Examples of such BG fields:

1) Electric Field *Schwinger effect*

Work of the Lorentz force
over Compton wavelength

$$eE \lambda_{\text{comp}} = mc^2$$



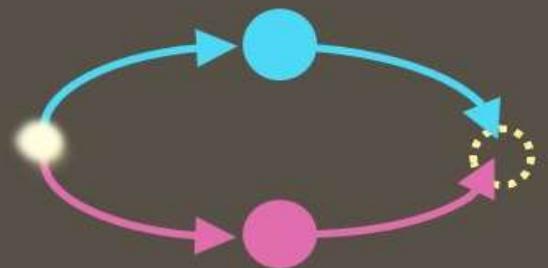
Rest energy of charged particle



J. Schwinger (1951)

Quantum Vacuum

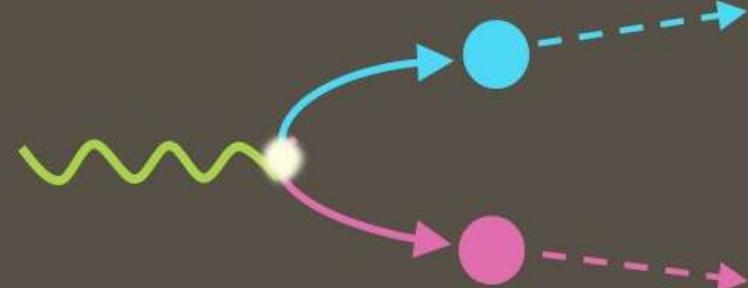
Virtual particles



background field

Particle Production

Actual particles



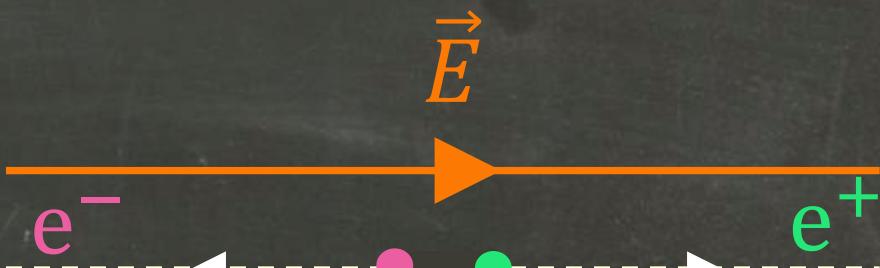
Background field can upgrade them into actual particles!

Examples of such BG fields:

1) Electric Field *Schwinger effect*

Work of the Lorentz force
over Compton wavelength

$$eE \lambda_{\text{comp}} = mc^2$$



The Electric field that can create electron pairs

$$E = \frac{m_e^2 c^3}{e\hbar} = 10^{18} \text{ V/m}$$

Rest energy of charged particle



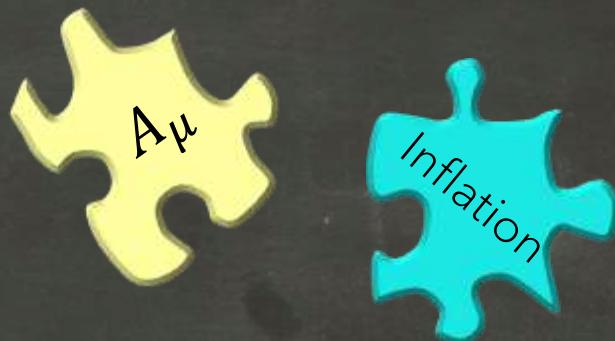
J. Schwinger (1951)

What about Schwinger Effect in Early Universe?

Schwinger effect in **scalar QED** in 4d de Sitter

- T. Kobayashi, N. Afshordi 2014

It requires assuming an ad hoc **constant Electric Field**



What about Schwinger Effect in Early Universe?

Schwinger effect in **scalar QED** in 4d de Sitter

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It requires assuming an ad hoc **constant Electric Field**



How about **Axion-inflation** (quasi-de Sitter)?!

- i) a natural candidate for the inflaton field
- ii) Naturally coupled to gauge fields

It naturally generates a **constant Electric Field**



What about Schwinger Effect in Early Universe?

Schwinger effect in **scalar QED** in 4d de Sitter

- T. Kobayashi, N. Afshordi 2014

Schwinger effect in **axion-inflation**



K. Lozanov

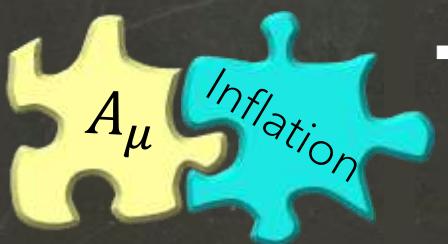


E. Komatsu

- K. Lozanov, **A. M.**, E. Komatsu 2018
- **A. M.**, E. Komatsu 2019
- V. Domcke, Y. Ema, K. Mukaida, R. Sato 2019
- L. Mirzagholi, **A. M.**, K. Lozanov 2019
-

How about **Axion-inflation**!?

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What about Schwinger Effect in Early Universe?

Schwinger effect in **scalar QED** in 4d de Sitter

- T. Kobayashi, N. Afshordi 2014

Schwinger effect in **axion-inflation**



K. Lozanov



E. Komatsu

- K. Lozanov, A. M., E. Komatsu 2018

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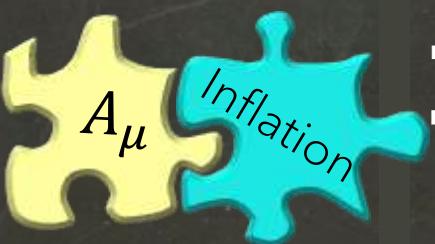
-

- E. Komatsu 2022 **nature reviews physics**

New physics from the polarized light of the cosmic microwave background

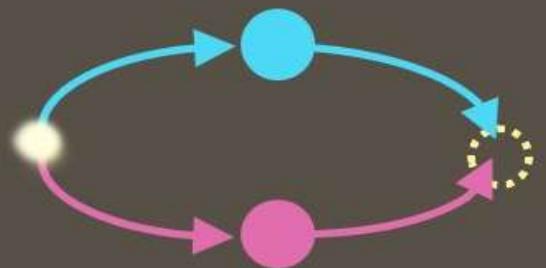
How about **Axion-inflation**!?

- i) a natural candidate for the inflaton field
- ii) Naturally coupled to gauge fields



Quantum Vacuum

Virtual particles

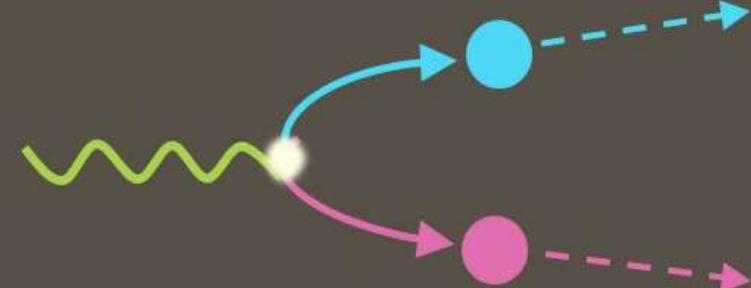


background field

Background field can upgrade them into actual particles!

Particle Production

Actual particles



Examples of such BG fields:

2) Gravitational

one particle fall into the BH, while the other escapes...

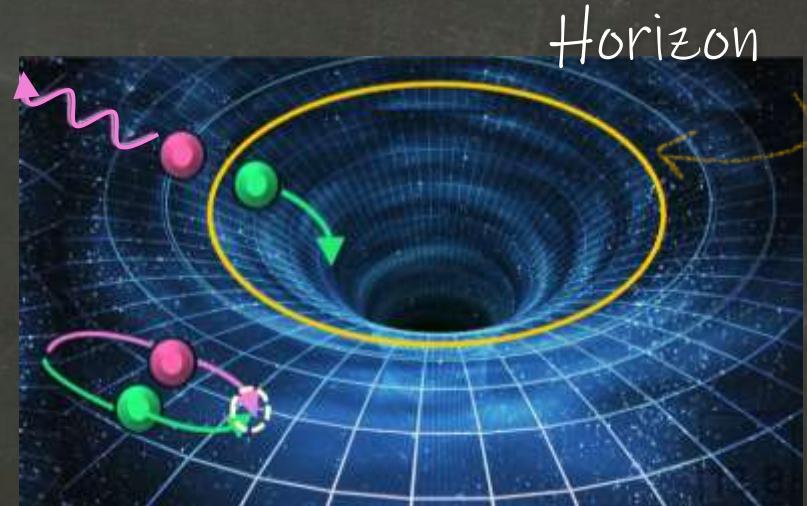


S. Hawking (1974)

Hawking radiation

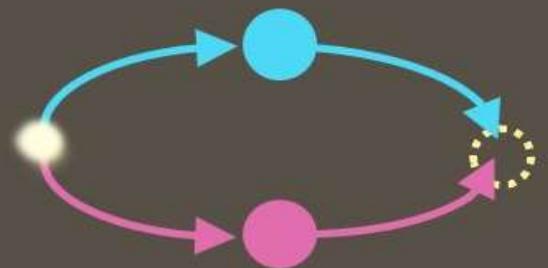
Power BH emitted is

$$P = \frac{\pi c^3 M_{pl}^4}{240} \frac{1}{M^2}$$



Quantum Vacuum

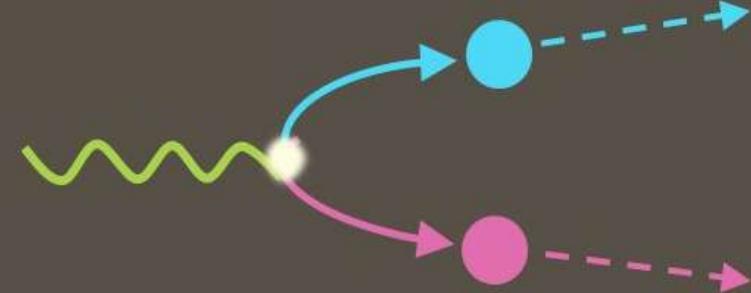
Virtual particles



background field

Particle Production

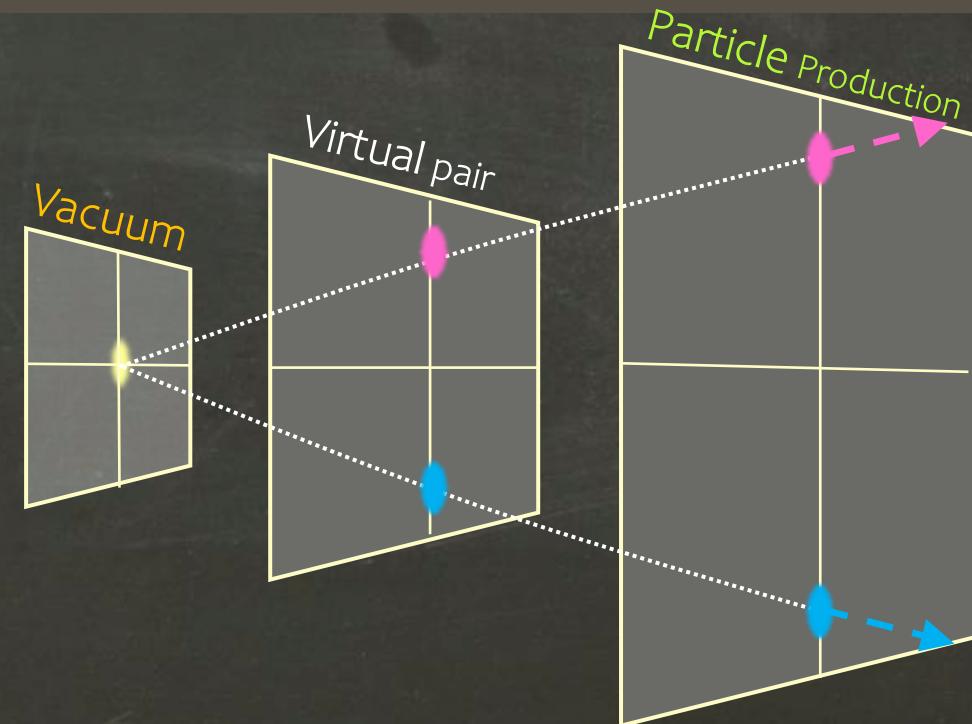
Actual particles



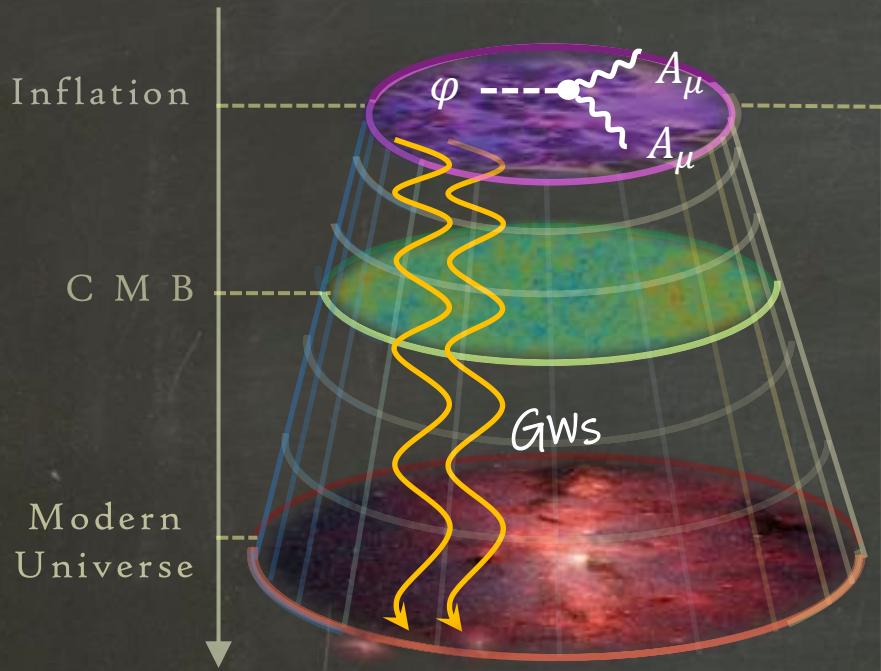
Background field can upgrade them into actual particles!

Examples of such BG fields:

- 1) Electric Field *Schwinger effect*
- 2) Gravitational
- i) Hawking radiation
- ii) *expansion of the Universe!*

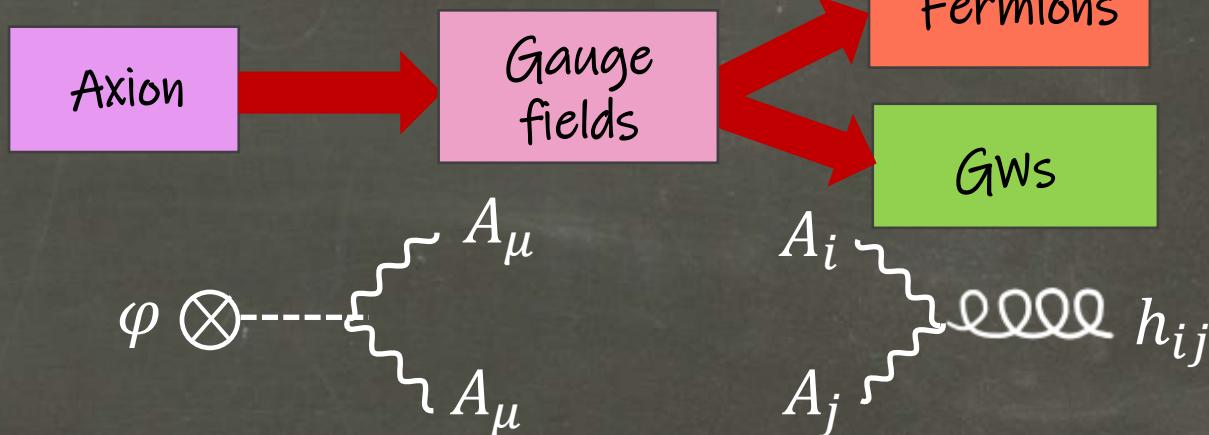


Inflation Particle Physics



Axion-inflation and gauge fields (non-Abelian)

Particle Production
In Axion-Inflation



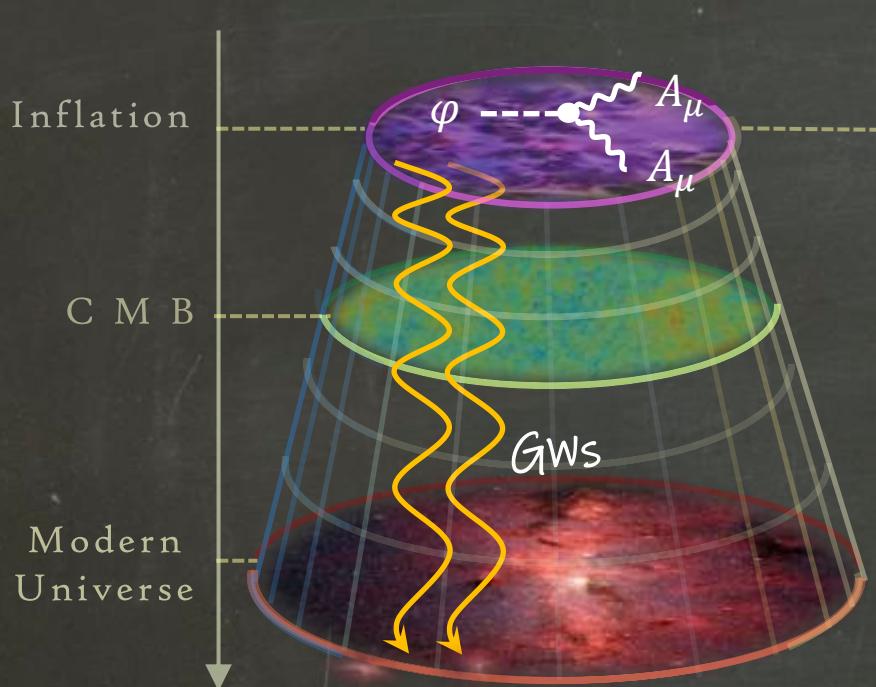
A. M., & Sheikh-Jabbari, 2011
P. Adshead, M. Wyman, 2012

A.M., 2019
Mirzagholi, A.M., Lozanov 2019

A. M. et. al, 2011 & 2013
Dimastrogiovanni et. al 2013
P. Adshead et. al, 2013

Inflation Particle Physics

A. M., & Sheikh-Jabbari, 2011
P. Adshead, M. Wyman, 2012



Vacuum Gws:
Unpolarized & Gaussian

Axion-inflation and gauge fields (non-Abelian)

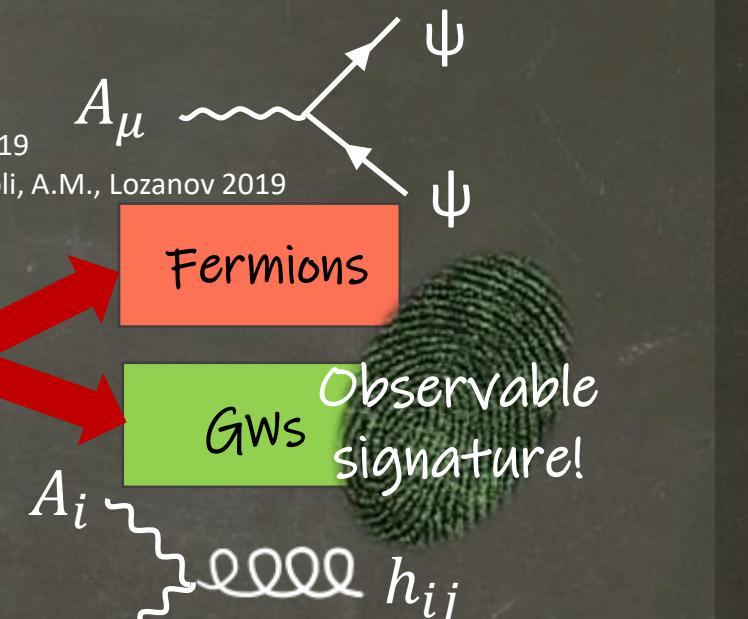
Particle Production
In Axion-Inflation



$$\varphi \otimes \begin{cases} A_\mu \\ A_\mu \\ A_\mu \end{cases}$$



A.M., 2019
Mirzagholi, A.M., Lozanov 2019



A. M. et. al, 2011 & 2013
Dimastrogiovanni et. al 2013
P. Adshead et. al, 2013



Sourced Gws:
Chiral & non-Gaussian

New Tensorial mode in $SU(2)$ Gauge Field

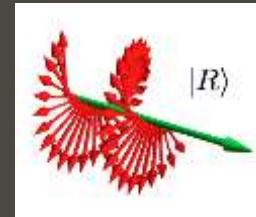
$$\bullet \delta A_i^a = (B_+ (t, k) e_{ij}^+ (\vec{k}) + B_- (t, k) e_{ij}^- (\vec{k})) \delta_j^a$$

$$B''_{\pm} + \underbrace{[k^2 \mp \delta_C k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a}]}_{\text{effective frequency}} B_{\pm} \approx 0$$

(δ_C and $\frac{m^2}{H^2}$ are given by BG)

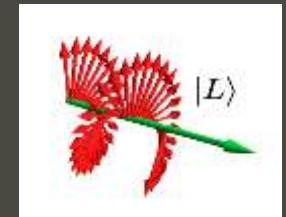
Right-handed

Circular polarizations



B_+

Left-handed



B_-

B_{\pm} is a new tensorial mode in
the perturbed $SU(2)$ gauge field!

A.M. & Sheikh-Jabbari, 2011

New Tensorial mode in $SU(2)$ Gauge Field

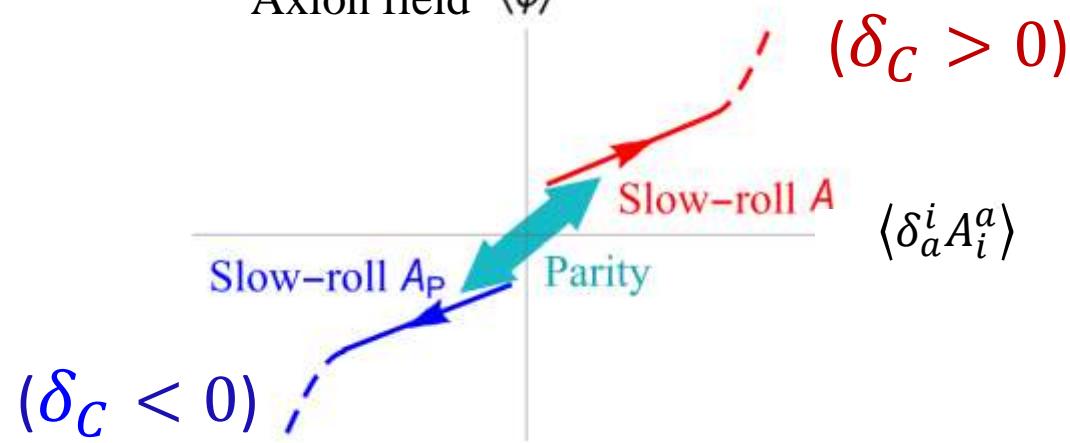
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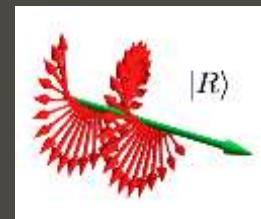
Vacuum structure

Axion field $\langle \phi \rangle$

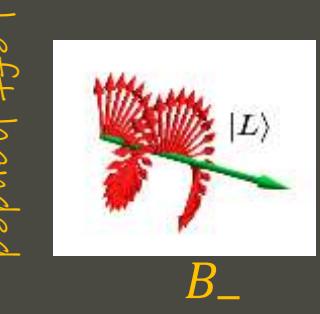


Right-handed

Circular polarizations



B_+



Left-handed

B_-

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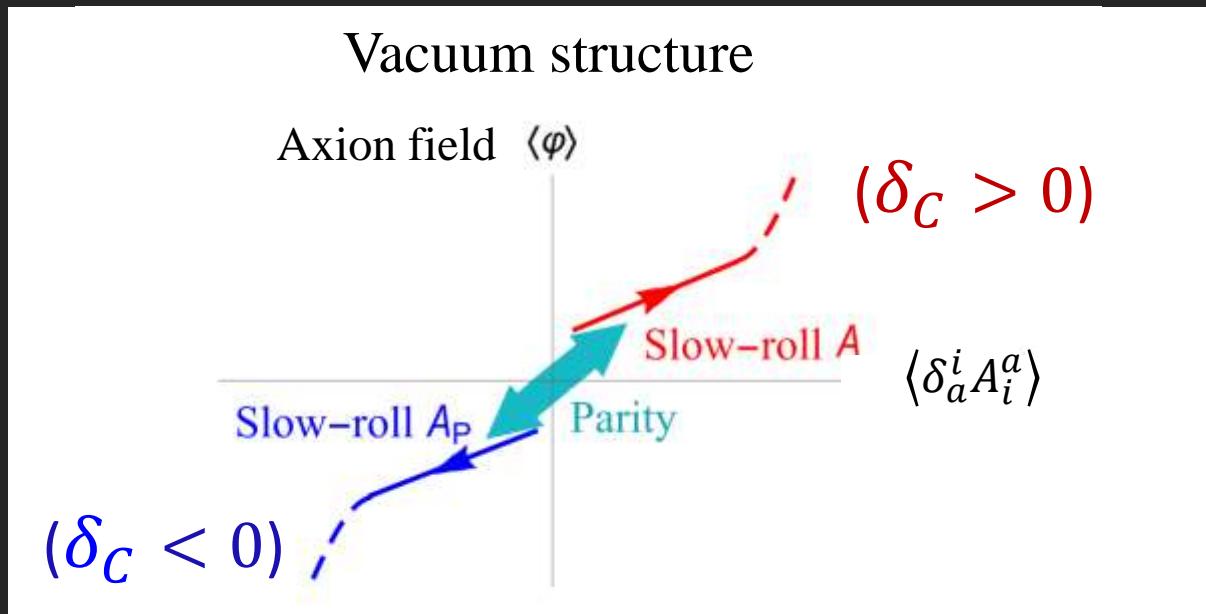
A.M. & Sheikh-Jabbari, 2011

New Tensorial mode in $SU(2)$ Gauge Field

- $\delta A_i^a = (B_+ (t, k) e_{ij}^+ (\vec{k}) + B_- (t, k) e_{ij}^- (\vec{k})) \delta_j^a$

$$B_\pm'' + \underbrace{\left[k^2 \mp \delta_C k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_\pm \approx 0$$

(δ_C and $\frac{m^2}{H^2}$ are given by BG)



For $\delta_C > 0$
Short tachyonic growth of B_+

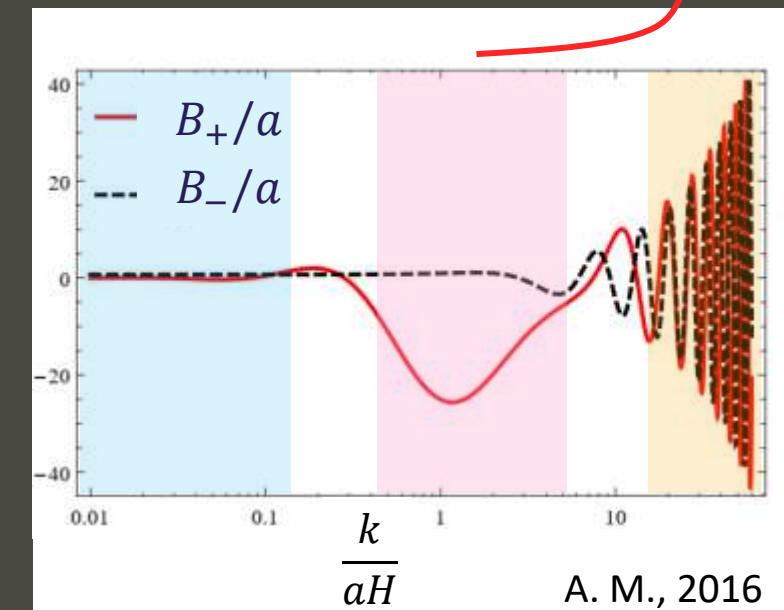


$$n_B \sim \frac{H^3}{6\pi^2} \delta_C^3 e^{\frac{(2-\sqrt{2})\pi}{2}\delta_C}$$

Chiral Field

Particle Production

A. M. and E. Komatsu, 2018



Gauge Field sources Primordial GWs

- $\delta A_i^a = (B_+(t, k) e_{ij}^+(\vec{k}) + B_-(t, k) e_{ij}^-(\vec{k})) \delta_j^a$
- The field equation: $B_\pm'' + [k^2 \mp \delta_C k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a}] B_\pm \approx 0$



- That sourced the GWs

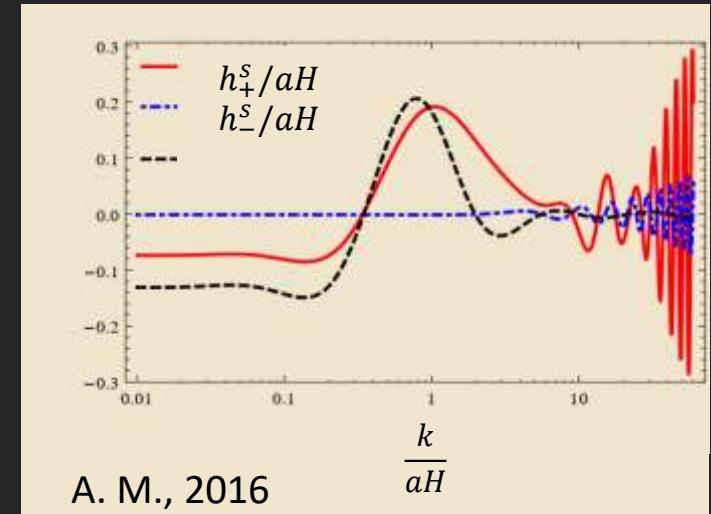
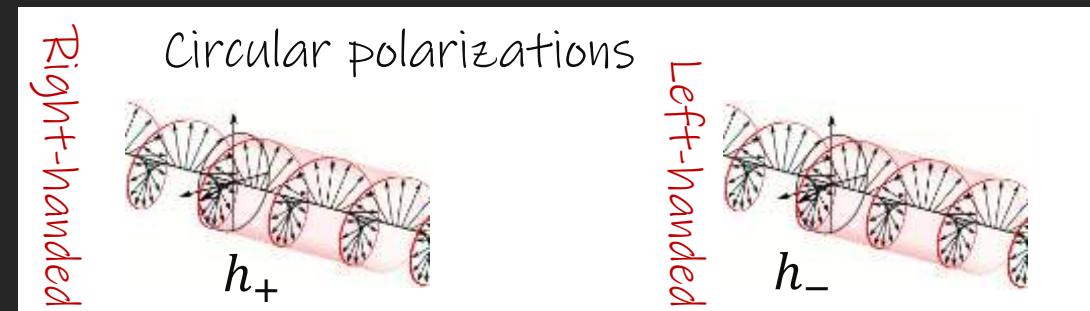
$$h_\pm'' + [k^2 - \frac{a''}{a}] h_\pm = \mathcal{H}^2 \Pi_\pm[B_\pm]$$

- Gravitational waves have two uncorrelated terms



$$h_\pm = \underbrace{h_\pm^{vac}}_{\substack{\text{Vacuum} \\ \text{GWs}}} + \underbrace{h_\pm^S}_{\substack{\text{Sourced by} \\ B_\pm}}$$

$h_+^{vac} = h_-^{vac}$ $h_+^S \neq h_-^S$



Novel Observable Signature: CMB

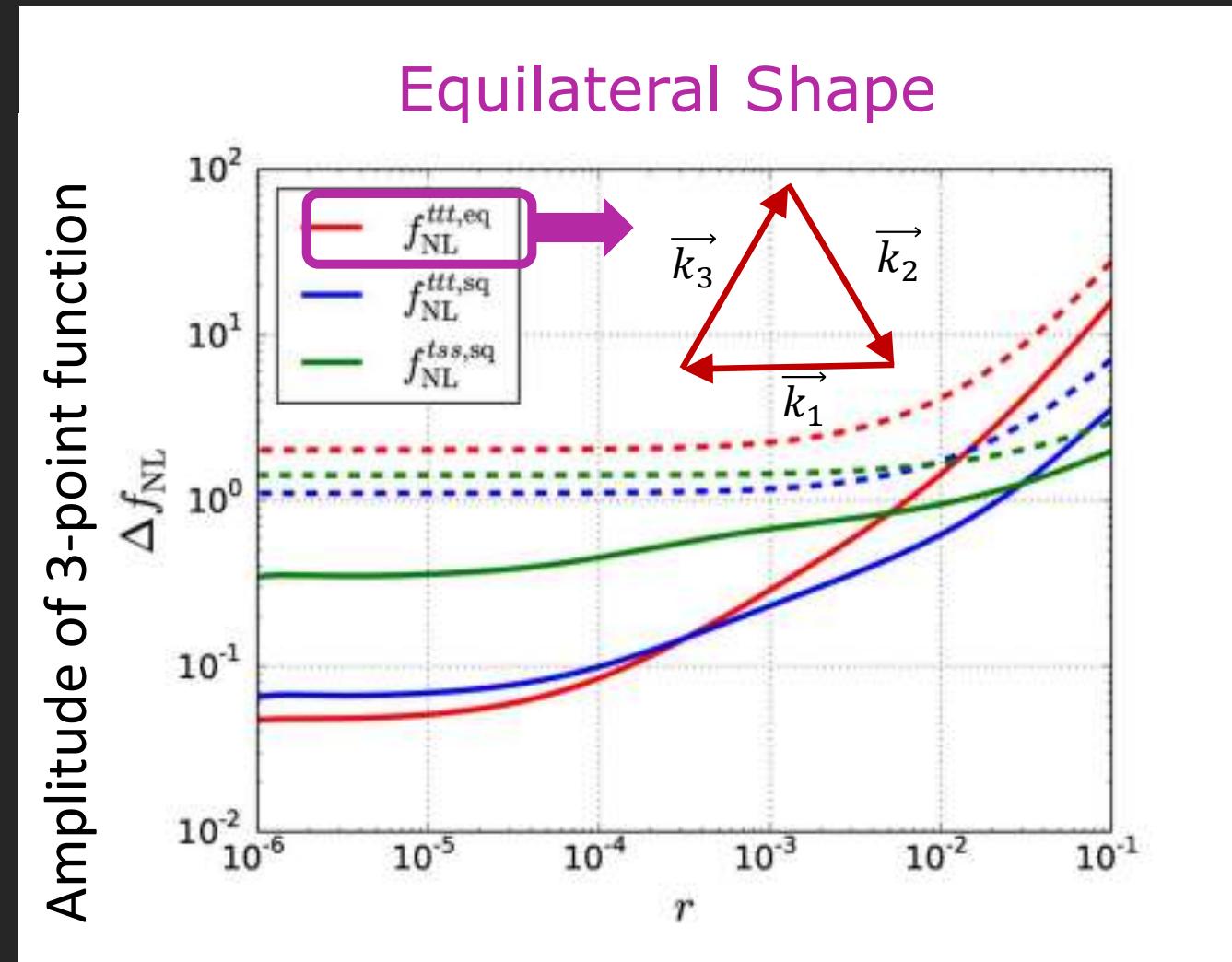
- The sourced tensor modes is Highly non-Gaussian.

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - ig [A_\mu, A_\nu]$$

Self-interaction

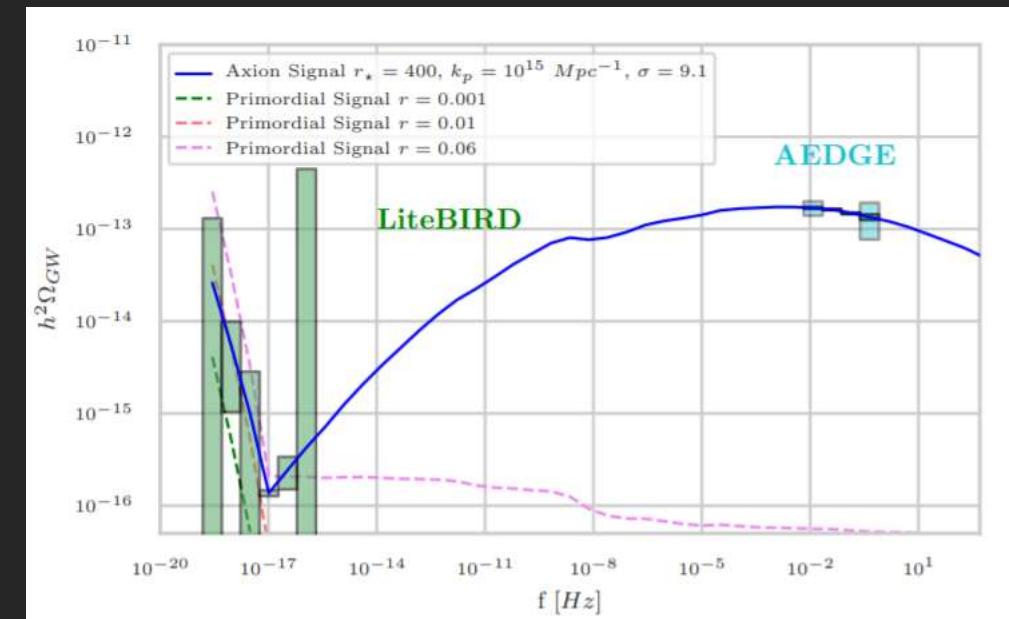
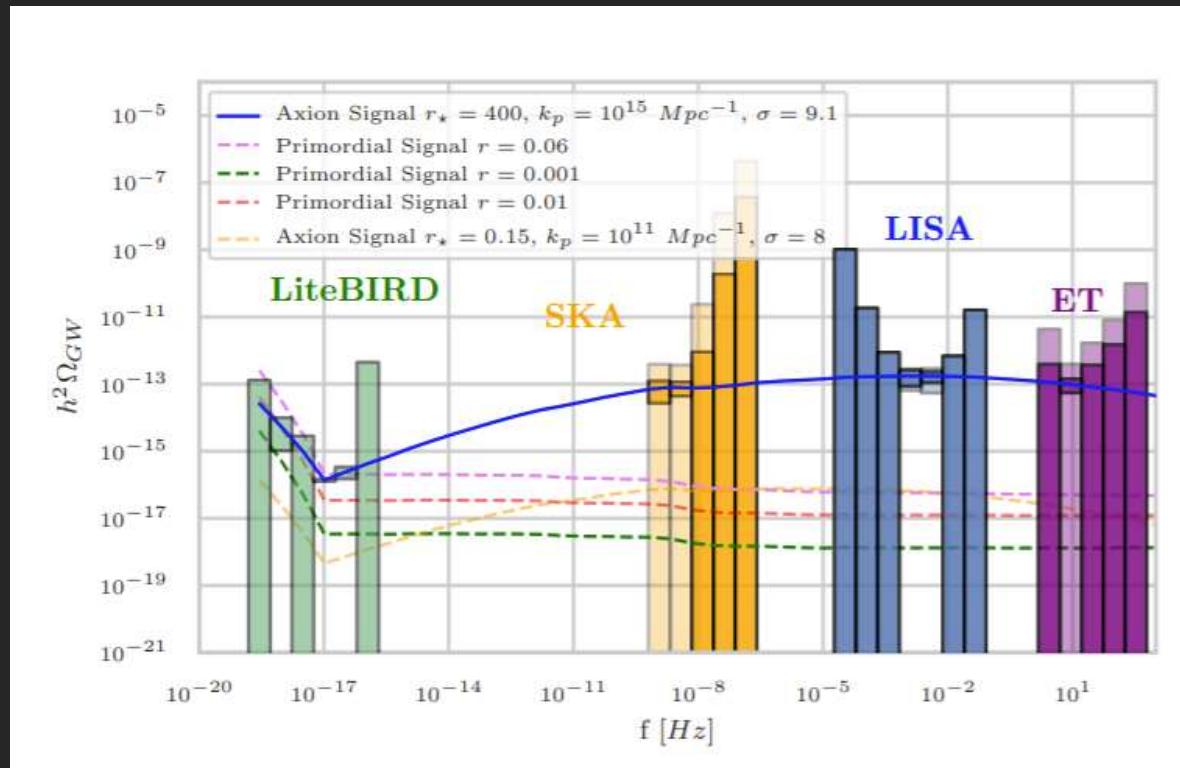
Agrawal, Fujita, Komatsu 2018

- That can be probe with future CMB missions., e.g. *Litebird* and *CMB-S4*!



Novel Observable Signature: Beyond CMB

Detection of this background is an excellent target for all GW experiments across at least 21 decades in frequencies.



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2020

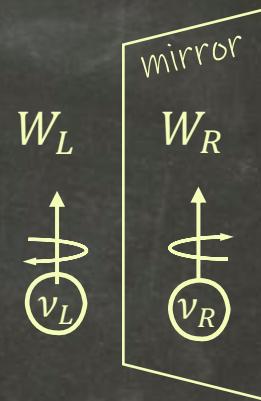
III) Embedding axion-inflation in Left-Right Symmetric Models

(How to Connect Inflaton to SM?)

Axion-Inflation



Left-Right Symmetric
Model (LRSM)



How to Connect it to the SM?

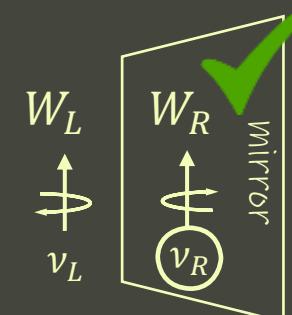
Let us Extend SM Gauge Symmetry by an $SU(2)_R$ and couple it to Axion Inflaton!

- Left-Right Symmetric Model + axion!

$$SU(2)_R \times SU(2)_L \times U(1)_{B-L} \longrightarrow SU(2)_L \times U(1)_Y$$

Left-Right Symmetric

SM Left-handed weak force



- Minimal Scenario of $SU(2)$ -axion inflation A. M., 2016 $f < 0.1 \text{ Mpl}$ & $\lambda < 0.1$

$$S_{AM} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 - \frac{1}{2} ((\partial_\mu \varphi)^2 - V(\varphi)) - \frac{\lambda}{8f} \varphi F \tilde{F} \right)$$

Axion Monodromy or any mechanism that gives a flat potential

Gauge field is $SU(2)_R$

A. M. arXiv: 2012.11516

A. M. arXiv: 2103.14611

Gravitational Leptogenesis: $\langle R\tilde{R} \rangle \neq 0!$



What makes Chiral Gravitational Waves?

To generate circularly polarized GWs, we need **Parity violation** in inflation.
Two possible models are

1) Chern-Simons Gravity $\mathcal{L}_{eff} = \frac{1}{\Lambda} \varphi R\tilde{R}$

Alexander, Peskin, Sheikh-Jabbari 2006

2) Non-Abelian Gauge fields in axion-inflation

A.M., Noorbala, Sheikh-Jabbari 2012

A.M. 2014 & 2016

Caldwell, Devulder 2017

Adshead, Long, Sfakianakis 2017

Alexander, McDonough, Spergel 2018

Kamada, Kume, Yamada, Yokoyama 2019



$\mathcal{L}_{eff} = \frac{1}{\Lambda} \varphi F\tilde{F}$ (Chiral Gauge Field \rightarrow Chiral Gws)

Axion-inflation is a generic setting for leptogenesis
(All the Sakharov conditions are satisfied)

A.M. 2014

Gravitational Leptogenesis: $\langle R\tilde{R} \rangle \neq 0!$



What makes Chiral Gravitational Waves?

To generate circularly polarized GWs, we need **Parity violation** in inflation.
Two possible models are

1) Chern-Simons Gravity $\mathcal{L}_{eff} = \frac{1}{\Lambda} \varphi R\tilde{R}$

Alexander, Peskin, Sheikh-Jabbari 2006

2) Non-Abelian Gauge fields in axion-inflation

A.M., Noorbala, Sheikh-Jabbari 2012

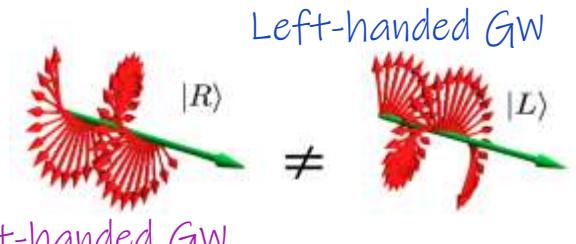
A.M. 2014 & 2016

Caldwell, Devulder 2017

Adshead, Long, Sfakianakis 2017

Alexander, McDonough, Spergel 2018

Kamada, Kume, Yamada, Yokoyama 2019



3) U(1) Gauge fields in axion-inflation

Papageorgiou, Peloso 2017

$$\mathcal{L}_{eff} = \frac{1}{\Lambda} \varphi F\tilde{F}$$

Axion-inflation is a generic setting for leptogenesis
(All the Sakharov conditions are satisfied)

A.M. 2014

Matter Asymmetry by Chiral Anomaly: $\langle F\tilde{F} \rangle \neq 0!$

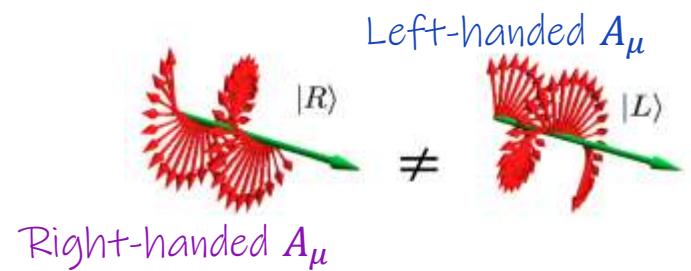
Axion-inflation is a generic setting for lepto/Baryogenesis
(All the Sakharov conditions are satisfied)



1) U(1) Gauge fields in axion-inflation

Domcke, Harling, Morgante, Mukaida 2019

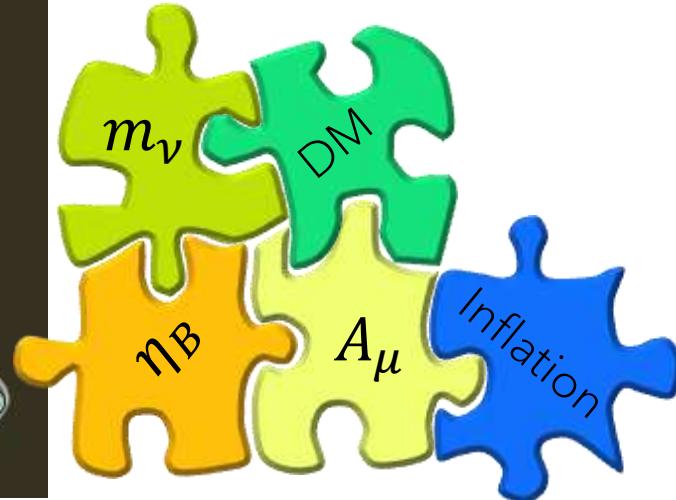
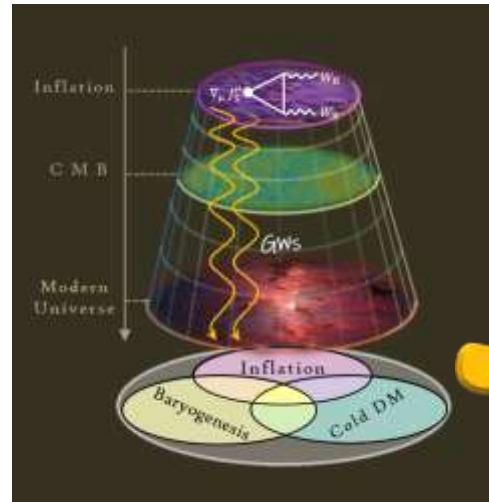
Domcke, Kamada, Mukaida, Schmitz, Yamada 2020



2) Non-Abelian Gauge fields in axion-inflation

A.M. 2019

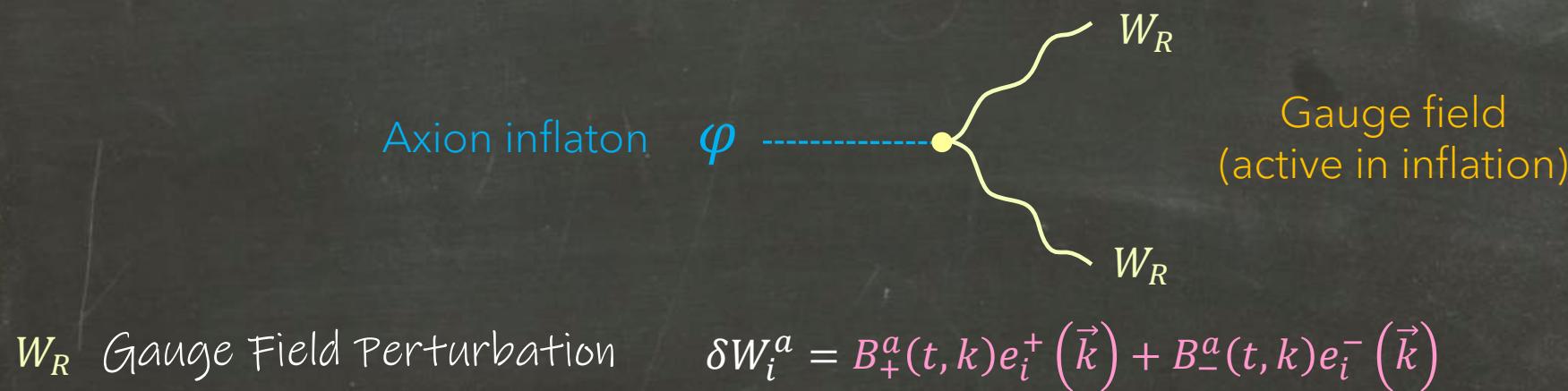
A.M. 2020, 2021



Gauge field Production in Inflation

Let us set the VEV of the Gauge field to zero $\langle W_R \rangle = 0$

- SM Gauge fields are diluted by inflation & unimportant , BUT $SU(2)_R$:



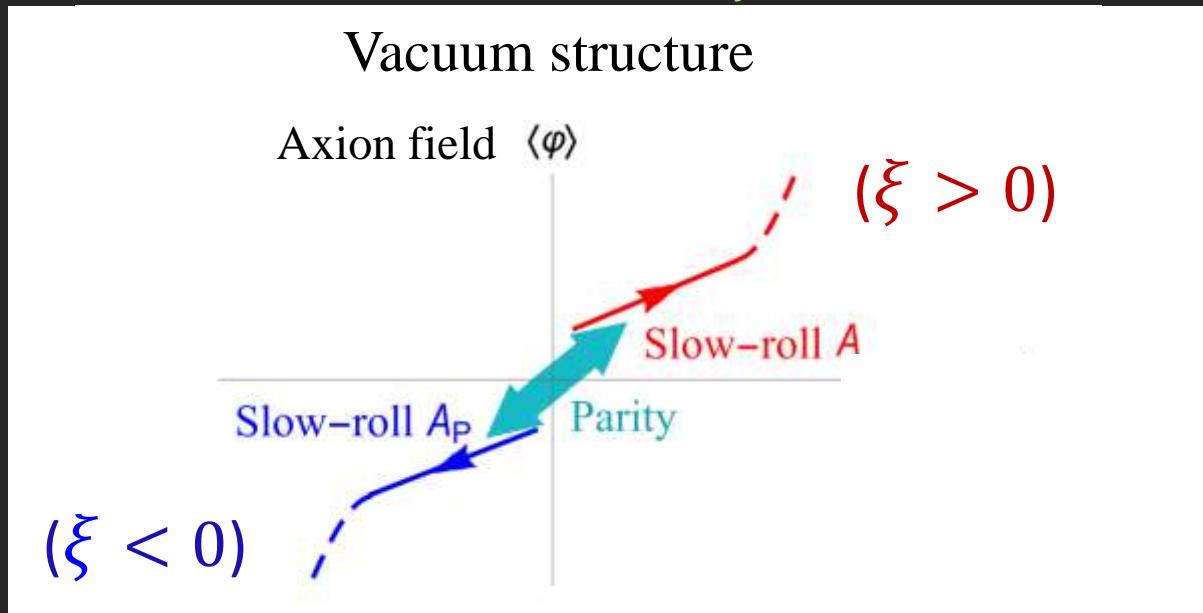
$SU(2)_{\mathbb{R}}$ Gauge Field

- $\delta W_i^a = B_+^a(t, k) e_i^+(\vec{k}) + B_-^a(t, k) e_i^-(\vec{k})$

$$B''_{\pm} + [k^2 \mp \xi k \mathcal{H}] B_{\pm} \approx 0$$

effective frequency

Given by the BG ($\xi = \frac{2\lambda \partial_t \varphi}{f_H}$)



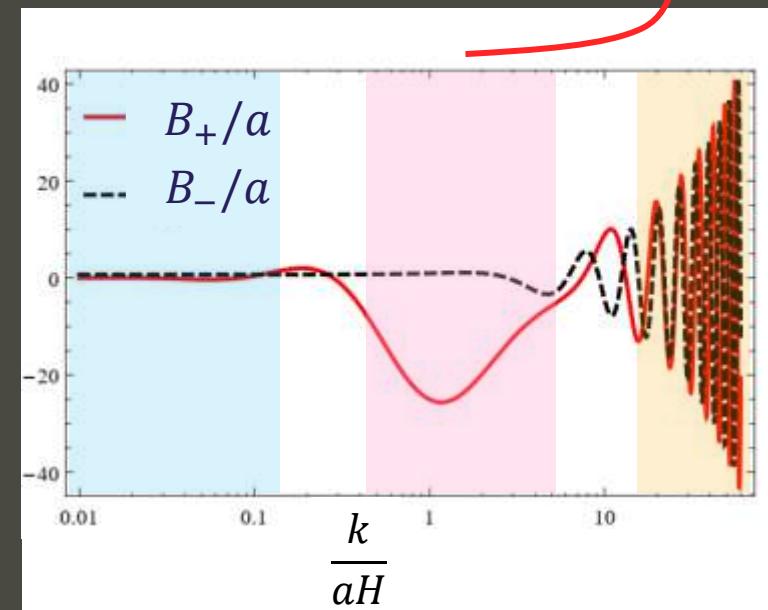
For $\xi > 0$
Short tachyonic growth of B_+



$$n_B \sim \frac{H^3}{6\pi^2} \xi^3 e^{\frac{(2-\sqrt{2})\pi}{2}\xi}$$

Chiral Field

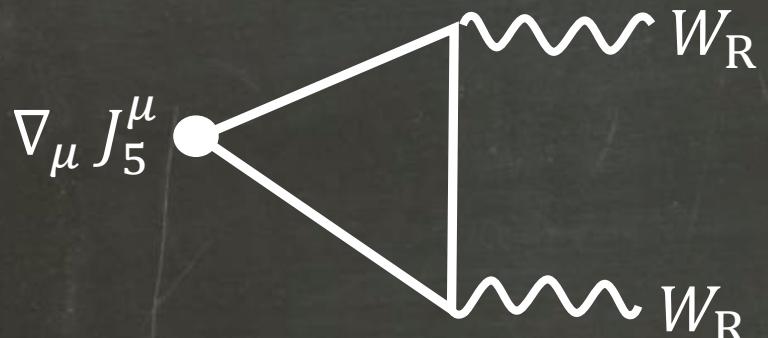
Particle Production



Lepton & quark Production in Inflation

- Left-handed fermions are diluted by inflation, BUT
- Right-handed fermions are generated by $SU(2)_R$ gauge field:

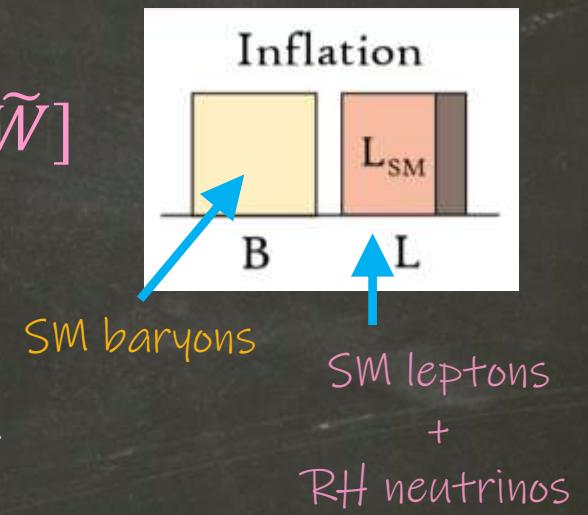
The key ingredient is the Chiral anomaly of $SU(2)_R$ in inflation:



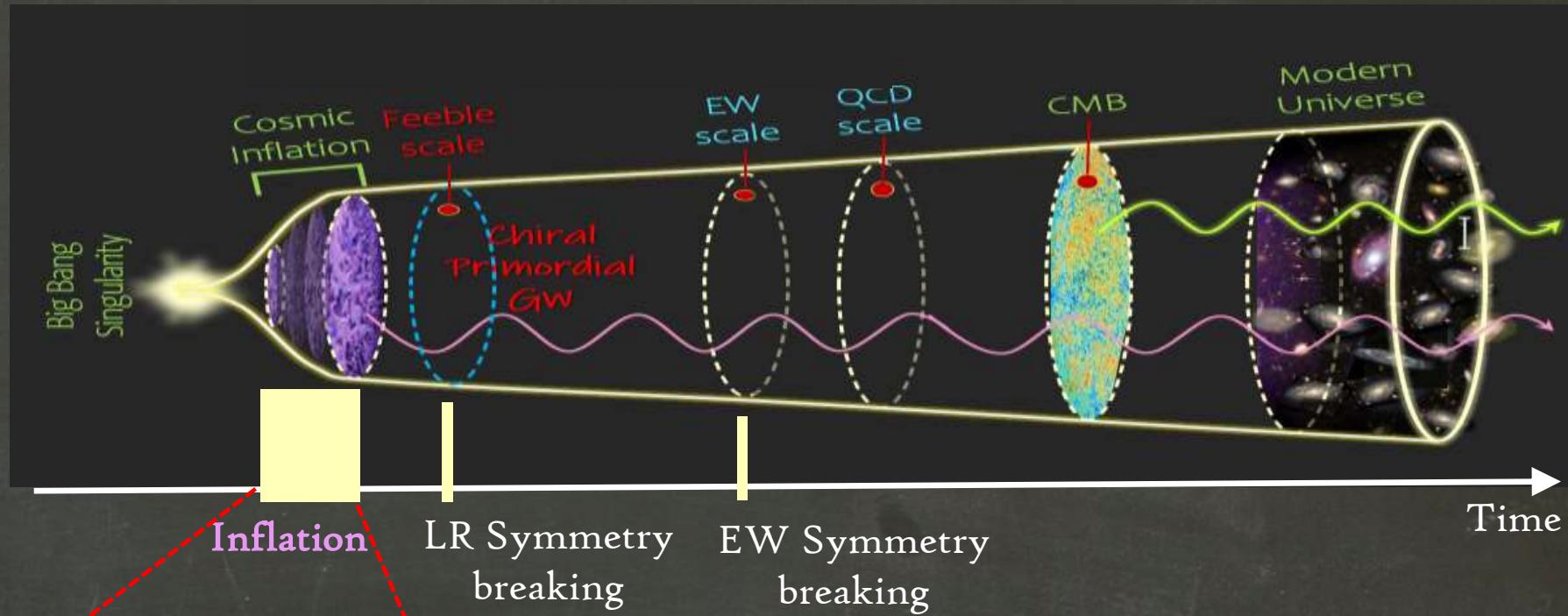
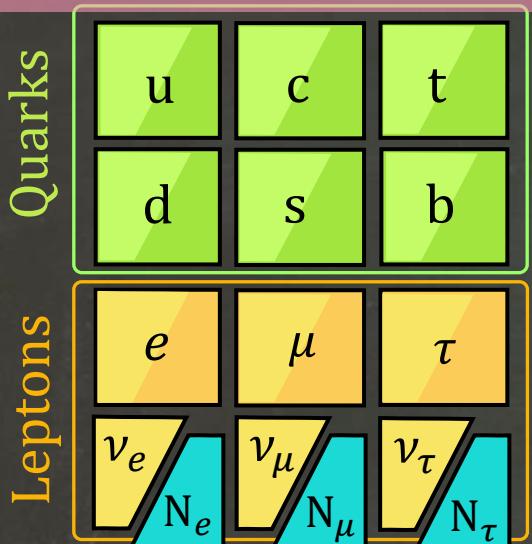
$$\nabla_\mu J_B^\mu = \nabla_\mu J_L^\mu = \frac{g^2}{16\pi^2} \text{tr}[W\tilde{W}]$$

$$n_B = n_L = \alpha_{inf}(\xi) H^3$$

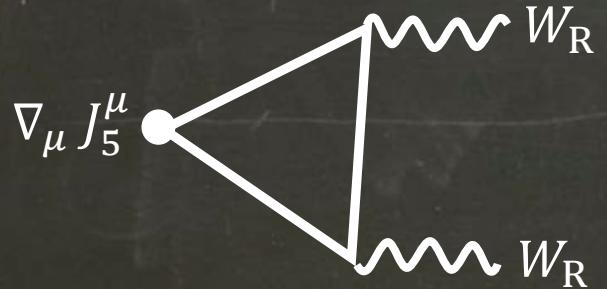
$$\alpha_{inf}(\xi) \sim \frac{g^2}{(2\pi)^4} e^{2\pi\xi}$$



Summary of the mechanism:



Chiral anomaly of $SU(2)_R$
In inflation

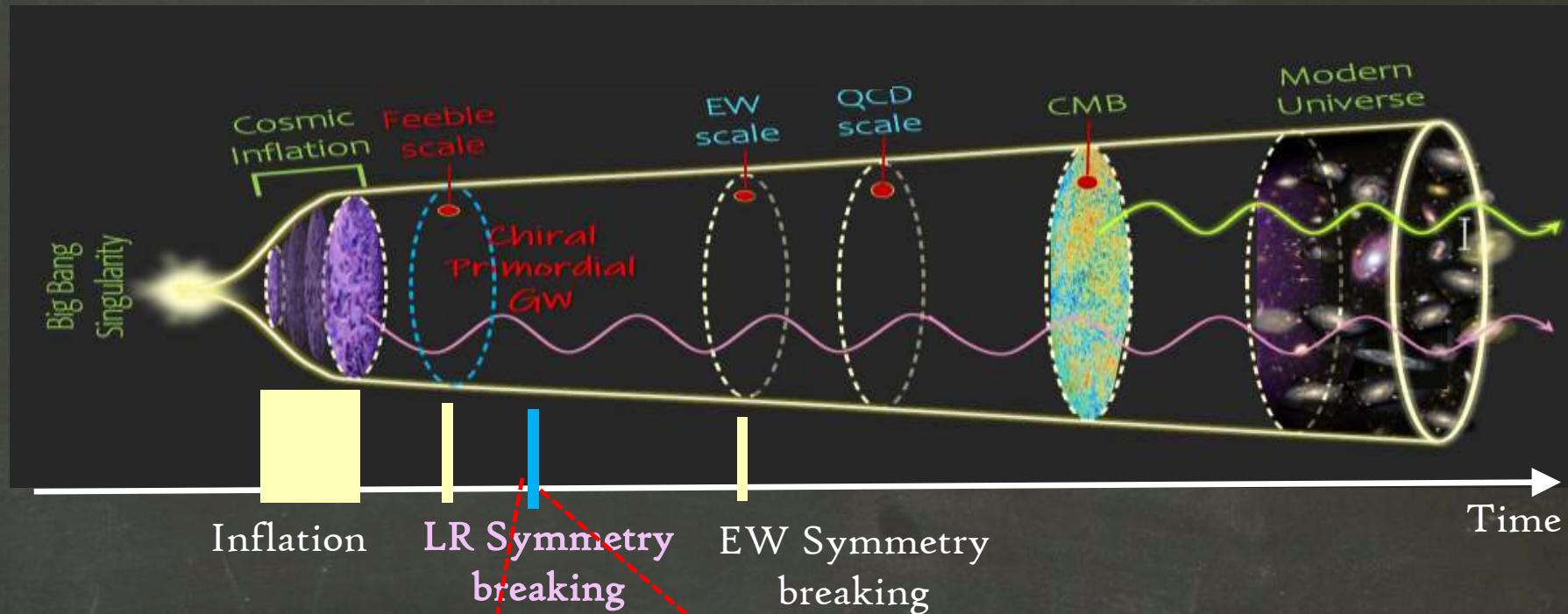
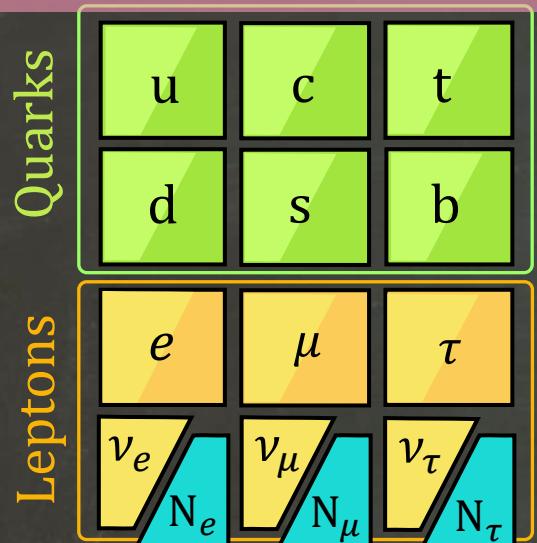


$$B = L = 3n_{CS}$$

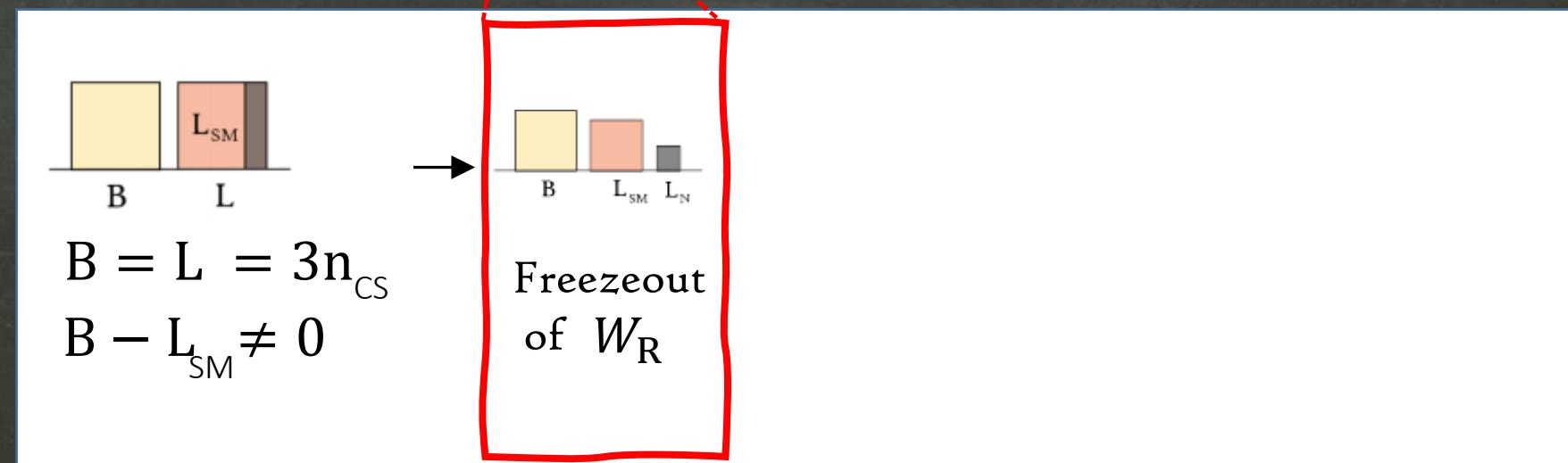
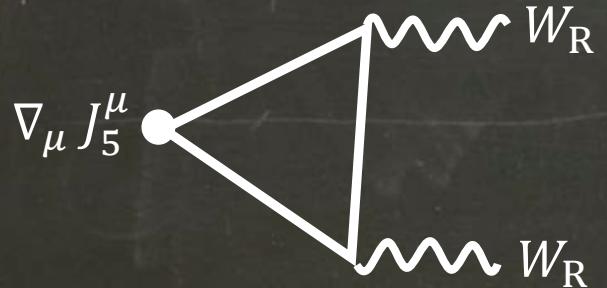
$$B - L_{SM} \neq 0$$

B = SM baryons
L = SM leptons + RH neutrinos

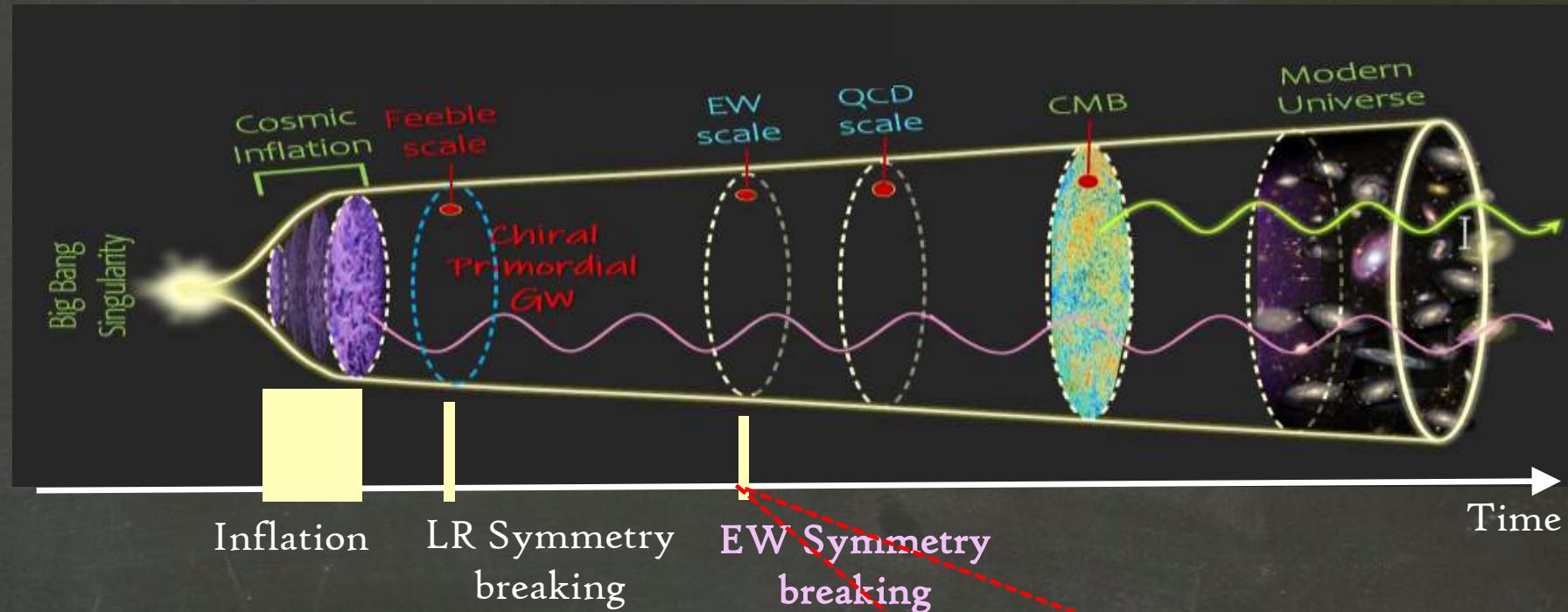
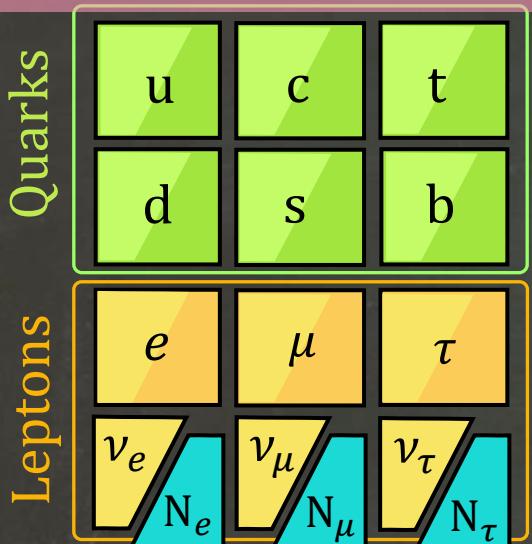
Summary of the mechanism:



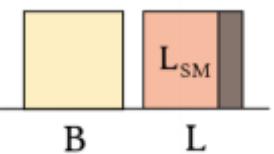
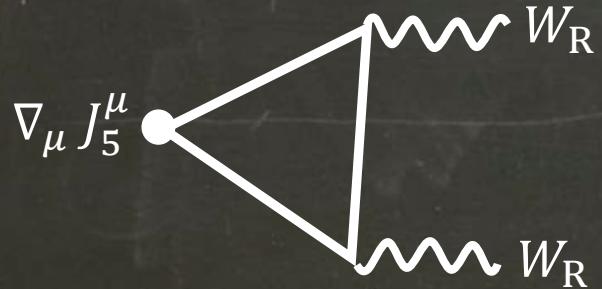
Chiral anomaly of $SU(2)_R$
In inflation



Summary of the mechanism:

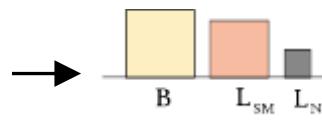


Chiral anomaly of $SU(2)_R$
In inflation

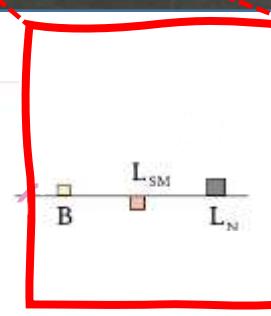


$$B = L = 3n_{CS}$$

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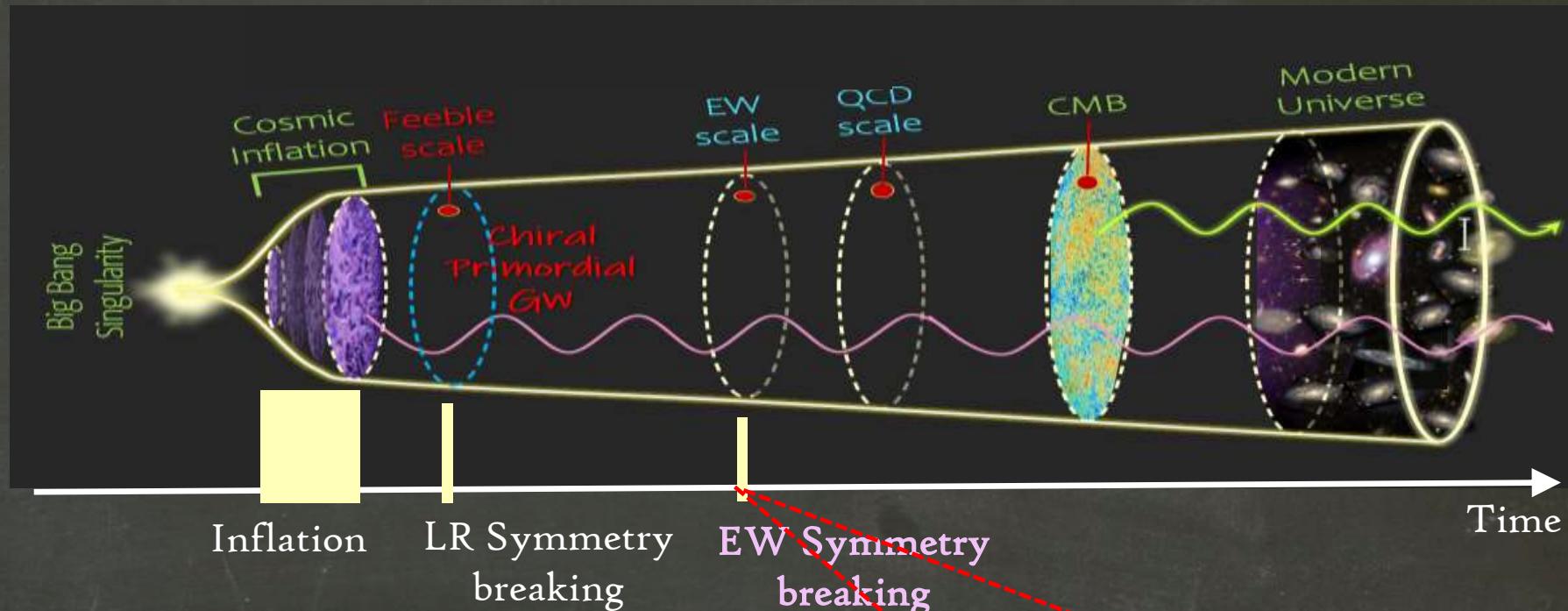
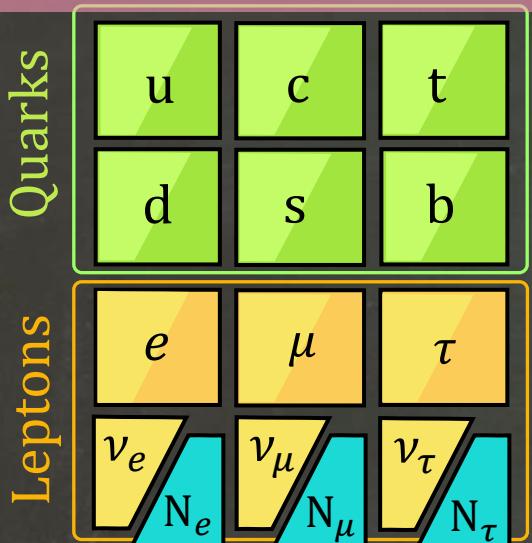


Freezeout
of W_R

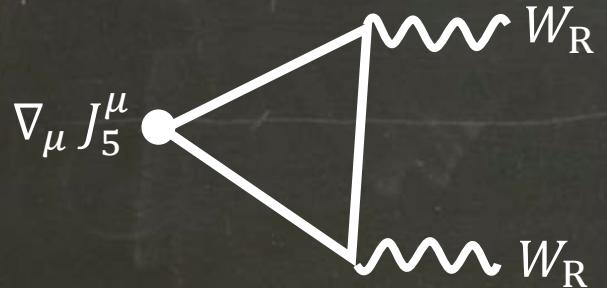


Spectator effects
reshuffle B, L_{SM} & L_N

Summary of the mechanism:

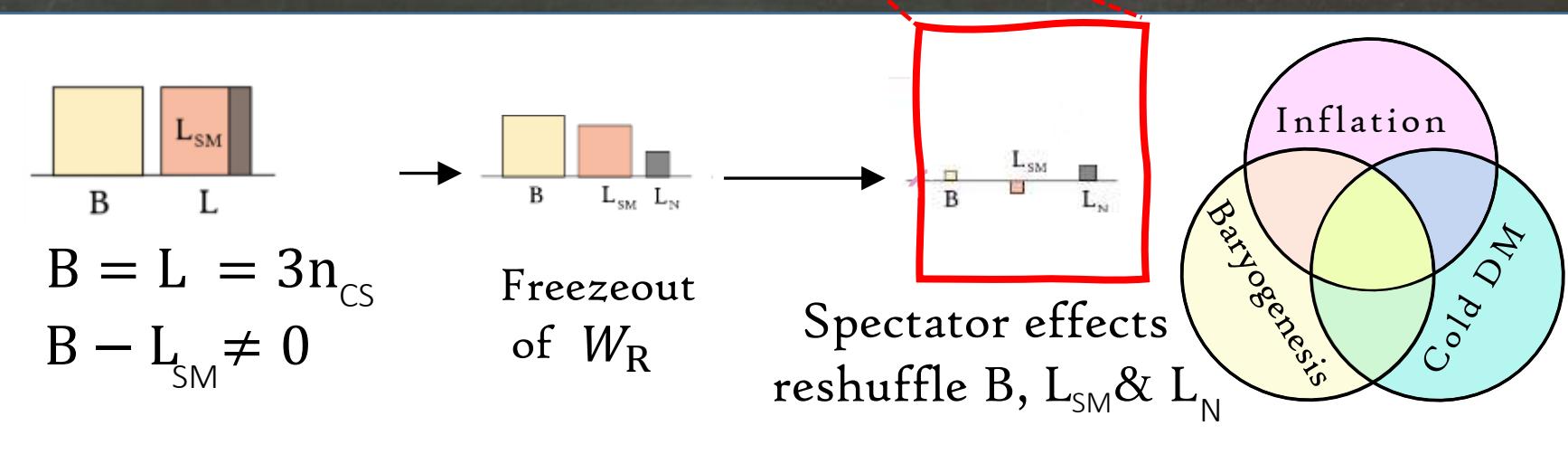


Chiral anomaly of $SU(2)_R$
In inflation

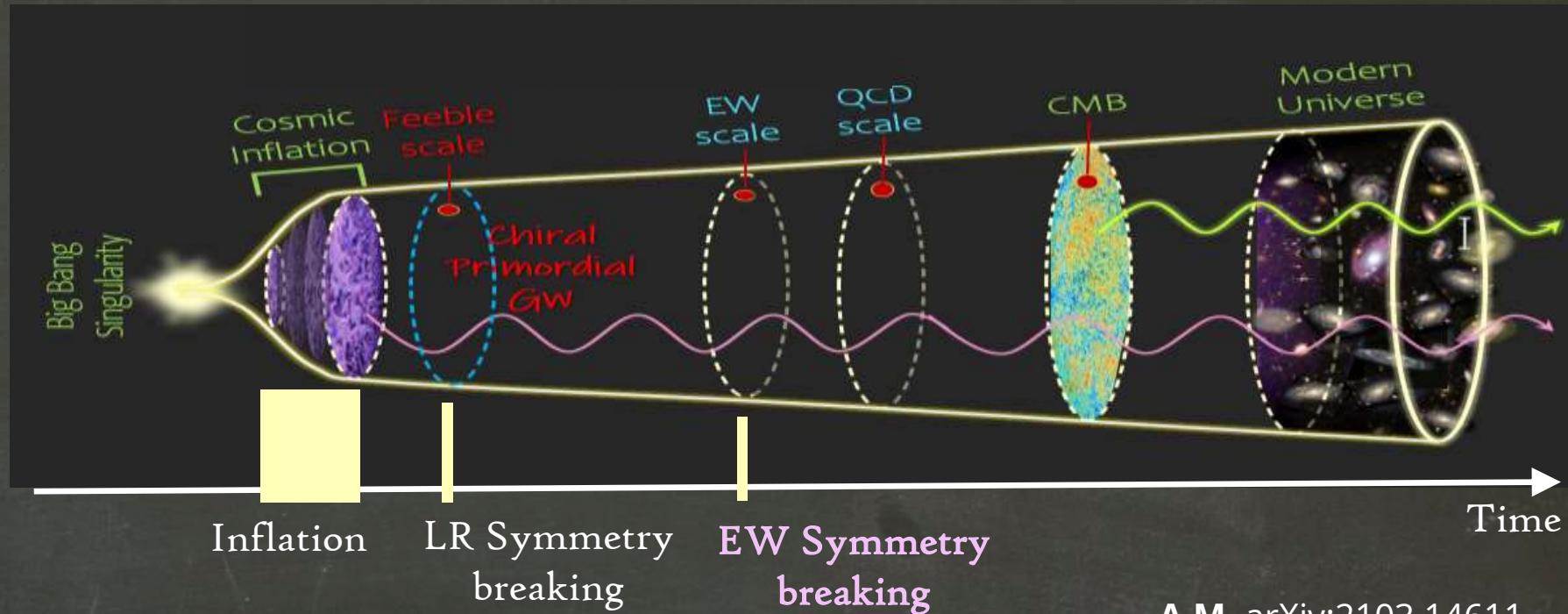
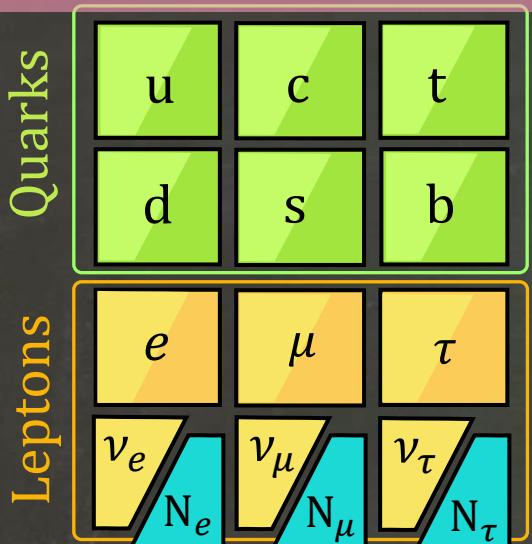


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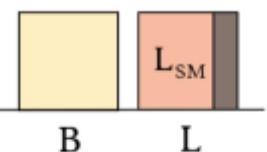
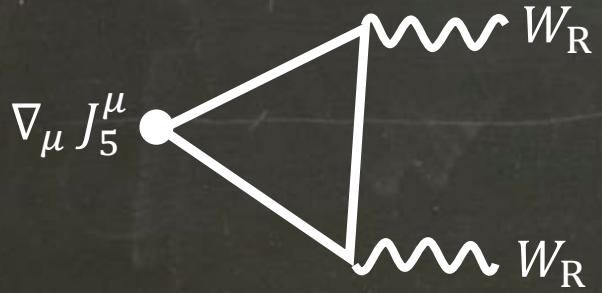


Summary of the mechanism:



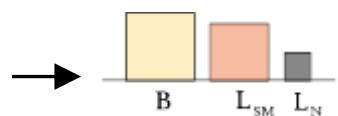
A.M. arXiv:2103.14611

Chiral anomaly of $SU(2)_R$
In inflation



$$B = L = 3n_{CS}$$

$$B - L_{SM} \neq 0$$



Freezeout
of W_R

Baryogenesis

$$\eta_B^0 \approx 3 \left(\frac{g_{\text{eff}}}{100} \right)^{\frac{3}{4}} \frac{\alpha_{\text{inf}}(\xi)}{(\delta_{\text{reh}})^{\frac{3}{4}}} \left(\frac{H}{M_{Pl}} \right)^{\frac{3}{2}}$$

DM

$$\Omega_{N_1} \approx 2.8 \frac{m_{N_1}}{m_p} \Omega_B$$

$$m_{N_1} \simeq 1.8 m_p = 1.7 \text{ GeV.}$$

Summary & Conclusions

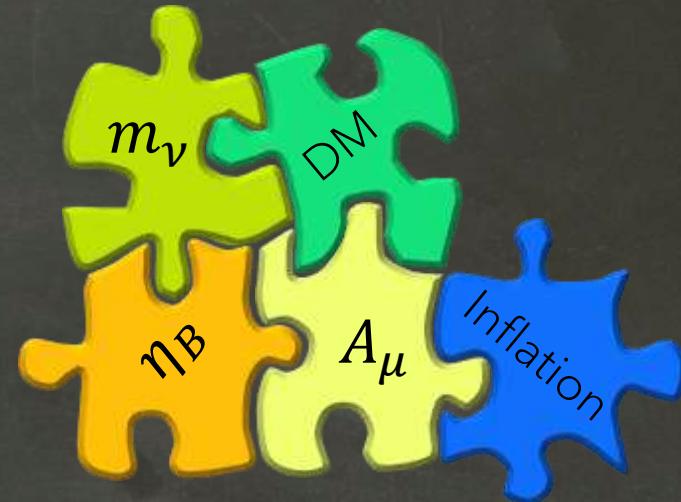


Gauge fields are expected to contribute in physics of axion inflation.

Compelling Consequences:

This Set-up is a **complete BSM** that can solve I-IV:

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM



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Compelling Consequences:

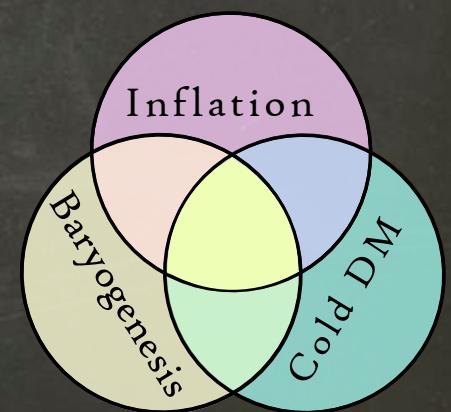
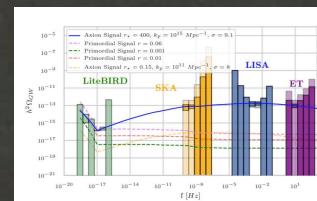
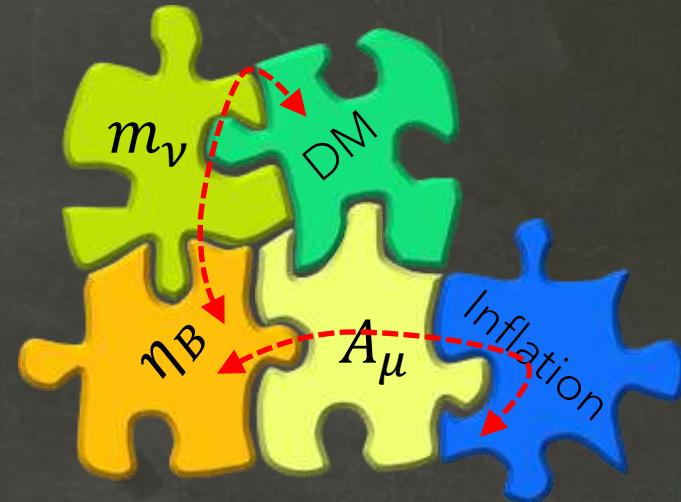
Puzzles of Particle Cosmology

This Set-up is a **complete BSM** that can solve I-IV:

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

It provides a deep connection between **inflation**, **baryogenesis** & **DM**

It comes with a cosmological smoking gun on **Primordial Gws**.



Open Questions & Future Directions



- Thermal Effects in inflation and Warm Inflation
- Strong Backreaction Regime
- Primordial Magnetic Fields
- Connection to the Standard Model

Great science, fresh sea & hills air come visit us in Swansea!



Swansea University
Prifysgol Abertawe

