

June 24th, 2025

Inflationary phenomenology of a non-canonical axion with Chern-Simons interaction

@ Axions in Stockholm 2025



UNIVERSITÀ
DEGLI STUDI
DI PADOVA



Jun'ya Kume (University of Padova)

Based on: arXiv:2501.02890 [astro-ph.CO]

with Marco Peloso, Nicola Bartolo

Outline

- Inflationary phenomenology with Chern-Simons term
- Production of $U(1)$ gauge field and perturbations
- Non-canonical case: large inertia of scalar modes
- Backreaction in non-canonical case...?
- Summary

- **inflation**: accelerating expansion before Hot Big-Bang (Starobinsky, Guth, Sato, ...)

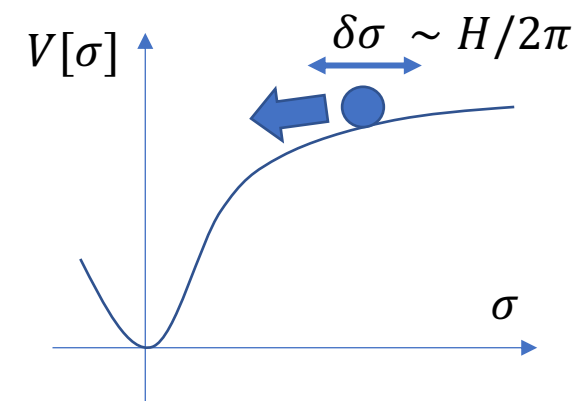
solves classical problems in Big-Bang cosmology

→ **origin of CMB fluctuation!**

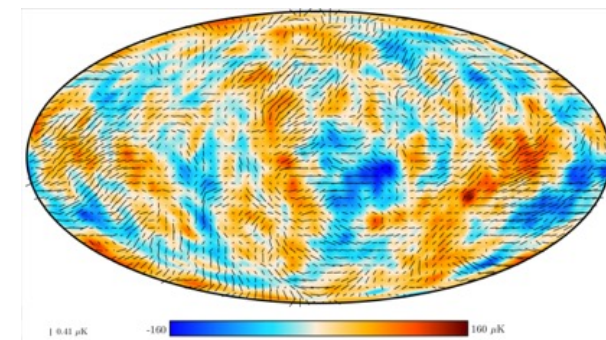
ex.) a scalar field (inflaton) $\sigma(t, \vec{x}) = \bar{\sigma}(t) + \delta\sigma(t, \vec{x})$

→ curvature perturbation $\zeta \cong H\delta\sigma/\dot{\bar{\sigma}}$

power spectrum & spectral index: $P_\zeta(k)$, $n_s - 1 = d\ln P_\zeta/d\ln k$



$$\delta T/T \sim 10^{-5}$$



©ESA/Planck

- **inflation**: accelerating expansion before Hot Big-Bang (Starobinsky, Guth, Sato, ...)

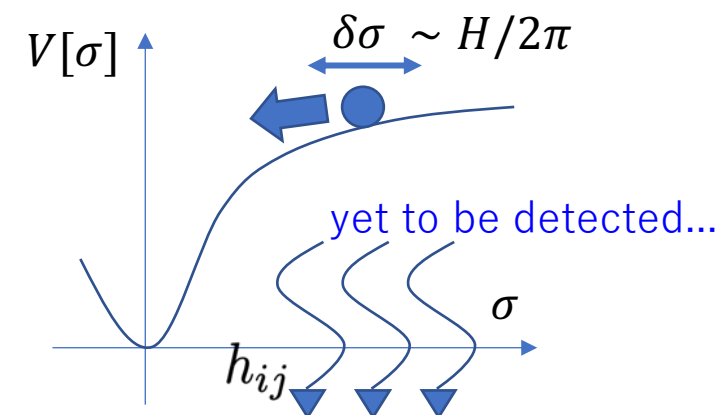
solves classical problems in Big-Bang cosmology

→ **origin of CMB fluctuation!**

ex.) a scalar field (inflaton) $\sigma(t, \vec{x}) = \bar{\sigma}(t) + \delta\sigma(t, \vec{x})$

→ curvature perturbation $\zeta \cong H\delta\sigma/\dot{\bar{\sigma}}$

power spectrum & spectral index: $P_\zeta(k)$, $n_s - 1 = d\ln P_\zeta / d\ln k$



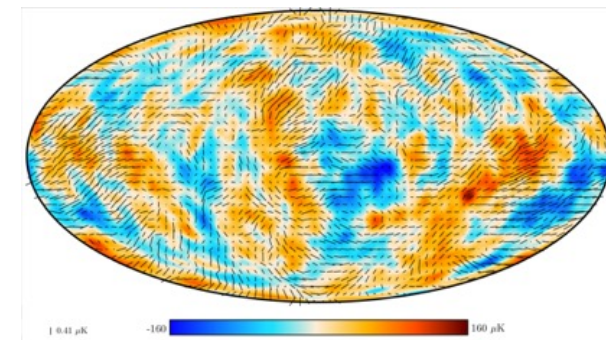
Tensor perturbation as well! → B-mode polarization

tensor-to-scalar ratio: $r \sim P_h/P_\zeta \lesssim 0.03$

vacuum fluctuation:

$$P_h = (2/\pi^2)(H/M_{Pl})^2 \quad \longrightarrow \quad H \lesssim 10^{13} \text{ GeV...!}?$$

$$\delta T/T \sim 10^{-5}$$



©ESA/Planck

- **inflation**: accelerating expansion before Hot Big-Bang (Starobinsky, Guth, Sato, ...)

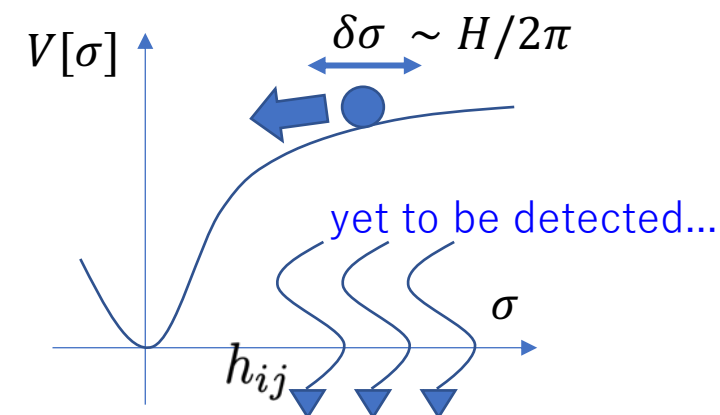
solves classical problems in Big-Bang cosmology

→ **origin of CMB fluctuation!**

ex.) a scalar field (inflaton) $\sigma(t, \vec{x}) = \bar{\sigma}(t) + \delta\sigma(t, \vec{x})$

→ curvature perturbation $\zeta \cong H\delta\sigma/\dot{\bar{\sigma}}$

power spectrum & spectral index: $P_\zeta(k)$, $n_s - 1 = d\ln P_\zeta/d\ln k$



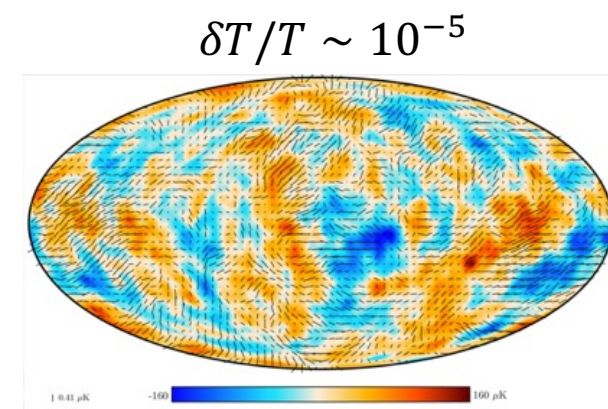
Tensor perturbation as well! → B-mode polarization

tensor-to-scalar ratio: $r \sim P_h/P_\zeta \lesssim 0.03$

vacuum fluctuation:

$$P_h = (2/\pi^2)(H/M_{Pl})^2 \quad \longrightarrow \quad H \lesssim 10^{13} \text{ GeV...!?$$

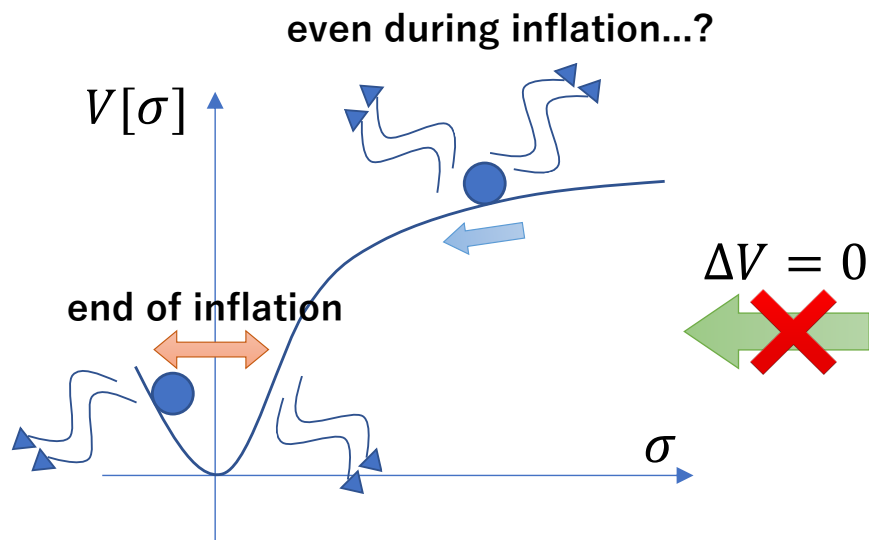
Not true if additional sourced component exists!



©ESA/Planck

- Particle production during inflation

exit from inflation $\rightarrow$ decay into matter fields — matter coupling expected!!



If inflaton is a pseudo-scalar (“axion-like”)...

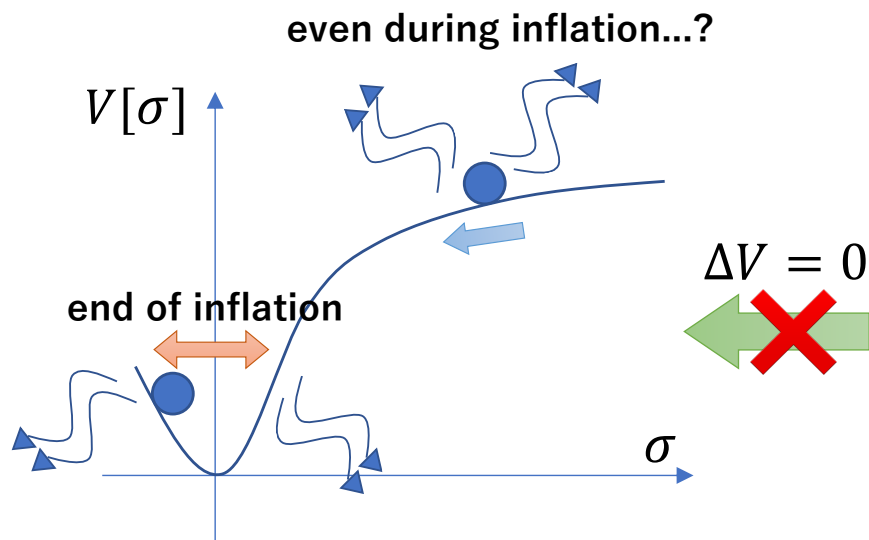
ex.) axial current, Chern-Simons (CS) term

$$\frac{\sigma}{f} \partial_\mu J_5^\mu \quad \underline{\underline{\frac{1}{4f} \sigma F_{\mu\nu} \tilde{F}^{\mu\nu}}} \quad \longleftrightarrow \quad \frac{1}{2f} (\partial_\mu \sigma) \epsilon^{\mu\nu\rho\sigma} A_\nu \partial_\rho A_\sigma$$

✓ compatible with shift symmetry $\phi \rightarrow \phi + \text{const.}$

- Particle production during inflation

exit from inflation $\rightarrow$ decay into matter fields — matter coupling expected!!



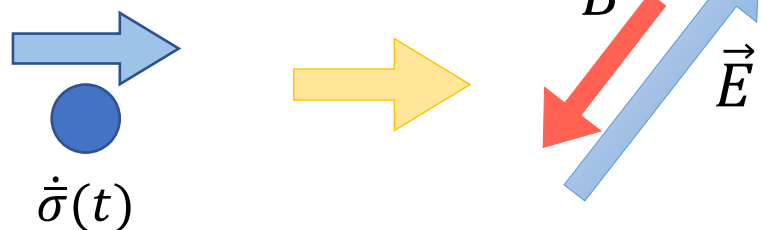
If inflaton is a pseudo-scalar (“axion-like”)...

ex.) axial current, Chern-Simons (CS) term

$$\frac{\sigma}{f} \partial_\mu J_5^\mu \quad \underline{\underline{\frac{1}{4f} \sigma F_{\mu\nu} \tilde{F}^{\mu\nu}}} \quad \longleftrightarrow \quad \frac{1}{2f} (\partial_\mu \sigma) \epsilon^{\mu\nu\rho\sigma} A_\nu \partial_\rho A_\sigma$$

✓ compatible with shift symmetry $\phi \rightarrow \phi + \text{const.}$

axion velocity



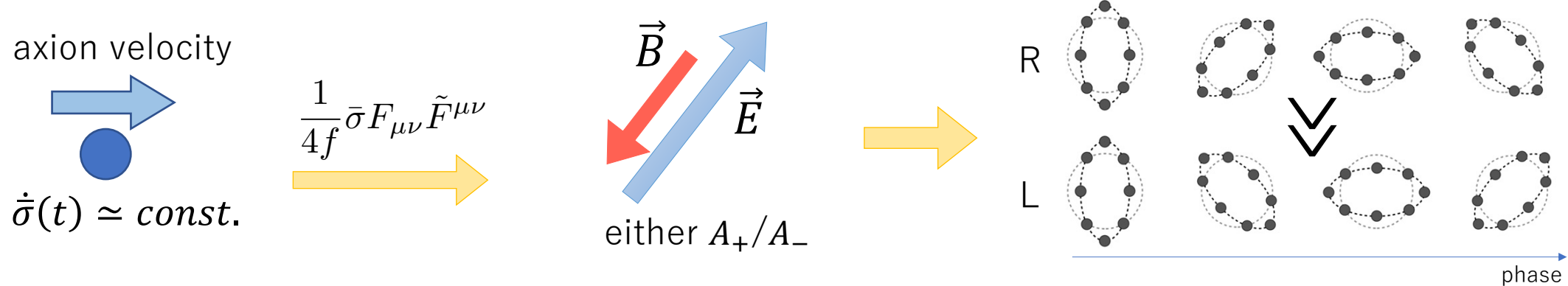
✓ violent amplification

enrich/complicates the primordial perturbations!!

$\rightarrow$ we consider sterile U(1) in our study

✂fermion production: Domcke & Mukaida 2018, Gorbar+2021, Fujita, JK+ 2022, ...

- **Polarized tensor modes** from U(1) CS term (Anber & Sorbo 2006, Sorbo 2011, ...)



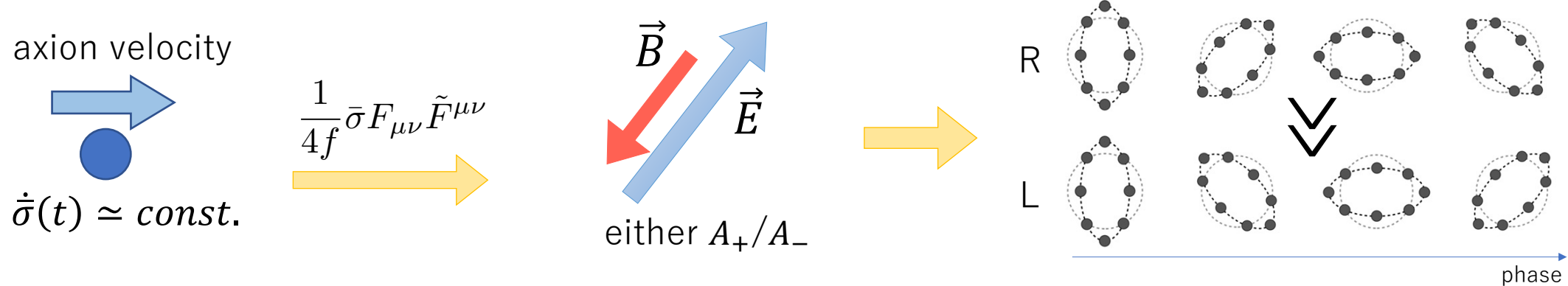
Q1: Visible tensor signal in CMB? – **No!** in the vanilla scenario (Barnaby & Peloso 2010, ...)

- $A + A \rightarrow \delta\sigma$: too efficient & highly non-Gaussian $\rightarrow r_{\text{tot}} \searrow$ & $\dot{\vec{\sigma}}$ cannot be large.



axion as spectator $\rightarrow$ indirect sourcing of ζ (Ferreira & Sloth 2014, Namba+ 2015)

- **Polarized tensor modes** from U(1) CS term (Anber & Sorbo 2006, Sorbo 2011, ...)



Q1: Visible tensor signal in CMB? – **No!** in the vanilla scenario (Barnaby & Peloso 2010, ...)

- $A + A \rightarrow \delta\sigma$: too efficient & highly non-Gaussian $\rightarrow r_{\text{tot}} \searrow$ & $\dot{\sigma}$ cannot be large.

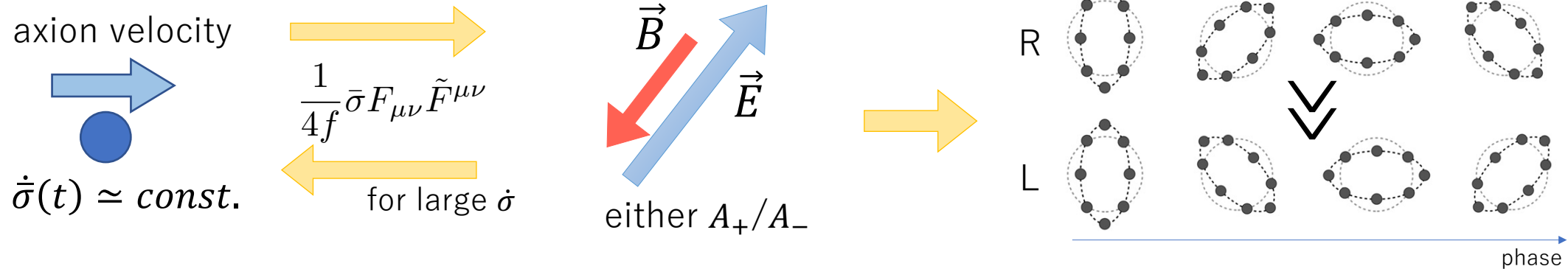


axion as spectator $\rightarrow$ indirect sourcing of ζ (Ferreira & Sloth 2014, Namba+ 2015)



A new solution to Q1! (in 2501.02890) ($\rightarrow$ work in progress: What about backreaction?)

- **Polarized tensor modes** from U(1) CS term (Anber & Sorbo 2006, Sorbo 2011, ...)



Q1: Visible tensor signal in CMB? – **No!** in the vanilla scenario (Barnaby & Peloso 2010, ...)

- $A + A \rightarrow \delta\sigma$: **too efficient & highly non-Gaussian** $\rightarrow r_{\text{tot}} \searrow$ & $\dot{\sigma}$ cannot be large.



axion as spectator $\rightarrow$ indirect sourcing of ζ (Ferreira & Sloth 2014, Namba+ 2015)



A new solution to Q1! (in 2501.02890) ($\rightarrow$ work in progress: What about backreaction?)

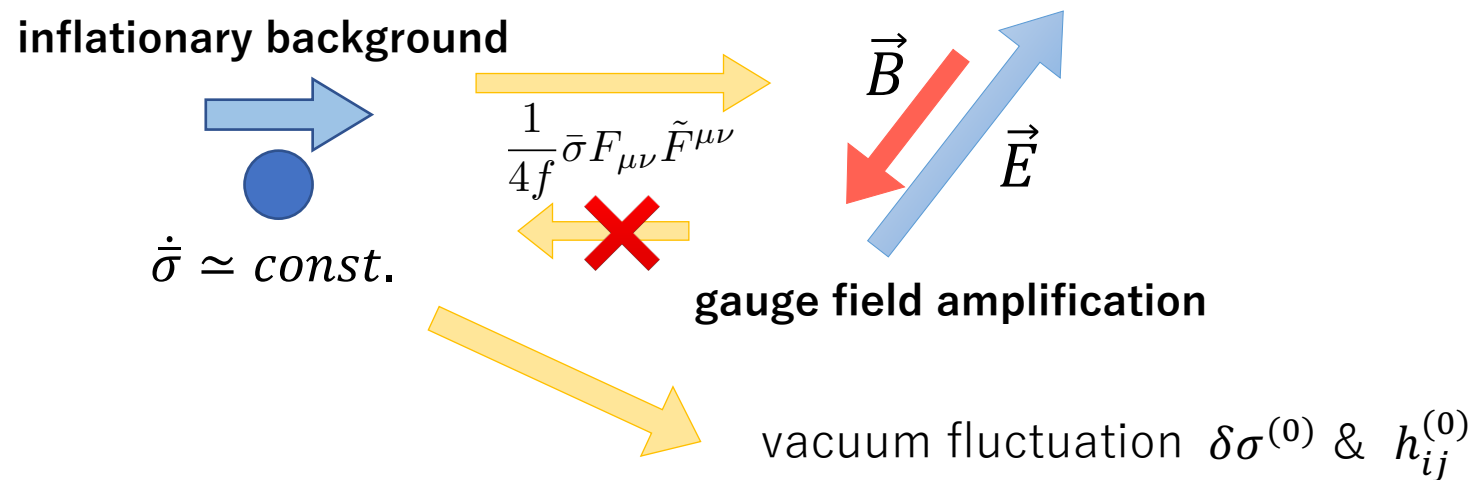
Q2: GWs at interferometer scales? – $\dot{\sigma}$ accelerated & **backreaction becomes relevant!**

- memory: $\bar{\sigma}(t' < t) \rightarrow A_+(t)$ $\longrightarrow$ **oscillatory behavior?** (Cheng+ 2015, Notari 2016, ...)

Outline

- Inflationary phenomenology with Chern-Simons term
- Production of $U(1)$ gauge field and perturbations
- Non-canonical case: large inertia of scalar modes
- Backreaction in non-canonical case...?
- Summary

- Linear & perturbative analysis for CMB signals



$$a \propto e^{Ht}$$

$$H^2 \simeq V/3M_{Pl}^2$$

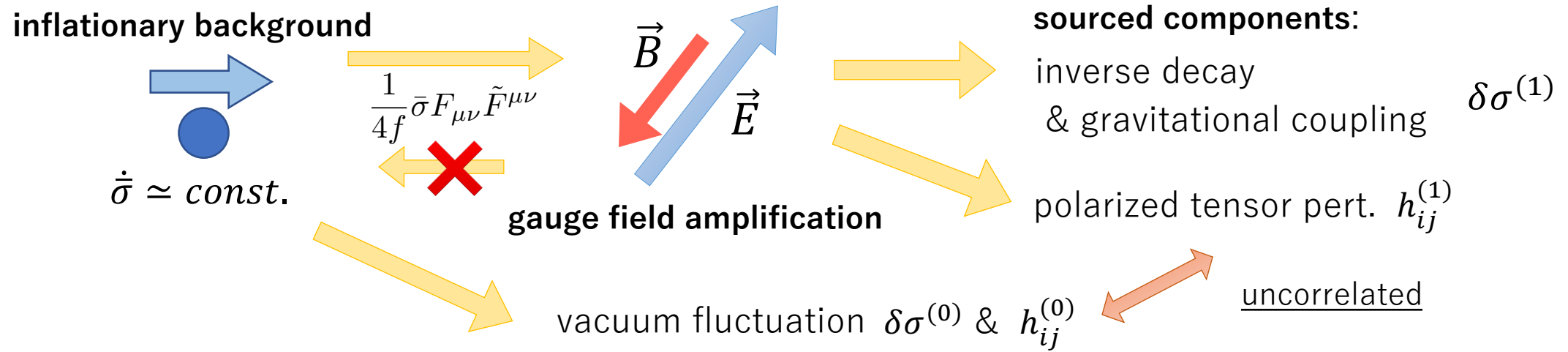
$$3H\dot{\sigma} \simeq -\partial V/\partial\sigma$$

$$\left[\partial_\tau^2 + k^2 \pm 2k \frac{\xi}{\tau} \right] \mathcal{A}_\pm(\tau, k) = 0$$

$$\left[\partial_\tau^2 + k^2 - \frac{z''}{z} \right] v_k^{(0)} = 0$$

$$v^{(0)} \rightarrow z_\sigma \delta\sigma^{(0)}, z_h h^{(0)}$$

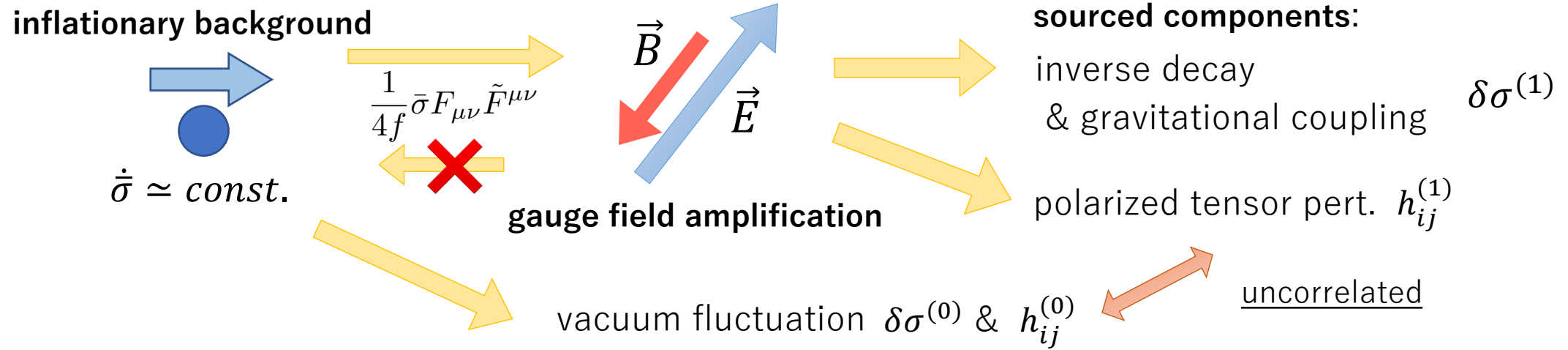
- Linear & perturbative analysis for CMB signals



$$\begin{aligned}
 a &\propto e^{Ht} \\
 H^2 &\simeq V/3M_{Pl}^2 \\
 3H\dot{\sigma} &\simeq -\partial V/\partial\sigma
 \end{aligned}
 \quad \longrightarrow \quad
 \begin{aligned}
 \left[\partial_\tau^2 + k^2 \pm 2k \frac{\xi}{\tau} \right] \mathcal{A}_\pm(\tau, k) &= 0 \\
 \left[\partial_\tau^2 + k^2 - \frac{z''}{z} \right] v_k^{(0)} &= 0
 \end{aligned}
 \quad \longrightarrow \quad
 \left[\partial_\tau^2 + k^2 - \frac{z''}{z} \right] v_k^{(1)} = \underline{\underline{Q[\mathcal{A}_+(\tau, k)]}}$$

$v^{(0)} \rightarrow z_\sigma \delta\sigma^{(0)}, z_h h^{(0)}$

- Linear & perturbative analysis for CMB signals



observables of our interest:

$$P_{\zeta}(k) = P_{\zeta}^{(0)}(k) + P_{\zeta}^{(1)}(k) \quad \text{with vacuum pert.: } 8\pi^2 \epsilon_I P_{\zeta}^{(0)} = H^2 / M_{Pl}^2$$

$$f_{\text{NL}} = \frac{10}{9(2\pi)^{5/2}} \frac{k^6}{P_{\zeta}^2} F|_{|\vec{k}_1|=|\vec{k}_2|=|\vec{k}_3|=k} \quad \langle \hat{\zeta}(0^-, \vec{k}_1) \hat{\zeta}(0^-, \vec{k}_2) \hat{\zeta}(0^-, \vec{k}_3) \rangle \equiv \delta^{(3)}(\vec{k}_1 + \vec{k}_2 + \vec{k}_3) F(\vec{k}_1, \vec{k}_2, \vec{k}_3)$$

$$r = (P_+ + P_-) / P_{\zeta} \quad P_{\pm}: \text{tensor power spectrum for } +/- \text{ polarization}$$

$\otimes \sigma$ can be a spectator $\rightarrow \varphi_I = \{\phi, \sigma\}$ ($\epsilon_I, \eta_I = \text{const.} \ll 1$. assumed in our study)

- Amplification of U(1) gauge field

$$\mathcal{L} \supset \frac{1}{4f} \sigma F_{\mu\nu} \tilde{F}^{\mu\nu} \rightarrow \text{circular pol.: } A_+/A_-$$

Quantization: $\hat{A}_\lambda(\tau, \mathbf{k}) = \hat{a}_\mathbf{k}^{(\lambda)} \mathcal{A}_\lambda(\tau, k) + \hat{a}_{-\mathbf{k}}^{(\lambda)\dagger} \mathcal{A}_\lambda^*(\tau, k)$

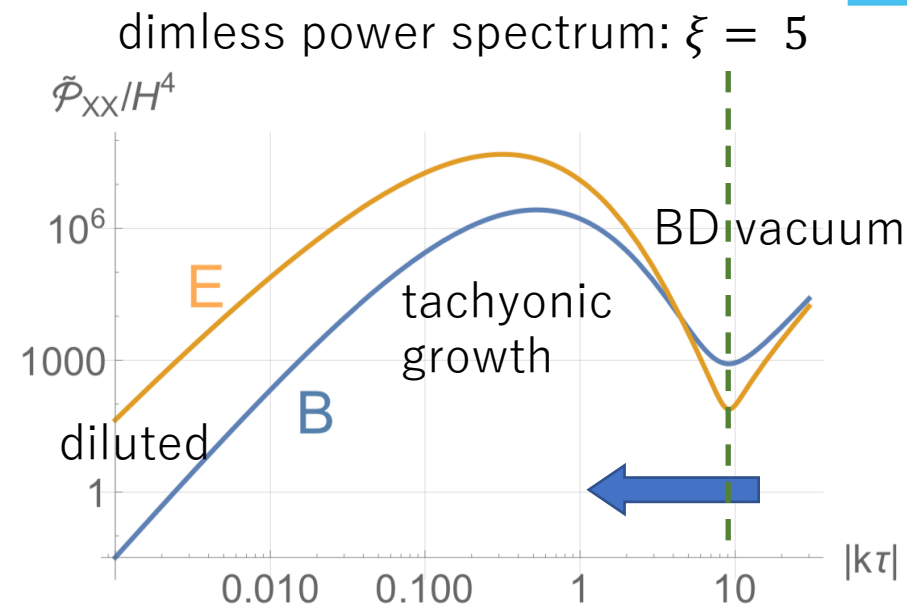
$$\Rightarrow \left[\partial_\tau^2 + k^2 \pm 2k \frac{\xi}{\tau} \right] \mathcal{A}_\pm(\tau, k) = 0 \quad \text{with} \quad \xi \equiv \frac{\dot{\sigma}}{2fH}$$

Only + mode experiences **exponential growth!** ($\xi \lesssim 5$ for negligible backreaction)

Imposing Bunch-Davies condition:

$$\mathcal{A}_+(\tau, k) = \frac{1}{\sqrt{2k}} e^{\pi\xi/2} W_{-i\xi, 1/2}(2ik\tau) \cong \frac{1}{\sqrt{2k}} \left(\frac{k}{2\xi aH} \right)^{1/4} e^{\pi\xi - 2\sqrt{2\xi k/(aH)}} \quad \leftarrow \text{around the peak}$$

Electromagnetic variables: $\hat{E}_i \equiv -\frac{1}{a^2} \hat{A}'_i$, $\hat{B}_i \equiv \frac{1}{a^2} \epsilon_{ijk} \partial_j \hat{A}_k$



- Sourced perturbations

$$\Delta\mathcal{S}_{sAA} = \frac{1}{2} \int d\tau d^3k \left[-\frac{\dot{\varphi}_I}{2M_p^2 H} \frac{1}{a} \left(\underbrace{a^4 Q_1 - \frac{ik_k}{k^2} (a^4 Q_{2,k})'}_{\text{gravitational coupling}} \right) v_I^\dagger + \underbrace{a^3 \frac{Q_3}{f}}_{\text{inverse decay}} v_\sigma^\dagger + \text{h.c.} \right] \quad \begin{array}{l} v_I: \text{canonical variables} \\ I = \{\sigma\} \text{ or } \{\phi, \sigma\} \end{array}$$

with $Q_1(x) \equiv \frac{1}{2} (\hat{E}_i \hat{E}_i + \hat{B}_i \hat{B}_i)$ $Q_{2,k}(x) \equiv \epsilon_{ijk} \hat{E}_i \hat{B}_j \ll Q_3(x) \equiv \hat{E}_i \hat{B}_i$

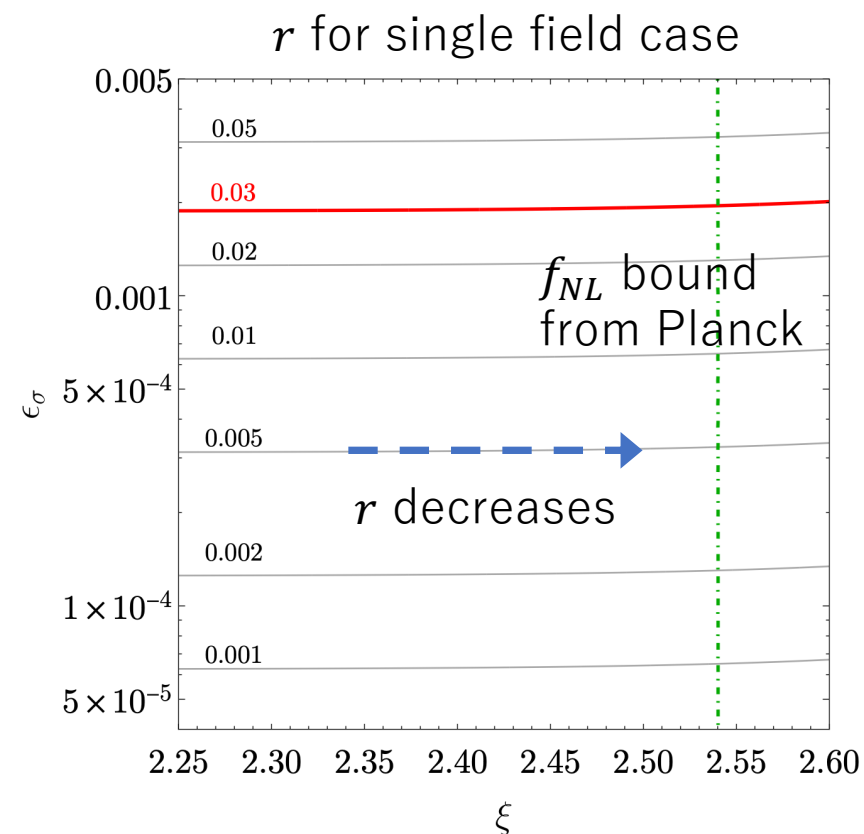
- single field case: $\{I, \varphi_I\} \rightarrow \sigma$

$$v_\sigma^{(1)} \rightarrow \zeta^{(1)} \quad > \quad \hat{E}_i \hat{E}_j + \hat{B}_i \hat{B}_j \quad h_{ij}^{(1)}$$

- two-field case:

$$v_\sigma^{(1)} \xrightarrow{\epsilon_\phi \Delta N} v_\phi^{(1)} \rightarrow \zeta^{(1)}$$

σ decays $\Delta N \lesssim 5$ e-folds
after the CMB mode crossing
 $\rightarrow$ visible sourced tensor
(Ferreira & Sloth 2014, Namba+ 2015)



Outline

- Inflationary phenomenology with Chern-Simons term
- Production of $U(1)$ gauge field and perturbations
- Non-canonical case: large inertia of scalar modes
- Backreaction in non-canonical case...?
- Summary

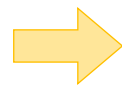
- Non-canonical scalar and perturbation

$$\mathcal{L} = K_\phi(X) - V(\hat{\phi}) \quad X \equiv -\frac{1}{2}g^{\mu\nu}\partial_\mu\hat{\phi}\partial_\nu\hat{\phi}$$

Scalar field (**b.g. & pert.**) acquires large inertia:

$$\underline{\underline{\left(K_{\phi,1} + \dot{\phi}^2 K_{\phi,2}\right) \ddot{\phi} + 3K_{\phi,1} \frac{\dot{a}}{a} \dot{\phi} + \frac{\partial V}{\partial \phi} = 0}} \quad K_{\phi,n} \equiv (\partial/\partial X)^n K_\phi$$

$$\text{sound speed: } c_{s,I}^2 \equiv \frac{K_{I,1}}{K_{I,1} + \dot{\phi}_I^2 K_{I,2}}$$



parametrical changes $\hat{\zeta} \simeq \frac{c_{s,I} H \tau}{\sqrt{2\epsilon_I} M_{\text{Pl}}} v_I$

- power spectrum

$$\mathcal{P}_\zeta^{(0)} = \frac{H^2}{8\pi^2 c_{s,I} \epsilon_I M_{\text{Pl}}^2} \rightarrow r = 16\epsilon_I c_{s,I}$$

- non-Gaussianity

$$f_{\text{NL}} = \frac{\langle \zeta \zeta \zeta \rangle}{\langle \zeta \zeta \rangle^2} \propto \frac{1}{c_s^2} \rightarrow \text{CMB bound on single field EFT: } c_s < 0.02$$

✂ standard scenario recovered by taking $c_s \rightarrow 1$

✂ smaller $c_s \leftrightarrow$ larger inertia ($\rightarrow$ persistence of the vacuum mode, enhancing the non-linearity...?)

- examples, but not for a pseudo-scalar...

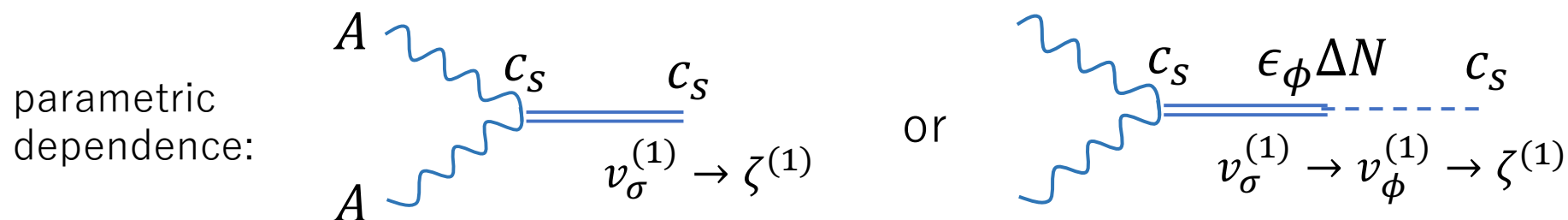
k-inflation:

Armendariz-Picon 1999, Garriga & Mukhanov 1999

DBI-model: Silverstein & Tong 2003, Alishahiha+ 2004

- Suppressing the scalar sourcing by gauge field

$$\hat{\zeta} \simeq \frac{c_{s,I} H \tau}{\sqrt{2\epsilon_I} M_{\text{Pl}}} v_I \quad \& \quad \frac{1}{2} \int d\tau d^3k \left[-\frac{\sqrt{K_{I,1}} \dot{\phi}_I}{2M_p^2 H} \frac{1}{ac_{s,I}} \left(c_{s,I}^2 a^4 Q_1 - \frac{ik_k}{k^2} (a^4 Q_{2,k})' \right) v_I^\dagger + \frac{c_{s,\sigma}}{\sqrt{K_{\sigma,1}}} a^3 \frac{Q_3}{f} v_\sigma^\dagger + \text{h.c.} \right]$$



single field case:

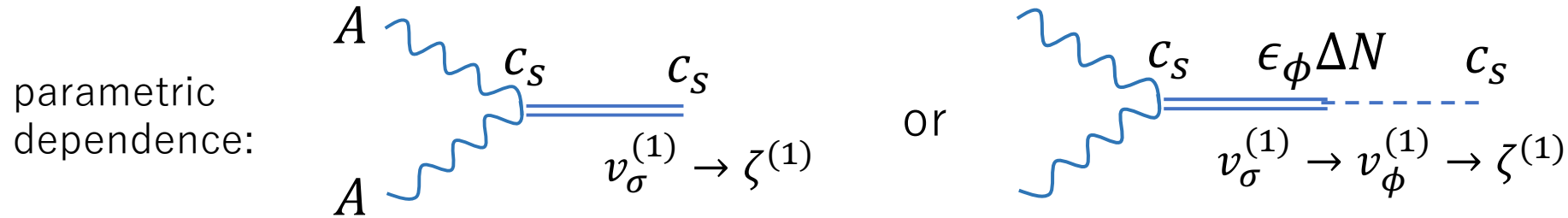
$$\hat{\zeta}^{(1)}(0^-, \vec{k}) \simeq \frac{H^2}{M_p^2} \int_{-\infty}^{0^-} d\tau' k \left(-\frac{k^3 \tau'^3}{3} \right) \left[\frac{1}{2} J_{1,2}(\tau', \vec{k}) - \frac{c_{s,\sigma}^2 \xi}{\epsilon_\sigma} J_3(\tau', \vec{k}) \right]$$

$\sim Q_1 + Q_2$ $\sim Q_3$

※ Q_2 not suppressed by $c_s \rightarrow$ must be included for smaller c_s

- Suppressing the scalar sourcing by gauge field

$$\hat{\zeta} \simeq \frac{c_{s,I} H \tau}{\sqrt{2\epsilon_I} M_{\text{Pl}}} v_I \quad \& \quad \frac{1}{2} \int d\tau d^3k \left[-\frac{\sqrt{K_{I,1}} \dot{\phi}_I}{2M_p^2 H} \frac{1}{ac_{s,I}} \left(c_{s,I}^2 a^4 Q_1 - \frac{ik_k}{k^2} (a^4 Q_{2,k})' \right) v_I^\dagger + \frac{c_{s,\sigma}}{\sqrt{K_{\sigma,1}}} a^3 \frac{Q_3}{f} v_\sigma^\dagger + \text{h.c.} \right]$$



single field case:

$$\hat{\zeta}^{(1)}(0^-, \vec{k}) \simeq \frac{H^2}{M_p^2} \int_{-\infty}^{0^-} d\tau' k \left(-\frac{k^3 \tau'^3}{3} \right) \left[\frac{1}{2} J_{1,2}(\tau', \vec{k}) - \frac{c_{s,\sigma}^2 \xi}{\epsilon_\sigma} J_3(\tau', \vec{k}) \right]$$

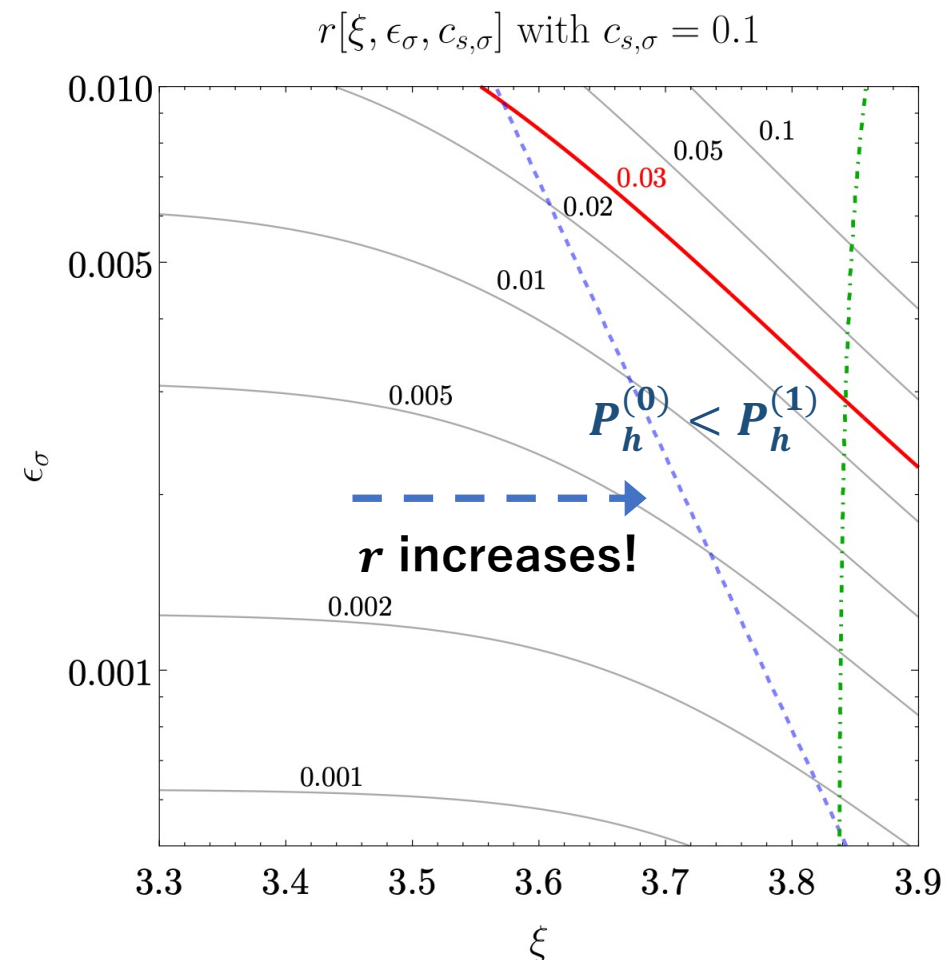
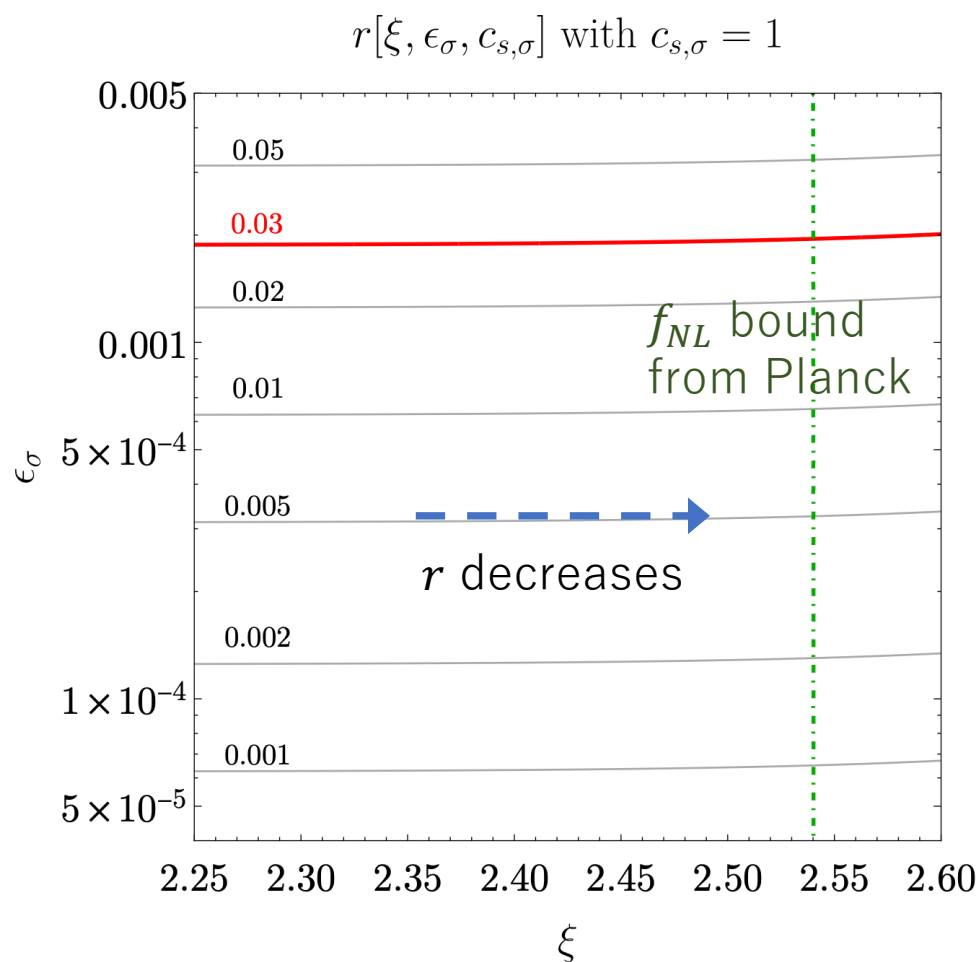
$\sim Q_1 + Q_2$ $\sim Q_3$

※ Q_2 not suppressed by $c_s \rightarrow$ must be included for smaller c_s

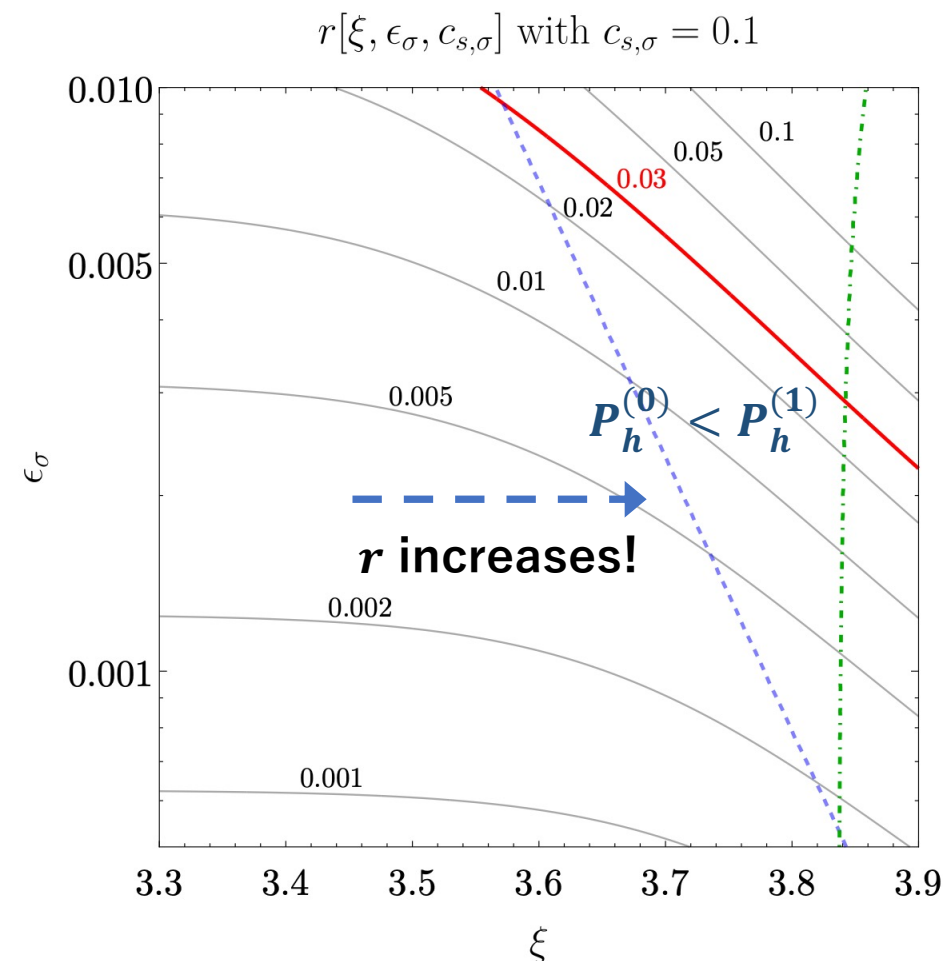
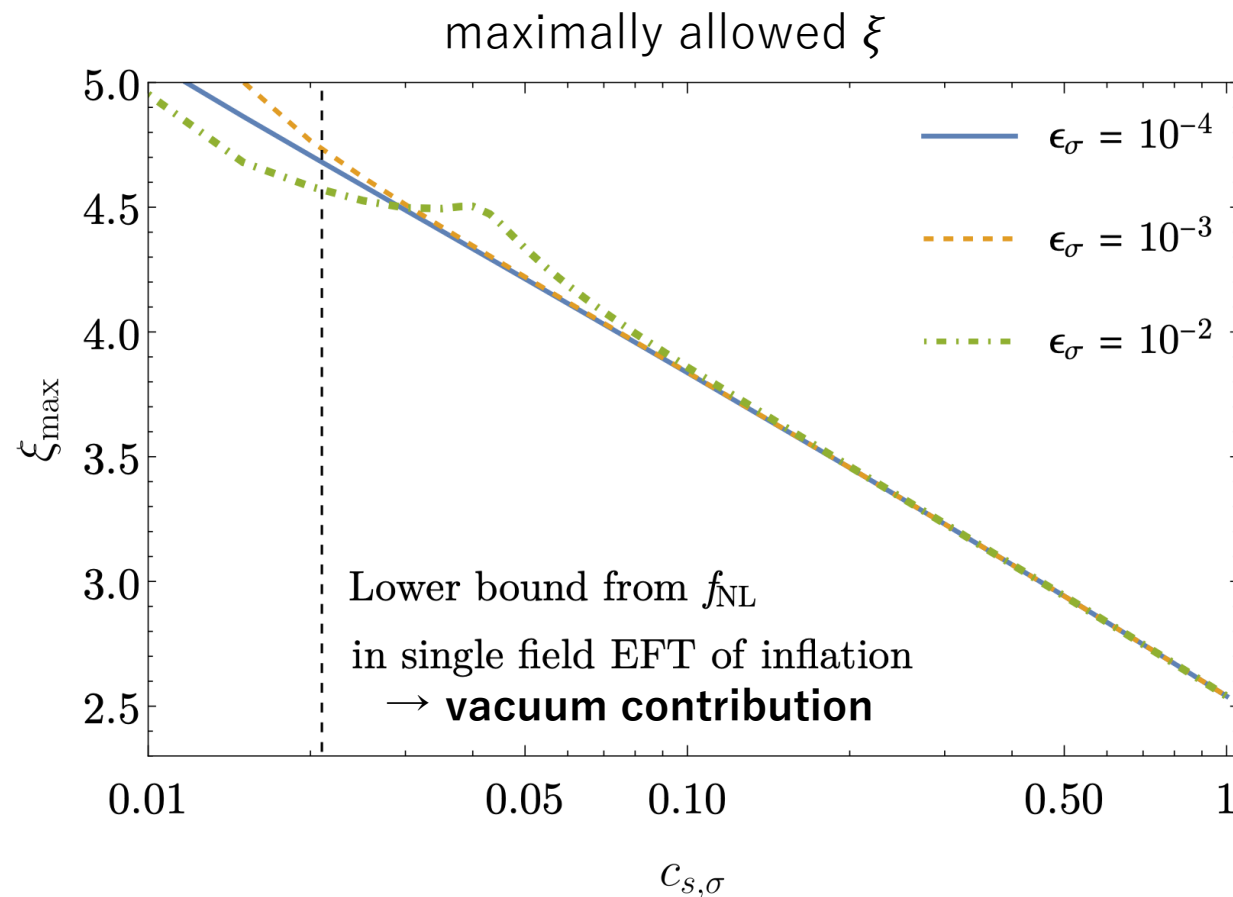
From the standard case, we get the suppression as $P_\zeta^{(1)} \propto c_s^4$ and $f_{NL} \propto c_s^6$!!

※※ Tensor sector not modified!

- Single field case (σ : inflaton, $\dot{\sigma}, \epsilon_\sigma, c_{s,\sigma} = \text{const.}$ assumed for simplicity)

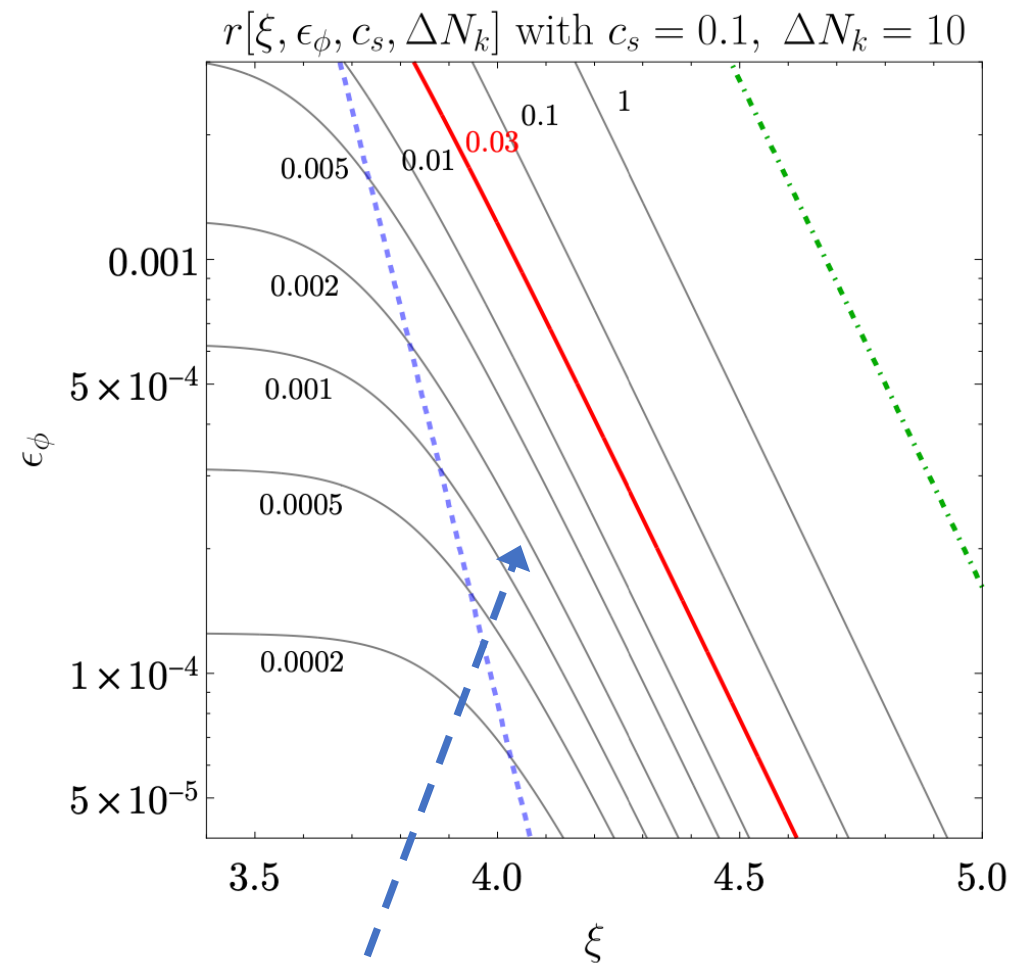
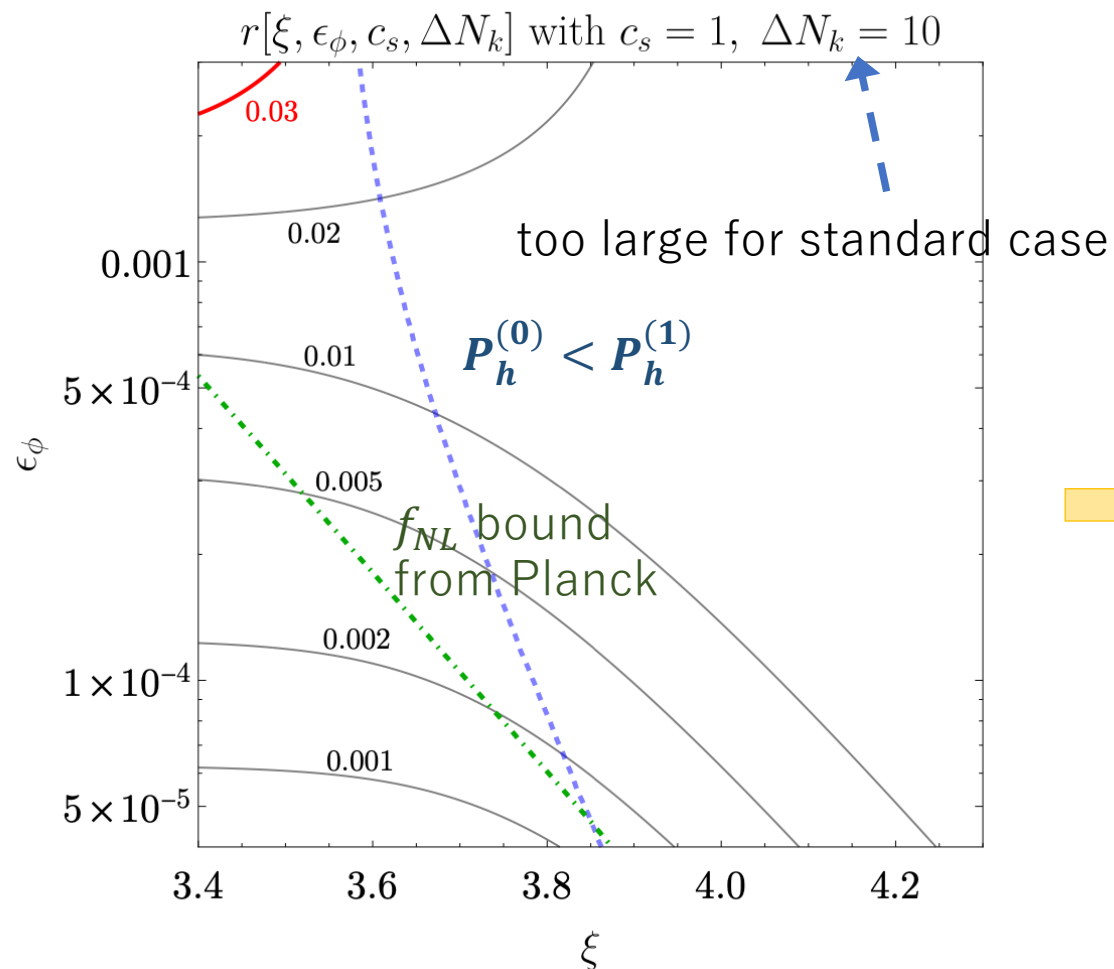


- Single field case (σ : inflaton, $\dot{\sigma}, \epsilon_\sigma, c_{s,\sigma} = \text{const.}$ assumed for simplicity)



exponential dependence on $\xi \rightarrow$ sourcing effect can be significantly large!

- two-field case (ϕ : inflaton, σ : spectator, $c_{s,\phi} = c_{s,\sigma} = c_s$)



The new window exists even for $\Delta N \sim 50 - 60$!!

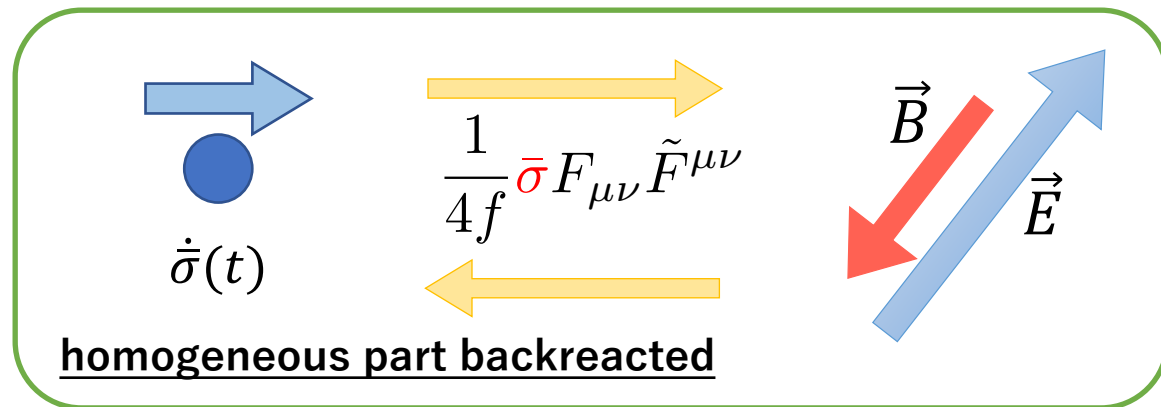
Outline

- Inflationary phenomenology with Chern-Simons term
- Production of $U(1)$ gauge field and perturbations
- Non-canonical case: large inertia of scalar modes
- Backreaction in non-canonical case...?
- Summary

- GWs at interferometer scales

$\delta\sigma$ loosely bounded on small scales $\rightarrow$ larger $\dot{\bar{\sigma}}(t)$ & subjected to the **backreaction**

- integro-differential system ($\bar{\sigma}(t) / A_+(t, k)$) (Cheng+ 2015, Notari 2016, Dall'Agata+ 2019, Domcke+ 2020)



polarized tensor pert. $h_{ij}^{(1)}$

scalar pert. $\delta\sigma^{(1)} \rightarrow$ PBHs...?

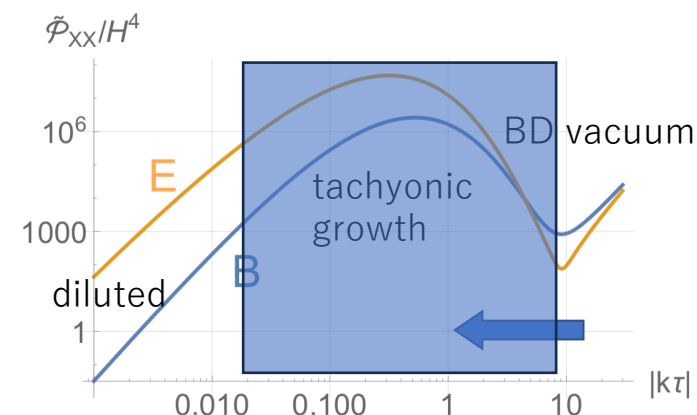
(Linde+ 2012, García-Bellido+ 2017)

$\rightarrow$ Mathematica code recently developed in García-Bellido+ 2023

$$\ddot{\bar{\sigma}} + 3H\dot{\bar{\sigma}} + \frac{\partial V}{\partial \sigma} = \frac{1}{f} \underline{\underline{\vec{E} \cdot \vec{B}}} \quad \leftarrow \text{adding relevant modes}$$

$$\langle \vec{E} \cdot \vec{B} \rangle_{\text{symm}} = -\frac{V_0^2}{8\pi^2 M_p^4} \frac{\tilde{H}}{e^{3N}} \int d\tilde{k} \tilde{k}^2 \sum_{\lambda} \lambda \frac{d}{dN} |\bar{A}_{\lambda}|^2$$

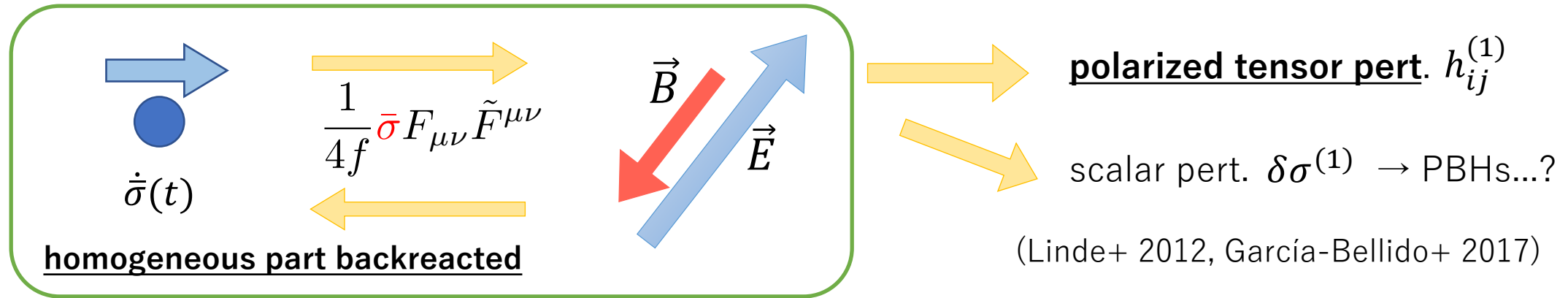
$\bar{\sigma}$ and EB spectrum with backreaction $\rightarrow h_{ij}^{(1)}$



- GWs at interferometer scales

$\delta\sigma$ loosely bounded on small scales $\rightarrow$ larger $\dot{\bar{\sigma}}(t)$ & subjected to the **backreaction**

- integro-differential system ($\bar{\sigma}(t) / A_+(t, k)$) (Cheng+ 2015, Notari 2016, Dall'Agata+ 2019, Domcke+ 2020)

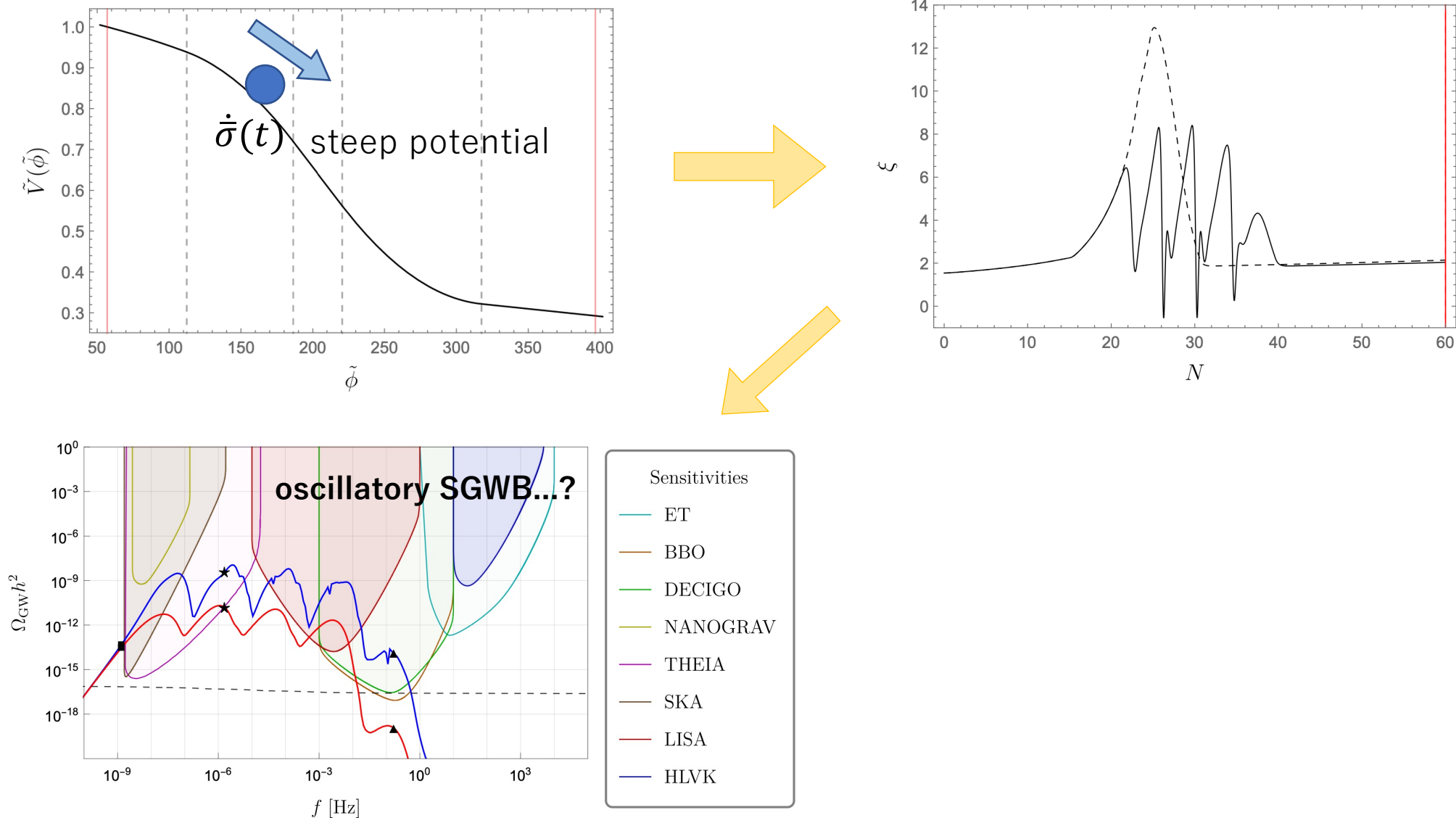


$\rightarrow$ Mathematica code recently developed in García-Bellido+ 2023

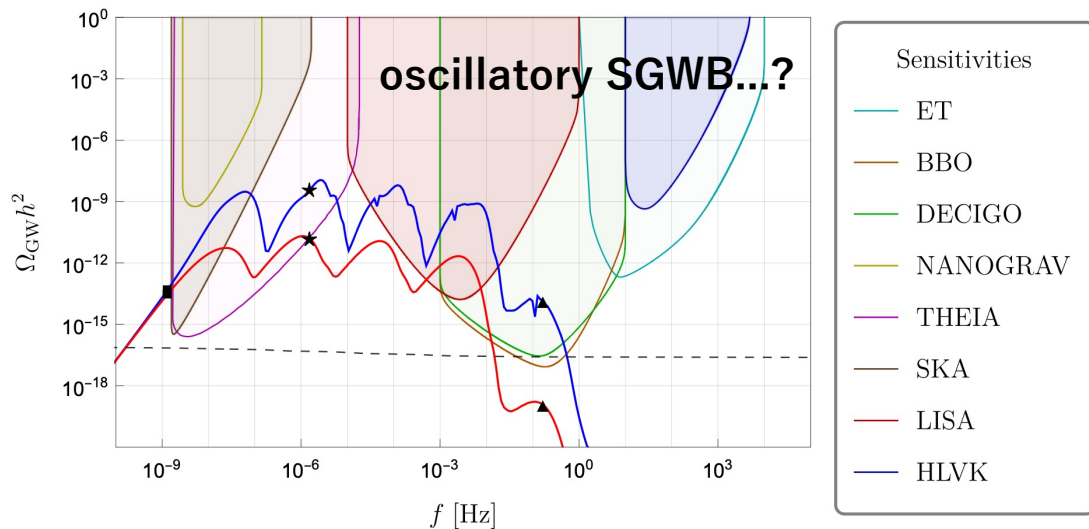
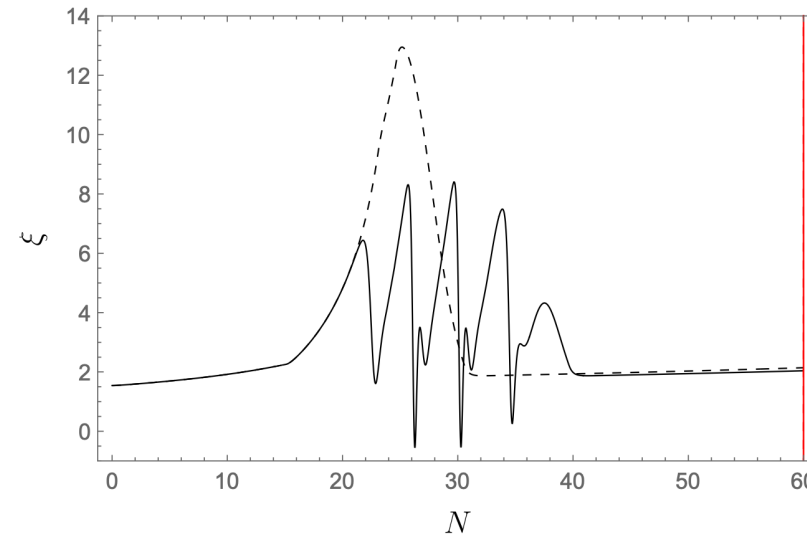
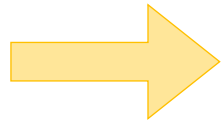
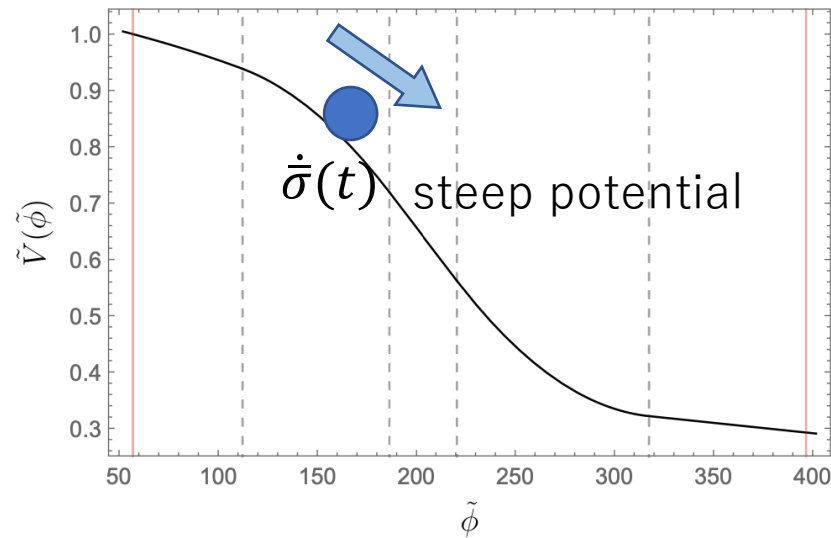
Other approaches:

- Gradient expansion (Sobol+ 2019, ...) $\rightarrow$ incorporating $\delta\sigma(t, \vec{x})$ in Domcke+ 2023
- Lattice simulation for $\sigma(t, \vec{x})$ (Caravano+ 2022, Figueroa+ 2023, Caravano & Peloso 2024)

- “First-step estimate” with homogeneous backreaction (García-Bellido+ 2023)



- “First-step estimate” with homogeneous backreaction (García-Bellido+ 2023)

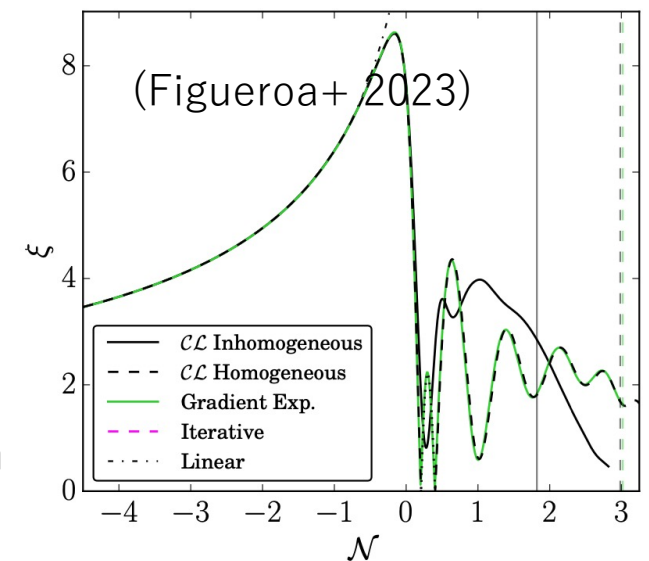


cf. lattice simulations

solid line for $\sigma(t, \vec{x})$

oscillation
→ smoothed out?

✱ at the end of inflation



- “Homogeneous backreaction” in non-canonical case (Very preliminary!!)

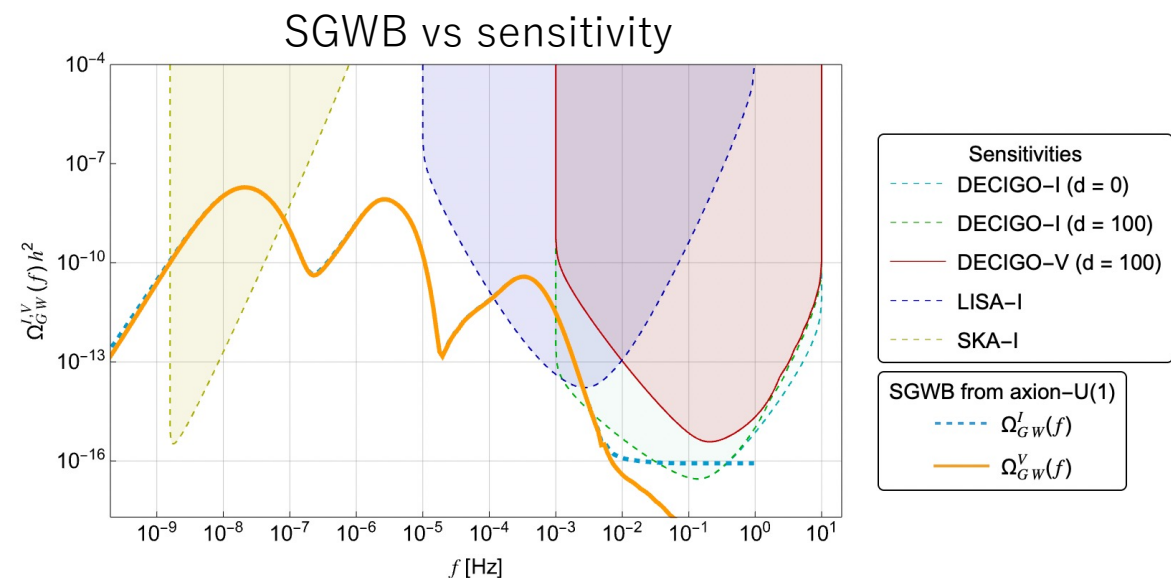
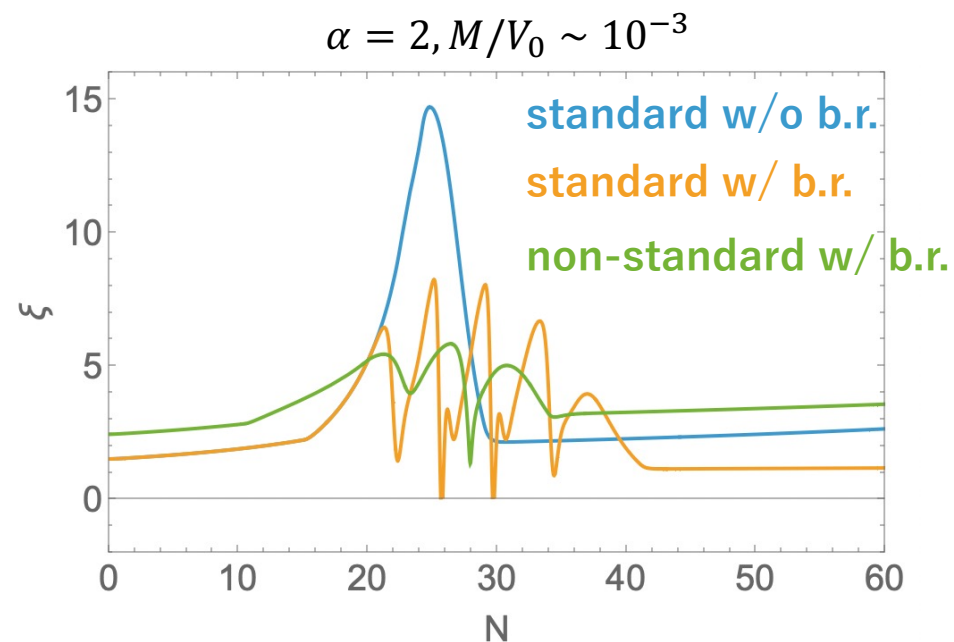
$$\underline{\underline{(K_{\sigma,1} + \dot{\sigma}^2 K_{\sigma,2}) \ddot{\sigma} + 3K_{\sigma,1} H \dot{\sigma} + \frac{\partial V}{\partial \sigma} = \frac{1}{f} \vec{E} \cdot \vec{B}}}$$

- What does the inertia bring?

➡ suppresses acceleration by $\partial V \rightarrow$ reducing ξ / also suppresses $\vec{E} \cdot \vec{B}$ effect on $\ddot{\sigma}$

- A toy example: $K_{\sigma}(Y) = Y(Y/M)^{\alpha-1}$ (Unnikrishnan 2008, Li & Liddle 2012, Lola+ 2020, ...)

$$\rightarrow K_{\sigma,1} + \dot{\sigma}^2 K_{\sigma,2} = (2\alpha - 1)K_{\sigma,1} \quad (c_{s,\sigma} = 1/(2\alpha - 1))$$



Outline

- Inflationary phenomenology with Chern-Simons term
- Production of $U(1)$ gauge field and perturbations
- Non-canonical case: large inertia of scalar modes
- Backreaction in non-canonical case...?
- Summary

Summary

- ✓ axion inflation + U(1) CS term $\rightarrow$ polarized tensor perturbation?
i) too efficient scalar sourcing and ii) backreaction
- ✓ Extension: non-canonical kinetic term for axion (and inflaton)
 - $\rightarrow$ Inverse decay contribution is suppressed by c_s !
 - $\rightarrow$ Sourced tensor becomes dominant at CMB while satisfying f_{NL} bound.
- ✓ Physics behind: large inertia of scalar
 - $\rightarrow$ generally applicable to other scenarios with “unwanted” scalar
 - For SU(2): Watanabe & Komatsu 2020, Dimastrogiovanni+ 2023, Murata & Kobayashi 2024...

June 24th, 2025

Inflationary phenomenology of a non-canonical axion with Chern-Simons interaction

@ Axions in Stockholm 2025



UNIVERSITÀ
DEGLI STUDI
DI PADOVA

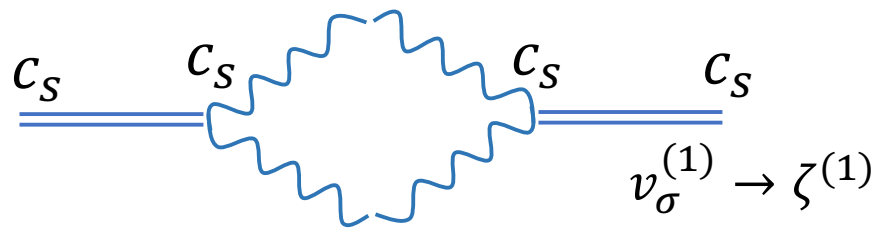


Jun'ya Kume (University of Padova)

Based on: arXiv:2501.02890 [astro-ph.CO]

with Marco Peloso, Nicola Bartolo

single field



$$\mathcal{P}_\zeta^{(1)}(k) \equiv \left[\mathcal{P}_\zeta^{(0)} \right]^2 e^{4\pi\xi} f_{2,\zeta} [\epsilon_\sigma, c_{s,\sigma}, \xi]$$

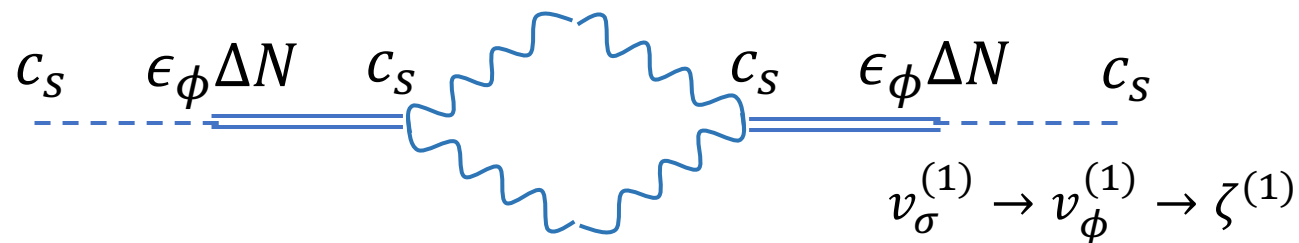
$c_{s,\sigma}^{-2}$ $\rightarrow$ $E \cdot B$ contribution $\propto c_{s,\sigma}^6$

$$f_{2,\zeta} [\epsilon_\sigma, c_{s,\sigma}, \xi] \simeq \frac{7.47 \times 10^{-5}}{\xi^6} c_{s,\sigma}^6 - \frac{1.92 \times 10^{-5}}{\xi^6} c_{s,\sigma}^4 \epsilon_\sigma + \frac{1.89 \times 10^{-6}}{\xi^6} c_{s,\sigma}^2 \epsilon_\sigma^2 \dots$$

$$F(\vec{k}_1, \vec{k}_2, \vec{k}_3) = \frac{\left[\mathcal{P}_\zeta^{(0)} \right]^3}{k_1^2 k_2^2 k_3^2} e^{6\pi\xi} f_{3,\zeta}$$

$E \cdot B$ contribution $\propto c_{s,\sigma}^9$

two-field



$$\mathcal{P}_\zeta^{(1)}(k) \equiv \left[\epsilon_\phi \mathcal{P}_\zeta^{(0)} \right]^2 e^{4\pi\xi} f_{2,\zeta} [c_s, \xi, \Delta N_k]$$

$$f_{2,\zeta} \simeq \frac{7.47 \times 10^{-5}}{\xi^6} c_s^6 (1 + c_s^2)^2 \Delta N_k^2 - \frac{1.92 \times 10^{-5}}{\xi^6} c_s^4 (1 + c_s^2) \Delta N_k \dots$$

$$F(\vec{k}_1, \vec{k}_2, \vec{k}_3) = \frac{\left[\epsilon_\phi \mathcal{P}_\zeta^{(0)} \right]^3}{k_1^2 k_2^2 k_3^2} e^{6\pi\xi} f_{3,\zeta}$$

tensor:

$$\mathcal{P}_\lambda^{(1)}(k) \equiv \frac{2}{\pi^2} \frac{H^4}{M_p^4} e^{4\pi\xi} f_{h,\lambda}(\xi) \quad f_{h,+}(\xi) \simeq \frac{4.3 \times 10^{-7}}{\xi^6}$$

- Analytic expression ex.) single field

$$\mathcal{P}_\zeta^{(1)}(k) = \left[\mathcal{P}_\zeta^{(0)} \right]^2 \frac{9\pi^3 \xi^2 e^{4\pi\xi}}{16} \int_1^\infty dx \int_0^1 dy \frac{(x^2 - 1)^2}{\sqrt{x^2 - y^2}} \mathcal{I}_\zeta^2 \left[\epsilon_\sigma, c_{s,\sigma}, \xi, \sqrt{\frac{x+y}{2}}, \sqrt{\frac{x-y}{2}} \right]$$

$$\begin{aligned} \mathcal{I}_\zeta \left[\epsilon_\sigma, c_{s,\sigma}, \xi, \sqrt{\tilde{p}}, \sqrt{\tilde{q}} \right] &\equiv c_{s,\sigma}^3 \left[\tilde{p}^{1/2} + \tilde{q}^{1/2} \right] \mathcal{T}_\zeta^{(E \cdot B)} \left[\xi, \sqrt{\tilde{p}} + \sqrt{\tilde{q}} \right] \\ &+ \epsilon_\sigma c_{s,\sigma} \left[c_{s,\sigma}^2 - (\tilde{p} - \tilde{q})^2 \right] \left\{ \mathcal{T}_\zeta^{(E^2)} \left[\xi, \sqrt{\tilde{p}} + \sqrt{\tilde{q}} \right] + \tilde{p}^{1/2} \tilde{q}^{1/2} \mathcal{T}_\zeta^{(B^2)} \left[\xi, \sqrt{\tilde{p}} + \sqrt{\tilde{q}} \right] \right\} \end{aligned}$$

$$\begin{aligned} \mathcal{T}_\zeta^{(E^2)} [\xi, Q] &\equiv \frac{1}{3\pi^{3/2} \xi^{1/2}} \int_0^\infty dx \frac{-c_s x \cos(c_s x) + \sin(c_s x)}{c_s^3} x^{-1/2} \exp \left[-2\sqrt{2\xi x} Q \right] \\ &\simeq \frac{1}{3\pi^{3/2} \xi^{1/2}} \int_0^\infty dx \frac{x^{5/2}}{3} \exp \left[-2\sqrt{2\xi x} Q \right] = \frac{5}{32\sqrt{2}\pi^{3/2} \xi^4 Q^7}, \end{aligned}$$

$$\begin{aligned} \mathcal{T}_\zeta^{(E \cdot B)} [\xi, Q] &\equiv \frac{\sqrt{2}}{3\pi^{3/2}} \int_0^\infty dx \frac{-c_s x \cos(c_s x) + \sin(c_s x)}{c_s^3} \exp \left[-2\sqrt{2\xi x} Q \right] \\ &\simeq \frac{\sqrt{2}}{3\pi^{3/2}} \int_0^\infty dx \frac{x^3}{3} \exp \left[-2\sqrt{2\xi x} Q \right] = \frac{35}{64\sqrt{2}\pi^{3/2} \xi^4 Q^8}, \end{aligned}$$

← c_s does not alter scale
→ amplitude suppression