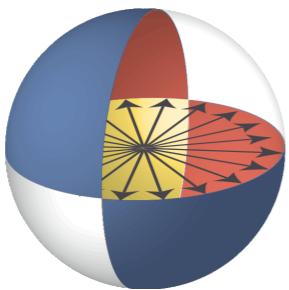


# Time-independence does not limit information flow

Alexey V. Gorshkov

Joint Quantum Institute (JQI)  
Joint Center for Quantum Information and Computer Science (QuICS)  
NIST and University of Maryland

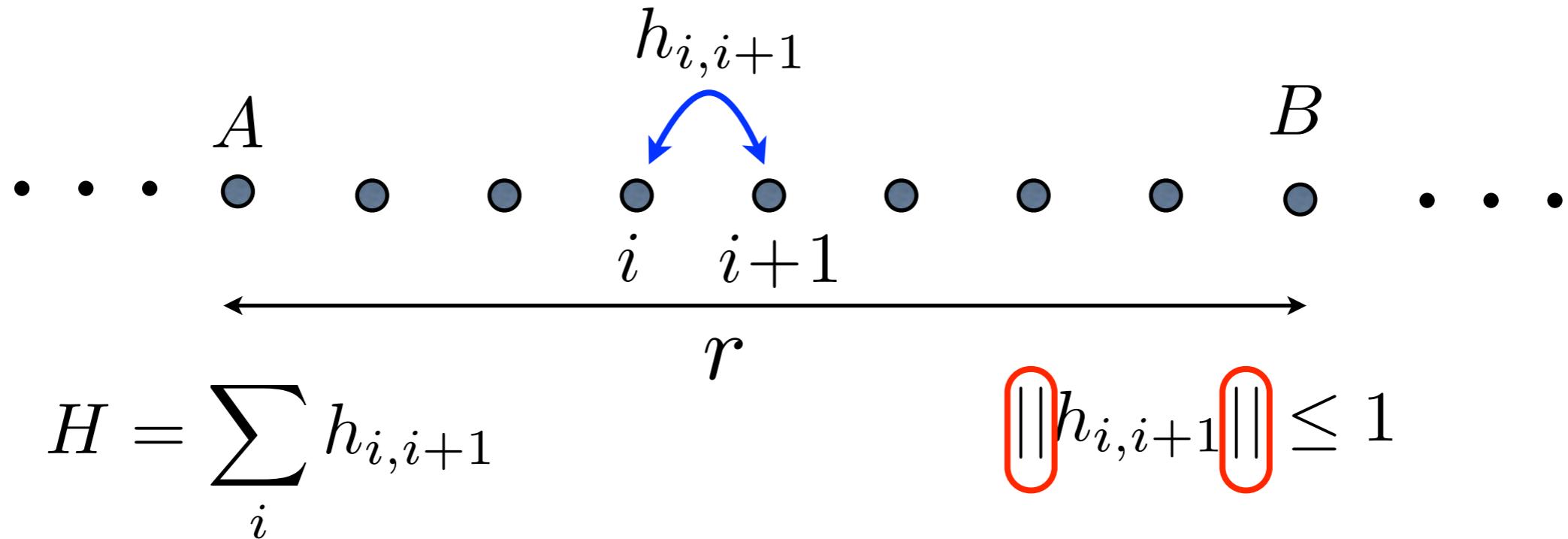


JOINT CENTER FOR  
QUANTUM INFORMATION  
AND COMPUTER SCIENCE



“Long-Range Interactions and Dynamics in Complex Quantum Systems”  
NORDITA, Stockholm, Sweden  
July 24, 2025

# Lieb-Robinson bounds

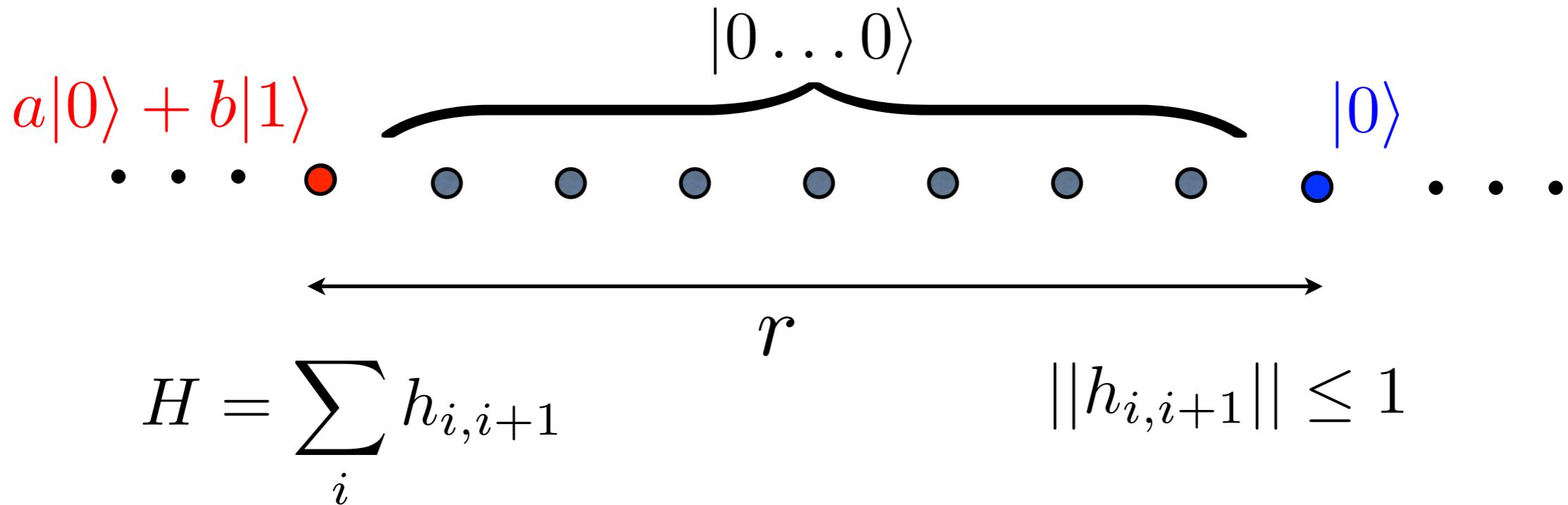


- arbitrary time dependence allowed
- arbitrary time-dependent on-site terms allowed
- $A(t) =$  Heisenberg evolution under  $H$
- what is the shortest time  $t$  to achieve  $\|[A(t), B]\| \sim 1$ ?
- answer:  $t \gtrsim r$
- bounds many things, including quantum state transfer time

E. Lieb & D. Robinson, 1972

Review: Chen, Lucas, Yin, Rep. Prog. Phys. 86, 116001 (2023)

# Lieb-Robinson bounds

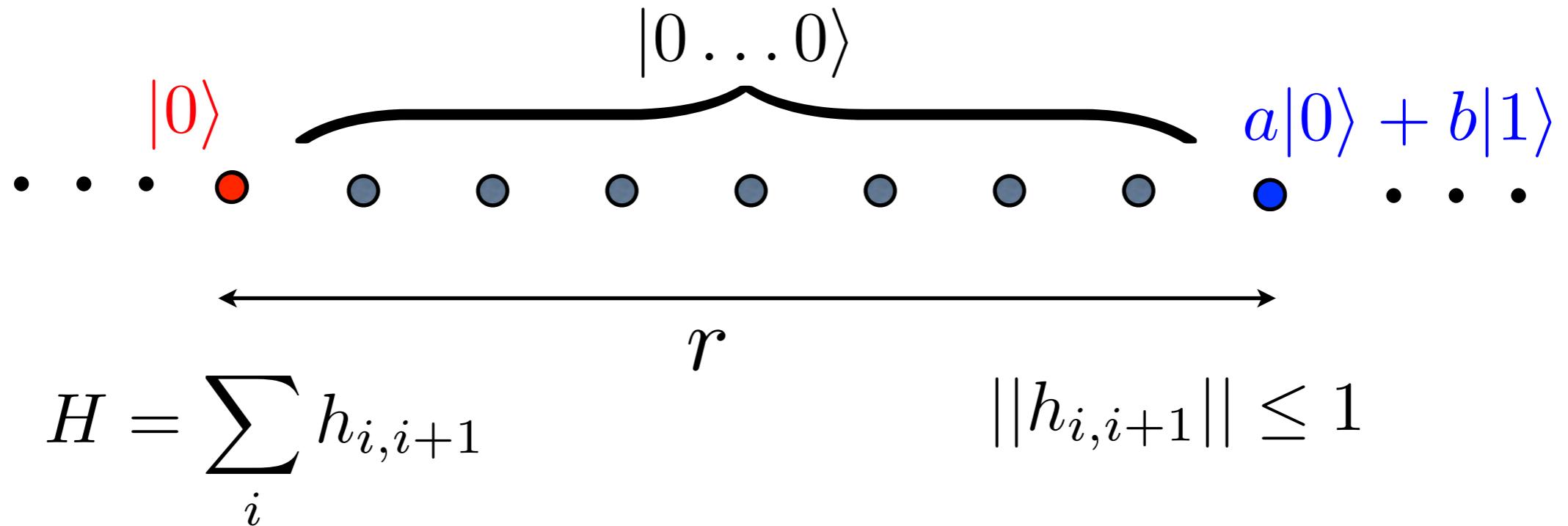


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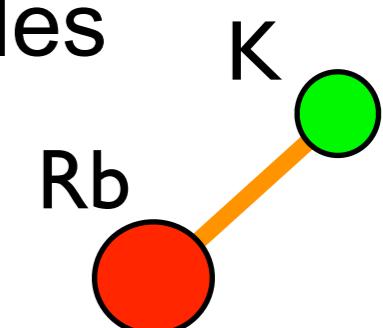
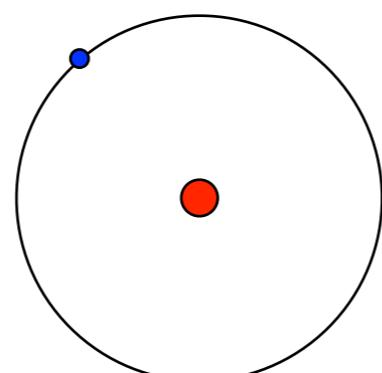
# Long-range interactions

AMO and other synthetic quantum systems often exhibit

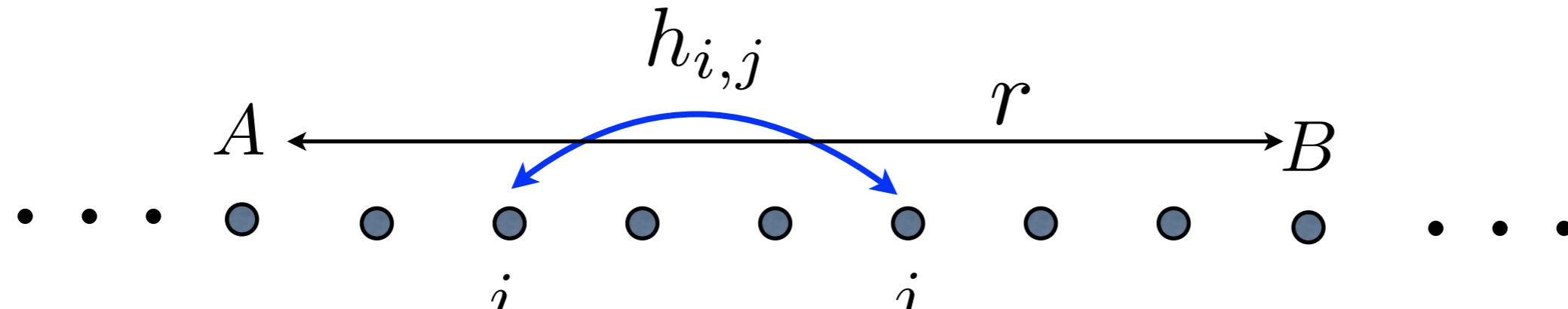
- long-range interactions = decaying with distance slower than exponential (e.g. decaying as  $1/r^\alpha$ )
- how quickly can quantum information propagate in these systems?

## Examples:

- $1/r^3$ : Rydberg or magnetic atoms, excitons, NV centers, polar molecules
- $1/r^6$ : Rydberg atoms
- $\sim 1/r^\alpha$  & other forms: ion crystals, atoms in multimode cavities or along waveguides



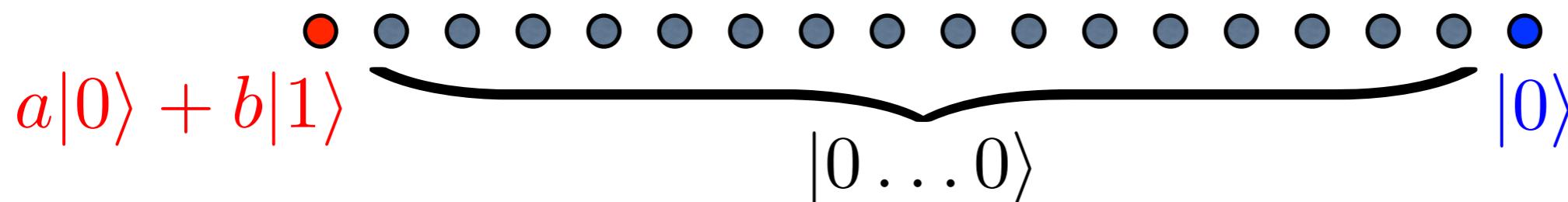
# Lieb-Robinson-type bounds for $r^{-\alpha}$ interactions



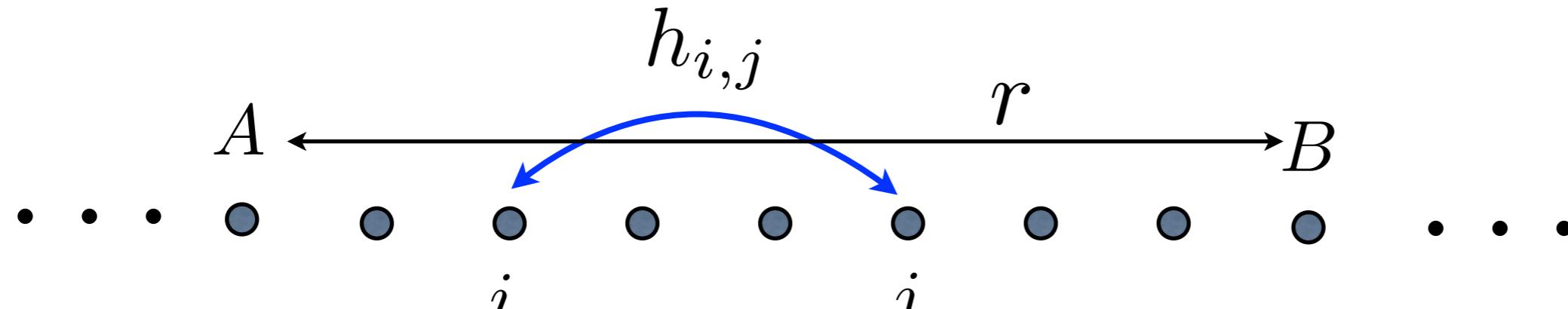
$$H = \sum_{i < j} h_{i,j}$$

$$\|h_{i,j}\| \leq \frac{1}{|i-j|^\alpha}$$

- arbitrary time dependence allowed
- arbitrary time-dependent on-site terms allowed
- consider all  $\alpha \geq 0$
- what is the shortest time  $t$  to achieve  $\|[A(t), B]\| \sim 1$ ?  
= shortest time to send quantum information over distance  $r$  in the sense of quantum state transfer?



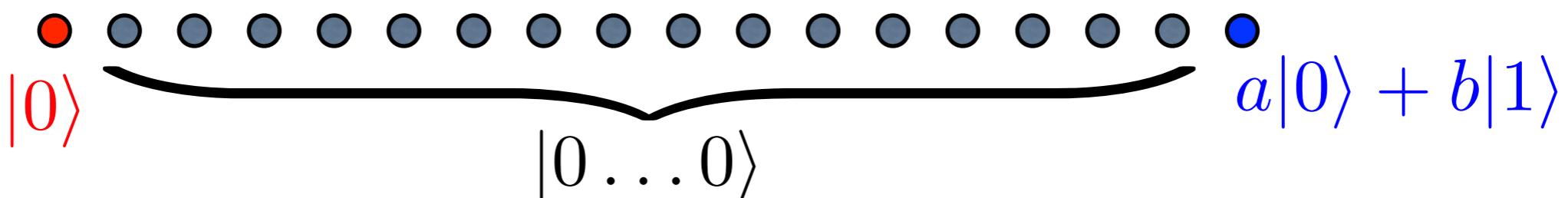
# Lieb-Robinson-type bounds for $r^{-\alpha}$ interactions



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# Lieb-Robinson-type bounds for $r^{-\alpha}$ interactions

~ “shortest time  $t$  to send quantum info over distance  $r$  ”

$d$  = dimension

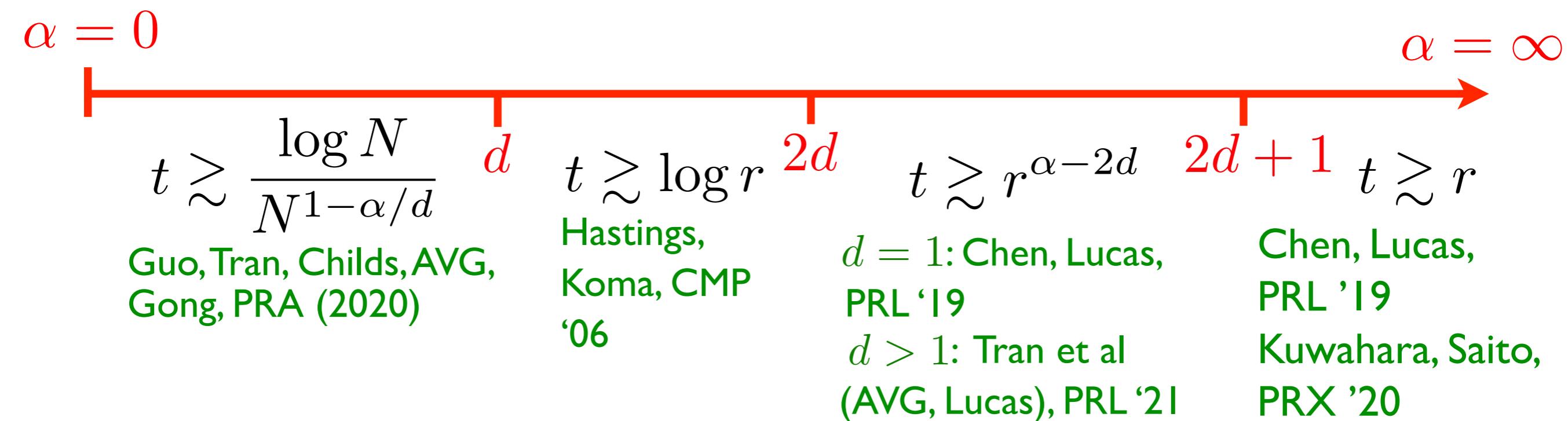


# Lieb-Robinson-type bounds for $r^{-\alpha}$ interactions

~ “shortest time  $t$  to send quantum info over distance  $r$ ”

$d$  = dimension

$N$  = total number of sites  
(formulas shown for  $N \sim r^d$ )



# Fastest known protocols

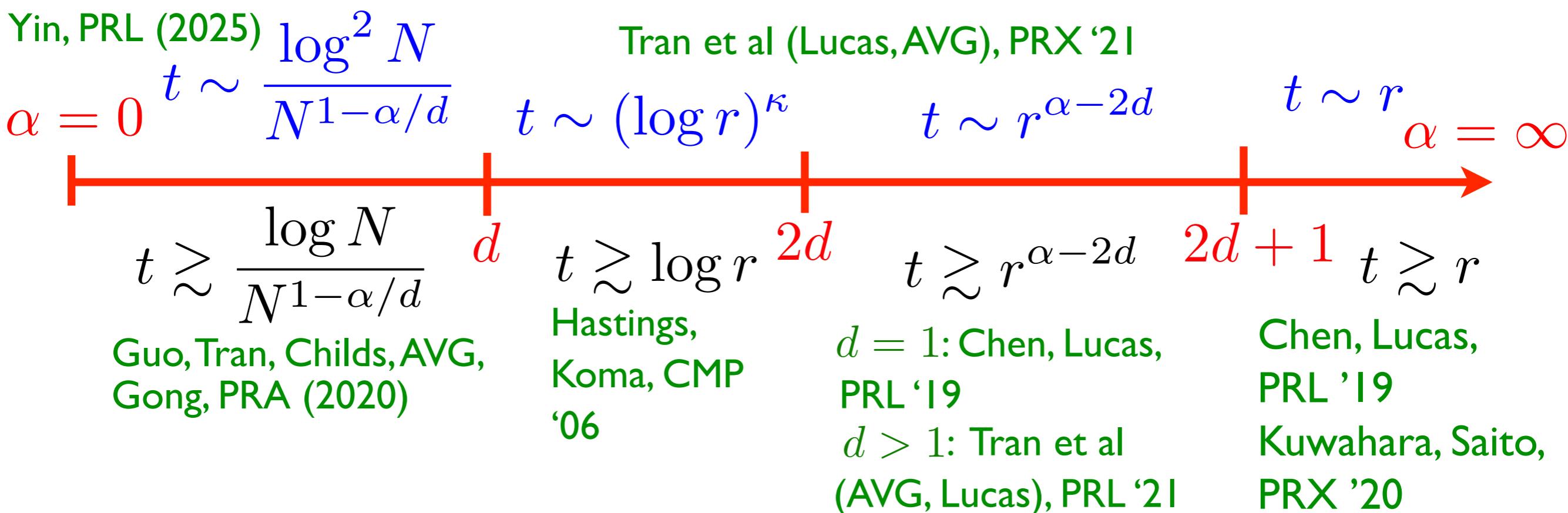
Shortest time  $t$  to send quantum info over distance  $r$

# $1/r^\alpha$ interactions in $d$ dimensions

- fastest protocols use time-dependent Hamiltonians
  - can we achieve the same with a time-independent Hamiltonian?
  - yes\*, i.e. time-independence does not limit information flow

\*need number of local ancilla qubits for each data qubit  
polylogarithmic in the number of data qubits

Mooney, Yuan, Ehrenberg, Baldwin, AVG, Childs, arXiv:2505.18254



# Fastest known protocols

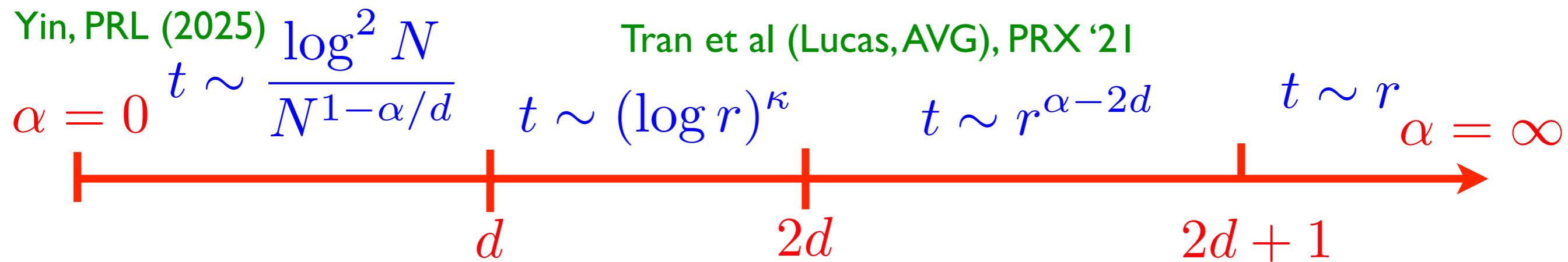
Shortest time  $t$  to send quantum info over distance  $r$

$1/r^\alpha$  interactions in  $d$  dimensions

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- approach: “staticize” time-dependent protocols using a clock construction

# Staticizing time-independent Hamiltonians

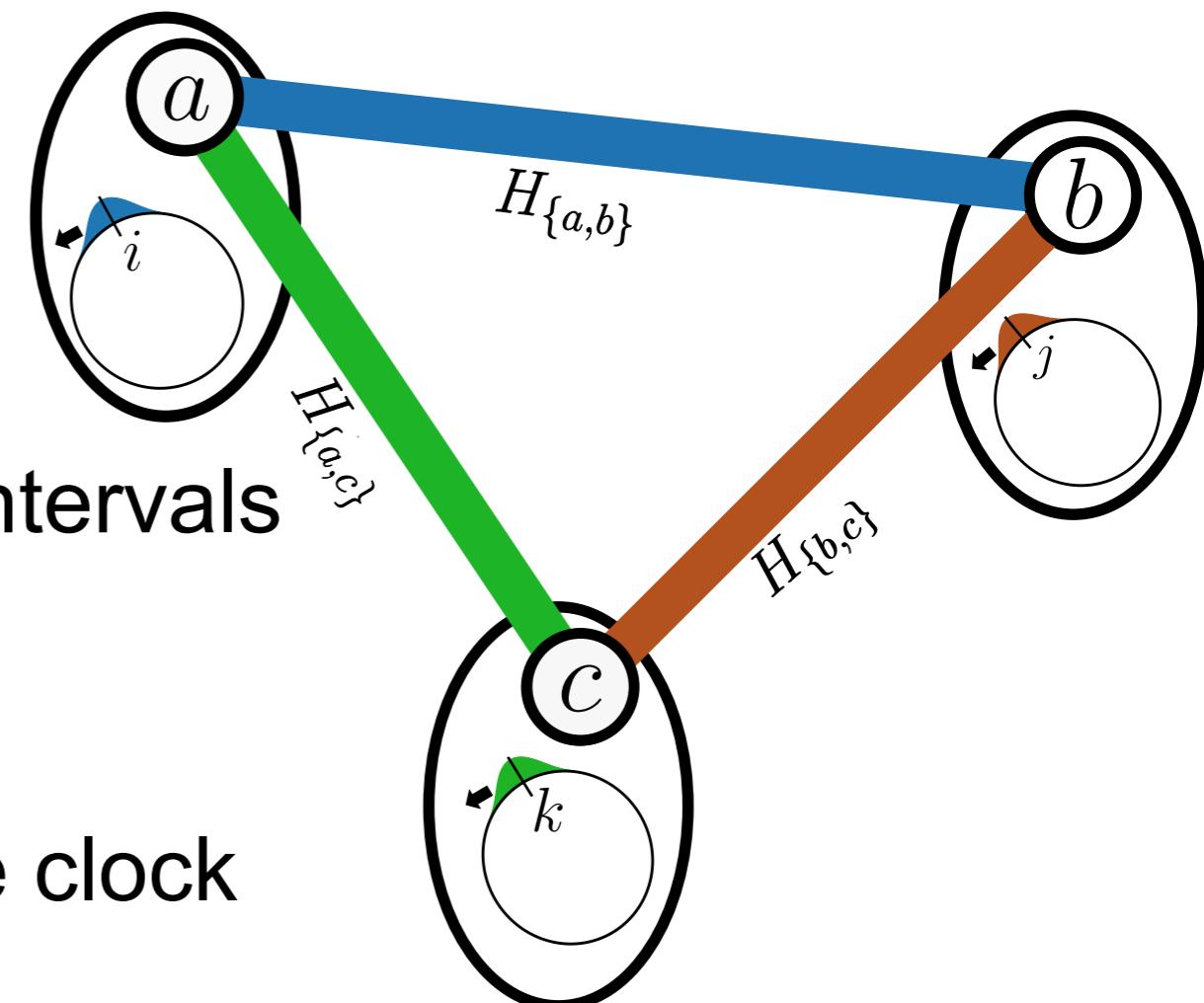
- Watkins, Wiebe, Roggero, Lee, arXiv:2203.11353: given a time-dependent Hamiltonian, output an equivalent (up to small controllable error) time-independent Hamiltonian driven by a global clock
- to preserve locality, we replace one global clock with many local clocks (one per site)

# Staticizing time-independent Hamiltonians

3-qubit example of our construction:

$$H(t) = H_{\{a,b\}}(t) + H_{\{b,c\}}(t) + H_{\{a,c\}}(t)$$

- for each edge  $e$ , we arbitrarily choose one of the vertices in  $e$  (call it  $\rho(e)$ ) to control the interaction  $H_e(t)$
- divide total time  $T$  into  $N_c$  small intervals of duration  $\delta = T/N_c$
- each clock has  $N_c$  states  $|k\rangle$
- clock Hamiltonian  $\Delta$  advances the clock on each site:  $e^{-i\Delta\delta}|k\rangle = |k+1\rangle$



$$\overline{H} = \Delta + \sum_k \sum_e H_e(k\delta) \otimes (|k\rangle\langle k|)_{\rho(e)}$$

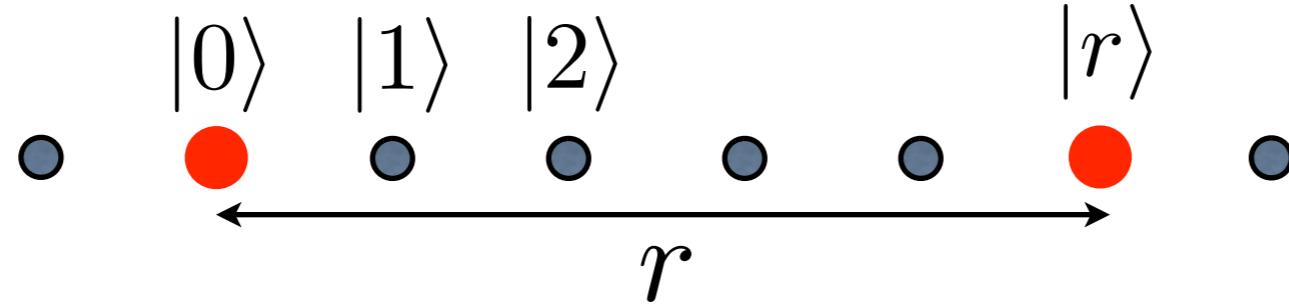
# Summary

- time-independence does not limit information flow, provided we allow for a polylogarithmic number of ancilla qubits per data qubit

# Outlook

- our staticization construction applies to any piecewise-continuous Hamiltonian, including circuit-based quantum algorithms, quantum annealing protocols, entangled-state preparation (e.g. for sensing)
  - would be interesting to investigate the specifics
- in some scenarios (architecture + application), it can be easier to implement Hamiltonian dynamics without time-dependent control
- our protocols incur error (which can be made arbitrarily small), but can we find a protocol that achieves perfect state transfer?
- can we reduce the local ancilla account to a constant or even to zero?
- can get rid of ancillas in the restricted setting of free-particle Hamiltonians!

# Free-particle bounds and protocols



$$H = \sum_{i < j} h_{ij}(t) |i\rangle\langle j| + h.c. + \sum_i \mu_i(t) |i\rangle\langle i| \quad |h_{ij}| \leq \frac{1}{|i - j|^\alpha}$$

- how long does it take to evolve from  $|0\rangle$  to  $|r\rangle$ ?

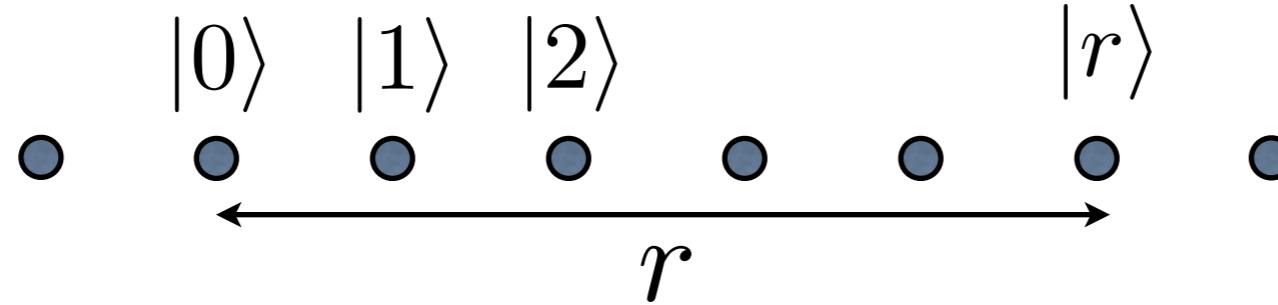
Equivalent to

$$H = \sum_{i < j} h_{ij}(t) c_i^\dagger c_j + h.c. + \sum_i \mu_i(t) c_i^\dagger c_i$$

$c_i^\dagger$  = bosonic or fermionic creation operators

- what is the shortest time  $t$  to achieve  $c_0^\dagger(t) = c_r^\dagger(0)$  ?

# Free-particle bounds and protocols



$$H = \sum_{i < j} h_{ij}(t) |i\rangle\langle j| + h.c. + \sum_i \mu_i(t) |i\rangle\langle i| \quad |h_{ij}| \leq \frac{1}{|i - j|^\alpha}$$

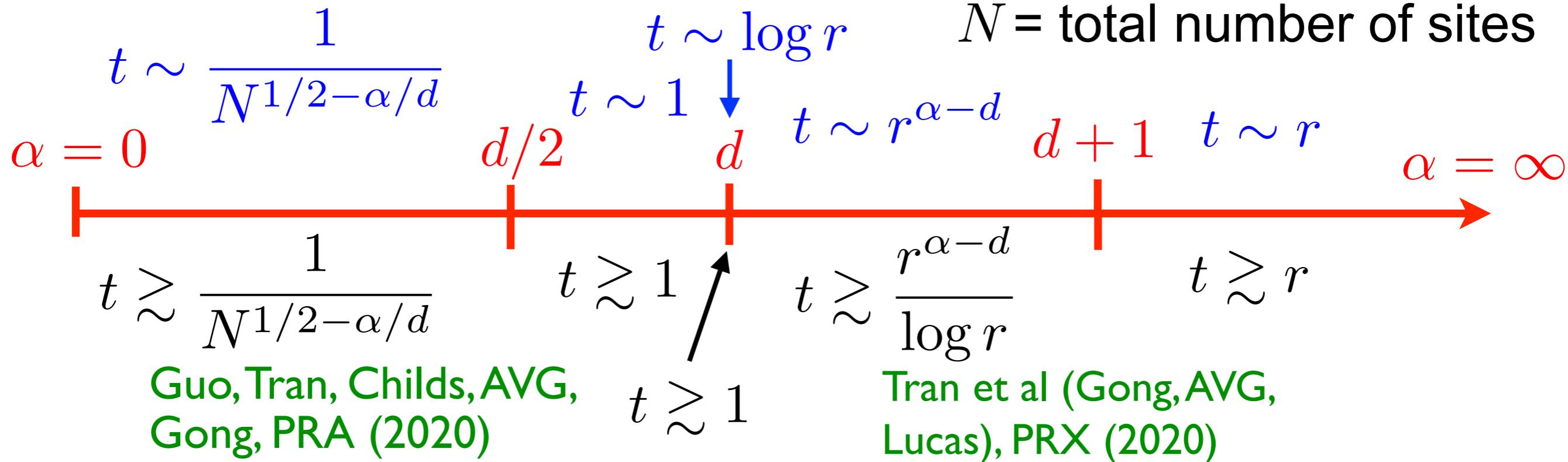
Slower than with

- how long does it take to evolve from  $|0\rangle$  to  $|r\rangle$ ? interactions.
- can we achieve the same with a time-independent Hamiltonian?

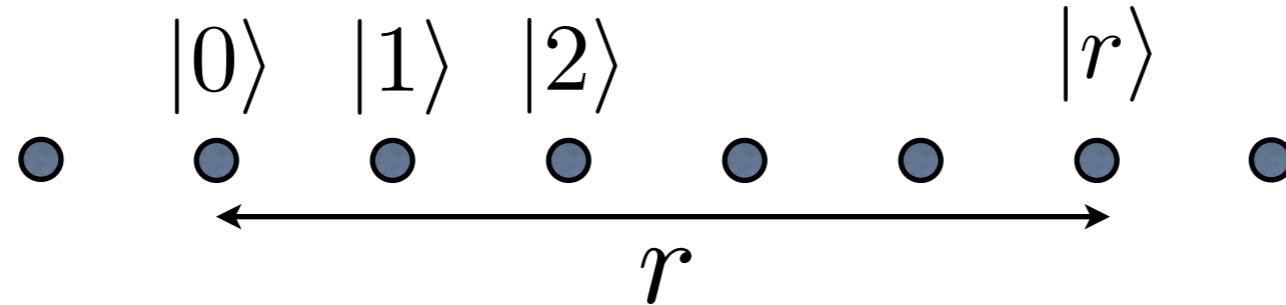
Guo, Tran, Childs, AVG,  
Gong, PRA (2020)

Tran et al (Gong, AVG, Lucas),  
PRX (2020)

Yes!



# Free-particle bounds and protocols



$$H = \sum_{i < j} h_{ij}(t) |i\rangle\langle j| + h.c. + \sum_i \mu_i(t) |i\rangle\langle i| \quad |h_{ij}| \leq \frac{1}{|i - j|^\alpha}$$

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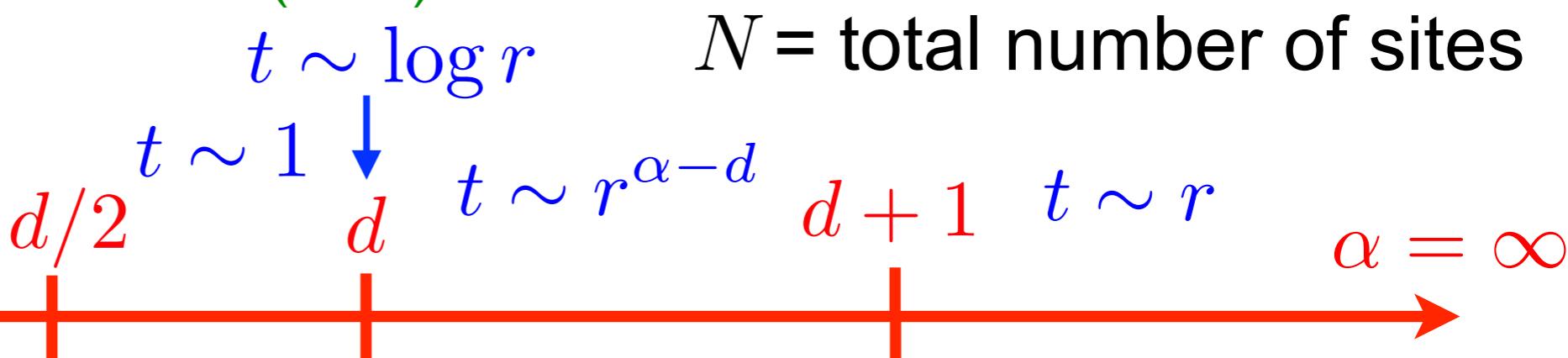
Guo, Tran, Childs, AVG,  
Gong, PRA (2020)

$$t \sim \frac{1}{N^{1/2-\alpha/d}}$$

$\alpha = 0$

Tran et al (Gong, AVG, Lucas),  
PRX (2020)

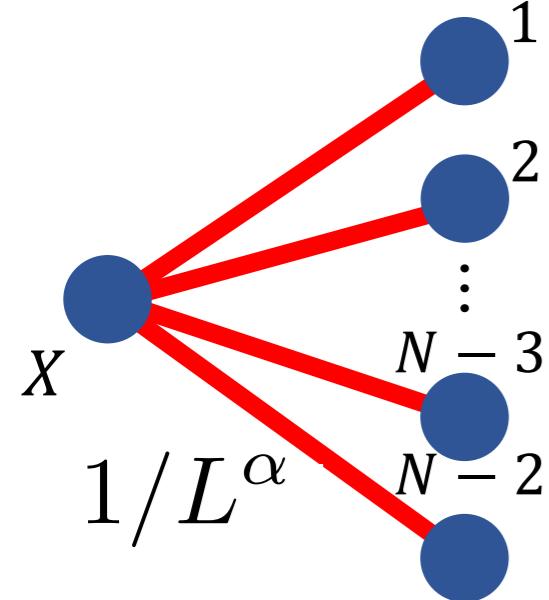
Yes!



Related prior work: Avellino, Fisher, Bose, PRA (2006); Gualdi, Kostak, Marzoli, Tombesi, PRA (2008); Hermes, Apollaro, Paganelli, Macri, PRA (2020); Lewis, Banchi, Teoh, Islam, Bose, Quantum Sci. Technol. (2023).

# Time-dependent protocol for $\alpha < d/2$

- $N \sim L^d$  sites on a d-dimensional cubic lattice of linear size  $L$
- interaction strength upper bounded by  $1/r^\alpha$
- want to evolve from  $|X\rangle$  to  $|Y\rangle$



$N^{1/2-\alpha/d}$

$|X\rangle$        $|\text{col}\rangle$

$|Y\rangle$

$$H = \frac{1}{L^\alpha} |X\rangle \sum_{i=1}^{N-2} \langle i| + h.c.$$

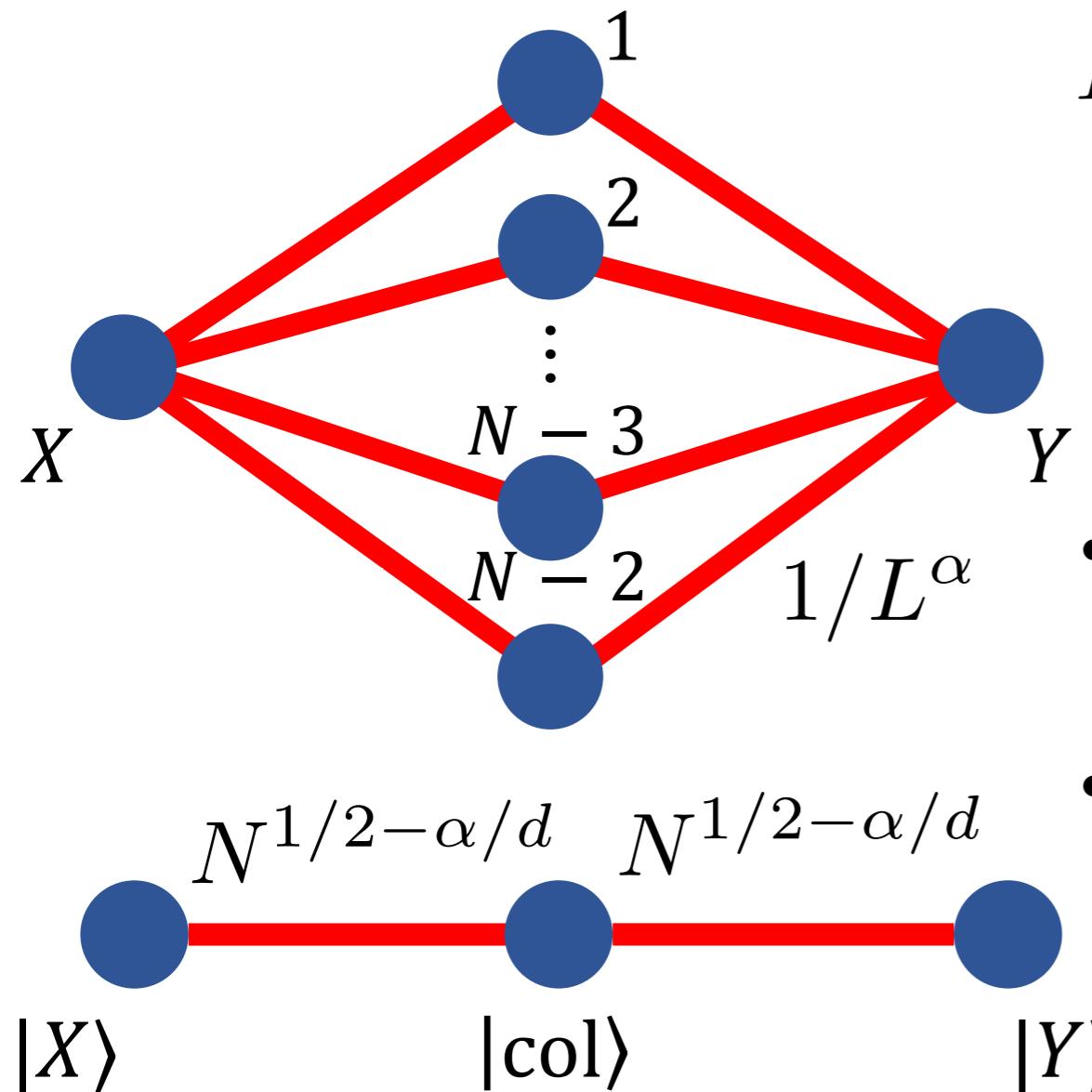
$$\sim \frac{\sqrt{N}}{L^\alpha} |X\rangle \langle \text{col}| + h.c.$$

$$|\text{col}\rangle = \frac{1}{\sqrt{N-2}} \sum_{i=1}^{N-2} |i\rangle$$

- takes time  $\sim 1/N^{1/2-\alpha/d}$  to hop from  $|X\rangle$  to  $|\text{col}\rangle$
- then hop from  $|\text{col}\rangle$  to  $|Y\rangle$

# Staticize the protocol for $\alpha < d/2$

- $N \sim L^d$  sites on a d-dimensional cubic lattice of linear size  $L$
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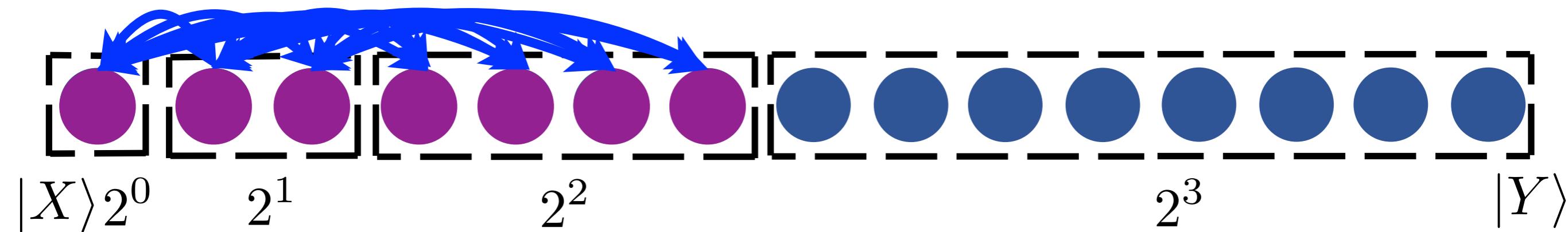
$$H = \frac{1}{L^\alpha} (|X\rangle + |Y\rangle) \sum_{i=1}^{N-2} \langle i| + h.c.$$

$$\sim \frac{\sqrt{N}}{L^\alpha} (|X\rangle + |Y\rangle) \langle \text{col} | + h.c.$$

- takes time  $\sim 1/N^{1/2-\alpha/d}$  to do a  $2\pi$  pulse from  $|X\rangle + |Y\rangle$  via  $|\text{col}\rangle$
- $|X\rangle \propto (|X\rangle + |Y\rangle) + (|X\rangle - |Y\rangle)$   
 $\rightarrow -(|X\rangle + |Y\rangle) + (|X\rangle - |Y\rangle)$   
 $\propto |Y\rangle$

# Time-dependent protocol for $d/2 < \alpha < d + 1$

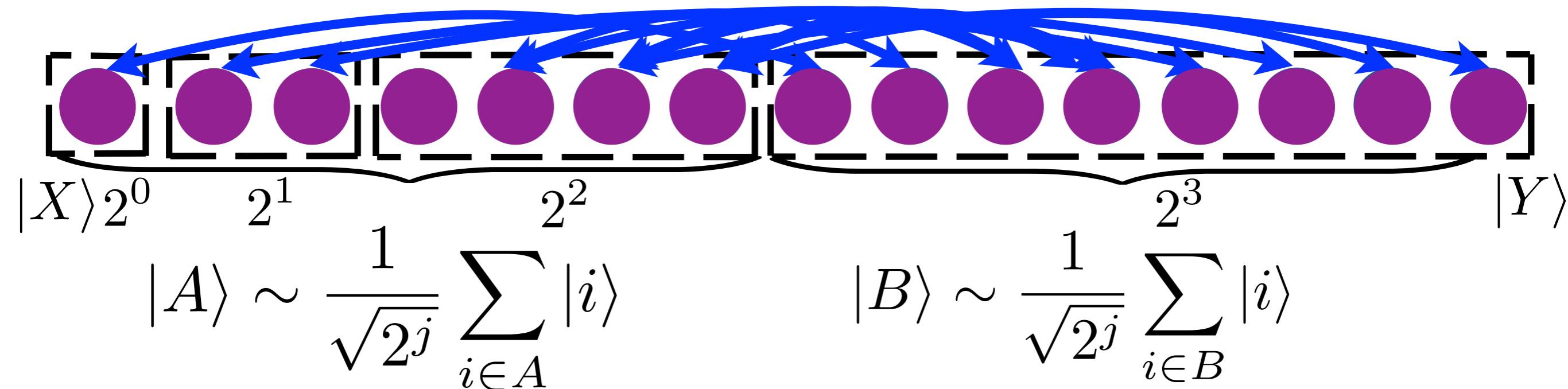
- $N \sim L^d$  sites on a d-dimensional cubic lattice of linear size  $L$
- interaction strength upper bounded by  $1/r^\alpha$
- want to evolve from  $|X\rangle$  to  $|Y\rangle$ 
  - show for  $d=1$



- spread to larger uniform superpositions, then reverse to  $|Y\rangle$

# Time-dependent protocol for $d/2 < \alpha < d + 1$

- $N \sim L^d$  sites on a d-dimensional cubic lattice of linear size  $L$
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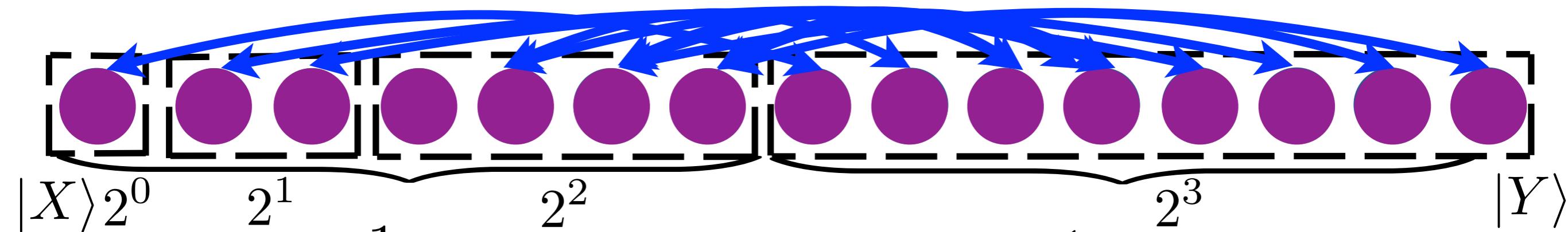


- spread to larger uniform superpositions, then reverse to  $|Y\rangle$
- time to spread to additional  $2^j$  sites  $\sim 2^{j(\alpha-1)}$

$$H \sim \frac{1}{(2^j)^\alpha} \sum_{i \in A, k \in B} |i\rangle \langle k| + h.c. \sim \frac{2^j}{(2^j)^\alpha} |A\rangle \langle B| + h.c.$$

# Time-dependent protocol for $d/2 < \alpha < d + 1$

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- interaction strength upper bounded by  $1/r^\alpha$
- want to evolve from  $|X\rangle$  to  $|Y\rangle$ 
  - show for  $d=1$

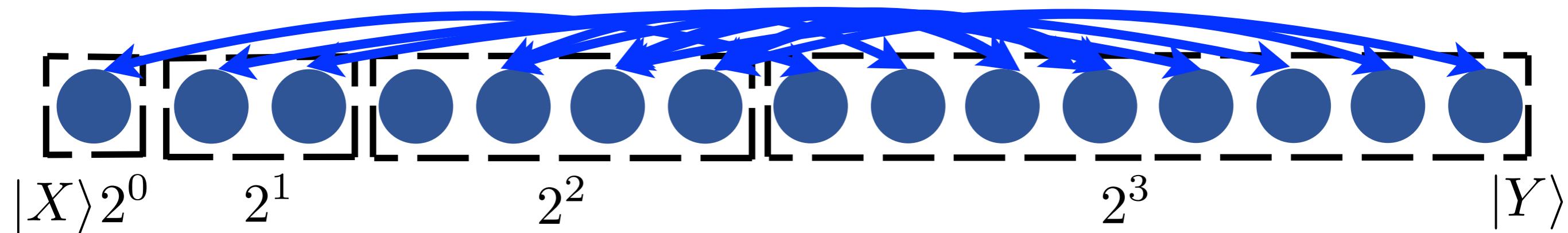


$$|A\rangle \sim \frac{1}{\sqrt{2^j}} \sum_{i \in A} |i\rangle$$

$$|B\rangle \sim \frac{1}{\sqrt{2^j}} \sum_{i \in B} |i\rangle$$

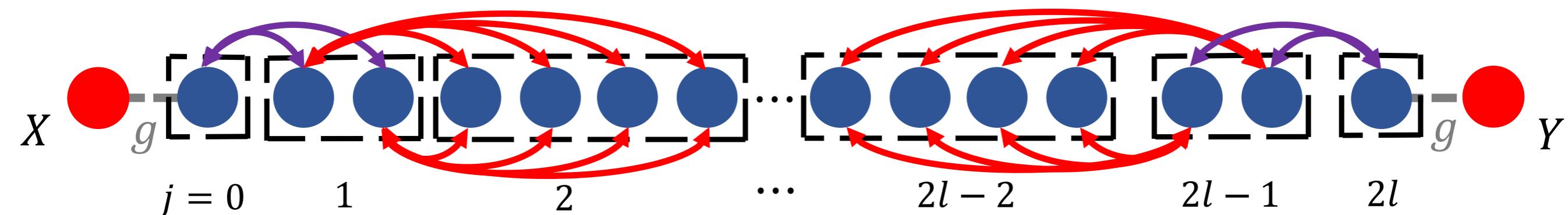
- spread to larger uniform superpositions, then reverse to  $|Y\rangle$
- time to spread to additional  $2^j$  sites  $\sim 2^{j(\alpha-1)}$ 
  - $\sim 1 \quad \alpha < 1$
  - $\sim \log L \quad \alpha = 1$
  - $\sim L^{\alpha-1} \quad \alpha > 1$
- time to spread to full lattice  $\sim \sum_{j=1} (2^{\alpha-1})^j$

# Staticize the protocol for $d/2 < \alpha < d + 1$

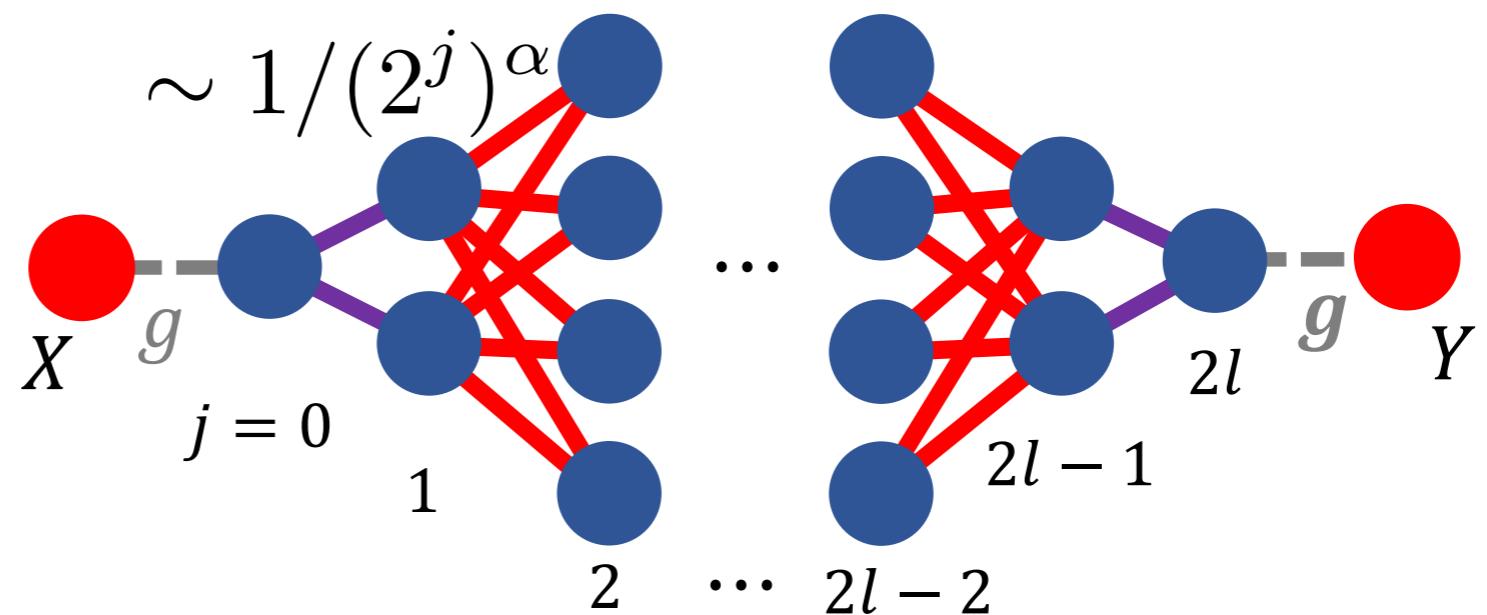


- turning simultaneously all the interactions needed to spread from  $|X\rangle$  and to concentrate onto  $|Y\rangle$  doesn't work

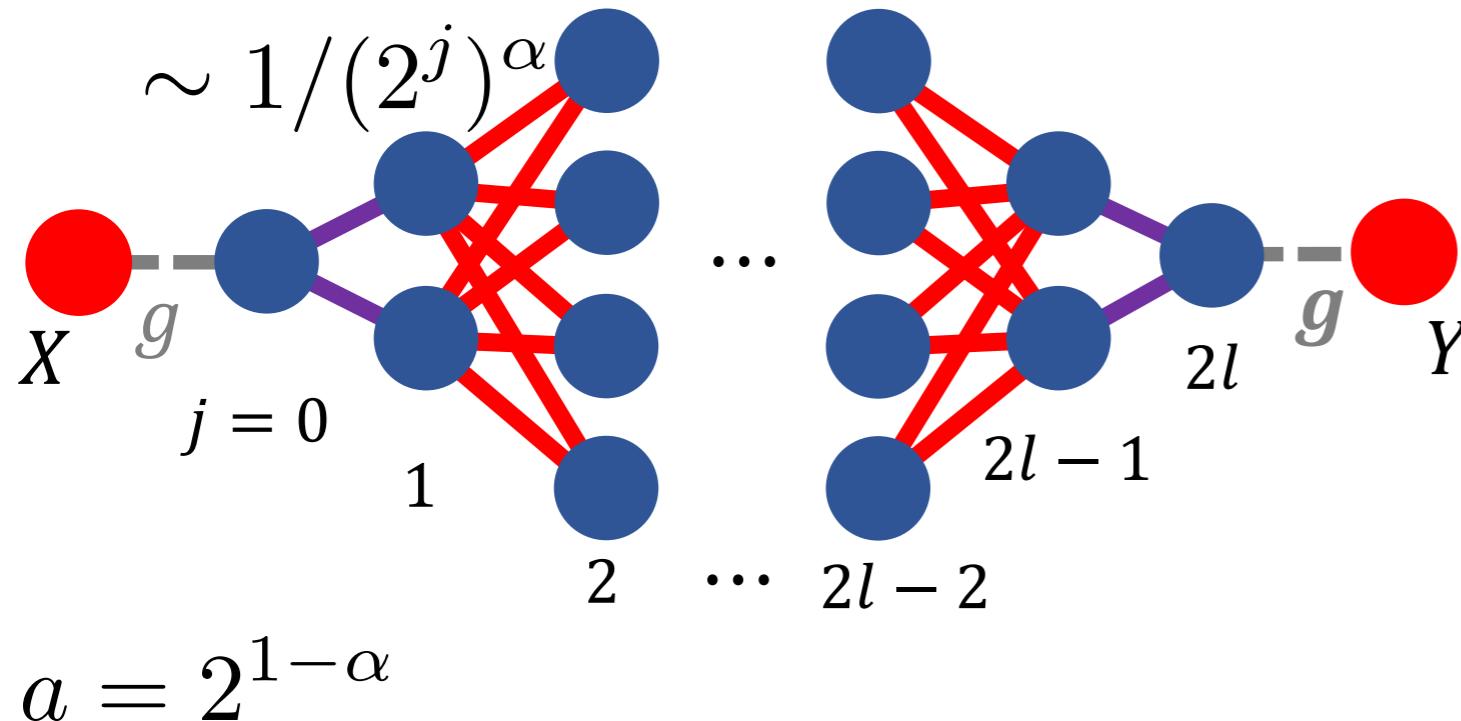
Staticize the protocol for  $d/2 < \alpha < d + 1$



- couple X and Y weakly to the rest of the chain
  - as before,  $2^j$  sites in block j, but halfway through the chain start reducing the block size
  - turn on all interactions (left half of chain: at same strength  $\sim 1/(2^j)^\alpha$ ) between neighboring blocks j and j+1

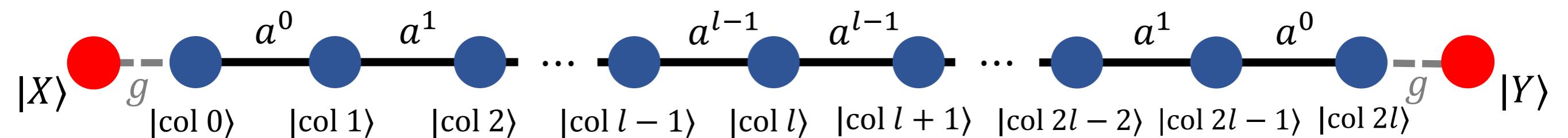


# Staticize the protocol for $d/2 < \alpha < d + 1$



$$|\text{col } j\rangle \sim \frac{1}{\sqrt{2^j}} \sum_{i \in \text{col } j} |i\rangle$$

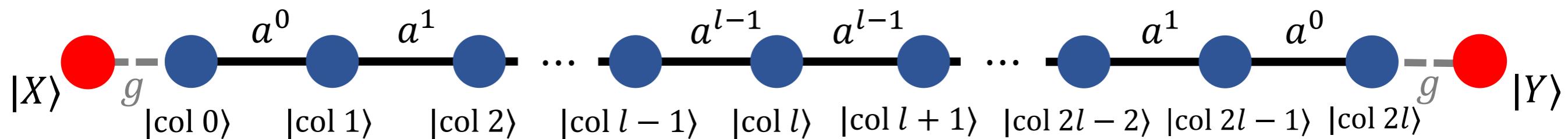
$$|\text{col } j+1\rangle \sim \frac{1}{\sqrt{2^j}} \sum_{i \in \text{col } j+1} |i\rangle$$



- left half: hopping amplitude between  $|\text{col } j\rangle$  and  $|\text{col } j+1\rangle$ :

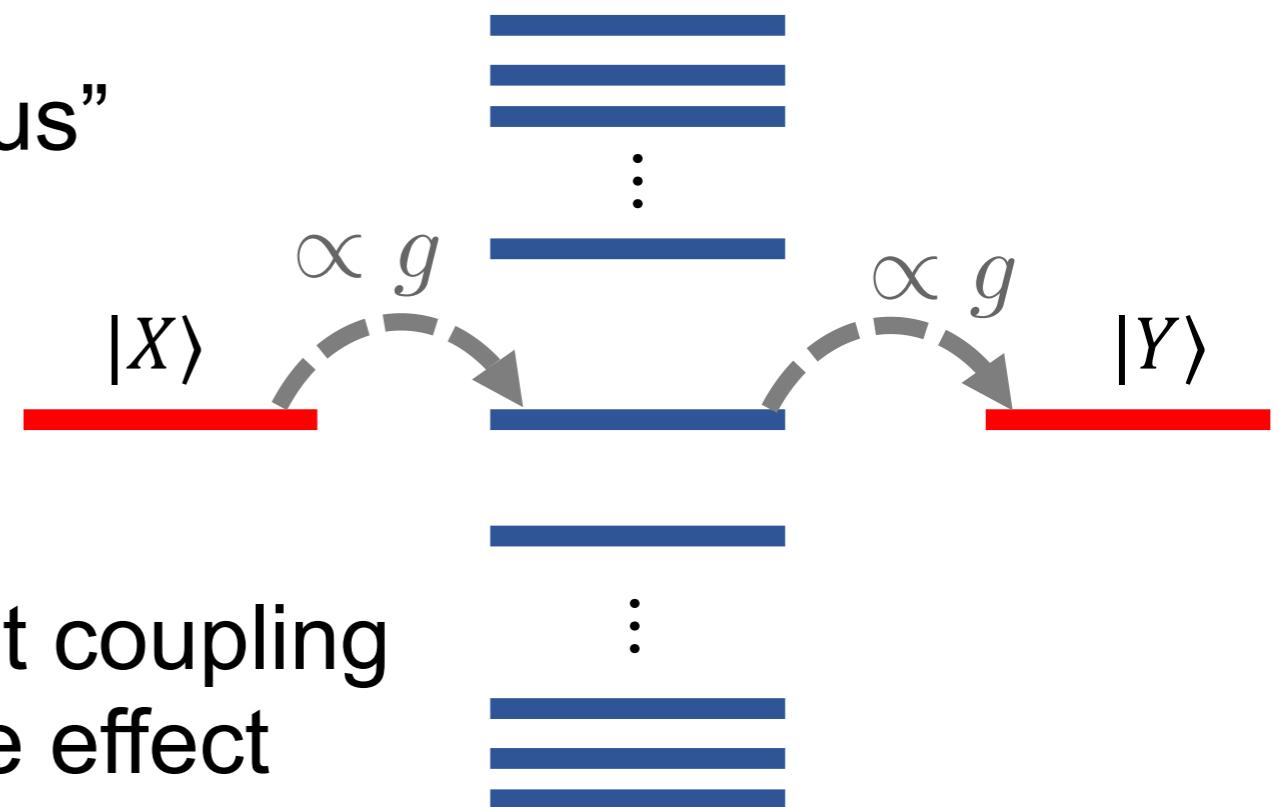
$$\sim \frac{(2^j)^2}{(\sqrt{2^j})^2} \frac{1}{(2^j)^\alpha} \sim \frac{2^j}{(2^j)^\alpha} = (2^{1-\alpha})^j$$

# Staticize the protocol for $d/2 < \alpha < d + 1$



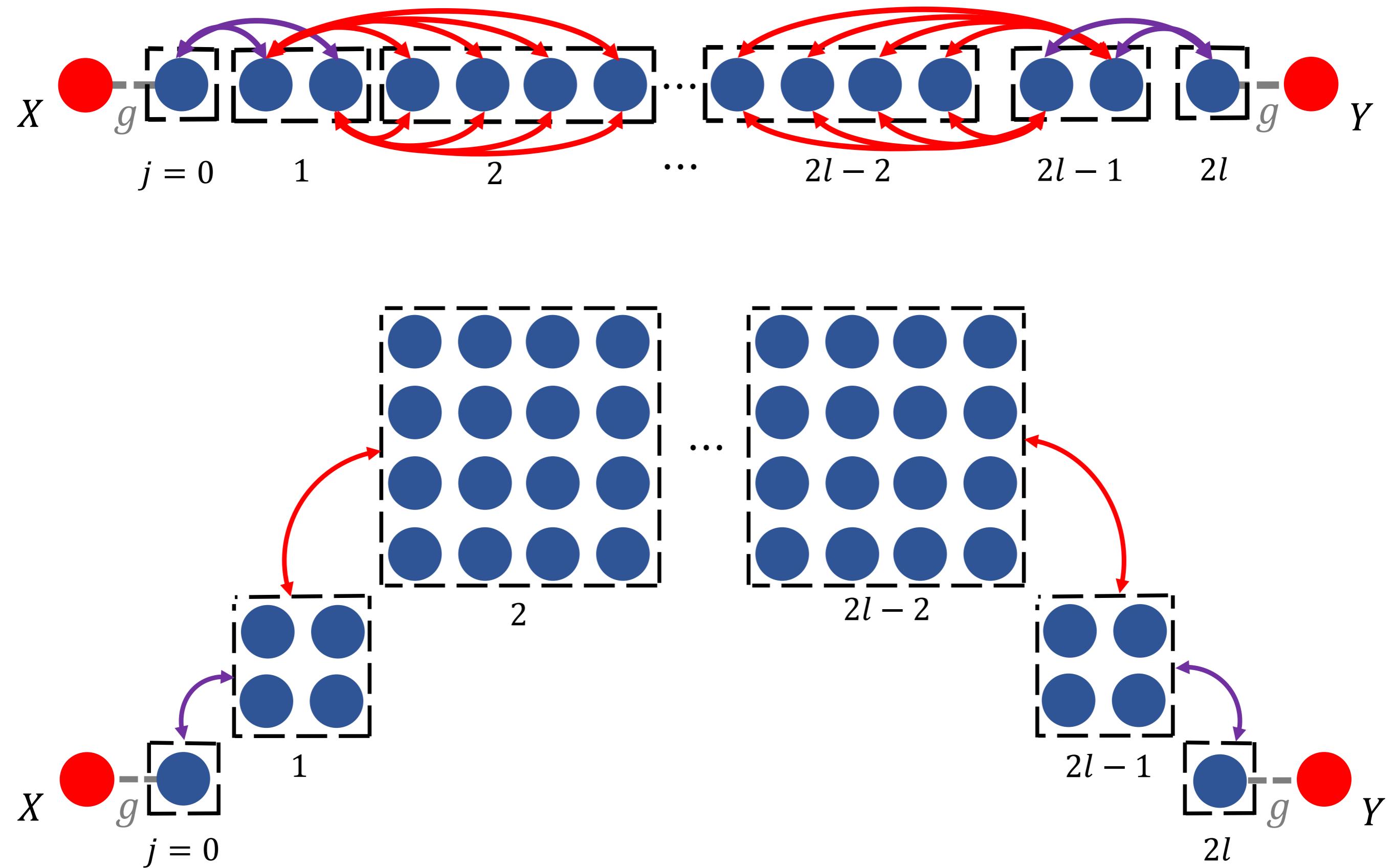
$$a = 2^{1-\alpha}$$

- X and Y coupled weakly to the “bus”
- spectrum of bus is symmetric
- tune X and Y to resonance with the zero-energy eigenstate
- need to make  $g$  small enough that coupling to off-resonant levels has negligible effect
- $\alpha = 1$  particularly easy: uniform hopping
- protocol time agrees with optimal one for all  $d/2 < \alpha < d + 1$



“Tunneling trick”: Li, Shi, Chen, Song, Sun, PRA (2005); Plenio, Semiao, NJP (2005); Wojcik, Łuczak, Kurzynski, Grudka, Gdala, Bednarska, PRA 72, 034303 (2005), etc...

# Staticize the protocol for $d/2 < \alpha < d + 1$



# Summary

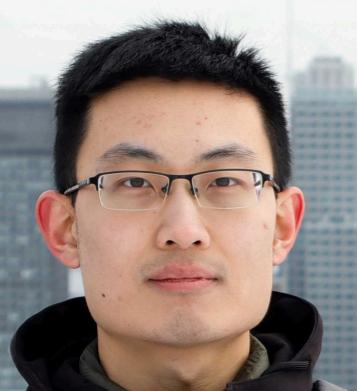
- time-independence does not limit information flow for free-particle Hamiltonians

# Outlook

- in some scenarios (architecture + application), it can be easier to implement Hamiltonians dynamics without time-dependent control
  - slower than interacting protocols but
    - do not depend on whether intermediate sites are occupied
    - utilize W ( $|10\dots0\rangle + |01\dots0\rangle + \dots + |00\dots1\rangle$ ) states instead of GHZ ( $|00\dots0\rangle + |11\dots1\rangle$ ) states
    - W states more robust against errors in Hamiltonian  
Tran et al (Gong, AVG, Lucas), PRX (2020); Hong, Lucas, PRA (2021)
  - we propose another time-independent protocol where hopping strength exactly follows  $J_{ij} = J_0/r_{ij}^\alpha$ :
    - can be naturally realized with synthetic quantum matter
    - suboptimal, but provides speedup over short-range protocols

# Thank You

Time independence does not limit information flow. I. The free-particle case



arXiv:2505.18249

Dong  
Yuan

(Tsinghua)

Chao  
Yin

(Boulder)

Connor  
Mooney

(→Michigan State)

Chris  
Baldwin

(→Michigan State)

Time independence does not limit information flow. II. The case with ancillas



arXiv:2505.18254

Connor  
Mooney

(Tsinghua)

Dong  
Yuan

Adam  
Ehrenberg

(→Michigan State)

Chris  
Baldwin

Andrew  
Childs

# Thank You

Optimal time-dependent protocols:

Free-particle,  $\alpha < d/2$



PRA 102, 010401 (2020)

Andrew  
Guo

(→ Quantinuum) (→ IBM)

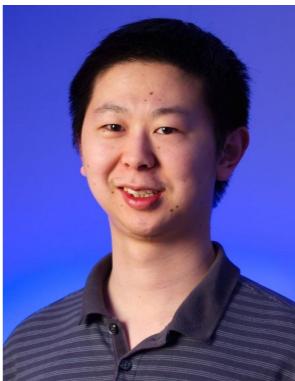
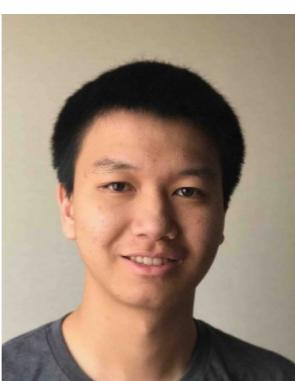
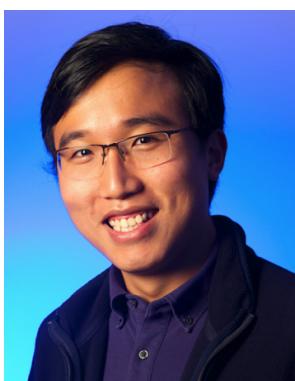
Minh  
Tran

Andrew  
Childs

Zhe-Xuan  
Gong  
(→ Mines)

Free-particle,  $d/2 < \alpha < d + 1$

PRX 10, 031009 (2020)



Minh  
Tran

(→ IBM) (Caltech)

Chi-Fang  
Chen

Adam  
Ehrenberg

Andrew  
Guo

Abhinav  
Deshpande (Boulder)

Yifan Hong

Zhe-Xuan  
Gong

Andy  
Lucas

(→ Quantinuum)(→ IBM) → Maryland)(→ Mines) (Boulder)

# Thank You

Optimal time-dependent protocols:

Interacting,  $\alpha > d$



Minh  
Tran  
(→ IBM)



Abhinav  
Deshpande  
(→ IBM)



Andrew  
Guo  
(→ Quantinuum)



Andy  
Lucas  
(Boulder)

PRX 11, 031016 (2021)

Interacting,  $\alpha < d$     Yin, PRL 134, 130604 (2025).

# Thank You

Quantum routing through bottlenecks



Dhruv  
Devulapalli



Chao  
Yin  
(Boulder) ( $\rightarrow$  Quantinuum)



Andrew  
Guo



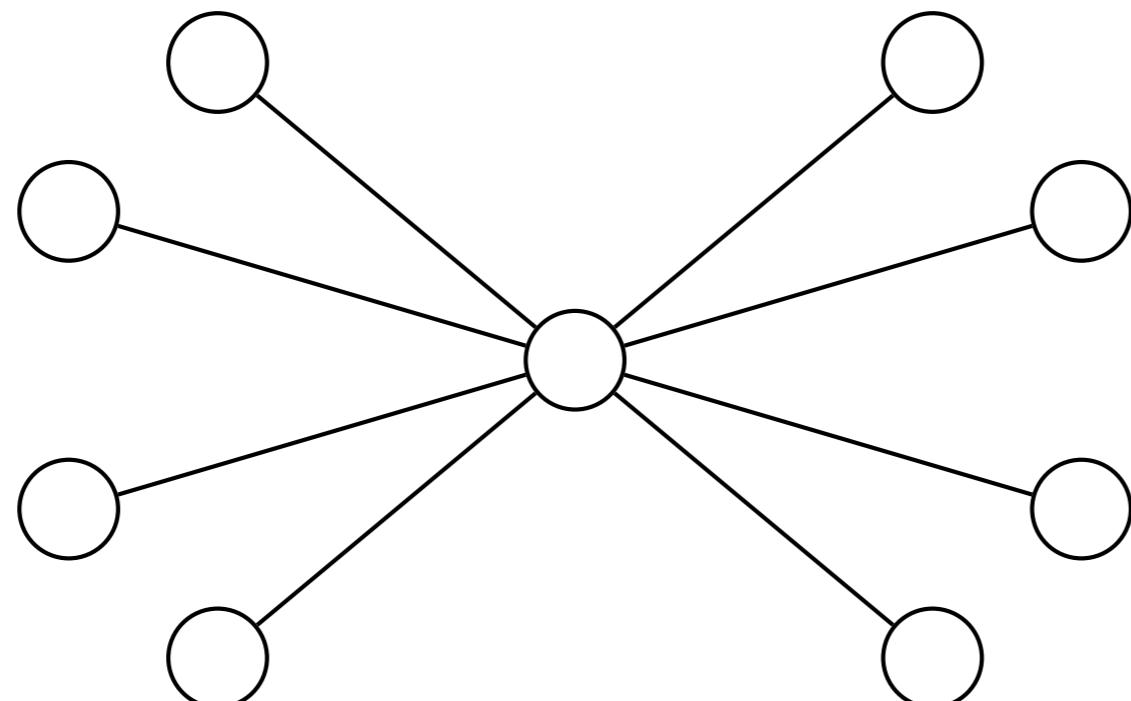
Eddie  
Schoute  
( $\rightarrow$  IBM)



Andrew  
Childs



Andy  
Lucas  
(Boulder)



arXiv:2505.16948

# Thank you



Zachary  
Eldredge  
(→ DoE)



Michael  
Foss-Feig  
(→ Quantinuum)



Jeremy  
Young  
(→ JILA)



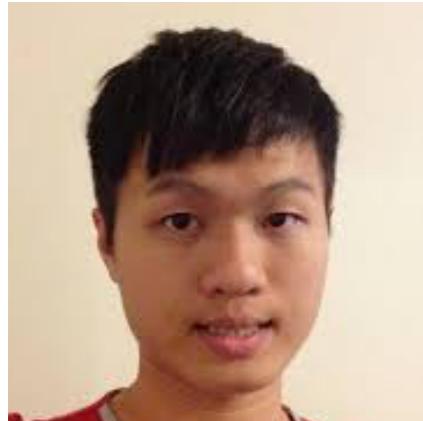
Jim Garrison  
(→ IBM)



Ali Hamed  
Moosavian



Yuan Su  
(→ IBM)



Su-Kuan Chu



Bill  
Fefferman  
(→ Chicago)



Paraj  
Titum (→ APL)



Fernando  
Brandão  
(Caltech)



Dima  
Abanin  
(Geneva)



Spiros  
Michalakis  
(Caltech)



Charles  
Clark



Simon  
Lieu  
(→ AWS)



Nishad  
Maskara  
(Caltech/UMD/  
Harvard)

\$\$\$: DoE, AFOSR, ARO, NSF, DARPA

# Thank you

Our other Lieb-Robinson papers:

PRL 113, 030602 (2014)

PRL 114, 157201 (2015)

PRL 119, 050501 (2017)

PRL 119, 170503 (2017)

PRX 9, 031006 (2019)

PRA 100, 052103 (2019)

PRL 129, 150604 (2022)

PRL 127, 160401(2021)

PRX Quantum 4, 020349 (2023)

arXiv:2110.15368

## Graduate Students

Zachary Eldredge → DoE  
Jeremy Young → JILA (NRC)  
Abhinav Deshpande → Caltech  
Yidan Wang → Harvard  
Minh Tran → MIT  
Ani Bapat → LBNL  
Fangli Liu → QuEra  
Andrew Guo → Sandia  
Ron Belyansky → Chicago  
Pradeep Niroula → J.P. Morgan  
Su-Kuan Chu → JILA  
Jake Bringewatt → Harvard  
Adam Ehrenberg → IDA  
Dhruv Devulapalli  
Sharoon Austin      Jeffery Yu  
Chris Fechisin      Jeet Shah  
Daniel Spencer      Joe Iosue  
Connor Mooney      Nick Li  
Zhenning Liu      Yunfei Wang  
Alexandra Behne      Vinay Kashyap  
Twesh Upadhyaya  
Thomas Steckmann  
Elizabeth Bennewitz  
Erfan Abbasgholinejad

\$\$\$\$: DoE, AFOSR, ARO, NSF, DARPA

# Thank You

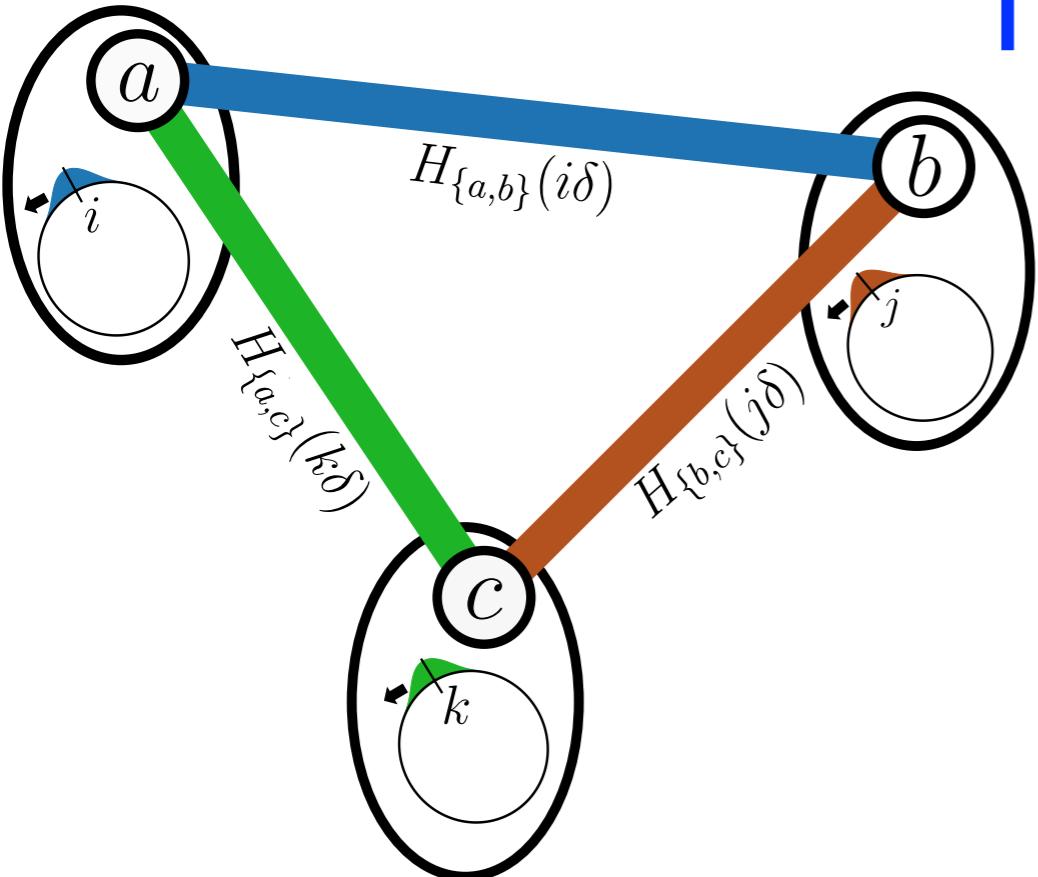
## High School Students, Undergraduate Students, and Visiting Graduate Students

P. Niroula (Harvard→UMD), J. Iosue (MIT→UMD), K. Wang (Stanford→Berkeley), N. Maskara (Caltech→Harvard), M. Kalinowski (Warsaw→Harvard), K. Qian (→MIT), H. Shastri (Reed), S. King (Rochester), N. Dong (Boulder), S. DeCoster (GATech), M. Whittman (Kansas), W. Gong (Tsinghua), T. Qian (→MIT), I. Liang (→Ivy League), A. Gorti (Cornell), T. Goel (MIT), R. Gong (Mount Holyoke), W. Deng (Peking), Jason Youm (Mont. Blair High School), Tianhao Liu (Peking), Dong Yuan (Tsinghua), Evan Zhang (Mont. Blair High School)

## Postdocs

Mohammad Maghrebi → Asst. Prof. @ Michigan State  
Zhe-Xuan Gong → Asst. Prof. @ Colorado School of Mines  
Sergey Syzranov → Asst. Prof. @ UC Santa Cruz  
Paraj Titum → Applied Physics Lab at Johns Hopkins  
Igor Boettcher → Asst. Prof. @ U Alberta  
Rex Lundgren → NSA Laboratory for Physical Sciences  
Zhicheng Yang → Asst. Prof. @ Peking U  
Chris Baldwin → Asst. Prof. @ Michigan State      Ali Fahimniya  
Oles Shtanko → IBM      Alex Cojocaru → Asst. Prof. @ Edinburgh      Alex Schuckert  
James Garrison → IBM      Seth Whitsitt → Northrop Grumman      Jacob Lin  
Przemek Bienias → AWS      Kishor Bharti → IHPC, Singapore      Sean Muleady  
Lucas Brady → NASA QuAIL      Luispe García-Pintos → Los Alamos      Yuxin Wang  
Yaroslav Kharkov → AWS      Ella Crane → MIT      Yan-Qi Wang  
Kunal Sharma → IBM      Brayden Ware → IBM      Yifan Hong  
Simon Lieu → AWS      Dominik Hangleiter → Berkeley      Anthony Brady  
Emil Khabiboulline      Lorcan Conlon      35

# Thank You



Mooney, Yuan, Ehrenberg, Baldwin,  
AVG, Childs, arXiv:2505.18254

Yuan, Yin, Mooney, Baldwin,  
Childs, AVG, arXiv:2505.18249

