



Hard Condensed Matter



NORDITA

The Nordic Institute for Theoretical Physics



Theoretical Quantum Matter

Partick Wong

Gabriel Cardoso

Dirac Materials
Dark Matter
Detection



Alexander
Balatsky



Quantum Printing
Amorphous oxides for Qubits
Inverse design through AI

H. Yerzhakov

Tien-Tien Yeh



Light –
Superconductors
interaction



A. Tyner



Avinash Pathapati

Material Informatics
Machine Learning Two-Level

Organic Materials
Database (OMDB)

Dynamical Order
Odd-frequency
superconductivity

[Homepage](#): for more info



Ivan
Khaymovich

NORDITA Ass. Prof.
in TQM group

Ergodicity breaking phases States



ergodic metal

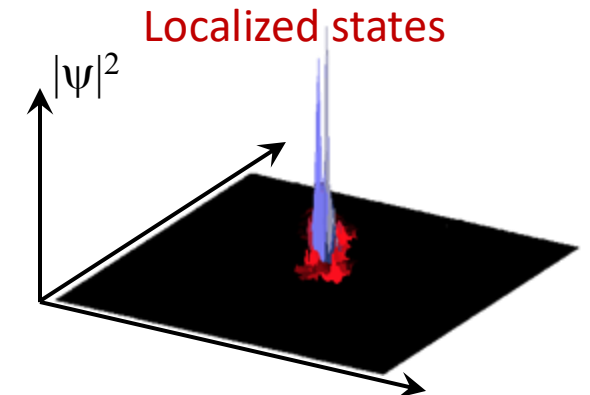
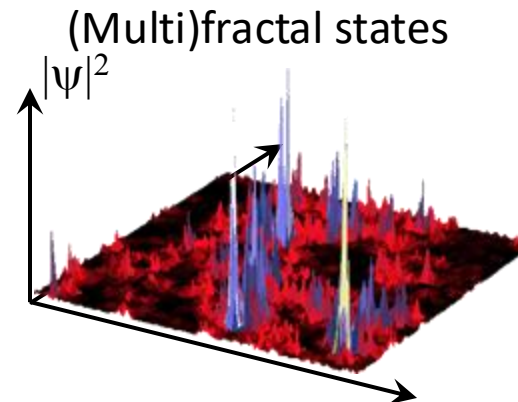
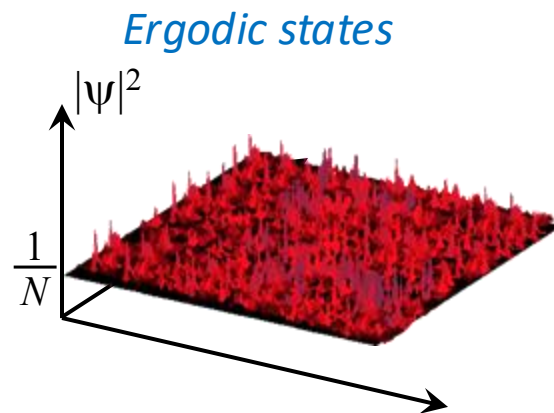


non-ergodic phase



insulator

disorder





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Ivan Khaymovich

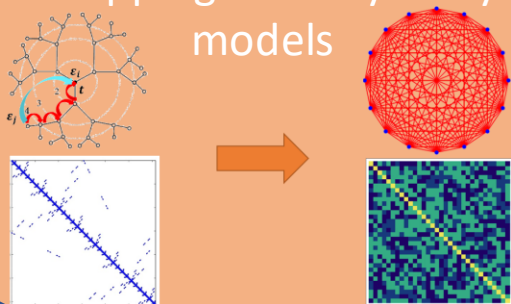
Ergodicity breaking phases



SCAN ME

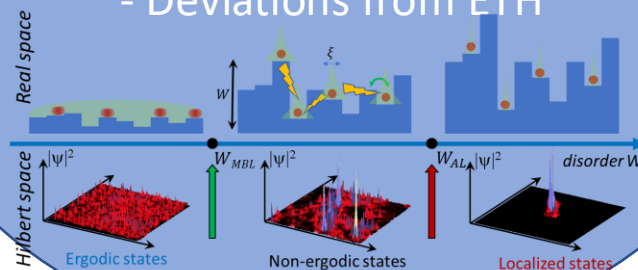
Random-matrix theory:

- Multifractal phases
- Mapping to many-body models



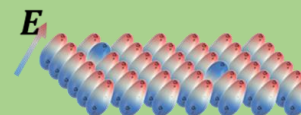
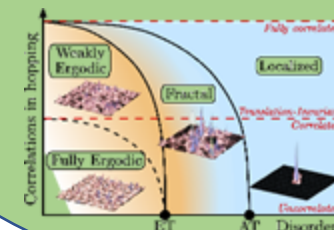
Many-body systems:

- Many-body localization vs Hilbert-space multifractality,
- Multifractality/entanglement
- Deviations from ETH

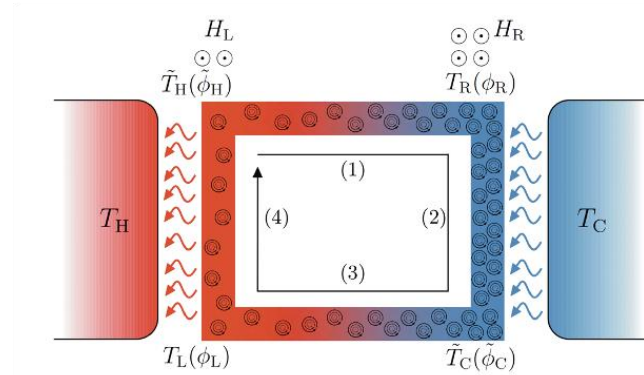


Long-range systems:

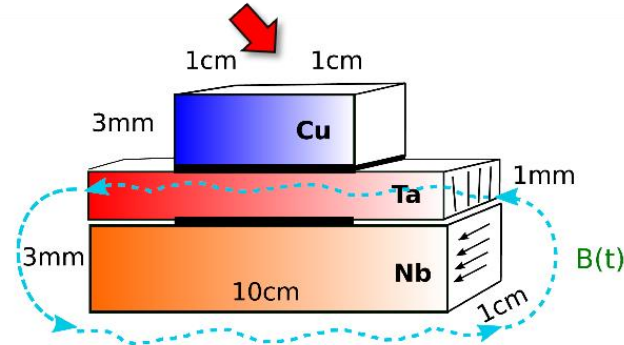
- Integrability, correlations,
- non-Hermitian/open models
- Localization and multifractality



Principles of solid-state quantum refrigeration and thermodynamic control in the nanoscale

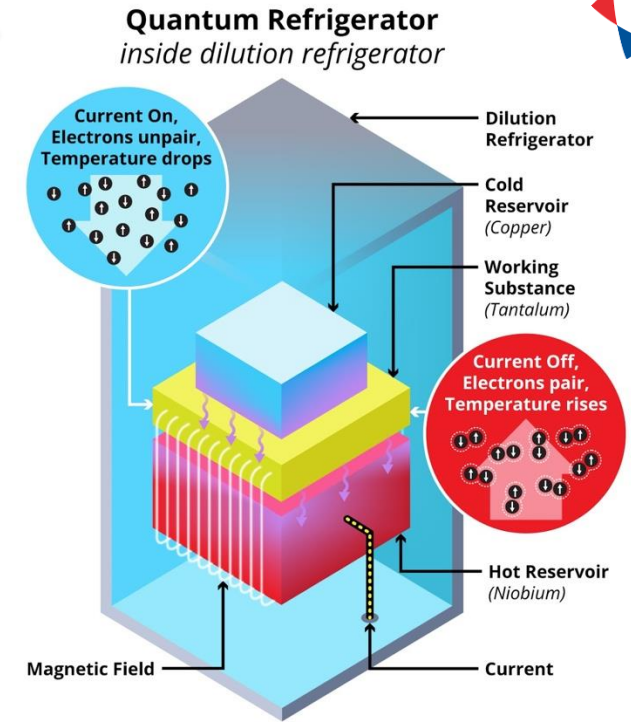


"The qubit goes here"



Fluxons in type II superconductors can act as puddles carrying heat in circulation.

Adiabatic magnetization of type I superconductor for cooling below 10mK



(University of Rochester illustrations / Michael Osadciw)



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Quantum Structure of Gravitational Radiation
Quasi-normal modes from nonlinear
Gravitational Effects



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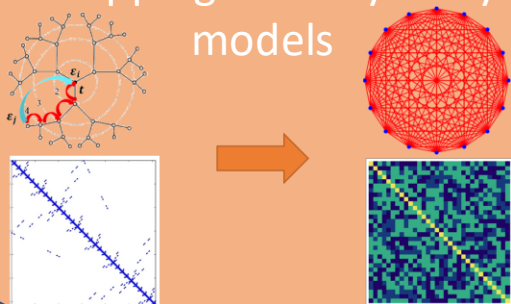
Ergodicity breaking phases



SCAN ME

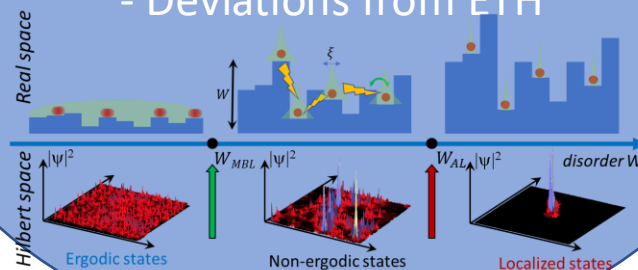
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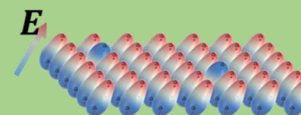
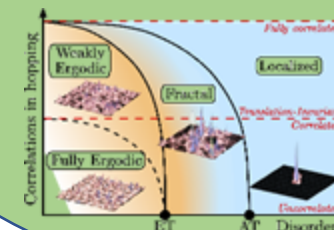
Many-body systems:

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- Deviations from ETH



Long-range systems:

- Integrability, correlations,
- non-Hermitian/open models
- Localization and multifractality



Mikael Fogelström



E-mail: mikael.fogelstrom@su.se

MSc projects:

Superconducting hybrid structures

Nanowires, Josephson junctions, microwave resonators
— key building blocks of next generation quantum devices —

1. What may You do

1. **Model proximity-induced superconductivity** in low-dimensional devices
2. Analyse **microwave/THz response** and kinetic inductance
3. Study **Andreev bound states** and Josephson physics
4. Work with **high-performance numerical codes** (Fortran, Python, etc.)

2. What You Will Learn

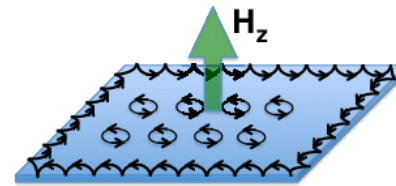
1. Quasiclassical Green-function methods
2. Superconducting transport and device physics
3. Numerical simulation & data analysis
4. Research-level scientific workflows

Topological Insulators Revolution

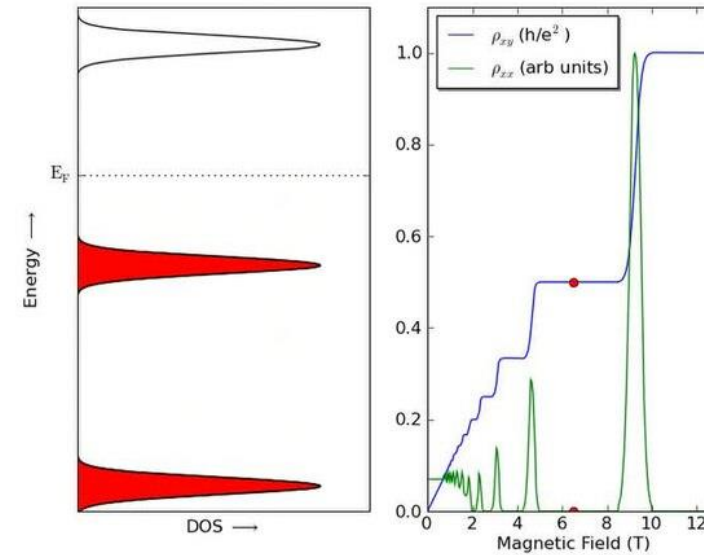
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Quantum Hall Effect
(Klaus von Klitzing., 1980)

External Magnetic Field



(b) Quantum Hall effect



Topological Insulators Revolution

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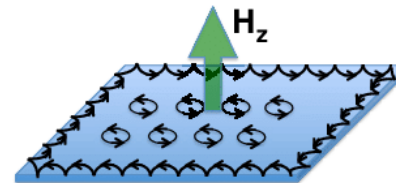
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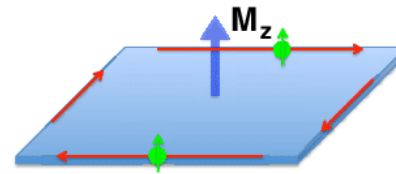


Anomalous QHE
Haldane (1988)

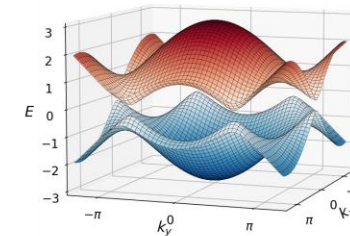
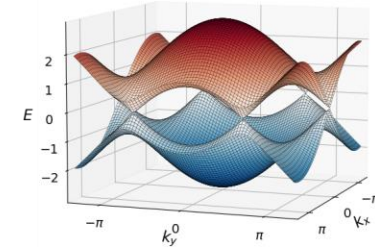
Intrinsic Magnetization



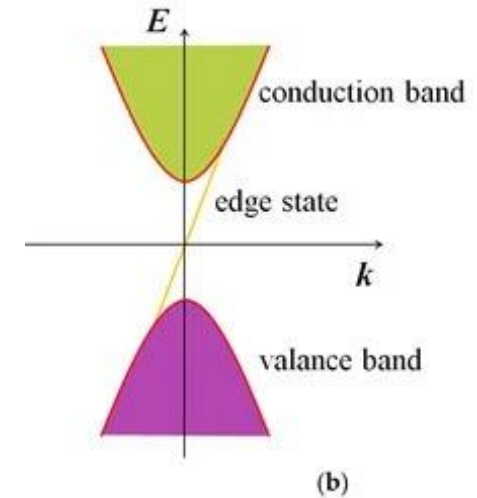
(b) Quantum Hall effect



(d) Quantum Anomalous Hall effect



Graphene



Topological Insulators Revolution

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Quantum Hall Effect
(Klaus von Klitzing., 1980)

External Magnetic Field



Anomalous QHE
Haldane (1988)

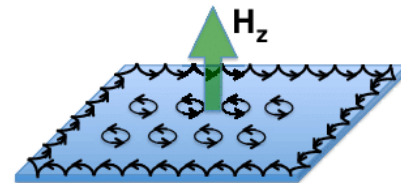
Intrinsic Magnetization



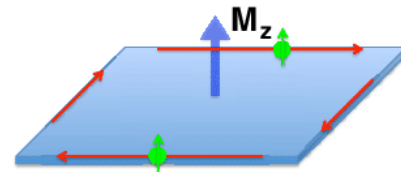
Quantum Spin Hall Effect
Kane & Mele (2005)

protected by

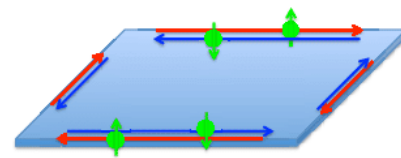
Fermionic
Time Reversal Symmetry



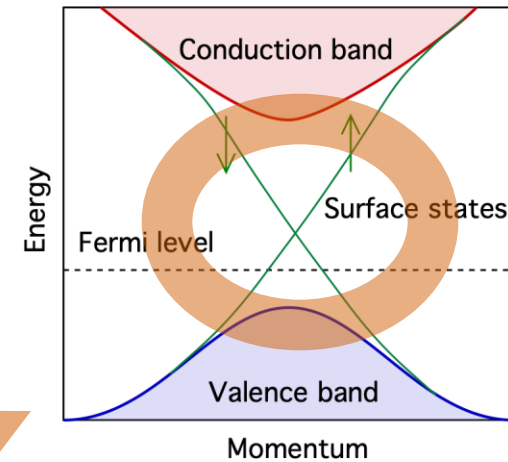
(b) Quantum Hall effect



(d) Quantum Anomalous Hall effect



(f) Quantum Spin Hall effect



Topological Insulators Revolution

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Quantum Hall Effect
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External Magnetic Field



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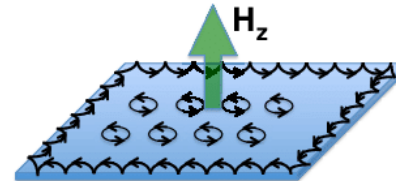
Intrinsic Magnetization



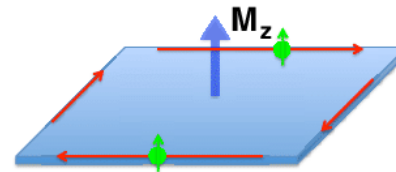
Quantum Spin Hall Effect
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protected by

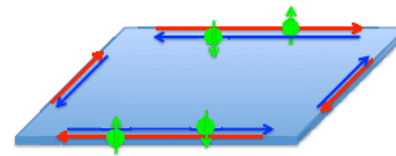
Fermionic
Time Reversal Symmetry



(b) Quantum Hall effect



(d) Quantum Anomalous Hall effect



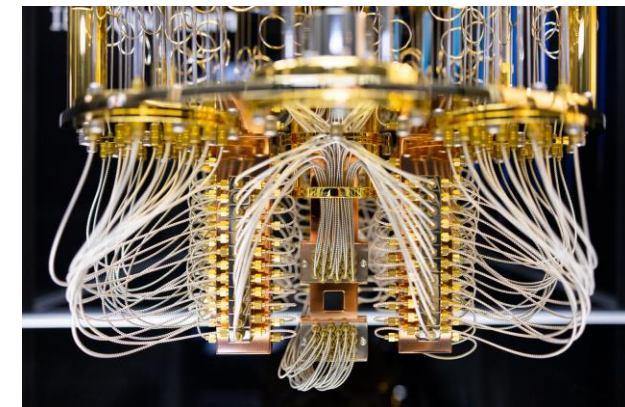
(f) Quantum Spin Hall effect

Robust quantum surface states

Substrate for QBits of Quantum Computers

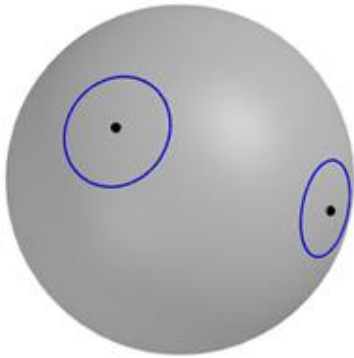
Important Investments

Race for the Quantum Supremacy
States (USA, Chine, Emirates, etc.) and
companies (Google, etc.)

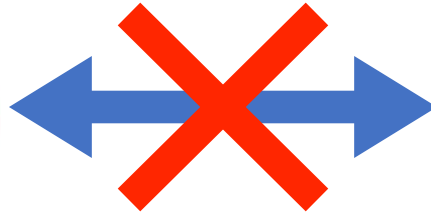


Topological?

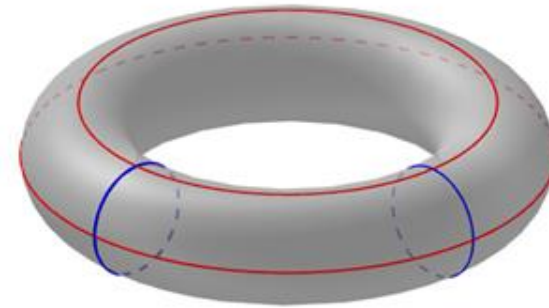
Topology: classification of manifolds with respect to their global features



$g = 0$

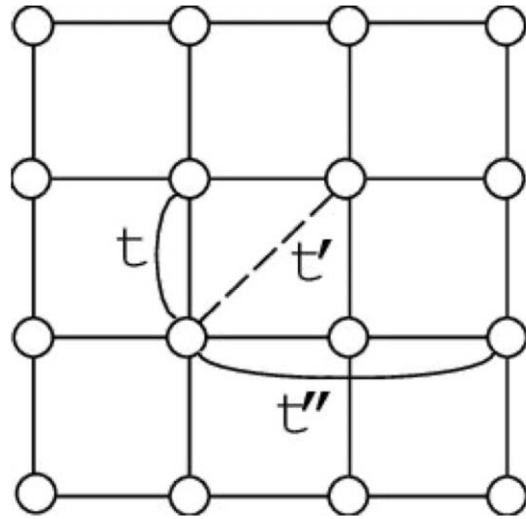


Exemple of topological invariant:
the genus g

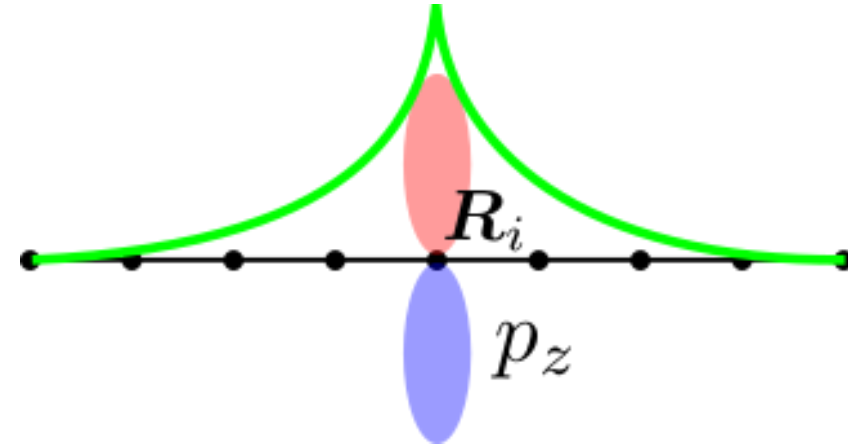


$g = 1$

Quantum Materials Modeling

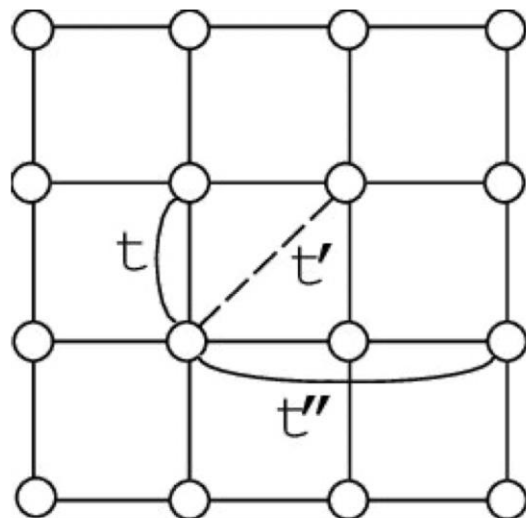


Localized Wannier functions



$$t_{\alpha\sigma,\beta\sigma'}(\mathbf{R}_i - \mathbf{R}_j) = \int d\mathbf{x} w_{\alpha\sigma}(\mathbf{x} - \mathbf{R}_i - \mathbf{r}_\alpha)^* \overset{\text{Kohn-Sham Hamiltonian}}{\mathfrak{h}(\mathbf{x})} w_{\beta\sigma'}(\mathbf{x} - \mathbf{R}_j - \mathbf{r}_\beta)$$

Quantum Materials Modeling



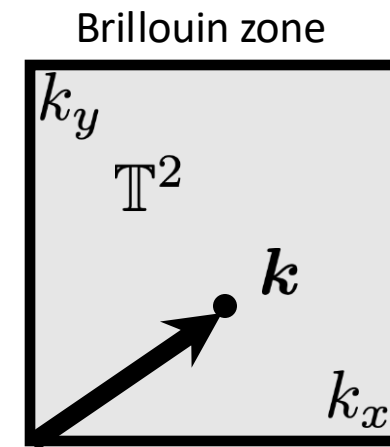
$$H(\mathbf{k}) \in \mathbb{C}^N \times \mathbb{C}^N$$

N degrees of freedom per unit cell:
Wyckoff positions, sub-lattice sites,
electronic orbitals, spins

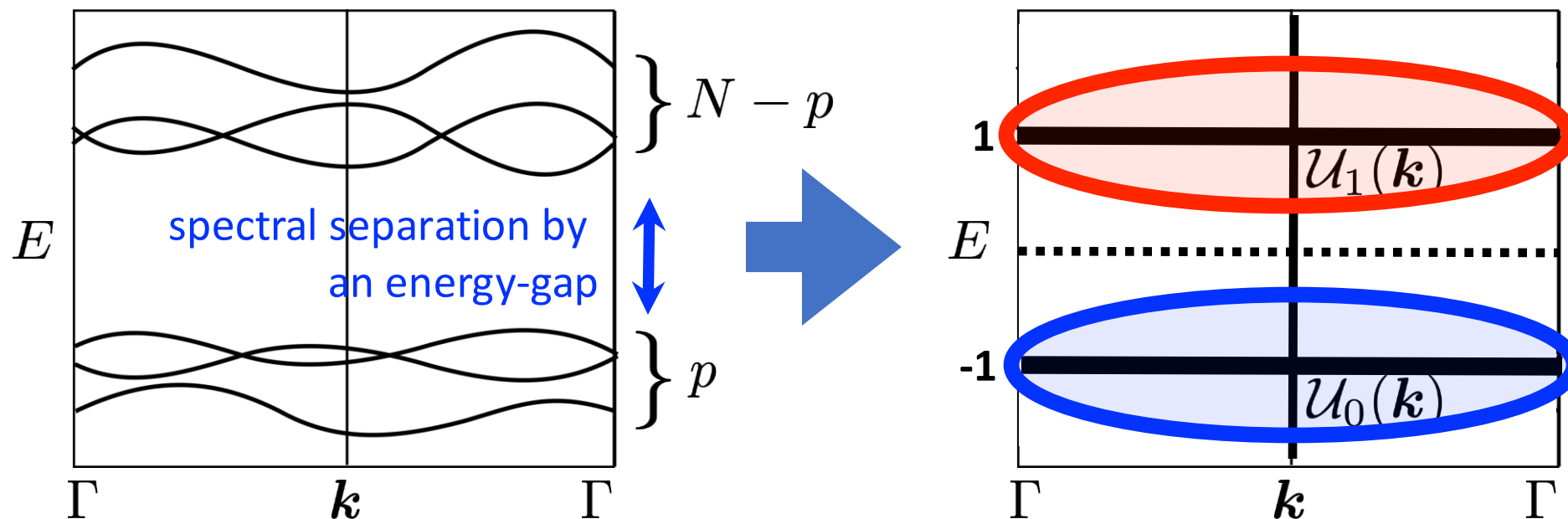
Bloch picture:

$$H_{\alpha\sigma,\beta\sigma'}(\mathbf{k}) = \sum_j e^{i\mathbf{k} \cdot (\mathbf{R}_j + \mathbf{r}_\beta - \mathbf{0} - \mathbf{r}_\alpha)} t_{\alpha\sigma,\beta\sigma'}(\mathbf{0} - \mathbf{R}_j)$$

Localized Wannier $\rightarrow$ Finite Fourier series (analytical)



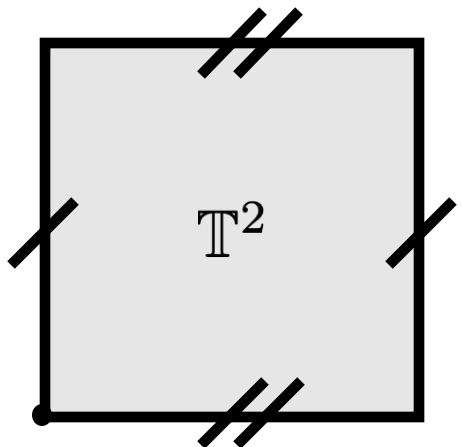
Space of gapped Hamiltonian



Grassmannian
(gauge structure)

$$\text{Gr}_{p,N}^{\mathbb{C}} \cong \text{U}(N) / [\text{U}(p) \times \text{U}(N - p)]$$

Homotopy classification of gapped Hamiltonian


$$\xrightarrow{H(\mathbf{k})} \mathrm{Gr}_{p,N}^{\mathbb{C}} \cong \mathrm{U}(N) / [\mathrm{U}(p) \times \mathrm{U}(N-p)]$$

(Bott periodicity)

$$\begin{aligned} [\mathbb{T}^2, \mathrm{Gr}_{p,N}^{\mathbb{C}}] &\cong \pi_2 \left(\mathrm{Gr}_{p,N}^{\mathbb{C}} \right) \xrightarrow{\quad} \pi_1 (\mathrm{U}(p)) \\ &= \pi_1 (\mathrm{SU}(p) \times \mathrm{U}(1)) \\ &= \pi_1 (\mathrm{SU}(p)) \times \pi_1 (\mathrm{U}(1)) \\ &= \pi_1 (\mathrm{U}(1)) = \mathbb{Z} \end{aligned}$$

(Chern number)

Chern number as the chirality of a Weyl node

Flow of Berry phase = Chern number

$$\Delta\gamma_B = \gamma_B[\text{NP}] - \gamma_B[\text{SP}] = 2\pi c_1[\mathcal{S}]$$

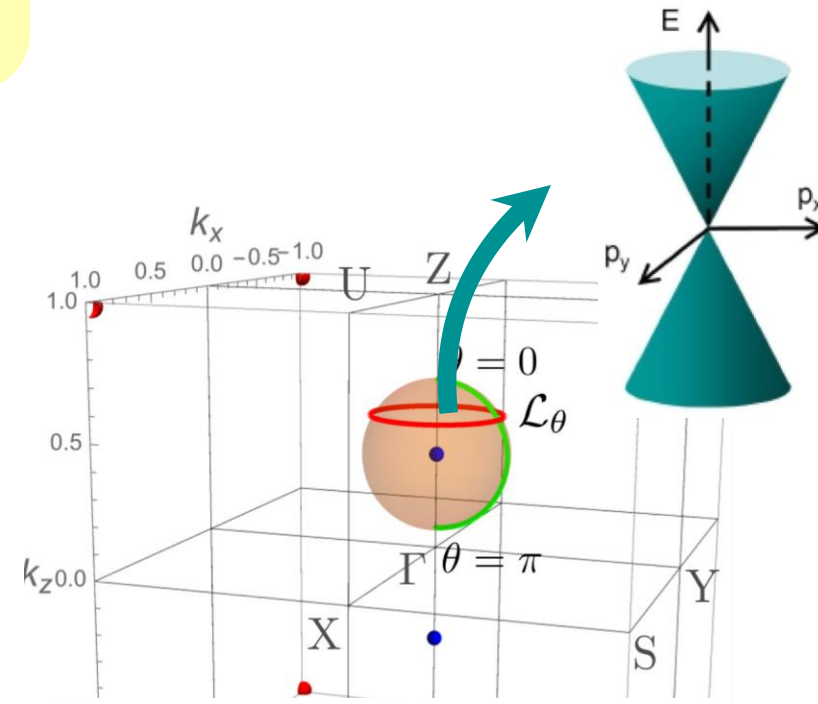
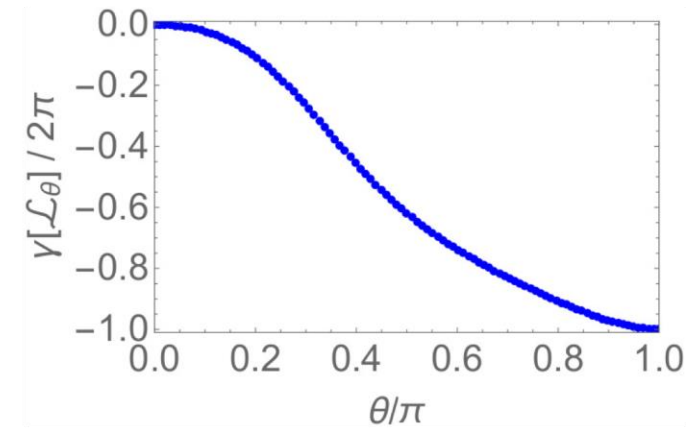
Loop integral over the occupied band subspace:

→ Wilson loop

$$\mathcal{W}[l_\theta] = \exp \left\{ \oint_{l_\theta} \mathcal{A}(\mathbf{k}) \cdot d\mathbf{l} \right\} \in U(p)$$

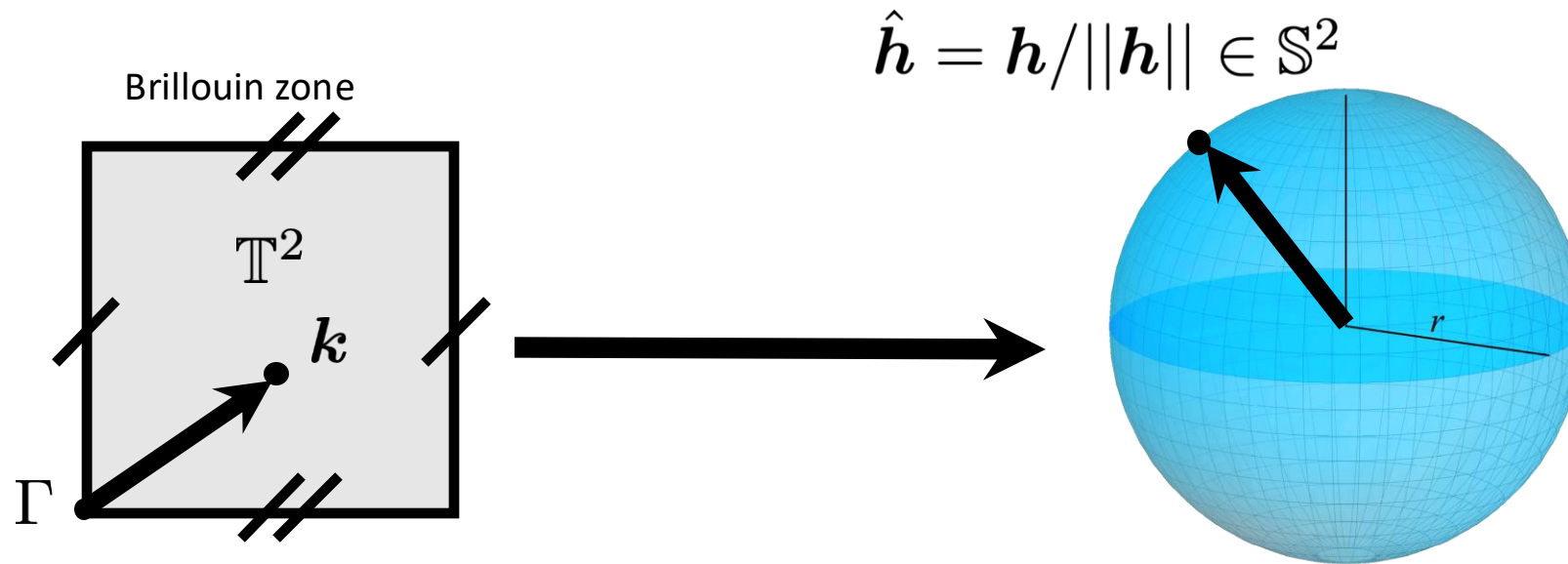
→ Berry phase

$$e^{i\gamma_B[l_\theta]} = \det \mathcal{W}[l_\theta] \in U(1)$$



A.J. Stone, Proc. R. Soc. Lond. A **351**, 141 (1976)

Gapped graphene: Chern insulator



Chern number: (Skyrmion number)

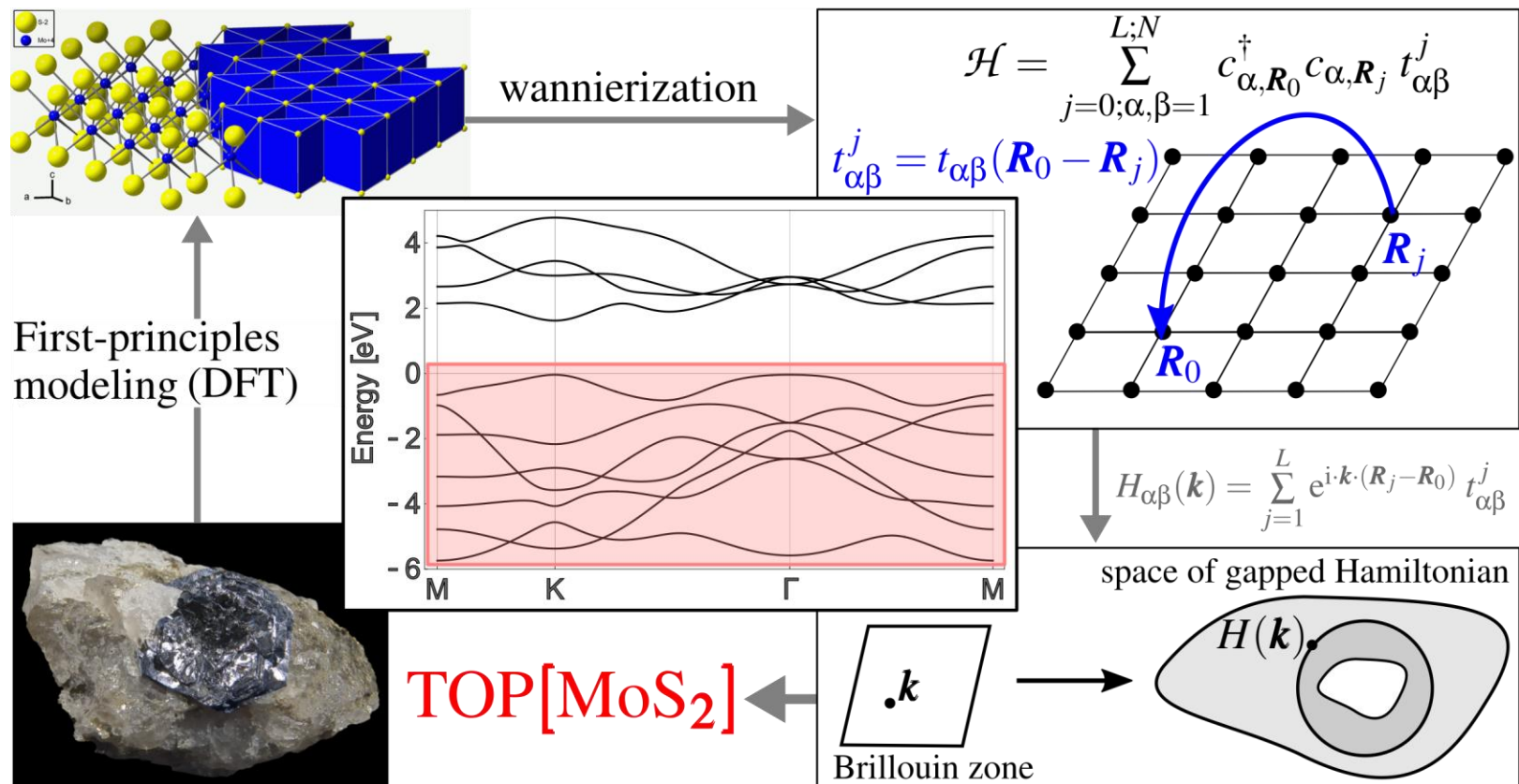
$$c_1 = \frac{1}{4\pi} \int_{\mathbb{T}^2} \hat{\mathbf{h}} \cdot \partial_{k_x} \hat{\mathbf{h}} \times \partial_{k_y} \hat{\mathbf{h}} dk_x dk_y \in \mathbb{Z}$$

Zoo of Topological Insulators

AZ	s\d	0	1	2	3	4	5	6	7
A	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0
AIII	1	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0	$\mathbb{Z}$
AI	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$	0	$\mathbb{Z}_2$	$\mathbb{Z}_2$
BDI	1	$\mathbb{Z}_2$	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$	0	$\mathbb{Z}_2$
D	2	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$	0
DIII	3	0	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$
AII	4	$\mathbb{Z}$	0	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	0	0	0
CII	5	0	$\mathbb{Z}$	0	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	0	0
C	6	0	0	$\mathbb{Z}$	0	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	0
CI	7	0	0	0	$\mathbb{Z}$	0	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$

2D Chern insulator

Topological Inverse Problem





NORDITA

Nordic Institute for
Theoretical Physics

Optimized Topological Quantum Systems

Exotic topology and geometry of crystalline systems

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December 2025



Marie Curie
Fellowship



Swedish
Research Council